



MATHS

BOOKS - CENGAGE PUBLICATION

PROBABILITY I

Illustration

1. A coin is tossed three times, consider the following events. A : No head appears, B: Exactly one head appears and C: Atleast two appear. Do they form a set of mutually exclusive and exhaustive events?

 [Watch Video Solution](#)

2. Find the probability of getting more than 7 when two dice are rolled.

 [Watch Video Solution](#)

3. A die is loaded so that the probability of a face i is proportional to i , $i = 1, 2, \dots, 6$. Then find the probability of an even number occurring when the die is rolled.



[Watch Video Solution](#)

4. Consider the experiment of tossing a coin. If the coin shows head, toss it again but if it shows tail then throw a die. Find the conditional probability of the event that the die shows a number greater than 4 given that there is at least one tail



[Watch Video Solution](#)

5. Four candidates A, B, C, D have applied for the assignment of coach a school cricket team. If A is twice as likely to be selected as B, and B and C are given about the same chance of being selected, while C is twice as

likely to be selected as D, what are the probability that (i) C will be selected ? (ii) A will not be selected?

 [Watch Video Solution](#)

6. If $\frac{1+3p}{3}$, $\frac{1-p}{1}$, $\frac{1-2p}{2}$ are the probabilities of 3 mutually exclusive events then find the set of all values of p.

 [Watch Video Solution](#)

7. A determinant is chosen at random from the set of all determinant of order 2 with elements 0 or 1 only. Find the probability that the determinant chosen is nonzero.

 [Watch Video Solution](#)

8. A die is rolled 4 times. The probability of getting a larger number than the previous number each time is $\frac{17}{216}$ b. $\frac{5}{432}$ c. $\frac{15}{432}$ d. none of

these



[Watch Video Solution](#)

9. If a coin is tossed n times, then find the probability that the head appears odd number of times.



[Watch Video Solution](#)

10. A card is drawn at random from a well-shuffled pack of 52 cards. Find the probability that it is neither a king nor a heart.



[Watch Video Solution](#)

11. A card is drawn from an ordinary pack of 52 cards and a gambler bets that, it is a spade or an ace. What are the odds against his winning this bet?



[Watch Video Solution](#)

12. A fair dice is thrown three times. If p , q and r are the numbers obtained on the dice, then find the probability that $i^p + i^q + i^r = 1$, where $I = \sqrt{-1}$.

 [Watch Video Solution](#)

13. A mapping is selected at random from the set of all the mappings of the set $A = \{1, 2, \dots, n\}$ into itself. Find the probability that the mapping selected is an injection.

 [Watch Video Solution](#)

14. Two integers x and y are chosen with replacement out of the set $\{0, 1, 2, 3, \dots, 10\}$. Then find the probability that $|x - y| > 5$.

 [Watch Video Solution](#)

15. Find the probability that the 3Ns come consecutively in the arrangement of the letters of the word CONSTANTINOPLE.

 [Watch Video Solution](#)

16. Out of $3n$ consecutive integers, three are selected at random. Find the probability that their sum is divisible by 3.

 [Watch Video Solution](#)

17. Find the probability that a randomly chosen three-digit number has exactly three factors.

 [Watch Video Solution](#)

18. If p and q are chosen randomly from the set $\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ with replacement, determine the probability that the roots of the equation $x^2 + px + q = 0$ are real.



[Watch Video Solution](#)

19. An integer is chosen at random and squared. Find the probability that the last digit of the square is 1 or 5.



[Watch Video Solution](#)

20. Four fair dices are thrown simultaneously. Find the probability that the highest number obtained is 4.



[Watch Video Solution](#)

21. An unbiased dice, with faces numbered 1,2,3,4,5,6, is thrown n times and the list of n numbers shown up is noted. Then find the probability that among the numbers 1,2,3,4,5,6 only three numbers appear in this list.



[Watch Video Solution](#)

22. Six points are there on a circle from which two triangles drawn with no vertex common. Find the probability that none of the sides of the triangles intersect.



[Watch Video Solution](#)

23. Balls are drawn one-by-one without replacement from a box containing 2 black, 4 white and 3 red balls till all the balls are drawn. Find the probability that the balls drawn are in the order 2 black, 4 white and 3 red.



[Watch Video Solution](#)

24. In how many ways three girls and nine boys can be seated in two vans, each having numbered seats, 3 in the front and 4 at the back? How many seating arrangements are possible if 3 girls sit together in a back row on adjacent seats? Now, if all the seating arrangements are equally likely,

what is the probability of 3 girls sitting together in a back row on adjacent seats?

 [Watch Video Solution](#)

25. Find the probability that the birth days of six different persons will fall in exactly two calendar months.

 [Watch Video Solution](#)

26. If 10 objects are distributed at random among 10 persons, then find the probability that at least one of them will not get anything.

 [Watch Video Solution](#)

27. 2^n players of equal strength are playing a knock out tournament. If they are paired at randomly in all rounds, find out the probability that

out of two particular players S_1 and S_2 , exactly one will reach in semi-final ($n \in N, n \geq 2$).



[Watch Video Solution](#)

28. Fourteen numbered balls (i.e. 1, 2, 3, ..., 14) are divided in three groups randomly. Find the probability that the sum of numbers on a balls, in each group, is odd.



[Watch Video Solution](#)

29. Five different digits from the set of numbers $\{1, 2, 3, 4, 5, 6, 7\}$ are written in random order. Find the probability that five-digit number thus formed is divisible by 9.



[Watch Video Solution](#)

30. Three married couples sit in a row. Find the probability that no husband sits with his wife.



[Watch Video Solution](#)

31. A box contains 6 nails and 10 nuts. Half of the nails and half of the nuts are rusted. If one item is chosen at random, then find the probability that it is rusted or is a nail.



[Watch Video Solution](#)

32. The probability that at least one of the events A and B occurs is 0.6. If A and B occur simultaneously with probability 0.2, then find $P(A) + P(B)$.



[Watch Video Solution](#)

33. If $P(A \cup B) = 3/4$ and $P(\bar{A}) = 2/3$, then find the value of $P(\bar{A} \cap B)$.

 [Watch Video Solution](#)

34. Let A, B, C be three events. If the probability of occurring exactly one event out of A and B is $1 - x$, out of B and C is $1 - 2x$, out of C and A is $1 - x$, and that of occurring three events simultaneously is x^2 , then prove that the probability that atleast one out of A, B, C will occur is greater than $1/2$.

 [Watch Video Solution](#)

35. Let A and B be any two events such that $P(A) = \frac{1}{2}$ and $P(B) = \frac{1}{3}$. Then find the value of $P(A' \cap B')' + P(A' \cup B')'$.

 [Watch Video Solution](#)

36. If A and B are events such that $P(A' \cup B') = \frac{3}{4}$, $P(A' \cap B') = \frac{1}{4}$ and $P(A) = \frac{1}{3}$, then find the value of $P(A' \cap B)$

 [Watch Video Solution](#)

37. A sample space consists of 9 elementary outcomes E_1, E_2, \dots, E_9 whose probabilities are:

E_1, E_2, \dots, E_9 whose probabilities are:

$$P(E_1) = P(E_2) = 0.09, P(E_3) = P(E_4) = P(E_5) = 0.1, P(E_6) = P(E_7)$$

If $A = \{E_1, E_5, E_8\}$, $B = \{E_2, E_5, E_8, E_9\}$ then

(a) Calculate $P(A)$, $P(B)$, and $P(A \cap B)$.

(b) Using the addition law of probability, calculate $P(A \cup B)$.

(c) List the composition of the event $A \cup B$, and calculate $P(A \cup B)$ by adding the probabilities of the elementary outcomes.

(d) Calculate $P(\overline{B})$ from $P(B)$, also calculate $P(\overline{B})$ directly from the elementary outcomes of B .

 [Watch Video Solution](#)

38. The following Venn diagram shows three events, A, B, and C, and also the probabilities of the various intersections.

Determine

(a) $P(A)$

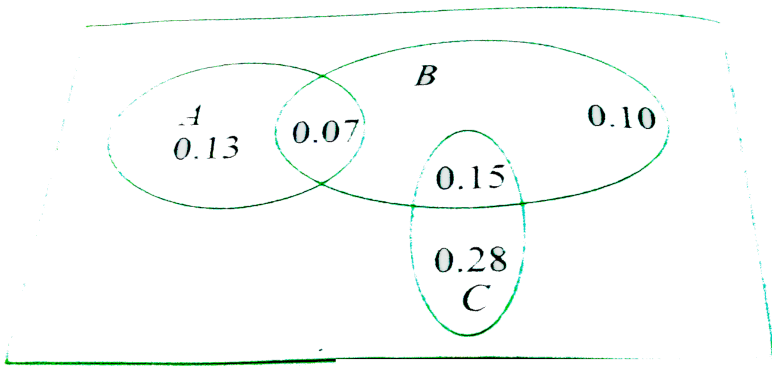
(b) $P(B \cap \bar{C})$

(c) $P(A \cup B)$

(d) $P(A \cap \bar{B})$

(e) $P(B \cap C)$

(f) Probability of the event that exactly one of A, B, and C occurs.



Watch Video Solution

39. Three numbers are chosen at random without replacement from $\{1,2,3,\dots,10\}$. The probability that the minimum of the chosen number is 3 or their maximum is 7, is:



Watch Video Solution

40. If A and B are two events such that $P(A) = \frac{1}{2}$ and $P(B) = \frac{2}{3}$, then show that

$$(a) P(A \cup B) \geq \frac{2}{3} \quad (b) \frac{1}{6} \leq P(A \cap B) \leq \frac{1}{2}$$

$$(c) P(A \cap \bar{B}) \leq \frac{1}{3} \quad (d) \frac{1}{6} \leq P(\bar{A} \cap B) \leq \frac{1}{2}$$



Watch Video Solution

41. Given two events A and B . If odds against A are as 2:1 and those in favour of $A \cup B$ are 3:1, then find the range of $P(B)$.



Watch Video Solution

42. The probabilities of three events A , B , and C are $P(A) = 0.6$, $P(B) = 0.4$, and $P(C) = 0.5$. If $P(A \cup B) = 0.8$, $P(A \cap C) = 0.3$, $P(A \cap B \cap C) = 0.2$, and $P(A \cup B \cup C) \geq 0.85$, then find the range of $P(B \cap C)$.



[Watch Video Solution](#)

43. Two dice are thrown. What is the probability that the sum of the numbers appearing on the two dice is 11, if 6 appears on the first?



[Watch Video Solution](#)

44. If $P(A) = 0.8$, and $P(B | A) = 0.4$, find $P(A \cap B)$



[Watch Video Solution](#)

45. If two events A and B are such that $P(A^c) = 0.3$, $P(B) = 0.4$, and $P(A \cap B^c) = 0.5$, then find the value

of $P[B / (A \cup B^c)]$.



[Watch Video Solution](#)

46. A coin is tossed three times, where

(i) A : head on third toss, B: heads on first two tosses

find $P(A/B)$.



[Watch Video Solution](#)

47. A die is thrown three times and the sum of the 3 numbers shown is 15.

The probability that the first throw was a four, is



[Watch Video Solution](#)

48. Assume that each child born is equally likely to be a boy or a girl. If a family has two children, what is the conditional probability that both are girls given that the youngest is a girl ?



[Watch Video Solution](#)

49. एक सिक्के को उछालने के परीक्षण पर विचार कीजिए। यदि सिक्के पर चित प्रकट हो तो सिक्के का पुनः उछालें परंतु यदि सिक्के पर पट प्रकट हो तो एक पासे को फेंकें। यदि घटना कम से कम एक पट प्रकट होना का घटित होना दिया गया है तो घटना पासे पर 4 से बड़ी संख्या प्रकट होना की सप्रतिबंध प्रायिकता ज्ञात कीजिए।



[View Text Solution](#)

50. A box contains 10 mangoes out of which 4 are rotten. Two mangoes are taken out together. If one of them is found to be good, then find the probability that the other is also good.



[Watch Video Solution](#)

51. An urn contains 10 black and 5 white balls. Two balls are drawn from the urn one after the other without replacement. What is the probability that both balls are black?



[Watch Video Solution](#)

52. Three cards are drawn successively, without replacement from a pack of 52 well shuffled cards. What is the probability that first, second and third cards are jack, queen and king, respectively ?



[Watch Video Solution](#)

53. One of the ten available keys opens the door. If we try the keys one after another, then find the following

- (i) the probability that the door is opened in the first attempt.
- (ii) the probability that the door is opened in the second attempt.
- (iii) the probability that the door is opened in the third attempt.
- (iv) the probability that the door is opened in the tenth attempt.



[Watch Video Solution](#)

54. A bag contains W white and 3 black balls. Balls are drawn one by one without replacement till all the black balls are drawn. Then find the probability that this procedure for drawing the balls will come to an end at the r th draw.

 [Watch Video Solution](#)

55. A fair coin is tossed repeatedly. If tail appears on first four tosses, then find the probability of head appearing on fifth toss.

 [Watch Video Solution](#)

56. If $P\left(\frac{B}{A}\right) = P\left(\frac{B}{A'}\right)$, then prove that A and B are independent.

 [Watch Video Solution](#)

57. A die marked 1, 2, 3 in red and 4, 5, 6 in green is tossed. Let A be the event, the number is even, and B be the event, the number is red. Are A and B independent?



[Watch Video Solution](#)

58. Three persons work independently on a problem. If the respective probabilities that they will solve it are $\frac{1}{3}$, $\frac{1}{4}$ and $\frac{1}{5}$, then find the probability that not can solve it.



[Watch Video Solution](#)

59. The probability of hitting a target by three marksmen are $\frac{1}{2}$, $\frac{1}{3}$ and $\frac{1}{4}$. Then find the probability that no one will hit the target when they fire simultaneously.



[Watch Video Solution](#)

60. An electrical system has open-closed switches S_1 , S_2 and S_3 as shown in fig. The switches operate independently of one another and the current will flow from $A \rightarrow B$ either if S_1 is closed or if both S_2 and S_3 are closed. If $P(S_1) = P(S_2) = P(S_3) = 1/2$, then find the probability that the circuit will work.

 [Watch Video Solution](#)

61. Differentiate with respect to x , $y = \sin(\log x)$

 [Watch Video Solution](#)

62. If four whole numbers taken at random are multiplied together, then find the probability that the last digit in the product is 1,3,7, or 9.

 [Watch Video Solution](#)

63. If A and B are two independent events, the probability that both A and B occur is $\frac{1}{8}$ and the probability that neither of them occurs is $\frac{3}{8}$. Find the probability of the occurrence of A.



[Watch Video Solution](#)

64. The unbiased dice is tossed until a number greater than 4 appears. What is the probability that an even number of tosses is needed?



[Watch Video Solution](#)

65. A pair of unbiased dice are rolled together till a sum of either 5 or 7 is obtained. Then find the probability that 5 comes before 7.



[Watch Video Solution](#)

66. An unbiased normal coin is tossed n times. Let E_1 : event that both heads and tails are present n tosses. E_2 : event that the coin shows up heads at most once. The value of n for which E_1 and E_2 are independent is _____.

 [Watch Video Solution](#)

67. X speaks truth in 60% and Y in 50% of the cases. Find the probability that they contradict each other narrating the same incident.

 [Watch Video Solution](#)

68. A person has undertaken a construction job. The probabilities are 0.80 that there will be a strike, 0.70 that the construction job will be completed on time if there is no strike, and 0.4 that the construction job will be completed on time if there is a strike. Determine the probability that the construction job will be completed on time.

 [Watch Video Solution](#)

69. A bag contains $n + 1$ coins. It is known that one of these coins shows heads on both sides, whereas the other coins are fair. One coin is selected at random and tossed. If the probability that the toss results in heads is $\frac{7}{12}$, then find the value of n .

[Watch Video Solution](#)

70. Factorise the following: $9x^2y^2 - 16$

[Watch Video Solution](#)

71. Urn A contains 6 red and 4 black balls and urn B contains 4 red and 6 black balls. One ball is drawn at random from urn A and placed in urn B. Then, one ball is drawn at random from urn B and placed in urn A. If one ball is drawn at random from urn A, then find the probability that it is found to be red.

[Watch Video Solution](#)

72. An urn contains 6 white and 4 black balls. A fair die whose faces are numbered from 1 to 6 is rolled and number of balls equal to that of the number appearing on the die is drawn from the urn at random. Find the probability that the balls selected are white.

[Watch Video Solution](#)

73. Suppose families always have one, two, or three children, with probabilities $\frac{1}{4}$, $\frac{1}{2}$, and $\frac{1}{4}$, respectively. Assume everyone eventually gets married and has children, then find the probability of a couple having exactly four grandchildren.

[Watch Video Solution](#)

74. On a normal standard die one of the 21 dots from any one of the six faces is removed at random with each dot equally likely to be chosen. If

the die is then rolled, then find the probability that the odd number appears.

 [Watch Video Solution](#)

75. about to only mathematics

 [Watch Video Solution](#)

76. An insurance company insured 2000 scooter drivers, 4000 car drivers and 6000 truck drivers. The probability of an accidents are 0.01, 0.03 and 0.15 respectively. One of the insured persons meets with an accident. What is the probability that he i

 [Watch Video Solution](#)

77. A laboratory blood test is 99% effective in detecting a certain disease when it is in fact, present. However, the test also yields a false positive

result for 0.5% of the healthy person tested (i.e. if a healthy person is tested, then, with probability 0.005, the test will imply he has the disease). If 0.1 percent of the population actually has the disease, what is the probability that a person has the disease given that his test result is positive ?

 [Watch Video Solution](#)

78. In an entrance test, there are multiple choice questions. There are four possible answers to each question, of which one is correct. The probability that a student knows the answer to a question is 90%. If the gets the correct answer to a question, then find the probability that he was guessing.

 [Watch Video Solution](#)

79. Each of the n urns contains 4 white and 6 black balls. The $(n + 1)$ th urn contains 5 white and 5 black balls. One of the $n + 1$ urns is chosen at

random and two balls turn out to be black. If the probability that the $(n + 1)$ th urn was chosen to draw the balls is $1/16$, then find the value of n .

 [Watch Video Solution](#)

80. Die A has 4 red and 2 white faces, whereas die B has 2 red and 4 white faces. A coin is flipped once. If it shows a head, the game continues by throwing die A: if it shows tail, then die B is to be used. If the probability that die A is used is $32/33$ when it is given that red turns up every time in first n throws, then find the value of n .

 [Watch Video Solution](#)

81. A bag contains n balls out of which some balls are white. If the probability that a bag contains exactly i white balls is proportional to i^3 . A ball is drawn at random from the bag and found to be white, then find the probability that the bag contains exactly 2 white balls.

 [Watch Video Solution](#)

82. A die is thrown 7 times. What is the chance that an odd number turns up exactly 4 times



[Watch Video Solution](#)

83. Suppose that 90% of people are right-handed. What is the probability that at most 6 of a random sample of 10 people are right-handed?



[Watch Video Solution](#)

84. An experiment succeeds twice as often as it fails. Find the probability that in the next five trials, there will be atleast 3 successes.



[Watch Video Solution](#)

85. What is the probability of guessing correctly at least 8 out of 10 answer on true-false examination?



[Watch Video Solution](#)

86. A rifleman is firing at a distance target and hence has only 10% chance of hitting it. Find the number of rounds; he must fire in order to have more than 50% chance of hitting it at least once.



[Watch Video Solution](#)

87. A and B play a series of games which cannot be drawn and p, q are their respective chance of winning a single game. What is the chance that A wins m games before B wins n games?



[Watch Video Solution](#)

Solved Example

1. When a fair dice is rolled, the number that comes up top is a number between one to six. Assuming we roll the dice once, to check the possibility of three coming up.

 [Watch Video Solution](#)

2. The sum of two positive quantities is equal to $2n$. the probability that their product is not less than $\frac{3}{4}$ times their greatest product is $\frac{3}{4}$ b. $\frac{1}{4}$ c. $\frac{1}{2}$ d. none of these

 [Watch Video Solution](#)

3. There are two bags each containing 10 books all having different titles but of the same size. A student draws out books from the first bag as well as from the second bag. Find the probability that the difference between the books drawn from the two bags does not exceed 2.

 [Watch Video Solution](#)

4. Two natural numbers x and y are chosen at random. What is the probability that $x^2 + y^2$ is divisible by 5?

 [Watch Video Solution](#)

5. If a fair coin is tossed thrice find the probability that there are at most one tail

 [Watch Video Solution](#)

6. Let $P(x)$ denote the probability of the occurrence of event x . Plot all those point $(x, y) = (P(A), P(B))$ in a plane which satisfies the conditions, $P(A \cup B) \geq 3/4$ and $1/8 \leq P(A \cap B) \leq 3/8$

 [Watch Video Solution](#)

7. In a certain city, only 2 newspapers A and B are published. It is known that 25% of the city population read A and 20% read B while 8% reads both A and B . It is also known that 30% of those who read A but not B look into advertisement and 40% of those who read B but not A look into advertisements while 50% of those who read both A and B look into advertisements. What is the percentage of the population who read an advertisement?

