



## PHYSICS

### BOOKS - RESNICK AND HALLIDAY PHYSICS (HINGLISH)

#### GAUSS' LAW

##### SAMPLE PROBLEM

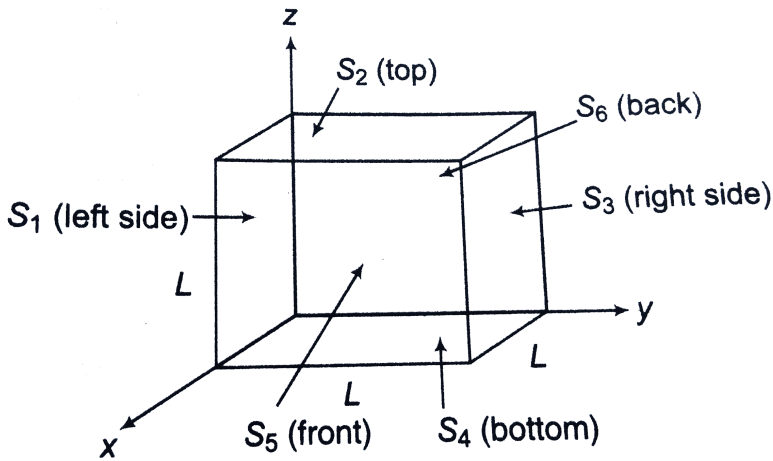
1. Consider a cylindrical surface of radius  $R$  and length  $l$  in a uniform electric field  $E$ . Compute the electric flux if the axis of the cylinder is parallel to the field direction.



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2. A cube has sides of length  $L$ . It is placed with one corner at the origin as shown in figure. The electric field is uniform and given by

$E = -B\hat{i} + C\hat{j} - D\hat{k}$ , where B, C and D are positive constants.

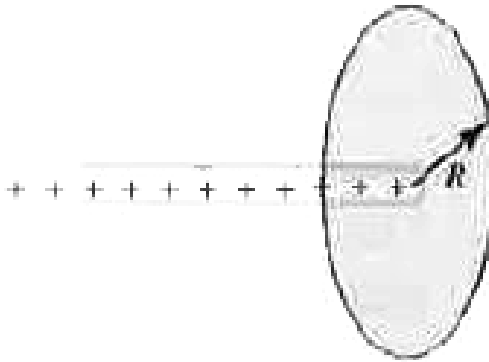


- (a) Find the electric flux through each of the six cube faces  $S_1$ ,  $S_2$ ,  $S_3$ ,  $S_4$  and  $S_5$  and  $S_6$ .
- (b) Find the electric flux through the entire cube.

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3. Calculation the flux through the flat disk held perpendicular to the end of a semi-infinite wire of charge per unit length  $\lambda$ . The radius of the disk is

R



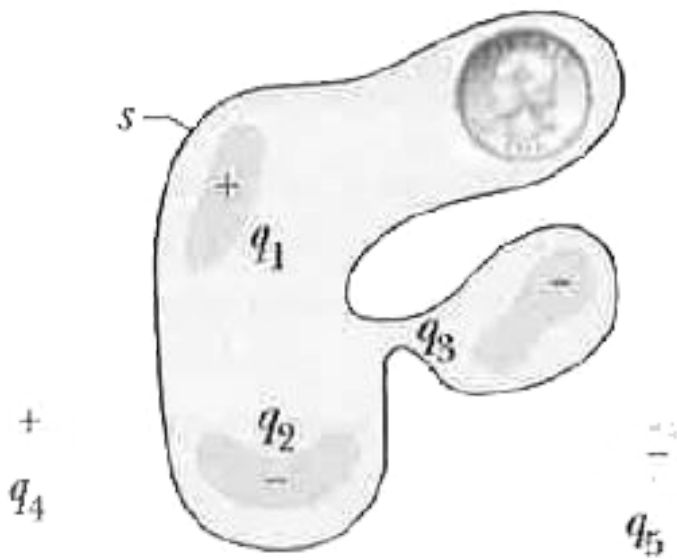
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4. shows five charged lumps of plastic and an electrically neutral coin.

The cross section of a Gaussian surface  $S$  is indicated. What is the net

electric flux through the surface if

$$q_1 = q_4 + 3.1nC, q_2 = q_5 = - 5.9nC \text{ and } q_3 = - 3.1nC ?$$

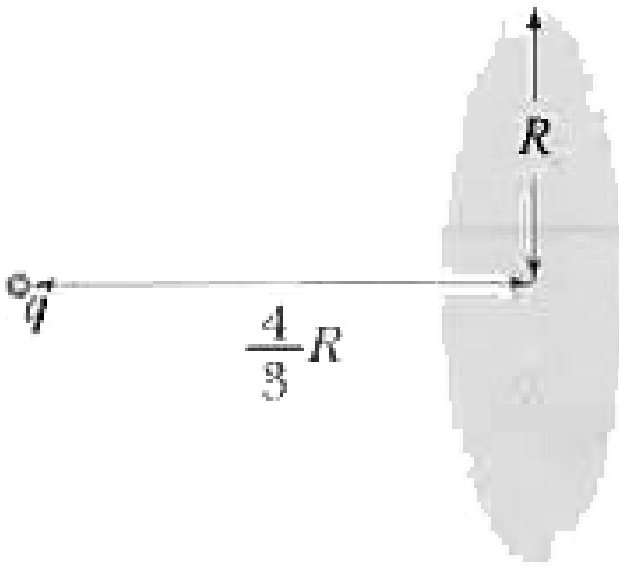


Five plastic objects, each with an electric charge, and a coin, which has no net charge. A Gaussian surface, shown in cross section, encloses three of the plastic objects and the coin.

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5. Finding flux due to a point charge through a disk. The line joining the charge to the center of the disk is perpendicular to the disk.





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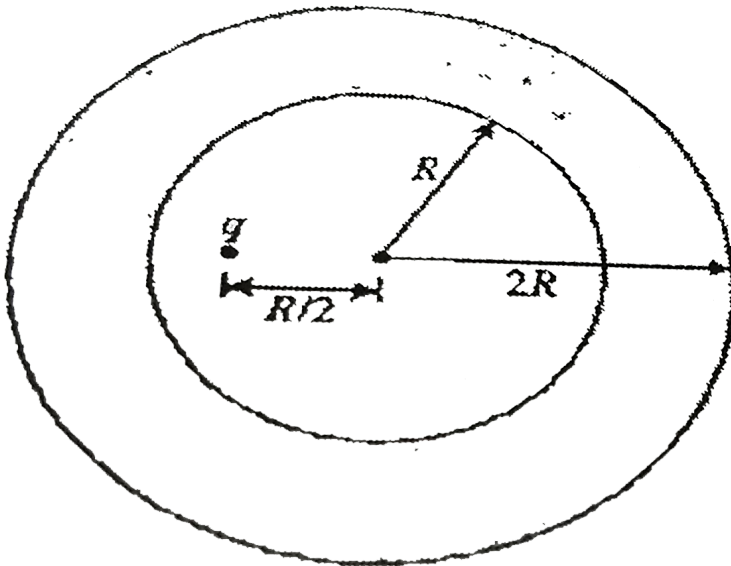
6. shows, in cross section, a plastic, spherical shell with uniform charge  $Q = -16e$  and radius  $R = 10\text{cm}$ . A particle with charge  $q = +5e$  is at the center. What is the electric field (magnitude and direction) at (a) point  $P_1$  at radial distance  $r_1 = 6.00\text{cm}$  and (b) point  $P_2$  at radial distance  $r_2 = 12.0\text{cm}$  ?

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7. किसी आवेशित संधारित पर नेट आवेश कितना होता है?

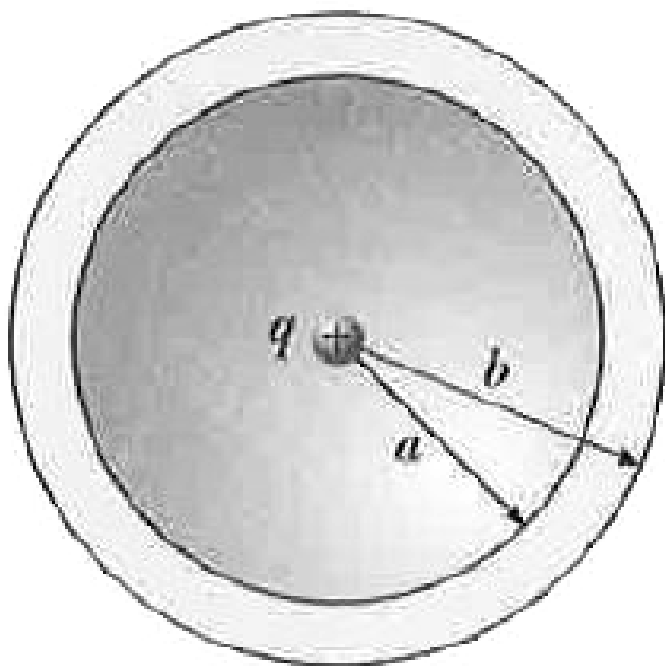
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8. Figure shows a cross-section of a spherical metal shell of inner radius  $R$  and out radius  $2R$ . A point charge  $q$  is located at a distance  $R/2$  from the centre of the shell. If the shell is electrically neutral, then which of the following statements is/are correct :



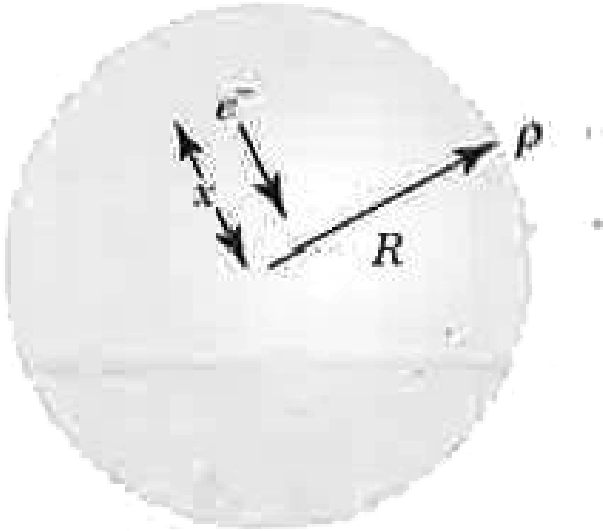
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9. a nonconducting spherical shell of inner radius  $a = 2.00$  cm and outer radius  $b = 2.40$  cm has (within its thickness) a positive volume charge density  $\rho = A/r$ , where  $A$  is a constant and  $r$  is the distance from the center of the shell. In addition, a small ball of charge  $q = 45.0$  fC is located at that center. What value should  $A$  have if the electric field in the shell ( $a < b < c$ ) is to be uniform?



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10. An electron is released from the surface of a uniformly and positively charged sphere (volume charge density  $\rho$ , fig) Show that the electron will execute SHM and find its time period



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11. Upward streamer in a lightning storm. The woman in was standing on a lookout platform high in the Sequoia National Park when a large storm cloud moved overhead. Some of the conduction electrons in her body were driven into the ground by the cloud's negatively charged base

leaving her positively charged. You can tell she was highly charged because

her hair strands repelled one another and extended away from her along the electric field lines produced by the charge on her.

