

## MATHS

### BOOKS - CENGAGE

### DETERMINANTS

#### Solved Examples And Exercises

1. If  $f(\theta) = \begin{vmatrix} \sin^2 A & \cot A & 1 \\ \sin^2 B & \cos B & 1 \\ \sin^2 C & \cos C & 1 \end{vmatrix}$ , then (a)  $\tan A + \tan B + c$  (b)  $\cot A \cot B \cot C$  (c)  $\sin^2 A + \sin^2 B + \sin^2 C$  (d) 0



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2. Let  $\Delta(x) = \begin{vmatrix} 3 & 3x & 3x^2 + 2a^2 \\ 3x & 3x^2 + 2a^2 & 3x^3 + 6a^2x \\ 3x^2 + 2a^2 & 3x^3 + 6a^2x & 3x^4 + 12a^2x^2 + 2a^4 \end{vmatrix}$  then



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3. The determinant Delta =  $| (a^2 + x)abacab(b^2 + x)bcacbc(c^2 + x) |$  is divisible by  
a.  $x$  b.  $x^2$  c.  $x^3$  d. none of these

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4. If  $f(x) = \begin{vmatrix} a & -1 & 0 \\ ax & a & -1 \\ ax^2 & ax & a \end{vmatrix}$ , then  $f(2x) - f(x)$  is divisible by  
(a)  $a$  (b)  $b$   
(c)  $c, d, e$  (d) none of these

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5. If  $(x) = |x^2+4x-3 \ 2x+4 \ 13 \ 2x^2+5x-9 \ 4x+5 \ 26 \ 8x^2-6x+1 \ 16 \ x-6 \ 104| = a x^3+b x^2+c x+d$ , then  
a.  $a=3$  b.  $b=0$  c.  $c=0$  d. none of these

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6. If  $|x^n x^{n+2} x^{2n} 1 x^a a x^{n+5} x^{a+6} x^{2n+5}| = 0, \forall x \in R$ , where  $n \in N$ ,

then value of  $a$  is n b.  $n - 1$  c.  $n + 1$  d. none of these



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7. Let  $x < 1$ , then value of  $\begin{bmatrix} x^2 + 2 & 2x + 1 & 1 \\ 2x + 1 & x + 2 & 1 \\ 3 & 3 & 1 \end{bmatrix}$  is a. none-negative b.

none-positive c. negative d. positive



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8. If  $f(x) = \begin{vmatrix} 0 & x-a & x-b \\ x+a & 0 & x-c \\ x+b & x+c & 0 \end{vmatrix}$  then



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9. Value of  $\begin{bmatrix} x+y & z & z \\ x & y+z & x \\ y & y & z+x \end{bmatrix}$ , where  $x, y, z$  are nonzero real number, is equal to  
a.  $xyz$  b.  $2xyz$  c.  $3xyz$  d.  $4xyz$



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10. Which of the following is not the root of the equation

$$\begin{vmatrix} x & -6 & -1 \\ 2 & -3x & x-3 \\ -3 & 2x & x+2 \end{vmatrix} = 0?$$

a. 2 b. 0 c. 1 d. -3



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11. If A,B,C are the angles of a non right angled triangle ABC. Then find the

value of:  $\begin{vmatrix} \tan A & 1 & 1 \\ 1 & \tan B & 1 \\ 1 & 1 & \tan C \end{vmatrix}$



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12. If  $f(x) = |xaaaaxaaax| = 0$ , then  $f'(x) = 0$  and  $f''(x) = 0$  has common root  $f''(x) = 0$  and  $f'(x) = 0$  has common root sum of roots of  $f(x) = 0$  is  $-3a$  none of these



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13. Evaluate  $\begin{bmatrix} \cos \alpha \cos \beta & \cos \alpha \sin \beta & -\sin \alpha \\ -\sin \beta & \cos \beta & 0 \\ \sin \alpha \cos \beta & \sin \alpha \sin \beta & \cos \alpha \end{bmatrix} = 0$



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14. Roots of the equation  $|xmn1axn1abx1abc1| = 0$  are independent of  $m$ , and  $n$  independent of  $a, b$ , and  $c$  depend on  $m, n$ , and  $a, b, c$  independent of  $m, n$  and  $a, b, c$



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15. Prove that the value of determinants is zero:

$$|a - bb - cc - ax - yy - zz - xp - qq - rr - p|$$



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16. If  $a, b, c$  are different, then the value of

$$|0x^2 - ax^3 - bx^2 + a0x^2 + cx^4 + bx - c0| = 0 \text{ is } \begin{array}{l} \text{c} \\ \text{b} \\ \text{c} \\ \text{c} \\ \text{b} \\ \text{d} \\ \text{0} \end{array}$$



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17. Prove that the value of each the following determinants is zero:

$$\begin{vmatrix} a_1 & la_1 + mb_1 & b_1 \\ a_2 & la_2 + mb_2 & b_2 \\ a_3 & la_3 + mb_3 & b_3 \end{vmatrix}$$



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18. If  $|b + + aa + ba + + + ac + aa + + + c| = k|abac|$ , then value

of  $k$  is  $\begin{array}{l} \text{1} \\ \text{b} \\ \text{2} \\ \text{c} \\ \text{3} \\ \text{d} \\ \text{4} \end{array}$



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19. A triangle has vertices  $A_i(x_i, y_i)$  for  $i = 1, 2, 3$ . If the orthocentre of triangle is  $(0, 0)$ , then prove that

$$|x_2 - x_3 y_2 - y_3 y_1(y_2 - y_3) + x_1(x_2 - x_3)x_3 - x_1 y_2 - y_3 y_2(y_3 - y_1) + x_1(y_2 - y_3)|$$



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20. If  $\alpha, \beta, \gamma$  are the roots of  $ax^3 + bx^2 + cx + d = 0$  and  $|\alpha\beta\gamma\beta\gamma\alpha\gamma\alpha\beta| = 0$ ,  $\alpha \neq \beta \neq \gamma$  then find the equation whose roots are  $\alpha + \beta - \gamma, \beta + \gamma - \alpha$ , and  $\gamma + \alpha - \beta$ .



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21. If  $\Delta = \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}$  and  $\Delta_1 = \begin{vmatrix} a_1 + pb_1 & b_1 + qc_1 & c_1 + ra_1 \\ a_2 + pb_2 & b_2 + qc^2 & c^2 + ra^2 \\ a_3 + pb_3 & b_3 + qc_3 & c_3 + ra_3 \end{vmatrix}$  then

$$\Delta_1 =$$



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22. Prove that the value of each the following determinants is zero:

$$\begin{vmatrix} (a^x + a^{-x})^2 & (a^x - a^{-x})^2 & 1 \\ (b^y + b^{-y})^2 & (b^y - b^{-y})^2 & 1 \\ (c^z + c^{-z})^2 & (c^z - c^{-z})^2 & 1 \end{vmatrix}$$



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23. The value of the determinant  $\begin{bmatrix} 1^2 & 2^2 & 3^2 & 4^2 \\ 2^2 & 3^2 & 4^2 & 5^2 \\ 3^2 & 4^2 & 5^2 & 6^2 \\ 4^2 & 5^2 & 6^2 & 7^2 \end{bmatrix}$  is equal to 1 b. 0 c. 2 d. 3



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24. If  $f(x) =$

$$|1xx + 12xx(x-1)(x+1)x3x(x-1)x(x-1)(x-2)(x+1)x(x-1)|$$

then  $f(500)$  is equal to 0 b. 1 c. 500 d. -500



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25. Show that  $\begin{vmatrix} \log x & \log y & \log z \\ \log 2x & \log 2y & \log 2z \\ \log 3x & \log 3y & \log 3z \end{vmatrix} = 0$



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26. If the system of equations  $x - ky - z = 0, kx - y - z = 0, x + y - z = 0$  has a nonzero solution, then the possible value of  $k$  are –1, 2 b. 1, 2 c. 0, 1 d. –1, 1