 [Watch Video Solution](#)

8. A box contains two 50 paise coins, five 25 paise coins and a certain fixed number N (≥ 2) of 10 and 5-paise coins. Five coins are taken out of the box at random. Find the probability that the total value of these 5 coins is less than 1 rupee and 50 paise.

 [Watch Video Solution](#)

9. Eight players $P_1, P_2, P_3, \dots, P_8$, play a knock out tournament. It is known that whenever the players P_i and P_j , play, the player P_i will win if $i < j$. Assuming that the players are paired at random in each round, what is the probability that the players P_4 , reaches the final ?

 [Watch Video Solution](#)

Exercise 9.1

1. Which of the following cannot be valid assignment of probabilities for outcomes of sample space $S = \{W_1, W_2, W_3, W_4, W_5, W_6, W_7\}$

Assignment	W_1	W_2	W_3	W_4	W_5	W_6	W_7
(a)	0.1	0.01	0.05	0.03	0.01	0.2	0.6
(b)	$\frac{1}{7}$	$\frac{1}{7}$	$\frac{1}{7}$	$\frac{1}{7}$	$\frac{1}{7}$	$\frac{1}{7}$	$\frac{1}{7}$
(c)	0.1	0.2	0.3	0.4	0.5	0.6	0.7
(d)	-0.1	0.2	0.3	0.4	-0.2	0.1	0.3
(e)	$\frac{1}{14}$	$\frac{2}{14}$	$\frac{3}{14}$	$\frac{4}{14}$	$\frac{5}{14}$	$\frac{6}{14}$	$\frac{15}{14}$

 [Watch Video Solution](#)

2. Consider the following assignments of probabilities for outcomes of sample space $S = \{1, 2, 3, 4, 5, 6, 7, 8\}$.

Number (X)	1	2	3	4	5	6	7	8
Probability, $P(X)$	0.15	0.23	0.12	0.10	0.20	0.08	0.07	0.05

Find the probability that

X is a prime number

(b) X is a number greater than 4.



[Watch Video Solution](#)

3. Find the probability that a leap year will have 53 Friday or 53 Saturdays.



[Watch Video Solution](#)

4. A die is loaded so that the probability of a face i is proportional to i , $i = 1, 2, \dots, 6$. Then find the probability of an even number occurring when the die is rolled.



 [Watch Video Solution](#)

5. Statement 1: The probability of drawing either an ace or a king from a pack of card in a single draw is $\frac{2}{13}$. Statement 2: for two events A and B which are not mutually exclusive, $P(A \cup B) = P(A) + P(B) - P(A \cap B)$.

 [Watch Video Solution](#)

6. Three faces of a fair dice are yellow, two are red and one is blue. Find the probability that the dice shows (a) yellow, (b) red and (c) blue face.

 [Watch Video Solution](#)

Exercise 9.2

1. If two fair dices are thrown and digits on dices are a and b , then find the probability for which $\omega^{ab} = 1$, (where ω is a cube root of unity).



[Watch Video Solution](#)

2. There are n letters and n addressed envelopes. Find the probability that all the letters are not kept in the right envelope.



[Watch Video Solution](#)

3. Find the probability of getting total of 5 or 6 in a single throw of two dice.



[Watch Video Solution](#)

4. Two integers are chosen at random and multiplied. Find the probability that the product is an even integer.



[Watch Video Solution](#)

5. If out of 20 consecutive whole numbers two are chosen at random, then find the probability that their sum is odd.

 [Watch Video Solution](#)

6. A bag contains 3 red, 7 white, and 4 black balls. If three balls are drawn from the bag, then find the probability that all of them are of the same color.

 [Watch Video Solution](#)

7. An ordinary cube has 4 blank faces, one face mark 2 and another marked 3, then what is the probability of obtaining 12 in 5 throws?

 [Watch Video Solution](#)

8. If the letters of the word REGULATIONS be arranged at random, find the probability that there will be exactly four letters between the R and the E .



[Watch Video Solution](#)

9. A five digit number is formed but the digits 1,2,3,4,5 without repetition. Find the probability that the number is divisible by 4.



[Watch Video Solution](#)

10. Five persons entered the lift cabin on the ground floor of an 8-floor house. Suppose each of them can leave the cabin independently at any floor beginning with the first. The probability of all five persons leaving at different floors, is



[Watch Video Solution](#)

11. Two friends A and B have equal number of daughters. There are three cinema tickets which are to be distributed among the daughters of A and B . The probability that all the tickets go to the daughters of A is $1/20$. Find the number of daughters each of them have.



[Watch Video Solution](#)

12. about to only mathematics



[View Text Solution](#)

13. There are eight girls among whom two are sisters, all of them are to sit on a round table. Find the probability that the two sisters do not sit together.



[Watch Video Solution](#)

14. A bag contains 50 tickets numbered 1, 2, 3, ..., 50 of which five are drawn at random and arranged in ascending order of magnitude ($x_1 < x_2 < x_3 < x_4 < x_5$) find the probability that $x_3 = 30$.



[Watch Video Solution](#)

15. A pack of 52 cards is divided at random into two equal parts. Find the probability that both parts will have an equal number of black and red cards.



[Watch Video Solution](#)

16. If a digit is chosen at random from the digits 1, 2, 3, 4, 5, 6, 7, 8, 9, then the probability that the digit is even, is

(a) $\frac{4}{9}$

(b) $\frac{5}{9}$

(c) $\frac{1}{9}$

(d) $\frac{2}{3}$



[Watch Video Solution](#)

17. If two distinct numbers m and n are chosen at random from the set $\{1, 2, 3, \dots, 100\}$, then find the probability that $2^m + 2^n + 1$ is divisible by 3.



[Watch Video Solution](#)

18. Two number a and b are chosen at random from the set of first 30 natural numbers. Find the probability that $a^2 - b^2$ is divisible by 3.



[Watch Video Solution](#)

19. Twelve balls are distributed among three boxes, find the probability that the first box will contains three balls.



[Watch Video Solution](#)

1. A and B are two candidates seeking admission in IIT. The probability that A is selected is 0.5 and the probability that A and B are selected is at most 0.3. Is it possible that the probability of B getting selected is 0.9?

 [Watch Video Solution](#)

2. If A and B are events such that $P(A' \cup B') = \frac{3}{4}$, $P(A' \cap B') = \frac{1}{4}$ and $P(A) = \frac{1}{3}$, then find the value of $P(A' \cap B)$

 [Watch Video Solution](#)

3. If $P(A \cap B) = \frac{1}{2}$, $P(A \cup B) = \frac{1}{3}$, $P(A) = p$, $P(B) = 2p$, then find the value of p .

 [Watch Video Solution](#)

4. In a class of 125 students 70 passed in Mathematics, 55 in statistics, and 30 in both. Then find the probability that a student selected at random from the class has passed in only one subject.

 [Watch Video Solution](#)

5. In a certain population, 10% of the people are rich, 5% are famous, and 3% are rich and famous. Then find the probability that a person picked at random from the population is either famous or rich but not both.

 [Watch Video Solution](#)

6. Three students A , B and C are in a swimming race. A and B have the same probability of winning and each is twice as likely to win as C . Find the probability that the B or C wins. Assume no two reach the winning point simultaneously.

 [Watch Video Solution](#)

7. Let A, B, C be three events such that $P(A) = 0.3, P(B) = 0.4, P(C) = 0.8, P(A \cap B) = 0.88, P(A \cap C) = 0.88$. If $P(A \cup B \cup C) \geq 0.75$, then show that $0.23 \leq P(B \cap C) \leq 0.48$.



[Watch Video Solution](#)

MCQ

1. A sample space consists of 3 sample points with associated probabilities given as $2p, p^2, 4p - 1$. Then the value of p is $p = a. \sqrt{11} - 3$
b. $\sqrt{10} - 3$ c. $\frac{1}{4} < p < \frac{1}{2}$ d. none

A. $p = \sqrt{11} - 3$

B. $\sqrt{10} - 3$

C. $\frac{1}{4} < p < \frac{1}{2}$

D. none of these

Answer: A



[Watch Video Solution](#)

2. Let E be an event which is neither a certainty nor an impossibility. If probability is such that $P(E) = 1 + \lambda + \lambda^2$ and $P(E') = (1 + \lambda)^2$ in terms of an unknown λ . Then $P(E)$ is equal to 1 b. $3/4$ c. $1/4$ d. none of these

A. 1

B. $\frac{3}{4}$

C. $\frac{1}{4}$

D. none of these

Answer: B



[Watch Video Solution](#)

3. Three balls marked with 1, 2 and 3 are placed in an urn. One ball is drawn, its number is noted, then the ball is returned to the urn. This

process is repeated and then repeated once more. Each ball is equally likely to be drawn on each occasion. If the sum of the number noted is 6, then the probability that the ball numbered with 2 is drawn at all the three occasions, is

A. $\frac{1}{27}$

B. $\frac{1}{7}$

C. $\frac{1}{6}$

D. $\frac{1}{3}$

Answer: B



[Watch Video Solution](#)

4. A draws a card from a pack of n cards marked 1, 2, ; n . The card is replaced in the pack and B draws a card. Then the probability that A draws a higher card than B is $(n + 1) / 2n$ b. $1 / 2$ c. $(n - 1) / 2n$ d. none of these

A. $(n + 1) / 2n$

B. $1 / 2$

C. $(n - 1) / 2n$

D. none of these

Answer: C



Watch Video Solution

5. South African cricket captain lost toss of a coin 13 times out of 14. The chance of this happening was a. $7 / 2^{13}$ b. $1 / 2^{13}$ c. $13 / 2^{14}$ d. none

A. $7 / 2^{13}$

B. $1 / 2^{13}$

C. $13 / 2^{14}$

D. $13 / 2^{13}$

Answer: A

 [Watch Video Solution](#)

6. Find the probability that birthdays of any two members out of five members in a family fall on Sunday.

A. $(12 \times 5^3) / 7^5$

B. $(10 \times 6^2) / 7^5$

C. $2/5$

D. $(10 \times 6^3) / 7^5$

Answer: D

 [Watch Video Solution](#)

7. Three houses are available in a locality. Three persons apply for the houses. Each applies for one houses without consulting others. The probability that all three apply for the same houses is $1/9$ b. $2/9$ c. $7/9$ d. $8/9$

A. $1/9$

B. $2/9$

C. $7/9$

D. $8/9$

Answer: A



Watch Video Solution

8. The numbers $1, 2, 3, \dots, n$ are arranged in a random order. The probability that the digits $1, 2, 3, \dots, k$ ($k < n$) appear as neighbours in that order is

A. $1/n!$

B. $k!/n!$

C. $(n - k)!/n!$

D. $(n - k + 1)!/n!$

Answer: D



[Watch Video Solution](#)

9. Words from the letters of the word PROBABILITY are formed by taking all letters at a time. The probability that both B 's are not together and both I 's are not together is $\frac{52}{55}$ b. $\frac{53}{55}$ c. $\frac{54}{55}$ d. none of these

A. $\frac{52}{55}$

B. $\frac{53}{55}$

C. $\frac{54}{55}$

D. none of these

Answer: B



[Watch Video Solution](#)

10. There are only two women among 20 persons taking part in a pleasure trip. The 20 persons are divided into two groups, each group consisting

of 10 person. Then the probability that the two women will be in the same group is $\frac{9}{19}$ b. $\frac{9}{38}$ c. $\frac{9}{35}$ d. none

A. $\frac{9}{19}$

B. $\frac{9}{38}$

C. $\frac{9}{35}$

D. none of these

Answer: A



Watch Video Solution

11. Five different games are to be distributed among 4 children randomly.

The probability that each child get at least one game is $\frac{1}{4}$ b. $\frac{15}{64}$ c.

$\frac{5}{9}$ d. $\frac{7}{12}$

A. $\frac{1}{4}$

B. $\frac{15}{64}$

C. $\frac{21}{64}$

D. none of these

Answer: B



[Watch Video Solution](#)

12. A drawer contains 5 brown socks and 4 blue socks well mixed a man reaches the drawer and pulls out socks at random. What is the probability that they match? $\frac{4}{9}$ b. $\frac{5}{8}$ c. $\frac{5}{9}$ d. $\frac{7}{12}$

A. $\frac{4}{9}$

B. $\frac{5}{8}$

C. $\frac{5}{9}$

D. $\frac{7}{12}$

Answer: A



[Watch Video Solution](#)

13. A four figure number is formed of the figures 1, 2, 3, 4, 5 with no repetitions. The probability that the number is divisible by 5 is $\frac{3}{4}$ b. $\frac{1}{4}$ c. $\frac{1}{8}$ d. none of these

A. $\frac{3}{4}$

B. $\frac{1}{4}$

C. $\frac{1}{8}$

D. none of these

Answer: B



[Watch Video Solution](#)

14. Twelve balls are distributed among three boxes, find the probability that the first box will contains three balls.

A. $\frac{110}{9} \left(\frac{2}{3}\right)^{10}$

B. $\frac{9}{110} \left(\frac{2}{3}\right)^{10}$

C. $\frac{{}^{12}C_3}{12^3} \times 2^9$

D. $\frac{{}^{12}C_3}{3^{12}}$

Answer: A



Watch Video Solution

15. A cricket club has 15 members, of them of whom only 5 can bowl. If the names of 15 members are put into a box and 11 are drawn at random, then the probability of getting an eleven containing at least 3 bowlers is
7/13 b. 6/13 c. 11/158 d. 12/13

A. 7/13

B. 6/13

C. 11/15

D. 12/13

Answer: D



Watch Video Solution

16. Seven girls $G_1, G_2, G_3, \dots, G_7$ are such that their ages are in order $G_1 < G_2 < G_3 < \dots < G_7$. Five girls are selected at random and arranged in increasing order of their ages. The probability that G_5 and G_7 are not consecutive is

A. $\frac{20}{21}$

B. $\frac{19}{21}$

C. $\frac{17}{21}$

D. $\frac{13}{21}$

Answer: C

[Watch Video Solution](#)

17. A local post office is to send M telegrams which are distributed at random over N communication channels, ($N > M$). Each telegram is

sent over any channel with equal probability. Chance that not more than one telegram will be sent over each channel is:

A. $\frac{{}^N C_M \times N!}{M^N}$

B. $\frac{{}^N C_M \times M!}{N^M}$

C. $1 - \frac{{}^N C_M \times M!}{M^N}$

D. $1 - \frac{{}^N C_M \times N!}{N^M}$

Answer: B



Watch Video Solution

18. Dialling a telephone number an old man forgets the last two digits remembering only that these are different dialled at random. The probability that the number is dialled correctly is 1/45 b. 1/90 c. 1/100 d. none of these

A. 1/45

B. 1/90

C. $1/100$

D. none of these

Answer: B



[Watch Video Solution](#)

19. If A and B each toss three coins. The probability that both get the same number of heads is

A. $(3/4)^{50}$

B. $(2/7)^{50}$

C. $(1/8)^{50}$

D. $(7/8)^{50}$

Answer: A



[Watch Video Solution](#)

20. In a game called odd man out $m(m > 2)$ persons toss a coin to determine who will buy refreshments for the entire group. A person who gets an outcome different from that of the rest of the members of the group is called the odd man out. The probability that there is a loser in any game is (A) $\frac{1}{2m}$ (B) $\frac{m}{2^{m-1}}$ (C) $\frac{2}{m}$ (D) none of these

A. $1/2m$

B. $m/2^{m-1}$

C. $2/m$

D. none of these

Answer: B



[Watch Video Solution](#)

21. $2n$ boys are randomly divided into two subgroups containing n boys each. The probability that the two tallest boys are in different groups is a. $n/(2n - 1)$ b. $(n - 1)/(2n - 1)$ c. $(n - 1)/4n^2$ d. none of these

A. $n / (2n - 1)$

B. $(n - 1)(2n - 1)$

C. $(n - 1) / 4n^2$

D. none of these

Answer: A



Watch Video Solution

22. If the papers of 4 students can be checked by any one of the 7 teachers, then the probability that all the 4 papers are checked by exactly 2 teachers is $2/7$ b. $12/49$ c. $32/343$ d. none of these

A. $2/7$

B. $12/49$

C. $32/343$

D. $6/49$

Answer: D



Watch Video Solution

23. Two events A and B are mutually not exclusive events if $P(A)=1/4, P(B)=2/5$ and $P(A \cup B)=1/2$ then find $P(A \cap B^c)$

A. $P(A) \leq 1 - P(B)$

B. $P \leq P(\bar{A} \cap \bar{B}) = P \leq P(\bar{A}) - P \leq P(\bar{B})$

C. $\left[-\frac{7}{9}, \frac{4}{9} \right]$

D. $\left[\frac{1}{3}, \frac{2}{3} \right]$

Answer: B



Watch Video Solution

24. A natural number is chosen at random from the first 100 natural numbers. The probability that $x + \frac{100}{x} > 50$ is 1/10 b. 11/50 c. 11/20

d. none of these

A. $\frac{1}{10}$

B. $\frac{11}{50}$

C. $\frac{11}{20}$

D. none of these

Answer: C



[Watch Video Solution](#)

25. A dice is thrown six times, it being known that each time a different digit is shown. The probability that a sum of 12 will be obtained in the first three throws is $\frac{5}{24}$ b. $\frac{25}{216}$ c. $\frac{3}{20}$ d. $\frac{1}{12}$

A. $\frac{5}{24}$

B. $\frac{25}{216}$

C. $\frac{3}{20}$

D. $\frac{1}{12}$

Answer: C



Watch Video Solution

26. If a is an integer lying in $[-5, 30]$, then the probability that the graph of $y = x^2 + 2(a + 4)x - 5a + 64$ is strictly above the x-axis is

A. $1/6$

B. $7/36$

C. $2/9$

D. $3/5$

Answer: C



Watch Video Solution

27. Four die are thrown simultaneously. The probability that 4 and 3 appear on two of the die given that 5 and 6 have appeared on other two die is a) $1/6$ b) $1/36$ c) $12/151$ d) none of these

A. $1/6$

B. $1/36$

C. $12/151$

D. none of these

Answer: C



[Watch Video Solution](#)

28. A $2n$ digit number starts with 2 and all its digits are prime, then the probability that the sum of all 2 consecutive digits of the number is prime is a. 4×2^{3n} b. 4×2^{-3n} c. 2^{3n} d. none of these

A. 4×2^{-3n}

B. 4×2^{-3n}

C. 2^{-3n}

D. none of these

Answer: B



Watch Video Solution

29. In a n – sided regular polygon, the probability that the two diagonal chosen at random will intersect inside the polygon is: (a.)