Lightning did not strike the woman, but she was in extreme danger because that electric field was on the verge of causing electrical breakdown in the surrounding air. Such a breakdown would have occurred along a path extending away from her in what is called an upward streamer. an upwars stremer. An upward streamer is dangerous because the resulting ionization of molecules in the air suddenly frees a tremendous number of electrons from those molecules. Had the women in develpoed an upward streamer, the free electrons in the air would have moved to neutral ize her producing a large, perhaps fatal, charge flow through her body . That charge flow is dangerous because it could have interfered with or even stopped her breathing (which is obviously necessary for oxygen) and the steady beat of her heart (which is obviously necessary for the blood flow that carries the oxygen). The charge flow could also have caused burns.

Let's model her body as a narrow vertical cylinder of height  $L = 1.8\text{m}$  and

radius  $R = 0.10\text{m}$ . Assume that charge  $Q$  was uniformly distributed along the cylinder and that electrical breakdown would have occurred if the electric field magnitude along her body had exceeded the critical value  $E_c = 2.4\text{MN/C}$ . What value of  $Q$  would have put the air along

her body on the verge of breakdown ?

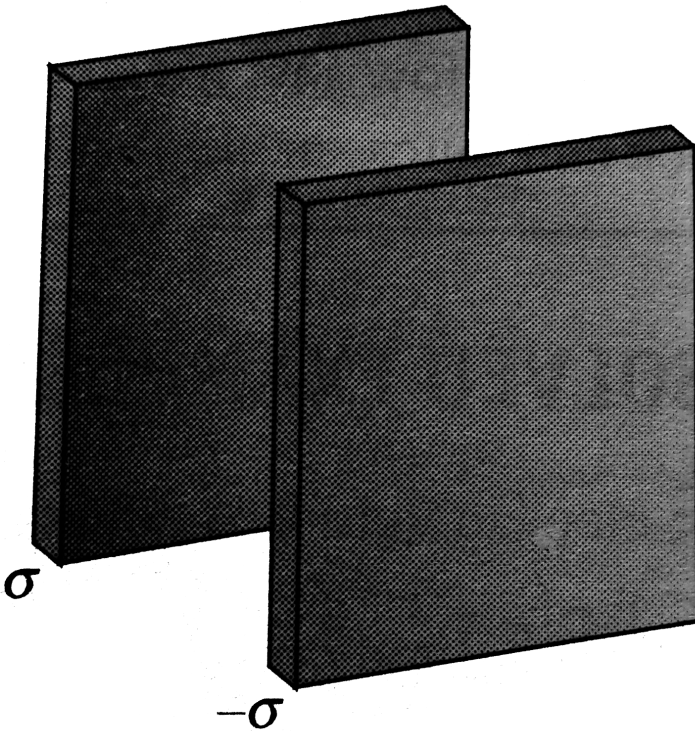


*Courtesy NCA &*



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12. Two infinite, non-conducting sheets of charge are parallel to each other, as shown in figure. The sheet on the left has a uniform surface charge density  $\sigma$ , and the one on the right has a uniform charge density  $-\sigma$ . Calculate the electric field at points (a) to the left of, (b) in between, and (c) to the right of the two sheets.

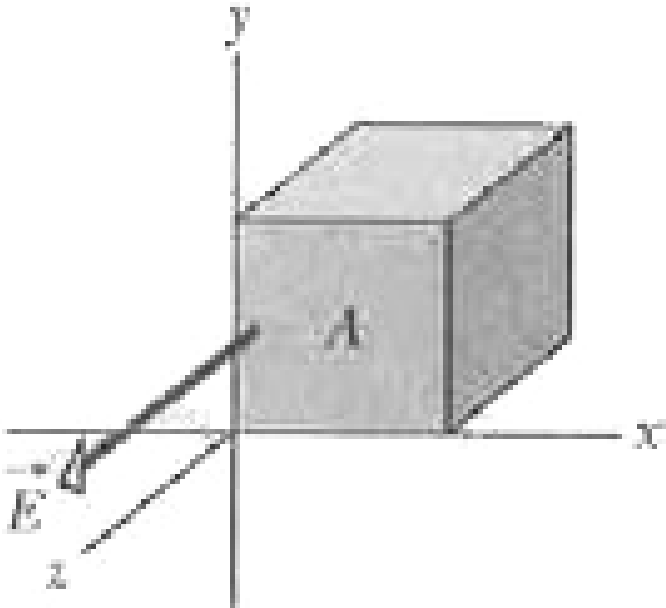


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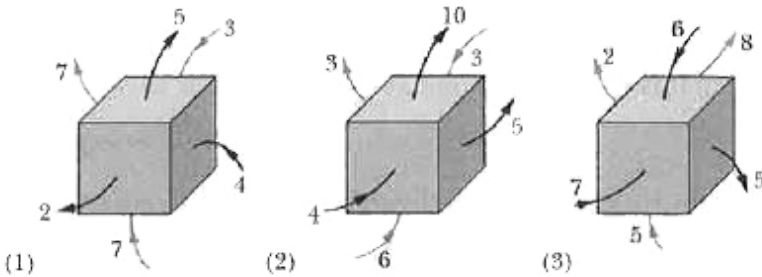
## CHECKPOINT

1. The figure here shows a Gaussian cube of face area  $A$  immersed in a uniform electric field  $\vec{E}$  that has the positive direction of the  $z$  axis. In terms of  $E$  and  $A$ , what is the flux through (a) the front face (which is in the  $xy$  plane), (b) the rear face, (c) the top face, and (d) the whole cube?



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2. The figure shows three situations in which a Gaussian cube sits in an electric field. The arrows and the values indicate the directions of the field lines and the magnitudes (in  $N - m^2 / C$ ) of the flux through the six sides of each cube . (The lighter arrow are for the hidden faces.) In which situation does the cube enclose (a) a positive net charge, (b) a negative net charge, and (c ) zero net charge ?



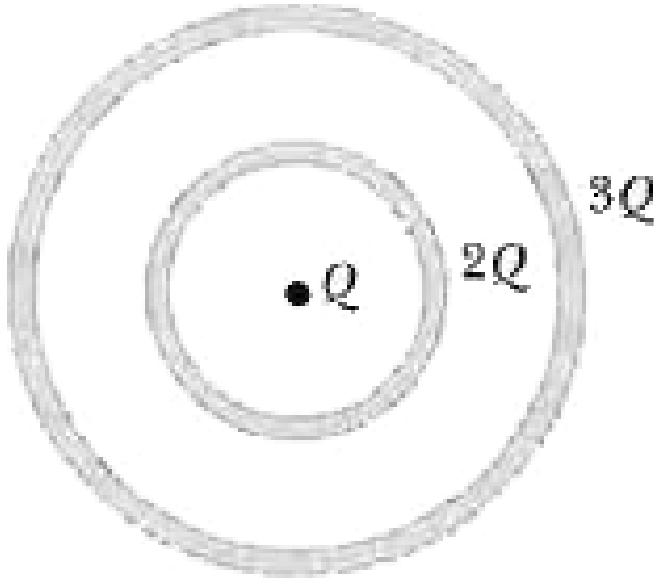
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3. If net flux through a Gaussian surface is zero, then find whether the following statements are correct or not.

The net charge inside the surface is zero.

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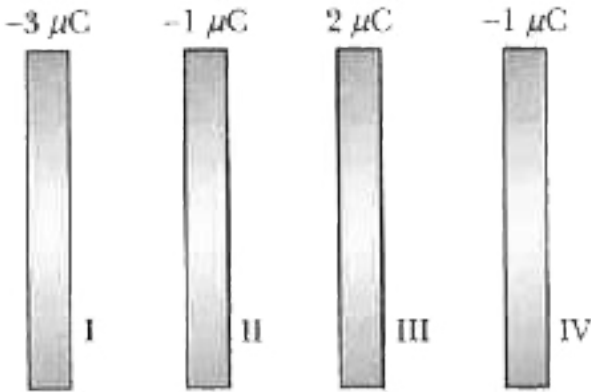
4. As shown in the figure, a charge of  $Q$  is kept in the inner cavity and a charge of  $2Q$  is imparted to the inner shell. A charge of  $3Q$  is imparted to the outermost shell. (a) Find charge at each of the surfaces. (b) Find  $\vec{E}$  in the first annular region and outside.



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5. Four large charged conducting sheets kept parallel to each other. Find the charge on each of the eight faces and electric field in region I, II, III IV

as shown in the figures below.



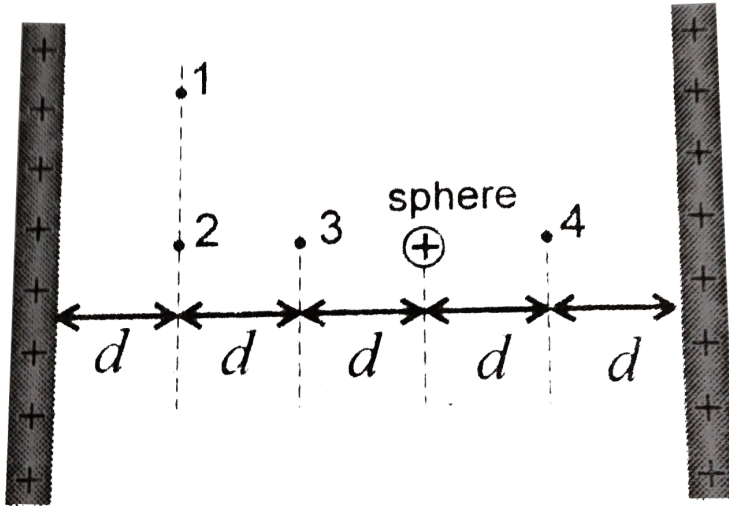
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6. Consider the charges  $q, q$  and  $-q$  placed at the vertices of an equilateral triangle of each side  $l$ . What is the force on each charge ?

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7. The figure shows two large, closely placed, parallel, nonconducting sheets with identical (positive) uniform surface charge densities, and a sphere with a uniform (positive) volume charge density. Four points

marked as 1,2,3, and 4 are shown in the space in between. If  $E_1$ ,  $E_2$ ,  $E_3$ , and  $E_4$  are magnitude of net electric fields at these points, respectively, then



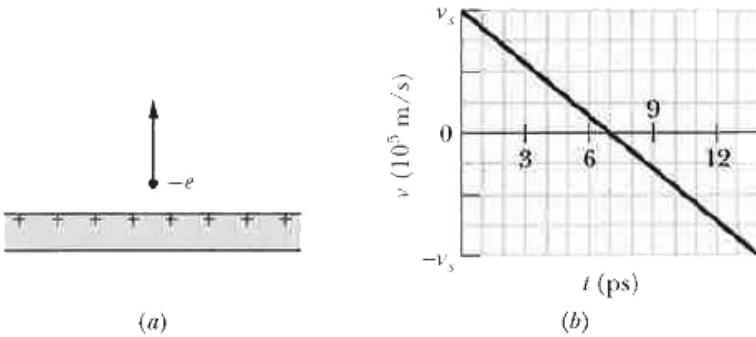
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## PROBLEMS

1. An infinite line charge produces a field of  $7.182 \times 10^8 \text{ N/C}$  at distance of 2 cm. the linear charge density is

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2. an electron is shot directly away from a uniformly charged plastic sheet, at speed  $v_3 = 1.6 \times 10^5 \text{ m/s}$ . The sheet is nonconducting, flat, and very large. Figure 23-41b gives the electron's vertical velocity component  $v$  versus time  $t$  until the return to the launch point. What is the sheet's surface charge density?