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27.  $\begin{bmatrix} 1 & 1+p & 1+p+q \\ 2 & 3+2p & 4+3p+2q \\ 3 & 6+3p & 10+6p+3q \end{bmatrix} = 1$



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28. If  $\begin{vmatrix} a & b & a\alpha + b \\ b & c & b\alpha + c \\ a\alpha + b & b\alpha + c & 0 \end{vmatrix} = 0$ , prove that a,b,c, are in G.P. or  $\alpha$  is a root of  $ax^2 + 2bx+c=0$



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29. By using properties of determinants , show that :

$$\begin{bmatrix} 1 + a^2 - b^2 & 2ab & -2b \\ 2ab & 1 - a^2 + b^2 & 2a \\ 2b & -2a & 1 - a^2 - b^2 \end{bmatrix} = (1 + a^2 + b^2)^3$$



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30. Which of the following values of  $\alpha$  satisfy the equation

$$\begin{vmatrix} (1 + \alpha)^2 & (1 + 2\alpha)^2 & (1 + 3\alpha)^2 \\ (2 + \alpha)^2 & (2 + 2\alpha)^2 & (2 + 3\alpha)^2 \\ (3 + alph)^2 & (2 + 2\alpha)^2 & (2 + 3\alpha)^2 \end{vmatrix} = 648\alpha ?$$



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31. solve  $\begin{bmatrix} 3a & -a+b & -a+c \\ -b+a & 3b & -b+c \\ -c+a & -c+b & 3c \end{bmatrix} = 3(a+b+c)(ab+bc+ca)$



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32. If the system of equations  $x + ay = 0$ ,  $az + y = 0$ , and  $ax + z = 0$  has infinite solutions, then the value of equation has no solution is – 3 b.  
1 c. 0 d. 3



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33.

$$\begin{bmatrix} 6i & -3i & 1 \\ 4 & 3i & -1 \\ 20 & 3 & i \end{bmatrix}$$

=x+i y , then a. x=3, y=1 b. x=1, y=3 c. x=0, y=3 d. x=0, y=0



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**34.** The value of  $\begin{vmatrix} yz & zx & xy \\ p & 2q & 3r \\ 1 & 1 & 1 \end{vmatrix}$ , where  $x, y, z$  are respectively,  $p$ th,  $(2q)$ th,  $(3r)$ th terms of an H.P. is

- a. -1 b. 0 c. 1 d. none of these



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**35.** Prove that

$$\begin{vmatrix} (\beta + \gamma - \alpha - \delta)^4 & (\beta + \gamma - \alpha - \delta)^2 & 1 \\ (\gamma + \alpha - \beta - \delta)^4 & (\gamma + \alpha - \beta - \delta)^2 & 1 \\ (\alpha + \beta - \gamma - \delta)^4 & (\alpha + \beta - \gamma - \delta)^2 & 1 \end{vmatrix} = -64(\alpha - \beta)(\alpha - \gamma)(\alpha - \delta)$$



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**36.** Prove that the value of each the following determinants is zero:

$$\begin{vmatrix} \sin^2\left(x + \frac{3\pi}{2}\right) \sin^2\left(x + \frac{5\pi}{2}\right) \sin^2\left(x + \frac{7\pi}{2}\right) \sin^{x+\frac{3\pi}{2}} \sin^{x+\frac{5\pi}{2}} \sin^{x+\frac{7\pi}{2}} \sin^x \end{vmatrix}$$



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37. The number of values of  $k$  for which the lines

$(k + 1)x + 8y = 4k$  and  $kx + (k + 3)y = 3k - 1$  are coincident is

---



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38.

Prove

that

$$|b + ca - bac + ab - cba + bc - ac| = 3ab - a^3 - b^3 - c^3.$$



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39.

If

$$|a^2b^2c^2(a + 1)^2(b + 1)^2(c + 1)^2(a - 1)^2(b - 1)^2(c - 1)^2| = k(a - b)(b - c)$$

then find the value of  $k$ .



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40.

Statement

1:

Delta =  $|my + nzmq + nrmb + nckz - mxkr - mpkc - ma - nx - ky|$  is equal to 0. Statement 2: The value of skew symmetric matrix of order 3 is zero.



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41.

Prove

that

$$= |111abcbc + a^2ac + b^2ab + c^2| = 2(a - b)(b - c)(c - a)$$



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42. If the determinant  $| \cos(\theta+\phi) \sin\theta \ -\cos\theta \ -\sin(\theta+\phi) \ \cos\theta \ \sin\theta \ \cos 2\phi \ \sin\phi \ \cos\phi |$  is positive is independent of  $\theta$  is independent of  $\varphi$  none of these



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43. The system of equations  $-2x + y + z = a$ ,  $x - 2y + z = b$ ,  $x + y - 2z = c$ , has: (a) no solution if  $a + b + c \neq 0$  (b) unique solution if  $a + b + c = 0$  (c) infinite number of solutions if  $a + b + c = 0$  (d) none of these



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44. Show that if  $x_1, x_2, x_3 \neq 0$

$$|x_1 + a_1 b_1 a_1 b_2 a_1 b_3 a_2 b_1 x_2 + a_2 b_2 a_2 b_3 a_3 b_1 a_3 b_2 x_3 + a_3 b_3| = x_1 x_2 x_3 \left(1 + \frac{a_1}{x_1} + \frac{a_2}{x_2} + \frac{a_3}{x_3}\right)$$

.



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45. determinant  $\begin{vmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{vmatrix}$



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46. If  $\Delta_r = \begin{vmatrix} 2^{r-1} & 2 \cdot 3^{r-1} & 4 \cdot 5^{r-1} \\ \alpha & \beta & \gamma \\ 2^n - 1 & 3^n - 1 & 5^n - 1 \end{vmatrix}$ , then find the value of  $\Delta$



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47. The values of  $k \in R$  for which the system of equations  $x + ky + 3z = 0, kx + 2y + 2z = 0, 2x + 3y + 4z = 0$  admits of nontrivial solution is  
a. 2 b. 5/2 c. 3 d. 5/4



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48. A determinant of second order is made with the elements 0 and 1. Find the number of determinants with non-negative values.



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49. If  $a, b, c$  are nonzero real numbers such that  $|baabcaacaa| = 0$ , then  
a.  $\frac{1}{a} + \frac{1}{b\omega} + \frac{1}{c\omega^2} = 0$  b.  $\frac{1}{a} + \frac{1}{b\omega^2} + \frac{1}{c\omega} = 0$  c.  $\frac{1}{a\omega} + \frac{1}{b\omega^2} + \frac{1}{c} = 0$

d. none of these



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50. Prove that the determinant  $\begin{bmatrix} x & \sin \theta & \cos \theta \\ -\sin \theta & -x & 1 \\ \cos \theta & 1 & x \end{bmatrix}$  is independent of theta.



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51. Consider the determinant  $f(x) = |0x^2 - ax^3 - bx^2 + a0x^2 + cx^4 + bx - c0|$ . Statement 1:  $f(x) = 0$  has one root  $x = 0$ . Statement 2: The value of skew symmetric determinant of odd order is always zero.



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52. Find the value of  $|124 - 130410|$



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53. Consider the system of the equation  $kx + y + z = 1$ ,  $x + ky + z = k$ , and  $x + y + kz = k^2$ . Statement 1: System equations has infinite solutions when  $k = 1$ . Statement 2: If the determinant  $|1\ 1\ 1\ k\ k\ 1\ k^2\ 1\ k| = 0$ , then  $k = -1$ .