$\frac{{}^n C_2}{{}^n C_2 - n}$ (b.) $\frac{n(n-1) C_2}{{}^n C_2 - n}$ (c.) $\frac{{}^n C_4}{{}^n C_2 - n}$

(d.) none of these

A. $\frac{{}^n C_2}{{}^n C_2 - n}$

B. $\frac{n(n-1) C_2}{{}^n C_2 - n}$

C. $\frac{{}^n C_4}{{}^n C_2 - n}$

D. none of these

Answer: C



Watch Video Solution

30. A three-digit number is selected at random from the set of all three-digit numbers. The probability that the number selected has all the three digits same is $\frac{1}{9}$ b. $\frac{1}{10}$ c. $\frac{1}{50}$ d. $\frac{1}{100}$

A. $\frac{1}{9}$

B. $\frac{1}{10}$

C. $\frac{1}{50}$

D. $\frac{1}{100}$

Answer: D



Watch Video Solution

31. Two numbers a, b are chosen from the set of integers 1, 2, 3, ..., 39.

Then probability that the equation $7a - 9b = 0$ is satisfied is

A. $1/247$

B. $2/247$

C. $4/741$

D. $5/741$

Answer: C



[Watch Video Solution](#)

32. One mapping is selected at random from all mappings of the set

$S = \{1, 2, 3, \dots, n\}$ into itself. If the probability that the mapping is one-

one is $3/32$, then the value of n is 2 b. 3 c. 4 d. none of these

A. 2

B. 3

C. 4

D. none of these

Answer: C



[Watch Video Solution](#)

33. A composite number is selected at random from the first 30 natural numbers and it is divided by 5. The probability that there will be remainder is $14/19$ b. $5/19$ c. $5/6$ d. $7/15$

A. $14/19$

B. $5/19$

C. $5/6$

D. $7/15$

Answer: A



[Watch Video Solution](#)

34. Forty teams play a tournament. Each team plays every other team just once. Each game results in a win for one team. If each team has a 50% chance of winning each game, the probability that at the end of the tournament, every team has won a different number of games is

a. $1/780$
b. $40!/2^{780}$ c. $40!/2^{780}$ d. none of these

A. $1/780$

B. $40!/2^{780}$

C. $36/{}^{64}C_3$

D. $98/{}^{64}C_3$

Answer: B



[Watch Video Solution](#)

35. about to only mathematics

A. $196/{}^{64}C_3$

B. $49 / {}^{64}C_3$

C. $36 / {}^{64}C_3$

D. $98 / {}^{64}C_3$

Answer: A



[View Text Solution](#)

36. A bag has 10 balls. Six ball are drawn in an attempt and replaced. Then another draw of 5 balls is made from the bag. The probability that exactly two balls are common to both the draw is a. $5/21$ b. $2/21$ c. $7/21$ d. $3/21$

A. $5/21$

B. $2/21$

C. $7/21$

D. $3/21$

Answer: A

[Watch Video Solution](#)

37. Find the probability that a randomly chosen three-digit number has exactly three factors.

A. $2/225$

B. $7/900$

C. $1/800$

D. none of these

Answer: B

[Watch Video Solution](#)

38. Let p, q , be chosen one by one from the set $\{1, \sqrt{2}, \sqrt{3}, 2, e, \pi\}$ with replacement. Now a circle is drawn taking (p, q) as its centre. Then the probability (rational points are those points whose both the coordinates are rational) $2/3$ b. $7/8$ c. $8/9$ d. none of these

A. $\frac{2}{3}$

B. $\frac{7}{8}$

C. $\frac{8}{9}$

D. none of these

Answer: C



Watch Video Solution

39. Three integers are chosen at random from the set of first 20 natural numbers. The chance that their product is a multiple of 3 is $\frac{194}{285}$ b. $\frac{1}{57}$ c. $\frac{13}{19}$ d. $\frac{3}{4}$

A. $\frac{194}{285}$

B. $\frac{1}{57}$

C. $\frac{13}{19}$

D. $\frac{3}{4}$

Answer: A



Watch Video Solution

40. Five different marbles are placed in 5 different boxes randomly. Then the probability that exactly two boxes remain empty is (each box can hold any number of marbles) $\frac{2}{5}$ b. $\frac{12}{25}$ c. $\frac{3}{5}$ d. none of these

A. $\frac{2}{5}$

B. $\frac{12}{25}$

C. $\frac{3}{5}$

D. none of these

Answer: C



Watch Video Solution

41. There are 10 prizes, five As, three Bs and two Cs, placed in identical sealed envelopes for the top 10 contestants in a mathematics contest. The prizes are awarded by allowing winners to select an envelope at random from those remaining. Then the 8th contestant goes to select the prize, the probability that the remaining three prizes are one A and B and one C is $\frac{1}{4}$ b. $\frac{1}{3}$ c. $\frac{1}{12}$ d. $\frac{1}{10}$

A. $\frac{1}{4}$

B. $\frac{1}{3}$

C. $\frac{1}{12}$

D. $\frac{1}{10}$

Answer: A



Watch Video Solution

42. A car is parked among N cars standing in a row, but not at either end. On his return, the owner finds that exactly r of the N places are still

occupied. The probability that the places neighboring his car are empty is

$$\frac{(r-1)!}{(N-1)!} \quad \text{b.} \quad \frac{(r-1)!(N-r)!}{(N-1)!} \quad \text{c.} \quad \frac{(N-r)(N-r-1)}{(N-1)(N+2)} \quad \text{d.} \\ \frac{{}^{(N-r)}C_2}{{}^{(N-1)}C_2}$$

A. $\frac{(r-1)!}{(N-1)!}$

B. $\frac{(r-1)!(N-r)!}{(N-1)!}$

C. $\frac{(N-r)(N-r-1)}{(N+1)(N+2)}$

D. $\frac{{}^{N-r}C_2}{{}^{N-1}C_2}$

Answer: D



Watch Video Solution

43. Let A be a set containing n elements. A subset P of the set A is chosen at random. The set A is reconstructed by replacing the elements of P , and another subset Q of A is chosen at random. The probability that $P \cap Q$ contains exactly m ($m < n$) elements, is

A. $\frac{3^{n-m}}{4^n}$

B. $\frac{{}^n C_m \cdot 3^m}{4^n}$

C. $\frac{{}^n C_m \cdot 3^{n-m}}{4^n}$

D. none of these

Answer: C



Watch Video Solution

44. Two dice are thrown at a time. find the probability that the sum of the outcomes will be 6. a)5/36 b)8/36 c) 4/9 d) 1/3

A. 5 / 36

B. 8 / 36

C. 4 / 9

D. 1 / 3

Answer: C



Watch Video Solution

45. If a and b are chosen randomly from the set consisting of number 1, 2, 3, 4, 5, 6 with replacement. Then the probability that

$$\lim_{x \rightarrow 0} [(a^x + b^x)/2]^{2/x} = 6 \text{ is}$$

A. $1/3$

B. $1/4$

C. $1/9$

D. $2/9$

Answer: C



[Watch Video Solution](#)

46. Mr. A lives at origin on the Cartesian plane and has his office at $(4, 5)$. His friend lives at $(2, 3)$ on the same plane. Mrs. A can go to his office travelling one block at a time either in the $+y$ or $+x$ direction. If all possible paths are equally likely then the probability that Mr. A passed his

friends house is (shortest path for any event must be consider4ed) $1/2$ b.

10/21 c. $1/4$ d. 11/21

A. $1/2$

B. 10/21

C. $1/4$

D. 11/21

Answer: B



Watch Video Solution

47. If A and B are two events, the probability that exactly one of them occurs is given by

a. $P(A) + P(B) - 2P(A \cap B)$ b. $P(A \cap B) + P(A \cap B')$ c.

$P(A \cup B) - P(A \cap B)$ d. $P(A') + P(B') - 2P(A' \cap B')$

A. $P(A) + P(B) - 2P(A \cap B)$

B. $P(A \cap \bar{B}) + P(\bar{A} \cap B)$

$$C. P(A \cup B) - P(A \cap B)$$

$$D. P(\bar{A}) + P(\bar{B}) - 2P(\bar{A} \cap \bar{B})$$

Answer: A::B::C::D



Watch Video Solution

48. If p and q are chosen randomly from the set $\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ with replacement, determine the probability that the roots of the equation $x^2 + px + q = 0$ are real.

A. are real is $33/50$

B. are imaginary is $19/50$

C. are real and equal is $3/50$

D. are real and distinct is $3/5$

Answer: B::C::D



Watch Video Solution

49. If A and B are two events such that $P(A) = 3/4$ and $P(B) = 5/8$, then (correct options may be more than one)

A. $P(A \cup B) \geq 3/4$

B. $P(A' \cap B) \leq 1/4$

C. $1/8 \leq P(A \cap B') \leq 3/8$

D. $3/8 \leq P(A \cap B) \leq 5/8$

Answer: A::B::C::D



Watch Video Solution

50. If A and B are mutually exclusive events, then (a) $P(A) \leq P(\bar{B})$ (b) $P(A) > P(B)$ (c) $P(B) \leq P(\bar{A})$ (d) $P(A) > P(B)$

A. $P(A) \leq P(\bar{B})$

B. $P(A) > P(B)$

C. $P(B) \leq P(\bar{A})$

D. $P(A) > P(B)$

Answer: A::C



Watch Video Solution

51. Probability if n heads in $2n$ tosses of a fair coin can be given by

a. $\prod_{r=1}^n \left(\frac{2r-1}{2r} \right)$

b. $\prod_{r=1}^n \left(\frac{n+r}{2r} \right)$

c. $\sum_{r=0}^n \left(\frac{{}^n C_r}{2^n} \right)^2$

d. $\frac{\sum_{r=0}^n ({}^n C_r)^2}{\sum_{r=0}^{2n} ({}^{2n} C_r)^2}$



Watch Video Solution

52. about to only mathematics

A. $P_1 = 1/9$

B. $P_1 = 1/16$

C. $P_2 = 1/3$

D. $P_2 = 1/4$

Answer: A::C



Watch Video Solution

53. A bag contains b blue balls and r red balls. If two balls are drawn at random, the probability of drawing two red balls is five times the probability of drawing two blue balls. Furthermore, the probability of drawing one ball of each color is six times the probability of drawing two blue balls. Then (a) $b + r = 9$ (b) $br = 18$ (c) $|b - r| = 4$ (d) $b/r = 2$

A. $b + r = 9$

B. $br = 18$

C. $|b - r| = 4$

D. $b/r = 2$

Answer: A::B



Watch Video Solution

54. Two numbers are selected randomly from the set $S = \{1, 2, 3, 4, 5, 6\}$ without replacement one by one. The probability that minimum of the two numbers is less than 4 is $\frac{1}{15}$ b. $\frac{14}{15}$ c. $\frac{1}{5}$ d. $\frac{4}{5}$

A. the smallest value of two is less than 3 is $\frac{13}{28}$

B. the bigger value of two is more than 5 is $\frac{9}{14}$

C. product of two number is even is $\frac{11}{14}$

D. none of these

Answer: A::B::C



Watch Video Solution

1. A shopping mall is running a scheme: Each packet of detergent SURF contains a coupon which bears letter of the word SURF, if a person buys at least four packets of detergent SURF, and produce all the letters of the word SURF, then he gets one free packet of detergent.

If a person buys 8 such packets, then the probability that he gets two free packets is

A. 4^8

B. 8^4

C. ${}^{11}C_3$

D. ${}^{12}C_4$

Answer: C



[Watch Video Solution](#)

2. A shopping mall is running a scheme: Each packet of detergent SURF contains a coupon which bears letter of the word SURF, if a person buys

at least four packets of detergent SURF, and produce all the letters of the word SURF, then he gets one free packet of detergent.

If person buys 8 such packets, then the probability that he gets exactly one free packets is

- A. $7/33$
- B. $102/495$
- C. $13/55$
- D. $34/165$

Answer: D



[Watch Video Solution](#)

3. A shopping mall is running a scheme: Each packet of detergent SURF contains a coupon which bears letter of the word SURF, if a person buys at least four packets of detergent SURF, and produce all the letters of the word SURF, then he gets one free packet of detergent.

If a person buys 8 such packets, then the probability that he gets two free packets is

A. $1/7$

B. $1/5$

C. $1/42$

D. $1/165$

Answer: D



[Watch Video Solution](#)

4. There are two die A and B both having six faces. Die A has three faces marked with 1, two faces marked with 2, and one face marked with 3. Die B has one face marked with 1, two faces marked with 2, and three faces marked with 3. Both dices are thrown randomly once. If E be the event of getting sum of the numbers appearing on top faces equal to x and let P(E) be the

probability of event E, then

$P(E)$ is minimum when x equals to

A. 5

B. 3

C. 4

D. 6

Answer: C



Watch Video Solution

5. There are two die A and B both having six faces. Die A has three faces marked with 1, two faces marked with 2, and one face marked with 3. Die B has one face marked with 1, two faces marked with 2, and three faces marked with 3. Both dices are thrown randomly once. If E be the event of getting sum of the numbers appearing on top faces equal to x and let $P(E)$ be the probability of event E, then $P(E)$ is minimum when x equals to

A. 3

B. 4

C. 5

D. 6

Answer: B



[Watch Video Solution](#)

6. There are two die A and B both having six faces. Die A has three faces marked with 1, two faces marked with 2, and one face marked with 3. Die B has one face marked with 1, two faces marked with 2, and three faces marked with 3. Both dices are thrown randomly once. If E be the event of getting sum of the numbers appearing on top faces equal to x and let $P(E)$ be the probability of event E, then

$P(E)$ is maximum when x equal to

A. $5/9$

B. $\frac{6}{7}$

C. $\frac{7}{18}$

D. $\frac{8}{19}$

Answer: C



Watch Video Solution

7. A cube having all of its sides painted is cut by two horizontal, two vertical, and other two planes so as to form 27 cubes all having the same dimensions. Of these cubes, a cube is selected at random.

The probability that the cube selected has two sides painted is (a) $\frac{4}{9}$ (b) $\frac{1}{27}$ (c) $\frac{1}{18}$ (d) $\frac{5}{54}$

A. $\frac{1}{9}$

B. $\frac{1}{27}$

C. $\frac{1}{18}$

D. $\frac{5}{54}$

Answer: B



[Watch Video Solution](#)

8. A cube having all of its sides painted is cut by two horizontal, two vertical, and other two planes so as to form 27 cubes all having the same dimensions. Of these cubes, a cube is selected at random.

The probability that the cube selected has two sides painted is (a) $\frac{4}{9}$ (b) $\frac{1}{27}$ (c) $\frac{1}{18}$ (d) $\frac{5}{54}$

A. $\frac{1}{9}$

B. $\frac{4}{9}$

C. $\frac{8}{27}$

D. none of these

Answer: B



[Watch Video Solution](#)

9. A cube having all of its sides painted is cut to be two horizontal , two vertical and other two planes, so as to form 27 cubes all having the same dimenions of these cubes, a cube is selected at random.

If P_1 be the probability that the cube selected having atleast one of its sides painted, then the value of $27P_1$, is

A. 18

B. 20

C. 22

D. 26

Answer: D



[Watch Video Solution](#)

10. There are some experiment in which the outcomes cannot be identified discretely. For example, an ellipse of eccentricity $2\sqrt{2}/3$ is inscribed in a circle and a point within the circle is chosen at random.

Now, we want to find the probability that this point lies outside the ellipse. Then, the point must lie in the shaded region shown in Figure. Let the radius of the circle be a and length of minor axis of the ellipse be $2b$.

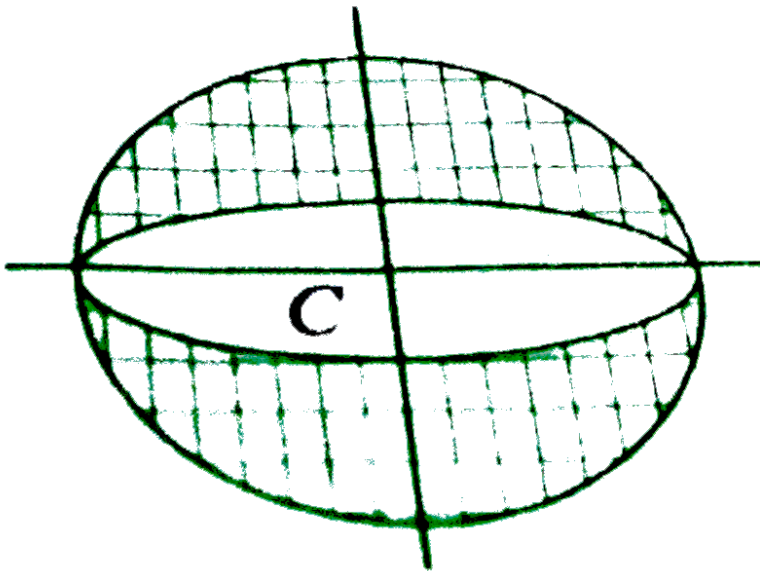
Given that

$$1 - \frac{b^2}{a^2} = \frac{8}{9} \text{ or } \frac{b^2}{a^2} = \frac{1}{9}$$

Then, the area of circle serves as sample space and area of the shaded region represents the area for favorable cases. Then, required probability is

$$\begin{aligned} p &= \frac{\text{Area of shaded region}}{\text{Area of circle}} \\ &= \frac{\pi a^2 - \pi ab}{\pi a^2} = 1 - \frac{b}{a} = 1 - \frac{1}{3} = \frac{2}{3} \end{aligned}$$

Now, answer the following questions.



Two persons A and B agree to meet at a place between 5 and 6 pm. The first one to arrive waits for 20 min and then leave. If the time of their arrival be independent and at random, then the probability that A and B meet is

- A. $1/4$
- B. $1/2$
- C. $1/3$
- D. $1/\sqrt{2}$

Answer: A

 [Watch Video Solution](#)

11. There are some experiment in which the outcomes cannot be identified discretely. For example, an ellipse of eccentricity $2\sqrt{2}/3$ is inscribed in a circle and a point within the circle is chosen at random. Now, we want to find the probability that this point lies outside the ellipse. Then, the point must lie in the shaded region shown in Figure. Let

the radius of the circle be a and length of minor axis of the ellipse be $2b$.

Given that

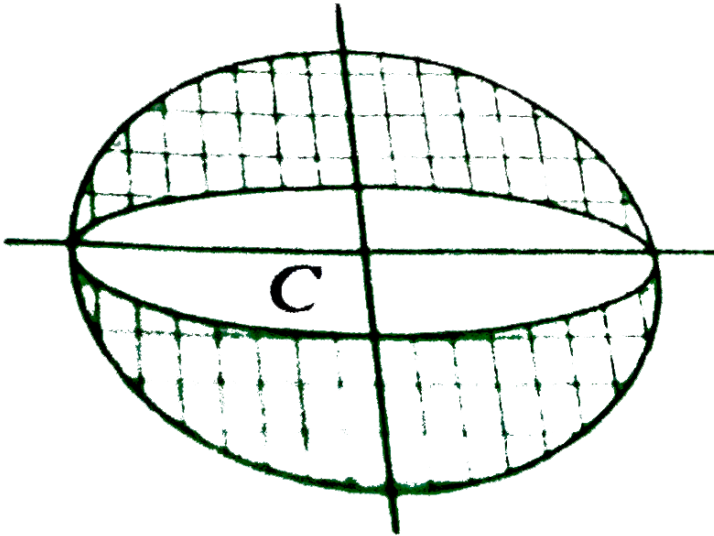
$$1 - \frac{b^2}{a^2} = \frac{8}{9} \text{ or } \frac{b^2}{a^2} = \frac{1}{9}$$

Then, the area of circle serves as sample space and area of the shaded region represents the area for favorable cases. Then, required probability

is

$$\begin{aligned} p &= \frac{\text{Area of shaded region}}{\text{Area of circle}} \\ &= \frac{\pi a^2 - \pi ab}{\pi a^2} = 1 - \frac{b}{a} = 1 - \frac{1}{3} = \frac{2}{3} \end{aligned}$$

Now, answer the following questions.



A point is selected at random inside a circle. The probability that the point is closer to the center of the circle than to its circumference is

A. $1/4$

B. $1/3$

C. $2/3$

D. $5/9$

Answer: D



Watch Video Solution

12. If the squares of a 8×8 chessboard are painted either red or black at random.

The probability that all the squares in any column are of same color and that of a row are of alternating color is

A. $(1 - 1/2^7)^8$

B. $1/2^{56}$

C. $1 - 1/2^7$

D. none of these

Answer: A



Watch Video Solution

13. If the squares of a 8×8 chess board are painted either red and black at random .The probability that not all squares in any column is alternating in colour is

A. $\frac{{}^{64}C_{32}}{2^{64}}$

B. $\frac{64!}{32!.2^{64}}$

C. $\frac{(2^7 - 1)^8}{2^{56}}$

D. none of these

Answer: A



Watch Video Solution

14. If the squares of a 8×8 chess board are painted either red and black at random. The probability that not all squares in any column is alternating in colour is

A. $1/2^{64}$

B. $1 - 1/2^{63}$

C. $1/2$

D. none of these

Answer: B



[Watch Video Solution](#)

Match

1. n whole are randomly chosen and multiplied

Column I, Column II

The probability that the last digit is 1,3,7, or 9 is, p. $\frac{8^n - 4^n}{10^n}$

The probability that the last digit is 2,4,6, or 8 is, q. $\frac{5^n - 4^n}{10^n}$

The probability that the last digit is 5 is, r. $\frac{4^n}{10^n}$

The probability that the last digit is zero is, s. $\frac{10^n - 8^n - 5^n + 4^n}{10^n}$

- A. a b c d
q s s r
- B. a b c d
r q q p
- C. a b c d
q p p s
- D. a b c d
q s p r

Answer: A::B::C::D



Watch Video Solution

2. Three distinct numbers a, b and c are chosen at random from the numbers 1, 2, ..., 100. The probability that

List I

List II

a. a, b, c are in AP is

p. $\frac{53}{161700}$

b. a, b, c are in GP is

q. $\frac{1}{66}$

c. $\frac{1}{a} \cdot \frac{1}{b} \cdot \frac{1}{c}$ are in GP is

r. $\frac{1}{22}$

d. a + b + c is divisible by 2 is

s. $\frac{1}{2}$

A. Option a. a b c d
 q s s r

B. Option b. a b c d
 r q q p

C. Option c. a b c d
 q p p s

D. Option d. a b c d
 q s p r

Answer: C

 [Watch Video Solution](#)

Numerical Value Type

1. If the probability of a six digit number N whose six digit sare 1,2,3,4,5,6 written as random order is divisible by 6 is p , then the value of $1/p$ is_____.

 [Watch Video Solution](#)

2. If the probability that the product of the outcomes of three rolls of a fair dice is a prime number is p , then the value of $1/(4p)$ is _____.

 [Watch Video Solution](#)

3. There are two red, two blue, two white, and certain number (greater than 0) of green socks in a drawer. If two socks are taken at random from the drawer without replacement, the probability that they are of the same color is $1/5$, then the number of green socks are _____.