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3. A conducting sphere of radius 10 cm has an unknown charge. If the electric field 20 cm from the centre of the sphere is  $1.5 \times 10^3 \text{ N/C}$  and points radially inward, what is the net charge on the sphere?

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4. A spherical conducting shell of inner radius  $s_1$  and outer radius  $r_2$  has a charge  $Q$ . (a) A charge  $q$  is placed at the centre of the shell. What is the surface charge density on the inner and outer surfaces of the shell ?



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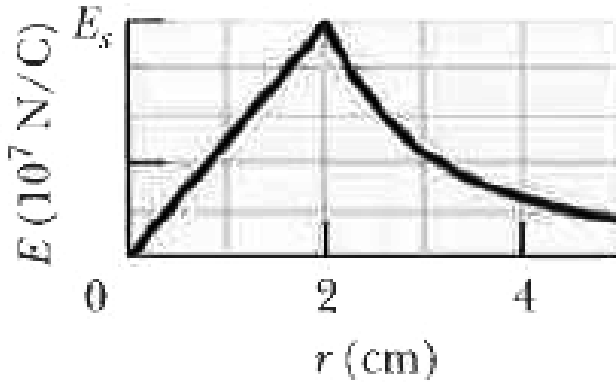
5. A metal spherical shell has an inner radius  $R_1$  and outer radius  $R_2$ . A charge  $Q$  is placed at the center of the spherical cavity. What will be surface charge density on (i) the inner surface, and (ii) the outer surface ?



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6. gives the magnitude of the electric field inside and outside a sphere with a positive charge distributed uniformly throughout its volume. The scale of the vertical axis is set by  $E_x = 10 \times 10^7$  N/C. (a) What is the

charge on the sphere? (b) What is the field magnitude at  $r = 8.0$  m?

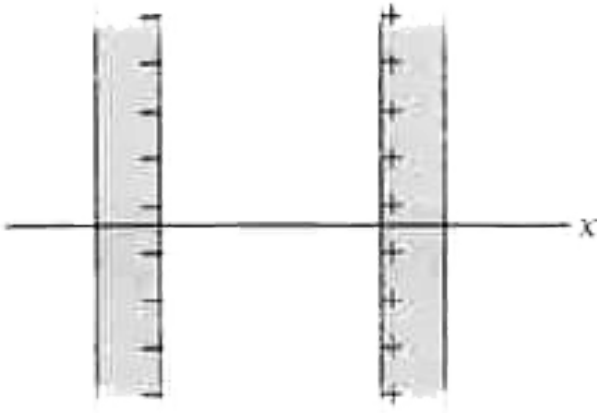


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7. two large, thin metal plates are parallel and close to each other. On their inner faces, the plates have excess surface charge densities of opposite signs and magnitude  $2.31 \times 10^{-22} \frac{C}{m^2}$ . In unit-vector notation, what is the electric field at points (a) to the left of the plates,



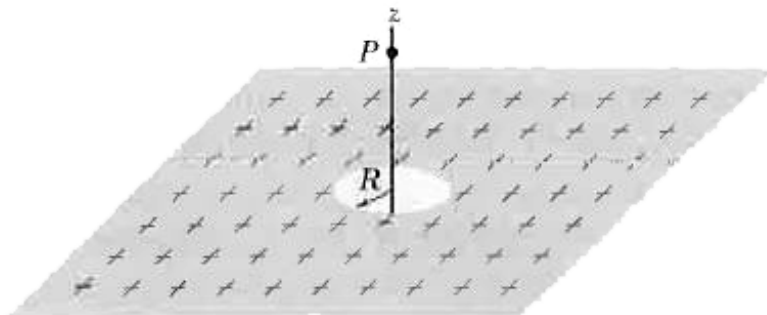
(b) to the right of them, and (c) between them?



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8. a small circular hole of radius  $R=1.30$  cm has been cut in the middle of an infinite, flat, nonconducting surface that has uniform charge density  $\sigma = 4.50 \mu\frac{C}{m^2}$ . A z axis, with its origin at the hole's center, is perpendicular to the surface. In unitvector notation, what is the electric

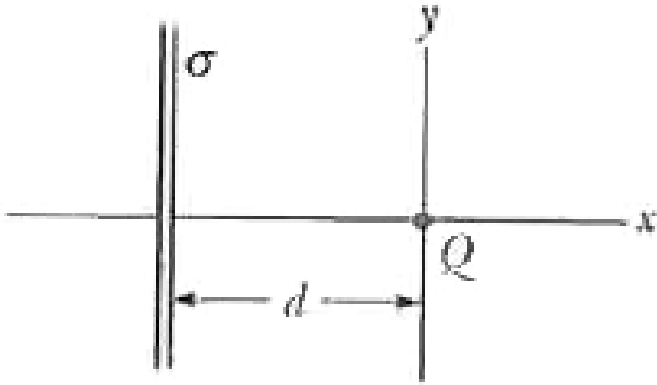
field at point P at  $z = 2.56 \text{ cm}$ ?



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9. shows a very large nonconducting sheet that has a uniform surface charge density of  $\sigma = -2.00 \mu\text{C}/\text{m}^2$  it also shows a particle of charge  $Q = 8.00 \mu\text{C}$ , at ore 2 Problem 9. distance  $d$  from the sheet. Both are fixed in place. If  $d = 0.200 \text{ m}$ , at what (a) positive and (b) negative coordinate on the  $x$  axis (other than infinity) is the net electric field  $\vec{E} \neq t$  of the sheet and particle zero? (c) If  $d = 0.950 \text{ m}$ , at what coordinate on

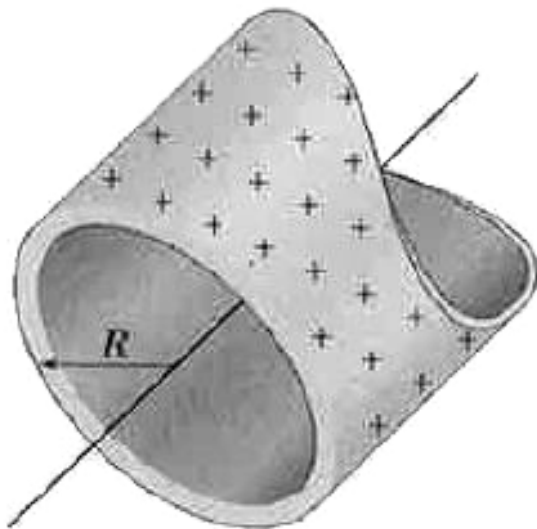
the x axis is  $\int_e - (\neq t) = 0$ ?



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10. shows a section of a long, thin-walled metal tube of radius  $R=2.50$  cm, with a charge per unit length of  $\lambda = 2.00 \times 10^{-8}$  C/m. What is the magnitude  $E$  of the electric field at radial distance (a)  $r = R/2.00$  and (b)  $r$

=  $2.00R$ ? © Graph E versus  $r$  for the range  $r = 0$  to  $2.00R$ .



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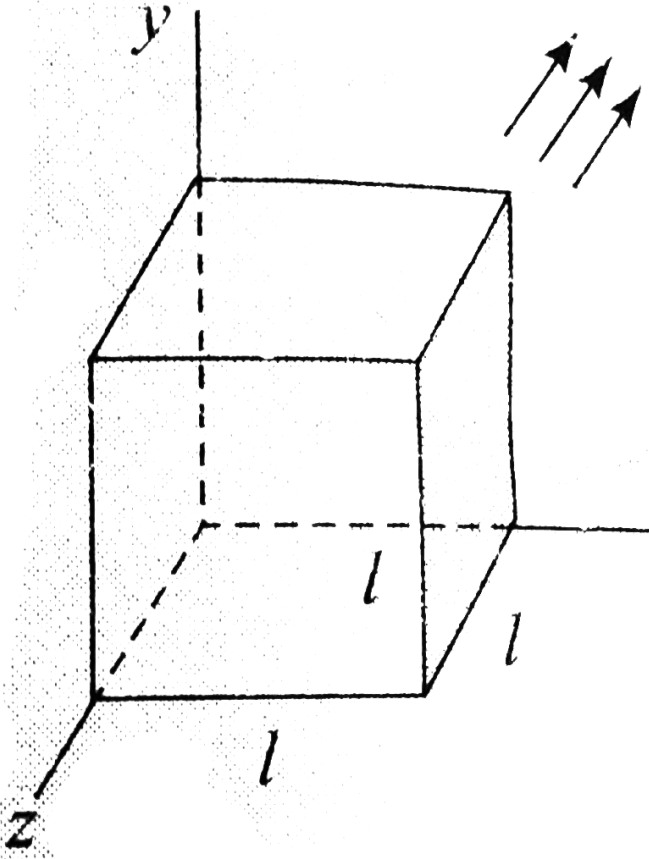
11. A cube of edge length  $l = 2.50\text{cm}$  is positioned as shown in Fig. 3.20.

A uniform magnetic field given by  $\vec{B} = (5.00\hat{i} + 4.00\hat{j} + 3.00\hat{k})\text{T}$

exists throughout the region.

(a) Calculate the flux through the shaded face.

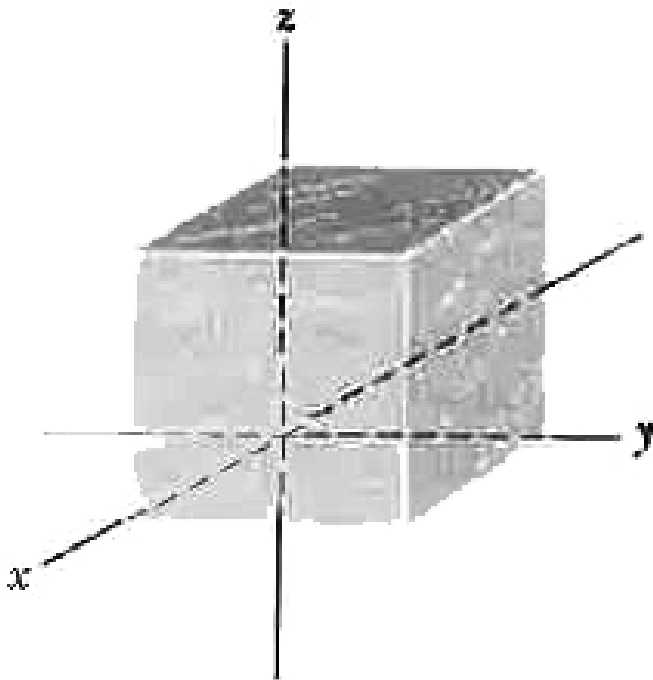
(b) What is the total flux through the six faces ?