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54. If  $a, b, c \in R$ , then find the number of real roots of the equation

$$\Delta = \begin{vmatrix} x & c & -b \\ -c & x & a \\ b & -a & x \end{vmatrix} = 0$$



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55.  $\Delta = \begin{vmatrix} a & a^2 & 0 \\ 1 & 2a+b & (a+b) \\ 0 & 1 & 2a+3b \end{vmatrix}$  is divisible by a.  $a+b$  b.  $a+2b$  c.  $2a+3b$  d.  $a^2$



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56. Without expanding at any stage, prove that the value of each of the

following determinants is zero. (1)  $\begin{vmatrix} 0 & p-q & p-r \\ q-p & 0 & q-r \\ r-p & r-q & 0 \end{vmatrix}$  (2)  $\begin{vmatrix} 41 & 1 & 5 \\ 79 & 7 & 9 \\ 29 & 5 & 3 \end{vmatrix}$

(3)  $\begin{vmatrix} 1 & w & w^2 \\ w & w^2 & 1 \\ w^2 & 1 & w \end{vmatrix}$ , where  $w$  is cube root of unity



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57. If  $a, b, c$  are all positive, and are  $p^{th}, q^{th}$  and  $r^{th}$  terms of a G.P., show

that  $\begin{vmatrix} \log a & p & 1 \\ \log b & q & 1 \\ \log c & r & 1 \end{vmatrix} = 0$ .



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58. If the entries in a  $3 \times 3$  determinant are either 0 or 1, then the greatest value of their determinants is



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59. The value of the determinant of  $n^{\text{th}}$  order, being given by  $|x \ 1 \ 1 \ 1 \ x \ 1 \ 1 \ 1 \ x|$  is      a.  $(x - 1)^{n-1}(x + n - 1)$       b.  $(x - 1)^n(x + n - 1)$       c.  $(1 - x)^{-1}(x + n - 1)$  d. none of these



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60. Solve the equation  $\begin{bmatrix} x+a & x & x \\ x & x+a & x \\ x & x & x+a \end{bmatrix} = 0, a \neq 0$



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61. If  $a_1 b_1, c_1, a_2 b_2 c_2$  and  $a_3 b_3 c_3$  are three digit even natural numbers and  $= |c_1 a_1 b_1 c_2 a_2 b_2 c_3 a_3 b_3|$ , then is divisible by 2 but not necessarily by 4 divisible by 4 but not necessarily by 8 divisible by 8 none of these



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**62.** If  $= \begin{vmatrix} abc & b^2c & c^2b \\ abc & c^2a & ca^2 \\ abc & a^2b & b^2a \end{vmatrix} = 0$ , ( $a, b, c \in R$ ) and are all different and nonzero), then prove that  $a + b + c = 0$ .



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**63.** The value of  $\begin{vmatrix} yz & zx & xy \\ p & 2q & 3r \\ 1 & 1 & 1 \end{vmatrix}$ , where  $x, y, z$  are respectively,  $p$ th,  $(2q)$  th, and  $(3r)$  th terms of an H.P. is a. -1 b. 0 c. 1 d. none of these



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**64.** Show that the determinant  $|a^2 + b^2 + c^2bc + ca + ac + ca + ac + ca + ab + ba^2 + b^c + c^2bc + ca + ac + ca|$  is always non-negative.



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65. If  $x \neq 0, y \neq 0, z \neq 0$  and  $\begin{vmatrix} 1+x & 1 & 1 \\ 1+y & 1+2y & 1 \\ 1+z & 1+z & 1+3z \end{vmatrix} = 0$ , then  $x^{-1} + y^{-1} + z^{-1}$  is equal to a.1 b.-1 c.-3 d. none of these



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66. If  $x \neq y \neq z$  and  $\begin{vmatrix} x & x^2 & 1+x^3 \\ y & y^2 & 1+y^3 \\ z & z^2 & 1+z^3 \end{vmatrix} = 0$ , then the value of  $xyz$  is a.1 b. 2 c. -1 d. 2



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67. Prove that

$$\begin{vmatrix} 2 & \alpha + \beta + \gamma + \delta & \alpha\beta + \gamma\delta \\ \alpha + \beta + \gamma + \delta & 2(\alpha + \beta)(\gamma + \delta) & \alpha\beta(\gamma + \delta) + \gamma\delta(\alpha + \beta) \\ \alpha\beta + \gamma\delta & \alpha\beta(\gamma + \delta) + \gamma\delta(\alpha + \beta) & 2\alpha\beta\gamma\delta \end{vmatrix}$$



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68. Solve for  $x$ ,  $|x - 6 - 12 - 3 \times - 3 - 32 \times + 2| = 0$ .



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69. The value of determinant  $|111^m C_1^{m+1} C_1^{m+2} C_1^m C_2^{m+1} C_2^{m+2} C_2|$  is equal to  
a. 1 b.  $-1$  c. 0 d. none of these



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70. Solve the equation  
 $|a - xcbcb - xabac - x| = 0$  where  $a + b + c \neq 0$ .



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71. If  $a^2 + b^2 + c^2 = -2$  and  $f(x) = |a + a^2x(1 + b^2)x(1 + c^2)x(1 + a^2)x| + b^2x(1 + c^2)x(1 + a^2)x(1 + b^2)x$ , then  $f(x)$  is a polynomial of degree  
a. 0 b. 1 c. 2 d. 3



72. Consider the set A of all determinants of order 3 with entries 0 or 1 only. Let B be the subset of A consisting of all determinants with value 1. Let C be the subset of the set of all determinants with value –1. Then

A. A) C his empty

B. null

C. null

D. null



73.

Solve:

$$|x^2 - 1x^2 + 2x + 12x^2 + 3x + 12x^2 + x - 12x^2 + 5x - 32x^2 + 4x - 36x^2|$$



74. If  $|x3636x6x3| = |2x7x7272x| = |45x5x4x45| = 0$ , then  $x$  is equal to 0 b. -9 c. 3 d. none of these



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75. If  $A_1B_1C_1$ ,  $A_2B_2C_2$  and  $A_3B_3C_3$  are three digit numbers, each of which is divisible by k, then  $\Delta = \begin{vmatrix} A_1 & B_1 & C_1 \\ A_2 & B_2 & C_2 \\ A_3 & B_3 & C_3 \end{vmatrix}$  is



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76. If  $f'(x) = |mxmx - pmx + p \cap + pn - pmx + 2nmx + 2n + pmx + 2n -$ , then  $y = f(x)$  represents a straight line parallel to x-axis a straight line parallel to y-axis parabola a straight line with negative slope



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77. If  $\sum_{n=1}^n \alpha_n = an^2 + bn$ , where  $a, b$  are constants and  $\alpha_1, \alpha_2, \alpha_3 \in \{1, 2, 3, \dots, 9\}$  and  $25\alpha_1, 37\alpha_2, 49\alpha_3$  be three digit number, then prove that  $|\alpha_1\alpha_2\alpha_3 57925\alpha_1 37\alpha_2 49\alpha_3| = 0$



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78. The determinant  $|xp + yxyyp + zyz0xp + yyp + z| = 0$  if  $x, y, z$

A. a) if  $x, y, z$  are in AP

B. b)  $x, y, z$  are in GP

C. c)  $x, y, z$  are in HP

D. d)  $xy, zy, zx$  are in AP



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79. Using properties of determinant prove that

$$|a + b + c - c - b - ca + b + c - a - b - aa + b + c| = 2(a + b)(b + c)(c + a)$$



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80. Show that

$$\left| \begin{smallmatrix} xC_r^x C_{r+1}^x C_{r+2}^y C_r^y C_{r+1}^y C_{r+2}^z C_r^z C_{r+1}^z C_{r+1}^z \\ xC_r^{x+1} C_{r+1}^{x+2} C_{r+2}^y C_r^y \end{smallmatrix} \right| = \left| \begin{smallmatrix} xC_r^x C_{r+1}^x C_{r+2}^y C_r^y C_{r+1}^y C_{r+2}^z C_r^z C_{r+1}^z C_{r+1}^z \\ xC_r^{x+1} C_{r+1}^{x+2} C_{r+2}^y C_r^y \end{smallmatrix} \right|$$



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81. If  $\omega \neq 1$  is a cube root of unity and  $x + y + z \neq 0$ , then prove that

$$\left| \begin{smallmatrix} x & y & z & y & z & x & zz & x & y \\ 1+\omega & \omega+\omega^2 & \omega^2+1 & \omega+\omega^2 & \omega^2+1 & 1+\omega & \omega^2+1 & 1+\omega & \omega+\omega^2 \end{smallmatrix} \right| = 0$$

if  $x = y = z$



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**82.** Statement 1: If the system of equation  $\lambda x + (b - a)y + (c - a)z = 0$ ,  $(a - b)x + \lambda y + (c - b)z = 0$ , and  $(a - c)x + (c - b)y + \lambda z = 0$  has a non trivial solution, then the value of  $\lambda$  is 0. Statement 2: the value of skew symmetric matrix of order 3 is order.