 [Watch Video Solution](#)

4. A dice is weighted such that the probability of rolling the face numbered n is proportional to n^2 ($n = 1, 2, 3, 4, 5, 6$). The dice is rolled twice, yielding the number a and b . The probability that $a > b$ is p then the value of $[2/p]$ (where $[\cdot]$ represents greatest integer function) is _____.

 [Watch Video Solution](#)

5. In a knockout tournament 2^n equally skilled players, S_1, S_2, S_{2^n} are participating. In each round, players are divided in pair at random and winner from each pair moves in the next round. If S_2 reaches the semi-final, then the probability that S_1 wins the tournament is $1/84$. The value of n equals_____.



[Watch Video Solution](#)

6. Five different games are to be distributed among 4 children randomly. The probability that each child get at least one game is $1/4$ b. $15/64$ c. $5/9$ d. $7/12$



[Watch Video Solution](#)

7. A bag contains 10 different balls. Five balls are drawn simultaneously and then replaced and then seven balls are drawn. The probability that

exactly three balls are common to the two draw is p , then the value of $12p$ is _____.



[Watch Video Solution](#)

ARCHIVES

1. Four numbers are chosen at random (without replacement) from the set $\{1, 2, 3, \dots, 20\}$. Statement-1: The probability that the chosen numbers when arranged in some order will form an AP is $\frac{1}{85}$. Statement-2: If the four chosen numbers form an AP, then the set of all possible values of common difference is $\{1, 2, 3, 4, 5\}$. (1) Statement-1 is true, Statement-2 is true; Statement-2 is not the correct explanation for Statement-1 (2) Statement-1 is true, Statement-2 is false (3) Statement-1 is false, Statement-2 is true (4) Statement-1 is true, Statement-2 is true; Statement-2 is the correct explanation for Statement-1

A. Statement 1 is false, statement 2 is true.

B. Statement 1 is true, statement 2 is true, statement 2 is a correct explanation for statement 1.

C. Statement 1 is true, statement 2 is true, statement 2 is not a correct explanation for statement 2.

D. Statement 1 is true, statement 2 is false.

Answer: D



Watch Video Solution

2. An urn contains nine balls of which three are red, four are blue and two are green. Three balls are drawn at random without replacement from the urn. The probability that the three balls have different colour is

A. $\frac{2}{23}$

B. $\frac{1}{3}$

C. $\frac{2}{7}$

D. $\frac{1}{21}$

Answer: C



Watch Video Solution

3. If two different numbers are taken from the set $\{0, 1, 2, 3, \dots, 10\}$; then the probability that their sum as well as absolute difference are both multiple of 4, is: (1) $\frac{14}{45}$ (2) $\frac{7}{55}$ (3) $\frac{6}{55}$ (4) $\frac{12}{55}$

A. $\frac{7}{55}$

B. $\frac{6}{55}$

C. $\frac{12}{55}$

D. $\frac{14}{45}$

Answer: B



Watch Video Solution

4. For three events A, B and C , P (Exactly one of A or B occurs) = P (Exactly one of B or C occurs) = P (Exactly one of C or A occurs) = $\frac{1}{4}$ and P (All the three events occur simultaneously) = $\frac{1}{16}$. Then the probability that at least one of the events occurs, is :

A. $\frac{3}{16}$

B. $\frac{7}{32}$

C. $\frac{7}{16}$

D. $\frac{7}{64}$

Answer: C



[Watch Video Solution](#)

JEE Advanced

1. Let ω be a complex cube root unity with $\omega \neq 1$. A fair die is thrown three times. If r_1, r_2 and r_3 are the numbers obtained on the die, then the

probability that $\omega^{r^1} + \omega^{r^2} + \omega^{r^3} = 0$ is 1/18 b. 1/9 c. 2/9 d. 1/36

A. 1/18

B. 1/9

C. 2/9

D. 1/36

Answer: C



Watch Video Solution

2. about to only mathematics

A. $\frac{1}{2}$

B. $\frac{1}{3}$

C. $\frac{2}{3}$

D. $\frac{3}{4}$

Answer: A

[Watch Video Solution](#)

3. Three randomly chosen nonnegative integers x , y and z are found to satisfy the equation $x + y + z = 10$. Then the probability that z is even,

is: (a) $\frac{5}{12}$ (b) $\frac{1}{2}$ (c) $\frac{6}{11}$ (d) $\frac{36}{55}$

A. $\frac{1}{2}$

B. $\frac{36}{55}$

C. $\frac{6}{11}$

D. $\frac{5}{11}$

Answer: C

[Watch Video Solution](#)

4. Box 1 contains three cards bearing numbers 1, 2, 3; box 2 contains five cards bearing numbers 1, 2, 3, 4, 5; and box 3 contains seven cards bearing numbers 1, 2, 3, 4, 5, 6, 7. A card is drawn from each of the boxes. Let x_i be

the number on the card drawn from the i th box, $i = 1, 2, 3$. The probability that $x_1 + x_2 + x_3$ is odd is

A. a. $\frac{29}{105}$

B. b. $\frac{53}{105}$

C. c. $\frac{57}{105}$

D. d. $\frac{1}{2}$

Answer: B



Watch Video Solution

5. Box 1 contains three cards bearing numbers 1, 2, 3; box 2 contains five cards bearing numbers 1, 2, 3, 4, 5; and box 3 contains seven cards bearing numbers 1, 2, 3, 4, 5, 6, 7. A card is drawn from each of the boxes. Let x_i be the number on the card drawn from the i th box, $i = 1, 2, 3$. The probability that x_1, x_2, x_3 are in an arithmetic progression is

A. $\frac{9}{105}$

B. $\frac{10}{105}$

C. $\frac{11}{105}$

D. $\frac{7}{105}$

Answer: C



Watch Video Solution

6. Five boys and four girls sit in a row randomly. The probability that no two girls sit together

A. $\frac{5}{42}$

B. $\frac{1}{8}$

C. $\frac{7}{40}$

D. $\frac{1}{5}$

Answer: A



Watch Video Solution

7. PARAGRAPH A There are five students S_1, S_2, S_3, S_4 and S_5 in a music class and for them there are five seats R_1, R_2, R_3, R_4 and R_5 arranged in a row, where initially the seat R_i is allotted to the student $S_i, i = 1, 2, 3, 4, 5$. But, on the examination day, the five students are randomly allotted five seats. For $i = 1, 2, 3, 4$, let T_i denote the event that the students S_i and S_{i+1} do NOT sit adjacent to each other on the day of the examination. Then, the probability of the event $T_1 \cap T_2 \cap T_3 \cap T_4$ is $\frac{1}{15}$ (b) $\frac{1}{10}$ (c) $\frac{7}{60}$ (d) $\frac{1}{5}$

A. $\frac{1}{15}$

B. $\frac{1}{10}$

C. $\frac{7}{60}$

D. $\frac{1}{5}$

Answer: C



Watch Video Solution

1. Eight players $P_1, P_2, P_3, \dots, P_8$, play a knock out tournament. It is known that whenever the players P_i and P_j , play, the player P_i will win if $i < j$. Assuming that the players are paired at random in each round, what is the probability that the players P_4 , reaches the final ?

 [Watch Video Solution](#)

2. Suppose A and B shoot independently until each hits his target. They have probabilities $3/5$ and $5/7$ of hitting the targets at each shot. Find probability that B will require more shots than A .

 [Watch Video Solution](#)

3. A tennis match of best of 5 sets is played by two players A and B . The probability that first set is won by A is $1/2$ and if he lost the first, then

probability of his winning the next set is $1/4$, otherwise it remains same.

Find the probability that A wins the match.

 [Watch Video Solution](#)

4. A coin has probability p of showing head when tossed. It is tossed n times. Let P_n denote the probability that no two (or more) consecutive heads occur. Prove that

$P_1 = 1$, $P_2 = 1 - p^2$ and $P_n = (1 - p)P_{n-1} + p(1 - p)P_{n-2}$ for all $n \geq 3$.

 [Watch Video Solution](#)

5. The probability of hitting a target by three marksmen are $1/2$, $1/3$ and $1/4$. Then find the probability that one and only one of them will hit the target when they fire simultaneously.

 [Watch Video Solution](#)

6. Factorise the following: $a^4 + 2a^2b^2 + b^4$



[Watch Video Solution](#)

7. If A and B are two independent events, prove that $P(A \cup B) \cdot P(A' \cap B') \leq P(C)$, where C is an event defined that exactly one of A and B occurs.



[Watch Video Solution](#)

8. Two players P_1 and P_2 are playing the final of a chess championship, which consists of a series of matches. Probability of P_1 winning a match is $2/3$ and that of P_2 is $1/3$. Thus winner will be the one who is ahead by 2 games as compared to the other player and wins at least 6 games. Now, if the player P_2 wins the first four matches, find the probability of P_1 winning the championship.



[Watch Video Solution](#)

9. Consider a game played by 10 people in which each flips a fair up coin at the same time. If all but one of the coins comes up the same, then the odd persons wins (e.g., if there are nine tails and one head then head wins). If such a situation does not occur, the players flips again. Find the probability that game is settled on or after n th toss.

 [Watch Video Solution](#)

10. about to only mathematics

 [Watch Video Solution](#)

11. simplify the expression: $(7m - 8n)^2 + (7m + 8n)^2$

 [Watch Video Solution](#)

12. An urn contains 2 white and 2 black balls. A ball is drawn at random. If it is white, it is not replaced into urn, otherwise it is replaced along with another ball of the same colour. The process is repeated, find the probability that the third ball drawn is black.

 [Watch Video Solution](#)

13. An unbiased coin is tossed. If the result is a head, a pair of unbiased dice is rolled and the number obtained by adding the numbers on two faces is noted. If the result is a tail, a card from a well-shuffled pack of 11 cards numbered 2, 3, 4, ..., 12 is picked and the number on the card is noted. What is the probability that the noted number is either 7 or 8?

 [Watch Video Solution](#)

14. Answer the following questions : If m things are distributed among a men and women, show that the probability of receiving odd number of

things by 'men is $\frac{1}{2} \left[\frac{(b+a)^m - (b-a)^m}{(b+a)^m} \right]$.

 [Watch Video Solution](#)

15. Simplify the expression: $(ab + bc)^2 - 2ab^2c$

 [Watch Video Solution](#)

16. From an urn containing a white and b black balls, k balls are drawn and laid aside, their color unnoted. Then one more ball is drawn. Find the probability that it is white assuming that $k < a, b$

 [Watch Video Solution](#)

17. A bag contains n balls, one of which is white. The probability that A and B speak truth are P_1 and P_2 , respectively. One ball is drawn from the bag and A and B both assert that it is white. Find the probability that drawn ball is actually white.



[Watch Video Solution](#)

18. A bag contains a total of 20 books on physics and mathematics, Any possible combination of books is equally likely. Ten books are chosen from the bag and it is found that it contains 6 books of mathematics. Find out the probability that the remaining books in the bag contains 3 books on mathematics.



[Watch Video Solution](#)

19. In a test, an examinee either guesses or copies or knows the answer to a multiple choice question with four choices. The probability that he makes a guess is $\frac{1}{3}$ and the probability that he copies the answer is $\frac{1}{6}$. The probability that his answer is correct given that he copied it is $\frac{1}{8}$. Find the probability that he knew the answer to the question, given that he correctly answered it.



[Watch Video Solution](#)

20. A box contains N coins m of which are fair and the rest are biased. The probability of getting a head when a fair coin is tossed is $1/2$, while it is $2/3$ when a biased coin is tossed. A coin is drawn from the box at random and is tossed twice. The first time it shows head and the second time it shows tail. What is the probability that the coin drawn is fair?



[Watch Video Solution](#)

21. about to only mathematics



[View Text Solution](#)

CONCEPT APPCICATION EXERCISE 14.1

1. Three coins are tossed. If one of them shows tail, then find the probability that all three coins show tail.



[Watch Video Solution](#)

2. If two events A and B are such that $P(A^c) = 0.3$, $P(B) = 0.4$, and $P(A \cap B^c) = 0.5$, then find the value of $P[B/(A \cup B^c)]$.

 [Watch Video Solution](#)

3. In a single throw of two dice what is the probability of obtaining a number greater than 7, if 4 appears on the first dice?

 [Watch Video Solution](#)

4. A coin is tossed three times in succession. If E is the event that there are at least two heads and F is the event in which first throw is a head, then find $P(E/F)$.

 [Watch Video Solution](#)

5. Consider a sample space S representing the adults in a small town who have completed the requirements for a college degree. They have been categorized according to sex and employment as follows: , Employed, Unemployed Male, 460, 40 Female, 140, 260 An employed person is selected at random. Find the probability that the chosen one is a male.



[Watch Video Solution](#)

CONCEPT APPCICATION EXERCISE 14.2

1. A bag contains 5 white and 3 black balls. Four balls are successively drawn out without replacement. What is the probability that they are alternately of different colours?



[Watch Video Solution](#)

2. Cards are drawn one-by-one at random from a well-shuffled pack of 52 playing cards until 2 aces are obtained from the first time. The probability

that 18 draws are obtained for this is

 [Watch Video Solution](#)

3. In a multiple choice question, there are four alternative answers of which one or more than one is correct. A candidate will get marks on the question only if he ticks the correct answer. The candidate decides to tick answers at a random. If he is allowed up to three chances to answer the question, then find the probability that he will get marks on it.

 [Watch Video Solution](#)

CONCEPT APPLICATION EXERCISE 14.3

1. A coin is tossed three times. Event A: two heads appear. Event B: last should be head. Then identify whether events A and B are independent or dependent.

 [Watch Video Solution](#)

2. Events A and B are such that $P(A) = \frac{1}{2}$, $P(B) = \frac{7}{12}$ and $P(\text{not A or not B}) = \frac{1}{4}$. State whether A and B are independent ?

 [Watch Video Solution](#)

3. Two cards are drawn one by one randomly from a pack of 52 cards. Then find the probability that both of them are Jack.

 [Watch Video Solution](#)

4. The probability of happening an event A in one trial is 0.4. Find the probability that the event A happens at least one in three independent trials.

 [Watch Video Solution](#)

5. In a bag there are 6 balls of which 3 are white and 3 are black. They are drawn successively with replacement. What is the chance that the colours are alternate ?



[Watch Video Solution](#)

6. A man performs 10 trials of an experiment, if the probability of getting '4 successes' is maximum, then find the probability of failure in each trial.



[Watch Video Solution](#)

7. A man and a woman appear in an interview for two vacancies in the same post. The probability of mans selection is $\frac{1}{4}$ and that the womans selection is $\frac{1}{3}$. What is the probability that none of them will be selected?



[Watch Video Solution](#)

8. The probability that Krishna will be alive 10 years hence is $\frac{7}{15}$ and that Hari will be alive is $\frac{7}{10}$. What is the probability that both Krishna and Hari will be dead 10 years hence?



[Watch Video Solution](#)

9. A binary number is made up to 8 digits. Suppose that the probability of an incorrect digit appearing is p and that the errors in different digits are independent of each other. Then find the probability of forming an incorrect number.



[Watch Video Solution](#)

10. The probability of India winning a test match against West Indies is $\frac{1}{2}$. Assuming independence from match to match, find the probability that in a match series Indias second win occurs at the third test.



[Watch Video Solution](#)

11. about to only mathematics



[View Text Solution](#)

12. A bag contains a white and b black balls. Two players, A and B alternately draw a ball from the bag, replacing the ball each time after the draw till one of them draws a white ball and wins the game. A begins the game. If the probability of A winning the game is three times that of B , then find the ratio $a : b$



[Watch Video Solution](#)

CONCEPT APPLICATION EXERCISE 14.4

1. An urn contains 5 red and 5 black balls. A ball is drawn at random, its colour is noted and is returned to the urn. Moreover, 2 additional balls of the colour drawn are put in the urn and then a ball is drawn at random. What is the probability that the second ball is red?



[Watch Video Solution](#)

2. A bag contains 3 white, 3 black and 2 red balls. One by one, three balls are drawn without replacing them. Find the probability that the third ball is red.



[Watch Video Solution](#)

3. Two thirds of the students in a class are boys and the rest girls. It is known that the probability of a girl getting a first class is 0.25 and that of a boy getting a first class is 0.28. Find the probability that a student chosen at random will get first class marks in the subject.



[Watch Video Solution](#)

4. A number is selected at random from the first 25 natural numbers. If it is a composite number, then it is divided by 6. But if it is not a composite

number, it is divided by 2. Find the probability that there will be no remainder in the division.

 [Watch Video Solution](#)

5. A real estate man has eight master keys to open several new homes. Only one master key will open any given house. If 40% of these homes are usually left unlocked, what is the probability that the real estate man can get into a specific home if he selects three master keys at random before leaving the office?

 [Watch Video Solution](#)

6. An urn contains m white and n black balls. A ball is drawn at random and is put back into the urn along with k balls of the same colour as that of the ball drawn. a ball is again drawn at random. Show that the probability of drawing a white ball now does not depend on k .

 [Watch Video Solution](#)

7. A box contains 12 red and 6 white balls. Balls are drawn from the bag one at a time without replacement. If in 6 draws, there are at least 4 white balls, find the probability that exactly one white ball is drawn in the next two draws. (Binomial coefficients can be left as such).



[Watch Video Solution](#)

CONCEPT APPLICATION EXERCISE 14.5

1. A card from a pack of 52 cards is lost. From the remaining cards of the pack; two cards are drawn and are found to be hearts. Find the probability of the missing card to be a heart.



[Watch Video Solution](#)

2. There are three coins, One is two headed coin, another is a biased coin that comes up head 75% of the time and third is an unbiased coin. One of

the three coins is chosen at random and tossed. If its shows head, what is the probability that it was the two headed coin?

 [Watch Video Solution](#)

3. Probability that A speaks truth is $\frac{4}{5}$. A coin is tossed. A reports that a head appears. The probability that actually there was head is (A) $\frac{4}{5}$ (B) $\frac{1}{2}$ (C) $\frac{1}{5}$ (D) $\frac{2}{5}$

 [Watch Video Solution](#)

4. A bag contains 5 balls. Two balls are drawn and are found to be white. What is the probability that all the balls are white?

 [Watch Video Solution](#)

5. The chance of defective screws in three boxes A, B, C are $\frac{1}{5}$, $\frac{1}{6}$, $\frac{1}{7}$, respectively. A box is selected at random and

a screw draw in from it at random is found to be defective. Then find the probability that it came from box A .



[Watch Video Solution](#)

6. Assume that the chances of a patient having a heart attack is 40%. It is also assumed that a meditation and yoga course reduce the risk of heart attack by 30% and prescription of certain drug reduces its chances by 25%. At a time a patient can choose any one of the two options with equal probabilities. It is given that after going through one of the two options the patient selected at random suffers a heart attack. Find the probability that the patient followed a course of meditation and yoga?



[Watch Video Solution](#)

7. The probability that a particular day in the month of July is a rainy day is $\frac{3}{4}$. Two person whose credibility and $\frac{4}{5}$ and $\frac{2}{3}$, respectively, claim that 15th July was a rainy day. Find the probability that it was really a rainy day.



[Watch Video Solution](#)

CONCEPT APPLICATION EXERCISE 14.6

1. A fair coin is tossed n times. If the probability that head occurs 6 times is equal to the probability that head occurs 8 times, then find the value of n .

 Watch Video Solution

2. A die is thrown 4 times. Find the probability of getting at most two 6's.

 Watch Video Solution

3. The probability that a student is not a swimmer is $\frac{1}{5}$. Then the probability that out of five students, four are swimmers is (A)

${}^5C_4 \left(\frac{4}{5}\right)^4 \frac{1}{5}$ (B) $\left(\frac{4}{5}\right)^4 \frac{1}{5}$ (C) ${}^5C_1 \frac{1}{5} \left(\frac{4}{5}\right)^4$ (D) None of these

 Watch Video Solution

[Watch Video Solution](#)

4. about to only mathematics

 [Watch Video Solution](#)

5. Numbers are selected at random, one at a time, from the two digit numbers 00,01,02...,99 with replacement. An event E occurs if the only product of the two digits of a selected number is 18. If four numbers are selected, find the probability that the event E occurs at least 3 times.

