



MATHS

BOOKS - CENGAGE

DETERMINANT

Solved Examples And Exercises

1. If $f(\theta) = \begin{vmatrix} \sin^2 A & \cot A & 1 \\ \sin^2 B & \cos B & 1 \\ \sin^2 C & \cos C & 1 \end{vmatrix}$, then (a) $\tan A + \tan B + \tan C$ (b) $\cot A \cot B \cot C$ (c)

$\sin^2 A + \sin^2 B + \sin^2 C$ (d) 0



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2. Let $\Delta(x) = \begin{vmatrix} 3 & 3x & 3x^2 + 2a^2 \\ 3x & 3x^2 + 2a^2 & 3x^3 + 6a^2x \\ 3x^2 + 2a^2 & 3x^3 + 6a^2x & 3x^4 + 12a^2x^2 + 2a^4 \end{vmatrix}$ then

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3. The determinant $\Delta = \begin{vmatrix} (a^2 + x) & ab & ac & ab \\ (b^2 + x) & bc & ac & bc \\ (c^2 + x) & & & \end{vmatrix}$ is divisible by a.x b. x^2 c. x^3 d. none of these

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4. If $f(x) = \begin{vmatrix} a & -1 & 0 \\ ax & a & -1 \\ ax^2 & ax & a \end{vmatrix}$, then $f(2x) - f(x)$ is divisible by (a) a (b) b (c) c, d, e

(d) none of these

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5. If $(x) = |x^2 + 4x - 3 \quad 2x + 4 \quad 13 \quad 2x^2 + 5x - 9 \quad 4x + 5 \quad 26 \quad 8x^2 - 6x + 1 \quad 16 \quad x - 6 \quad 104| = a x^3 + b x^2 + c x + d$, then $a = 3b$, $b = 0$, $c = 0$, $d = 0$ d. none of these

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6. If $|x^n x^{n+2} x^{2n} 1 x^a a x^{n+5} x^{a+6} x^{2n+5}| = 0, \forall x \in R$, where $n \in N$, then value of a is n b. $n - 1$ c. $n + 1$ d. none of these

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7. Let $x < 1$, then value of $\begin{bmatrix} x^2 + 2 & 2x + 1 & 1 \\ 2x + 1 & x + 2 & 1 \\ 3 & 3 & 1 \end{bmatrix}$ is a. none-negative b. none-positive c. negative d. positive

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8. If $f(x) = \begin{vmatrix} 0 & x-a & x-b \\ x+a & 0 & x-c \\ x+b & x+c & 0 \end{vmatrix}$ then

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9. Value of $\begin{bmatrix} x+y & z & z \\ x & y+z & x \\ y & y & z+x \end{bmatrix}$, where x, y, z are nonzero real number, is equal to xyz b. $2xyz$ c. $3xyz$ d. $4xyz$

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10. Which of the following is not the root of the equation

$$\begin{vmatrix} x & -6 & -1 \\ 2 & -3x & x-3 \\ -3 & 2x & x+2 \end{vmatrix} = 0? \text{ a. } 2 \text{ b. } 0 \text{ c. } 1 \text{ d. } -3$$

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11. If A,B,C are the angles of a non right angled triangle ABC. Then find the

value of:
$$\begin{vmatrix} \tan A & 1 & 1 \\ 1 & \tan B & 1 \\ 1 & 1 & \tan C \end{vmatrix}$$

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12. If $f(x) = |x^3 - ax^2 + ax^2 - x^3| = 0$, then $f'(x) = 0$ and $f''(x) = 0$ has common root $f''(x) = 0$ and $f'(x) = 0$ has common root sum of roots of $f(x) = 0$ is $-3a$ none of these

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13. Evaluate
$$\begin{bmatrix} \cos\alpha\cos\beta & \cos\alpha\sin\beta & -\sin\alpha \\ -\sin\beta & \cos\beta & 0 \\ \sin\alpha\cos\beta & \sin\alpha\sin\beta & \cos\alpha \end{bmatrix} = 0$$

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14. Roots of the equation $|xmn1axn1abx1abc1| = 0$ are independent of m , and n independent of a, b , and c depend on m, n , and a, b, c independent of m, n and a, b, c



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15. Prove that the value of determinants is zero:

$$\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix} = 0$$



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16. If a, b, c are different, then the value of

$$\begin{vmatrix} 0 & a & b & c \\ a & 0 & b & c \\ b & a & 0 & c \\ c & b & c & 0 \end{vmatrix} = 0$$



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17. Prove that the value of each the following determinants is zero:

$$\begin{vmatrix} a_1 & la_1 + mb_1 & b_1 \\ a_2 & la_2 + mb_2 & b_2 \\ a_3 & la_3 + mb_3 & b_3 \end{vmatrix}$$

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18. If $|b + + aa + ba + + + ac + aa + + c| = k|abaca|$, then value of k is 1 b.

2 c. 3 d. 4

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19. A triangle has vertices $A_i(x_i, y_i)$ for $i = 1, 2, 3$. If the orthocentre of triangle is $(0, 0)$, then prove that

$$x_2 - x_3 y_2 - y_3 y_1 (y_2 - y_3) + x_1 (x_2 - x_3) x_3 - x_1 y_2 - y_3 y_2 (y_3 - y_1) + x_1 (x_3 - x_1) x_1 -$$

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20. If α, β, γ are the roots of

$$ax^3 + bx^2 + cx + d = 0 \text{ and } |\alpha\beta\gamma\beta\gamma\alpha\gamma\alpha\beta| = 0, \alpha \neq \beta \neq \gamma \text{ then find the equation}$$

whose roots are $\alpha + \beta - \gamma, \beta + \gamma - \alpha, \text{ and } \gamma + \alpha - \beta$.

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21. If $\Delta = \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}$ and $\Delta_1 = \begin{vmatrix} a_1 + pb_1 & b_1 + qc_1 & c_1 + ra_1 \\ a_2 + pb_2 & b_2 + qc_2 & c_2 + ra_2 \\ a_3 + pb_3 & b_3 + qc_3 & c_3 + ra_3 \end{vmatrix}$ then

$$\Delta_1 =$$

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22. Prove that the value of each the following determinants is zero:

$$\begin{vmatrix} (a^x + a^{-x})^2 & (a^x - a^{-x})^2 & 1 \\ (b^y + b^{-y})^2 & (b^y - b^{-y})^2 & 1 \\ (c^z + c^{-z})^2 & (c^z - c^{-z})^2 & 1 \end{vmatrix}$$

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23. The value of the determinant $\begin{vmatrix} 1^2 & 2^2 & 3^2 & 4^2 \\ 2^2 & 3^2 & 4^2 & 5^2 \\ 3^2 & 4^2 & 5^2 & 6^2 \\ 4^2 & 5^2 & 6^2 & 7^2 \end{vmatrix}$ is equal to 1 b. 0 c. 2

d. 3

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24. If $f(x) = |1x + 12x(x - 1)(x + 1)x3x(x - 1)x(x - 1)(x - 2)(x + 1)x(x - 1)|$ then $f(500)$ is equal to 0 b. 1 c. 500 d. -500

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25. Show that $\begin{vmatrix} \log x & \log y & \log z \\ \log 2x & \log 2y & \log 2z \\ \log 3x & \log 3y & \log 3z \end{vmatrix} = 0$

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26. If the system of equations $x - ky - z = 0$, $kx - y - z = 0$, $x + y - z = 0$ has a nonzero solution, then the possible value of k are -1, 2 b. 1, 2 c. 0, 1 d. -1, 1

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27.
$$\begin{bmatrix} 1 & 1+p & 1+p+q \\ 2 & 3+2p & 4+3p+2q \\ 3 & 6+3p & 10+6p+3q \end{bmatrix} = 1$$

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28. If
$$\begin{vmatrix} a & b & a\alpha + b \\ b & c & b\alpha + c \\ a\alpha + b & b\alpha + c & 0 \end{vmatrix} = 0$$
, prove that a, b, c , are in G.P. or α is a root of $ax^2 + 2bx + c = 0$

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29. By using properties of determinants, show that :

$$\begin{vmatrix} 1 + a^2 - b^2 & 2ab & -2b \\ 2ab & 1 - a^2 + b^2 & 2a \\ 2b & -2a & 1 - a^2 - b^2 \end{vmatrix} = (1 + a^2 + b^2)^3$$

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30. Which of the following values of α satisfy the equation

$$\begin{vmatrix} (1 + \alpha)^2 & (1 + 2\alpha)^2 & (1 + 3\alpha)^2 \\ (2 + \alpha)^2 & (2 + 2\alpha)^2 & (2 + 3\alpha)^2 \\ (3 + \alpha)^2 & (2 + 2\alpha)^2 & (2 + 3\alpha)^2 \end{vmatrix} = 648\alpha?$$

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31. solve $\begin{vmatrix} 3a & -a + b & -a + c \\ -b + a & 3b & -b + c \\ -c + a & -c + b & 3c \end{vmatrix} = 3(a + b + c)(ab + bc + ca)$

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32. If the system of equations $x + ay = 0$, $az + y = 0$, and $ax + z = 0$ has infinite solutions, then the value of equation has no solution is -3 b. 1 c. 0 d. 3

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33.

$$\begin{bmatrix} 6i & -3i & 1 \\ 4 & 3i & -1 \\ 20 & 3 & i \end{bmatrix}$$

$=x+iy$, then a. $x=3, y=1$ b. $x=1, y=3$ c. $x=0, y=3$ d. $x=0, y=0$

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34. The value of $\begin{vmatrix} yz & zx & xy \\ p & 2q & 3r \\ 1 & 1 & 1 \end{vmatrix}$, where x, y, z are respectively, p th, $(2q)$ th, and

$(3r)$ th terms of an H.P. is a. -1 b. 0 c. 1 d. none of these



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35.

Prove

that

$$\begin{vmatrix} (\beta + \gamma - \alpha - \delta)^4 & (\beta + \gamma - \alpha - \delta)^2 & 1 \\ (\gamma + \alpha - \beta - \delta)^4 & (\gamma + \alpha - \beta - \delta)^2 & 1 \\ (\alpha + \beta - \gamma - \delta)^4 & (\alpha + \beta - \gamma - \delta)^2 & 1 \end{vmatrix} = -64(\alpha - \beta)(\alpha - \gamma)(\alpha - \delta)(\beta - \delta)(\gamma - \delta)$$



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36. Prove that the value of each the following determinants is zero:

$$\begin{vmatrix} \sin^2\left(x + \frac{3\pi}{2}\right) & \sin^2\left(x + \frac{5\pi}{2}\right) & \sin^2\left(x + \frac{7\pi}{2}\right) \\ \sin^{x + \frac{3\pi}{2}} & \sin^{x + \frac{5\pi}{2}} & \sin^{x + \frac{7\pi}{2}} \\ \sin^{x - \frac{3\pi}{2}} & \sin^{x - \frac{5\pi}{2}} & \sin^{x - \frac{7\pi}{2}} \end{vmatrix}$$



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37. The number of values of k for which the lines

$(k + 1)x + 8y = 4k$ and $kx + (k + 3)y = 3k - 1$ are coincident is _____



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38. Prove that $|b + ca - bac + ab - cba + bc - ac| = 3ab - a^3 - b^3 - c^3$

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39. If

$$\left| a^2 b^2 c^2 (a+1)^2 (b+1)^2 (c+1)^2 (a-1)^2 (b-1)^2 (c-1)^2 \right| = k(a-b)(b-c)(c-a),$$

then find the value of k

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40. Statement 1:

$\Delta = |my + nzmq + nrmb + nckz - mxkr - mpkc - ma - nx - ky - np - kq - na - kb|$

is equal to 0. Statement 2: The value of skew symmetric matrix of order 3

is zero.

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41. Prove that $\begin{vmatrix} 1 & 1 & 1 \\ abc & bc & c \\ a^2 & ac & b^2 \end{vmatrix} = 2(a-b)(b-c)(c-a)$

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42. If the determinant $\begin{vmatrix} \cos(\theta+\phi) & \sin\theta & -\cos\theta \\ -\sin(\theta+\phi) & \cos\theta & \sin\theta \\ \cos2\phi & \sin\phi & \cos\phi \end{vmatrix}$ is positive is independent of θ is independent of ϕ none of these

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43. The system of equations $-2x + y + z = a$, $x - 2y + z = b$, $x + y - 2z = c$, has: (a)no solution if $a + b + c \neq 0$ (b)unique solution if $a + b + c = 0$ (c)infinite number of solutions if $a + b + c = 0$ (d)none of these

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44. Show that if $x_1, x_2, x_3 \neq 0$

$$\begin{vmatrix} x_1 + a_1 b_1 a_1 b_2 a_1 b_3 a_2 b_1 x_2 + a_2 b_2 a_2 b_3 a_3 b_1 a_3 b_2 x_3 + a_3 b_3 \\ \cdot \\ \cdot \end{vmatrix} = x_1 x_2 x_3 \left(1 + \frac{a_1 b_1}{x_1} + \right.$$



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45. determinant $\begin{vmatrix} \cos \theta & \sin \theta & -\sin \theta & \cos \theta \end{vmatrix}$



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46. If $\Delta_r = \begin{vmatrix} 2^{r-1} & 2 \cdot 3^{r-1} & 4 \cdot 5^{r-1} \\ \alpha & \beta & \gamma \\ 2^n - 1 & 3^n - 1 & 5^n - 1 \end{vmatrix}$, then find the value of Δ



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47. The values of $k \in R$ for which the system of equations $x + ky + 3z = 0$, $kx + 2y + 2z = 0$, $2x + 3y + 4z = 0$ admits of nontrivial solution is 2 b. $5/2$ c. 3 d. $5/4$

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48. A determinant of second order is made with the elements 0 and 1. Find the number of determinants with non-negative values.

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49. If a, b, c are nonzero real numbers such that $|baabcaacaa| = 0$, then $\frac{1}{a} + \frac{1}{b\omega} + \frac{1}{c\omega^2} = 0$ b. $\frac{1}{a} + \frac{1}{b\omega^2} + \frac{1}{c\omega} = 0$ c. $\frac{1}{a\omega} + \frac{1}{b\omega^2} + \frac{1}{c} = 0$ d. none of these

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50. Prove that the determinant $\begin{bmatrix} x & \sin\theta & \cos\theta \\ -\sin\theta & -x & 1 \\ \cos\theta & 1 & x \end{bmatrix}$ is independent of θ .

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51. Consider the determinant $f(x) = \begin{vmatrix} 0x^2 - ax^3 - bx^2 + a0x^2 + cx^4 + bx - c0 \end{vmatrix}$.

Statement 1: $f(x) = 0$ has one root $x = 0$. Statement 2: The value of skew symmetric determinant of odd order is always zero.

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52. Find the value of $|124 - 130410|$

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53. Consider the system of the equation $kx + y + z = 1$, $x + ky + z = k$, and $x + y + kz = k^2$. Statement 1: System equations has infinite solutions when $k = 1$. Statement 2: If the determinant $\begin{vmatrix} 1 & 1 & 1 \\ k & k & k \\ 1 & k^2 & 1 \end{vmatrix} = 0$, then $k = -1$.

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54. If $a, b, c \in R$, then find the number of real roots of the equation

$$\Delta = \begin{vmatrix} x & c & -b \\ -c & x & a \\ b & -a & x \end{vmatrix} = 0$$

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55. $\Delta = \begin{vmatrix} a & a^2 & 0 \\ 1 & 2a + b & (a + b) \\ 0 & 1 & 2a + 3b \end{vmatrix}$ is divisible by $a + b$ b. $a + 2b$ c. $2a + 3b$ d. a^2

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56. Without expanding at any stage, prove that the value of each of the

following determinants is zero. (1) $\begin{vmatrix} 0 & p-q & p-r \\ q-p & 0 & q-r \\ r-p & r-q & 0 \end{vmatrix}$ (2) $\begin{vmatrix} 41 & 1 & 5 \\ 79 & 7 & 9 \\ 29 & 5 & 3 \end{vmatrix}$ (3)

$$\begin{vmatrix} 1 & w & w^2 \\ w & w^2 & 1 \\ w^2 & 1 & w \end{vmatrix}, \text{ where } w \text{ is cube root of unity}$$

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57. If a, b, c are all positive, and are p^{th} , q^{th} and r^{th} terms of a G.P., show that

$$\begin{vmatrix} \log a & p & 1 \\ \log b & q & 1 \\ \log c & r & 1 \end{vmatrix} = 0.$$

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58. If the entries in a 3×3 determinant are either 0 or 1, then the greatest value of their determinants is



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59. The value of the determinant of n^{th} order, being given by $|x111x111x|$ is $(x - 1)^{n-1}(x + n - 1)$ b. $(x - 1)^n(x + n - 1)$ c. $(1 - x)^{-1}(x + n - 1)$ d. none of these



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60. Solve the equation
$$\begin{bmatrix} x + a & x & x \\ x & x + a & x \\ x & x & x + a \end{bmatrix} = 0, a \neq 0$$



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61. If $a_1b_1, c_1, a_2b_2c_2$ and $a_3b_3c_3$ are three digit even natural numbers and $= |c_1a_1b_1c_2a_2b_2c_3a_3b_3|$, then is divisible by 2 but not necessarily by 4 divisible by 4 but not necessarily by 8 divisible by 8 none of these



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62. If
$$= \begin{vmatrix} abc & b^2c & c^2b \\ abc & c^2a & ca^2 \\ abc & a^2b & b^2a \end{vmatrix} = 0, (a, b, c \in R) \text{ and are all different and nonzero), then prove that } a + b + c = 0.$$

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63. The value of
$$\begin{vmatrix} yz & zx & xy \\ p & 2q & 3r \\ 1 & 1 & 1 \end{vmatrix}, \text{ where } x, y, z \text{ are respectively, } p\text{th, } (2q) \text{ th, and } (3r) \text{ th terms of an H.P. is a. -1 b. 0 c. 1 d. none of these}$$

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64. Show that the determinant
$$\begin{vmatrix} a^2 + b^2 + c^2 & bc & ca & ac & ca & ac & ca & ac & ca & abc \\ a^2 & b^2 & c^2 & bc & ca & ac & ca & ac & ca & abc \\ a^2 & b^2 & c^2 & bc & ca & ac & ca & ac & ca & abc \end{vmatrix}$$
 is always non-negative.





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65. If $x \neq 0, y \neq 0, z \neq 0$ and $\begin{vmatrix} 1+x & 1 & 1 \\ 1+y & 1+2y & 1 \\ 1+z & 1+z & 1+3z \end{vmatrix} = 0$, then

$x^{-1} + y^{-1} + z^{-1}$ is equal to a.1 b.-1 c.-3 d. none of these



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66. If $x \neq y \neq z$ and $\begin{vmatrix} x & x^2 & 1+x^3 \\ y & y^2 & 1+y^3 \\ z & z^2 & 1+z^3 \end{vmatrix} = 0$, then the value of xyz is a.1 b.2 c.-1

d.2



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67.

Prove

that

$$\begin{vmatrix} 2 & \alpha + \beta + \gamma + \delta & \alpha\beta + \gamma\delta \\ \alpha + \beta + \gamma + \delta & 2(\alpha + \beta)(\gamma + \delta) & \alpha\beta(\gamma + \delta) + \gamma\delta(\alpha + \beta) \\ \alpha\beta + \gamma\delta & \alpha\beta(\gamma + \delta) + \gamma\delta(\alpha + \beta) & 2\alpha\beta\gamma\delta \end{vmatrix}$$

[Watch Video Solution](#)68. Solve for x , $|x - 6 - 12 - 3 \times - 3 - 32 \times + 2| = 0$.[Watch Video Solution](#)

69. The value of determinant $\begin{vmatrix} 1 & 1 & 1 \\ C_1^{m+1} & C_1^{m+2} & C_1^m \\ C_2^{m+1} & C_2^{m+2} & C_2^m \end{vmatrix}$ is equal to 1 b. -1 c. 0 d. none of these

[Watch Video Solution](#)70. Solve the equation $|a - xcbcb - xabac - x| = 0$ where $a + b + c \neq 0$.[Watch Video Solution](#)

71. If $a^2 + b^2 + c^2 = -2$ and $f(x) =$

$$\left| \begin{array}{cccc} a + a^2x(1 + b^2) & x(1 + c^2) & x(1 + a^2) & x \\ 1 + b^2x(1 + c^2) & x(1 + a^2) & x(1 + b^2) & x \\ 1 + c^2x(1 + a^2) & x(1 + b^2) & x(1 + c^2) & x \\ 1 + a^2x(1 + b^2) & x(1 + c^2) & x(1 + a^2) & x \end{array} \right|$$

, then $f(x)$ is a polynomial of degree 0 b. 1 c. 2 d. 3



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72. Consider the set A of all determinants of order 3 with entries 0 or 1 only. Let B be the subset of A consisting of all determinants with value 1. Let C be the subset of the set of all determinants with value -1. Then

A. A) C his empty

B. null

C. null

D. null



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73.

Solve:

$$|x^2 - 1x^2 + 2x + 12x^2 + 3x + 12x^2 + x - 12x^2 + 5x - 32x^2 + 4x - 36x^2 - x - 26x^2 - 7x$$

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74. If $|x3636x6x3| = |2x7x7272x| = |45x5x4x45| = 0$, then x is equal to 0 b.
-9 c. 3 d. none of these

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75. If $A_1B_1C_1, A_2B_2C_2$ and $A_3B_3C_3$ are three digit numbers, each of which

is divisible by k , then $\Delta = \begin{vmatrix} A_1 & B_1 & C_1 \\ A_2 & B_2 & C_2 \\ A_3 & B_3 & C_3 \end{vmatrix}$ is

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76. If $f'(x) = |mxmx - pmx + p \cap + pn - pmx + 2nmx + 2n + pmx + 2n - p|$,
 then $y = f(x)$ represents a straight line parallel to x-axis a straight line
 parallel to y-axis parabola a straight line with negative slope

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77. If $\sum_{n=1}^n \alpha_n = an^2 + bn$, where a, b are constants and
 $\alpha_1, \alpha_2, \alpha_3 \in \{1, 2, 3, \dots, 9\}$ and $25\alpha_1, 37\alpha_2, 49\alpha_3$ be three digit number,
 then prove that $|\alpha_1\alpha_2\alpha_3 57925\alpha_1 37\alpha_2 49\alpha_3| = 0$

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78. The determinant $|xp + yxyyp + zyz0xp + yyp + z| = 0$ if x, y, z

A. a) if x, y, z are in AP

B. b) x, y, z are in GP

C. c) x, y, z are in HP

D. d) xy, zy, zx are in AP



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79. Using properties of determinant prove that

$$|a + b + c \quad -c - b - ca \quad a + b + c - a - b - aa + b + c| = 2(a + b)(b + c)(c + a)$$



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80. Show that

$$\begin{vmatrix} xC_r^x C_{r+1}^x C_{r+2}^y C_r^y C_{r+1}^y C_{r+2}^z C_r^z C_{r+1}^z C_{r+1} \\ \wedge \end{vmatrix} = \begin{vmatrix} xC_r^{x+1} C_{r+1}^{x+2} C_{r+2}^y C_r^{y+1} C_{r+1}^{y+2} C \\ \wedge \end{vmatrix}$$



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81. If $\omega \neq 1$ is a cube root of unity and $x + y + z \neq 0$, then prove that

$$\begin{vmatrix} x & y & z & y & z & x & zz & x & y \\ 1 + \omega & \omega + \omega^2 & \omega^2 + 1 & \omega + \omega^2 & \omega^2 + 1 & 1 + \omega & \omega^2 + 1 & 1 + \omega & \omega + \omega^2 \end{vmatrix} = 0 \quad \text{if}$$

$$x = y = z$$



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82. Statement 1: If the system of equation

$$\lambda x + (b - a)y + (c - a)z = 0, (a - b)x + \lambda y + (c - b)z = 0, \text{ and } (a - c)x + (b - c)y + \lambda z = 0$$

has a non trivial solution, then the value of λ is 0. Statement 2: the value of skew symmetric matrix of order 3 is order.