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**83.** If  $A$ ,  $B$  and  $C$  are the angles of a triangle, show that  $| -1 + \cos B \cos C + \cos B \cos B \cos C + \cos A - 1 + \cos A \cos A - 1 + \cos A \cos B | = 0$



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**84.** If  $\alpha, \beta, \gamma$  are the angles of a triangle and system of equations  $\cos(\alpha - \beta)x + \cos(\beta - \gamma)y + \cos(\gamma - \alpha)z = 0$ ,  $\cos(\alpha + \beta)x + \cos(\beta + \gamma)y + \cos(\gamma + \alpha)z = 0$ ,  $\sin(\alpha + \beta)x + \sin(\beta + \gamma)y + \sin(\gamma + \alpha)z = 0$  has non-trivial solutions, then triangle is necessarily a. equilateral b. isosceles c. right angled d. acute angled



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85. Without expanding the determinants, prove that

$$|103115114111108106104113116| + |113116104108106111115114103| = 0$$



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86.

Given

$a = x/(y - z)$ ,  $b = y/(z - x)$ , and  $c = z/(x - y)$ , where  $x, y, z$  and  $z$  are not all zero, then the value of  $ab + bc + ca$  is  
a. 0 b. 1 c. -1 d. none of these



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87. Find the value of determinant

$$\left| \left( \sqrt{(13)} + \sqrt{3}, 2\sqrt{5}, \sqrt{5} \right) \sqrt{(15)} + \sqrt{(26)} 5 \sqrt{(10)} 3 + \sqrt{(65)} \sqrt{(15)} 5 \right|$$



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88.  $a, b, c$  are distinct real numbers not equal to one. If  $ax + y + z = 0, x + by + z = 0, \text{ and } x + y + cz = 0$  have nontrivial solution, then the value of  $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c}$  is equal to a. 1 b. -1 c. zero d. none of these



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89. Prove that the value of the determinant  $\left| -75 + 3i\frac{2}{3} - 4i5 - 3i84 + 5i\frac{2}{3} + 4i4 - fi9 \right|$  is real.



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90. If the system of linear equation  $x + y + z = 6, x + 2y + 3z = 14, \text{ and } 2x + 5y + \lambda z = \mu(\lambda, \mu R)$  has a unique solution, then  $\lambda = 8$  b.  $\lambda = 8, \mu = 36$  c.  $\lambda = 8, \mu \neq 36$  d. none of these



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91. If  $a_r = (\cos 2r\pi + i \sin 2r\pi)^{1/9}$ , then prove that

$$|a_1 a_2 a_3 a_4 a_5 a_6 a_7 a_8 a_9| = 0.$$



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92. Let  $f(x) = |2 \cos^2 x \sin 2x - \sin x \sin 2x| 2 \sin^2 x \cos x \sin x - \cos x|_0$

. Then the value of  $\int_0^{\pi/2} [f(x) + f'(x)] dx$  is a.  $\pi$  b.  $\pi/2$  c.  $2\pi$  d.  $3\pi/2$



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93. Using properties of determinants, prove that

$$\begin{vmatrix} -a^2 & ab & ac \\ ba & -b^2 & bc \\ ca & cb & -c^2 \end{vmatrix} = 4a^2b^2c^2$$



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94. The number of positive integral solutions of the equation

$$\begin{vmatrix} x^3 + 1 & x^2y & x^2z \\ xy^2 & y^3 + 1 & y^2z \\ xz^2 & z^2y & z^3 + 1 \end{vmatrix} = 11 \text{ is}$$



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95. If the value of determinant  $|(a,1,1),(1,b,1)(1,1,c)|$  is positive , then



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96. By using properties of determinants. Show that: (i)

$$\begin{vmatrix} x+4 & 2x & 2x \\ 2x & x+4 & 2x \\ 2x & 2x & x+4 \end{vmatrix} = (5x-4)(4-x)^2 \quad (\text{ii})$$

$$\begin{vmatrix} y+k & y & y \\ y & y+k & y \\ y & y & y+k \end{vmatrix} = y^2(3y+k)$$



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97. Using properties of determinants, evaluate  $|184089408919889198440|$ .



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98. if  $A_1, B_1, C_1 \dots \dots$  are respectively the cofactors of the elements  $a_1, b_1, c_1 \dots \dots$  of the determinant

$$\Delta = \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}, \Delta \neq 0 \text{ then the value of } \begin{vmatrix} B_2 & C_2 \\ B_3 & C_3 \end{vmatrix} \text{ is equal to}$$



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99. Solve for  $x$

$$|x - 22x - 33 \times -4x - 42x - 93x - 16x - 82x - 273x - 64| = 0.$$



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100. If  $\Delta_1 = |x \mathbf{a} x \mathbf{b} a x \mathbf{a}|$  and  $\Delta_2 = |x \mathbf{b} a x|$  are the given determinants, then  $\Delta_1 = 3(\Delta_2)^2$  b.  $\frac{d}{dx}(\Delta_1) = 3\Delta_2$  c.

$$\frac{d}{dx}(\text{Delta}_1) = 3(\text{Delta}_2)^2 \quad d. \quad \text{Delta}_1 = 3\text{Delta}_2^2 / 2$$



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101. Without expanding evaluate the determinant

$$\begin{vmatrix} \sin \alpha & \cos \alpha & \sin(\alpha + \delta) \\ \sin \beta & \cos \beta & \sin(\beta + \delta) \\ \sin \gamma & \cos \gamma & \sin(\gamma + \delta) \end{vmatrix}$$



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102. if  $y = \sin mx$ , then the value of the determinant

$$\begin{vmatrix} y & y_1 & y_2 \\ y_3 & y_4 & y_5 \\ y_6 & y_7 & y_8 \end{vmatrix} \quad \text{Where } y_n = \frac{d^n y}{dx^n} \text{ is}$$



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103. Find the value of the determinant  $|1111123413610141020|$



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104. The parameter on which the value of the determinant

$$|1aa^2\cos(p-d)x \cos px \cos(p+d)x \sin(p-d)x \sin px \sin(p+d)x|$$

does not depend is a b. p c. d d. x



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105. If  $x = cy + bz$ ,  $y = az + cx$ ,  $z = bx + ay$ , where  $x, y, z$  are not all zeros, then find the value of  $a^2 + b^2 + c^2 + 2abc$ .