 [Watch Video Solution](#)

EXERCISE

1. A man has 3 pairs of black socks and 2 pair of brown socks kept together in a box. If he dressed hurriedly in the dark, the probability that

after he has put on a black sock, he will then put on another black sock is

1/3 b. 2/3 c. 3/5 d. 2/15

A. 1/3

B. 2/3

C. 3/5

D. 2/15

Answer: A



Watch Video Solution

2. There are 20 cards. Ten of these cards have the letter I printed on them and the other 10 have the letter I printed on them. If three cards picked up at random and kept in the same order, the probability of making word IIT is 1/9, 1/3 b. 1/16, 1/4 c. 1/4, 1/2 d. none of these

A. 4/27

B. 5/38

C. $1/8$

D. $9/80$

Answer: B



[Watch Video Solution](#)

3. One ticket is selected at random from 100 tickets numbered 00,01,02,...,98,99. If x_1 , and x_2 denotes the sum and product of the digits on the tickets, then $P(x_1 = 9/x_2 = 0)$ is equal to

A. $2/19$

B. $19/100$

C. $1/50$

D. none of these

Answer: A



[Watch Video Solution](#)

4. Let A and B be two events such that $P(A \cap B') = 0.20$, $P(A' \cap B) = 0.15$, $P(A' \cap B') = 0.1$, then $P(A/B)$ is equal to

A. $11/14$

B. $2/11$

C. $2/7$

D. $1/7$

Answer: A



[Watch Video Solution](#)

5. A father has 3 children with at least one boy. The probability that he has 2 boys and 1 girl is a. $1/4$ b. $1/3$ c. $2/3$ d. none of these

A. $1/4$

B. $1/3$

C. $2/3$

D. None of these

Answer: B



Watch Video Solution

6. In a certain town, 40% of the people have brown hair, 25% have brown eyes, and 15% have both brown hair and brown eyes. If a person selected at random from the town has brown hair, the probability that he also has brown eyes is $1/5$ b. $3/8$ c. $1/3$ d. $2/3$

A. $1/5$

B. $3/8$

C. $1/3$

D. $2/3$

Answer: B



[Watch Video Solution](#)

7. Let A and B are events of an experiment and

$P(A) = 1/4$, $P(A \cup B) = 1/2$, then value of $P(B/A^c)$ is

A. $2/3$

B. $1/3$

C. $5/6$

D. $1/2$

Answer: B



[Watch Video Solution](#)

8. The probability that an automobile will be stolen and found within one week is 0.0006. Then probability that an automobile will be stolen is

0.0015. the probability that a stolen automobile will be found in the week is 0. 3 b. 0. 4 c. 0. 5 d. 0. 6

A. 0.3

B. 0.4

C. 0.5

D. 0.6

Answer: B



[Watch Video Solution](#)

9. A pair of numbers is picked up randomly (without replacement) from the set $\{1,2,3,5,7,11,12,13,17,19\}$. The probability that the number 11 was picked given that the sum of the numbers was even is nearly 0. 1 b. 0. 125 c. 0. 24 d. 0. 18



[Watch Video Solution](#)

10. All the jacks, queens, kings, and aces of a regular 52 cards deck are taken out. The 16 cards are thoroughly shuffled and may opponent, a person who always tells the truth, simultaneously draws two cards at random and says, "I hold at least one ace". The probability that he holds two aces is (a) $\frac{2}{8}$ (b) $\frac{4}{9}$ (c) $\frac{2}{3}$ (d) $\frac{1}{9}$

A. $\frac{2}{8}$

B. $\frac{4}{9}$

C. $\frac{2}{3}$

D. $\frac{1}{9}$

Answer: D



Watch Video Solution

11. One ticket is selected at random from 100 tickets numbered 00, 01, 02, ..., 99. Suppose A and B are the sum and product of the digit found on the ticket, respectively. Then $P((A = 7) / (B = 0))$ is given by

A. $2/13$

B. $2/19$

C. $1/50$

D. None of these

Answer: B



Watch Video Solution

12. about to only mathematics

A. $1/2$

B. $7/18$

C. $3/4$

D. $5/12$

Answer: D



Watch Video Solution

13. Cards are drawn one-by-one at random from a well-shuffled pack of 52 playing cards until 2 aces are obtained from the first time. The probability that 18 draws are obtained for this is

A. $\frac{3}{34}$

B. $\frac{17}{455}$

C. $\frac{561}{15925}$

D. None of these

Answer: C



[Watch Video Solution](#)

14. A bag contains n white and n red balls. Pairs of balls are drawn without replacement until the bag is empty. Show that the probability that each pair consists of one white and one red ball is $\frac{2^n}{2^n C_n}$



[Watch Video Solution](#)

15. A six-faced dice is so biased that it is twice as likely to show an even number as an odd number when thrown. It is thrown twice, the probability that the sum of two numbers thrown is even is $\frac{1}{12}$ b. $\frac{1}{6}$ c. $\frac{1}{3}$ d. $\frac{5}{9}$

A. $\frac{1}{12}$

B. $\frac{1}{6}$

C. $\frac{1}{3}$

D. $\frac{5}{9}$

Answer: D



[Watch Video Solution](#)

16. about to only mathematics

A. $\frac{1}{2}$

B. 1

C. $\frac{3}{2}$

D. $\frac{3}{4}$

Answer: B



[Watch Video Solution](#)

17. A problem in mathematics is given to three students A, B, C and their respective probability of solving the problem is $\frac{1}{2}, \frac{1}{3}$ and $\frac{1}{4}$.

Probability that the problem is solved is $\frac{3}{4}$ b. $\frac{1}{2}$ c. $\frac{2}{3}$ d. $\frac{1}{3}$

A. $\frac{3}{4}$

B. $\frac{1}{2}$

C. $\frac{2}{3}$

D. $\frac{1}{3}$

Answer: A



Watch Video Solution

18. Let A, B, C be three mutually independent events. Consider the two statements S_1 and S_2 .

S_1 : A and $B \cup C$ are independent

S_2 : A and $B \cap C$ are independent. Then,

A. both S_1 and S_2 are true

B. only S_1 is true

C. only S_2 is true

D. neither S_1 nor S_2 is true

Answer: A



Watch Video Solution

19. Three ships $A, B,$ and C sail from England to India. If the ratio of their arriving safely are 2:5, 3:7, and 6:11, respectively, then the probability of all

the ships for arriving safely is 18/595 b. 6/17 c. 3/10 d. 2/7

A. 18/595

B. 6/17

C. 3/10

D. 2/7

Answer: A



Watch Video Solution

20. Cards are drawn one by one without replacement from a pack of 52 cards. The probability that 10 cards will precede the first ace is

A. A. 241/1456

B. B. 164/4168

C. C. 451/884

D. D. None of these

Answer: B



Watch Video Solution

21. Five horses are in a race. Mr. A selects two of the horses at random and bets on them. The probability that Mr. A selected the winning horse is $\frac{3}{5}$ b. $\frac{1}{5}$ c. $\frac{2}{5}$ d. $\frac{4}{5}$

A. $\frac{3}{5}$

B. $\frac{1}{5}$

C. $\frac{2}{5}$

D. $\frac{4}{5}$

Answer: C



Watch Video Solution

22. Let A and B be two events such that $p(\overline{A \cup B}) = \frac{1}{6}$, $p(A \cap B) = \frac{1}{4}$ and $p(\overline{A}) = \frac{1}{4}$, where \overline{A} stands for the complement of the event A.

Then the events A and B are (1) mutually exclusive and independent (2) equally likely but not independent (3) independent but not equally likely (4) independent and equally likely

- A. equally likely but not independent equally likely and mutually exclusive
- B. equally like and mutually exclusive
- C. Mutually exclusive and independent
- D. independent but not equally likely

Answer: D



Watch Video Solution

23. A class consists of 80 students, 25 of them are girls and 55 are boys. If 10 of them are rich and the remaining are poor and also 20 of them are

intelligent, then the probability of selecting an intelligent rich girls is a.

5 / 128 b. 25 / 128 c. 5 / 512 d. none of these

A. 5 / 128

B. 25 / 128

C. 5 / 512

D. None of these

Answer: C



Watch Video Solution

24. Events A and C are independent. If the probabilities relating A , B , and C are

$$P(A) = 1/5, P(B) = 1/6; P(A \cap C) = 1/20; P(B \cup C) = 3/8.$$

Then events B and C are independent events B and C are mutually exclusive events B and C are neither independent nor mutually exclusive events B and C are equiprobable

A. events B and C are independent

B. events B and C are mutually exclusive

C. events B and C are neither independent nor mutually exclusive

D. events B and C are equiprobable

Answer: A



Watch Video Solution

25. Let A and B be two events. Suppose $P(A) = 0.4$, $P(B) = p$, and $P(A \cup B) = 0.7$. The value of p for which A and B are independent is $1/3$ b. $1/4$ c. $1/2$ d. $1/5$

A. $1/3$

B. $1/4$

C. $1/2$

D. $1/5$

Answer: C



[Watch Video Solution](#)

26. Balls are drawn one-by-one without replacement from a box containing 2 black, 4 white and 3 red balls till all the balls are drawn. Find the probability that the balls drawn are in the order 2 black, 4 white and 3 red.

A. $1/1260$

B. $1/7560$

C. $1/126$

D. None of these

Answer: A



[Watch Video Solution](#)

27. If any four numbers are selected and they are multiplied, then the probability that the last digit will be 1, 3, 5 or 7 is

A. $\frac{4}{625}$

B. $\frac{18}{625}$

C. $\frac{16}{625}$

D. None of these

Answer: C



[Watch Video Solution](#)

28. If odds against solving a question by three students are 2:1, 5:2, and 5:3, respectively, then probability that the question is solved only by one student is

A. $\frac{31}{56}$

B. $\frac{24}{56}$

C. $\frac{23}{56}$

D. None of these

Answer: C



Watch Video Solution

29. An unbiased coin is tossed 6 times. The probability that third head appears on the sixth trial is $\frac{5}{16}$ b. $\frac{5}{32}$ c. $\frac{5}{8}$ d. $\frac{5}{64}$

A. $\frac{5}{16}$

B. $\frac{2}{32}$

C. $\frac{5}{8}$

D. $\frac{5}{64}$

Answer: B



Watch Video Solution

30. A coin is tossed 7 times. Then the probability that at least 4 consecutive heads appear is $\frac{3}{16}$ b. $\frac{5}{32}$ c. $\frac{3}{16}$ d. $\frac{1}{8}$

A. $\frac{3}{16}$

B. $\frac{5}{32}$

C. $\frac{3}{16}$

D. $\frac{1}{8}$

Answer: B



[Watch Video Solution](#)

31. Three critics review a book. Odds in favour of the book are 5:2, 4:3 and 3:4 respectively for three critics. Find the probability that the majority are in favour of the book.

A. $\frac{35}{49}$

B. $\frac{125}{343}$

C. $164/343$

D. $209/343$

Answer: D



[Watch Video Solution](#)

32. *A* and *B* play a game of tennis. The situation of the game is as follows: if one scores two consecutive points after a deuce, he wins; if loss of a point is followed by win of a point, it is deuce. The chance of a server to win a point is $2/3$. The game is a deuce and *A* is serving. Probability that *A* will win the match is (serves are change after each game) $3/5$ b. $2/5$ c. $1/2$ d. $4/5$

A. $3/5$

B. $2/5$

C. $1/2$

D. $4/5$

Answer: C



[Watch Video Solution](#)

33. An unbiased cubic die marked with 1, 2, 2, 3, 3, 3 is rolled 3 times. The probability of getting a total score of 4 or 6 is

A. $16/216$

B. $50/216$

C. $60/216$

D. None of these

Answer: B



[Watch Video Solution](#)

34. A fair die is tossed repeatedly. A wins if it is 1 or 2 on two consecutive tosses and B wins if it is 3, 4, 5 or 6 on two consecutive tosses. The

- probability that A wins if the die is tossed indefinitely is $1/3$ b. $5/21$ c. $1/4$ d. $2/5$
- A. $1/3$
 - B. $5/21$
 - C. $1/4$
 - D. $2/5$

Answer: B



[Watch Video Solution](#)

35. Whenever horses a, b, c race together, their respective probabilities of winning the race are $0.3, 0.5,$ and $0.2,$ respectively. If they race three times, the probability that the same horse wins all the three races, and the probability that a, b, c each wins one race are, respectively

- A. $8/50, 9/50$
- B. $16/100, 3/100$

C. $12/50$, $15/50$

D. $10/50$, $8/50$

Answer: A



[Watch Video Solution](#)

36. A man alternately tosses a coin and throws a die beginning with the coin. The probability that he gets a head in the coin before he gets a 5 or 6 in the dice is $3/4$ b. $1/2$ c. $1/3$ d. none of these

A. $3/4$

B. $1/2$

C. $1/3$

D. None of these

Answer: A



[Watch Video Solution](#)

37. If p is the probability that a man aged x will die in a year, then the probability that out of n men A_1, A_2, A_n each aged x , A_1 will die in an year and be the first to die is $1 - (1 - p)^n$ b. $(1 - p)^n$ c. $1/n[1 - (1 - p)^n]$ d. $1/n(1 - p)^n$

A. $1 - (1 - p)^n$

B. $(1 - p)^n$

C. $1/n[1 - (1 - p)^n]$

D. $1/n(1 - p)^n$

Answer: C



Watch Video Solution

38. Thirty two players ranked 1 to 32 are playing is a knockout tournament. Assume that in every match between any two players, the better ranked player wins the probability that ranked 1 and ranked 2

players are winner and runner up, respectively, is $\frac{16}{31}$ b. $\frac{1}{2}$ c. $\frac{17}{31}$ d.

none of these

A. $\frac{16}{31}$

B. $\frac{1}{2}$

C. $\frac{17}{31}$

D. None of these

Answer: A



Watch Video Solution

39. A pair of unbiased dice are rolled together till a sum of either 5 or 7 is obtained. Then find the probability that 5 comes before 7.

A. $\frac{2}{5}$

B. $\frac{3}{5}$

C. $\frac{4}{5}$

D. None of these

Answer: A



[Watch Video Solution](#)

40. A fair coin is tossed 10 times. Then the probability that two heads do not occur consecutively is $\frac{7}{64}$ b. $\frac{1}{8}$ c. $\frac{9}{16}$ d. $\frac{9}{64}$

A. $\frac{7}{64}$

B. $\frac{1}{8}$

C. $\frac{9}{16}$

D. $\frac{9}{64}$

Answer: D



[Watch Video Solution](#)

41. A die is thrown a fixed number of times. If probability of getting even number 3 times is same as the probability of getting even number 4 times, then probability of getting even number exactly once is $1/6$ b. $1/9$ c. $5/36$ d. $7/128$

A. $1/6$

B. $1/9$

C. $5/36$

D. $7/128$

Answer: D



Watch Video Solution

42. A pair of fair dice is thrown independently three times. The probability of getting a score of exactly 9 twice is (1) $1/729$ (2) $8/9$ (3) $8/729$ (4) $8/243$

A. $8/9$

B. $7/29$

C. $8/243$

D. $1/729$

Answer: C



Watch Video Solution

43. The probability that a bulb produced by a factory will fuse after 150 days if used is 0.50. what is the probability that our of 5 such bulbs none will fuse after 150 days of use? $1 - (19/20)^5$ b. $(19/20)^5$ c. $(3/4)^5$ d. $90(1/4)^5$

A. $1 - (19/20)^5$

B. $(19/20)^5$

C. $(3/4)^5$

D. $90(1/4)^5$

Answer: B



Watch Video Solution

44. The box contains tickets numbered from 1 to 20. Three tickets are drawn from the box with replacement. The probability that the largest number on the tickets is 7 is a. $\frac{2}{19}$ b. $\frac{7}{20}$ c. $1 - (\frac{7}{20})^3$ d. none of these



Watch Video Solution

45. Two players toss 4 coins each. The probability that they both obtain the same number of heads is a. $\frac{5}{256}$ b. $\frac{1}{16}$ c. $\frac{35}{128}$ d. none of these

A. $\frac{5}{256}$

B. $\frac{1}{16}$

C. $\frac{35}{128}$

D. None of these

Answer: C



Watch Video Solution

46. A coin is tossed $2n$ times. The chance that the number of times one gets head is not equal to the number of times one gets tails is

$\frac{(2n!)}{(n!)^2} \left(\frac{1}{2}\right)^{2n}$ b. $1 - \frac{(2n!)}{(n!)^2}$ c. $1 - \frac{(2n!)}{(n!)^2} \frac{1}{4^n}$ d. none of these

A. $\frac{(2n!)}{(n!)^2} \left(\frac{1}{2}\right)^{2n}$

B. $1 - \frac{(2n!)}{(n!)^2}$

C. $1 - \frac{(2n!)}{(n!)^2} \frac{1}{4^n}$

D. None of these

Answer: C



Watch Video Solution

47. A box contains 24 identical balls of which 12 are white and 12 are black. The balls are drawn at random from the box one at a time with replacement. The probability that a white ball is drawn for the 4th time on the 7th draw is $\frac{5}{64}$ b. $\frac{27}{32}$ c. $\frac{5}{32}$ d. $\frac{1}{2}$

A. $\frac{5}{64}$

B. $\frac{27}{32}$

C. $\frac{5}{32}$

D. $\frac{1}{2}$

Answer: C



Watch Video Solution

48. In a game a coin is tossed $2n + m$ times and a player wins if he does not get any two consecutive outcomes same for at least $2n$ times in a row. The probability that player wins the game is a. $\frac{m + 2}{2^{2n} + 1}$ b. $\frac{2n + 2}{2^{2n}}$ c. $\frac{2n + 2}{2^{2n+1}}$ d. $\frac{m + 2}{2^{2n}}$

A. $\frac{m + 2}{2^{2n} + 1}$

B. $\frac{2n + 2}{2^{2n}}$

C. $\frac{2n + 2}{2^{2n+1}}$

D. $\frac{m + 2}{2^{2n}}$

Answer: D



Watch Video Solution

49. A and B toss a fair coin each simultaneously 50 times. The probability that both of them will not get tail at the same toss is

A. $1/9$

B. $3/16$

C. $5/16$

D. $3/8$

Answer: C

 [Watch Video Solution](#)

50. A fair coin is tossed 100 times. The probability of getting tails 1, 3, ..., 49 times is $\frac{1}{2}$ b. $\frac{1}{4}$ c. $\frac{1}{8}$ d. $\frac{1}{16}$

A. $\frac{1}{2}$

B. $\frac{1}{4}$

C. $\frac{1}{8}$

D. $\frac{1}{16}$

Answer: B

 [Watch Video Solution](#)

51. A fair die is thrown 20 times. The probability that on the 10th throw, the fourth six appears is

a. $\frac{{}^{20}C_{10} \times 5^6}{6^{20}}$

b. $\frac{120 \times 5^7}{6^{10}}$

c. $\frac{84 \times 5^6}{6^{10}}$

d. none of these

A. ${}^{20}C_{10} \times 5^6 / 6^{20}$

B. $120 \times 5^7 / 6^{10}$

C. $84 \times 5^6 / 6^{10}$

D. None of these

Answer: C



Watch Video Solution

52. A speaks truth in 605 cases and B speaks truth in 70% cases. The probability that they will say the same thing while describing a single event is $\frac{2}{19}$ b. $\frac{3}{29}$ c. $\frac{17}{19}$ d. $\frac{4}{29}$

A. 0.56

B. 0.54

C. 0.38

D. 0.94

Answer: B



[Watch Video Solution](#)

53. The probability that a teacher will give an unannounced test during any class meeting is $\frac{1}{5}$. If a student is absent twice, find the probability that the student will miss at least one test.

A. $\frac{4}{5}$

B. $\frac{2}{5}$

C. $\frac{7}{25}$

D. $\frac{9}{25}$

Answer: D



[Watch Video Solution](#)

54. There are two urns A and B . Urn A contains 5 red, 3 blue and 2 white balls, urn B contains 4 red, 3 blue, and 3 white balls. An urn is chosen at random and a ball is drawn. Probability that the ball drawn is red is a. $9/10$ b. $1/2$ c. $11/20$ d. $9/20$

A. $9/10$

B. $1/2$

C. $11/20$

D. $9/20$

Answer: D



[Watch Video Solution](#)

55. A bag contains 20 coins. If the probability that the bag contains exactly 4 biased coin is $3/4$ and that of exactly 5 biased coin is $2/3$, then the probability that all the biased coin are sorted out from bag is exactly

10 draws is $\frac{5}{10} \frac{{}^{16}C_6}{{}^{20}C_9} + \frac{1}{11} \frac{{}^{15}C_5}{{}^{20}C_9}$ b. $\frac{2}{33} \left[\frac{{}^{16}C_6 + 5^{15}C_5}{{}^{20}C_9} \right]$

c. $\frac{5}{33} \frac{{}^{16}C_7}{{}^{20}C_9} + \frac{1}{11} \frac{{}^{15}C_6}{{}^{20}C_9}$ d. none of these

A. $\frac{5}{10} \frac{{}^{16}C_6}{{}^{20}C_9} + \frac{1}{11} \frac{{}^{15}C_5}{{}^{20}C_9}$

B.