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83. If A, B and C are the angels of a triangle, show that

$$-1 + \cos B \cos C + \cos C \cos A - 1 + \cos A \cos B - 1 + \cos A - 1 + \cos B - 1 + \cos A - 1$$



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84. If α, β, γ are the angles of a triangle and system of equations

$$\cos(\alpha - \beta)x + \cos(\beta - \gamma)y + \cos(\gamma - \alpha)z = 0$$

$$\cos(\alpha + \beta)x + \cos(\beta + \gamma)y + \cos(\gamma + \alpha)z = 0$$

$\sin(\alpha + \beta)x + \sin(\beta + \gamma)y + \sin(\gamma + \alpha)z = 0$ has non-trivial solutions, then

triangle is necessarily a. equilateral b. isosceles c. right angled d. acute angled

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85. Without expanding the determinants, prove that $|103115114111108106104113116| + |113116104108106111115114103| = 0$

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86. Given $a = x/(y - z)$, $b = y/(z - x)$, and $c = z/(x - y)$, where x, y, z are not all zero, then the value of $ab + bc + ca$ is 0 b. 1 c. -1 d. none of these

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87. Find the value of determinant $\left| \left(\sqrt{13} + \sqrt{3}, 2\sqrt{5}, \sqrt{5} \right) \sqrt{15} + \sqrt{26} 5\sqrt{10} 3 + \sqrt{65} \sqrt{15} 5 \right|$

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88. a, b, c are distinct real numbers not equal to one. If $ax + y + z = 0$, $x + by + z = 0$, and $x + y + cz = 0$ have nontrivial solution, then the value of $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c}$ is equal to a. 1 b. -1 c. zero d. none of these

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89. Prove that the value of the determinant

$$\begin{vmatrix} -75 + 3i\frac{2}{3} & -4i5 & -3i84 + 5i\frac{2}{3} + 4i4 - fi9 \end{vmatrix} \text{ is real.}$$

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90. If the system of linear equation $x + y + z = 6$, $x + 2y + 3z = 14$, and $2x + 5y + \lambda z = \mu$ ($\lambda, \mu \in \mathbb{R}$) has a unique solution, then $\lambda = 8$ b. $\lambda = 8, \mu = 36$ c. $\lambda = 8, \mu \neq 36$ d. none of these

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91. If $a_r = (\cos 2r\pi + is \in 2r\pi)^{1/9}$, then prove that

$$|a_1 a_2 a_3 a_4 a_5 a_6 a_7 a_8 a_9| = 0.$$

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92. Let $f(x) = \left| 2\cos^2 x \sin 2x - \sin x \sin 2x 2\sin^2 x \cos x \sin x - \cos x 0 \right|$. Then the value of $\int_0^{\pi/2} [f(x) + f'(x)] dx$ is a. π b. $\pi/2$ c. 2π d. $3\pi/2$

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93. Using properties of determinants, prove that

$$\begin{vmatrix} -a^2 & ab & ac \\ ba & -b^2 & bc \\ ca & cb & -c^2 \end{vmatrix} = 4a^2 b^2 c^2$$

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94. The number of positive integral solutions of the equation

$$\begin{vmatrix} x^3 + 1 & x^2y & x^2z \\ xy^2 & y^3 + 1 & y^2z \\ xz^2 & z^2y & z^3 + 1 \end{vmatrix} = 11 \text{ is}$$

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95. If the value of determinant $|(a,1,1),(1,b,1),(1,1,c)|$ is positive, then

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96. By using properties of determinants. Show that: (i)

$$\begin{vmatrix} x+4 & 2x & 2x \\ 2x & x+4 & 2x \\ 2x & 2x & x+4 \end{vmatrix} = (5x-4)(4-x)^2 \text{ (ii) } \begin{vmatrix} y+k & y & y \\ y & y+k & y \\ y & y & y+k \end{vmatrix} = y^2(3y+k)$$

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97. Using properties of determinants, evaluate $|184089408919889198440|$

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98. if A_1, B_1, C_1, \dots are respectively the cofactors of the elements a_1, b_1, c_1, \dots of the determinant

$$\Delta = \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}, \Delta \neq 0 \text{ then the value of } \begin{vmatrix} B_2 & C_2 \\ B_3 & C_3 \end{vmatrix} \text{ is equal to}$$

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99. Solve for x $|x - 22x - 33 \times - 4x - 42x - 93x - 16x - 82x - 273x - 64| = 0$.

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100. If $\Delta_1 = |x \ a \ x \ b \ a \ a \ x|$ and $\Delta_2 = |x \ b \ a \ x|$ are the given determinants,

then $\Delta_1 = 3(\Delta_2)^2$ b. $\frac{d}{dx}(\Delta_1) = 3\Delta_2$ c.

$\frac{d}{dx}(\Delta_1) = 3(\Delta_2)^2$ d. $\Delta_1 = 3\Delta_2^{2/3}$

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101. Without expanding evaluate the determinant $\begin{vmatrix} \sin \alpha & \cos \alpha & \sin(\alpha + \delta) \\ \sin \beta & \cos \beta & \sin(\beta + \delta) \\ \sin \gamma & \cos \gamma & \sin(\gamma + \delta) \end{vmatrix}$

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102. if $y = \sin mx$, then the value of the determinant

$\begin{vmatrix} y & y_1 & y_2 \\ y_3 & y_4 & y_5 \\ y_6 & y_7 & y_8 \end{vmatrix}$ Where $y_n = \frac{d^n y}{dx^n}$ is

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103. Find the value of the determinant $|1111123413610141020|$

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104. The parameter on which the value of the determinant

$\begin{vmatrix} 1 & a^2 \cos(p-d)x & \cos p x & \cos(p+d)x \\ \sin(p-d)x & \sin p x & \sin(p+d)x & x \end{vmatrix}$ does not depend is a b p c d d x

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105. If $x = cy + bz$, $y = az + cx$, $z = bx + ay$, where x, y, z are not all zeros,

then find the value of $a^2 + b^2 + c^2 + 2abc$

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106. If $\begin{vmatrix} b^2 + c^2 & ab & ac \\ ab & c^2 + a^2 & bc \\ ca & cb & a^2 + b^2 \end{vmatrix} = ka^2b^2c^2$, then the value of k is

a. $a^2b^2c^2$ b. $bc + ca + ab$ c. abc d. none of these

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107. The value of $\left| -1213 + 2\sqrt{22} + 2\sqrt{21}3 - 2\sqrt{22} - 2\sqrt{21} \right|$ is equal to

a. zero b. $-16\sqrt{2}$ c. $-8\sqrt{2}$ d. none of these

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108. Find the following system of equations is consistent, $(a + 1)^3x + (a + 2)^3y = (a + 3)^3$ $(a + 1)x + (a + 2)y = a + 3$ $x + y = 1$, then find the value of a

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109. Prove the identities:
$$\begin{vmatrix} b^2 + c^2 & ab & ac \\ ba & c^2 + a^2 & bc \\ ca & cb & a^2 + b^2 \end{vmatrix} = 4a^2b^2c^2$$

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110. Prove that

$$\begin{bmatrix} 1 + a^2 + a^4 & 1 + ab + a^2b^2 & 1 + ac + a^2c^2 \\ 1 + ab + a^2b^2 & 1 + b^2 + b^4 & 1 + bc + b^2c^2 \\ 1 + ac + a^2c^2 & 1 + bc + b^2c^2 & 1 + c^2 + c^4 \end{bmatrix} = (a - b)^2(b - c)^2(c - a)^2$$

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111. If x, y, z are in A.P., then the value of the determinant are in A.P., then the value of the determinant

$|a + 2a + 3a + 2xa + 3a + 4a + 2ya + 4a + 5a + 2z|$ is a. 1 b. 0 c. $2a$ d. a

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112.

Prove

that

$$\begin{vmatrix} (b+x)(c+x) & (c+x)(a+x) & (a+x)(b+x) \\ (b+y)(c+y) & (c+y)(a+y) & (a+y)(b+y) \\ (b+z)(c+z) & (c+z)(a+z) & (a+z)(b+z) \end{vmatrix} = (a-b)(b-c)(c-a)(x-y)(y-z)(z-x)$$

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113. If $a + b + c = 0$, one root of $\begin{bmatrix} a-x & c & b \\ c & b-x & a \\ b & a & c-x \end{bmatrix} = 0$ is a. $x = 1$ b. $x = 2$

c. $x = a^2 + b^2 + c^2$ d. $x = 0$

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114. Factorize the following

$$3a + b + ca^3 + b^3 + c^3a + b + ca^2 + b^2 + c^2a^4 + b^4 + c^4a^2 + b^2 + c^2a^3 + b^3 + c^3$$

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115. Let $\{D_1, D_2, D_3, D_n\}$ be the set of third order determinant that can be made with the distinct non-zero real numbers a_1, a_2, a_q . Then

$\sum_{i=1}^n D_i = 1$ b. $\sum_{i=1}^n D_i = 0$ c. $D_i - D_j, \forall i, j$ d. none of these

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116. If $g(x) = \frac{f(x)}{(x-a)(x-b)(x-c)}$, where $f(x)$ is a polynomial of degree < 3 ,

then prove that

$$\frac{dg(x)}{dx} = \left| 1af(a)(x-a)^{-2}1bf(b)(x-b)^{-2}1cf(c)(x-c)^{-2} \right| + \left| a^2a1b^2b1c^2c1 \right|$$

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117. If the equation $2x + 3y + 1 = 0$, $3x + y - 2 = 0$, and $ax + 2y - b = 0$ are consistent, then prove that $a - b = 2$.

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118. If w is a complex cube root of unity, then value of

$$= \left| a_1 + b_1 w a_1 w^2 + b_1 c_1 + b_1 w a_2 + b_2 w a_2 w^2 + b_2 c_2 + b_2 w a_3 + b_3 w a_3 w^2 + b_3 c_3 \right|$$

is a. 0 b. -1 c. 2 d. none of these



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119.

Let

$$f(x) = \left| \cos(x + x^2) \sin(x + x^2) - \cos(x + x^2) \sin(x - x^2) \cos(x - x^2) \sin(x - x^2) \right| \sin 2x$$

. Find the value of $f'(0)$



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120. If $f(x)$, $g(x)$ and $h(x)$ are three polynomials of degree 2, then prove that

$$\varphi(x) = \left| f(x)g(x)h(x)f'(x)g'(x)h'(x)f''(x)g''(x)h''(x) \right| \text{ is a constant polynomial}$$



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121. If a, b, c are in G.P. with common ratio r_1 and α, β, γ are in G.P. with common ratio r_2 and equations $ax + \alpha y + z = 0, bx + \beta y + z = 0, cx + \gamma y + z = 0$ have only zero solution, then which of the following is not true? a. $a + b + c$ b. abc c. 1 d. none of these

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122. Show that: $|ab - + ba + abc - aa - + ac| = (a + b + c)(a^2 + b^2 + c^2)$

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123. In triangle ABC , if $\left| \frac{\cot A}{2} \frac{\cot B}{2} \frac{\cot C}{2} \frac{\tan B}{2} + \frac{\tan C}{2} \frac{\tan B}{2} + \frac{\tan A}{2} \frac{\tan A}{2} + \frac{\tan B}{2} \right|$ then the triangle must be a. equilateral b. isosceles c. obtuse angled d. none of these

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124. If $a, b, c, d, e,$ and f are in G.P. then the value of
$$\begin{vmatrix} (a^2) & (d^2) & x \\ (b^2) & (e^2) & y \\ (c^2) & (f^2) & z \end{vmatrix}$$

depends on (A) x and y (B) x and z (C) y and z (D) independent of $x, y,$ and z

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125. Prove that:
$$\begin{vmatrix} (b+c)^2 & a^2 & a^2 \\ b^2 & (c+a)^2 & b^2 \\ c^2 & c^2 & (a+b)^2 \end{vmatrix} = 2abc(a+b+c)^3$$

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126. if $x_i = a_i b_i c_i$, $i = 1, 2, 3$ are three-digit positive integers such that

$$a_1 \quad a_2 \quad a_3$$

each x_i is a multiple of 19 then prove that $b_1 \quad b_2 \quad b_3$ is divisible by

$$c_1 \quad c_2 \quad c_3$$

19.

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127. The system of linear equations $x + \lambda y - z = 0$, $\lambda x - y - z = 0$, $x + y - \lambda z = 0$ has a non-trivial solution for : (1) infinitely many values of λ . (2) exactly one value of λ . (3) exactly two values of λ . (4) exactly three values of λ .

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128. If $pqr \neq 0$ and the system of equations $(p+a)x + by + cz = 0$, $ax + (q+b)y + cz = 0$, $ax + by + (r+c)z = 0$ has nontrivial solution, then

value of $\frac{a}{p} + \frac{b}{q} + \frac{c}{r}$ is -1 b. 0 c. 0 d. ∞ - 2

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129. If $c < 1$ and the system of equations $x + y - 1 = 0$, $2x - y - c = 0$, and $bx + 3by - c = 0$ is consistent, then the possible real values of b are $a. b\left(-3\frac{3}{4}\right)$ b. $b\left(-\frac{3}{2}, 4\right)$ c. $b\left(-\frac{3}{4}, 3\right)$ d. none of these



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130. Prove that

$$\begin{vmatrix} x^2 & x^2 - (y - z)^2 & yz \\ y^2 & y^2 - (z - x)^2 & zx \\ z^2 & z^2 - (x - y)^2 & xy \end{vmatrix} = (x - y)(y - z)(z - x)(x + y + z)(x^2 + y^2 + z^2)$$



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131. If a, b and c are real numbers, and

$$\Delta = \begin{vmatrix} b+c & c+a & a+b \\ c+a & a+b & b+c \\ a+b & b+c & c+a \end{vmatrix} = 0$$

Show that either $a + b + c = 0$ or $a = b = c$.

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132. If a, b, c are non-zero, then the system of equations $(\alpha + a)x + \alpha y + \alpha z = 0$, $\alpha x + (\alpha + b)y + \alpha z = 0$, $\alpha x + \alpha y + (\alpha + c)z = 0$ has a non-trivial solution if $\alpha^{-1} =$ (A) $-(a^{-1} + b^{-1} + c^{-1})$ (B) $a + b + c$ (C) $\alpha + a + b + c = 1$ (D) none of these

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133. Prove that

$$\left| ab + ca^2bc + ab^2ca + bc^2 \right| = -(a + b + c) \times (a - b)(b - c)(c - a)$$

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134. If $a > 0$ and discriminant of $ax^2 + 2bx + c$ is negative, then

$$\begin{vmatrix} a & b & ax + b \\ b & c & bx + c \\ ax + b & bx + c & 0 \end{vmatrix} \begin{matrix} \text{is +ve b. } (ac - b)^2 (ax^2 + 2bx + c) \\ \text{c. -ve d. 0} \end{matrix}$$

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135. If $\begin{vmatrix} a - b - c & 2a & 2a \\ 2b & b - c - a & 2b \\ 2c & 2c & c - a - b \end{vmatrix} = (a + b + c)$

$\times (x + a + b + c)^2$, $x \neq 0$ and $a + b + c \neq 0$ then x is equal to

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136. If $a_1, a_2, a_3, \dots, a_n, \dots$ are in G.P., then the determinant $\Delta =$

$$\begin{vmatrix} \log a_n & \log a_{n+1} & \log a_{n+2} \\ \log a_{n+3} & \log a_{n+4} & \log a_{n+5} \\ \log a_{n+6} & \log a_{n+7} & \log a_{n+8} \end{vmatrix} \text{ is equal to}$$

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137. By using properties of determinants, show that :

$$\begin{vmatrix} a^2 + 1 & ab & ac \\ ab & b^2 + 1 & bc \\ ca & cb & c^2 + 1 \end{vmatrix} = 1 + a^2 + b^2 + c^2$$

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138. Let $\vec{a}_r = x_r \hat{i} + y_r \hat{j} + z_r \hat{k}$, $r = 1, 2, 3$ be three mutually perpendicular

unit vectors, then the value of $\begin{vmatrix} x_1 & x_2 & x_3 \\ y_1 & y_2 & y_3 \\ z_1 & z_2 & z_3 \end{vmatrix}$ is equal to 0 b. ± 1 c. ± 2 d.

none of these

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139. The number of distinct real roots of $\begin{vmatrix} \sin x & \cos x & \cos x \\ \cos x & \sin x & \cos x \\ \cos x & \cos x & \sin x \end{vmatrix} = 0$ in the

interval $\pi/4 \leq x \leq \pi/4$ is 0 b. 2 c. 1 d. 3

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140. Let a, b, c be real numbers with $a^2 + b^2 + c^2 = 1$. Show that the equation

$$|ax - by - cbx - aycx + abx + ay - ax + by - y + bcx + acy + b - ax - by + c| = 0$$

represents a straight line.

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141. If lines $px + qy + r = 0$, $qx + ry + p = 0$ and $rx + py + q = 0$ are concurrent, then prove that $p + q + r = 0$ (where p, q, r are distinct).

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142. If $p\lambda^4 + q\lambda^3 + r\lambda^2 + s\lambda + t = \begin{vmatrix} \lambda^2 + 3\lambda & \lambda - 1 & \lambda + 3 \\ \lambda^2 + 1 & 2 - \lambda & \lambda - 3 \\ \lambda^2 - 3 & \lambda + 4 & 3\lambda \end{vmatrix}$ then $t =$

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143. Find the value of λ if $2x^2 + 7xy + 3y^2 + 8x + 14t + \lambda = 0$ represents a pair of straight lines

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144. If x, y, z are different from zero and $\Delta = \begin{vmatrix} a & b - y & c - z \\ a - x & b & c - z \\ a - x & b - y & c \end{vmatrix} = 0$,

then the value of the expression $\frac{a}{x} + \frac{b}{y} + \frac{c}{z}$ is 0 b. -1 c. 1 d. 2

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145. If A, B, C are angles of a triangles, then the value of

$$\begin{vmatrix} e^{2iA} & e^{-iC} & e^{-iB} \\ e^{-iC} & e^{2iB} & e^{-iA} \\ e^{-iB} & e^{-iA} & e^{2iC} \end{vmatrix}$$
 is 1 b. -1 c. -2 d. -4



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146. For the equation $\begin{vmatrix} 1 & x & x^2 \\ x^2 & 1 & x \\ x & x^2 & 1 \end{vmatrix} = 0$, There are exactly two distinct

roots There is one pair of equation real roots. There are three pairs of equal roots Modulus of each root is 2



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147. Let $\Delta_r = \left| r - 1 \quad n6(r - 1)^2 \quad 2n^2 \quad 4n - 2(r - 1)^2 \quad 3n^3 \quad 3n^2 - 3n \right|$ Show that

$\sum_{r=1}^n \Delta_r$ is constant.



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148. Let m be a positive integer and $\Delta_r = \begin{vmatrix} 2r - 1 & {}^m C_r & 1 \\ m^2 - 1 & 2^m & m + 1 \\ \sin^2(m^2) & \sin^2 m & \sin(m^2) \end{vmatrix}$. Then

the value of $\sum_{r=0}^m \Delta_r$

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149. Prove that

$|1 + a11111 + b11111 + c11111 + d| = abcd \left(a + \frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d} \right)$. Hence

find the value of the determinant if a, b, c, d are the roots of the equation

$$px^4 + qx^3 + rx^2 + sx + t = 0.$$

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150. Find the area of a triangle having vertices $A(3, 2)$, $B(11, 8)$, and $C(8, 12)$.

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151. If $D_k = 1 + 2kn^2 + n + 1n^2 + n2k - 1n^2n^2 + n + 1$ and $\sum_{k=1}^n D_k = 56$, then n equals 4 b. 6 c. 8 d. none of these

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152. If $a \neq p, b \neq q, c \neq r$ and $|pbc aqcabr| = 0$, then find the value of

$$\frac{p}{p-a} + \frac{q}{q-b} + \frac{r}{r-c}$$

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153. If x_1, x_2, x_3 as well as y_1, y_2, y_3 are in G.P. with same common ratio, then prove that the points (x_1, y_1) , (x_2, y_2) , and (x_3, y_3) are collinear.

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154. If the lines $a_1x + b_1y + 1 = 0$, $a_2x + b_2y + 1 = 0$ and $a_3x + b_3y + 1 = 0$ are concurrent, show that the points (a_1, b_1) , (a_2, b_2) and (a_3, b_3) are collinear.

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155. For a fixed positive integer n , if $n! = |n!(n+1)!(n+2)!(n+1)!(n+2)!(n+3)!(n+2)!(n+3)!(n+4)!|$, then show that $\left[\frac{1}{n} \left((n!)^3 - 4 \right) \right]$ is divisible by n .

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156. The number of values of a for which the lines $2x + y - 1 = 0$, $ax + 3y - 3 = 0$, and $3x + 2y - 2 = 0$ are concurrent is 0 (b) 1 (c) 2 (d) infinite



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157. If the lines $ax + y + 1 = 0$, $x + by + 1 = 0$ and $x + y + c = 0$ (a, b, c being distinct and different from 1) are concurrent, then prove that

$$\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} = 1.$$



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158. If $(1 + ax + bx^2)^4 = a_0 + a_1x + a_2x^2 + \dots + a_8x^8$ when

$a, b, a_0, a_1, a_2, \dots, a_8 \in R$ such that $a_0 + a_1 + a_2 \neq 0$ and
$$\begin{vmatrix} a_0 & a_1 & a_2 \\ a_1 & a_2 & a_0 \\ a_2 & a_0 & a_1 \end{vmatrix} = 0$$

then the value of $5\frac{a}{b}$ (A) 6 (B) 8 (C) 10 (D) 12



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159. Find the value of λ for which the homogeneous system of equations:

$$2x + 3y - 2z = 0 \quad 2x - y + 3z = 0 \quad 7x + \lambda y - z = 0 \quad \text{has non-trivial solutions.}$$

Find the solution.

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160. If $f, g,$ and h are differentiable functions of

$$x \text{ and } \Delta(x) = \begin{vmatrix} fgh & (xf)' & (xg)' & (xh)' \\ (x^2f)'' & (x^2g)'' & (x^2h)'' \end{vmatrix}, \text{ prove}$$

$$\Delta' = \begin{vmatrix} f & g & h & f' & g' & h' \\ (x^3f)'' & (x^3g)'' & (x^3h)'' \end{vmatrix}$$

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161. If a, b, c are positive and unequal, show that value of the determinant

$$\Delta = \begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix} \text{ is negative}$$

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162. if $= \begin{vmatrix} x^n & n! & 2 \\ \cos x & \cos. \frac{n\pi}{2} & 4 \\ \sin x & \sin. \frac{n\pi}{2} & 8 \end{vmatrix}$, then find the value of

$$\frac{d^n}{dx^n}[f(x)]_{x=0} \cdot (n \in \mathbb{Z}).$$

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163. Without expanding a determinant at any stage, show that $\left| \begin{matrix} x^2 + x, x + 1, x + 2 \\ 2x^2 + 3x - 1, 3x, 3x - 3 \\ x^2 + 2x + 3, 2x - 1, 2x - 1 \end{matrix} \right| = x^2$

$$\left| \begin{matrix} x^2 + x, x + 1, x + 2 \\ 2x^2 + 3x - 1, 3x, 3x - 3 \\ x^2 + 2x + 3, 2x - 1, 2x - 1 \end{matrix} \right| = x^2$$

are determinant of order 3 not involving x

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164. Show that
$$\begin{vmatrix} bc - a^2 & ca - b^2 & ab - c^2 \\ ca - b^2 & ab - c^2 & bc - a^2 \\ ab - c^2 & bc - a^2 & ca - b^2 \end{vmatrix}$$

$$\begin{vmatrix} a^2 & c^2 & 2ca - b^2 \\ 2ab - c^2 & b^2 & a^2 \\ b^2 & 2ac - a^2 & c^2 \end{vmatrix}.$$



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165. Show that the system of equations $3x - y + 4z = 3$, $x + 2y - 3z = -2$ and $6x + 5y + \lambda z = -3$ has at least one solution for any real number λ .

Find the set of solutions of $\lambda = -5$



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166. Show that
$$\begin{vmatrix} 2bc - a^2 & c^2 & b^2 \\ c^2 & 2ca - b^2 & a^2 \\ b^2 & a^2 & 2ab - c^2 \end{vmatrix} = \begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}^2$$



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167. If $y = |\sin x \cos x \sin x \cos x - \sin x \cos x \times 11| = f \in d \frac{dy}{dx}$.



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168. Consider the system of equation $x + y + z = 6$, $x + 2y + 3z = 10$, and $x + 2y + \lambda z = \mu$. Statement 1: if the system has infinite number of solutions, then $\mu = 10$. Statement 2: The determinant $|116121012\mu| = 0$ if or $\mu = 10$.