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12. At each point on the surface of the cube shown in Fig. 23-47, the electric field is parallel to the  $z$  axis. The length of each edge of the cube

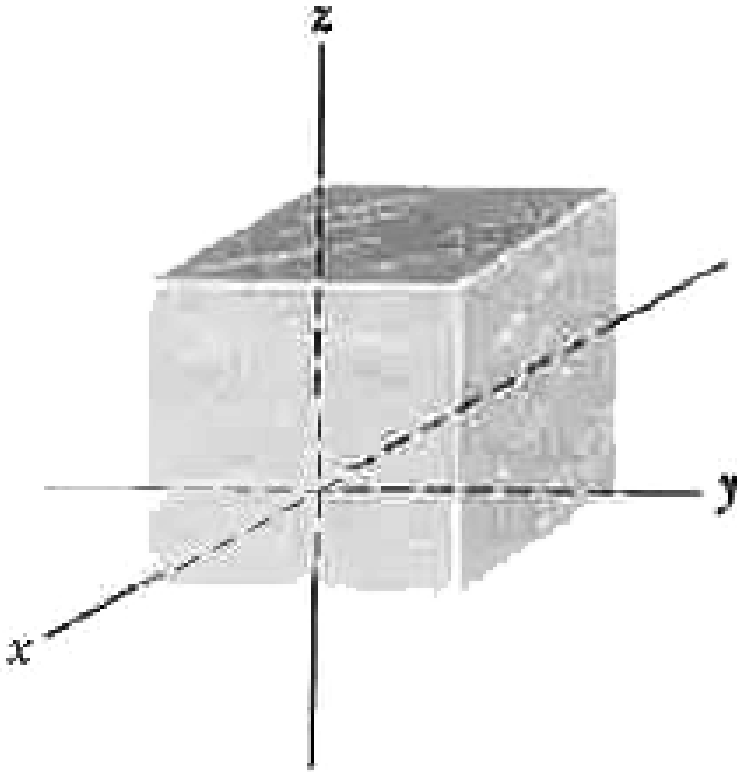
is 4.0 m. On the top face of the cube the field is  $\vec{E} = -34\hat{k}$  N/C, and on the bottom face it is  $\vec{E} = +20\hat{k}$  N/C. Determine the net charge contained within the cube.



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13. shows a Gaussian surface in the shape of a cube with edge length 5.60 m. What are (a) the net flux  $\phi$  through the surface and (b) the net charge  $q_{enc}$  enclosed by the surface if  $\vec{E} = (3.00y\hat{j})$  N/C with  $y$  in meters? What

are (c)  $\phi$  and (d)  $\theta_{enc}$  if  $\vec{E} = \left[ -17.0\hat{i} + (6.00 + 3.00y\hat{j}) \right] \text{ N/C}$ ?



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14. a proton is a distance  $d/2$  directly above the center of a square of side  $d$ . What is the magnitude of the electric flux through the square ?

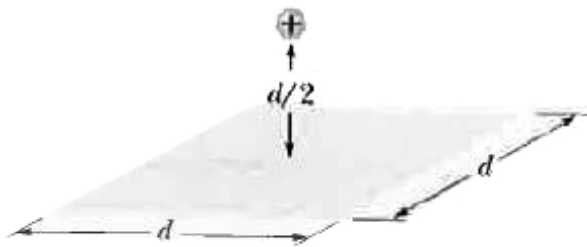


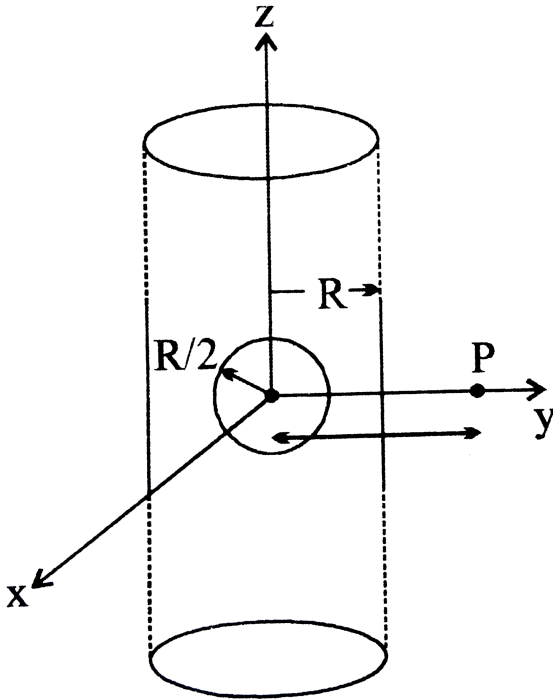
Figure 23-48 Problem 14.

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15. An infinitely long solid cylinder of radius  $R$  has a uniform volume charge density  $\rho$ . It has a spherical cavity of radius  $R/2$  with its centre on the axis of cylinder, as shown in the figure. The magnitude of the electric field at the point  $P$ , which is at a distance  $2R$  from the axis of the



cylinder, is given by the expression  $\frac{23rR}{16ke_0}$ . The value of  $k$  is .

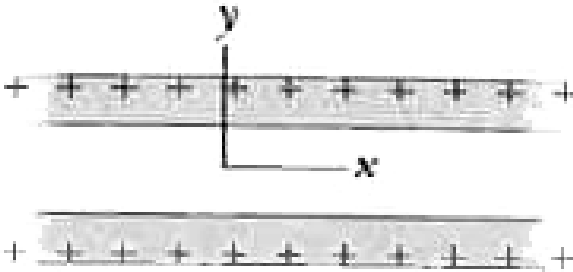


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16. Electric field intensity at a point due to an infinite sheet of charge having surface charge density  $\sigma$  is  $E$ . If sheet were conducting electric intensity would be

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17. show cross section through two large, parallel, nonconducting sheets with identical distributions of positive charge with surface charge density  $\sigma = 2.31 \times 10^{-27} \text{ C/m}^2$ . In unit-vector notation, what is  $\vec{E}$  at points (a) above the sheets, (b) between them, and (c) below them ?

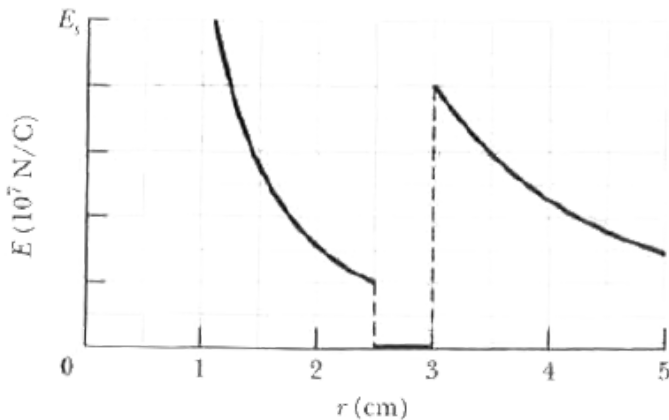


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18. A small non-conducting ball of mass  $m=1\text{mg}$  and charge  $q = 2 \times 10^{-8} \text{ C}$  hangs from an insulating thread that makes an angle  $\theta = 30^\circ$  with vertical uniformly charged non-conducting sheet. Considering the gravitational force on the ball and assuming that the sheet extends for vertically and into out of the page. Calculate surface charge density of sheet.

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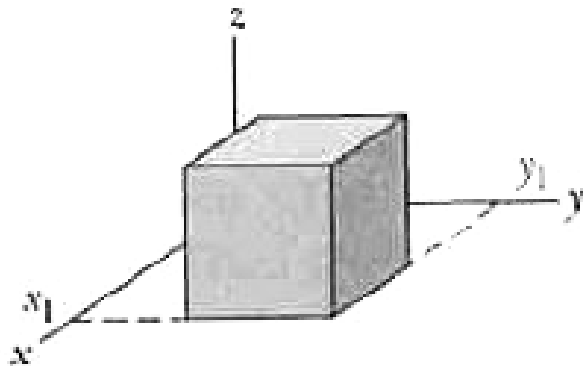
19. A charge particle is held at the center of a spherical shell. Gives the magnitude  $E$  of the electric field versus radial distance  $r$ . The scale of the vertical axis is set by  $E_x = 5.0 \times 10^7 \text{ N/C}$ . Approximately, what is the net charge on the shell ?



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20. shows a close Gaussian surface in the shape of a cube of edge length  $2.00 \text{ m}$ , with one corner at  $x_1 = 5.00 \text{ m}$ ,  $y_1 = 4.00 \text{ m}$ . The cube lies in a region where the electric field vector is given by

$\vec{E} = +23.0\hat{i} - 2.00\hat{j} - 16.0\hat{k} \text{ N/C}$ , with  $y$  in meters. What is the net charge contained by the cube?



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21. Two charge concentric spherical shell have radii  $10.0\text{cm}$  and  $15.0\text{cm}$ . The charge on the inner shell is  $7.50 \times 10^{-8}\text{C}$ , and that on the outer shell is  $6.33 \times 10^{-8}\text{C}$ . Find the electric field (a) at  $r = 12.0\text{cm}$  and (b) at  $r = 20.0\text{cm}$ .

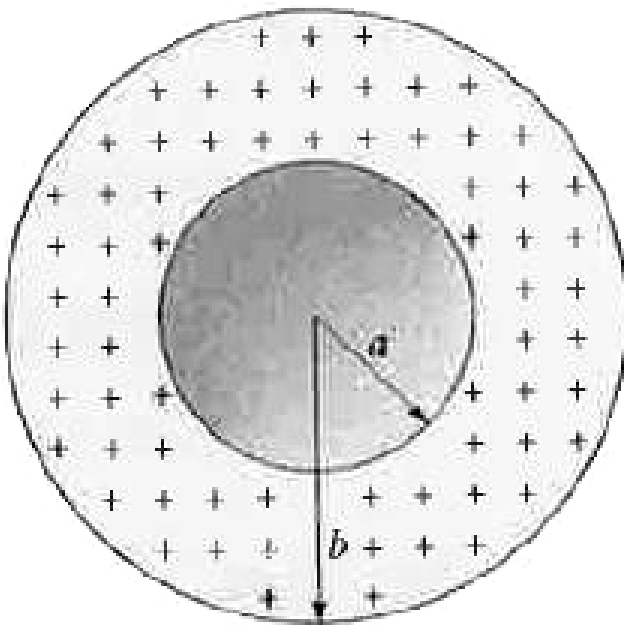
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22. show a spherical shell with uniform volume charge density  $\rho = 1.56 \text{ nC/m}^3$ , inner radius  $a = 10.0 \text{ cm}$  and outer radius  $b = 2.00a$ . What is the magnitude of the electric field at radial distance

(a)

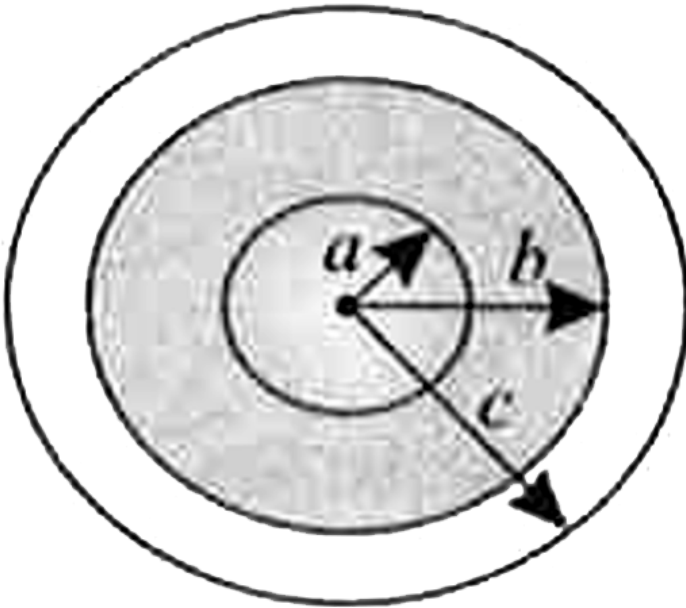
$r = 0$ , (b)  $r = a/2.00$  (c)  $r = a$ , (d)  $r = 1.50a$ , (e)  $r = b$ , and (f)  $r = 3.00b$

?