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106. If  $\begin{vmatrix} b^2 + c^2 & ab & ac \\ ab & c^2 + a^2 & bc \\ ca & cb & a^2 + b^2 \end{vmatrix} = ka^2b^2c^2$ , then the value of  $k$  is abc

b.  $a^2b^2c^2$  c.  $bc + ca + ab$  d. none of these



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**107.** The value of  $| -1213 + 2\sqrt{22} + 2\sqrt{213} - 2\sqrt{22} - 2\sqrt{21} |$  is equal to

- a. zero b.  $-16\sqrt{2}$  c.  $-8\sqrt{2}$  d. none of these



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**108.** Find the following system of equations is consistent,

$$(a+1)^3x + (a+2)^3y = (a+3)^3 \quad (a+1)x + (a+2)y = a+3$$

$$x + y = 1, \text{ then find the value of } a$$



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**109.** Prove the identities:  $\begin{vmatrix} b^2 + c^2 & ab & ac \\ ba & c^2 + a^2 & bc \\ ca & cb & a^2 + b^2 \end{vmatrix} = 4a^2b^2c^2$



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**110.** Prove that

$$\begin{bmatrix} 1 + a^2 + a^4 & 1 + ab + a^2b^2 & 1 + ac + a^2c^2 \\ 1 + ab + a^2b^2 & 1 + b^2 + b^4 & 1 + bc + b^2c^2 \\ 1 + ac + a^2c^2 & 1 + bc + b^2c^2 & 1 + c^2 + c^4 \end{bmatrix} = (a - b)^2(b - c)^2(c - a)^2$$



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**111.** If  $x, y, z$  are in A.P., then the value of the determinant are in A.P., then

the value of the determinant

$|a + 2a + 3a + 2xa + 3a + 4a + 2ya + 4a + 5a + 2z|$  is a. 1 b. 0 c. 2a d.

a



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**112.** Prove that

$$\begin{vmatrix} (b+x)(c+x) & (c+x)(a+x) & (a+x)(b+x) \\ (b+y)(c+y) & (c+y)(a+y) & (a+y)(b+y) \\ (b+z)(c+z) & (c+z)(a+z) & (a+z)(b+z) \end{vmatrix} = (a-b)(b-c)(c-a)$$



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113. If  $a + b + c = 0$ , one root of  $\begin{bmatrix} a - x & c & b \\ c & b - x & a \\ b & a & c - x \end{bmatrix} = 0$  is a.

- x = 1 b. x = 2 c.  $x = a^2 + b^2 + c^2$  d. x = 0



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114. Factorize the following

$$|3a + b + ca^3 + b^3 + c^3a + b + ca^2 + b^2 + c^2a^4 + b^4 + c^4a^2 + b^2 + c^2a^3 +$$



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115. Let  $\{D_1, D_2, D_3, D_n\}$  be the set of third order determinant that can be made with the distinct non-zero real numbers  $a_1, a_2, a_q$ . Then

$$\sum_{i=1}^n D_i = 1 \text{ b. } \sum_{i=1}^n D_i = 0 \text{ c. } D_i = D_j, \forall i, j \text{ d. none of these}$$



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116. If  $g(x) = \frac{f(x)}{(x-a)(x-b)(x-c)}$ , where  $f(x)$  is a polynomial of degree  $< 3$ , then prove that

$$\frac{dg(x)}{dx} = |1af(a)(x-a)^{-2}1bf(b)(x-b)^{-2}1cf(c)(x-c)^{-2}| + |a^2a1b^2b1c|$$



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117. If the equation

$2x + 3y + 1 = 0, 3x + y - 2 = 0$ , and  $ax + 2y - b = 0$  are consistent, then prove that  $a - b = 2$ .



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118. If  $w$  is a complex cube root of unity, then value of

$$= |a_1 + b_1wa_1w^2 + b_1c_1 + b_1wa_2 + b_2wa_2w^2 + b_2c_2 + b_2wa_3 + b_3wa_3w^2 +$$

is a. 0 b.  $-1$  c. 2 d. none of these



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119.

Let

$$f(x) = |\cos(x + x^2)\sin(x + x^2) - \cos(x + x^2)\sin(x - x^2)\cos(x - x^2)\sin(x - x^2)|$$

. Find the value of  $f'(0)$ .



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120. If  $f(x)$ ,  $g(x)$  and  $h(x)$  are three polynomials of degree 2, then prove that

$$\varphi(x) = |f(x)g(x)h(x)f'(x)g'(x)h'(x)f^x g^x h^x| \text{ is a constant polynomial}$$



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121. If  $a, b, c$  are in G.P. with common ratio  $r_1$  and  $\alpha, \beta, \gamma$  are in G.P. with common ratio  $r_2$  and equations  $ax + \alpha y + z = 0, bx + \beta y + z = 0, cx + \gamma y + z = 0$  have only zero solution, then which of the following is not true? a.  $a + b + c$  b.  $abc$  c. 1 d. none of these



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122. Show that:

$$|ab - + ba + cbc - aa - + ac| = (a + b + c)(a^2 + b^2 + c^2).$$



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123. In triangle  $ABC$ , if

$$\left| \frac{\cot A}{2} \frac{\cot B}{2} \frac{\cot C}{2} \frac{\tan B}{2} + \frac{\tan C}{2} \frac{\tan B}{2} + \frac{\tan A}{2} \frac{\tan A}{2} + \frac{\tan B}{2} \right|$$

then the triangle must be  
a. equilateral b. isosceles c. obtuse angled d.  
none of these



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124. If  $a, b, c, d, e$ , and  $f$  are in G.P. then the value of  $\begin{vmatrix} (a^2) & (d^2) & x \\ (b^2) & (e^2) & y \\ (c^2) & (f^2) & z \end{vmatrix}$

depends on (A)  $x$  and  $y$  (B)  $x$  and  $z$  (C)  $y$  and  $z$  (D) independent of  $x, y$ , and  $z$



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125. Prove that:

$$\begin{vmatrix} (b+c)^2 & a^2 & a^2 \\ b^2 & (c+a)^2 & b^2 \\ c^2 & c^2 & (a+b)^2 \end{vmatrix} = 2abc(a+b+c)^3$$



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126. if  $x_i = a_i b_i C_i$   $i = 1, 2, 3$  are three-digit positive integer such that

each  $x_i$  is a multiple of 19 then prove that  $\begin{matrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{matrix}$  is divisible by 19.



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127. The system of linear equations  $x + \lambda y - z = 0$   $\lambda x - y - z = 0$   $x + y - \lambda z = 0$  has a non-trivial solution for : (1) infinitely many values of  $\lambda$  . (2) exactly one value of  $\lambda$  . (3) exactly two values of  $\lambda$  . (4) exactly three values of  $\lambda$  .



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128. If  $pqr \neq 0$  and the system of equation  $(p+a)x + by + cz = 0$ ,  $ax + (q+b)y + cz = 0$ ,  $ax + by + (r+c)z = 0$  has nontrivial solution, then value of  $\frac{a}{p} + \frac{b}{q} + \frac{c}{r}$  is  
a. -1 b. 0 c. 0 d. -2



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129. If  $c < 1$  and the system of equations  $x + y - 1 = 0$ ,  $2x - y - c = 0$ , and  $bx + 3by - c = 0$  is consistent, then the possible real values of  $b$  are  
a.  $b\left(-3\frac{3}{4}\right)$  b.  $b\left(-\frac{3}{2}, 4\right)$  c.  $b\left(-\frac{3}{4}, 3\right)$  d. none of these



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130. Prove that
- $$\begin{vmatrix} x^2 & x^2 - (y-z)^2 & yz \\ y^2 & y^2 - (z-x)^2 & zx \\ z^2 & z^2 - (x-y)^2 & xy \end{vmatrix} = (x-y)(y-z)(z-x)(x+y+z)(x^2 + y^2 + z^2 - xy - yz - zx)$$



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131. If  $a, b$  and  $c$  are real numbers, and

$$\Delta = \begin{bmatrix} b+c & C+a & a+b \\ c+a & a+b & b+c \\ a+b & b+c & c+a \end{bmatrix} = 0$$

Show that either  $a + b + c = 0$  or  $a = b = c$ .