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169. Consider the system of linear equations in x, y and z :
 $(\sin 3\theta)x - y + z = 0$
 $(\cos 2\theta)x + 4y + 3z = 0$
 $3x + 7y + 7z = 0$
 Which of the following can be the value of θ for which the system has a non-trivial

solution

$$n\pi + (-1)^n \frac{\pi}{6}, \forall n \in \mathbb{Z}$$

$$n\pi + (-1)^n \frac{\pi}{3}, \forall n \in \mathbb{Z}$$

$$n\pi + (-1)^n \frac{\pi}{9}, \forall n \in \mathbb{Z} \text{ none of these}$$



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170. Prove without expansion that

$$|ah + bgab + chbf + bafhb + bcaf + bbg + fc| = a|ah + bgahbf + bahbaf + bcgf|$$



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171. If α, β and γ are real number without expanding at any stage prove that

$$\begin{vmatrix} 1 & \cos(\beta - \alpha) & \cos(\gamma - \alpha) \\ \cos(\alpha - \beta) & 1 & \cos(\gamma - \beta) \\ \cos(\alpha - \gamma) & \cos(\beta - \gamma) & 1 \end{vmatrix} = 0.$$



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172. If 3 digit numbers $A28$, $3B9$ and $62C$ are divisible by a fixed constant 'K' where A, B, C are integers lying between 0 and 9, then determinant

$$\begin{vmatrix} A & 3 & 6 \\ 8 & 9 & C \\ 2 & B & 2 \end{vmatrix} \text{ is always divisible by}$$

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173. If $a = \cos\theta + i\sin\theta$, $b = \cos2\theta - i\sin2\theta$, $c = \cos3\theta + i\sin3\theta$ and if

$$\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix} = 0 \text{ then } \text{a. } \theta = 2k\pi, k \in Z \quad \text{b. } \theta = (2k + 1)\pi, k \in Z \quad \text{c.}$$

$\theta = (4k + 1)\pi, k \in Z$ d. none of these

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174. Prove that

$$\begin{vmatrix} a_1\alpha_1 + b_1\beta_1 & a_1\alpha_2 + b_1\beta_2 & a_1\alpha_3 + b_1\beta_3 \\ a_2\alpha_1 + b_2\beta_1 & a_2\alpha_2 + b_2\beta_2 & a_2\alpha_3 + b_2\beta_3 \\ a_3\alpha_1 + b_3\beta_1 & a_3\alpha_2 + b_3\beta_2 & a_3\alpha_3 + b_3\beta_3 \end{vmatrix}$$

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175. If α, β, γ are the roots of $px^3 + qx^2 + r = 0$, then the value of the

determinant $\begin{vmatrix} \alpha\beta & \beta\gamma & \gamma\alpha \\ \beta\gamma & \gamma\alpha & \alpha\beta \\ \gamma\alpha & \alpha\beta & \beta\gamma \end{vmatrix}$ is p b. q c. 0 d. r

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176. Prove that

$$\left| (a-x)^2(a-y)^2(a-z)^2(b-x)^2(b-y)^2(b-z)^2(c-x)^2(c-y)^2(c-z)^2 \right| =$$

$$\left| (1+ax)^2(1+bx)^2(1+cx)^2(1+ay)^2(1+by)^2(1+cy)^2(1+az)^2(1+bz)^2(1+cz)^2 \right|$$

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177. If $\left| \begin{matrix} 1 & x^2 & x^2 \\ x^2 & 1 & x^2 \\ x^2 & x^2 & 1 \end{matrix} \right| = 0$, then find the value of

$$\left| \begin{matrix} x^3 & -10x & -x^4 \\ -10x & x^4 & x^3 \\ -x^4 & x^3 & -10 \end{matrix} \right|$$

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178.

If

$$\left| x^n x^{n+2} x^{n+3} y^n y^{n+2} y^{n+3} z^n z^{n+2} z^{n+3} \right| = (x-y)(y-z)(z-x) \left(\frac{1}{x} + \frac{1}{y} + \frac{1}{z} \right),$$

then n equals 1 b. -1 c. 2 d. -2



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179. Solve the system of the equations: $ax + by + cz = d$

$$a^2x + b^2y + c^2z = d^2 \quad a^3x + b^3y + c^3z = d^3$$

Will the solution always exist and be unique?



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180. if $\begin{vmatrix} a & b-c & c+b \\ a+c & b & c-a \\ a-b & a+b & c \end{vmatrix} = 0$ then the line $ax + by + c = 0$

passes through the fixed point which is



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181. If $2ax - 2y + 3z = 0$, $x + ay + 2z = 0$, and $2 + az = 0$ have a nontrivial solution, find the value of a .

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182. If $[.]$ denotes the greatest integer less than or equal to the real number under consideration and $-1 \leq x < 0$, $0 \leq y < 1$, $1 \leq z < 2$, then the

value of the determinant $\begin{vmatrix} [x] + 1 & [y] & [z] \\ [x] & [y] + 1 & [z] \\ [x] & [y] & [z] + 1 \end{vmatrix}$ is

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183. if $(x) = a + bx + cx^2$ and α, β, γ are the roots of the equation

$x^3 = 1$ then $\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$ is equal to

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184. If x, y and z are not all zero and connected by the equations $a_1x + b_1y + c_1z = 0$, $a_2x + b_2y + c_2z = 0$, and $(p_1 + \lambda q_1)x + (p_2 + \lambda q_2)y + (p_3 + \lambda q_3)z = 0$, show that $\lambda = - \frac{a_1b_1c_1a_2b_2c_2p_1p_2p_3}{a_1b_1c_1a_2b_2c_2q_1q_2q_3}$



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185. Find λ for which the system of equations $x + y - 2z = 0$, $2x - 3y + z = 0$, $x - 5y + 4z = \lambda$ is consistent and find the solutions for all such values of λ .



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186. If p, q, r are in A.P. then value of determinant $\begin{vmatrix} a^2 + 2^{n+1} + 2pb^2 + 2^{n+2} + 3qc^2 + p2^n + p2^{n+1} & 2qa^2 + 2^n + pb^2 + 2^{n+1} & c^2 - r \end{vmatrix}$ is a) 0 (b) Independent from a, b, c (c) $a^2b^2c^2 - 2^n$ (d) Independent from n



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187. For what values of k , the following system of equations possesses a nontrivial solution over the set of rationals:

$c + ky + 3z = 0$, $3c + ky - 2z = 0$, $2c + 3y - 4x = 0$. Also find the solution for this value of k

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188. Let $a, b, c \in R$ such that no two of them are equal and satisfy

$\begin{vmatrix} 2a & b & c \\ b & c & 2a \\ c & 2a & b \end{vmatrix} = 0$, then equation $24ax^2 + 8bx + 4c = 0$ has (a) at least one

root in $[0, 1]$ (b) at least one root in $\left[-\frac{1}{2}, \frac{1}{2}\right]$ (c) at least one root in $[-1, 0]$

(d) at least two roots in $[0, 2]$

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189. Solve by Cramers rule $x + y + z = 6$, $x - y + z = 2$, $3x + 2y - 4z = -5$

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190. The value of the determinant $\begin{vmatrix} ka & k^2 + a^2 & 1 \\ kb & k^2 + b^2 & 1 \\ kc & k^2 + c^2 & 1 \end{vmatrix}$ is (A)

$k(a+b)(b+c)(c+a)$ (B) $kabc(a^2 + b^2 + c^2)$ (C) $k(a-b)(b-c)(c-a)$ (D)

$k(a+b-c)(b+c-a)(c+a-b)$

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191. Find the value of a and b if the system of equation

$a^2x - by = a^2 - b$ and $bx = b^2y = 2 + 4b$ (i) posses unique solution (ii) infinite

solutions

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192. If $(x_1 - x_2)^2 + (y_1 - y_2)^2 = a^2$, $(x_2 - x_3)^2 + (y_2 - y_3)^2 = b^2$,

$(x_3 - x_1)^2 + (y_3 - y_1)^2 = c^2$, and

$$k \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix} = (a + b + c)(b + c - b)(c + a - b) \times (a + b - c), \text{ then the value}$$

of k is 1 b. 2 c. 4 d. none of these

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193. $f(x) = \left| \cos \times 12\sin \times {}^2_2x \tan \times 1 \right|$. Then value of $(\lim)_{x \rightarrow 0} \frac{f(x)}{x}$ is equal to

1 b. -1 c. zero d. none of these

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194. If the system of linear equation $x + 2ay + az = 0$, $x + 3by + bz = 0$, $x + 4cy + cz = 0$ has a non-trivial solution then show that a, b, c are in H.P.

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195. Let α be a repeated root of a quadratic equation $f(x) = 0$ and $A(x), B(x), C(x)$ be polynomials of degrees 3, 4, and 5, respectively, then show that $|A(x)B(x)C(x)A(\alpha)B(\alpha)C(\alpha)A'(\alpha)B'(\alpha)C'(\alpha)|$ is divisible by $f(x)$, where prime (') denotes the derivatives.

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196. If $\left| a^2 + \lambda^2 ab + c \lambda ca - b \lambda ab - c \lambda b^2 + \lambda^2 bc + aca + b \lambda bc - a \lambda c^2 + \lambda^2 \right| \lambda c - b - c \lambda ab - a \lambda$, then the value of λ is a) 8 b. 27 c. 1 d. -1

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197. Value of $\left| 1 + x_1 1 + x_1 x_1 + x_1 x^2 1 + x_2 1 + x_2 x_1 + x_2 x^2 1 + x_3 1 + x_3 x_1 + x_3 x^2 \right|$ depends upon x o n l y b. x₁ o n l y c. x₂ only d. none of these

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198. If $\Delta(x) = |\alpha + x\theta + x\lambda + x\beta + x\phi + x\mu + x\gamma + x\psi + xv + x|$ show that $\Delta'(x) = \Delta(0) + Sx$, where S denotes the sum of all the cofactors of all elements in $\Delta(0)$ and dash denotes the derivative with respect of x .

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199. The value of determinant $|bc - a^2ac - b^2ab - c^2ac - b^2ab - c^2bc - a^2ab - c^2bc - a^2ac - b^2|$ is a. always positive b. always negative c. always zero d. cannot say anything

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200. If $l_1^2 + m_1^2 + n_1^2 = 1$ etc., and $l_1l_2 + m_1m_2 + n_1n_2 = 0$, etc. and

$$\Delta = \begin{vmatrix} l_1 & m_1 & n_1 \\ l_2 & m_2 & n_2 \\ l_3 & m_3 & n_3 \end{vmatrix} \text{ then}$$



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201. Let $\begin{vmatrix} x & 2 & x \\ x^2 & x & 6 \\ x & x & 6 \end{vmatrix} = Ax^4 + Bx^3 + Cx^2 + Dx + E$. Then the value of $5A$

$+4B + 3C + 2D + E$ is equal to



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202. Let a, b, c be the real numbers. The following system of equations in

$x, y,$ and z $\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{a^2} = 1, \frac{x^2}{a^2} - \frac{y^2}{b^2} + \frac{z^2}{a^2} = 1, -\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{a^2} = 1$ has a.

no solution b. unique solution c. infinitely many solutions d. finitely many

solutions



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203. The value of the determinant

$$|[\sin\theta, \cos\theta, \sin 2\theta], \left[\sin\left(\theta + \frac{2\pi}{3}\right), \cos\left(\theta + \frac{2\pi}{3}\right), \sin\left(2\theta + \frac{4\pi}{3}\right) \right], \left[\sin\left(\theta - \frac{2\pi}{3}\right), \cos\left(\theta - \frac{2\pi}{3}\right), \sin\left(2\theta - \frac{4\pi}{3}\right) \right]|$$

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204. Find the value of the determinant $|baabpqr111|$, where a , b , and c are respectively, the p th, q th, and r th terms of a harmonic progression.

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205. let $a > 0, d > 0$ find the value of the determinant

$$\begin{vmatrix} \frac{1}{a} & \frac{1}{a(a+d)} & \frac{1}{(a+d)(a+2d)} \\ \frac{1}{a+d} & \frac{1}{(a+d)(a+2d)} & \frac{1}{(a+2d)(a+3d)} \\ \frac{1}{a+2d} & \frac{1}{(a+2d)(a+3d)} & \frac{1}{(a+3d)(a+4d)} \end{vmatrix}$$

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206. For all values of A,B,C and P,Q,R show that

$$\begin{vmatrix} \cos(A - P) & \cos(A - Q) & \cos(A - R) \\ \cos(B - P) & \cos(B - Q) & \cos(B - R) \\ \cos(C - P) & \cos(C - Q) & \cos(C - R) \end{vmatrix} = 0$$

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207. Let λ and α be real. Find the set of all values of λ for which the system

of linear equations

$$\lambda x + (\sin\alpha)y + (\cos\alpha)z = 0, \quad x + (\cos\alpha)y + (\sin\alpha)z = 0, \quad -x + (\sin\alpha)y - (\cos\alpha)z = 0.$$

have trivial solution

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208. Prove that

$$|ax - by - cz + bxcx + azay + bxby - cz - axbz + cycx + azbz + cycz - ax - by| = (\dots)$$

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209. If $(x) = |\alpha + x\theta + x\lambda + x\beta + x\varphi + x\mu + x\gamma + x\psi + xv + x|$ show that $\Delta^{\wedge}(x) = 0$ and $\Delta^{\wedge}(0) = Sx$, where S denotes the sum of all the cofactors of all elements in $\Delta(0)$ and dash denotes the derivative with respect of x .

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210. If α, β, γ are different from 1 and are the roots of $ax^3 + bx^2 + cx + d = 0$ and $(\beta - \gamma)(\gamma - \alpha)(\alpha - \beta) = \frac{25}{2}$, then prove that

$$\left| \frac{\alpha}{1-\alpha} \frac{\beta}{1-\beta} \frac{\gamma}{1-\gamma} \alpha\beta\gamma \alpha^2\beta^2\gamma^2 \right| = \frac{25d}{2(a+b+c+d)}$$

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211. If $p + q + r = 0 = a + b + c = 0$, then the value of the determinant $\begin{vmatrix} pa & qb & rc \\ qb & rc & pa \\ rc & pa & qb \end{vmatrix}$ is a. 0 b. $pa + qb + rc$ c. 1 d. none of these

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212.

Let

$$= \begin{vmatrix} 2a_1b_1a_1b_2 + a_2b_1a_1b_3 + a_3b_1a_1b_2 + a_2b_1a_2b_2a_2b_3 + a_3b_2a_1b_3 + a_3b_1a_3b_2 \\ \dots \end{vmatrix}$$

. Expressing as the product of two determinants, show that = 0. Hence,

show that if

$$ax^2 + 2hxy + by^2 + 2gx + 2fy + c = (lx + my + n)(l'x + m'y + n), \text{ then } \dots$$

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213. If $2s = a + b + c$ and $A = \begin{vmatrix} a^2 & (s - a)^2 & (s - a)^2 \\ (s - b)^2 & b^2 & (s - b)^2 \\ (s - c)^2 & (s - c)^2 & c^2 \end{vmatrix}$ then $\det A$

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214. Evaluate $\begin{vmatrix} \dots \\ \dots \\ \dots \end{vmatrix}$

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215. Using factor theorem, show that

$$\begin{vmatrix} -2a & a+b & c+a \\ a+b & -2a & b+c \\ c+a & c+b & -2c \end{vmatrix} = 4(a+b)(b+c)(c+a)$$

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216. If a determinant of order 3×3 is formed by using the numbers 1 or -1 then minimum value of determinant is :

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217. If $z = |-53 + 4i5 - 7i3 - 4i68 + 7i5 + 7i8 - 7i9|$, then z is purely real
purely imaginary $a + ib$, where $a \neq 0, b \neq 0$ d. $a + ib$, where $b = 4$

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218. If $\omega = cis \frac{2\pi}{3}$, then number of distinct roots of
$$\begin{vmatrix} z+1 & \omega & \omega^2 \\ \omega & z+\omega^2 & 1 \\ \omega^2 & 1 & z+\omega \end{vmatrix} = 0.$$

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219. If ω is the complex cube root of unity then

$$\begin{vmatrix} 1 & 1+i+\omega^2 & \omega^2 \\ 1-i & -1 & \omega^2-1 \\ -i & -i+\omega-1 & -1 \end{vmatrix} =$$

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220. If

$$ax^{12} + by^{12} + cz^{12} = ax^{22} + by^{22} + cz^{22} = ax^{32} + by^{32} + cz^{32} = d, ax^{23} + by^{23} + cz^{23} = d,$$

then prove that
$$\left| x_1 y_1 z_1 x_2 y_2 z_2 x_3 y_3 z_3 \right| = (d-f) \left\{ \frac{(d+2f)}{abc} \right\}^{1/2}$$

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221. If $A, B,$ and C are the angles of triangle, show that the system of equations

$$x \sin 2A + y \sin C + z \sin B = 0, \sin C + y \sin 2B + z \sin A = 0, \text{ and } x \sin B + y \sin A + z \sin 2C = 0$$

posses nontrivial solution. Hence, system has infinite solutions.

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222. Let α, β, γ are the real roots of the equation

$$x^3 + ax^2 + bx + c = 0 (a, b, c \in R \text{ and } a \neq 0)$$

If the system of equations $(\in u, v, \text{ and } w)$ given by $\alpha u + \beta v + \gamma w = 0$ $\beta u + \gamma v + \alpha w = 0$ $\gamma u + \alpha v + \beta w = 0$

has non-trivial solutions then the value of a^2/b is _____.

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223. If $a_1, a_2, a_3, 54, a_6, a_7, a_8, a_9$ are in H.P., and $D = \begin{vmatrix} a_1 & a_2 & a_3 & 45 & a_6 & a_7 & a_8 & a_9 \end{vmatrix}$,

then the value of $[D]$ is where $[.]$ represents the greatest integer function

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224. If $f(x)$ is a polynomial of degree < 3 , prove that

$$\left| \frac{1af(a)/(x-a)1bf(b)/(x-b)1cf(c)/(x-c)}{1aa^21 \wedge 21 \wedge 2} \right| = \frac{f(x)}{(x-a)(x-b)(x-c)}$$

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225. Prove that $|acc - a + bcbb - cb + ca - bb - c0a - cxyz1 + x + y| = 0$

implies that a, b, c are in A.P. or a, c, b are in G.P.

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226. Solve for $x \in R$:

$$\begin{vmatrix} (x+a)(x-a) & (x+b)(x-b) & (x+c)(x-c) \\ (x-a)^3 & (x-b)^3 & (x-c)^3 \\ (x+a)^3 & (x+b)^3 & (x+c)^3 \end{vmatrix} = 0, a, b$$

and c being distinct real numbers.

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227. Absolute value of sum of roots of the equation $|x + 22x + 33x + 42x + 33x + 44x + 53x + 55c + 810x + 17| = 0$ is _____.

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228. Let α_1, α_2 and β_1, β_2 be the roots of the equation $ax^2 + bx + c = 0$ and $px^2 + qx + r = 0$ respectively. If the system of equations $\alpha_1 y + \alpha_2 z = 0$ and $\beta_1 y - \beta_2 z = 0$ has a non trivial solution then prove that $\frac{b^2}{q^2} = \frac{ac}{pr}$

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229. The product of all values of t , for which the system of equations $(a - t)x + by + cz = 0$, $bx + (c - t)y + az = 0$, $cx + ay + (b - t)z = 0$ has non-trivial solution, is $|a - c - b - cb - a - b - ac|$ (b) $|abcbcacab|$ $|acaba|$ (d) $|aa + + c + + a + aa + b|$

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230. Let $\omega = -\frac{1}{2} + i\frac{\sqrt{3}}{2}$, then value of the determinant $\begin{bmatrix} 1 & 1 & 1 \\ 1 & -1 & -\omega^2 \\ \omega^2 & \omega^2 & \omega \end{bmatrix}$

is (a) 3ω (b) $3\omega(\omega - 1)$ (c) $3\omega^2$ (d) $3\omega(1 - \omega)$

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231. If $\Delta = \begin{vmatrix} -xa & -xaab & -x \\ x^2 - (a-b) & x + a^2 + b^2 + ab & x^2 - (a+b) + x + a^2 + b^2 - ab \\ a + b - x & a + b - x & a + b - x \end{vmatrix}$, then a factor is

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232. If $g(x) = \left| a^{-x} e^{x \log_e a} x^2 a^{-3x} e^{3x \log_e a} x^4 a^{-5x} e^{5x \log_e a} 1 \right|$, then graphs of $g(x)$ is symmetrical about the origin graph of $g(x)$ is symmetrical about the y-axis

$\left(\frac{d^4 g(x)}{dx^4} \right)_{x=0} = 0$ $f(x) = g(x) \times \log\left(\frac{a-x}{a+x}\right)$ is an odd function

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233. the sum of values of p for which the equations $x+y+z=1x+2y+4z=p$ and $x+4y+10z=p^2$ have a solution is _____

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234. The value of $|\alpha|$ for which the system of equation

$$\alpha x + y + z = \alpha - 1$$

$$x + \alpha y + z = \alpha - 1$$

$$x + y + \alpha z = \alpha - 1$$

has no solution, is _____

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235. Let $D_1 = |aba + bc dc + da ba - b|$ and $D_2 = |aca + cb db + da ca + b + c|$

then the value of $\left| \frac{D_1}{D_2} \right|$, where $b \neq 0$ and $a \neq bc$, is _____.

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236. If $|x + y + z + 2x + 3x + 2y + 4x + 3y + 2z + 3x + 6x + 3y + 10x + 6y + 3z| = 64$, then the real value of x is _____.

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237. If $\left| \int_0^{\pi} \cos \theta \sin \theta \, d\theta \right|$, then the value of $(\dots)^2$

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238. _____ If

$$\left| x^n x^{n+2} x^{n+4} y^n y^{n+2} y^{n+4} z^n z^{n+2} z^{n+4} \right| = \left(\frac{1}{y^2} - \frac{1}{x^2} \right) \left(\frac{1}{z^2} - \frac{1}{y^2} \right) \left(\frac{1}{x^2} - \frac{1}{z^2} \right)$$

then n is _____.

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239. _____ The _____ value _____ of

$$\left| 2x_1 y_1 x_1 y_2 + x_2 y_1 x_1 y_3 + x_3 y_1 x_1 y_2 + x_2 y_1^2 x_2 y_2 x_2 y_3 + x_3 y_2 x_1 y_3 + x_3 y_1 x_2 y_3 + x_3 y_2^2 \right|$$

is.



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240. Given $A = |ab2cde2flm2n|$, $B = |f2de2n4l2mc2ab|$, then the value of B/A is _____.