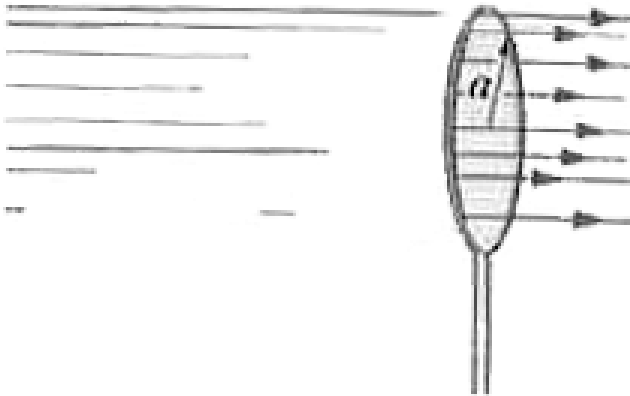
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23. In figure , a solid sphere of radius  $a = 2.00\text{cm}$  is concentric with a spherical conduction shell of inner radius  $b = 2.00 a$  and outer radius  $c = 2.40 a$ . the sphere has a net uniform charge  $q_1 = + 5.00\text{C}$ . The shell has a net charge  $q_2 = - q_1$ . Distance (a)  $r=0$  (b)  $r= a/2.00$  (c)  $r=a$  (d)  $r = 1.50 a$  (e)  $r= 2.30a$  and (f)  $r= 3.50 a$  ? what si the net charge on the (g) inner and (h) outer surface of the shell ?



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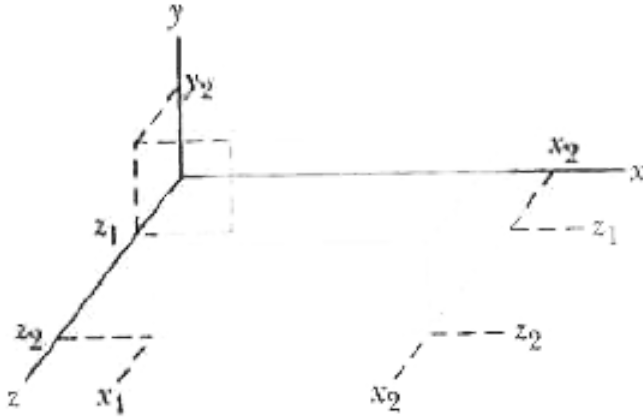
24. a butterfly net is in a uniform electric field of magnitude  $E = 4.5 \text{ mN/C}$ . The rim a circle of radius  $a = 11 \text{ cm}$ , is aligned perpendicular to the field. The net contains no net charge. Find the electric flux through the netting.



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25. The box-like Gaussian surface encloses a net charge of  $+32\epsilon_0 \text{ C}$  and lies in an electric field given by  $\vec{E} = [(10.0 + 2.00x)\hat{i} - 3.00\hat{j} + bz\hat{k}] \text{ N/C}$ , with  $x$  and  $z$  in meters and  $b$  a constant. The bottom face is in the  $xz$  plane, the top face is in the horizontal plane passing through  $y_2 = 1.00 \text{ m}$ , For

$x_1 = 1.00\text{m}$ ,  $x_2 = 4.00\text{m}$ ,  $z_1 = 1.00\text{m}$ , and  $z_2 = 3.00\text{m}$ , what is  $b$  ?



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26. A uniformly charged conducting sphere of 2.4 m diameter has a surface charge density of  $180.0\mu\text{C}/\text{m}^2$  (i) Find the charge on the sphere. (ii) what is the total flux leaving the surface of the sphere ?

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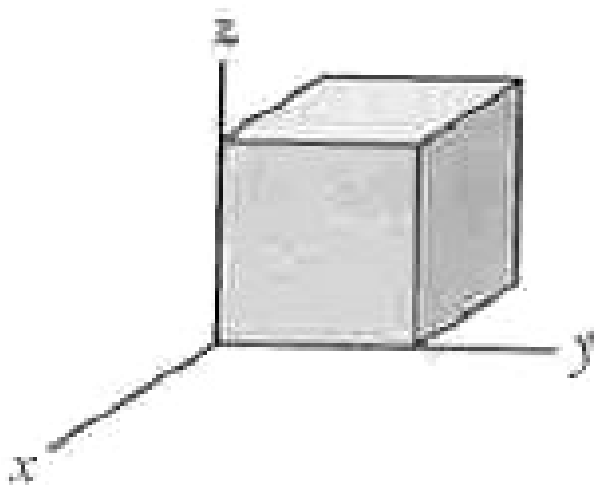
27. A point charge  $q$  is placed at one corner of a cube of edge  $a$ . The flux through each of the cube faces is

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28. shows a closed Gaussian surface in the shape of a cube of edge length  $1.50\text{m}$ . It lies in a region where the nonuniform electric field is given by  $\vec{E} = (3.00 + 4.00)\hat{i} + 6.00\hat{j} + 7.00\hat{k}\text{N/C}$ , with  $x$  in meters.

What is the net charge contained by cube ?



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29. When identical point charges are placed at the vertices of a cube of edge length ' $a$ ' each of them experiences a net force of magnitude  $F$ .

Now these charges are placed on the vertices of another cube of edge length ' $b$ '. What will be magnitude of the net force on any of the charges? These cubes are simply geometrical constructs and not made by any matter.

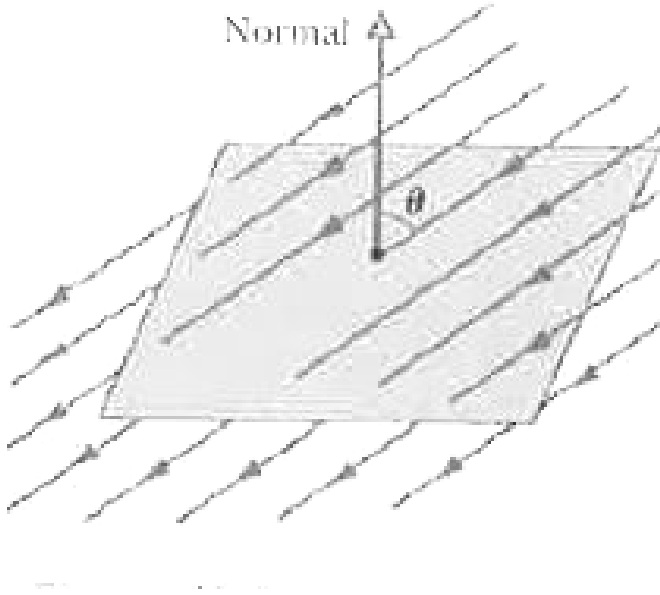
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**30.** The electric field near the surface of the earth is  $300V/m$ . The surface density of charge on the earth's surface is

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**31.** The square surface shown measure  $6.8mm$  on each side. It is immersed in a uniform electric field with magnitude  $E = 1800 N/C$  and with field lines at an angle of  $\theta = 35^\circ$  with a normal to the surface, as shown. Take that normal to be directed "outward," as though the surface were one face of a box (a) Calculate the electric flux through the surface. (b) If the angle is raduced by a few degres, does the flux increase,

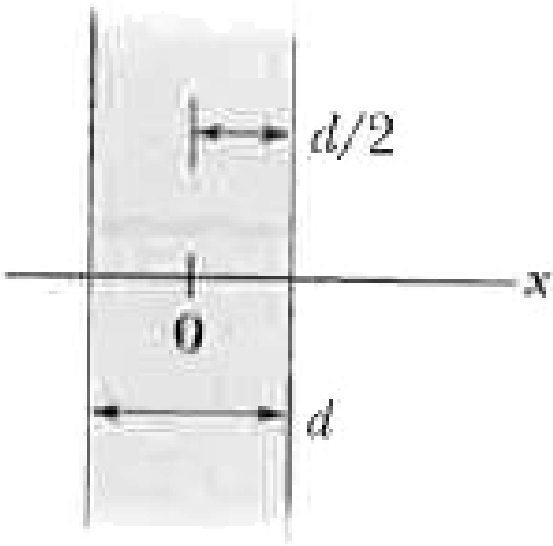
decreases, or remain the same ?



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**32.** shows a cross section through a very large nonconducting slab of thickness  $d = 9.40$  mm and uniform volume charge density  $\rho = 1.89 \text{ fC/m}^3$ . The origin of an x axis is at the slab's center. What is the magnitude of the slab's electric field at an x coordinate of (a) 0, (b)

2.00mm, (c)4.70mm, and (d)26.0mm ?



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33. shows two nonconducting spherical shell fixed in place. Shell 1 has uniform surface charge density  $+6.0\mu\text{C}/\text{m}^2$  on its outer surface and radius  $3.0\text{cm}$ , shell 2 has uniform surface charge density  $+4.0\mu\text{C}/\text{m}^2$  on its inner surface and radius  $2.0\text{cm}$ , the shell centers are separated by  $L = 12\text{cm}$ . In unit vector notation, what is the net electric field at

$$x = 2.0 \text{ cm} ?$$

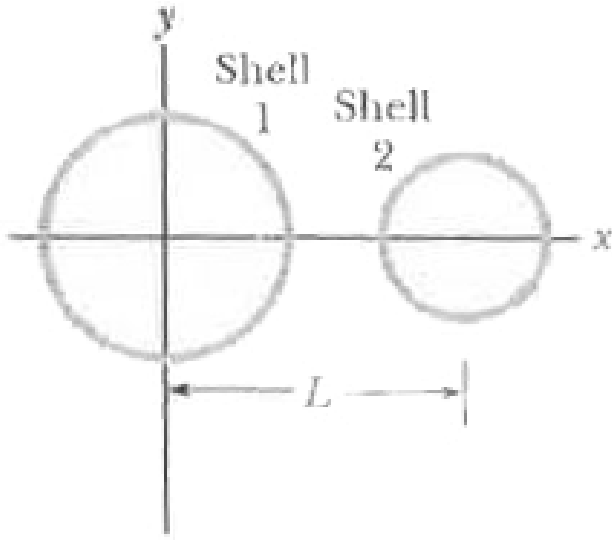


Figure 23-63 Problem 36.



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**34.** Flux and nonconducting shells. A charged particle is suspended at the center of two concentric spherical shells that are very thin and made of nonconducting material. Shows a cross section. Gives the net flux  $\phi$  through a Gaussian sphere centered on the particle, as a function of the radius  $r$  of the sphere. The scale of the vertical axis is set by  $\phi_s = 10 \times 10^5 \text{ N} \cdot \text{m}^2 / \text{C}$  (a) What is the charge of the central particle ?

What are the net charge of (b) shell A and (c) shell B ?