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132. If  $a, b, c$  are non-zero, then the system of equations

$$(\alpha + a)x + \alpha y + \alpha z = 0, \alpha x + , (\alpha + b)y + \alpha z = 0, \alpha x + \alpha y + (\alpha + c)z$$

has a non-trivial solution if  $\alpha^{-1} =$  (A)  $-(a^{-1} + b^{-1} + c^{-1})$  (B)

$a + b + c$  (C)  $\alpha + a + b + c = 1$  (D) none of these



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133. Prove that

$$|ab + ca^2bc + ab^2ca + bc^2| = - (a + b + c) \times (a - b)(b - c)(c - a).$$



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134. If  $a > 0$  and discriminant of  $ax^2 + 2bx + c$  is negative, then

$$\begin{vmatrix} a & b & ax + b \\ b & c & bx + c \\ ax + b & bx + c & 0 \end{vmatrix} \text{ is } +ve \text{ b. } (ac - b)^2(ax^2 + 2bx + c) \text{ c. } -ve \text{ d.}$$

0



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135. If  $\begin{vmatrix} a - b - c & 2a & 2a \\ 2b & b - c - a & 2b \\ 2c & 2c & c - a - b \end{vmatrix} = (a + b + c)$

$\times (x + a + b + c)^2$ ,  $x \neq 0$  and  $a + b + c \neq 0$  then  $x$  is equal to



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136. If  $a_1, a_2, a_3, \dots, a_n, \dots$  are in G.P., then the determinant  $\Delta =$

$$\begin{vmatrix} \log a_n & \log a_{n+1} & \log a_{n+2} \\ \log a_{n+3} & \log a_{n+4} & \log a_{n+5} \\ \log a_{n+6} & \log a_{n+7} & \log a_{n+8} \end{vmatrix} \text{ is equal to}$$



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137. By using properties of determinants , show that :

$$\begin{bmatrix} a^2 + 1 & ab & ac \\ ab & b^2 + 1 & bc \\ ca & cb & c^2 + 1 \end{bmatrix} = 1 + a^2 + b^2 + c^2$$



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138. Let  $\vec{a}_r = x_r \hat{i} + y_r \hat{j} + z_r \hat{k}, r = 1, 2, 3$  be three mutually

perpendicular unit vectors, then the value of  $\begin{vmatrix} x_1 & x_2 & x_3 \\ y_1 & y_2 & y_3 \\ z_1 & z_2 & z_3 \end{vmatrix}$  is equal to 0

b.  $\pm 1$  c.  $\pm 2$  d. none of these



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139. The number of distinct real roots of  $\begin{vmatrix} \sin x & \cos x & \cos x \\ \cos x & \sin x & \cos x \\ \cos x & \cos x & \sin x \end{vmatrix} = 0$  in the

interval  $\pi/4 \leq x \leq \pi/4$  is 0 b. 2 c. 1 d. 3



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140. Let  $a, b, c$  be real numbers with  $a^2 + b^2 + c^2 = 1$ . Show that the equation

$|ax - by - cbx - aycx + abx + ay - ax + by - y + bcx + acy + b - ax|$   
represents a straight line.



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141. If lines  $px + qy + r = 0$ ,  $qx + ry + p = 0$  and  $rx + py + q = 0$  are concurrent, then prove that  $p + q + r = 0$  (where  $p, q, r$  are distinct).



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142. If  $p\lambda^4 + q\lambda^3 + r\lambda^2 + s\lambda + t = \begin{vmatrix} \lambda^2 + 3\lambda & \lambda - 1 & \lambda + 3 \\ \lambda^2 + 1 & 2 - \lambda & \lambda - 3 \\ \lambda^2 - 3 & \lambda + 4 & 3\lambda \end{vmatrix}$  then  $t =$



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**143.** Find the value of  $\lambda$  if  $2x^2 + 7xy + 3y^2 + 8x + 14t + \lambda = 0$  represents a pair of straight lines

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**144.** If  $x, y, z$  are different from zero and

$$\text{Delta} = \begin{vmatrix} a & b - y & c - z \\ a - x & b & c - z \\ a - x & b - y & c \end{vmatrix} = 0, \text{ then the value of the expression } \frac{a}{x} + \frac{b}{y} + \frac{c}{z} \text{ is}$$

a. 0 b. -1 c. 1 d. 2

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**145.** If  $A, B, C$  are angles of a triangles, then the value of

$$\begin{vmatrix} e^{2iA} & e^{-iC} & e^{-iB} \\ e^{-iC} & e^{2iB} & e^{-iA} \\ e^{-iB} & e^{-iA} & e^{2iC} \end{vmatrix}$$

is 1 b. -1 c. -2 d. -4

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146. For the equation  $\begin{vmatrix} 1 & x & x^2 \\ x^2 & 1 & x \\ x & x^2 & 1 \end{vmatrix} = 0$ , There are exactly two distinct

roots There is one pair of equation real roots. There are three pairs of equal roots Modulus of each root is 2



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147. Let  $\Delta_r = |r - 1|n6(r - 1)^22n^24n - 2(r - 1)^23n^33n^2 - 3n|$ .

Show that  $\sum_{r=1}^n \Delta_r$  is constant.



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148. Let  $m$  be a positive integer and  $\Delta r = \begin{vmatrix} 2r - 1 & {}^m C_r & 1 \\ m^2 - 1 & 2^m & m + 1 \\ \sin^2(m^2) & \sin^2 m & \sin(m^2) \end{vmatrix}$ .

Then the value of  $\sum_{r=0}^m \Delta r$



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**149.**

Prove

that

$$|1 + a11111 + b11111 + c11111 + d| = abcd \left( a + \frac{1}{a} + b + \frac{1}{b} + c + \frac{1}{c} + d + \frac{1}{d} \right).$$

Hence find the value of the determinant if  $a, b, c, d$  are the roots of the equation  $px^4 + qx^3 + rx^2 + sx + t = 0$ .



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**150.** Find the area of a triangle having vertices  $A(3, 2)$ ,  $B(11, 8)$ , and  $C(8, 12)$ .



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**151.**

If

$$D_k = 1 \cap 2kn^2 + n + 1n^2 + n2k - 1n^2n^2 + n + 1 \text{ and } \sum_{k=1}^n D_k = 56.$$

then  $n$  equals a. 4 b. 6 c. 8 d. none of these



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**152.** If  $a \neq p, b \neq q, c \neq r$  and  $|pbcaqcabr| = 0$ , then find the value of

$$\frac{p}{p-a} + \frac{q}{q-b} + \frac{r}{r-c}.$$



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**153.** If  $x_1, x_2, x_3$  as well as  $y_1, y_2, y_3$  are in G.P. with same common ratio, then prove that the points  $(x_1, y_1), (x_2, y_2)$ , and  $(x_3, y_3)$  are collinear.



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**154.** If the lines  $a_1x + b_1y + 1 = 0$ ,  $a_2x + b_2y + 1 = 0$  and  $a_3x + b_3y + 1 = 0$  are concurrent, show that the points  $(a_1, b_1)$ ,  $(a_2, b_2)$  and  $(a_3, b_3)$  are collinear.



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155. For a fixed positive integer  $n$ , if  $= |n!(n+1)!(n+2)!(n+1)!(n+2)!(n+3)!(n+2)!(n+3)!(n+4)|$ , then show that  $\left[ / \left( (n!)^3 \right) - 4 \right]$  is divisible by  $n$ .



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156. The number of values of  $a$  for which the lines  $2x + y - 1 = 0$ ,  $ax + 3y - 3 = 0$ , and  $3x + 2y - 2 = 0$  are concurrent is 0 (b) 1 (c) 2 (d) infinite



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157. If the lines  $ax + y + 1 = 0$ ,  $x + by + 1 = 0$  and  $x + y + c = 0$  ( $a, b, c$  being distinct and different from 1) are concurrent, then prove that  $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} = 1$ .