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Single correct Answer

$$1. \begin{vmatrix} 1 & \cos\alpha & \cos\beta \\ \cos\alpha & 1 & \cos\gamma \\ \cos\beta & \cos\gamma & 1 \end{vmatrix} = \begin{vmatrix} 0 & \cos\alpha & \cos\beta \\ \cos\alpha & 0 & \cos\beta \\ \cos\beta & \cos\gamma & 0 \end{vmatrix}$$

if $\cos^2\alpha + \cos^2\beta + \cos^2\gamma =$

A. 1

B. 2

C. 3/2

D. $1/2$

Answer: A



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2. If α, β, γ are roots of the equation $x^2(px + q) = r(x + 1)$, then the value of

determinant $\begin{vmatrix} 1 + \alpha & 1 & 1 \\ 1 & 1 + \beta & 1 \\ 1 & 1 & 1 + \gamma \end{vmatrix}$ is

A. $\alpha\beta\gamma$

B. $1 + \frac{1}{\alpha} + \frac{1}{\beta} + \frac{1}{\gamma}$

C. 0

D. none of these

Answer: C



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3. if $\omega \neq 1$ is a cube root of unity and $x + y + z \neq 0$, then prove that

$$\begin{vmatrix} \frac{x}{1+\omega} & \frac{y}{\omega+\omega^2} & \frac{z}{\omega^2+1} \\ \frac{y}{\omega+\omega^2} & \frac{z}{\omega^2+1} & \frac{x}{1+\omega} \\ \frac{z}{\omega^2+1} & \frac{x}{1+\omega} & \frac{y}{\omega+\omega^2} \end{vmatrix}$$

A. $x^2 + y^2 + z^2 = 0$

B. $x + y\omega + z\omega^2 = 0$ or $x = y = z$

C. $x \neq y \neq z \neq 0$

D. $x=2y=3z$

Answer: B



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4. If $a = \cos\left(\frac{4\pi}{3}\right) + i\sin\left(\frac{4\pi}{3}\right)$ then $\begin{vmatrix} 1 & 1 & 1 \\ 1 & a & a^2 \\ 1 & a^2 & a \end{vmatrix}$

A. purely real

B. purely imaginary

C. 0

D. none of these

Answer: B



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5. If α is a root of $x^4 = 1$ with negative principal argument then the

principal argument of $\Delta(\alpha) = \begin{vmatrix} 1 & 1 & 1 \\ \alpha^n & \alpha^{n+1} & \alpha^{n+3} \\ \frac{1}{\alpha^{n+1}} & \frac{1}{\alpha^n} & 0 \end{vmatrix}$ is

A. $\frac{5\pi}{14}$

B. $-\frac{3\pi}{4}$

C. $\frac{\pi}{4}$

D. $-\frac{\pi}{4}$

Answer: B



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6. $\Delta_1 = \begin{vmatrix} x & b & b \\ a & x & b \\ a & a & x \end{vmatrix}$ and $\Delta_2 = \begin{vmatrix} x & b \\ a & x \end{vmatrix}$ are the given determinations then

A. $\Delta_1 = 3(\Delta_2)^2$

B. $\frac{d}{dx}(\Delta_1) = 3\Delta_2$

C. $\frac{d}{dx}(\Delta_1) = 3(\Delta_2)^2$

D. $\Delta_1 = 3\Delta_2^{3/2}$

Answer: B



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7. If $a^2 + b^2 + c^3 + ab + bc + ca \leq 0$ for all, $a, b, c \in R$, then the value of the determinant

$$\begin{vmatrix} (a+b+2)^2 & a^2+b^2 & 1 \\ 1 & (b+c+2)^2 & b^2+c^2 \\ c^2+a^2 & 1 & (c+a+2)^2 \end{vmatrix}, \text{ is equal to}$$

A. 65

B. $a^2 + b^2 + c^2 + 31$

C. $4(a^2 + b^2 + c^2)$

D. 0

Answer: A



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8. Product of roots of equation $\begin{vmatrix} 1 + 2x & 1 & 1 - x \\ 2 - x & 2 + x & 3 + x \\ x & 1 + x & 1 - x^2 \end{vmatrix} = 0$ is

A. $1/2$

B. $3/4$

C. $4/3$

D. $1/4$

Answer: A



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9. If $x \neq 0, y \neq 0, z \neq 0$ and $|1 + x| |1 + y| |1 + z| = 0$, then $x^{-1} + y^{-1} + z^{-1}$ is equal to

1 b. -1 c. -3 d. none of these

A. 0

B. 1

C. 3

D. 6

Answer: C



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10. If $Y = SX$, $Z = tX$ all the variables being differentiable functions of x and lower suffices denote the derivative with respect to x and

$$\begin{vmatrix} X & Y & X \\ X_1 & Y_1 & Z_1 \\ X_2 & Y_2 & Z_2 \end{vmatrix} + \begin{vmatrix} S_1 & t_1 \\ S_2 & t_2 \end{vmatrix} = X^n, \text{ then } n =$$

A. 1

B. 2

C. 3

D. 4

Answer: C



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11. If $w \neq 1$ is a cube root of unity and $\Delta = \begin{vmatrix} x + w^2 & w & 1 \\ w & w^2 & 1 + x \\ 1 & x + w & w^2 \end{vmatrix} = 0$,

then value of x is

A. 0

B. 2

C. -1

D. None of these

Answer: A



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12. Let $|A| = \left| a_{ij} \right|_{3 \times 3} \neq 0$ Each element a_{ij} is multiplied by k^{i-j} Let $|B|$ the resulting determinant, where $k_1|A| + k_2|B| = a$ then $k_1 + k_2 =$

A. 1

B. -1

C. 0

D. 2

Answer: C

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13. If α, β, γ are the roots of $x^3 + px^2 + q = 0$, where $q = 0$, then

$$\Delta = \begin{bmatrix} 1 & 1 & 1 \\ \frac{1}{\alpha} & \frac{1}{\beta} & \frac{1}{\gamma} \\ \frac{1}{\beta} & \frac{1}{\gamma} & \frac{1}{\alpha} \\ \frac{1}{\gamma} & \frac{1}{\alpha} & \frac{1}{\beta} \end{bmatrix} \text{ equals}$$

A. $\alpha\beta\gamma$

B. $\alpha + \beta + \gamma$

C. 0

D. None of these

Answer: C



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14. If $a - 2b + c = 1$, then the value of $\begin{vmatrix} x+1 & x+2 & x+a \\ x+2 & x+3 & x+b \\ x+3 & x+4 & x+c \end{vmatrix}$ is

A. x

B. $-x$

C. -1

D. 1

Answer: C



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15. Let $x > 0, y > 0, z > 0$ are respectively the $2^{nd}, 3^{rd}, 4^{th}$ terms of a G.P.

$$\text{and } \Delta = \begin{vmatrix} x^k & x^{k+1} & x^{k+2} \\ y^k & y^{k+1} & y^{k+2} \\ z^k & z^{k+1} & z^{k+2} \end{vmatrix} = (r-1)^2 \left(1 - \frac{1}{r^2}\right) \text{ (where } r \text{ is the common}$$

ratio), then

A. $k = -1$

B. $k = 1$

C. $k = 0$

D. None of these

Answer: A



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16. If $a, b, c, d > 0$, $x \in R$ and

$(a^2 + b^2 + c^2)x^2 - 2(ab + bc + cd)x + b^2 + c^2 + d^2 \leq 0$, then

$$\begin{vmatrix} 33 & 14 & \log a \\ 65 & 27 & \log b \\ 97 & 40 & \log c \end{vmatrix} =$$

A. 1

B. -1

C. 0

D. none of these

Answer: C



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17.

Show

that

$$\left| {}^{\wedge}x C_r^x C_{r+1}^x C_{r+2}^y C_{r+1}^y C_{r+2}^z C_{r+1}^z C_{r+1} \right| = \left| {}^{\wedge}x C_r^{x+1} C_{r+1}^{x+2} C_{r+2}^y C_r^{y+1} C_{r+1}^{y+2} C_{r+1}^z \right|$$

A. 0

B. 2^n

C. ${}^{x+y+z}C_r$

D. ${}^{x+y+z}C_{r+2}$

Answer: A



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18. If $\begin{vmatrix} {}^9C_4 & {}^9C_5 & {}^{10}C_r \\ {}^{10}C_6 & {}^{10}C_7 & {}^{11}C_{r+2} \\ {}^{11}C_8 & {}^{11}C_9 & {}^{12}C_{r+4} \end{vmatrix} = 0$, then the value of r is equal to

A. 3

B. 4

C. 5

D. 6

Answer: C



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19. If either of the two P, Q and R are equal and $P + Q + R = 180^\circ$, then

the value of $\begin{vmatrix} 1 & 1 + \sin P & \sin P(1 + \sin P) \\ 1 & 1 + \sin Q & \sin Q(1 + \sin Q) \\ 1 & 1 + \sin R & \sin R(1 + \sin R) \end{vmatrix}$ is

A. 0

B. 1

C. $\sin(P + Q + R)$

D. $\sin P \sin Q \sin R$

Answer: A



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20. In a triangle ABC , if a, b, c are the sides opposite to angles A, B, C

respectively, then the value of $\begin{vmatrix} b \cos C & a & c \cos B \\ c \cos A & b & a \cos C \\ a \cos B & c & b \cos A \end{vmatrix}$ is

A. 1

B. -1

C. 0

D. $a\cos A + b\cos B + c\cos C$

Answer: C



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If $a = 1 + 2 + 4 + \dots$ to n terms

21. $b = 1 + 3 + 9 + \dots$ to n terms

$c = 1 + 5 + 25 + \dots$ to n terms

then
$$\begin{vmatrix} a & 2b & 4c \\ 2 & 2 & 2 \\ 2^n & 3^n & 5^n \end{vmatrix} =$$

A. $(30)^n$

B. $(10)^n$

C. 0

D. $2^n + 3^n + 5^n$

Answer: C



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22. If $a_1, a_2, a_3, 54, a_6, a_7, a_8, a_9$ are in H.P., and $D = \left| a_1 a_2 a_3 45 a_6 a_7 a_8 a_9 \right|$, then the value of $[D]$ is where $[.]$ represents the greatest integer function

A. 4

B. 5

C. 6

D. 7

Answer: B



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23.
$$\begin{vmatrix} \frac{1}{c} & \frac{1}{c} & -\frac{a+b}{c^2} \\ -\frac{b+c}{c^2} & \frac{1}{a} & \frac{1}{a} \\ \frac{-b(b+c)}{a^2c} & \frac{a+2b+c}{ac} & \frac{-b(a+b)}{ac^2} \end{vmatrix}$$
 is

- A. dependent on a, b, c
- B. dependent on a
- C. dependent on b
- D. independent on a, b and c

Answer: A



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24.

The

equation

$$\begin{vmatrix} (1+x)^2 & (1-x)^2 & -(2+x^2) \\ 2x+1 & 3x & 1-5x \\ x+1 & 2x & 2-3x \end{vmatrix} + \begin{vmatrix} (1+x)^2 & 2x+1 & x+1 \\ (1-x)^2 & 3x & 2x \\ 1-2x & 3x-2 & 2x-3 \end{vmatrix} = 0 \text{ has (a)}$$

no real solution (b) 4 real solutions (c) two real and two non-real solutions (d) infinite number of solutions, real or non-real

A. has no real solution

B. has 4 real solutions

C. has two real and two non-real solutions

D. has infinite number of solutions, real or non-real

Answer: D



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25. Let $\Delta_1 = \begin{bmatrix} ap^2 & 2ap & 1 \\ aq^2 & 2aq & 1 \\ ar^2 & 2ar & 1 \end{bmatrix}$ and $\Delta_2 = \begin{bmatrix} apq & a(p+q) & 1 \\ aqr & a(q+r) & 1 \\ arp & a(r+p) & 1 \end{bmatrix}$ then

A. $\Delta_1 = \Delta_2$

B. $\Delta_2 = 2\Delta_1$

C. $\Delta_1 = 2\Delta_2$

D. $\Delta_1 + 2\Delta_2 = 0$

Answer: D



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26. Area of triangle whose vertices are $(a, a^2), (b, b^2), (c, c^2)$ is $\frac{1}{2}$. and area of another triangle whose vertices are $(p, p^2), (q, q^2)$ and (r, r^2) is

4, then the value of $\begin{vmatrix} (1+ap)^2 & (1+bp)^2 & (1+cp)^2 \\ (1+aq)^2 & (1+bp)^2 & (1+cq)^2 \\ (1+ar)^2 & (1+br)^2 & (1+cr)^2 \end{vmatrix}$ is (A) 2 (B) 4 (C) 8 (D)

16

A. 2

B. 4

C. 8

D. 16

Answer: D



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27. The value of $\begin{vmatrix} \beta\gamma & \beta\gamma' + \beta'\gamma & \beta'\gamma' \\ \gamma\alpha & \gamma\alpha' + \gamma'\alpha & \gamma'\alpha' \\ \alpha\beta & \alpha\beta' + \alpha'\beta & \alpha'\beta' \end{vmatrix}$ is

A. $(\alpha\beta' - \alpha'\beta)(\beta\gamma' - \beta'\gamma)(\gamma\alpha' - \gamma'\alpha)$

B. $(\alpha\alpha' - \beta\beta')(\beta\beta' - \gamma\gamma')(\gamma\gamma' - \alpha\alpha')$

C. $(\alpha\beta' + \alpha'\beta)(\beta\gamma' + \beta'\gamma)(\gamma\alpha' + \gamma'\alpha)$

D. None of these

Answer: A



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28. If $\begin{vmatrix} a & b & a \\ b & c & 1 \\ c & a & 1 \end{vmatrix} = 2010$ and if $\begin{vmatrix} c-a & c-b & ab \\ a-b & a-c & bc \\ b-c & b-a & ca \end{vmatrix} - \begin{vmatrix} c-a & c-b & c^2 \\ a-b & a-c & a^2 \\ b-c & b-a & b^2 \end{vmatrix} = p$,

then the number of positive divisors of p is

A. 36

B. 49

C. 64

D. 81

Answer: D



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29. Let $\begin{vmatrix} a & l & m \\ l & b & n \\ m & n & c \end{vmatrix} \begin{vmatrix} bc - n^2 & mn - lc & ln - bm \\ mn - lc & ac - m^2 & ml - an \\ ln - bm & lm - an & ab - l^2 \end{vmatrix} = 64$. If the value of

$$\begin{vmatrix} 2a + 3l & 3l + 5m & 5m + 4a \\ 2l + 3b & 3b + 5n & 5n + 4l \\ 2m + 3n & 3n + 5c & 5c + 4m \end{vmatrix} = \lambda \text{ then } \left[\frac{\lambda}{2} \right] \text{ equals}$$

A. 120

B. 240

C. 360

D. 480

Answer: C



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30. The value of $\begin{vmatrix} x^2 + y^2 & ax + by & x + y \\ ax + by & a^2 + b^2 & a + b \\ x + y & a + b & 2 \end{vmatrix}$ depends on

A. a

B. b

C. x

D. none of these

Answer: D



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31. If $u = ax + by + cz$, $v = ay + bz + cx$, $w = ax + bx + cy$, then the value of

$$\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix} \times \begin{vmatrix} x & y & z \\ y & z & x \\ z & x & y \end{vmatrix} \text{ is}$$

A. $u^2 + v^2 + w^2 - 2uvw$

B. $u^3 + v^3 + w^3 - 3uvw$

C. 0

D. none of these

Answer: B



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32. If the number of positive integral solutions of $u + v + w = n$ be

denoted by P_n then the absolute value of
$$\begin{vmatrix} P_n & P_{n+1} & P_{n+2} \\ P_{n+1} & P_{n+2} & P_{n+3} \\ P_{n+2} & P_{n+3} & P_{n+4} \end{vmatrix}$$
 is

A. -1

B. 2

C. 3

D. 4

Answer: A



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33. If $f(x), g(x)$ are polynomials of degree 4 and $\begin{vmatrix} f(x) & g(x) & h(x) \\ a & b & c \\ p & q & r \end{vmatrix}$
 $= mx^4 + nx^3 + rx^2 + sx + r$ be an identity in x , then

$$\begin{vmatrix} f'(0) - f'(0) & g''(0) - g''(0) & h''(0) - h''(0) \\ a & b & c \\ p & q & r \end{vmatrix} \text{ is}$$

A. $2(3n - r)$

B. $2(2n - 3r)$

C. $3(n - 2r)$

D. none of these

Answer: A



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34. If $f(x) = \begin{vmatrix} x-2 & (x-1)^2 & x^3 \\ (x-1) & x^2 & (x+1)^3 \\ x & (x+1)^2 & (x+2)^3 \end{vmatrix}$ then coefficient of x in $f(x)$ is

A. -4

B. -2

C. -6

D. 0

Answer: B

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35. If $f(x) = \begin{vmatrix} \sin x & \cos x & \tan x \\ x^3 & x^2 & x \\ 2x & 1 & x \end{vmatrix}$, then $\lim_{x \rightarrow 0} \frac{f(x)}{x^2} =$

A. 0

B. 3

C. 2

D. 1

Answer: D



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36. If the system of linear equations $x + 2ay + az = 0, x + 3by + bz = 0,$
 $x + 4cy + cz = 0$ has a non-zero solution, then a, b, c

A. A. P.

B. G. P.

C. H. P.

D. satisfies $a + 2b + 3c = 0$

Answer: C



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37. Find all values of λ for which the system of equations

$$(\lambda - 1)x + (3\lambda + 1)y + 2\lambda z = 0$$
$$(\lambda - 1)x + (4\lambda - 2)y + (\lambda + 3)z = 0$$
$$2x + (3\lambda + 1)y + 3(\lambda + 3)z = 0$$

possess non-trivial solution and find the ratios $x:y:z$, where λ has the smallest of these value.

A. 3:2:1

B. 3:3:2

C. 1:3:1

D. 1:1:1

Answer: D



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38. The system of homogenous equations

$$tx + (t + 1)y + (t - 1)z = 0,$$

$$(t + 1)x + ty + (t + 2)z = 0,$$

$(t - 1)x + (t + 2)y + tz = 0$ has a non trivial solution for

A. exactly three real values of t

B. exactly two real values of t

C. exactly one real values of t

D. infinite number of values of t

Answer: C



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39. If a, b, c are non-zero, then the system of equations $(\alpha + a)x + \alpha y + \alpha z = 0$, $\alpha x + (\alpha + b)y + \alpha z = 0$, $\alpha x + \alpha y + (\alpha + c)z = 0$ has a non-trivial solution if $\alpha^{-1} =$ (A) $-(a^{-1} + b^{-1} + c^{-1})$ (B) $a + b + c$ (C) $\alpha + a + b + c = 1$ (D) none of these

A. $2\alpha = a + b + c$

B. $\alpha^{-1} = a + b + c$

C. $\alpha + a + b + c = 1$

D. $\alpha^{-1} = -(a^{-1} + b^{-1} + c^{-1})$

Answer: D



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40. The values of θ , λ for which the following equations $\sin\theta x - \cos\theta y + (\lambda + 1)z = 0$, $\cos\theta x + \sin\theta y - \lambda z = 0$, $\lambda x + (\lambda + 1)y + \cos\theta z = 0$ have non trivial solution, is

A. $\theta = n\pi, \lambda \in R - \{0\}$

B. $\theta = 2n\pi, \lambda$ is any rational number

C. $\theta = (2n + 1)\pi, \lambda \in R^+, n \in I$

D. $\theta = (2n + 1)\frac{\pi}{2}, \lambda \in R, n \in I$

Answer: D



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41. If the system of equation
(, $x - 2y + z = a$), ($2x + y - 2z = b$), and , ($x + 3y - 3z = c$)
have at least one solution, then

A. $a + b + c = 0$

B. $a - b + c = 0$

C. $-a + b + c = 0$

D. $a + b - c = 0$

Answer: B



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42. If A, B, C are the angles of a triangle, the system of equations

$(\sin A)x + y + z = \cos A$, $x + (\sin B)y + z = \cos B$, $x + y + (\sin C)z = 1 - \cos C$ has

A. No solution

B. Unique solution

C. Infinitely many solutions

D. Finitely many solutions

Answer: B



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Comprehension

1. A 3×3 determinant has entries either 1 or -1.

Let $S_3 =$ set of all determinants which contain determinants such that product of elements of any row or any column is -1 For example

$$\begin{vmatrix} 1 & -1 & 1 \\ 1 & 1 & -1 \\ -1 & 1 & 1 \end{vmatrix} \text{ is an element of the set } S_3.$$

Number of elements of the set $S_3 =$

A. 10

B. 16

C. 12

D. 18

Answer: B



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2. A 3×3 determinant has entries either 1 or -1.

Let $S_3 =$ set of all determinants which contain determinants such that product of elements of any row or any column is -1 For example

$\begin{vmatrix} 1 & -1 & 1 \\ 1 & 1 & -1 \\ -1 & 1 & 1 \end{vmatrix}$ is an element of the set S_3 .

Number of elements of the set $S_n =$

A. 2^n

B. 2^{n-1}

C. 2^{2n}

D. $2^{(n-1)^2}$

Answer: D



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Multiple Correct Answer

1. consider the fourth -degree polynomial equation

$$\begin{vmatrix} a_1 + b_1x & a_1x^2 + b_1 & c_1 \\ a_2 + b_2x^2 & a_2x^2 + b_2 & c_2 \\ a_3 + b_3x^2 & a_3x^2 + b_3 & c_3 \end{vmatrix} = 0$$

Without expanding the determinant find all the roots of the equation.

A. $x = 1$

B. $x = -1$

C. $\begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix} = 0$

D. none of these

Answer: A::B::C



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2. If $a_i, i = 1, 2, \dots, 9$ are perfect odd squares, then $\begin{vmatrix} a_1 & a_2 & a_3 \\ a_4 & a_5 & a_6 \\ a_7 & a_8 & a_9 \end{vmatrix}$ is

always a multiple of

A. 4

B. 7

C. 16

D. 64

Answer: A::C::D



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3. if determinant $\begin{vmatrix} \cos(0 + \phi) & -\sin(0 + \phi) & \cos 2\phi \\ \sin 0 & \cos 0 & \sin \phi \\ -\cos 0 & \sin 0 & \cos \phi \end{vmatrix}$ is

- A. independent of θ for all $\lambda \in R$
- B. independent of θ and α when $\lambda = 1$
- C. independent of θ and α when $\lambda = -1$
- D. independent of λ for all θ

Answer: A::C



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4. A solution set of the equations $x + 2y + z = 1$, $x + 3y + 4z = k$,
 $x + 5y + 10z = k^2$ is

- A. $(1 + 5\lambda, -3\lambda, \lambda)$
- B. $(5\lambda - 1, 1 - 3\lambda, \lambda)$

C. $(1 + 6\lambda, -2\lambda, \lambda)$

D. $(1 - 6\lambda, \lambda, \lambda)$

Answer: A::B



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5. Consider the system of equations : $x\sin\theta - 2y\cos\theta - az = 0, x + 2y + z = 0,$

$$-x + y + z = 0, \theta \in R$$

A. The given system will have infinite solutions for $a = 2$

B. The number of integer values of a is 3 for the system to have nontrivial solutions.

C. For $a = 1$ there exists θ for which the system will have infinite solutions

D. For $a = 3$ there exists θ for which the system will have unique solutions

Answer: B::C::D



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Examples

1. find the value of $\begin{vmatrix} 1 & 2 & 4 \\ -1 & 3 & 0 \\ 4 & 1 & 0 \end{vmatrix}$



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2. Prove that the determinant $\Delta = \begin{vmatrix} x & \sin\theta & \cos\theta \\ -\sin\theta & -x & 1 \\ \cos\theta & 1 & x \end{vmatrix}$ is independent

of θ .



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3. The parameter on which the value of the determinant $\begin{vmatrix} 1 & a^2 \cos(p-d)x & \cos px & \cos(p+d)x \\ \sin(p-d)x & \sin px & \sin(p+d)x & x \end{vmatrix}$ does not depend is a b p c d x

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4. Let a, b, c be positive and not all equal. Show that the value of the

determinant $\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$ is negative

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5. If $a, b, c \in R$, then find the number of real roots of the equation $|xc - b - cxab - ax| = 0$

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6. If $x + y + z = 0$, prove that
$$\begin{vmatrix} ax & by & cz \\ cy & az & bx \\ bz & cx & ay \end{vmatrix} = xyz \begin{vmatrix} a & b & c \\ c & a & b \\ b & c & a \end{vmatrix}$$

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7. If $p\lambda^4 + q\lambda^3 + r\lambda^2 + s\lambda + t = \begin{vmatrix} \lambda^2 + 3\lambda & \lambda - 1 & \lambda + 3 \\ \lambda^2 + 1 & 2 - \lambda & \lambda - 3 \\ \lambda^2 - 3 & \lambda + 4 & 3\lambda \end{vmatrix}$ then $t =$

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8. The largest value of a third order determinant whose elements are equal to 1 or 0 is

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9. Prove that the value of the determinant

$$\begin{vmatrix} -7 & 5 + 3i & \frac{2}{3} - 4i \\ 5 - 3i & 8 & 4 + 5i \\ \frac{2}{3} + 4i & 4 - 5i & 9 \end{vmatrix} \text{ is real}$$



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10. Without expanding the determinants Prove that

$$\begin{vmatrix} 103 & 115 & 114 \\ 111 & 108 & 106 \\ 104 & 113 & 116 \end{vmatrix} + \begin{vmatrix} 113 & 116 & 104 \\ 108 & 106 & 111 \\ 115 & 114 & 103 \end{vmatrix} = 0$$



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11. Prove that

$$\begin{vmatrix} ax & by & cz \\ x^2 & y^2 & z^2 \\ 1 & 1 & 1 \end{vmatrix} = \begin{vmatrix} a & c & c \\ x & y & z \\ yz & xz & xy \end{vmatrix}$$



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12. for $x, y, z > 0$ Prove that

$$\begin{vmatrix} 1 & \log_x y & \log_x z \\ \log_y x & 1 & \log_y z \\ \log_z x & \log_z y & 1 \end{vmatrix} = 0$$



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13. without expanding at any stage Prove that

$$\begin{vmatrix} 0 & a & -b \\ -a & 0 & -c \\ b & c & 0 \end{vmatrix} = 0$$



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14. consider the fourth -degree polynomial equation

$$\begin{vmatrix} a_1 + b_1x & a_1x^2 + b_1 & c_1 \\ a_2 + b_2x^2 & a_2x^2 + b_2 & c_2 \\ a_3 + b_3x^2 & a_3x^2 + b_3 & c_3 \end{vmatrix} = 0$$

Without expanding the determinant find all the roots of the equation.

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15. Let $\Delta_r = \begin{vmatrix} r - 1 & n & 6(r - 1)^2 & 2n^2 & 4n - 2(r - 1)^2 & 3n^3 & 3n^2 - 3n \end{vmatrix}$ Show that $\sum_{r=1}^n \Delta_r$ is constant.