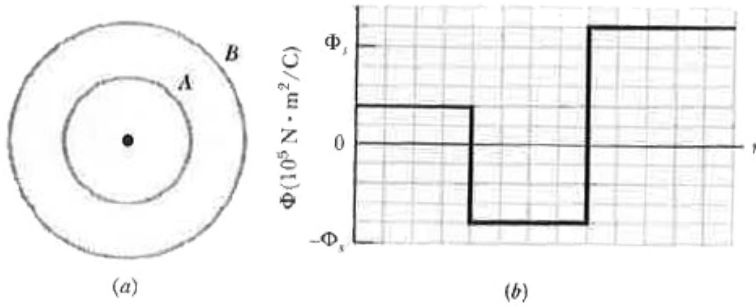
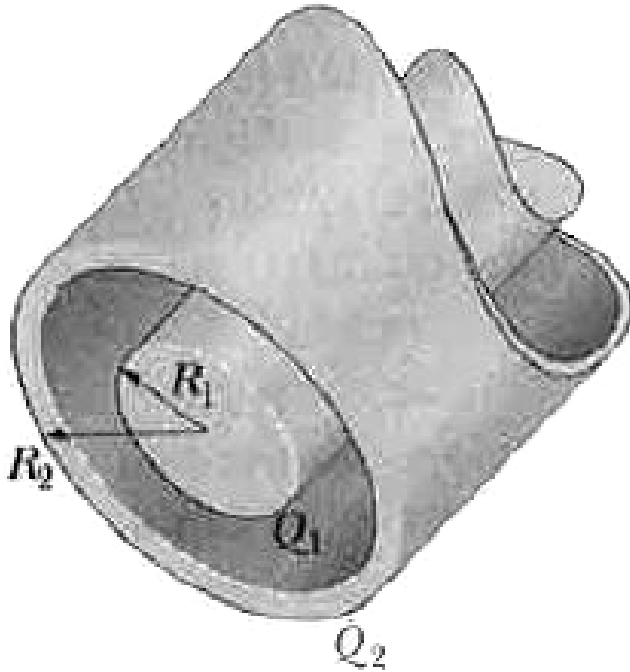


Figure 23-65 Problem 38.

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35. is a section of a conducting rod of radius  $R_1 = 1.30 \text{ mm}$  and length  $L = 11.0 \text{ m}$  inside a thin-walled coaxial conducting cylindrical shell of radius  $R_2 = 10.0R_1$  and the (same) length  $L$ . The net charge on the rod is  $Q_1 = -5.22 \times 10^{-13} \text{ C}$ , that on the shell is  $Q_2 = -2.00Q_1$ . What are the (a) magnitude  $E$  and (b) direction (radially inward or outward) of the electric field at radial distance  $r = 2.00R_2$ ? What are (c)  $E$  and (d) the direction at  $r = 5.00R_1$ ? What is the charge on the (e) interior and

(f) exterior surface of the shell ?



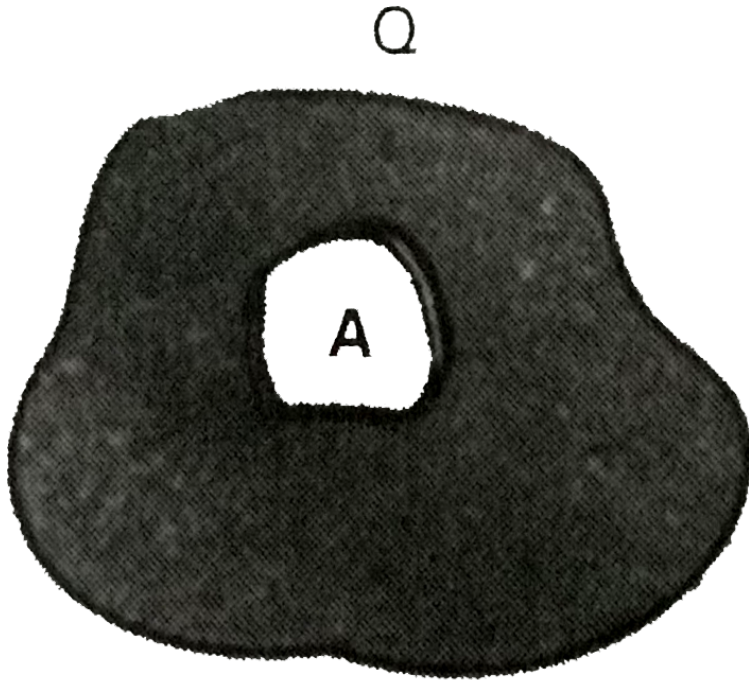
© 23-66 Problem 39.



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**36.** A conductor A with a cavity as shown in Fig. is given a charge  $Q$ . Show that the entire charge must appear on the outer surface of the

conductor.



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37. A metal sphere centered at the origin has a radius  $R$  and a net charge  $Q$ . The electric field at the point  $x = 5R$  is  $E_0$ . The sphere is replaced by a different metal sphere centered at the origin with radius  $2R$  and a net charge  $Q_0$ . The field at  $x = 5R$  is still  $E_0$ . What is the ratio of  $Q$  and  $Q_0$ ?



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**38.** 10 सेमी भुजा तथा नगण्य मोटाई की वर्गाकार चालक प्लेट के पृष्ठ पर 20 मिक्रोकूलोम आवेश एकसामान रूप से विपरत है। (A) प्लेट के केंद्र से 1 मिमी दूरी पर वैधुत क्षेत्र की तीव्रता ज्ञात कीजिए।

(B) प्लेट को बिंदु आवेश मानकर 10 मीटर दूरी पर वैधुत क्षेत्र की तीव्रता ज्ञात कीजिए।

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**39.** An electron is fired directly towards the center of a large metal plate that has excess negative charge with surface charge density  $= 2.0 \times 10^{-6} C/m^2$ . If the initial kinetic energy of electron is 100 eV and if it is to stop due to repulsion just as it reaches the plate, how far from the plate must it be fired ?

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**40.** When a metal slab is placed between the charged identical , parallel plates , the potential difference between the plates



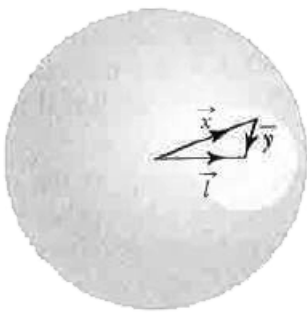
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**41.** Three identical metal plates with large surface areas are kept parallel to each as shown in figure (30-E8). The leftmost plate is given a charge  $Q$ , the rightmost a charge  $-2Q$  and the middle one remains neutral. Find the charge appearing on the outer surface of the rightmost plate.

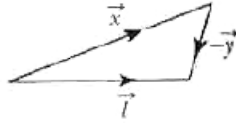


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**42.** If a cavity is made as shown in the uniformly charged sphere find the electric field at an arbitrary point inside the cavity.



(a)



(b)

Figure 23-67 Problem 46.

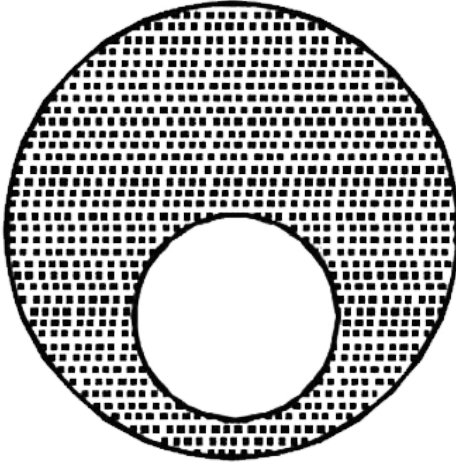


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## PRACTICE QUESTIONS (SINGLE CORRECT CHOICE TYPE)

1. A spherical portion has been removed from a solid sphere having a charge distributed uniformly in its volume as shown in the figure. The

electric field inside the emptied space is



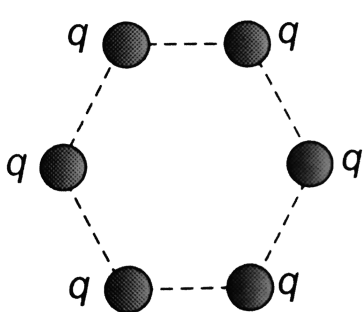
- A. Zero everywhere
- B. Non zero and uniform
- C. Non-uniform
- D. Zero only at its centre

**Answer: A**

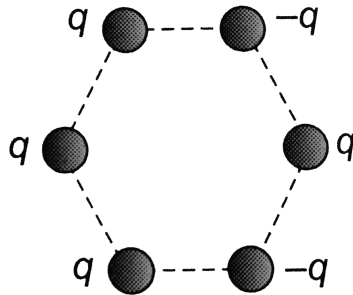


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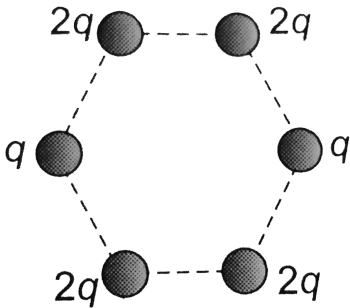
2. Figure below show regular hexagons with charges at the vertices. In which of the following cases the electric field at the centre is not zero



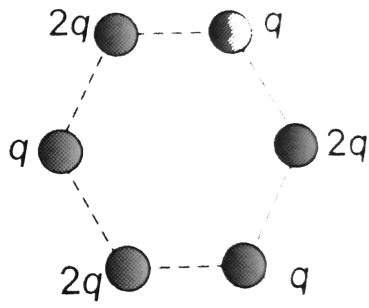
Case (1)



Case (2)



Case (3)



Case (4)

- A. Inside a uniformly charged spherical shell.
- B. In a spherical cavity inside a uniformly charged sphere.
- C. In front of an infinite sheet of uniform surface charge density.
- D. At a distance  $x$  from a point charge  $q$ .

**Answer: D**



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3. For a given surface the Gauss's law is stated as  $\oint \vec{E} \cdot d\vec{A} = 0$ . From this we can conclude that

- A. E is necessarily zero on the surface .
- B. E is perpendicular to the surface at every point.
- C. The total flux through the surface is zero.
- D. The flux is only going out of the surface.

**Answer: C**



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4. If the uniform electric field is  $3 \times 10^3 \hat{i} \text{ NC}^{-1}$ , then the flux of this field through a square of 10 cm on a side whose plane is parallel to the y-z-

plane is?

A.  $30N \cdot m^2 / C$

B.  $40N \cdot m^2 / C$

C.  $50N \cdot m^2 / C$

D.  $60N \cdot m^2 / C$

**Answer: A**



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5. A cubical gaussian surface encloses 24 C of charge. The electric flux through each surface of the cube is

A. zero  $N \cdot m^2 / C$

B.  $4.0 \times 10^5 N \cdot m^2 / C$

C.  $1.6 \times 10^5 N \cdot m^2 / C$

D.  $3.1 \times 10^5 N \cdot m^2 / C$

**Answer: B**



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6. If the electric flux entering and leaving an enclosed surface respectively is  $\phi_1$  and  $\phi_2$ , the electric charge inside the surface will be

A.  $(\phi_1 + \phi_2)\epsilon_0$

B.  $(\phi_1 - \phi_2)\epsilon_0$

C.  $\frac{\phi_1 + \phi_2}{\epsilon_0}$

D.  $\frac{\phi_1 - \phi_2}{\epsilon_0}$

**Answer: B**



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7. A uniformly charged conducting sphere of 2.4 m diameter has a surface charge density of  $80.0\mu\text{C}/\text{m}^2$ . What is the total electric flux leaving the



surface of the sphere?