C. $\frac{5}{33} \frac{{}^{16}C_7}{{}^{20}C_9} + \frac{1}{11} \frac{{}^{15}C_6}{{}^{20}C_9}$

D. None of these

Answer: B



Watch Video Solution

56. A bag contains 3 red and 3 green balls and a person draws out 3 at random. He then drops 3 blue balls into the bag and again draws out 3 at random. The chance that the 3 later balls being all of different colors is 15 % b. 20 % c. 27 % d. 40 %

A. 15 %

B. 20 %

C. 27 %

D. 40 %

Answer: C



Watch Video Solution

57. A bag contains 20 coins. If the probability that the bag contains exactly 4 biased coin is $\frac{1}{3}$ and that of exactly 5 biased coin is $\frac{2}{3}$, then the probability that all the biased coin are sorted out from bag is exactly 10 draws is

a. $\frac{5}{10} \frac{{}^{.16}C_6}{{}^{.20}C_9} + \frac{1}{11} \frac{{}^{.15}C_5}{{}^{.20}C_9}$

b. $\frac{2}{33} \left[\frac{{}^{.16}C_6 + 5 \cdot {}^{.15}C_5}{{}^{.20}C_9} \right]$

c. $\frac{5}{33} \frac{{}^{.16}C_7}{{}^{.20}C_9} + \frac{1}{11} \frac{{}^{.15}C_6}{{}^{.20}C_9}$

d. none of these

A. $\frac{5}{33} \frac{{}^{16}C_6}{{}^{20}C_9} + \frac{1}{11} \frac{{}^{15}C_5}{{}^{20}C_9}$

B. $\frac{2}{33} \left[\frac{{}^{16}C_6 + 5^{15}C_5}{{}^{20}C_6} \right]$

C. $\frac{5}{33} \frac{{}^{16}C_7}{{}^{20}C_9} + \frac{1}{11} \frac{{}^{15}C_6}{{}^{20}C_9}$

D. None of these

Answer: C



Watch Video Solution

58. An urn contains 3 red balls and n white balls. Mr. A draws two balls together from the urn. The probability that they have the same color is $1/2$. Mr. B. Draws one balls form the urn, notes its color and replaces it. He then draws a second ball from the urn and finds that both balls have the same color is $5/8$. The possible value of n is (a)9 b. 6 c. 5 d. 1

A. 9

B. 6

C. 5

D. 1

Answer: D



Watch Video Solution

59. A student can solve 2 out of 4 problems of mathematics, 3 out of 5 problem of physics, and 4 out of 5 problems of chemistry. There are equal number of books of math, physics, and chemistry in his shelf. He selects one book randomly and attempts 10 problems from it. If he solves the first problem, then the probability that he will be able to solve the second problem is $\frac{2}{3}$ b. $\frac{25}{38}$ c. $\frac{13}{21}$ d. $\frac{14}{23}$

A. $\frac{2}{3}$

B. $\frac{25}{38}$

C. $\frac{13}{21}$

D. $\frac{14}{23}$

Answer: B



Watch Video Solution

60. An event X can take place in conjunction with any one of the mutually exclusive and exhaustive events A, B and C . If A, B, C are equiprobable and the probability of X is $5/12$, and the probability of X taking place when A has happened is $3/8$, while it is $1/4$ when B has taken place, then the probability of X taking place in conjunction with C is a. $5/8$ b. $3/8$ c. $5/24$ d. none of these



[Watch Video Solution](#)

61. An artillery target may be either at point I with probability $8/9$ or at point II with probability $1/9$ we have 55 shells, each of which can be fired either at point I or II. Each shell may hit the target, independent of the other shells, with probability $1/2$. Maximum number of shells must be fired at point I to have maximum probability is 20 b. 25 c. 29 d. 35

A. 20

B. 25

C. 29

D. 35

Answer: C



[Watch Video Solution](#)

62. A bag contains some white and some black balls, all combinations of balls being equally likely. The total number of balls in the bag is 10. If three balls are drawn at random without replacement and all of them are found to be black, the probability that the bag contains 1 white and 9 black balls is

A. $14/55$

B. $15/55$

C. $2/11$

D. $8/55$

Answer: A



[Watch Video Solution](#)

63. A letter is known to have come either from LONDON or CLIFTON. On the envelope just two consecutive letters ON are visible. What is the probability that the letter has come from (i) LONDON (ii) CLIFTON?

A. $1/7$

B. $12/17$

C. $17/30$

D. $3/5$

Answer: B



[Watch Video Solution](#)

64. A doctor is called to see a sick child. The doctor knows (prior to the visit) that 90% of the sick children in that neighbourhood are sick with the flu, denoted by F , while 10% are sick with the measles, denoted by

M . A well-known symptom of measles is a rash, denoted by R . The probability having a rash for a child sick with the measles is 0.95. however, occasionally children with the flu also develop a rash, with conditional probability 0.08. upon examination the child, the doctor finds a rash. The what is the probability that the child has the measles? 91 / 165 b. 90 / 163 c. 82 / 161 d. 95 / 167

A. 91 / 165

B. 90 / 163

C. 82 / 161

D. 95 / 167

Answer: D



Watch Video Solution

65. On a Saturday night, 20% of all drivers in U.S.A. are under the influence of alcohol. The probability that a drive under the influence of alcohol will have an accident is 0.001. The probability that a sober drive will have an

accident is 0.00. if a car on a Saturday night smashed into a tree, the probability that the driver was under the influence of alcohol is $\frac{3}{7}$ b. $\frac{4}{7}$ c. $\frac{5}{7}$ d. $\frac{6}{7}$

A. $\frac{3}{7}$

B. $\frac{4}{7}$

C. $\frac{5}{7}$

D. $\frac{6}{7}$

Answer: C



Watch Video Solution

66. A purse contains 2 six-sided dice. One is normal fair die, while the other has two 1's, two 3's and two 5's. A die is picked up and rolled. Because of some secret magnetic attraction of the unfair die, there is 75 % chance of picking the unfair die and a 25 % chance of picking a fair die. The die is rolled and shows up the face 3. The probability that a fair die was picked up is

A. A. $1/7$

B. B. $1/4$

C. C. $1/6$

D. D. $1/24$

Answer: A



Watch Video Solution

67. There are 3 bags which are known to contain 2 white and 3 black, 4 white and 1 black, and 3 white and 7 black ball, respectively. A ball is drawn at random from one of the bags and found to be the black ball. Then the probability that it was drawn from the bag containing the most black ball is $7/15$ b. $5/19$ c. $3/4$ d. none of these

A. $7/15$

B. $5/19$

C. $3/4$

D. None of these

Answer: A



[Watch Video Solution](#)

68. A hat contains a number of cards with 30% white on both sides, 50% black on one side and white on the other side, 20% black on both sides. The cards are mixed up, and a single card is drawn at random and placed on the table. Its upper side shows up black. The probability that its other side is also black is

A. $2/9$

B. $4/9$

C. $2/3$

D. $2/7$

Answer: B



[Watch Video Solution](#)

MULTIPLE CHOICE ANSWER TYPE

1. If A and B are two independent events such that $P(A) = 1/2$, $P(B) = 1/5$, then find $P(A \cup B)$ and $P(A|B)$

A. $P(A \cup B) = 3/5$

B. $P(A | B) = 1/4$

C. $P(A / A \cup B) = 5/6$

D. $P(A \cap B | \bar{A} \cup \bar{B}) = 0$

Answer: A::C::D



[Watch Video Solution](#)

2. Let A and B be two events such that

$P(A \cap B') = 0.20$, $P(A' \cap B) = 0.15$, $P(A' \cap B') = 0.1$, then $P(A/B)$

is equal to

A. $P(A | B) = 2/7$

B. $P(A | B) = 2/7$

C. $P(A \cup B) = 0.55$

D. $P(A | B) = 1/2$

Answer: A::B::C



Watch Video Solution

3. The probability that a married man watches certain TV show is 0.4 and the probability that a married woman watches the show is 0.5. The probability that a man watches the show, given that his wife does, is 0.7.

Then

A. the probability that married couple watches the show is 0.35

B. the probability that a wife watches the show given that her husband does is $7/8$

C. the probability that at least one person of a married couple will watch the show is 0.55

D. None of these

Answer: A::B::C



Watch Video Solution

4. A and B are two events defined as follows:

A: It rains today with $P(A) = 40\%$

B: It rains tomorrow with $P(B) = 50\%$

Also, $P(\text{it rains today and tomorrow}) = 30\%$

Also, $E_1: P(A \cap B) / (A \cup B)$ and

$E_2: P(\{(A \cap \bar{B}) \text{ or } (B \cap \bar{A})\} / (A \cup B))$. Then which of the following

is/are true ?

(a) A and B are independent events

(b) $P(A/B) < P(B/A)$

(c) E_1 and E_2 are equiprobable

$$(d) P\left(\frac{A}{A \cup B}\right) = P(B/(A \cup B))$$

A. $P(A/B) < P(B/A)$

B. $P(A/B) < P(B/A)$

C. E_1 and E_2 are equiprobable

D. $P(A/(A \cup B)) = P(B/(A \cup B))$

Answer: B::C



Watch Video Solution

5. Two whole numbers are randomly selected and multiplied. Consider two events E_1 and E_2 defined as E_1 : Their product is divisible by 5 and E_2 Unit's place in their product is 5 Which of the following statement(s) is/are correct?

A. E_1 is twice as likely to occur as E_2

B. E_1 and E_2 are disjoint

C. $P(E_2 / E^1) = 1/4$

D. $P(E_1 / E_2) = 1$

Answer: C::D



Watch Video Solution

6. The probability that a 50-years-old man will be alive at 60 is 0.83 and the probability that a 45-years-old women will be alive at 55 is 0.87. Then

(a). Probability both the person are alive

(b). Probability at least a person is alive

A. the probability that both will be alive is 0.7221

B. at least one of them will alive is 0.9779

C. at least one of them will alive is 0.8230

D. the probability that both will be alive is 0.6320

Answer: A::B



Watch Video Solution

7. Which of the following statement is/are correct?

A. Three coins are tossed once. At least two of them must land the same way. No matter whether they land heads or tails, the third coin is equally likely to land either the same ways or oppositely. So, the chance that all the three coins land the same ways is $1/2$.

B. Let $0 < P(B) < 1$ and $P(A | B) = P(A/B^C)$. Then A and B are independent.

C. Suppose an urn contains "w" white and "b" black balls and a ball is drawn from it and is replaced along with "d" additional balls of the same color. Now a second ball is drawn from it. The probability that the second drawn ball is white is independent of the value of "d"

D. A,B,C simultaneously satisfy

$$P(ABC) = P(A)P(B)P(C)$$

$$P(ABC\bar{C}) = P(A)P(B)P(\bar{C})$$

$$P(A\bar{B}C) = P(A)P(\bar{B})P(C)$$

$$P(A - BC) = P(\bar{A})P(B)P(C)$$

Then A, B C are independent.

Answer: B::C::D

 [Watch Video Solution](#)

8. A bag initially contains 1 red and 2 blue balls. An experiment consisting of selecting a ball at random, noting its color and replacing it together with an additional ball of the same color. If three such trials are made, then (A) Probability that at least one blue ball is drawn is 0.9 (B) Probability that exactly one blue ball is drawn is 0.2 (C) Probability that all the drawn balls are red given that all the drawn balls are of same color is 0.2 (D) Probability that at least one red ball is drawn is 0.6

A. probability that at least one blue balls is drawn is 0.9

B. probability that exactly one blue ball is drawn is 0.2

C. probability that all the drawn balls are red given that all the drawn balls are of same color is 0.2

D. probability that at least one red ball is drawn is 0.6

Answer: A::B::C::D



Watch Video Solution

9. $P(A) = 3/8$; $P(B) = 1/2$; $P(A \cup B) = 5/8$, which of the following do/does hold good? a. $P(A^c / B) = 2P(A / B^c)$ b. $P(B) = 2P(A / B^c)$ c. $15P(A^c / B^c) = 8P(B / A^c)$ d. $P(A / B^c) = (A \cap B)$

A. $P(A^C / B) = 2P(A / B^C)$

B. $P(B) = P(A / B)$

C. $15P(A^C / B^C) = 8P(B / A^C)$

D. $P(A / B^C) = (A \cap B)$

Answer: A::B::C::D



Watch Video Solution

10. In a precision bombing attack, there is a 50% chance that any one bomb will strike the target. Two direct hits are required to destroy the target completely. The number of bombs which should be dropped to give a 99% chance or better of completely destroying the target can be

12 b. 11 c. 10 d. 13

A. 12

B. 11

C. 10

D. 13

Answer: A::B::D



Watch Video Solution

11. If A and B are two events, then which one of the following is/are always true?

A. $P(A \cap B) \geq P(A) + P(B) - 1$

B. $P(A \cap B) \leq P(A)$

C. $P(A' \cap B') \geq P(A') + P(B') - 1$

D. $P(A \cap B) = P(A)P(B)$

Answer: A::B::C



Watch Video Solution

12. If A and B are two independent events such that $P(A) = 1/2$ and $P(B) = 1/5$, then

A. $P(A/B) = 1/2$

B. $P\left(\frac{A}{A \cup B}\right) = \frac{5}{6}$

C. $P\left(\frac{A \cap B}{A' \cup B'}\right) = 0$

D. None of these

Answer: A::B::C



Watch Video Solution

13. If A and B are two independent events such that $P(\bar{A} \cap B) = 2/15$ and $P(A \cap \bar{B}) = 1/6$, then $P(B)$ is

A. $1/5$

B. $1/6$

C. $4/5$

D. $5/6$

Answer: B::C



Watch Video Solution

14. about to only mathematics

A. probability that neither bus will be late on a particular date is $7/10$

B. probability that bus A is late given that bus B is late is $18/28$

C. `

D.

Answer: A::B::C



[Watch Video Solution](#)

15. A fair coin is tossed 99 times. Let X be the number of times head occurs. The $P(X=r)$ maximum when r is

A. 49

B. 52

C. 51

D. 50

Answer: A::D



Watch Video Solution

16. If the probability of choosing an integer k out of $2m$ integers $1, 2, 3, \dots, 2m$ is inversely proportional of k^4 ($1 \leq k \leq m$). If x_1 is the probability that chosen number is odd and x_2 is the probability that chosen number is even, then $x_1 > 1/2$ b. $x_1 > 2/3$ c. $x_2 < 1/2$ d. $x_2 < 2/3$

A. $x_1 > 1/2$

B. $x_1 > 2/3$

C. $x_2 < 1/2$

D. $x_2 < 2/3$

Answer: A::C



Watch Video Solution

17. A lot contains 50 defective and 50 non-defective bulbs. Two bulbs are drawn at random one at a time with replacement. The events A, B and C are defined as the first bulb is defective, the second bulb is non-defective, the two bulbs are both defective or non-defective, respectively. Then,

- A. A and B are independent
- B. B and C are independent
- C. A and C are independent
- D. A,B and C are pairwise independent

Answer: A::B::C



[Watch Video Solution](#)

LINKED COMPREHENSION TYPE

1. In a class of 10 student, probability of exactly i students passing an examination is directly proportional to i^2 . Then answer the following

questions:

If a student selected at random is found to have passed the examination, then the probability that he was the only student who has passed the examination is

A. $1/11$

B. $5/77$

C. $25/77$

D. $10/77$

Answer: B



[Watch Video Solution](#)

2. In a class of 10 students, probability of exactly i students passing an examination is directly proportional to i^2 . Then answer the following questions:

If a student selected at random is found to have passed the

examination, then the probability that he was the only student who has passed the examination is

A. (a) $1/7$

B. (b) $11/35$

C. (c) $11/14$

D. (d) None of these

Answer: C



Watch Video Solution

3. In a class of 10 student, probability of exactly i students passing an examination is directly proportional to i^2 . Then answer the following questions:

If a students selected at random is found to have passed the examination, then the probability that he was the only student who has passed the examination is

A. $1/3025$

B. $1/605$

C. $1/275$

D. $1/121$

Answer: A

 [Watch Video Solution](#)

4. In an objective paper, there are two sections of 10 questions each. For "section 1", each question has 5 options and only one option is correct and "section 2" has 4 options with multiple answers and marks for a question in this section is awarded only if he ticks all correct answers. Marks for each question in "section 1" is 1 and in "section 2" is 3. (There is no negative marking.) If a candidate attempts only two questions by guessing, one from "section 1" and one from "section 2", the probability that he scores in both questions is

A. $74/75$

B. B. 1/25

C. C. 1/15

D. D. 1/75

Answer: D



Watch Video Solution

5. In an objective paper, there are two sections of 10 questions each. For "section 1", each question has 5 options and only one option is correct and "section 2" has 4 options with multiple answers and marks for a question in this section is awarded only if he ticks all correct answers. Marks for each question in "section 1" is 1 and in "section 2" is 3. (There is no negative marking.) If a candidate attempts only two questions by guessing, one from "section 1" and one from "section 2", the probability that he scores in both questions is

A. $\frac{1}{5} \left(\frac{1}{15}\right)^3$

B. $\frac{4}{5} \left(\frac{1}{15}\right)^3$

C. $\frac{1}{5}\left(\frac{14}{15}\right)^3$

D. None of these

Answer: D



Watch Video Solution

6. In an objective paper, there are two sections of 10 questions each. For "section 1", each question has 5 options and only one option is correct and "section 2" has 4 options with multiple answers and marks for a question in this section is awarded only if he ticks all correct answers. Marks for each question in "section 1" is 1 and in "section 2" is 3. (There is no negative marking.) If a candidate attempts only two questions by guessing, one from "section 1" and one from "section 2", the probability that he scores in both questions is

A. $\left(\frac{1}{75}\right)^{10}$

B. $1 - \left(\frac{1}{75}\right)^{10}$

C. $\left(\frac{74}{75}\right)^{10}$

D. None of these

Answer: B



[Watch Video Solution](#)

7. A JEE aspirant estimates that she will be successful with an 80 % chance if she studies 10 hours per day, with a 60 % chance if she studies 7 hours per day and with 40 % chance if she studies 4 hours per day. She further believes that she will study 10 hours, 7 hours and 4 hours per day with probabilities 0.1, 0.2 and 0.7 respectively. The chance she will be successful is: A. 0.28 B. 0.38 C. 0.48 D. 0.58



[Watch Video Solution](#)

8. A JEE aspirant estimates that she will be successful with an 80 % chance if she studies 10 hours per day, with 60 % chance if she studies 7 hours per day, and with a 40 % chance if she studies 4 hours per day. She further believes that she will study 10 hours, 7 hours, and 4 hours

per day with probabilities 0.1, 0.2 and 0.7, respectively.

The chance she will be successful if she studies for 4hours is

A. $6/12$

B. $7/12$

C. $8/12$

D. $9/12$

Answer: B



Watch Video Solution

9. A JEE aspirant estimates that she will be successful with an 80 % chance if she studies 10 hours per day, with 60 % chance if she studies 7 hours per day, and with a 40 % chance if she studies 4 hours per day. She further believes that she will study 10 hours, 7 hours, and 4 hours per day with probabilities 0.1, 0.2 and 0.7, respectively.

The chance she will not be successful if she studies for 4hours is

A. 18 / 26

B. 19 / 26

C. 20 / 26

D. 21 / 26

Answer: D



[Watch Video Solution](#)

10. Let S and T are two events defined on a sample space with probabilities

$$P(S) = 0.5, P(T) = 0.69, P(S/T) = 0.5$$

Events S and T are

A. mutually exclusive

B. independent

C. Mutually exclusive and independent

D. neither mutually exclusive nor independent

Answer: B



[Watch Video Solution](#)

11. Let S and T are two events defined on a sample space with probabilities

$$P(S) = 0.5, P(T) = 0.69, P(S/T) = 0.5$$

The value of P(S and T) is

A. 0.3450

B. 0.2500

C. 0.6900

D. 0.350

Answer: A



[Watch Video Solution](#)

12. Let S and T are two events defined on a sample space with probabilities

$$P(S) = 0.5, P(T) = 0.69, P(S/T) = 0.5$$

The value of $P(S \text{ or } T)$ is

A. 0.6900

B. 1.19

C. 0.8450

D. 0

Answer: C



[Watch Video Solution](#)

13. An amoeba either splits into two or remains the same or eventually dies out immediately after completion of every second with probabilities, respectively, $1/2$, $1/4$ and $1/4$. Let the initial amoeba be called as mother amoeba and after every second, the amoeba, if it is distinct from the

previous one, be called as 2nd, 3rd,...generations.

The probability that after 2 s all the amoeba population dies out is

A. $9/32$

B. $11/32$

C. $1/2$

D. $3/32$

Answer: D



Watch Video Solution

14. An amoeba either splits into two or remains the same or eventually dies out immediately after completion of every second with probabilities, respectively, $1/2$, $1/4$ and $1/4$. Let the initial amoeba be called as mother amoeba and after every second, the amoeba, if it is distinct from the previous one, be called as 2nd, 3rd,...generations.

The probability that after 2 s exactly 4 amoeba are alive is

A. $1/16$

B. $1/8$

C. $3/4$

D. $1/2$

Answer: B



[Watch Video Solution](#)

15. An amoeba either splits into two or remains the same or eventually dies out immediately after completion of every second with probabilities, respectively, $1/2$, $1/4$ and $1/4$. Let the initial amoeba be called as mother amoeba and after every second, the amoeba, if it is distinct from the previous one, be called as 2nd, 3rd,...generations.