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16. Find the value of $\begin{vmatrix} 41 & 1 & 5 \\ 79 & 7 & 9 \\ 29 & 5 & 3 \end{vmatrix}$

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17. Find the value of determinant

$$\begin{vmatrix} \sqrt{13} + \sqrt{32}\sqrt{5}\sqrt{5}\sqrt{15} & \sqrt{26} & 5\sqrt{10} & 3 + \sqrt{65}\sqrt{15} & 5 \end{vmatrix}$$

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18. Find the value of the determinant

$$\begin{vmatrix} 1 & 1 & 1 & 1 \\ 1 & 2 & 3 & 4 \\ 1 & 3 & 6 & 10 \\ 1 & 4 & 10 & 20 \end{vmatrix}$$

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19. Prove that

$$\begin{vmatrix} \sin\alpha & \cos\alpha & \sin(\alpha + \delta) \\ \sin\beta & \cos\beta & \sin(\beta + \delta) \\ \sin\gamma & \cos\gamma & \sin(\gamma + \delta) \end{vmatrix} = 0$$

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20. Solve for x $|x^3 - 22x^2 - 33x - 4x^3 - 42x^2 - 93x - 16x^3 - 82x^2 - 273x - 64| = 0$.

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21. By using properties of determinants, prove the following:

$$|x + 4 \quad 2x \quad 2x^2 \quad x + 4| = (5x + 4)(4 - x)^2$$

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22. prove that
$$\begin{bmatrix} a - b - c & 2a & 2a \\ 2b & b - c - a & 2b \\ 2c & 2c & c - a - b \end{bmatrix} = (a + b + c)^3$$

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23. if $x_i = a_i b_i c_i, i = 1, 2, 3$ are three- digit positive integer such that

each x_i is a multiple of 19 then prove that $\det \begin{Bmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{Bmatrix}$ is

divisible by 19.

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24. If a, b and c are real numbers, and

$$\Delta = \begin{vmatrix} b+c & C+a & a+b \\ c+a & a+b & b+c \\ a+b & b+c & c+a \end{vmatrix} = 0$$

Show that either $a + b + c = 0$ or $a = b = c$.

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25. Find the value of the determinant $|baabpqr111|$, where a, b , and c are respectively, the p th, q th, and r th terms of a harmonic progression.

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26.

if a_1, a_2, a_3, \dots are in A.P, then find the value of the following determinant:

$$\begin{vmatrix} a_p + a_{p+m} + a_{p+2m} & 2a_p + 3a_{p+m} + 4a_{p+2m} & 4a_p + 9a_{p+m} + 16a_{p+2m} \\ a_p + a_{q+m} + a_{q+2m} & 2a_q + 3a_{q+m} + 4a_{q+2m} & 4a_q + 9a_{q+m} + 16a_{q+2m} \\ a_r + a_{r+m} + a_{r+2m} & 2a_r + 3a_{r+m} + 4a_{r+2m} & 4a_r + 9a_{r+m} + 16a_{r+2m} \end{vmatrix}$$

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27. Prove that

$$\left| \begin{pmatrix} 1, & \beta\gamma + \alpha\delta, & \beta^2\gamma^2 + \alpha^2, & \delta^2 \end{pmatrix}, \begin{pmatrix} 1, & \gamma\alpha + \beta\delta, & \gamma^2\alpha^2 + \beta^2\delta^2 \end{pmatrix}, \begin{pmatrix} 1, & \alpha\beta + \gamma\delta, & \alpha^2\beta^2 + \gamma^2\delta^2 \end{pmatrix} \right|$$

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28. Prove that

$$\left| \begin{matrix} ab + ca^2bc + ab^2ca + bc^2 \\ - (a + b + c) \times (a - b)(b - c)(c - a) \end{matrix} \right|$$

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29. Prove that

$$\begin{vmatrix} x^2 & x^2 - (y - z)^2 & yz \\ y^2 & y^2 - (z - x)^2 & zx \\ z^2 & z^2 - (x - y)^2 & xy \end{vmatrix}$$

$$= (x - y)(y - z)(z - x)(x + y + z)(x^2 + y^2 + z^2)$$

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30. If a, b, c are all distinct and $\begin{vmatrix} a & a^3 & a^4 - 1 \\ b & b^3 & b^4 - 1 \\ c & c^3 & c^4 - 1 \end{vmatrix} = 0$, show that

$$abc(ab+bc+ac) = a+b+c$$

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31. Prove that $\begin{vmatrix} a^2 + 1 & ab & ac \\ ab & b^2 + 1 & bc \\ ac & bc & c^2 + 1 \end{vmatrix} = 1 + a^2 + b^2 + c^2$

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32. prove that
$$\begin{vmatrix} (b+c)^2 & bc & ac \\ ba & (c+a)^2 & cb \\ ca & cb & (a+b)^2 \end{vmatrix}$$

$$\begin{vmatrix} (b+c)^2 & a^2 & a^2 \\ b^2 & (c+a)^2 & b^2 \\ c^2 & c^2 & (a+b)^2 \end{vmatrix} = 2abc(a+b+c)^3$$

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33. Let a, b, c be real numbers with $a^2 + b^2 + c^2 = 1$. Show that the equation

$$|ax - by - cbx - aycx + abx + ay - ax + by - y + bcx + acy + b - ax - by + c| = 0$$

represents a straight line.

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34. If $a^2 + b^2 + c^2 = 1$, then prove that

$$\left| a^2 + (b^2 + c^2) \cos \phi \right| ab(1 - \cos \phi) ac(1 - \cos \phi) ba(1 - \cos \phi) b^2 + (c^2 + a^2) \cos \phi bc(1 - \cos \phi)$$

is independent of $a, b,$ ·



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35. Find the area of a triangle having vertices $A(3, 2), B(11, 8),$ and $C(8, 12)$ ·



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36. If the lines $a_1x + b_1y + 1 = 0, a_2x + b_2y + 1 = 0$ and $a_3x + b_3y + 1 = 0$ are concurrent, show that the points $(a_1, b_1), (a_2, b_2)$ and (a_3, b_3) are collinear.



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37. The number of values of a for which the lines $2x + y - 1 = 0,$ $ax + 3y - 3 = 0,$ and $3x + 2y - 2 = 0$ are concurrent is 0 (b) 1 (c) 2 (d) infinite



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38. If the lines $ax + y + 1 = 0$, $x + by + 1 = 0$ and $x + y + c = 0$ (a, b, c being distinct and different from 1) are concurrent, then prove that

$$\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} = 1.$$



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39. Find the value of λ if $2x^2 + 6xy + 3y^2 + 8x + 14y + \lambda = 0$ represent a pair of straight lines.



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40. show that the determinant

$$\begin{vmatrix} a^2 + b^2 + c^2 & bc + ca + ab & bc + ca + ab \\ bc + ca + ab & a^2 + b^2 + c^2 & bc + ca + ab \\ bc + ca + ab & bc + ca + ab & a^2 + b^2 + c^2 \end{vmatrix}$$

is always non-negative.



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41. Factorize the following

$$3a + b + ca^3 + b^3 + c^3a + b + ca^2 + b^2 + c^2a^4 + b^4 + c^4a^2 + b^2 + c^2a^3 + b^3 + c^3$$



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42. prove that

$$\begin{vmatrix} (a-x)^2 & (a-y)^2 & (a-z)^2 \\ (b-x)^2 & (b-y)^2 & (b-z)^2 \\ (c-x)^2 & (c-y)^2 & (c-z)^2 \end{vmatrix}$$

$$\begin{vmatrix} (1+ax)^2 & (1+bx)^2 & (1+cx)^2 \\ (1+ay)^2 & (1+by)^2 & (1+cy)^2 \\ (1+az)^2 & (1+bx)^2 & (1+cz)^2 \end{vmatrix}$$

$$= 2(b-c)(c-a)(a-b) \times (y-z)(z-x)(x-y)$$



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43. If α, β, γ are real numbers, then without expanding at any stage, show that $|\cos(\beta - \alpha)\cos(\gamma - \alpha)\cos(\alpha - \beta)\cos(\gamma - \beta)\cos(\alpha - \gamma)\cos(\beta - \gamma)| = 0$

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44. If $\begin{vmatrix} 1 & x & x^2 \\ x & x^2 & 1 \\ x^2 & 1 & x \end{vmatrix} = 3$ then find the value of $\begin{vmatrix} x^3 - 1 & 0 & x - x^4 \\ 0 & x - x^4 & x^3 - 1 \\ x - x^4 & x^3 - 1 & 0 \end{vmatrix}$

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45. Show that

$$\left| bc - a^2ca - b^2ab - c^2ca - b^2ab - c^2bc - a^2ab - c^2bc - a^2ca - b^2 \right| = \left| a^2c^22ac - b^22a \right|$$

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46. Let $f(x) = \begin{vmatrix} \cos x & \sin x & \cos x \\ \cos 2x & \sin 2x & 2\cos 2x \\ \cos 3x & \sin 3x & 3\cos 3x \end{vmatrix}$ then find the values of $f(0)$ and $f(\pi/2)$.

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47. If $f(x) = \begin{vmatrix} x^n & 2\cos x & \frac{\cos(n\pi)}{2} & 4\sin x & \frac{\sin(n\pi)}{2} & 8 \end{vmatrix}$ then find the value of $\frac{d^n}{dx^n} (f(x))_{x=0}$ $n \in \mathbb{Z}$

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48. If $f, g,$ and h are differentiable functions of

x and $\Delta(x) = \begin{vmatrix} fgh & (xf)' & (xg)' & (xh)' \\ (x^2f)'' & (x^2g)'' & (x^2h)'' \end{vmatrix}$ prove

$\Delta'(x) = \begin{vmatrix} (fgh)' & f'g'h' & (x^3f)'' & (x^3g)'' & (x^3h)'' \end{vmatrix}$

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49. Let α be a repeated root of a quadratic equation $f(x) = 0$ and $A(x), B(x), C(x)$ be polynomials of degrees 3, 4, and 5, respectively, then show that $|A(x)B(x)C(x)A(\alpha)B(\alpha)C(\alpha)A'(\alpha)B'(\alpha)C'(\alpha)|$ is divisible by $f(x)$, where prime (') denotes the derivatives.

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50. if $\Delta(x) = \begin{vmatrix} a_1 + x & b_1 + x & c_1 + x \\ a_2 + x & b_2 + x & c_2 + x \\ a_3 + x & b_3 + x & c_3 + x \end{vmatrix}$ then show that $\Delta(x) = 0$

and that $\Delta(x) = \Delta(0) + sx$. where s denotes the sum of all the cofactors of all the elements in $\Delta(0)$

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51. If $\Delta(x) = \begin{vmatrix} 1 & x^2 & x^2 & 6 & 4x & 39 & x & -7 \end{vmatrix}$ then find the value of $\int_0^1 \Delta(x) dx$

without expanding $\Delta(x)$.



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52. Find the value of a and b if the system of equations $a^2x - by = a^2 - b$ and $bx = b^2y = 2 + 4b$ (i) possesses unique solution (ii) infinite solutions



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53. If a system of three linear equations $x + 4ay + a = 0$, $x + 3by + b = 0$, and $x + 2cy + c = 0$ is consistent, then prove that a, b, c are in H.P.



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54. Solve by Cramer's rule $x + y + z = 6$, $x - y + z = 2$, $3x + 2y - 4z = -5$



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55. For what values of p and q the system of equations $2x + py + 6z = 8$, $x + 2y + qz = 5$, $x + y + 3z = 4$ has i no solution ii a unique solution iii in finitely many solutions.

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56. If $2ax - 2y + 3z = 0$, $x + ay + 2z = 0$, and $2 + az = 0$ have a nontrivial solution, find the value of a .

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57. For what values of k , the following system of equations possesses a nontrivial solution over the set of rationals:
 $c + ky + 3z = 0$, $3c + ky - 2z = 0$, $2c + 3y - 4x = 0$. Also find the solution for this value of k .

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58. Using factor theorem, show that

$$\begin{vmatrix} -2a & a+b & c+a \\ a+b & -2a & b+c \\ c+a & c+b & -2c \end{vmatrix} = 4(a+b)(b+c)(c+a)$$

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59. If a, b and c are non-zero real number then prove that

$$\begin{vmatrix} b^2c^2 & bc & b+c \\ c^2a^2 & ca & c+a \\ a^2b^2 & ab & a+b \end{vmatrix} = 0$$

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60. Prove that

$$|ax - by - cz + bxcx + azay + bxby - cz - axbz + cycx + azbz + cycz - ax - by| = (x$$

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61. If $f(x)$ is a polynomial of degree < 3 , prove that

$$\left| \frac{1af(a)}{(x-a)} \frac{1bf(b)}{(x-b)} \frac{1cf(c)}{(x-c)} \right| \div \left| 1aa^2 \ 1 \ 21 \ 2 \right| = \frac{f(x)}{(x-a)(x-b)(x-c)}$$

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$$62. \begin{vmatrix} 2a_1b_1 & a_1b_2 + a_2b_1 & a_1b_3 + a_3b_1 \\ a_1b_2 + a_2b_1 & 2a_2b_2 & a_2b_3 + a_3b_2 \\ a_1b_3 + a_3b_1 & a_3b_2 + a_2b_3 & 2a_3b_3 \end{vmatrix} =$$

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63. Find the value of

$$\begin{vmatrix} \cos\left(\frac{2\pi}{63}\right) & \cos\left(\frac{3\pi}{70}\right) & \cos\left(\frac{4\pi}{77}\right) \\ \cos\left(\frac{\pi}{72}\right) & \cos\left(\frac{\pi}{40}\right) & \cos\left(\frac{3\pi}{88}\right) \\ 1 & \cos\left(\frac{\pi}{90}\right) & \cos\left(\frac{2\pi}{99}\right) \end{vmatrix}$$

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64. Let $f(t) = \begin{vmatrix} \cos t & t & 1 \\ 2\sin t & t & 2t \\ \sin t & t & t \end{vmatrix}$. Then find $\lim_{t \rightarrow 0} \frac{f(t)}{t^2}$

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65. it

$$x_1^2 + 2y_1^2 + 3z_1^2 = x_2^2 + 2y_2^2 + 3z_2^2 = x_3^2 + 2y_3^2 + 3z_3^2 = 2 \text{ and } x_2x_3 + 2y_2y_3 + 3z_2z_3 =$$

Then find the value of $\begin{vmatrix} x_1 & y_1 & z_1 \\ x_2 & y_2 & z_2 \\ x_3 & y_3 & z_3 \end{vmatrix}$

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66. about to only mathematics

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67. If $bc + qr = ca + rp = ab + pq = -1$ and $(abc, pqr \neq 0)$ then $\begin{vmatrix} ap & a & p \\ bq & b & q \\ cr & c & r \end{vmatrix}$

is (A) 1 (B) 2 (C) 0 (D) 3

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Exercise 12.1

1. Evaluate $|\cos\alpha\cos\beta\cos\alpha\sin\beta - \sin\alpha - \sin\beta\cos\beta\sin\alpha\cos\beta\sin\alpha\sin\beta\cos\alpha|$

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2. If A,B,C are the angles of a non right angled triangle ABC. Then find the

value of: $\begin{vmatrix} \tan A & 1 & 1 \\ 1 & \tan B & 1 \\ 1 & 1 & \tan C \end{vmatrix}$

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3. If $e^{i\theta} = \cos\theta + i\sin\theta$, find the value of

$$\left| 1e^{i\pi/3}e^{i\pi/4}e^{-i\pi/3}1e^{i2\pi/3}e^{-i\pi/4}e^{-i2\pi/3}1 \right|$$

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4. Find the number of real root of the equation

$$|0x - ax - bx + a0x - cx + bx + c0| = 0, a \neq b \neq c \text{ and } b(a + c) > ac$$

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5. If α, β, γ are the roots of

$$ax^3 + bx^2 + cx + d = 0 \text{ and } |\alpha\beta\gamma\beta\gamma\alpha\gamma\alpha\beta| = 0, \alpha \neq \beta \neq \gamma \text{ then find the equation}$$

whose roots are $\alpha + \beta - \gamma, \beta + \gamma - \alpha$, and $\gamma + \alpha - \beta$.

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6. A triangle has vertices $A_i(x_i, y_i)$ for $i = 1, 2, 3$. If the orthocenter of triangle is $(0, 0)$ then prove that

$$\begin{vmatrix} x_2 - x_3 & y_2 - y_3 & y_1(y_2 - y_3) + x_1(x_2 - x_3) \\ x_3 - x_1 & y_3 - y_1 & y_2(y_3 - y_1) + x_2(x_3 - x_1) \\ x_1 - x_2 & y_1 - y_2 & y_3(y_1 - y_2) + x_3(x_1 - x_2) \end{vmatrix} = 0$$

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7. if $\omega \neq 1$ is cube root of unity and $x+y+z \neq 0$ then

$$\begin{vmatrix} \frac{x}{1+\omega} & \frac{y}{\omega+\omega^2} & \frac{z}{\omega^2+1} \\ \frac{y}{\omega+\omega^2} & \frac{z}{\omega^2+1} & \frac{x}{1+\omega} \\ \frac{z}{\omega^2+1} & \frac{x}{1+\omega} & \frac{y}{\omega+\omega^2} \end{vmatrix} = 0 \text{ if}$$

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1. Prove that the value of determinant $\begin{vmatrix} 1 & \omega & \omega^2 \\ \omega & \omega^2 & 1 \\ \omega^2 & 1 & \omega \end{vmatrix} = 0$

where ω is complex cube root of unity .

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2. Prove that $\begin{vmatrix} a & a^2 & bc \\ b & b^2 & ac \\ c & c^2 & ab \end{vmatrix} \begin{vmatrix} 1 & 1 & 1 \\ a^2 & b^2 & c^2 \\ a^3 & b^3 & c^3 \end{vmatrix}$

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3. if $\Delta = \begin{vmatrix} abc & a_2 & c^2b \\ abc & c^2a & ca^2 \\ abc & a^2b & b^2a \end{vmatrix} = 0$, ($a, b, c \in R$ and are all

different and non-zero) the prove that $a + b + c = 0$

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4. if $a_r = (\cos 2r\pi + i \sin 2r\pi)^{1/9}$ then prove that

$$\begin{vmatrix} a_1 & a_2 & a_3 \\ a^4 & a^5 & a_6 \\ a_7 & a_8 & a_9 \end{vmatrix} = 0$$

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5. Given $A = |ab2cde2flm2n|$, $B = |f2de2n4l2mc2ab|$, then the value of B/A is _____.

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Exercise 12.3

1. Prove that the value of each the following determinants zero:

$$(a) \begin{vmatrix} a_1 & la_1 + mb_1 & b_1 \\ a_2 & la_2 + mb_2 & b_2 \\ a_3 & la_3 + mb_3 & b_3 \end{vmatrix}$$



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2. using properties of determinants evaluate

$$\begin{vmatrix} 18 & 40 & 89 \\ 40 & 89 & 198 \\ 89 & 198 & 440 \end{vmatrix}$$



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3. Prove that $\begin{vmatrix} 18 & 40 & 89 \\ 40 & 89 & 198 \\ 89 & 198 & 440 \end{vmatrix} = 3abc - a^3 - b^3 - c^3$



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$$4. \begin{bmatrix} 1 & 1+p & 1+p+q \\ 2 & 3+2p & 4+3p+2q \\ 3 & 6+3p & 10+6p+3q \end{bmatrix} = 1$$



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$$5. \text{ Show that } \begin{vmatrix} a-x & c & b \\ c & b-x & a \\ b & a & c-x \end{vmatrix} = 0$$

where $a + b + c \neq 0$



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6. Show that:

$$[3a - a + b - a + c - b + a3b - b + c - c + a - c + b3c] = 3(a + b + c)(ab + bc + ca)$$



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7. Using properties of determinants Prove that

$$\begin{vmatrix} a+b+c & -c & -b \\ -c & a+b+c & -a \\ -b & -a & a+b+c \end{vmatrix} = 2(a+b)(b+c)(c+a)$$

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8. Solve $\begin{vmatrix} x^2 - 1 & x^2 + 2x + 1 & 2x^2 + 3x + 1 \\ 2x^2 + x - 1 & 2x^2 + 5x - 3 & 4x^2 + 4x - 3 \\ 6x^2 - x - 2 & 6x^2 - 7x + 2 & 12x^2 - 5x - 2 \end{vmatrix} = 0$

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9. By using properties of determinants, show that :

$$\begin{bmatrix} 1 + a^2 - b^2 & 2ab & -2b \\ 2ab & 1 - a^2 + b^2 & 2a \\ 2b & -2a & 1 - a^2 - b^2 \end{bmatrix} = (1 + a^2 + b^2)^3$$

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10. Show that if $x_1, x_2, x_3 \neq 0$

$$\begin{vmatrix} x_1 + a_1b_1 & a_1b_2 & a_1b_3 \\ a_2b_1 & x_2 + a_2b_2 & a_2b_3 \\ a_3b_1 & a_3b_2 & x_3 + a_3b_3 \end{vmatrix}$$

$$= x_1x_2x_3 \left(1 + \frac{a_1b_1}{x_1} + \frac{a_2b_2}{x_2} + \frac{a_3b_3}{x_3} \right)$$



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11. If A, B and C are the angles of a triangle, show that

$$-1 + \cos B \cos C + \cos C \cos A + \cos A \cos B - 1 + \cos A - 1 + \cos B - 1 + \cos A - 1$$



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12. If $\begin{vmatrix} a^2 & b^2 & c^2 \\ (a+b)^2 & (b+1)^2 & (c+1)^2 \\ (a-1)^2 & (b-1)^2 & (c-1)^2 \end{vmatrix} = k(a-b)(b-c)(c-a)$ then the value of

k is a. 4 b. -2 c. -4 d. 2



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13. Prove that $\Delta = \begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ bc + 1^2 & ac + b^2 & ab + c^2 \end{vmatrix}$

$$= 2(a - b)(b - c)(c - 1)$$



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14. Evaluate $\begin{vmatrix} \cdot^x C_1 & \cdot^x C_2 & \cdot^x C_3 \\ \cdot^y C_1 & \cdot^y C_2 & \cdot^y C_3 \\ \cdot^z C_1 & \cdot^z C_2 & \cdot^z C_3 \end{vmatrix}$



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15. if $\Delta_r = \begin{vmatrix} 2^{r-1} & 2 \times 3^{r-1} & 4 \times 5^{r-1} \\ \alpha & \beta & \gamma \\ 2^n - 1 & 3^n - 1 & 5^n - 1 \end{vmatrix}$

then find the value of $\sum_{r=1}^n \Delta_r$.

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16. Prove that

$$|1 + a11111 + b11111 + c11111 + d| = abcd \left(a + \frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d} \right). \quad \text{Hence}$$

find the value of the determinant if a, b, c, d are the roots of the equation

$$px^4 + qx^3 + rx^2 + sx + t = 0.$$

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17. Prove that

$$\begin{vmatrix} 1 & ab & \frac{1}{a} + \frac{1}{b} \\ 1 & bc & \frac{1}{b} + \frac{1}{c} \\ 1 & ca & \frac{1}{c} + \frac{1}{a} \end{vmatrix} = 0$$

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18. Prove the identities: $\left| b^2 + c^2abacbac^2 + a^2bacba^2 + b^2 \right| = 4a^2b^2c^2$

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19. Show that

$$\begin{vmatrix} a & b - c & c + b \\ a + c & b & c - a \\ a - b & b + a & c \end{vmatrix} = (a + b + c)(a^2 + b^2 + c^2)$$

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Exercise 12.4

1. If x_1, x_2, x_3 as well as y_1, y_2, y_3 are in G.P. with same common ratio, then prove that the points (x_1, y_1) , (x_2, y_2) , and (x_3, y_3) are collinear.



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2. If lines $px + qy + r = 0$, $qx + ry + p = 0$ and $rx + py + q = 0$ are concurrent, then prove that $p + q + r = 0$ (where p, q, r are distinct).



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3. _____ if

$$(x_1, x_2)^2 + (y_1 - y_2)^2 = a^2, (x_2 - x_3)^2 + (y_2 - y_3)^2 = b^2 (x_3 - x_1)^2 + (y_3 - y_1)^2$$

where a, b, c are positive then prove that

$$4 \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix} = (a + b + c)(b + c - a)(c + a - b)(a + b - c)$$

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4. it is known that the equation of hyperbola and that of its pair of asymptotes differ by constant . If equation of hyperbola is $x^2 + 4xy + 3y^2 - 4x + 2y + 1 = 0$ then find the equation of its pair of asymptotes.

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Exercise 12.5

1. Prove that

$$|(b+x)(c+x)(v+x)(a+x)(a+x)(b+x)(b+y)(c+y)(c+x)(a+t)(a+y)(b+y)(b$$

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$$2. \Delta = \begin{vmatrix} 1 + a^2 + a^4 & 1 + ab + a^2b^2 & 1 + ac + a^2c^2 \\ 1 + ab + a^2b^2 & 1 + b^2 + b^4 & 1 + bc + b^2c^2 \\ 1 + ac + a^2c^2 & 1 + bc + b^2c^2 & 1 + c^2 + c^4 \end{vmatrix} \text{ is equal to}$$

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3.