A.  $1.6 \times 10^6 N \cdot m^2 / C$

B.  $3.2 \times 10^8 N \cdot m^2 / C$

C.  $4.8 \times 10^8 N \cdot m^2 / C$

D.  $6.4 \times 10^8 N \cdot m^2 / C$

**Answer: A**



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**8.** Which of the following is true for electric flux through a Gaussian surface ?

A.  $8.5 \times 10^9 N \cdot m^2 / C$

B.  $1.3 \times 10^7 N \cdot m^2 / C$

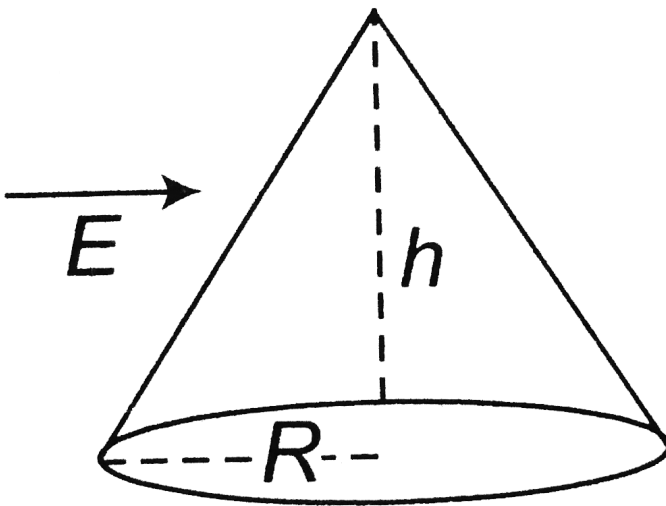
C.  $7.2 \times 10^5 N \cdot m^2 / C$

D.  $6.8 \times 10^8 N \cdot m^2 / C$

Answer: A

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9. A cone lies in a uniform electric field  $E$  as shown in figure. The electric flux entering the cone is



A.  $\frac{1}{2}E\pi R^2$

B.  $E\pi R^2$

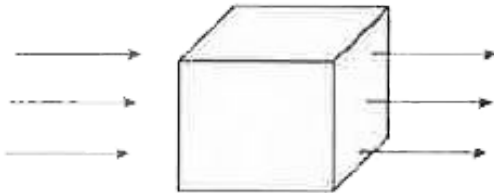
C.  $2E\pi R^2$

D.  $4E\pi R^2$

Answer: B

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10. A cubical Gaussian surface is placed in a uniform electric field as shown in the figure to the right. The length of each edge of the cube is  $1.0\text{m}$ . The uniform electric field has a magnitude of  $5.0 \times 10^8\text{N/C}$  and passes through the left and right sides of the cube perpendicular to the surface. What is the total electric flux that passes through the cubical Gaussian surface?



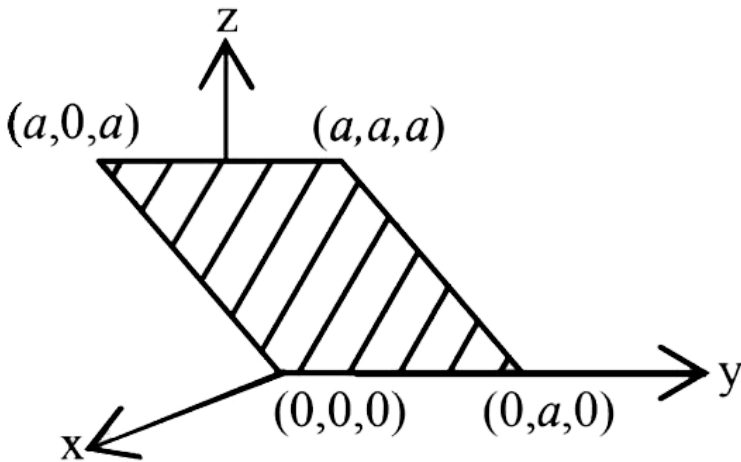
- A.  $5.0 \times 10^8\text{N} \cdot \text{m}^2 / \text{C}$
- B.  $2.5 \times 10^6\text{N} \cdot \text{m}^2 / \text{C}$
- C. zero  $\text{N} \cdot \text{m}^2 / \text{C}$
- D.  $3.0 \times 10^9\text{N} \cdot \text{m}^2 / \text{C}$

Answer: C

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11. Consider an electric field  $\vec{E} = E_0 \hat{x}$  where  $E_0$  is a constant .

The flux through the shaded area (as shown in the figure) due to this field is



A.  $2E_0a^2$

B.  $\sqrt{2}E_0a^2$

C.  $E_0a^2$

D.  $\frac{E_0 a^2}{\sqrt{2}}$

**Answer: C**



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12. A plane surface of area  $200\text{cm}^2$  is kept in a uniform electric field of intensity  $200\text{ N/C}$ . if the angle between the normal to the surface and field is  $60^\circ$ , the electric flux through the surface is

A.  $1.56 \times 10^6\text{ N} \cdot \text{m}^2 / \text{C}$

B.  $1.42 \times 10^5\text{ N} \cdot \text{m}^2 / \text{C}$

C.  $6.60 \times 10^5\text{ N} \cdot \text{m}^2 / \text{C}$

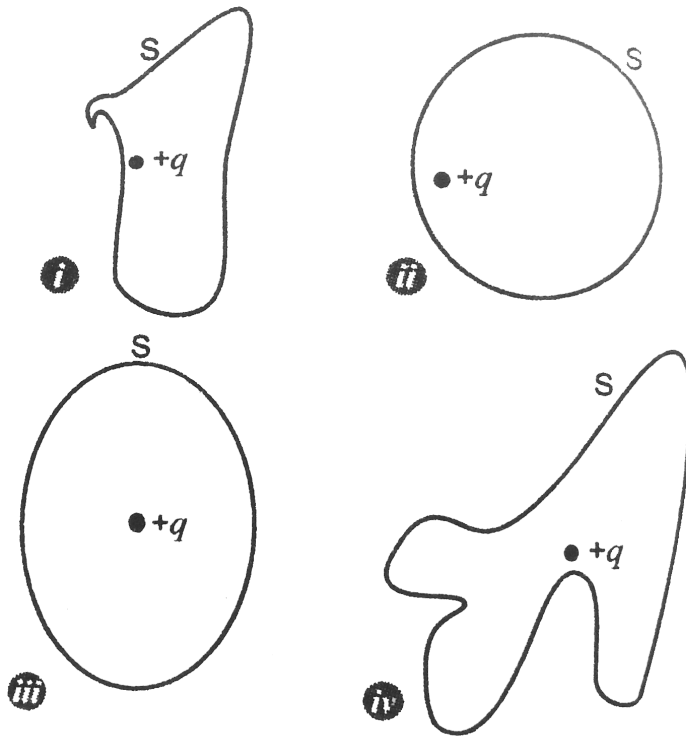
D.  $5.49 \times 10^4\text{ N} \cdot \text{m}^2 / \text{C}$

**Answer: C**



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13. The electric flux through the surface



A.  $46N \cdot m^2 / N$

B.  $220N \cdot m^2 / C$

C.  $92N \cdot m^2 / C$

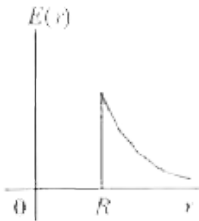
D.  $35N \cdot m^2 / C$

Answer: D

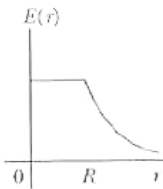


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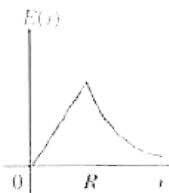
14. A thin spherical shell of radius  $R$  has charge  $Q$  spread uniformly over its surface. Which of the following graphs most closely represents the electric field  $E(r)$  produced by the shell in the range  $0 \leq r < \infty$ , where  $r$  is the distance from the centre of the shell?



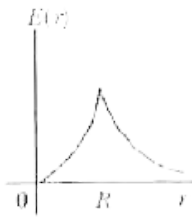
A.



B.



C.



D.

**Answer: A**

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15. Let there be a spherically symmetric charge distribution with charge density varying as  $\rho(r) = \rho \left( \frac{5}{4} - \frac{r}{R} \right)$  upto  $r = R$ , and  $\rho(r) = 0$  for  $r > R$ , where  $r$  is the distance from the origin. The electric field at a distance  $r$  ( $r < R$ ) from the origin is given by

A.  $\frac{\rho_0}{4\epsilon_0} \left( \frac{r}{3} - \frac{r^2}{4R} \right)$

B.  $\frac{\rho_0}{\epsilon_0} \left( \frac{r}{3} - \frac{r^2}{4R} \right)$

C.  $\frac{\rho_0}{3\epsilon_0} \left( \frac{r}{3} - \frac{r^2}{4R} \right)$

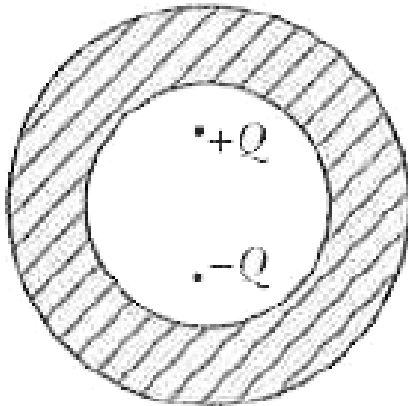
D.  $\frac{\rho_0}{12\epsilon_0} \left( \frac{r}{3} - \frac{r^2}{4R} \right)$



Answer: B

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16. Shown in the figure are two point charges  $+Q$  and  $-Q$  inside the cavity of a spherical shell. The charges are kept near the surface of the cavity on opposite sides of the center of the shell. If  $\sigma_1$  is the surface charge on the inner surface and  $Q_1$  net charge on it and  $\sigma_2$  the surface charge on the outer surface and  $Q_2$  net charge on it then



- A.  $\sigma_1 \neq 0, Q_1 \neq 0$   
 $\sigma_2 \neq 0, Q_2 \neq 0$
- B.  $\sigma_1 \neq 0, Q_1 = 0$   
 $\sigma_2 \neq 0, Q_2 = 0$

- C.  $\sigma_1 \neq 0, Q_1 = 0$   
 $\sigma_2 = 0, Q_2 = 0$
- D.  $\sigma_1 = 0, Q_1 = 0$   
 $\sigma_2 = 0, Q_2 = 0$

**Answer: D**

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17. A uniformly charged conducting sphere of 2.4 m diameter has a surface charge density of  $80.0 \mu\text{C}/\text{m}^2$ . What is the total electric flux leaving the surface of the sphere?

- A.  $2.89 \times 10^5 \text{ N/C}$ , radially inward
- B.  $9.38 \times 10^5 \text{ N/C}$ , radially outward
- C.  $6.49 \times 10^5 \text{ N/C}$ , radially outward
- D.  $1.30 \times 10^6 \text{ N/C}$ , radially inward

**Answer: A**

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18. Consider three different closed surfaces, Surface A is a sphere of radius  $R$ , Surface B is a sphere of radius  $2R$ , and surface C is a cube with side length  $R$ . At the geometric center of each closed surface is a small ball that is completely enclosed by the surface and carries electrical charge  $+q$ . Assuming that there are no other charged objects inside any of the surfaces, rank the surfaces based on the field line flux through them, from largest to smallest.