The probability that amoeba population will be maximum after completion of 3 s is

A. $1/2^7$

B. $1/2^6$

C. $1/2^8$

D. None of these

Answer: A



Watch Video Solution

16. Two fair dice are rolled. Let $P(A_i) > 0$ denote the event that the sum of the faces of the dice is divisible by i .

Which one of the following events is most probable?

A. A_3

B. A_4

C. A_5

D. A_6

Answer: A



[Watch Video Solution](#)

17. Two fair dice are rolled. Let $P(A_i) > 0$ denote the event that the sum of the faces of the dice is divisible by i .

Which one of the following events is most probable?

A. (3, 4)

B. (4, 6)

C. (2, 3)

D. (4, 2)

Answer: C



[Watch Video Solution](#)

18. Two fair dice are rolled. Let $P(A_i) > 0$ denote the event that the sum of the faces of the dice is divisible by i .

The number of all possible ordered pair (i,j) for which the events

A_i and a_j are independent is

A. 6

B. 12

C. 13

D. 25

Answer: D



Watch Video Solution

19. A player tosses a coin and score one point for every head and two points for every tail that turns up. He plays on until his score reaches or passes n . P_n denotes the probability of getting a score of exactly n .

The value of $P(n)$ is equal to

A. (a) $(1/2)[P_{n-1} + P_{n-2}]$

B. (b) $(1/2)[2P_{n-1} + P_{n-2}]$

C. (c) $(1/2)[P_{n-1} + 2P_{n-2}]$

D. (d) None of these

Answer: A



Watch Video Solution

20. A player tosses a coin and score one point for every head and two points for every tail that turns up. He plays on until his score reaches or passes n . P_n denotes the probability of getting a score of exactly n .

The value of $P_n + (1/2)P_{n-1}$ is equal to

A. (a) $1/2$

B. (b) $2/3$

C. (c) 1

D. (d) None of these

Answer: C



Watch Video Solution

21. A player tosses a coin and score one point for every head and two points for every tail that turns up. He plays on until his score reaches or passes n . P_n denotes the probability of getting a score of exactly n .

The value of $P(n)$ is equal to

A. $P_{100} > 2/3$

B. $P_{100} < 2/3$

C. $P_{100}, P_{101} > 2/3$

D. None of these

Answer: C

[Watch Video Solution](#)

22. A fair die is tossed repeatedly until a 6 is obtained. Let X denote the number of tosses required.

The probability that $X = 3$ equals

A. $25/216$

B. $25/36$

C. $5/36$

D. $125/216$

Answer: A



[Watch Video Solution](#)

23. A fair die is tossed repeatedly until a 6 is obtained. Let X denote the number of tosses required.

The probability that $X \geq 3$ equals

A. $125/216$

B. $25/36$

C. $5/36$

D. $25/216$

Answer: B



[Watch Video Solution](#)

24. A fair die is tossed repeatedly until a 6 is obtained. Let X denote the number of tosses required.

The probability that $X = 3$ equals

A. $125/216$

B. $25/36$

C. $5/36$

D. $25/216$

Answer: D



[Watch Video Solution](#)

25. Let U_1 , and U_2 , be two urns such that U_1 , contains 3 white and 2 red balls, and U_2 , contains only 1 white ball. A fair coin is tossed. If head appears then 1 ball is drawn at random from U_1 , and put into U_2 . However, if tail appears then 2 balls are drawn at random from U_1 , and put into U_2 . Now 1 ball is drawn at random from U_2 . Then, the probability of the drawn ball from U_2 , being white is

A. $\frac{13}{30}$

B. $\frac{23}{30}$

C. $\frac{19}{30}$

D. $\frac{11}{30}$

Answer: B



[Watch Video Solution](#)

26. A box contains 7 red balls, 8 green balls and 5 white balls. A ball is drawn at random from the box. Find the probability that the ball is white.

A. $\frac{1}{4}$

B. $\frac{11}{23}$

C. $\frac{15}{23}$

D. $\frac{12}{23}$

Answer: D



Watch Video Solution

27. A box B_1 contains 1 white ball, 3 red balls, and 2 black balls. Another box B_2 contains 2 white balls, 3 red balls and 4 black balls. A third box B_3 contains 3 white balls, 4 red balls, and 5 black balls.

If 1 ball is drawn from each of the boxes B_1 , B_2 and B_3 , the probability that all 3 drawn balls are of the same color is

A. $82/648$

B. $90/648$

C. $558/648$

Answer: A



Watch Video Solution

28. A box B_1 contains 1 white ball, 3 red balls, and 2 black balls. Another box B_2 contains 2 white balls, 3 red balls and 4 black balls. A third box B_3 contains 3 white balls, 4 red balls, and 5 black balls.

If 2 balls are drawn (without replacement) from a randomly selected box and one of the balls is white and the other ball is red the probability that these 2 balls are drawn from box B_2 is

- A. $22/85$
- B. $126/181$
- C. $65/181$
- D. $55/181$

Answer: D



Watch Video Solution

29. Let n_1 and n_2 be the number of red and black balls, respectively, in box I. Let n_3 and n_4 be the numbers of red and black balls, respectively, in the box II.

A ball is drawn at random from box I and transferred to box II. If the probability of drawing a red ball from box I, after this transfer, is $1/3$, then the possible values of n_1 and n_2 is (are)

- A. $n_1 = 3, n_2 = 3, n_3 = 5, n_4 = 15$
- B. $n_1 = 3, n_2 = 6, n_3 = 10, n_4 = 50$
- C. $n_1 = 8, n_2 = 6, n_3 = 5, n_4 = 20$
- D. $n_1 = 6, n_2 = 12, n_3 = 5, n_4 = 20$

Answer: A:B



Watch Video Solution

30. Let n_1 and n_2 be the number of red and black balls, respectively, in box I. Let n_3 and n_4 be the numbers of red and black balls, respectively, in the box II.

A ball is drawn at random from box I and transferred to box II. If the probability of drawing a red ball from box I, after this transfer, is $1/3$, then the possible values of n_1 and n_2 is (are)

A. $n_1 = 4$ and $n_2 = 6$

B. $n_1 = 2$ and $n_2 = 3$

C. $n_1 = 10$ and $n_2 = 20$

D. $n_1 = 3$ and $n_2 = 6$

Answer: C::D



[Watch Video Solution](#)

31. Football teams T_1 and T_2 have to play two games are independent.

The probabilities of T_1 winning, drawing and losing a game against T_2

are $\frac{1}{6}$, $\frac{1}{6}$ and $\frac{1}{3}$, respectively. Each team gets 3 points for a win, 1 point for a draw and 0 point for a loss in a game. Let X and Y denote the total points scored by teams T_1 and T_2 respectively, after two games.

$P(X = Y)$ is

A. $\frac{1}{4}$

B. $\frac{5}{36}$

C. $\frac{1}{2}$

D. $\frac{13}{36}$

Answer: B



[Watch Video Solution](#)

32. Football teams T_1 and T_2 have to play two games against each other.

It is assumed that the outcomes of the two games are independent. The

probabilities of T_1 winning. Drawing and losing a game against T_2 are

$\frac{1}{2}$, $\frac{1}{6}$ and $\frac{1}{3}$ respectively. Each team gets 3 points for a win. 1 point for a

draw and 0 point for a loss in a game.

Let X and Y denote the total points scored by teams T_1 and T_2 respectively. after two games.

A. $\frac{11}{36}$

B. $\frac{1}{3}$

C. $\frac{13}{36}$

D. $\frac{1}{2}$

Answer: C



Watch Video Solution

33. A fair die is tossed repeatedly until a 6 is obtained. Let X denote the number of tosses required.

The probability that $X = 3$ equals

A. $25/216$

B. $25/36$

C. $5/36$

D. $125/216$

Answer: A



[Watch Video Solution](#)

34. A fair die is tossed repeatedly until a 6 is obtained. Let X denote the number of tosses required.

The probability that $X \geq 3$ equals

A. $125/216$

B. $25/36$

C. $5/36$

D. $25/216$

Answer: B



[Watch Video Solution](#)

35. A fair die is tossed repeatedly until a 6 is obtained. Let X denote the number of tosses required.

The conditional probability that $X \geq 6$ given $X > 3$ equals

A. A. $125/216$

B. B. $25/36$

C. C. $5/36$

D. D. $25/216$

Answer: D



[Watch Video Solution](#)

36. Let U_1 , and U_2 , be two urns such that U_1 , contains 3 white and 2 red balls, and U_2 , contains only 1 white ball. A fair coin is tossed. If head appears then 1 ball is drawn at random from U_1 , and put into U_2 , . However, if tail appears then 2 balls are drawn at random from U_1 , and put into U_2 . . Now 1 ball is drawn at random from U_2 , .Then, the probability of the drawn ball from U_2 , being white is

A. $\frac{13}{30}$

B. $\frac{23}{30}$

C. $\frac{19}{30}$

D. $\frac{11}{30}$

Answer: B



Watch Video Solution

37. Let U_1 , and U_2 , be two urns such that U_1 , contains 3 white and 2 red balls, and U_2 , contains only 1 white ball. A fair coin is tossed. If head appears then 1 ball is drawn at random from U_1 , and put into U_2 , . However, if tail appears then 2 balls are drawn at random from U_1 , and put into U_2 . . Now 1 ball is drawn at random from U_2 , .Then, the probability of the drawn ball from U_2 , being white is

A. $\frac{17}{23}$

B. $\frac{11}{23}$

C. $\frac{15}{23}$

D. $\frac{12}{23}$

Answer: D



Watch Video Solution

38. A box B_1 contains 1 white ball, 3 red balls, and 2 black balls. Another box B_2 contains 2 white balls, 3 red balls and 4 black balls. A third box B_3 contains 3 white balls, 4 red balls, and 5 black balls.

If 1 ball is drawn from each of the boxes B_1 , B_2 and B_3 , the probability that all 3 drawn balls are of the same color is

A. $82/648$

B. $90/648$

C. $558/648$

D. $566/648$

Answer: A



Watch Video Solution

39. A box B_1 contains 1 white ball, 3 red balls, and 2 black balls. Another box B_2 contains 2 white balls, 3 red balls and 4 black balls. A third box B_3 contains 3 white balls, 4 red balls, and 5 black balls.

If 2 balls are drawn (without replacement) from a randomly selected box and one of the balls is white and the other ball is red the probability that these 2 balls are drawn from box B_2 is

A. $116/182$

B. $126/181$

C. $65/181$

D. $55/181$

Answer: D



Watch Video Solution

40. Let n_1 and n_2 be the number of red and black balls, respectively, in box I. Let n_3 and n_4 be the numbers of red and black balls, respectively, in the box II.

A ball is drawn at random from box I and transferred to box II. If the probability of drawing a red ball from box I, after this transfer, is $1/3$, then the possible values of n_1 and n_2 is (are)

- A. $n_1 = 3, n_2 = 3, n_3 = 5, n_4 = 15$
- B. $n_1 = 3, n_2 = 6, n_3 = 10, n_4 = 50$
- C. $n_1 = 8, n_2 = 6, n_3 = 5, n_4 = 20$
- D. $n_1 = 6, n_2 = 12, n_3 = 5, n_4 = 20$

Answer: A::B



[Watch Video Solution](#)

41. Let n_1 and n_2 be the number of red and black balls, respectively, in box I. Let n_3 and n_4 be the numbers of red and black balls, respectively,

in the box II.

A ball is drawn at random from box I and transferred to box II. If the probability of drawing a red ball from box I, after this transfer, is $\frac{1}{3}$, then the possible values of n_1 and n_2 is (are)

A. $n_1 = 4$ and $n_2 = 6$

B. $n_1 = 2$ and $n_2 = 3$

C. $n_1 = 10$ and $n_2 = 20$

D. $n_1 = 3$ and $n_2 = 6$

Answer: C::D



[Watch Video Solution](#)

42. Football teams T_1 and T_2 have to play two games are independent.

The probabilities of T_1 winning, drawing and losing a game against T_2

are $\frac{1}{6}$, $\frac{1}{6}$ and $\frac{1}{3}$, respectively. Each team gets 3 points for a win, 1 point

for a draw and 0 point for a loss in a game. Let X and Y denote the total

points scored by teams T_1 and T_2 respectively, after two games.

$P(X = Y)$ is

A. $\frac{1}{4}$

B. $\frac{5}{12}$

C. $\frac{1}{2}$

D. $\frac{7}{12}$

Answer: B



[Watch Video Solution](#)

43. Football teams T_1 and T_2 have to play two games are independent.

The probabilities of T_1 winning, drawing and losing a game against T_2

are $\frac{1}{6}$, $\frac{1}{6}$ and $\frac{1}{3}$, respectively. Each team gets 3 points for a win, 1 point

for a draw and 0 point for a loss in a game. Let X and Y denote the total

points scored by teams T_1 and T_2 respectively, after two games.

$P(X = Y)$ is

A. $\frac{11}{36}$

B. $\frac{1}{3}$

C. $\frac{13}{36}$

D. $\frac{1}{2}$

Answer: C



[Watch Video Solution](#)

MATRIX MATCH TYPE

1. An urn contains four black and eight white balls. Three balls are drawn from the urn without replacement. Three events are defined on this experiment. A: Exactly one black ball is drawn. B.: All balls are drawn are of the same color. C: Third drawn ball is black. Match the entries of column I with none, one or more entries of column II. Column I, Column II The events A and B are, p. mutually exclusive The events B and C are, q.

independent The events C and A are, r. neither independent nor mutually exclusive The events A , B and C are, s. exhaustive

 [View Text Solution](#)

2. Simplify the following : $(4m + 5n)^2 + (5m + 4n)^2$

 [Watch Video Solution](#)

3. Match the following lists:

List I	List II
a. If lines $3x + y - 4 = 0$, $x - 2y - 6 = 0$, and $\lambda x + 4y + \lambda^2 = 0$ are concurrent, then the value of λ is	p. -4
b. If the points $(\lambda + 1, 1)$, $(2\lambda + 1, 3)$, and $(2\lambda + 2, 2\lambda)$ are collinear, then the value of λ is	q. $-1/2$
c. If the line $x + y - 1 - \lambda/2 = 0$, passing through the intersection of $x - y + 1 = 0$ and $3x + y - 5 = 0$, is perpendicular to one of them, then the value of λ is	r. 4
d. If the line $y - x - 1 + \lambda = 0$ is equidistant from the points $(1, -2)$ and $(3, 4)$, then λ is	s. 2

5. Match the following lists:

 [Watch Video Solution](#)

4. Consider the lines represented by equation $(x^2 + xy - x) \times (x - y) = 0$ forming a triangle. Then match the following lists:

List I	List II
a. Orthocenter of triangle	p. $(1/6, 1/2)$
b. Circumcenter	q. $(1/(2 + 2\sqrt{2}), 1/2)$
c. Centroid	r. $(0, 1/2)$
d. Incenter	s. $(1/2, 1/2)$



Watch Video Solution

5. Consider the lines represented by equation $(x^2 + xy - x) \times (x - y) = 0$ forming a triangle. Then match the following lists:

List I	List II
a. Orthocenter of triangle	p. $(1/6, 1/2)$
b. Circumcenter	q. $(1/(2 + 2\sqrt{2}), 1/2)$
c. Centroid	r. $(0, 1/2)$
d. Incenter	s. $(1/2, 1/2)$

A. $q s s r$

B. $q r s r$

C. $q s r p$

D. $r s p q$

Answer: B



Watch Video Solution

6. A bag contains some white and some black balls, all combinations of balls being equally likely. The total number of balls in the bag is 10. If three balls are drawn at random without replacement and all of them are found to be black, the probability that the bag contains 1 white and 9 black balls is

A. $q s s r$

B. $r s q p$

C. $q s r p$

D. $q p r q$

Answer: D

 Watch Video Solution

7. Match the following lists :

List I (A, B, C are matrices)	List II
a. If $ A = 2$, then $ 2A^{-1} =$ (where A is of order 3)	p. 1
b. If $ A = 1/8$, then $ \text{adj}(\text{adj}(2A)) =$ (where A is of order 3)	q. 4
c. If $(A + B)^2 = A^2 + B^2$, and $ A = 2$, then $ B =$ (where A and B are of odd order)	r. 24
d. $ A_{2 \times 2} = 2$, $ B_{3 \times 3} = 3$ and $ C_{4 \times 4} = 4$, then $ ABC $ is equal to	s. 0
	t. does not exist

 Watch Video Solution

8. An urn contains r red balls and b black balls. Now, match the following lists:



Watch Video Solution

9. Let A and B are two independent events. Such that $P(A) = 1/3$ and $P(B) = 1/4$. Then match the following lists:



A. $q \ s \ s \ r$

B. $q \ r \ s \ r$

C. $q \ s \ r \ p$

D. $r \ s \ p \ q$

Answer: B



Watch Video Solution

10. A bag contains some white and some black balls, all combinations of balls being equally likely. The total number of balls in the bag is 10. If three balls are drawn at random without replacement and all of them are found to be black, the probability that the bag contains 1 white and 9 black balls is

A. $q \ s \ s \ r$

B. $r \ s \ q \ p$

C. $q \ s \ r \ p$

D. $q \ p \ r \ q$

Answer: D



[Watch Video Solution](#)

NUMARICAL VALUE TYPE

1. If two loaded dice each have the property that 2 or 4 is three times as likely to appear as 1, 3, 5, or 6 on each roll. When two such dice are rolled, the probability of obtaining a total of 7 is p , then value of $[1/p]$ is, where $[x]$ represents the greatest integer less than or equal to x .

 [Watch Video Solution](#)

2. An urn contains 3 red balls and n white balls. Mr. A draws two balls together from the urn. The probability that they have the same color is $1/2$. Mr. B. Draws one ball from the urn, notes its color and replaces it. He then draws a second ball from the urn and finds that both balls have the same color is $5/8$. The possible value of n is (a) 9 b. 6 c. 5 d. 1

 [Watch Video Solution](#)

3. Suppose A and B are two events with $P(A) = 0.5$ and $P(A \cup B) = 0.8$. Let $P(B) = p$ if A and B are mutually exclusive and $P(B) = q$ if A and B are independent events, then value of q/p is ____.



Watch Video Solution

4. Thirty two players ranked 1 to 32 are playing in a knockout tournament. Assume that in every match between any two players, the better ranked player wins the probability that ranked 1 and ranked 2 players are winner and runner up, respectively, is $\frac{16}{31}$ b. $\frac{1}{2}$ c. $\frac{17}{31}$ d. none of these



Watch Video Solution

5. If A and B are two events such that $P(A) = 0.6$ and $P(B) = 0.8$, if the greatest value that $P(A/B)$ can have is p, then the value of $8p$ is _____.



Watch Video Solution

6. A die is thrown three times. The chance that the highest number shown on the die is 4 is p, then the value of $[1/p]$ is where $[.]$ represents greatest integer function is _____.

A. A. 4

B. B. 5

C. C. 6

D. D. 7

Answer: 5



[Watch Video Solution](#)

7. Two cards are drawn from a well shuffled pack of 52 cards. The probability that one is a heart card and the other is a king is p , then the value of $104p$ is _____.



[Watch Video Solution](#)

8. A fair coin is flipped n times. Let E be the event "a head is obtained on the first flip" and let F_k be the event "exactly k heads are obtained". Then the value of $\frac{n}{k}$ for which E and F_k are independent is _____.



[Watch Video Solution](#)

9. An unbiased normal coin is tossed n times. Let

E_1 : event that both heads and tails are present in n tosses.

E_2 : event that the coin shows up heads at most once.

The value of n for which E_1 and E_2 are independent is _____.



[Watch Video Solution](#)

10. In a knockout tournament 2^n equally skilled players, S_1, S_2, S_{2n} are participating. In each round, players are divided in pair at random and winner from each pair moves in the next round. If S_2 reaches the semi-final, then the probability that S_1 wins the tournament is $1/84$. The value of n equals _____.



[Watch Video Solution](#)

11. Of the three independent events E_1 , E_2 , and E_3 , the probability that only E_1 occurs is α only E_2 occurs is β , and only E_3 occurs is γ . Let the probability p that none of events E_1 , E_2 , or E_3 occurs satisfy the equations $(\alpha - 2\beta)p = \alpha\beta$ and $(\beta - 3\gamma)p = 2\beta\gamma$. All the given probabilities are assumed to lie in the interval $(0, 1)$. Then

$$\frac{\text{Probability of occurrence of } E_1}{\text{Probability of occurrence of } E_3} =$$

 [Watch Video Solution](#)

12. about to only mathematics

 [Watch Video Solution](#)

13. If two loaded dice each have the property that 2 or 4 is three times as likely to appear as 1, 3, 5, or 6 on each roll. When two such dice are rolled, the probability of obtaining a total of 7 is p , then value of $[1/p]$ is, where $[x]$ represents the greatest integer less than or equal to x .