Prove

that

$$|2\alpha + \beta + \gamma + \delta| \alpha\beta + \gamma\delta \alpha + \beta + \gamma + \delta = 2(\alpha + \beta)(\gamma + \delta) \alpha\beta(\gamma + \delta) + \gamma\delta(\alpha + \beta)\alpha\beta + \gamma\delta\alpha\beta(\gamma + \delta)$$

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4. For all values of A, B, C and P, Q, R show that

$$|\cos(A - P)\cos(A - Q)\cos(A - R)\cos(B - P)\cos(B - Q)\cos(B - R)\cos(C - P)\cos(C - Q)\cos(C - R)|$$

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5. Show that: $\left| b^2 + c^2 abacbac^2 + a^2 bacba^2 + b^2 \right| = 4a^2 b^2 c^2$

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6. Express $\left| 2bc - a^2 c^2 b^2 c^2 2ca - b^2 a^2 b 6 2 a^2 2ab - c^2 \right|$ as square of a determinant of hence evaluate if.

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Exercise 12.6

1. Let $f(x) = \begin{vmatrix} \cos(x + x^2) & \sin(x + x^2) & -\cos(x + x^2) \\ \sin(x - x^2) & \cos(x - x^2) & \sin(x - x^2) \\ \sin 2x & 0 & \sin(2x^2) \end{vmatrix}$.

Find the value of $f'(0)$.

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2. If $f(x), g(x)$ and $h(x)$ are three polynomials of degree 2, then prove that $\varphi(x) = |f(x)g(x)h(x)f'(x)g'(x)h'(x)f''(x)g''(x)h''(x)|$ is a constant polynomial.

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3. If $g(x) = \frac{f(x)}{(x-a)(x-b)(x-c)}$, where $f(x)$ is a polynomial of degree < 3 , then prove that

$$\frac{dg(x)}{dx} = \left| 1af(a)(x-a)^{-2}1bf(b)(x-b)^{-2}1cf(c)(x-c)^{-2} \right| + \left| a^2a1b^2b1c^2c1 \right|$$

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4. If $f(x) = \begin{vmatrix} \cos(x + \alpha) & \cos(x + \beta) & \cos(x + \gamma) \\ \sin(x + \alpha) & \sin(x + \beta) & \sin(x + \gamma) \\ \sin(\beta - \gamma) & \sin(\gamma - \alpha) & \sin(\alpha - \beta) \end{vmatrix}$ and

$f(0) = 2$ then find the value of $\sum_{r=1}^{30} |f(r)|$.

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5. $f(x) = \begin{vmatrix} \cos x & x & 1 \\ 2\sin x & x^2 & 2x \\ \tan x & x & 1 \end{vmatrix}$ then find the value of

$$\lim_{x \rightarrow 0} \frac{f(x)}{x}$$

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Exercise 12.7

1. Find the following system of equations is consistent, $(a + 1)^3x + (a + 2)^3y = (a + 3)^3(a + 1)x + (a + 2)y = a + 3 + 1$, then find the value of a .

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2. Solve the system of the equations: $ax + by + cz = d$ $a^2x + b^2y + c^2z = d^2$ $a^3x + b^3y + c^3z = d^3$ Will the solution always exist and be unique?

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3. consider the system of equations : $3x - y + 4z = 3$

$$x + 2y - 3z = -2$$

$$6x + 5y + \lambda z = -3$$

Prove that system of equation has at least one solution for all real values of λ .also prove that infinite solutions of the system of equations satisfy

$$\frac{7x - 4}{-5} = \frac{7y + 9}{13} = z$$



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4. If the equation $2x + 3y + 1 = 0$, $3x + y - 2 = 0$, and $ax + 2y - b = 0$ are consistent, then prove that $a - b = 2$.



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5. if x, y and z are not all zero and connected by the equations $a_1x + b_1y + c_1z = 0$, $a_2x + b_2y + c_2z = 0$ and

$(p_1 + \lambda q_1)x + (p_2 + \lambda q_2)y + (p_3 + \lambda q_3)z = 0$ show that

$$\lambda = - \frac{\begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ p_1 & p_2 & p_3 \end{vmatrix}}{\begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ q_1 & q_2 & q_3 \end{vmatrix}}$$



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Exercise (Single)

1. if $\theta \in R$ then maximum value of $\Delta = \begin{vmatrix} 1 & 1 & 1 \\ 1 & 1 + \sin\theta & 1 \\ 1 & 1 & 1 + \cos\theta \end{vmatrix}$ is

A. $\sqrt{3}/2$

B. $1/2$

C. $1/\sqrt{2}$

D. None of these

Answer: B



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2. If $p + q + r = a + b + c = 0$, then the determinant $\begin{vmatrix} pa & qb & rc \\ qc & ra & pb \\ rb & pc & qa \end{vmatrix}$ equals

A. 0

B. $pa + qb + rc$

C. 1

D. none of these

Answer: A



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3. If α, β, γ are the roots of $px^2 + qx^2 + r = 0$, then the value of the determinant $|\alpha\beta\beta\gamma\gamma\alpha\beta\gamma\gamma\alpha\alpha\beta\gamma\alpha\alpha\beta\beta\gamma|$ is p b. q c. 0 d. r

A. p

B. q

C. 0

D. r

Answer: C



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4. If $f(x) = a + bx + cx^2$ and α, β, γ are the roots of the equation $x^3 = 1$, then $|abc|$ is equal to $f(\alpha) + f(\beta) + f(\gamma)$
 $f(\alpha)f(\beta) + f(\beta)f(\gamma) + f(\gamma)f(\alpha) - f(\alpha)f(\beta)f(\gamma)$

A. $f(\alpha) + f(\beta) + f(\gamma)$

B. $f(\alpha)f(\beta) + f(\beta)f(\gamma) + f(\gamma)f(\alpha)$

C. $f(\alpha)f(\beta)f(\gamma)$

D. $-f(\alpha)f(\beta)f(\gamma)$

Answer: D

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5. If $[.]$ denotes the greatest integer less than or equal to the real number under consideration, and $-1 \leq x < 0, 0 \leq y < 1, 1 \leq a < 2$, then the value

of the determinant
$$\begin{vmatrix} [x] + 1 & [y] & [z] \\ [x] & [y] + 1 & [z] \\ [x] & [y] & [z] + 1 \end{vmatrix}$$
 is

- a. $[x]$
- b. $[y]$
- c. $[z]$
- d. none of these

- A. $[x]$
- B. $[y]$
- C. $[z]$
- D. none of these

Answer: C

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6. if $a = \cos\theta + i\sin\theta$, $b = \cos2\theta - i\sin2\theta$, $c = \cos3\theta + i\sin3\theta$ and if

$$\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix} = 0 \text{ then}$$

A. $\theta = 2k\pi, k \in \mathbb{Z}$

B. $\theta = (2k + 1)\pi, k \in \mathbb{Z}$

C. $\theta = (4k + 1)\pi, k \in \mathbb{Z}$

D. none of these

Answer: A



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7. If $\begin{vmatrix} x^n & x^{n+2} & x^{n+3} \\ y^n & y^{n+2} & y^{n+3} \\ z^n & z^{n+2} & z^{n+3} \end{vmatrix} = (x - y)(y - z)(z - x) \left(\frac{1}{x} + \frac{1}{y} + \frac{1}{z} \right)$, then n equals

A. 1

B. -1

C. 2

D. -2

Answer: B



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8. If the determinant $\begin{vmatrix} \cos 2x & \sin^2 x & \cos 4x \\ \sin^2 x & \cos 2x & \cos^2 x \\ \cos 4x & \cos^2 x & \cos 2x \end{vmatrix}$ is expanded in powers of $\sin x$

, then the constant term is

A. 1

B. 0

C. -1

D. 2

Answer: C



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9. about to only mathematics

A. -2

B. -4

C. 0

D. -8

Answer: B



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10. If $A + B + C = \pi$ and $e^{i\theta} = \cos\theta + i\sin\theta$ and $z = \begin{vmatrix} e^{2iA} & e^{-iC} & e^{-iB} \\ e^{-iC} & e^{2iB} & e^{-iA} \\ e^{-iB} & e^{-iA} & e^{2iC} \end{vmatrix}$, then

A. 1

B. -1

C. -2

D. -4

Answer: D

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11. If a, b, c are different, then the value of x for which

$$\begin{vmatrix} 0 & x^2 - a & x^3 - b \\ x^2 + a & 0 & x^2 + c \\ x^4 + b & x - c & 0 \end{vmatrix} = 0 \text{ is}$$

A. a

B. c

C. b

D. 0

Answer: D



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12. If the value of determinant $|(a,1,1),(1,b,1),(1,1,c)|$ is positive, then

A. $abc > 1$

B. $abc > -8$

C. $abc > -8$

D. $abc > -2$

Answer: B



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13. if A_1, B_1, C_1, \dots are respectively the cofactors of the elements a_1, b_1, c_1, \dots of the determinant

$$\Delta = \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}, \Delta \neq 0 \text{ then the value of } \begin{vmatrix} B_2 & C_2 \\ B_3 & C_3 \end{vmatrix} \text{ is equal to}$$

A. $a_1^2 \Delta$

B. $a_1 \Delta$

C. $a_1 \Delta^2$

D. $a_1^2 \Delta^2$

Answer: B



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14. If $a, b, c, d, e,$ and f are in G.P. then the value of $\left| a^2 d^2 x b^2 e^2 y c^2 f^2 z \right|$ depends on x and y b. x and z c. y and z d. independent of $x, y,$ and z

A. x and y

B. x and z

C. y and z

D. independent of x,y and z

Answer: D

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15. Let $x < 1$, then value of $|x^2 + 22x + 112x + 1x + 21331|$ is a. none-negative b. none-positive c. negative d. positive

A. non-negative

B. non- positive

C. begative

D. positive

Answer: C

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16. The value of $\left| -1213 + 2\sqrt{22} + 2\sqrt{213} - 2\sqrt{22} - 2\sqrt{21} \right|$ is equal to a. zero

b. $-16\sqrt{2}$ c. $-8\sqrt{2}$ d. none of these

A. 0

B. $-16\sqrt{2}$

C. $-8\sqrt{2}$

D. none of these

Answer: B



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17. Let $\{D_1, D_2, D_3, D_n\}$ be the set of third order determinant that can be made with the distinct non-zero real numbers a_1, a_2, a_q . Then

$\sum_{i=1}^n D_i = 1$ b. $\sum_{i=1}^n D_i = 0$ c. $D_i - D_j, \forall i, j$ d. none of these

A. $\sum_{i=1}^n D_i = 1$

$$B. \sum_{i=1}^n D_i = 0$$

$$C. D_i D_j, \forall i, j$$

D. None of these

Answer: B

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18. if w is a complex cube root to unity then value of

$$\Delta = \begin{vmatrix} a_1 + b_1 w & a_1 w^2 + b_1 & c_1 + b_1 \bar{w} \\ a_2 + b_2 w & a_2 w^2 + b_2 & c_2 + b_2 \bar{w} \\ a_3 + b_3 w & a_3 w^2 + b_3 & c_3 + b_3 \bar{w} \end{vmatrix} \text{ is}$$

A. 0

B. -1

C. 2

D. none of these

Answer: A



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19. If $a + b + c = 0$, one root of $|a - x \quad c \quad b \quad c \quad b - x \quad a \quad b \quad a \quad c - x| = 0$ is $x = 1$ b. $x = 2$ c.

$x = a^2 + b^2 + c^2$ d. $x = 0$

A. $x = 1$

B. $x = 2$

C. $x = a^2 + b^2 + c^2$

D. $x = 0$

Answer: D



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20. If x, y, z are in A.P. , then the value of the determinant are in A.P. , then

the value of the determinant

$|a + 2a + 3a + 2xa + 3a + 4a + 2ya + 4a + 5a + 2z|$ is a. 1 b. 0 c. $2a$ d. a

A. 1

B. 0

C. $2a$

D. a

Answer: B



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21. If $a_1, a_2, a_3, \dots, a_n, \dots$ are in G.P., then the determinant $\Delta =$

$$\begin{vmatrix} \log a_n & \log a_{n+1} & \log a_{n+2} \\ \log a_{n+3} & \log a_{n+4} & \log a_{n+5} \\ \log a_{n+6} & \log a_{n+7} & \log a_{n+8} \end{vmatrix} \text{ is equal to}$$

A. 1

B. 0

C. $2a$

D. a

Answer: B



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22. Value of $|x + yzzxy + zxyyz + x|$, where x, y, z are nonzero real number, is equal to xyz b. $2xyz$ c. $3xyz$ d. $4xyz$

A. xyz

B. $2xyz$

C. $3xyz$

D. $4xyz$

Answer: D



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23. Which of the following is not the root of the equation

$$|x - 6 - 12 - 3 \times -3 - 32 \times + 2| = 0? \quad \text{a. } 2 \quad \text{b. } 0 \quad \text{c. } 1 \quad \text{d. } -3$$

A. 2

B. 0

C. 1

D. -3

Answer: B



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24. The value of the determinant $\begin{vmatrix} kak^2 + a^2 & 1kbk^2 + b^2 & 1kck^2 + c^2 \\ 1 & 1 & 1 \end{vmatrix}$ is

$$k(a+b)(b+c)(c+a)$$

$$kabc(a^2 + b^2 + c^2)$$

$$k(a-b)(b-c)(c-a)$$

$$k(a+b-c)(b+c-a)(c+a-b)$$

A. $k(a+b)(b+c)(c+a)$

B. $kabc(a^2 + b^2 + c^2)$

$$C. k(a - b)(b - c)(c - a)$$

$$D. k(a + b - c)(b + c - a)(c + a - b)$$

Answer: C



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$$25. \text{ If } \begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^3 & b^3 & c^3 \end{vmatrix} = (a - b)(b - c)(c - a)(a + b + c)$$

where a, b, c are all different, then the determinant

$$\begin{vmatrix} 1 & 1 & 1 \\ (x - a)^2 & (x - b)^2 & (x - c)^2 \\ (x - b)(x - c) & (x - c)(x - a) & (x - a)(x - b) \end{vmatrix} \text{ vanishes when}$$

A. $a + b + c = 0$

B. $x = \frac{1}{3}(a + b + c)$

C. $x = \frac{1}{2}(a + b + c)$

D. $x = a + b + c$

Answer: B



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26. If $f'(x) = |mx + p|$, then $y = f(x)$ represents a straight line parallel to x-axis a straight line

parallel to y-axis parabola a straight line with negative slope

- A. a straight line parallel to x-axis
- B. a straight line parallel to y-axis
- C. parabola
- D. a straight line with negative slope

Answer: B



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27. If $|x^3 6^3 6x^3| = |2x^7 7^2 7^2 x| = |45x^5 4x^4 45| = 0$, then x is equal to 0 b. -9

c. 3 d. none of these

A. 0

B. -9

C. 3

D. none of these

Answer: B



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28. If
$$\begin{vmatrix} x^n & x^{n+2} & x^{2n} \\ 1 & x^a & a \\ x^{n+5} & x^{a+6} & x^{2n+5} \end{vmatrix} = 0, \forall x \in R, \text{ where } n \in N, \text{ then value of } a \text{ is}$$

(a) n

(b) $n - 1$

(c) $n + 1$

(d) none of these

A. n

B. $n-1$

C. $n+1$

D. none of these

Answer: C



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29. for the equation
$$\begin{vmatrix} 1 & x & x^2 \\ x^2 & 1 & x \\ x & x^2 & 6 \end{vmatrix} = 0$$

A. There are exactly two distinct roots

B. there is one pair of equation real roots

C. There are three pairs of equal roots

D. Modulus of each root is 2

Answer: C

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30. If $a^2 + b^2 + c^2 = -2$ and $f(x) = |a + a^2x(1 + b^2)x(1 + c^2)x(1 + a^2)x1 + b^2x(1 + c^2)x(1 + a^2)x(1 + b^2)x1 + c^2x$, then $f(x)$ is a polynomial of degree 0 b. 1 c. 2 d. 3

A. 0

B. 1

C. 2

D. 3

Answer: C

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31. The value of the determinant $\begin{vmatrix} 1 & 1 & 1 \\ \cdot^m C_1 & \cdot^{m+1} C_1 & \cdot^{m+2} C_1 \\ \cdot^m C_2 & \cdot^{m+1} C_2 & \cdot^{m+2} C_2 \end{vmatrix}$ is equal to

- A. 1
- B. -1
- C. 0
- D. none of these

Answer: A



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32. The value of determinant

$$\begin{vmatrix} n C_{r-1} & C_r & (r+1)^{n+2} C_{r+1} & C_r^n & C_{r+1}^n & (r+2)^{n+2} C_{r+2} & C_{r+1}^n & C_{r+2}^n & (r+3)^{n+2} C_{r+3} \end{vmatrix}$$

is $n^2 + n - 2$ b. 0 c. $n + 3 C_{r+3}$ d. $n C_{r-1} + n C_r + n C_{r+1}$

A. $n^2 + n - 1$

B. 0

C. ${}^{n+3}C_{r+3}$

D. ${}^nC_{r-1} + {}^nC_r + {}^nC_{r+1}$

Answer: B

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33. if $f(x) = \begin{vmatrix} x & a & a \\ a & x & a \\ a & a & x \end{vmatrix} = 0$ then

A. $f(x) = 0$ and $f(x) = 0$ has one common root

B. $f(x) = 0$ and $f(x) = 0$ has one common root

C. sum of roots of $f(x) = 0$ is $-3a$

D. none of these

Answer: B

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34. If $x \neq y \neq z$ and $\begin{vmatrix} x & x^2 & 1+x^3 \\ y & y^2 & 1+y^3 \\ z & z^2 & 1+z^3 \end{vmatrix} = 0$, then $xyz =$

A. 1

B. 2

C. -1

D. -2

Answer: C

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35. if $x \neq 0, y \neq 0, z \neq 0$ and $\begin{vmatrix} 1+x & 1 & 1 \\ 1+y & 1+2y & 1 \\ 1+z & 1+z & 1+3z \end{vmatrix} = 0$ then

$x^{-1} + y^{-1} + z^{-1}$ is equal to

A. -1

B. -2

C. -3

D. none of these

Answer: C



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36. if $a_1b_1c_1$, $a_2b_2c_2$ and $a_3b_3c_3$ are three-digit even natural numbers and

$$\Delta = \begin{vmatrix} c_1 & a_1 & b_1 \\ c_2 & a_2 & b_2 \\ c_3 & a_3 & b_3 \end{vmatrix} \text{ then } \Delta \text{ is}$$

A. divisible by 2 but not necessarily by 4

B. divisible by 4 but not necessarily by 8

C. divisible by 8

D. none of these

Answer: A



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37. if $\begin{vmatrix} b+c & c+a & a+b \\ a+b & b+c & c+a \\ c+a & a+b & b+c \end{vmatrix} = k \begin{vmatrix} a & b & c \\ c & a & b \\ b & c & a \end{vmatrix}$ then the value of k is

A. 1

B. 2

C. 3

D. 4

Answer: B



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38.

suppose

$$D = \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}$$

and

$$D' = \begin{vmatrix} a_1 + pb_1 & b_1 + qc_1 & c_1 + ra_1 \\ a_2 + pb_2 & b_2 + qc_2 & c_2 + ra_2 \\ a_3 + pb_3 & b_3 + qc_3 & c_3 + ra_3 \end{vmatrix}. \text{ Then}$$

A. $D' = D$

B. $D' = D(1 - pqr)$

C. $D = D(1 + p + q + r)$

D. $D' = D(1 + pqr)$

Answer: D



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39. The value of the determinant

$$\begin{vmatrix} \log_a\left(\frac{x}{y}\right) & \log_a\left(\frac{y}{z}\right) & \log_a\left(\frac{z}{x}\right) \\ \log_b\left(\frac{y}{z}\right) & \log_b\left(\frac{z}{x}\right) & \log_b\left(\frac{x}{y}\right) \\ \log_c\left(\frac{z}{x}\right) & \log_c\left(\frac{x}{y}\right) & \log_c\left(\frac{y}{z}\right) \end{vmatrix}$$

A. 1

B. -1

C. 0

D. $\frac{1}{6} \log_a xyz$

Answer: C



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40. If $a > 0, b > 0, c > 0$ are respectively the p th, q th, r th terms of a G.P., then the value of the determinant

$$\begin{vmatrix} \log a & p & 1 \\ \log b & q & 1 \\ \log c & r & 1 \end{vmatrix}, \text{ is}$$

- A. 0
- B. $\log(abc)$
- C. $-(p + q + r)$
- D. none of these

Answer: A



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41. If $a > 0$ and discriminant of $ax^2 + 2bx + c$ is negative, then

$= abax + cbx + cax + x + c0$ is +ve b. $(ac - b)^2(ax^2 + 2bx + c)$ c. -ve d. 0

A. +ve

B. $(ac - b)^2(ax^2 + 2bx + c)$

C. -ve

D. 0

Answer: C



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42. The number of distinct real roots of $\begin{vmatrix} \sin x & \cos x & \cos x \\ \cos x & \sin x & \cos x \\ \cos x & \cos x & \sin x \end{vmatrix} = 0$ in the interval $-\frac{\pi}{4} \leq x \leq \frac{\pi}{4}$ is

A. 0

B. 2

C. 1

D. 3

Answer: C



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43. if $D_k = \begin{vmatrix} 1 & n & n \\ 2k & n^2 + n + 1 & n^2 + n \\ 2k - 1 & n^2 & n^2 + n + 1 \end{vmatrix}$ and $\sum_{k=1}^n D_k = 56$ then n

equals

A. 4

B. 6

C. 8

D. 7

Answer: D

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44. the value of $\sum_{r=2}^n (-2)^r \begin{vmatrix} {}^{n-2}C_{r-2} & {}^{n-2}C_{r-1} & {}^{n-2}C_r \\ -3 & 1 & 1 \\ 2 & -1 & 0 \end{vmatrix} (n > 2)$

A. $2n - 1 + (-1)^n$

B. $2n + 1 + (-1)^{n-1}$

C. $2n - 3 + (-1)^n$

D. none of these

Answer: A



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45. if $\Delta = \begin{vmatrix} 3 & 4 & 5 & x \\ 4 & 5 & 6 & y \\ 5 & 6 & 7 & z \\ x & y & z & 0 \end{vmatrix} = 0$ then

A. x, y, z are in A.P.

B. x, y, z are in G.P

C. x, y, z are in H.P

D. none of these

Answer: A



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46. Roots of the equations $\begin{vmatrix} x & m & n & 1 \\ a & x & n & 1 \\ a & b & x & 1 \\ a & b & c & 1 \end{vmatrix} = 0$ are

- A. independent of m and n
- B. independent of a,b and c
- C. depend on m,n and a,b,c
- D. independent of m,n and a,b,c

Answer: A



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47. If x, y, z are different from zero and $\Delta = ab - yc - za - xbc - za - xb - yc = 0$, then the value of the expression $\frac{a}{x} + \frac{b}{y} + \frac{c}{z}$ is 0 b. -1 c. 1 d. 2

A. 0

B. -1

C. 1

D. 2

Answer: D



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48. about to only mathematics

A. 0

B. 3

C. 6

D. 12

Answer: B



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49. In triangle ABC, if

$$\left| \begin{array}{ccc} 1 & 1 & 1 \\ \cot\left(\frac{A}{2}\right) & \cot\left(\frac{B}{2}\right) & \cot\left(\frac{C}{2}\right) \\ \tan\left(\frac{B}{2}\right) + \tan\left(\frac{C}{2}\right) & \tan\left(\frac{C}{2}\right) + \tan\left(\frac{A}{2}\right) & \tan\left(\frac{A}{2}\right) + \tan\left(\frac{B}{2}\right) \end{array} \right| \text{ then the}$$

triangle must be (A) Equilateral (B) Isosceles (C) Right Angle (D) none of these

- A. equilateral
- B. isosceles
- C. obtuse angled
- D. none of these

Answer: B



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50. If $\begin{vmatrix} a & b-c & b+c \\ a+c & b & c-a \\ a-b & a+b & c \end{vmatrix} = 0$ then the line $ax + by + c = 0$ passes

through the fixed point which is

A. (1, 2)

B. (1, 1)

C. (-2, 1)

D. (1, 0)

Answer: B



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51. The determinant $\begin{vmatrix} y^2 & -xy & x^2 \\ a & b & c \\ a' & b' & c' \end{vmatrix}$ is equal to