A.  $A > B > C$

B.  $A > C > B$

C.  $B > C > A$

D. All are equal

**Answer: D**



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19. एक लम्बे सीधे तार में  $3.5A$  विद्युत धारा प्रवाहित हो रही है | तार से  $20\text{ cm}$  पर स्थित किसी बिंदु पर चुम्बकीय क्षेत्र का परिमाण ज्ञात कीजिए |

A.  $1.9 \times 10^{10} N/C$

B.  $6.1 \times 10^{13} N/C$

C.  $4.8 \times 10^{-7} N/C$

D.  $1.5 \times 10^6 N/C$

**Answer: C**



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20. Two spherical shells have a common center. A charge of  $-1.6 \times 10^{-6}$  C is spread uniformly over the inner shell, which has a radius of  $0.050m$ . A charge of  $+5.1 \times 10^{-6}C$  is spread uniformly over the outer shell, which has a radius of  $0.15m$ . Find the magnitude and direction of the electric field at distance (measured from the common center) of  $0.20m$ .

A.  $7.9 \times 10^5 \text{ N/C}$ , radially outward

B.  $5.9 \times 10^5 \text{ N/C}$ , radially inward

C.  $3.2 \times 10^5 \text{ N/C}$ , radially outward

D. zero N/C

**Answer: A**

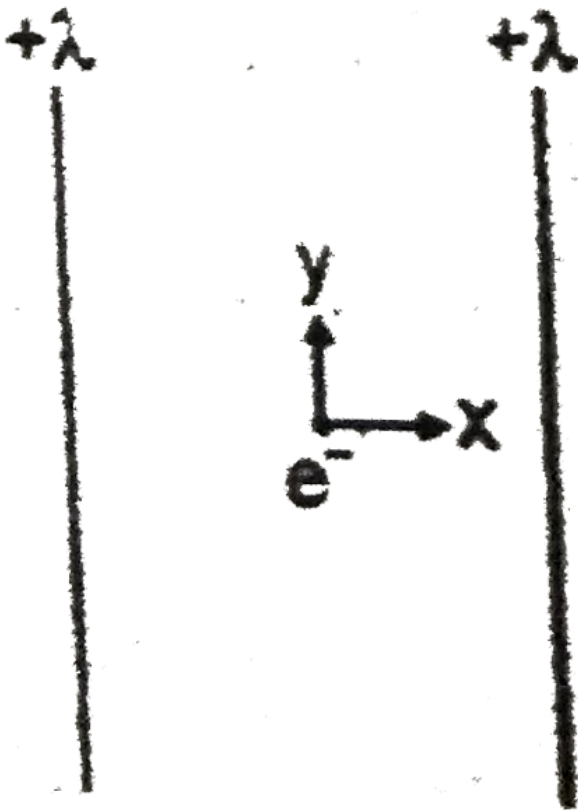


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## PRACTICE QUESTIONS (MORE THAN ONE CORRECT CHOICE TYPE)

1. An electron is placed just in the middle between two long fixed line charges of charge density  $+\lambda$  each. The wires are in the  $xy$  plane (do not

consider gravity)



- A. The equilibrium of the electron will be unstable along  $x$  direction.
- B. The equilibrium of the electron will be neutral along  $y$  direction.
- C. The equilibrium of the electron will be stable along  $z$  direction.
- D. The equilibrium of the electron will be stable along  $y$  direction.

Answer: A::B::C



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2. A non conducting solid sphere of radius  $R$  is uniformly charged. The magnitude of electric field intensity due to the sphere at a distance  $r$  from its centre

- A. Increases as  $r$  increases for  $r < R$
- B. Decreases as  $r$  increases for  $0 < r < R$
- C. Decreases as  $r$  increases for  $R < r < \infty$
- D. Is discontinuous at  $r = R$

**Answer: A::C**



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**PRACTICE QUESTIONS (LINKED COMPREHENSION)**

1. A sphere of charges of radius  $R$  carries a positive charge whose volume charge density depends only on the distance  $r$  from the ball's centre as  $\rho = \rho_0 \left(1 - \frac{r}{R}\right)$ , where  $\rho_0$  is constant. Assume  $\epsilon_0$  as the permittivity of space.

The magnitude of the electric field as a function of the distance  $r$  outside the ball is given by

A.  $E = \frac{\rho_0 R^3}{8\epsilon_0 r^2}$

B.  $E = \frac{\rho_0 R^3}{12\epsilon_0 r^2}$

C.  $E = \frac{\rho_0 R^3}{16\epsilon_0 r^2}$

D.  $E = \frac{\rho_0 R^3}{24\epsilon_0 r^2}$

**Answer: B**



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2. A sphere of charges of radius  $R$  carries a positive charge whose volume charge density depends only on the distance  $r$  from the ball's centre as



$\rho = \rho_0 \left(1 - \frac{r}{R}\right)$ , where  $\rho_0$  is constant. Assume epsilon as the permittivity of space.

The value of distance  $r_m$  at which electric field intensity is maximum is given by

A.  $r_m = \frac{R}{3}$

B.  $r_m = \frac{3R}{2}$

C.  $r_m = \frac{2R}{3}$

D.  $r_m = \frac{4R}{3}$

**Answer: C**



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3. A sphere of charges of radius  $R$  carries a positive charge whose volume charge density depends only on the distance  $r$  from the ball's centre as  $\rho = \rho_0 \left(1 - \frac{r}{R}\right)$ , where  $\rho_0$  is constant. Assume epsilon as the permittivity of space.

the maximum electric field intensity is

A.  $\frac{\rho_0 R}{9\epsilon}$

B.  $\frac{\rho_0 \epsilon}{9R}$

C.  $\frac{\rho_0 R}{3\epsilon}$

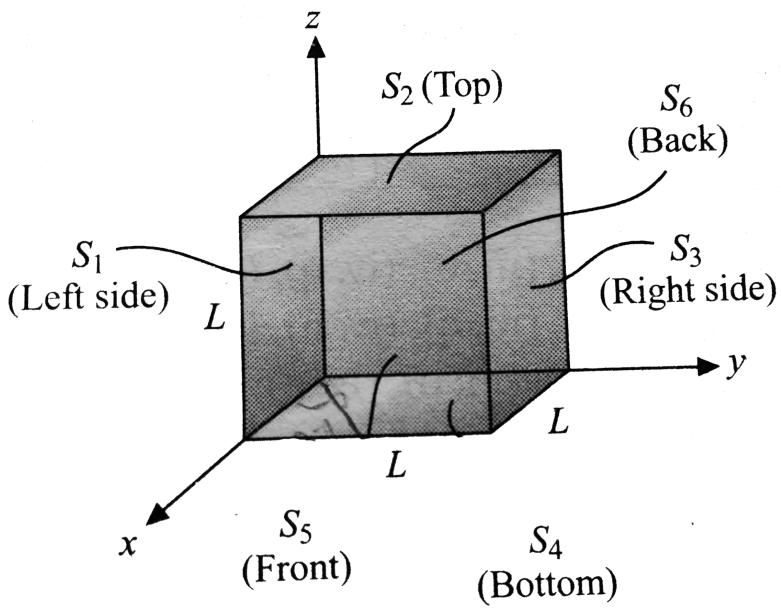
D.  $\frac{\rho_0 R}{6\epsilon}$

**Answer: A**



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4. The cube shown in Fig. 2.119 has sides of length  $L = 10.0\text{cm}$  . The electric field is uniform , has a magnitude  $E = 4.00 \times 10^3 \text{NC}^{-1}$  and is parallel to the  $xy$  plane at an angle of  $37^\circ$  measured from the  $+x$  - axis toward the  $+y$ - axis .



The surface that have zero flux are

- A.  $S_1$  and  $S_3$
- B.  $S_5$  and  $S_6$
- C.  $S_2$  and  $S_4$
- D.  $S_1$  and  $S_2$

**Answer: C**



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5. The cube shown in Fig. 2.119 has sides of length  $L = 10.0\text{cm}$  . The electric field is uniform , has a magnitude  $E = 4.00 \times 10^3 \text{NC}^{-1}$  and is parallel to the  $xy$  plane at an angle of  $37^\circ$  measured from the  $+x$  - axis toward the  $+y$  - axis .



Electric flux passing through surface  $S_1$  is

A.  $-24\text{N} \cdot \text{m}^2 / \text{C}$

B.  $24\text{N} \cdot \text{m}^2 / \text{C}$

C.  $32\text{N} \cdot \text{m}^2 / \text{C}$

D.  $-32\text{N} \cdot \text{m}^2 / \text{C}$

**Answer: A**



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6. The cube shown in Fig. 2.119 has sides of length  $L = 10.0\text{cm}$  . The electric field is uniform , has a magnitude  $E = 4.00 \times 10^3 \text{NC}^{-1}$  and is parallel to the  $xy$  plane at an angle of  $37^\circ$  measured from the  $+x$  - axis

toward the  $+y - a\xi s$ .



Electric flux passing through surface  $S_6$  is

A.  $-24N \cdot m^2 / C$

B.  $24N \cdot m^2 / C$

C.  $32N \cdot m^2 / C$

D.  $-32N \cdot m^2 / C$

**Answer: D**



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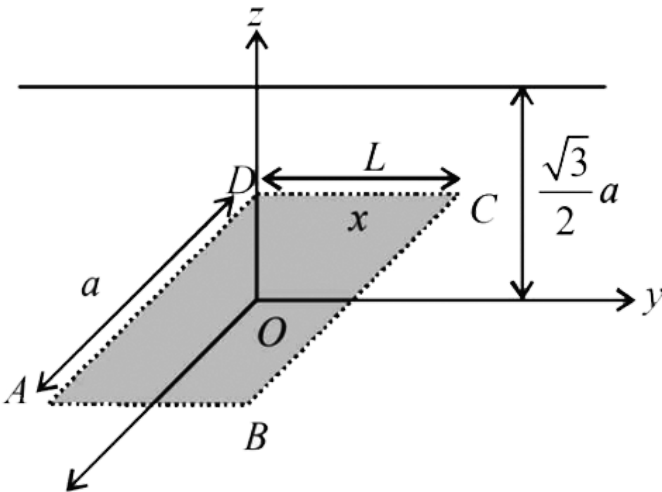
### PRACTICE QUESTIONS (INTEGER TYPE)

1. A parallel plate capacitor of capacitance  $3\mu F$  has total charge  $+15\mu C$  on one plate and total charge  $-15\mu C$  on the other plate. The separation

between the plates is 1mm. The electric field between the plates has magnitude: (in N/C)

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2. An infinity long uniform line charge distribution of charge per unit length  $\lambda$  lies parallel to the  $y$ -axis in the  $y - z$  plane at  $z = \frac{\sqrt{3}}{2} a$  (see figure). If the magnitude of the flux of the electric field through the rectangular surface ABCD lying in the  $x - y$  plane with its centre at the origin is  $\frac{\lambda L}{\epsilon_0}$  ( $\epsilon_0 =$  permittivity of free space), then the value of  $n$  is



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3. A system consists of a ball of radius  $R$  carrying spherically symmetric charge and the surrounding space filled with a charge of volume density  $\rho = \alpha/r$ , where  $\alpha$  is a constant,  $r$  is the distance from the centre of the ball. Find the ball's the charge at which the magnitude of the electric field strength vector is independent of  $r$  outside the ball. How high is this strength? The permittives of the ball and the surrounding space are assumed to be equal to unity.



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