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**158.** If  $(1 + ax + bx^2)^4 = a_0 + a_1x + a_2x^2 + \dots + a_8x^8$  when

$a, b, a_0, a_1, a_2, \dots, a_8 \in R$  such that  $a_0 + a_1 + a_2 \neq 0$  and

$$\begin{vmatrix} a_0 & a_1 & a_2 \\ a_1 & a_2 & a_0 \\ a_2 & a_0 & a_1 \end{vmatrix} = 0 \text{ then the value of } 5 \frac{a}{b}$$

(A) 6 (B) 8 (C) 10 (D) 12



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**159.** Find the value of  $\lambda$  for which the homogeneous system of equations:

$2x + 3y - 2z = 0$     $2x - y + 3z = 0$     $7x + \lambda y - z = 0$  has non-trivial solutions. Find the solution.



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**160.** If  $f, g, \text{ and } h$  are differentiable functions of

$x$  and  $(x) = |fgh(x)f'(xg')(xh')(x^{f^2}f'')(x^2g'')(x^2h')|$  prove

$$\Delta' = |(f'g'h)f'g'h'(x^{3f''})(x^{3g''})(x^{3h''})|'$$



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**161.** If, a,b,c are positive and unequal, show that value of the determinant

$$\Delta = \begin{bmatrix} a & b & c \\ b & c & a \\ c & a & b \end{bmatrix}$$
 is negative



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**162.** if  $= \begin{vmatrix} x^n & n! & 2 \\ \cos x & \cos. \frac{n\pi}{2} & 4 \\ \sin x & \sin. \frac{n\pi}{2} & 8 \end{vmatrix}$ , then find the value of  $\frac{d^n}{dx^n} [f(x)]_{x=0}$ . ( $n \in z$ ).



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**163.** Without expanding a determinant at any stage, show that |

$$|x^2 + x, x + 1, x + 2|, |, 2x^2 + 3x - 1, 3x, 3x - 3|, |x^2 + 2x + 3, 2x - 1, 2|$$

are determinant of order 3 not involving  $x$ .



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164. Show that

$$\begin{vmatrix} bc - a^2 & ca - b^2 & ab - c^2 \\ ca - b^2 & ab - c^2 & bc - a^2 \\ ab - c^2 & bc - a^2 & ca - b^2 \end{vmatrix} \\ \begin{vmatrix} a^2 & c^2 & 2ca - b^2 \\ 2ab - c^2 & b^2 & a^2 \\ b^2 & 2ac - a^2 & c^2 \end{vmatrix}.$$



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165. Show that the system of equations  $3x - y + 4z = 3$ ,  $x + 2y - 3z = -2$  and  $6x + 5y + \lambda z = -3$  has at least one solution for any real number  $\lambda$ . Find the set of solutions of  $\lambda = -5$



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166. Show that

$$\begin{vmatrix} 2bc - a^2 & c^2 & b^2 \\ c^2 & 2ca - b^2 & a^2 \\ b^2 & a^2 & 2ab - c^2 \end{vmatrix} = \begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}^2$$



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**167.** If  $y = |\sin x \cos x \sin x \cos x - \sin x \cos x \times 11| = f \in d \frac{dy}{dx}$ .



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**168.** Consider the system of equation  $x + y + z = 6$ ,  $x + 2y + 3z = 10$ , and  $x + 2y + \lambda z = \mu$ . Statement 1: if the system has infinite number of solutions, then  $\mu = 10$ . Statement 2: The determinant  $|1\ 1\ 6\ 1\ 2\ 1\ 0\ 1\ 2\ \mu| = 0$  or  $\mu = 10$ .



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**169.** Consider the system of linear equations in  $x, y$  and  $z$ :  
 $(\sin 3\theta)x - y + z = 0$   $(\cos 2\theta)x + 4y + 3z = 0$   $3x + 7y + 7z = 0$  Which of the following can be the value of  $\theta$  for which the system has a non-trivial solution  
A)  $n\pi + (-1)^n \frac{\pi}{6}$ ,  $\forall n \in Z$       B)  $n\pi + (-1)^n \frac{\pi}{3}$ ,  $\forall n \in Z$   
C)  $n\pi + (-1)^n \frac{\pi}{9}$ ,  $\forall n \in Z$       D) none of these



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170. Prove without expansion that

$$|ah + bggab + chbf + ba fhb + bcaf + bbg + fc| = a|ah + bgahbf + bahb|$$



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171. If  $\alpha, \beta$  and  $\gamma$  are real numbers without expanding at any stage prove

that

$$\begin{vmatrix} 1 & \cos(\beta - \alpha) & \cos(\gamma - \alpha) \\ \cos(\alpha - \beta) & 1 & \cos(\gamma - \beta) \\ \cos(\alpha - \gamma) & \cos(\beta - \gamma) & 1 \end{vmatrix} = 0.$$



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172. If 3 digit numbers  $A28, 3B9$  and  $62C$  are divisible by a fixed

constant 'K' where A, B, C are integers lying between 0 and 9, then

determinant  $\begin{vmatrix} A & 3 & 6 \\ 8 & 9 & C \\ 2 & B & 2 \end{vmatrix}$  is always divisible by



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**173.** If  $a = \cos \theta + i \sin \theta$ ,  $b = \cos 2\theta - i \sin 2\theta$ ,  $c = \cos 3\theta + i \sin 3\theta$  and

if  $\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix} = 0$  then a.  $\theta = 2k\pi, k \in Z$  b.  $\theta = (2k+1)\pi, k \in Z$  c.

$\theta = (4k+1)\pi, k \in Z$  d. none of these



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**174.** Prove that

$$|a_1\alpha_1 + b_1\beta_1a_1\alpha_2 + b_2\beta_2a_1\alpha_3 + b_1\beta_3a_2\alpha_1 + b_2\beta_1a_2\alpha_2 + b_2\beta_2a_2\alpha_3 + b_2\beta_3a_3\alpha_1|$$



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**175.** If  $\alpha, \beta, \gamma$  are the roots of  $px^3 + qx^2 + r = 0$ , then the value of the

determinant  $\begin{vmatrix} \alpha\beta & \beta\gamma & \gamma\alpha \\ \beta\gamma & \gamma\alpha & \alpha\beta \\ \gamma\alpha & \alpha\beta & \beta\gamma \end{vmatrix}$  is p b. q c. 0 d. r



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**176.** Prove that

$$|(a-x)^2(a-y)^2(a-z)^2(b-x)^2(b-y)^2(b-z)^2(c-x)^2(c-y)^2(c-z)|$$

$$|(1+ax)^2(1+bx)^2(1+cx)^2(1+ay)^2(1+by)^2(1+cy)^2(1+az)^2(1+bz)|$$



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**177.** If  $|1 \times^2 \times^2 1x^2 1x| = ,$  then find the value of

$$|x^3 - 10x - x^4|$$



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**178.** If

$$|x^n x^{n+2} x^{n+3} y^n y^{n+2} y^{n+3} z^n z^{n+2} z^{n+3}| = (x-y)(y-z)(z-x) \left( \frac{1}{x} + \frac{1}{y} \right)$$

then n equals 1 b. -1 c. 2 d. -2



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**179.** Solve the system of the equations:  $ax + by + cz = d$   
 $a^2x + b^2y + c^2z = d^2$   $a^3x + b^3y + c^3z = d^3$  Will the solution always exist and be unique?



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**180.** if  $\begin{vmatrix} a & b - c & c + b \\ a + c & b & c - a \\ a - b & a + b & c \end{vmatrix} = 0$  then the line  $ax + by + c = 0$

passes through the fixed point which is



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**181.** If  $2ax - 2y + 3z = 0$ ,  $x + ay + 2z = 0$ , and  $2 + az = 0$  have a nontrivial solution, find the value of  $a$ .