A. $\begin{vmatrix} bx + ay & cx + by \\ b'x + a'y & c'x + b'y \end{vmatrix}$

$$B. \begin{vmatrix} ax + by & bx + cy \\ a'x + b'y & b'x + c'y \end{vmatrix}$$

$$C. \begin{vmatrix} bx + cy & ax + by \\ b'x + c'y & a'x + b'y \end{vmatrix}$$

$$D. \begin{vmatrix} ax + by & bc + cy \\ a'x + b'y & b'x + c'y \end{vmatrix}$$

Answer: D



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52. Let $\vec{a}_r = x_r \hat{i} + y_r \hat{j} + z_r \hat{k}$, $r = 1, 2, 3$ three mutually perpendicular unit

vectors then the value of $\begin{vmatrix} x_1 & -x_2 & x_3 \\ y_1 & y_2 & y_3 \\ z_1 & z_2 & z_3 \end{vmatrix}$ is equal to

A. zero

B. ± 1

C. ± 2

D. none of these

Answer: B



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53. Let

$$\begin{vmatrix} y^5 z^6 (z^3 - y^3) & x^4 z^6 (x^3 - z^3) & x^4 y^5 (y^3 - x^3) \\ y^2 z^3 (y^6 - z^6) & xz^3 (z^6 - x^6) & xy^2 (x^6 - y^6) \\ y^2 \wedge (3) (z^3 - y^3) & xz^3 (x^3 - z^3) & xy^2 (y^3 - x^3) \end{vmatrix} \text{ and } \Delta_2 = \begin{vmatrix} x & y^2 & z^3 \\ x^4 & y^5 & z^6 \\ x^7 & y^8 & z^9 \end{vmatrix}$$

.Then $\Delta_1 \Delta_2$ is equal to

A. Δ_2^6

B. Δ_2^4

C. Δ_2^3

D. Δ_2^2

Answer: C



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54. the value of the determinant

$$\begin{vmatrix} (a_1 - b_1)^2 & (a_1 - b_2)^2 & (a_1 - b_3)^2 & (a_1 - b_4)^2 \\ (a_2 - b_1)^2 & (a_2 - b_2)^2 & (a_2 - b_3)^2 & (a_3 - b_4)^2 \\ (a_3 - b_1)^2 & (a_3 - b_2)^2 & (a_3 - b_3)^2 & (a_3 - b_4)^2 \\ (a_4 - b_1)^2 & (a_4 - b_2)^2 & (a_4 - b_3)^2 & (a_4 - b_4)^2 \end{vmatrix} \text{ is}$$

- A. dependant on $a_i, i = 1, 2, 3, 4$
- B. dependant on $b_i, i = 1, 2, 3, 4$
- C. dependant on $a_{ij}, b_i, i = 1, 2, 3, 4$
- D. 0

Answer: D



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55. if $\Delta(x) = \begin{vmatrix} \tan x & \tan(x+h) & \tan(x+2h) \\ \tan(x+2h) & \tan x & \tan(x+h) \\ \tan(x+h) & \tan(x+2h) & \tan x \end{vmatrix}$, then

The value of $\lim_{h \rightarrow 0} \frac{\Delta(\pi/3)}{\sqrt{3}h^2}$ is

A. 144

B. 81

C. 64

D. 36

Answer: A

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56. Value of $\begin{vmatrix} 1+x_1 & 1+x_1x & 1+x_1x^2 \\ 1+x_2 & 1+x_2x & 1+x_2x^2 \\ 1+x_3 & 1+x_3x & 1+x_3x^2 \end{vmatrix}$ depends upon

A. x only

B. x_1 only

C. x_2 only

D. none of these

Answer: D

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57. If
$$\begin{vmatrix} a^2 + \lambda^2 & ab + c\lambda & ca - b\lambda \\ ab - c\lambda & b^2 + \lambda^2 & bc + a \\ ca + b\lambda & bc - a\lambda & c^2 + \lambda^2 \end{vmatrix} \begin{vmatrix} \lambda & c & -b \\ -c & \lambda & a \\ b & -a & \lambda \end{vmatrix} = (1 + a^2 + b^2 + c^2)^3,$$
 then

the value of λ is

a. 8

b. 27

c. 1

d. -1

A. 8

B. 27

C. 1

D. -1

Answer: C



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58. Let $\begin{vmatrix} x & 2 & x \\ x^2 & x & 6 \\ x & x & 6 \end{vmatrix} = ax^4 + bx^3 + cx^2 + dx + e$ Then, the value of

$5a + 4b + 3c + 2d + e$ is equal to

A. zero

B. -16

C. 16

D. -11

Answer: D



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59. $\Delta_1 = \begin{vmatrix} x & b & b \\ a & x & b \\ a & a & x \end{vmatrix}$ and $\Delta_2 = \begin{vmatrix} x & b \\ a & x \end{vmatrix}$ are the given determinations then

A. $\Delta_1 = 3(\Delta_2)^2$

B. $\frac{d}{dx}(\Delta_1) = 3\Delta_2$

C. $\frac{d}{dx}(\Delta_1) = 3(\Delta_2)^2$

D. $\Delta_1 = 3\Delta_2^{3/2}$

Answer: B



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60. if $y = \sin mx$, then the value of the determinant

$$\begin{vmatrix} y & y_1 & y_2 \\ y_3 & y_4 & y_5 \\ y_6 & y_7 & y_8 \end{vmatrix} \quad \text{Where } y_n = \frac{d^n y}{dx^n} \text{ is}$$

A. m^9

B. m^2

C. m^3

D. 0

Answer: D



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61. Let $f(x) = \begin{vmatrix} 2\cos^2 x & \sin 2x & -\sin x \\ \sin 2x & 2\sin^2 x & \cos x \\ \sin x & -\cos x & 0 \end{vmatrix}$, then the value of $\int_0^{\pi/2} \{f(x) + f'(x)\} dx$

is

A. π

B. $\pi/2$

C. 2π

D. $3\pi/2$

Answer: A



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62. a, b, c are distinct real numbers not equal to one. If $ax + y + z = 0$, $x + by + z = 0$, and $x + y + cz = 0$ have nontrivial solution, then the value of $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c}$ is equal to a.1 b. -1 c.zero d. none of these

A. -1

B. 1

C. zero

D. none of these

Answer: B



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63. If the system of linear equation $x + y + z = 6$, $x + 2y + 3z = 14$, and $2x + 5y + \lambda z = \mu$ ($\lambda, \mu \in R$) has a unique solution, then $\lambda = 8$ b. $\lambda = 8, \mu = 36$ c. $\lambda = 8, \mu \neq 36$ d. none of these

A. $\lambda \neq 8$

B. $\lambda = 8, \mu \neq 36$

C. $\lambda = 8, \mu = 36$

D. none of these

Answer: A



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64. If α, β, γ are the angles of a triangle and system of equations

$$\cos(\alpha - \beta)x + \cos(\beta - \gamma)y + \cos(\gamma - \alpha)z = 0$$

$$\cos(\alpha + \beta)x + \cos(\beta + \gamma)y + \cos(\gamma + \alpha)z = 0$$

$\sin(\alpha + \beta)x + \sin(\beta + \gamma)y + \sin(\gamma + \alpha)z = 0$ has non-trivial solutions, then triangle is necessarily a. equilateral b. isosceles c. right angled d. acute angled

A. equilateral

B. isosceles

C. right angled

D. acute angled

Answer: B



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65. Given $a = x/(y - z)$, $b = y/(z - x)$, and $c = z/(x - y)$, where x, y, z are not all zero, then the value of $ab + bc + ca$ is 0 b. 1 c. -1 d. none of these

A. 0

B. 1

C. -1

D. none of these

Answer: C



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66. If $pqr \neq 0$ and the system of equation $(p + a)x + by - cz = 0$

$ax + (q + b)y + cz = 0$ $ac + by + (r + c)z = 0$ has nontrivial solution, then

value of $\frac{1}{p} + \frac{b}{q} + \frac{c}{r}$ is -1 b. 0 c.0 d. $\neg - 2$

A. -1

B. 0

C. 1

D. 2

Answer: A



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67. The value of $|\alpha|$ for which the system of equation

$$\alpha x + y + z = \alpha - 1$$

$$x + \alpha y + z = \alpha - 1$$

$$x + y + \alpha z = \alpha - 1$$

has no solution , is _____

A. either -2 or 1

B. -2

C. 1

D. not-2

Answer: B



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68. the set of equations $\lambda x - y + (\cos\theta)z = 0, 3x + y + 2z = 0, (\cos\theta)x + y + 2z = 0, \theta \leq 0 < 2\pi$ has non-trivial solution (s)

- A. for no value of λ and 0
- B. for all values of λ and 0
- C. for all values of λ and only two values of 0
- D. for only one value of λ and all values of 0

Answer: A

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69. If $c < 1$ and the system of equations $x + y - 1 = 0, 2x - y - c = 0, \text{ and } bx + 3by - c = 0$ is consistent, then the possible real values of b are $b\left(-3\frac{3}{4}\right)$ b. $b\left(-\frac{3}{2}, 4\right)$ c. $b\left(-\frac{3}{4}, 3\right)$ d. none of these

A. $b \in \left(-3\frac{3}{4}\right)$

B. $b \in \left(-\frac{3}{2}, 4\right)$

C. $b \in \left(-\frac{3}{4}, 3\right)$

D. none of these

Answer: C



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70. If a, b, c are in G.P. with common ratio r_1 and α, β, γ are in G.P. with common ratio r_2 and equations $ax + \alpha y + z = 0, bx + \beta y + z = 0, cx + \gamma y + z = 0$ have only zero solution, then which of the following is not true? a. $a + b + c = 1$ b. $abc = 1$ c. $r_1 = r_2$ d. none of these

A. $r_1 \neq 1$

B. $r_2 \neq 1$

C. $r_1 \neq r_2$

D. none of these

Answer: D



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71. The product of all values of t , for which the system of equations $(a - t)x + by + cz = 0$, $bx + (c - t)y + az = 0$, $cx + ay + (b - t)z = 0$ has non-trivial solution, is $|a - c - b - cb - a - b - ac|$ (b) $|abc bcacab|$ $|acaba|$ (d) $|aa + + c + + a + aa + b|$

A.
$$\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$$

B. $a + b + c$

C. $a^2 + b^2 + c^2$

D. 1

Answer: A



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72. Let λ and α be real. Then the numbers of integral values λ for which the system of linear equations

$$\lambda x + (\sin\alpha)y + (\cos\alpha)z = 0$$

$$x + (\cos\alpha)y + (\sin\alpha)z = 0$$

$-x + (\sin\alpha)y - (\cos\alpha)z = 0$ has non-trivial solutions is

A. 0

B. 1

C. 2

D. 3

Answer: D



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Exercise (Multiple)

1. Which of the following has/have value equal to zero ?

$$A. \begin{vmatrix} 8 & 2 & 7 \\ 12 & 3 & 5 \\ 16 & 4 & 3 \end{vmatrix}$$

$$B. \begin{vmatrix} 1/a & a^2 & bc \\ 1/b & b^2 & ac \\ 1/c & c^2 & ab \end{vmatrix}$$

$$C. \begin{vmatrix} a+b & 2a+b & 3a+b \\ 2a+b & 3a+b & 4a+b \\ 4a+b & 5a+b & 6a+b \end{vmatrix}$$

$$D. \begin{vmatrix} 2 & 43 & 6 \\ 7 & 35 & 4 \\ 3 & 17 & 2 \end{vmatrix}$$

Answer: A::B::C



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$$2. \text{ If } f(\alpha, \beta) = \begin{vmatrix} \cos\alpha & -\sin\alpha & 1 \\ \sin\alpha & \cos\alpha & 1 \\ \cos(\alpha + \beta) & -\sin(\alpha + \beta) & 1 \end{vmatrix}, \text{ then}$$

A. $f(300,200)=f(400,200)$

B. $f(200,400)=f(200,600)$

C. $f(100,200)=f(200,200)$

D. none of these

Answer: A::C



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3. if $f(\theta) = \begin{vmatrix} \sin\theta & \cos\theta & \sin\theta \\ \cos\theta & \sin\theta & \cos\theta \\ \cos\theta & \sin\theta & \sin\theta \end{vmatrix}$ then

A. $f(\theta) = 0$ has exactly 2 real solutions in $[0, \pi]$

B. $f(\theta) = 0$ has exactly 3 real solutions in $[0, \pi]$

C. range of function $\frac{f(\theta)}{1 - \sin 2\theta}$ is $[-\sqrt{2}, \sqrt{2}]$

D. range of function $\frac{f(\theta)}{\sin 2\theta - 1}$ is $[-3, 3]$ is $[-3, 3]$

Answer: A::C



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4. If $f(x) = \left| a - 10axa - 1ax^2axa \right|$, then $f(2x) - f(x)$ is divisible by a b c d e

d. none of these

A. x

B. a

C. $2a + 3x$

D. x^2

Answer: A::B::C

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5. $\Delta = \begin{vmatrix} 1 & 1+ac & 1+bc \\ 1 & 1+ad & 1+bd \\ 1 & 1+ae & 1+be \end{vmatrix}$ is independent of

A. a

B. b

C. c,d,e

D. none of these

Answer: A::B::C



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6. if $\Delta = \begin{vmatrix} -x & a & b \\ b & -x & a \\ a & b & -x \end{vmatrix}$ then a factor of Δ is

A. $a + b + x$

B. $x^2 - (a - b)x + a^2 + b^2 + ab$

C. $x^2 + (a + b)x + a^2 + b^2 - ab$

D. $a + b - x$

Answer: C::D



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7. the determinant $\Delta = \begin{vmatrix} a^2 + x & ab & ac \\ ab & b^2 + x & bc \\ ac & bc & c^2 + x \end{vmatrix}$ is divisible by

A. x

B. x^2

C. x^3

D. none of these

Answer: A::B



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8. $\begin{vmatrix} a^2 & 0 & 12a + b(a + b) \\ 0 & 12a + 3b & \\ \end{vmatrix}$ is divisible by $a + b$ b. $a + 2b$ c. $2a + 3b$

d. a^2

A. $a + b$

B. $a + 2b$

C. $2a + 3b$

D. a^2

Answer: A::B



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9. the roots of the equations
$$\begin{vmatrix} {}^x C_r & {}^{n-1} C_r & {}^{n-1} C_{r-1} \\ {}^{x+1} C_r & {}^n C_r & {}^n C_{r-1} \\ {}^{x+2} C_r & {}^{n+1} C_r & {}^{n+1} C_{r-1} \end{vmatrix} = 0$$

A. $x = n$

B. $x = n + 1$

C. $x = n - 1$

D. $x = n - 2$

Answer: A::C



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10. If $f(x) = \begin{vmatrix} 3 & 3x & 3x^2 + 2a^2 \\ 3x & 3x^2 + 2a^2 & 3x^3 + 6a^2x \\ 3x^2 + 2a^2 & 3x^3 + 6a^2x & 3x^4 + 12a^2x^2 + 2a^4 \end{vmatrix}$ then

A. $f'(x)=0$

B. $y=f(x)$ is a straight line parallel to x-axis

C. $\int_0^2 f(x)dx = 32a^4$

D. none of these

Answer: A::B



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11. Let $f(n) = \begin{vmatrix} n & n+1 & n+1 \\ \cdot^n P_n & \cdot^{n+1} P_{n+1} & \cdot^{n+2} P_{n+2} \\ \cdot^n C_n & \cdot^{n+1} C_{n+1} & \cdot^{n+2} C_{n+2} \end{vmatrix}$ where the symbols have

their usual meanings. then $f(n)$ is divisible by

A. $n^2 + n + 1$

B. $(n + 1)!$

C. $n!$

D. none of these

Answer: A:C

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12. If $\begin{vmatrix} a & b & a\alpha + b \\ b & c & b\alpha + c \\ a\alpha + b & b\alpha + c & 0 \end{vmatrix} = 0$, prove that a, b, c , are in G.P. or α is a

root of $ax^2 + 2bx+c=0$

A. a, b, c are in A.P

B. a, b, c are in G.P.

C. α is a root of the equation $ax^2 + bx + c = 0$

D. $(x - \alpha)$ is a factor fo $ax^2 + 2bx + c$

Answer: B::D

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13. if
$$\begin{vmatrix} \sin x & \sin y & \sin z \\ \cos x & \cos y & \cos z \\ \cos^3 x & \cos^3 y & \cos^3 z \end{vmatrix} = 0$$
 then which of the following is/are

possible ?

A. $x = y$

B. $y = z$

C. $x = z$

D. $x + y + z = \pi/2$

Answer: A::B::C::D



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14. If
$$\begin{vmatrix} x^2 + x & x + 1 & x - 2 \\ 2x^2 + 3x - 1 & 3x & 3x - 3 \\ x^2 + 2x + 3 & 2x - 1 & 2x - 1 \end{vmatrix} = xA + B$$
 then

A.
$$\begin{vmatrix} 1 & 1 & 1 \\ -1 & -3 & 3 \\ 4 & 0 & 0 \end{vmatrix}$$

B.
$$\begin{vmatrix} 0 & 1 & 2 \\ 1 & -2 & 3 \\ -4 & 0 & 0 \end{vmatrix}$$

C.
$$\begin{vmatrix} 1 & 1 & -2 \\ -3 & -2 & 3 \\ 4 & 0 & 1 \end{vmatrix}$$

D.
$$\begin{vmatrix} 0 & 1 & -2 \\ -1 & -3 & 3 \\ 4 & 0 & 0 \end{vmatrix}$$

Answer: A::D



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15. if $\begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ bc & ca & ab \end{vmatrix} = \begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^3 & b^3 & c^3 \end{vmatrix}$ where a, b, c are distinct

positive reals then the possible values of abc is/are

A. $\frac{1}{18}$

B. $\frac{1}{63}$

C. $\frac{1}{27}$

D. $\frac{1}{9}$

Answer: A::B



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16.
$$\begin{vmatrix} \cdot^x C_r & \cdot^x C_{r+1} & \cdot^x C_{r+2} \\ \cdot^y C_r & \cdot^y C_{r+1} & \cdot^y C_{r+2} \\ \cdot^z C_r & \cdot^z C_{r+1} & \cdot^z C_{r+2} \end{vmatrix}$$
 is equal to

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17. If
$$\begin{vmatrix} \sin\theta\cos\phi & \sin\theta\sin\phi & \cos\theta \\ \cos\theta\cos\phi & \cos\theta\sin\phi & -\sin\theta \\ -\sin\theta\sin\phi & \sin\theta\cos\phi & \theta \end{vmatrix}$$
 then

A. Δ is independent of theta

B. Δ is independent of ϕ

C. Δ is a constant

D.
$$\left[\frac{d\Delta}{d}(\theta) \right]_{\theta=\pi/2} = 0$$

Answer: B::D

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18. If $f(\theta) = \left| \sin^2 A \cot A \sin^2 B \cos B \sin^2 C \cos C \right|$, then $\tan A + \tan B + \tan C + \cot A \cot B \cot C \sin^2 A + \sin^2 B + \sin^2 C$ is

A. $\tan A + \tan B + \tan C$

B. $\cot A \cot B \cot C$

C. $\sin^2 A + \sin^2 B + \sin^2 C$

D. 0

Answer: D



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19. if determinant $\begin{vmatrix} \cos(\theta + \phi) & -\sin(\theta + \phi) & \cos 2\phi \\ \sin\theta & \cos\theta & \sin\phi \\ -\cos\theta & \sin\theta & \cos\phi \end{vmatrix}$ is

A. non-negative

B. independent of theta

C. independent of ϕ

D. none of these

Answer: A::B



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20. If $g(x) = \begin{vmatrix} a^{-x} & e^{x \log_e a} & x^2 \\ a^{-3x} & e^{3x \log_e a} & x^4 \\ a^{-5x} & e^{5x \log_e a} & 1 \end{vmatrix}$ then

A. graphs of $g(x)$ is symmetrical about the origin

B. graphs of $g(x)$ is symmetrical about the y-axis

C. $\frac{d^4 g(x)}{dx^4} \Big|_{x=0} = 0$

D. $f(x) = g(x) \times \log. \left(\frac{a-x}{a+x} \right)$ is an odd function

Answer: A::C



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21. If $\Delta(x) = \begin{vmatrix} x^2 + 4x - 3 & 2x + 4 & 13 \\ 2x^2 + 5x - 9 & 4x + 5 & 26 \\ 8x^2 - 6x + 1 & 16x - 6 & 104 \end{vmatrix} = ax^3 + bx^2 + cx + d$, then

A. $a = 3$

B. $b = 0$

C. $c = 0$

D. None of these

Answer: B::C

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22. if $\begin{vmatrix} yz - x^2 & zx - y^2 & xy - z^2 \\ xz - y^2 & xy - z^2 & yz - x^2 \\ xy - z^2 & yz - x^2 & zx - y^2 \end{vmatrix} = \begin{vmatrix} r^2 & u^2 & u^2 \\ u^2 & r^2 & u^2 \\ u^2 & u^2 & r^2 \end{vmatrix}$ then

A. $r^2 = x + y + z$

$$B. r^2 = x^2 = y^2 + z^2$$

$$C. u^2 = yz + zx + xy$$

$$D. u^2 = xyz$$

Answer: B::C



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23. which of the following is/are true for

$$\Delta = \begin{vmatrix} a^2 & 1 & a + c \\ 0 & b^2 + 1 & b + c \\ 0 & b + c & c^2 + 1 \end{vmatrix} ?$$

A. $\Delta \geq 0$ for real values of a,b,c

B. $\Delta \leq 0$ for real values of a,b,c

$$C. \Delta = \begin{vmatrix} bc - 1 & 0 & 0 \\ 1 & ac & -a \\ -b & -a & ab \end{vmatrix}$$

D. $\Delta = 0$ if $bc = 1$ where a,b,c are non-zero

Answer: A::C::D



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24. The values of $k \in R$ for which the system of equations $x + ky + 3z = 0$, $kx + 2y + 2z = 0$, $2x + 3y + 4z = 0$ admits of nontrivial solution is 2 b. $5/2$ c. 3 d. $5/4$

A. 2

B. $5/2$

C. 3

D. $5/4$

Answer: A::B



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25. The system of equations $-2x + y + z = a$ $x - 2y + z = b$ $x + y - 2z = c$ has

A. no solution if $a + b + c \neq 0$

B. unique solution if $a + b + c = 0$

C. infinite number of solutions if $a + b + c = 0$

D. None of these

Answer: A:C

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26. Let α, β and γ be the roots of the equations

$x^3 + ax^2 + bx + c = 0, (a \neq 0)$. If the system of equations $\alpha x + \beta y + \gamma z = 0$

$\beta x + \gamma y + \alpha z = 0$ and $\gamma x = \alpha y + \beta z = 0$ has non-trivial solution then

A. $a^2 = 3b$

B. $a^3 = 27c$

C. $b^3 = 27c^2$

D. $\alpha + \beta + \gamma = 0$

Answer: A::B::C



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Exercise (Comprehension)

1. Consider the function $f(x) = \begin{vmatrix} a^2 + x & ab & ac \\ ab & b^2 + x & bc \\ ac & bc & c^2 + x \end{vmatrix}$

Which of the following is true ?

- A. $f(x) = 0$ and $f(x) = 0$ have one positive common root
- B. $f(x) = 0$ and $f(x) = 0$ have one negative common root
- C. $f(x) = 0$ and $f(x) = 0$ have no common root
- D. None of these

Answer: D



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2. Consider the function $f(x) = \begin{vmatrix} a^2 + x & ab & ac \\ ab & b^2 + x & bc \\ ac & bc & c^2 + x \end{vmatrix}$

which of the following is true ?