 [Watch Video Solution](#)

14. An urn contains 3 red balls and n white balls. Mr. A draws two balls together from the urn. The probability that they have the same color is $\frac{1}{2}$. Mr. B. Draws one balls form the urn, notes its color and replaces it. He then draws a second ball from the urn and finds that both balls have the same color is $\frac{5}{8}$. The possible value of n is (a)9 b. 6 c. 5 d. 1

 Watch Video Solution

15. Suppose A and B are two events with $P(A) = 0.5$ and $P(A \cup B) = 0.8$. Let $P(B) = p$ if A and B are mutually exclusive and $P(B) = q$ if A and B are independent events, then the value of q/p is _____.

 Watch Video Solution

16. Thirty two players ranked 1 to 32 are playing in a knockout tournament. Assume that in every match between any two players, the better ranked player wins the probability that ranked 1 and ranked 2 players are winner and runner up, respectively, is $\frac{16}{31}$ b. $\frac{1}{2}$ c. $\frac{17}{31}$ d. none of these

 [Watch Video Solution](#)

17. If A and B are two events such that $P(A) = 0.6$ and $P(B) = 0.8$, if the greatest value that $P(A/B)$ can have is p, then the value of $8p$ is _____.

 [Watch Video Solution](#)

18. A die is thrown three times. The chance that the highest number shown on the die is 4 is p, then the value of $[1/p]$ is where $[.]$ represents greatest integer function is _____.

 [Watch Video Solution](#)

19. Two cards are drawn from a well shuffled pack of 52 cards. The probability that one is a heart card and the other is a king is p , then the value of $104p$ is _____.



Watch Video Solution

20. A fair coin is flipped n times. Let E be the event "a head is obtained on the first flip" and let F_k be the event "exactly k heads are obtained". Then the value of $\frac{n}{k}$ for which E and F_k are independent is _____.



Watch Video Solution

21. An unbiased normal coin is tossed n times. Let

E_1 : event that both heads and tails are present in n tosses.

E_2 : event that the coin shows up heads at most once.

The value of n for which E_1 and E_2 are independent is _____.



Watch Video Solution

22. In a knockout tournament 2^n equally skilled players, S_1, S_2, S_{2n} are participating. In each round, players are divided in pair at random and winner from each pair moves in the next round. If S_2 reaches the semi-final, then the probability that S_1 wins the tournament is $1/84$. The value of n equals _____.



[Watch Video Solution](#)

23. Of the three independent events $E_1, E_2,$ and $E_3,$ the probability that only E_1 occurs is α only E_2 occurs is $\beta,$ and only E_3 occurs is $\gamma.$ Let the probability p that none of events $E_1, E_2,$ or E_3 occurs satisfy the equations $(\alpha - 2\beta)p = \alpha\beta$ and $(\beta - 3\gamma)p = 2\beta\gamma.$ All the given probabilities are assumed to lie in the interval $(0, 1).$ Then

$$\frac{\text{Probability of occurrence of } E_1}{\text{Probability of occurrence of } E_3} =$$



[Watch Video Solution](#)

24. The minimum number of times a fair coin needs to be tossed, so that the probability of getting at least two heads is at least 0.96, is _____.



[Watch Video Solution](#)

SINGLE CORRECT ANSWER TYPE

1. One ticket is selected at random from 50 tickets numbered 00, 01, 02, ..., 49. Then the probability that the sum of the digits on the selected ticket is 8, given that the product of these digits is zero, is

A. $\frac{1}{14}$

B. $\frac{1}{7}$

C. $\frac{5}{14}$

D. $\frac{1}{50}$

Answer: A



[Watch Video Solution](#)

2. In a binomial distribution $B\left(n, p = \frac{1}{4}\right)$, if the probability of at least one success is greater than or equal to $\frac{9}{10}$, then n is greater than (1)

$$\frac{1}{(\log)_{10}^4 - (\log)_{10}^3}$$

$$(2) \frac{1}{(\log)_{10}^4 + (\log)_{10}^3}$$

$$(3) \frac{9}{(\log)_{10}^4 - (\log)_{10}^3}$$

$$(4) \frac{4}{(\log)_{10}^4 - (\log)_{10}^3}$$

$$A. \frac{1}{\log_{10} 4 - \log_{10} 3}$$

$$B. \frac{1}{\log_{10} 4 + \log_{10} 3}$$

$$C. \frac{9}{\log_{10} 4 - \log_{10} 3}$$

$$D. \frac{4}{\log_{10} 4 - \log_{10} 3}$$

Answer: A



Watch Video Solution

3. Consider 5 independent Bernoulli trials each with probability of success p . If the probability of at least one failure is greater than or equal to $\frac{31}{32}$, then p lies in the interval : (1) $\left(\frac{1}{2}, \frac{3}{4}\right]$ (2) $\left(\frac{3}{4}, \frac{11}{12}\right]$ (3) $\left[0, \frac{1}{2}\right]$ (4) $\left(\frac{11}{12}, 1\right]$

A. $\left(\frac{11}{12}, 1\right]$

B. $\left(\frac{1}{2}, \frac{3}{4}\right]$

C. $\left(\frac{3}{4}, \frac{11}{12}\right]$

D. $\left[0, \frac{1}{2}\right]$

Answer: D



Watch Video Solution

4. If C and D are two events such that $C \subset D$ and $P(D) \neq 0$, then the correct statement among the following is

A. $P(C | D) = \frac{P(D)}{P(D)}$

B. $P(C | D) = P(C)$

C. $P(C | D) \geq P(C)$

D. $P(C | D) < P(C)$

Answer: C



Watch Video Solution

5. Three numbers are chosen at random without replacement from $\{1, 2, 3, \dots, 8\}$. The probability that their minimum is 3, given that their maximum is 6, is

A. $\frac{3}{8}$

B. $\frac{1}{5}$

C. $\frac{1}{4}$

D. $\frac{2}{5}$

Answer: B

[Watch Video Solution](#)

6. A multiple choice examination has 5 questions. Each question has three alternative answers of which exactly one is correct. The probability that a student will get 4 or more correct answers just guessing is

A. $\frac{17}{3^5}$

B. $\frac{13}{3^5}$

C. $\frac{11}{3^5}$

D. $\frac{10}{3^5}$

Answer: C

[Watch Video Solution](#)

7. Let A and B be two events such that $P(\overline{A \cup B}) = 1/6$, $P(A \cap B) = 1/4$ and $P(\overline{A}) = 1/4$ where \overline{A} stands for complement of event A . Then events A and B are

A. mutually exclusive and independent

B. equally likely but not independent

C. Independent but not equally likely

D. independent and equally likely

Answer: C



Watch Video Solution

8. Twelve balls are distributed among three boxes, find the probability that the first box will contains three balls.

A. $\frac{55}{3} \left(\frac{2}{3}\right)^{11}$

B. $55 \left(\frac{2}{3}\right)^{10}$

C. $220 \left(\frac{1}{3}\right)^{12}$

D. $22 \left(\frac{1}{3}\right)^{11}$

Answer: A



Watch Video Solution

9. Let two fair six-faced dice A and B be thrown simultaneously. If E_1 is the event that die A shows up four, E_2 is the event that die B shows up two and E_3 is the event that the sum of numbers on both dice is odd, then which of the following statements is NOT True ?

- A. E_2 and E_3 are independent
- B. E_1 and E_3 are independent
- C. E_1 and E_2 and E_3 are independent
- D. E_1 and E_2 are independent

Answer: C



Watch Video Solution

10. A box contains 15 green and 10 yellow balls. If 10 balls are randomly drawn, one by one with replacement, then the variance of the number

of green balls drawn, is

A. $\frac{6}{25}$

B. $\frac{12}{5}$

C. 6

D. 4

Answer: B



[Watch Video Solution](#)

11. A bag contains 4 red and 6 black balls. A ball is drawn at random from the bag, its colour is observed and this ball along with two additional balls of the same colour are returned to the bag. If now a ball is drawn at random from the bag, If now a ball is drawn at random from the bag, then the probability that this drawn ball is red, is

A. $\frac{3}{4}$

B. $\frac{3}{10}$

C. $\frac{2}{5}$

D. $\frac{1}{5}$

Answer: C



Watch Video Solution

12. A signal which can be green or red with probability $\frac{4}{5}$ and $\frac{1}{5}$ respectively, is received by station A and then transmitted to station B. The probability of each station receiving the signal correctly is $\frac{3}{4}$. If the signal received at station B is green, then the probability that original signal was green is

A. $\frac{3}{5}$

B. $\frac{6}{7}$

C. $\frac{20}{23}$

D. $\frac{9}{20}$

Answer: C



Watch Video Solution

13. Four person independently solve a certain problem correctly with probabilities $\frac{1}{2}$, $\frac{3}{4}$, $\frac{1}{4}$, $\frac{1}{8}$. Then the probability that he problem is solve correctly by at least one of them is $\frac{235}{256}$ b. $\frac{21}{256}$ c. $\frac{3}{256}$ d. $\frac{253}{256}$

A. $\frac{235}{256}$

B. $\frac{21}{256}$

C. $\frac{3}{256}$

D. $\frac{253}{256}$

Answer: A



Watch Video Solution

14. A computer producing factory has only two plants T_1 and T_2 . Plant T_1 produces 20% and plant T_2 produces 80% of the total computers produced in the factory turn out to be defective. It is known that $P(\text{computer turns out to be defective given that it is produced in plant } T_1) = 10 P(\text{computer turns out to be defective given that it is produced in plant } T_2)$, where $P(E)$ denotes the probability of an event E . A computer produced in the factory is randomly selected and it does not turn out to be defective. Then the probability that it is produced in plant T_2 is

A. $\frac{36}{73}$

B. $\frac{47}{79}$

C. $\frac{78}{93}$

D. $\frac{75}{83}$

Answer: C



Watch Video Solution

15. One ticket is selected at random from 50 tickets numbered 00, 01, 02, ..., 49. Then the probability that the sum of the digits on the selected ticket is 8, given that the product of these digits is zero, is

A. $\frac{1}{14}$

B. $\frac{1}{7}$

C. $\frac{5}{14}$

D. $\frac{1}{50}$

Answer: A

 [Watch Video Solution](#)

16. In a binomial distribution $B\left(n, p = \frac{1}{4}\right)$, if the probability of at least one success is greater than or equal to $\frac{9}{10}$, then n is greater than (1)

(1) $\frac{1}{(\log)_{10}^4 - (\log)_{10}^3}$

(2) $\frac{1}{(\log)_{10}^4 + (\log)_{10}^3}$

$$(3) \frac{9}{(\log)_{10}^4 - (\log)_{10}^3}$$

$$(4) \frac{4}{(\log)_{10}^4 - (\log)_{10}^3}$$

$$A. \frac{1}{\log_{10} 4 - \log_{10} 3}$$

$$B. \frac{1}{\log_{10} 4 + \log_{10} 3}$$

$$C. \frac{9}{\log_{10} 4 - \log_{10} 3}$$

$$D. \frac{4}{\log_{10} 4 - \log_{10} 3}$$

Answer: A



Watch Video Solution

17. Consider 5 independent Bernoulli's trials each with probability of at least one failure is greater than or equal to $\frac{31}{32}$, then p lies in the interval

$$A. \left(\frac{11}{12}, 1 \right]$$

$$B. \left(\frac{1}{2}, \frac{3}{4} \right]$$

C. $\left(\frac{3}{4}, \frac{11}{12}\right]$

D. $\left[0, \frac{1}{2}\right]$

Answer: D



Watch Video Solution

18. If C and D are two events such that $C \subset D$ and $P(D) \neq 0$, then the correct statement among the following is

A. $P(C | D) = \frac{P(D)}{P(D)}$

B. $P(C | D) = P(C)$

C. $P(C | D) \geq P(C)$

D. $P(C | D) < P(C)$

Answer: C



Watch Video Solution

19. Three numbers are chosen at random without replacement from $\{1, 2, 3, \dots, 8\}$. The probability that their minimum is 3, given that their maximum is 6, is

A. $\frac{3}{8}$

B. $\frac{1}{5}$

C. $\frac{1}{4}$

D. $\frac{2}{5}$

Answer: B



[Watch Video Solution](#)

20. A multiple choice examination has 5 questions. Each question has three alternative answers of which exactly one is correct. The probability that a student will get 4 or more correct answers just guessing is

A. $\frac{17}{3^5}$

B. $\frac{13}{3^5}$

C. $\frac{11}{3^5}$

D. $\frac{10}{3^5}$

Answer: C



Watch Video Solution

21. Let A and B be two events such that $P(\overline{A \cup B}) = \frac{1}{6}$, $P(A \cap B) = \frac{1}{4}$ and $P(\overline{A}) = \frac{1}{4}$, where \overline{A} stands for the complement of the event A . Then the events A and B are

- A. mutually exclusive and independent
- B. equally likely but not independent
- C. Independent but not equally likely
- D. independent and equally likely

Answer: C

[Watch Video Solution](#)

22. If 12 identical balls are to be placed in 3 identical boxes, then the probability that one of the boxes contains exactly 3 balls is :

A. $\frac{55}{3} \left(\frac{2}{3}\right)^{11}$

B. $55 \left(\frac{2}{3}\right)^{10}$

C. $220 \left(\frac{1}{3}\right)^{12}$

D. $22 \left(\frac{1}{3}\right)^{11}$

Answer: A

[Watch Video Solution](#)

23. Let two fair six-faced dice A and B be thrown simultaneously. If E_1 is the event that die A shows up four, E_2 is the event that die B shows up two and E_3 is the event that the sum of numbers on both dice is odd, then which of the following statement is NOT True ?

- A. E_2 and E_3 are independent
- B. E_1 and E_3 are independent
- C. E_1 and E_2 and E_3 are independent
- D. E_1 and E_2 are independent

Answer: C

 [Watch Video Solution](#)

24. A box contains 15 green and 10 yellow balls. If 10 balls are randomly drawn, one-by-one, with replacement, then the variance of the number of green balls drawn is

- A. $\frac{6}{25}$
- B. $\frac{12}{5}$
- C. 6
- D. 4

Answer: B



[Watch Video Solution](#)

25. A bag contains 4 red and 6 black balls. A ball is drawn at random from the bag, its colour is observed and this ball along with two additional balls of the same colour are returned to the bag. If now a ball is drawn at random from the bag, then the probability that this drawn ball is red, is

A. $\frac{3}{4}$

B. $\frac{3}{10}$

C. $\frac{2}{5}$

D. $\frac{1}{5}$

Answer: C



[Watch Video Solution](#)

26. A signal which can be green or red with probability $\frac{4}{5}$ and $\frac{1}{5}$ respectively, is received by station A and then transmitted to station B. The probability of each station receiving the signal correctly is $\frac{3}{4}$. If the signal received at station B is green, then the probability that original signal was green is

A. $\frac{3}{5}$

B. $\frac{6}{7}$

C. $\frac{20}{23}$

D. $\frac{9}{20}$

Answer: C



[Watch Video Solution](#)

27. Four persons independently solve a certain problem correctly with probabilities $\frac{1}{2}, \frac{3}{4}, \frac{1}{4}, \frac{1}{8}$. Then the probability that the problem is solved correctly by at least one of them is

A. $\frac{235}{256}$

B. $\frac{21}{256}$

C. $\frac{3}{256}$

D. $\frac{253}{256}$

Answer: A

 [Watch Video Solution](#)

28. A computer producing factory has only two plants T_1 and T_2 . Plant T_1 produces 20% and plant T_2 produces 80% of the total computers produced. 7% of computers produced in the factory turn out to be defective. It is known that $P(\text{computer turns out to be defective, given that it is produced in plant } T_1) = 10 \times P(\text{computer turns out to be defective, given that it is produced in plant } T_2)$, where $P(E)$ denotes the probability of an event E . A computer produced in the factory is randomly selected and it does not turn out to be defective. Then, the probability that it is produced in plant T_2 , is

A. $\frac{36}{73}$

B. $\frac{47}{79}$

C. $\frac{78}{96}$

D. $\frac{75}{83}$

Answer: C



Watch Video Solution

MULTIPLE CORRECT ANSWER TYPE

1. Let E and F be two independent events. The probability that exactly one of them occurs is $\frac{11}{25}$ and the probability if none of them occurring is $\frac{2}{25}$. If $P(T)$ denotes the probability of occurrence of the event T , then

(a) $P(E) = \frac{4}{5}, P(F) = \frac{3}{5}$ (b) $P(E) = \frac{1}{5}, P(F) = \frac{2}{5}$ (c)

$P(E) = \frac{2}{5}, P(F) = \frac{1}{5}$ (d) $P(E) = \frac{3}{5}, P(F) = \frac{4}{5}$

A. $P(E) = \frac{4}{5}, P(F) = \frac{3}{5}$

$$\text{B. } P(E) = \frac{1}{5}, P(F) = \frac{2}{5}$$

$$\text{C. } P(E) = \frac{2}{5}, P(F) = \frac{1}{5}$$

$$\text{D. } P(E) = \frac{3}{5}, P(F) = \frac{4}{5}$$

Answer: A::D



Watch Video Solution

2. A ship is fitted with three engines E_1, E_2 and E_3 . The engines function independently of each other with respective probabilities $\frac{1}{2}, \frac{1}{4},$ and $\frac{1}{4}$. For the ship to be operational at least two of its engines must function. Let X denote the event that the ship is operational and

let X_1, X_2 and X_3 denote, respectively, the events that the engines E_1, E_2 and E_3 are function. Which of the following is/are true? (a)

$$P(X_1^c | X) = \frac{3}{16} \quad \text{(b) } P(\text{exactly two engines of the ship are functioning} | X) = \frac{7}{8} \quad \text{(c) } P(X | X_2) = \frac{5}{6} \quad \text{(d) } P(X | X_1) = \frac{7}{16}$$

$$\text{A. } P(X_1^c | X) = \frac{3}{16}$$

B. $P(\text{exactly two engines of the ship are functioning} | X) = \frac{7}{8}$

C. $P(X | X_1) = \frac{5}{16}$

D. $P(X | X_1) = \frac{7}{16}$

Answer: B::D

 [Watch Video Solution](#)

3. Let X and Y be two events such that $P(X) = \frac{1}{3}$, $P(X | Y) = \frac{1}{2}$ and $P(Y | X) = \frac{1}{3}$. Then

A. $P(Y) = \frac{1}{3}$

B. $P(X' | Y) = \frac{1}{2}$

C. $P(X \cup Y) = \frac{2}{3}$

D. $P(X \cap Y) = \frac{1}{5}$

Answer: A::B

 [Watch Video Solution](#)

4. Let E and F be two independent events. The probability that exactly one of them occurs is $\frac{11}{25}$ and the probability if none of them occurring is $\frac{2}{25}$. If $P(T)$ denotes the probability of occurrence of the event T , then

(a) $P(E) = \frac{4}{5}, P(F) = \frac{3}{5}$ (b) $P(E) = \frac{1}{5}, P(F) = \frac{2}{5}$ (c) $P(E) = \frac{2}{5}, P(F) = \frac{1}{5}$ (d) $P(E) = \frac{3}{5}, P(F) = \frac{4}{5}$

A. $P(E) = \frac{4}{5}, P(F) = \frac{3}{5}$

B. $P(E) = \frac{1}{5}, P(F) = \frac{2}{5}$

C. $P(E) = \frac{2}{5}, P(F) = \frac{1}{5}$

D. $P(E) = \frac{3}{5}, P(F) = \frac{4}{5}$

Answer: A:D



Watch Video Solution

5. A ship is fitted with three engines E_1, E_2 and E_3 . The engines function independently of each other with respective probabilities

$\frac{1}{2}$, $\frac{1}{4}$, and $\frac{1}{4}$. For the ship to be operational at least two of its engines must function. Let X denote the event that the ship is operational and let X_1, X_2 and X_3 denote, respectively, the events that the engines E_1, E_2 and E_3 are function. Which of the following is/are true? (a) $P(X_1^c | X) = \frac{3}{16}$ (b) $P(\text{exactly two engines of the ship are functioning} | X) = \frac{7}{8}$ (c) $P(X | X_2) = \frac{5}{6}$ (d) $P(X | X_1) = \frac{7}{16}$

A. $P(X_1^c | X) = \frac{3}{16}$

B. $P(\text{exactly two engines of the ship are functioning} | X) = \frac{7}{8}$

C. $P(X | X_1) = \frac{5}{16}$

D. $P(X | X_1) = \frac{7}{16}$

Answer: B::D



Watch Video Solution

6. Let X and Y be two events such that $P(X) = \frac{1}{3}$, $P(X | Y) = \frac{1}{2}$ and $P(Y | X) = \frac{2}{5}$. Then

$$\text{A. } P(Y) = \frac{4}{15}$$

$$\text{B. } P(X' | Y) = \frac{1}{2}$$

$$\text{C. } P(X \cup Y) = \frac{2}{5}$$

$$\text{D. } P(X \cap Y) = \frac{1}{5}$$

Answer: A::B



Watch Video Solution