- A. $f(x)$ has one +ve point of maxima.
- B. $f(x)$ has one -ve point of minima
- C. $f(x)=0$ has three distinct roots
- D. Local minimum value of $f(x)$ is zero

Answer: D



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3. Consider the function $f(x) = \begin{vmatrix} a^2 + x & ab & ac \\ ab & b^2 + x & bc \\ ac & bc & c^2 + x \end{vmatrix}$

In which of the following interval $f(x)$ is strictly increasing

A. $(-\infty, \infty)$

B. $(-\infty, 0)$

C. $(0, \infty)$

D. None of these

Answer: C



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4. Let $\Delta = \begin{vmatrix} -bc & b^2 + bc & c^2 + bc \\ a^2 + ac & -ac & c^2 + ac \\ a^2 + ab & b^2 + ab & -ab \end{vmatrix}$ and the equation

$px^3 + qx^2 + rx + s = 0$ has roots a, b, c where $a, b, c \in \mathbb{R}^+$

the value of Δ is

A. r^2/p^2

B. r^3/p^3

C. $-s/p$

D. none of these

Answer: B



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5. Let $\Delta = \begin{vmatrix} -bc & b^2 + bc & c^2 + bc \\ a^2 + ac & -ac & c^2 + ac \\ a^2 + ab & b^2 + ab & -ab \end{vmatrix}$ and the equation

$px^3 + qx^2 + rx + s = 0$ has roots a, b, c where $a, b, c \in R^+$

The value of Δ is

A. $\leq 9r^2/p^2$

B. $\geq 27s^2/p^2$

C. $\leq 27s^3/p^3$

D. none of these

Answer: B



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6. Let $\Delta = \begin{vmatrix} -bc & b^2 + bc & c^2 + bc \\ a^2 + ac & -ac & c^2 + ac \\ a^2 + ab & b^2 + ab & -ab \end{vmatrix}$ and the equation

$px^3 + qx^2 + rx + s = 0$ has roots a, b, c where $a, b, c \in R^+$

if $\Delta = 27$ and $a^2 + b^2 + c^2 = 3$ then

A. $3p + 2q = 0$

B. $4p + 3q = 0$

C. $3p + q = 0$

D. none of these

Answer: C



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7. if $x > m, y > n, z > r (x, y, z > 0)$ such that $\begin{vmatrix} x & n & r \\ m & y & r \\ m & n & z \end{vmatrix} = 0$

The value of $\frac{x}{x-m} + \frac{y}{y-n} + \frac{z}{z-r}$ is

A. 1

B. -1

C. 2

D. -2

Answer: C



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8. if $x > m, y > n, z > r (x, y, z > 0)$ such that $\begin{vmatrix} x & n & r \\ m & y & r \\ m & n & z \end{vmatrix} = 0$

the value of $\frac{m}{x-m} + \frac{n}{y-n} + \frac{r}{z-r}$ is

A. -2

B. -4

C. 0

D. -1

Answer: D



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9. if $x > m, y > n, z > r (x, y, z > 0)$ such that $\begin{vmatrix} x & n & r \\ m & y & r \\ m & n & z \end{vmatrix} = 0$

the value $\frac{xyz}{(x-m)(y-n)(z-r)}$ is

A. 27

B. $\frac{8}{27}$

C. $\frac{64}{27}$

D. None of these

Answer: B

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$$10. f(x) = \begin{vmatrix} x + c_1 & x + a & x + a \\ x + b & x + c_2 & x + a \\ x + b & x + b & x + c_3 \end{vmatrix} \text{ and } g(x) = (C_1 - x)(c_3 - x)$$

Coefficient of x in $f(x)$ is

A. $\frac{g(a) - f(b)}{b - a}$

B. $\frac{g(-a) - g(-b)}{b - a}$

C. $\frac{g(a) - g(b)}{b - a}$

D. none of these

Answer: C



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$$11. f(x) = \begin{vmatrix} x + c_1 & x + a & x + a \\ x + b & x + c_2 & x + a \\ x + b & x + b & x + c_3 \end{vmatrix} \text{ and } g(x) = (c_1 - x)(c_3 - x)$$

Which of the following is not a constant term in $f(x)$?

A. $\frac{bg(a) - ag(b)}{(b - a)}$

B. $\frac{bf(a) - af(-b)}{(b - a)}$

C. $\frac{bf(-a) - ag(b)}{(b - a)}$

D. none of these

Answer: D



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$$12. f(x) = \begin{vmatrix} x + c_1 & x + a & x + a \\ x + b & x + c_2 & x + a \\ x + b & x + b & x + c_3 \end{vmatrix} \text{ and } g(x) = (C_1 - x)(c_3 - x)$$

Which of the following is not true ?

A. $f(-a) = g(a)$

B. $f(-a) = g(-a)$

C. $f(-b) = g(b)$

D. none of these

Answer: B

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13. Suppose $f(x)$ is a function satisfying the following conditions:

$f(0) = 2, f(1) = 1$ f has a minimum value at $x = \frac{5}{2}$ For all

$x, f'(x) = |2ax^2 - 12ax + b + 1 + 1 - 12(ax + b)2ax + 2b + 12ax + b|$ where

a, b are some constants. Determine the constants a, b , and the function

$f(x)$

A. $1/4$

B. $1/2$

C. -1

D. 3

Answer: B



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14. Suppose $f(x)$ is a function satisfying the following conditions :

(i) $f(0)=2, f(1)=1$

(ii) f has a minimum value at $x = 5/2$

(iii) for all x , $f(x) = \begin{vmatrix} 2ax & 2ax - 1 & 2ax + b + 1 \\ b & b + 1 & -1 \\ 2(ax + b) & 2ax + 2b + 1 & 2ax + b \end{vmatrix}$

$f(x)=0$ has

- A. both roots positive
- B. both roots negative
- C. roots of opposite sign
- D. imaginary roots

Answer: D

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15. Suppose $f(x)$ is a function satisfying the following conditions :

(i) $f(0)=2, f(1)=1$

(ii) f has a minimum value at $x = 5/2$

(iii) for all x , $f(x) = \begin{vmatrix} 2ax & 2ax - 1 & 2ax + b + 1 \\ b & b + 1 & -1 \\ 2(ax + b) & 2ax + 2b + 1 & 2ax + b \end{vmatrix}$

Range of $f(x)$ is

- A. $[7/16, \infty)$
- B. $(-\infty, 15/16]$

C. $[3/4, \infty)$

D. none of these

Answer: A



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16. Consider the polynomial function

$$f(x) = \begin{vmatrix} (1+x)^a & (1+2x)^b & 1 \\ 1 & (1+x)^a & (1+2x)^b \\ (1+2x)^b & 1 & (1+x)^a \end{vmatrix} \quad \left| \begin{array}{l} a, b \text{ being positive integers. The} \\ \text{constant term in } f(x) \text{ is} \end{array} \right.$$

A. 2

B. 1

C. -1

D. 0

Answer: D



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17. Consider the polynomial function

$$f(x) = \begin{vmatrix} (1+x)^2 & (1+2x)^b & 1 \\ 1 & (1+x)^a & (1+2x)^b \\ (1+2x)^b & 1 & (1+x)^a \end{vmatrix}$$

a,b being positive integers.

the coefficient of x in f(x) is

A. 2^a

B. $2^a - 3 \times 2^b + 1$

C. 0

D. none of these

Answer: C



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18. Consider the polynomial function

$$f(x) = \begin{vmatrix} (1+x)^2 & (1+2x)^b & 1 \\ 1 & (1+x)^a & (1+2x)^b \\ (1+2x)^b & 1 & (1+x)^a \end{vmatrix}$$

a,b being positive integers.

Which of the following is true ?

- A. All the roots of the equation $f(x)=0$ are positive
- B. All the roots of the equation $f(x)=0$ are negative
- C. At least one of the equation $f(x)=0$ is repeating one .
- D. None of these

Answer: C



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19. Given that the system of equations $x = cy + bz, y = az + cx, z = bx + ay$ has nonzero solutions and and at least one of the a,b,c is a proper

fraction.

$a^2 + b^2 + c^2$ is

A. > 2

B. > 3

C. < 3

D. < 2

Answer: C



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20. Given that the system of equations $x = cy + bz, y = az + cx, z = bx + ay$ has nonzero solutions and at least one of the a, b, c is a proper fraction.

abc is

A. > -1

B. > 1

C. < 2

D. < 3

Answer: A



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21. Given that the system of equations $x = cy + bz, y = az + cx, z = bx + ay$ has nonzero solutions and at least one of the a, b, c is a proper fraction.

System has solution such that

A. $x, y, z \equiv (1 - 2a^2) : (1 - 2b^2) : (1 - 2c^2)$

B. $x, y, z \equiv \frac{1}{1 - 2a^2} : \frac{1}{1 - 2b^2} : \frac{1}{1 - 2c^2}$

C. $x, y, z \equiv \frac{a}{1 - a^2} : \frac{b}{1 - b^2} : \frac{c}{1 - c^2}$

D. $x, y, z \equiv \sqrt{1 - a^2} : \sqrt{1 - b^2} : \sqrt{1 - c^2}$

Answer: D



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22. Consider the system of equations

$$x + y + z = 6$$

$$x + 2y + 3z = 10$$

$$x + 2y + \lambda z = \mu$$

the system has unique solution if

A. $\lambda \neq 3$

B. $\lambda = 3, \mu = 10$

C. $\lambda = 3, \mu \neq 10$

D. none of these

Answer: A

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23. Consider the system of equations

$$x + y + z = 6$$

$$x + 2y + 3z = 10$$

$$x + 2y + \lambda z = \mu$$

the system has infinite solutions if

A. $\lambda \neq 3$

B. $\lambda = 3, \mu = 10$

C. $\lambda = 3, \mu \neq 10$

D. $\lambda = 3, \mu \neq 10$

Answer: B



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24. Consider the system of equations

$$x + y + z = 6$$

$$x + 2y + 3z = 10$$

$$x + 2y + \lambda z = \mu$$

The system has no solution if

- A. $\lambda \neq 3$
- B. $\lambda = 3, \mu = 10$
- C. $\lambda = 3, \mu \neq 10$
- D. none of these

Answer: C



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Matrix Match Type

1. Match the following lists :



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2. Match the following lists:



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3. If α, β, γ are the roots of $x^3 - 3x^2 + 3x - 1 = 0$ then match the list I with list II

$$\begin{array}{l} \text{List I: } \alpha, \beta, \gamma \\ \text{List II: } 1^2, 2^2, 3^2, 4^2, 5^2 \end{array}$$

then match the list I with list II



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4. consider the system of equations

$$\lambda x + y + z = 1$$

$$x + \lambda y + z = \lambda$$

$$x + y + \lambda z = \lambda^2$$

Now match the following lists:



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5. consider determinant $\Delta = \begin{vmatrix} a_{ij} \end{vmatrix}$ of order 3. If $\Delta = 2$ then match the following lists.



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Exercise (Numerical)

1. If $a_1, a_2, a_3, 54, a_6, a_7, a_8, a_9$ are in H.P., and $D = \begin{vmatrix} a_1 a_2 a_3 54 a_6 a_7 a_8 a_9 \end{vmatrix}$, then the value of $[D]$ is where $[.]$ represents the greatest integer function



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2. the sum of values of p for which the equations $x+y+z=1x+2y+4z=p$ and $x+4y+10z=p^2$ have a solution is _____

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3. The sum of roots of the equations

$$\begin{vmatrix} x+2 & 2x+3 & 3x+4 \\ 2x+3 & 3x+4 & 4x+5 \\ 3x+5 & 5x+8 & 10x+17 \end{vmatrix} = 0 \text{ is } \underline{\hspace{2cm}}$$

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4. Prove that

$$\begin{vmatrix} (\beta + \gamma - \alpha - \delta)^4 & (\beta + \gamma - \alpha - \delta)^2 & 1 \\ (\gamma + \alpha - \beta - \delta)^4 & (\gamma + \alpha - \beta - \delta)^2 & 1 \\ (\alpha + \beta - \gamma - \delta)^4 & (\alpha + \beta - \gamma - \delta)^2 & 1 \end{vmatrix} = -64(\alpha - \beta)(\alpha - \gamma)(\alpha - \delta)(\beta - \delta)(\gamma - \delta)$$

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5. If $f(x) = \begin{vmatrix} 1 & x & x+1 \\ 2x & x(x-1) & (x+1)x \\ 3x(x-1) & x(x-1)(x-2) & (x+1)x(x-1) \end{vmatrix}$ then the value of

$f(500)$ _____



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6.

if

$$|(x, x+y, x+y+z), (2x+3x+2y, 4x+3y+2z), (3x+6x+3y, 10x+6y+3z)| = 6$$

then the real value of x is



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7. Let $D_1 = |aba + bc dc + daba - b|$ and $D_2 = |aca + cbdb + daca + b + c|$ then

the value of $\left| \frac{D_1}{D_2} \right|$, where $b \neq 0$ and $d \neq bc$, is _____.



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8. if $a_1, a_2, a_3, \dots, a_{12}$ are in A.P and

$$\Delta_1 = \begin{vmatrix} a_1 a_5 & a_1 & a_2 \\ a_2 a_6 & a_2 & a_3 \\ a_3 a_7 & a_3 & a_4 \end{vmatrix} \quad \Delta_3 = \begin{vmatrix} a_2 b_{10} & a_2 & a_3 \\ a_3 a_{11} & a_3 & a_4 \\ a_3 a_{12} & a_4 & a_5 \end{vmatrix}$$

then $\Delta_1 : \Delta_2 =$ _____

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9. if $(1 + ax + bx^2)^4 = a_0 + a_1x + a_2x^2 + \dots + a_8x^8$, where $a, b, a_0, a_1, \dots, a_8 \in R$ such that $a_0 + a_1 + a_2 \neq 0$ and

$$\begin{vmatrix} a_0 & a_1 & a_2 \\ a_1 & a_2 & a_0 \\ a_2 & a_0 & a_1 \end{vmatrix} = 0 \text{ then the value of } 5 \cdot \frac{a}{b} \text{ is } \underline{\hspace{2cm}}$$

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10. $\begin{vmatrix} 5\sqrt{\log_e 3} & 5\sqrt{\log_e 3} & 3\sqrt{\log_e 3} \\ 3^{-\log_{1/3} 4} & (0.1)^{\log_{0.01} 4} & 7^{\log_7 3} \\ 7 & 3 & 5 \end{vmatrix}$ is equal to _____



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11. Let $a+b+c = s$ and $\begin{vmatrix} s+c & a & b \\ c & s+a & b \\ c & a & s+b \end{vmatrix} = 532$ then the value of s is



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12. Let $a, b, c, \in R$ not all are equal and $\Delta_1 = \begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$

$\Delta_2 = \begin{vmatrix} a+2b & b+3c & c+4a \\ b+2c & c+3a & a+4b \\ c+2a & a+3b & b+4c \end{vmatrix}$ then $\frac{\Delta_2}{\Delta_1} = \underline{\hspace{2cm}}$



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13. Three distinct points $P(3u^2, 2u^3)$; $Q(3v^2, 2v^3)$ and $R(3w^2, 2w^3)$ are collinear then

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14. if $\Delta_r = \begin{vmatrix} r & 612 & 915 \\ 101r^2 & 2r & 3r \\ r & \frac{1}{r} & \frac{1}{r^2} \end{vmatrix}$ then the value of

$\lim_{n \rightarrow \infty} \frac{1}{n^3} \left(\sum_{r=1}^n \Delta_r \right)$ is _____

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15. if $x=31, y=32$ and $z=33$ then the value of

$\begin{vmatrix} (x^2 + 1)^2 & (xy + 1)^2 & (xz + 1)^2 \\ (xy + 1)^2 & (y^2 + 1)^2 & (yz + 1)^2 \\ (xz + 1)^2 & (yz + 1)^2 & (z^2 + 1)^2 \end{vmatrix}$ is _____



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16. Let α, β, γ are the real roots of the equation $x^3 + ax^2 + bx + c = 0$ ($a, b, c \in \mathbb{R}$ and $a \neq 0$). If the system of equations (u, v, w) given by $\alpha u + \beta v + \gamma w = 0$, $\beta u + \gamma v + \alpha w = 0$, $\gamma u + \alpha v + \beta w = 0$ has non-trivial solutions then the value of a^2/b is _____.

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17. The value of $|\alpha|$ for which the system of equation

$$\alpha x + y + z = \alpha - 1$$

$$x + \alpha y + z = \alpha - 1$$

$$x + y + \alpha z = \alpha - 1$$

has no solution, is _____

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18. Number of values of θ lying in $[0, 100\pi]$ for which the system of equations $(\sin 3\theta) x - y + z = 0$, $(\cos 2\theta) x + 4y + 3z = 0$, $2x + 7y + 7z = 0$ has non-trivial solution is _____



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JEE Main Previous Year

1. Let a, b, c be such that $b(a+c) \neq 0$. If

$$\begin{vmatrix} a & a+1 & a-1 \\ -b & b+1 & b-1 \\ c & c-1 & c+1 \end{vmatrix} + \begin{vmatrix} a+1 & b+1 & c-1 \\ a-1 & b-1 & c+1 \\ (-1)^{n+2}a & (-1)^{n+1}b & (-1)^n c \end{vmatrix} = 0, \text{ Then the}$$

value of 'n' is:

- A. zero
- B. any even integer
- C. any odd integer
- D. any integer

Answer: 3



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2. Consider the system of linear equations:

$$x_1 + 2x_2 + x_3 = 3$$

$$2x_1 + 3x_2 + x_3 = 3$$

$$3x_1 + 5x_2 + 2x_3 = 1$$

The system has

- A. no solution
- B. infinite number of solutions
- C. exactly three solutions.
- D. a unique solution

Answer: 1



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3. The number of values of k for which the linear equations $4x + ky + 2z = 0$, $kx + 4y + z = 0$, $2x + 2y + z = 0$ possess a non-zero solution is : (1) 3 (2) 2 (3) 1 (4) zero

A. zero

B. 3

C. 2

D. 1

Answer: 3



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4. The number of values of k for which the system of equations:

$$kx + (3k + 2)y = 4k$$

$$(3k - 1)x + (9k + 1)y = 4(k + 1)$$
 has no solution, are

A. infinite

B. 1

C. 2

D. 3

Answer: 2



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5. If $\alpha, \beta \neq 0$, and $f(n) = \alpha^n + \beta^n$ and

$$|31 + f(1)1 + f(2)1 + f(1)1 + f(2)1 + f(3)1 + f(2)1 + f(3)1 + f(4)| = K(1 - \alpha)^2(1 - \beta)^2$$

, then K is equal to (1) $\alpha\beta$ (2) $\frac{1}{\alpha\beta}$ (3) 1 (4) -1

A. $\alpha\beta$

B. $\frac{1}{\alpha\beta}$

C. 1

D. -1

Answer: 3



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6. The set of all values of λ for which the system of linear equations

$$x - 2y - 2z = \lambda x$$

$$x + 2y + z = \lambda y$$

$$-x - y = \lambda z$$

has a non-trivial solution

- A. is an empty set
- B. is a singleton set
- C. contains two elements
- D. contains more than two elements

Answer: 3



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7. The system of linear equations $x + \lambda y - z = 0$ $\lambda x - y - z = 0$ $x + y - \lambda z = 0$ has a non-trivial solution for : (1) infinitely many values of λ . (2) exactly one value of λ . (3) exactly two values of λ . (4) exactly three values of λ .

- A. Exactly one value of λ
- B. Exactly two values of λ
- C. Exactly three values of λ
- D. Infinitely many values of λ

Answer: 3



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8. If S is the set of distinct values of ' b ' for which the following system of linear equations $x + y + z = 1$ $x + ay + z = 1$ $ax + by + z = 0$ has no solution, then S is : a finite set containing two or more elements (2) a singleton an empty set (4) an infinite set

- A. a singleton set
- B. an empty set
- C. an infinite set
- D. a finite set containing two or more elements

Answer: 1

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9. Let ω be a complex number such that $2\omega + 1 = z$ where $z = \sqrt{-3}$.

If $\left| 1111 - \omega^2 - 1\omega^2 1\omega^2 \omega^7 \right| = 3k$, then k is equal to : -1 (2) 1 (3) $-z$ (4) z

- A. 1
- B. $-z$
- C. z
- D. -1

Answer: 2



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10. If the system of linear equations $x+ky+3z=0$ $3x+ky-2z=0$ $2x+4y-3z=0$ has a non-zero solution (x,y,z) then $\frac{xz}{y^2}$ is equal to

A. 30

B. -10

C. 10

D. -30

Answer: 3



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11. If $\begin{vmatrix} x-4 & 2x & 2x \\ 2x & x-4 & 2x \\ 2x & 2x & x-4 \end{vmatrix} = (A+Bx)(x-A)^2$ then the ordered pair (A,B) is

equal to

A. (4, 5)

B. (-4, -5)

C. (-4, 3)

D. (-4, 5)

Answer: D



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JEE Advanced Previous Year

1. Which of the following values of α satisfying the equation

$$\left| (1 + \alpha)^2(1 + 2\alpha)^2(1 + 3\alpha)^2(2 + \alpha)^2(2 + 2\alpha)^2(2 + 3\alpha)^2(3 + \alpha)^2(3 + 2\alpha)^2(3 + 3\alpha)^2 \right|$$

-4 b. 9 c. -9 d. 4

A. -4

B. 9

C. -9

D. 4

Answer: 2,3



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2. Let $a, \lambda, \mu \in \mathbb{R}$, Consider the system of linear equations $ax + 2y = \lambda$ and $3x - 2y = \mu$. Which of the following statement (s) is (are) correct?

- A. If $\alpha = -3$ then the system has infinitely many solutions for all values of λ and μ
- B. If $\alpha \neq -3$ then the system has a unique solution for all values of λ and μ
- C. If $\lambda + \mu = 0$ then the system has infinitely many solutions for $\alpha = -3$
- D. If $\lambda + \mu \neq 0$ then the system has no solution for $\alpha = -3$

Answer: 2,3,4

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3. Let ω be the complex number $\cos\left(\frac{2\pi}{3}\right) + i\sin\left(\frac{2\pi}{3}\right)$. Then the number of

distinct complex cos numbers z satisfying $\Delta = \begin{vmatrix} z+1 & \omega & \omega^2 \\ \omega & z+\omega^2 & 1 \\ \omega^2 & 1 & z+\omega \end{vmatrix} = 0$

is

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4. The total number of distinct $x \in R$ for which

$\begin{vmatrix} x & x^2 & 1+x^3 \\ 2x & 4x^2 & 1+8x^3 \\ 3x & 9x^2 & 1+27x^3 \end{vmatrix} = 10$

is (A) 0 (B) 1 (C) 2 (D) 3

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5. For a real number α , if the system $\begin{bmatrix} 1 & \alpha & \alpha^2 \\ \alpha & 1 & \alpha \\ \alpha^2 & \alpha & 1 \end{bmatrix} [xyz] = [1 \ 1 \ 1]$ of linear equations, has infinitely many solutions, then $1 + \alpha + \alpha^2 =$

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6. Let P be a matrix of order 3×3 such that all the entries in P are from the set $\{-1, 0, 1\}$. Then, the maximum possible value of the determinant of P is _____.

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Question Bank

1. Number of real roots of the equation $[[1, x, x], [x, 1, x], [x, x, 1]] + [[1 - x, 1, 1], [1, 1 - x, 1], [1, 1, 1 - x]] = 0$ is

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2. If
$$\begin{vmatrix} \sqrt{3}x - x^2 & x - 1 & x - \sqrt{3} \\ \sqrt{3}x & x & \sqrt{3} - 1 \\ x - 1 & \sqrt{3} - x & x - 1 \end{vmatrix} = ax^4 + bx^3 + cx^2 + dx + e \quad \text{and}$$

$a + c = p + \sqrt{q}$, then $(p - q)$ is equal to

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3. If

$$f(x) = \begin{vmatrix} \cos(x + \alpha) & \cos(x + \beta) & \cos(x + \gamma) \\ \sin(x + \alpha) & \sin(x + \beta) & \sin(x + \gamma) \end{vmatrix}$$

and

$$f(0) = -2 \text{ then } \sum_{r=1}^{30} |f(r)| \text{ equals}$$

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4. Let $f(x) = \begin{vmatrix} 1 + \sin^2 x & \cos^2 x & 4\sin 2x \\ \sin^2 x & 1 + \cos^2 x & 4\sin 2x \\ \sin^2 x & \cos^2 x & 1 + 4\sin 2x \end{vmatrix}$, the maximum value of $f(x)$

is

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5. Given $2x - y + 2z = 1$, $x - 2y + z = -4$, and $x + y + \lambda z = 4$. Then the value of λ such that the given system of equation has no solution is

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6. If M and m are maximum and minimum value, respectively of

$\begin{vmatrix} 1 & \cos\theta & 1 \\ \cos\theta & 1 & \cos\theta \\ -1 & \cos\theta & 1 \end{vmatrix}$, then value of $(M + m)$ is

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7. The value of $\begin{vmatrix} \log_3 512 & \log_4 3 \\ \log_3 8 & \log_4 9 \end{vmatrix} \begin{vmatrix} \log_2 3 & \log_8 3 \\ \log_3 4 & \log_3 4 \end{vmatrix}$ is

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8. If $|(1, x, x^2), (x, x^2, 1), (x^2, 1, x)| = 3$, then the value of $|(x^3-1, 0, x-x^4), (0, x-x^4), x^3-1), (x-x^4, x^3-1, 0)|$

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9. If a, b, c are the sides of a scalene triangle such that $|(a, a^2, a^3-1), (b, b^2, b^3-1), (c, c^2, c^3-1)| = 0$, then the \geq ometric mean of a, b, c is

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10. Let $a + b + c = s$ and $|(s+c, a, b), (c, s+a, b), (c, a, s+b)|$ is equal to 54 then the value of s is

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