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182. If  $\lfloor \cdot \rfloor$  denotes the greatest integer less than or equal to the real number under consideration and  $-1 \leq x < 0, 0 \leq y < 1, 1 \leq z < 2$ ,

then the value of the determinant  $\begin{vmatrix} \lfloor x \rfloor + 1 & \lfloor y \rfloor & \lfloor z \rfloor \\ \lfloor x \rfloor & \lfloor y \rfloor + 1 & \lfloor z \rfloor \\ \lfloor x \rfloor & \lfloor y \rfloor & \lfloor z \rfloor + 1 \end{vmatrix}$  is



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183. if  $(x) = a + bx + cx^2$  and  $\alpha, \beta, \gamma$  are the roots of the equation

$x^3 = 1$  then  $\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$  is equal to



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184. If  $x, y$  and  $z$  are not all zero and connected by the equations  $a_1x + b_1y + c_1z = 0, a_2x + b_2y + c_2z = 0$ , and  $(p_1 + \lambda q_1)x + (p_2 + \lambda q_2) +$ , show that  $\lambda = - |a_1b_1c_1a_2b_2c_2p_1p_2p_3| \div |a_1b_1c_1a_2b_2c_2q_1q_2q_3|$



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**185.** Find  $\lambda$  for which the system of equations  $x + y - 2z = 0, 2x - 3y + z = 0, x - 5y + 4z = \lambda$  is consistent and find the solutions for all such values of  $\lambda$ .



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**186.** If  $p, q, r$  are in A.P. then value of determinant  $|a^2 + 2^{n+1} + 2pb^2 + 2^{n+2} + 3qc^2 + p2^n + p2^{n+1} 2qa^2 + 2^n + pb^2 + 2^{n+1} c^2|$  is a) 0 (b) Independent from  $a, b, c$  c)  $a^2b^2c^2 - 2^n$  (d) Independent from  $n$



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**187.** For what values of  $k$ , the following system of equations possesses a nontrivial solution over the set of rationals:  
 $c + ky + 3z = 0, 3c + ky - 2z = 0, 2c + 3y - 4x = 0$ . Also find the solution for this value of  $k$ .



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**188.** Let  $a, b, c \in R$  such that no two of them are equal and satisfy

$$\begin{vmatrix} 2a & b & c \\ b & c & 2a \\ c & 2a & b \end{vmatrix} = 0, \text{ then equation } 24ax^2 + 8bx + 4c = 0 \text{ has}$$

(a) at last one root in  $[0, 1]$  (b) at last one root in  $\left[ -\frac{1}{2}, \frac{1}{2} \right]$  (c) at last one root in  $[-1, 0]$  (d) at last two roots in  $[0, 2]$



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**189.** Solve by Cramers rule  $x + y + z = 6$   $x - y + z = 2$

$$3x + 2y - 4z = -5$$



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**190.** The value of the determinant

$$\begin{vmatrix} ka & k^2 + a^2 & 1 \\ kb & k^2 + b^2 & 1 \\ kc & k^2 + c^2 & 1 \end{vmatrix} \text{ is}$$

$$k(a+b)(b+c)(c+a) \quad (\text{B}) \quad kabc(a^2 + b^2 + c^2) \quad (\text{C})$$

$$k(a-b)(b-c)(c-a) \quad (\text{D}) \quad k(a+b-c)(b+c-a)(c+a-b)$$



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191. Find the value of  $a$  and  $b$  if the system of equation  
 $a^2x - by = a^2 - b$  and  $bx = b^2y = 2 + 4b$  (i) posses unique solution (ii)  
infinite solutions



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192. If  $(x_1 - x_2)^2 + (y_1 - y_2)^2 = a^2$ ,  $(x_2 - x_3)^2 + (y_2 - y_3)^2 = b^2$ ,  
 $(x_3 - x_1)^2 + (y_3 - y_1)^2 = c^2$ , and

$$k \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix} = (a + b + c)(b + c - b)(c + a - b) \times (a + b - c), \text{ then}$$

the value of  $k$  is 1 b. 2 c. 4 d. none of these



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193.  $f(x) = |\cos x \times 12 \sin x \times 2x \tan x \times 1|$ . Then value of  $(\lim)_{x \rightarrow 0} \frac{f(x)}{x}$   
is equal to 1 b. -1 c. zero d. none of these



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**194.** If the system of linear equation  $x + 2ay + az = 0$ ,  $x + 3by + bz = 0$ ,  $x + 4cy + cz = 0$  has a non-trivial solution then show that  $a, b, c$  are in H.P.



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**195.** Let  $\alpha$  be a repeated root of a quadratic equation  $f(x) = 0$  and  $A(x), B(x), C(x)$  be polynomials of degrees 3, 4, and 5, respectively, then show that  $|A(x)B(x)C(x)A(\alpha)B(\alpha)C(\alpha)A'(\alpha)B'(\alpha)C'(\alpha)|$  is divisible by  $f(x)$ , where prime (') denotes the derivatives.



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**196.** If  $|a^2 + \lambda^2 ab + c\lambda ca - b\lambda ab - c\lambda b^2 + \lambda^2 bc + aca + b\lambda bc - a\lambda c^2 + \lambda^2| |\lambda c -$ , then the value of  $\lambda$  is a) 8 b. 27 c. 1 d. -1



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197. Value of

$$|1 + x_1 1 + x_1 x_1 + x_1 x^2 1 + x_2 1 + x_2 x_1 + x_2 x^2 1 + x_3 1 + x_3 x_1 + x_3 x^2|$$

depends upon x<sub>0</sub> only b. x<sub>1</sub> only c. x<sub>2</sub> only d. none of these



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198. If  $(x) = |\alpha + x\theta + x\lambda + x\beta + x\varphi + x\mu + x\gamma + x\psi + xv + x|$

show that  $\Delta^{\hat{}}(x) = 0$  and  $\Delta(0) + Sx$ , where  $S$  denotes the sum of all the cofactors of all elements in  $\Delta(0)$  and dash denotes the derivative with respect of  $x$ .



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199. The value of determinant

$$|bc - a^2ac - b^2ab - c^2ac - b^2ab - c^2bc - a^2ab - c^2bc - a^2ac - b^2|$$

is a. always positive b. always negative c. always zero d. cannot say anything



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200. If  $l_1^2 + m_1^2 + n_1^2 = 1$  etc., and  $l_1l_2 + m_1m_2 + n_1n_2 = 0$ , etc. and

$$\Delta = \begin{vmatrix} l_1 & m_1 & n_1 \\ l_2 & m_2 & n_2 \\ l_3 & m_3 & n_3 \end{vmatrix} \text{ then}$$



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201. Let  $\begin{vmatrix} x & 2 & x \\ x^2 & x & 6 \\ x & x & 6 \end{vmatrix} = Ax^4 + Bx^3 + Cx^2 + Dx + E$ . Then the value

of  $5A + 4B + 3C + 2D + E$  is equal to



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202. Let  $a, b, c$  be the real numbers. The following system of equations in  $x, y, \text{ and } z$

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{a^2} = 1, \quad \frac{x^2}{a^2} - \frac{y^2}{b^2} + \frac{z^2}{a^2} = 1, \quad -\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{a^2} = 1 \text{ has}$$

- a. no solution b. unique solution c. infinitely many solutions d. finitely many solutions



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**203.** The value of the determinant

$$\left| [\sin \theta, \cos \theta, \sin 2\theta], \left[ \sin\left(\theta + \frac{2\pi}{3}\right), \cos\left(\theta + \frac{2\pi}{3}\right), \sin\left(2\theta + \frac{4\pi}{3}\right) \right], \left[ \sin\left(\theta + \frac{4\pi}{3}\right), \cos\left(\theta + \frac{4\pi}{3}\right), \sin\left(2\theta + \frac{8\pi}{3}\right) \right] \right|$$



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**204.** Find the value of the determinant  $|baabpqrl111|$ , where  $a, b, and c$  are respectively, the  $p$ th,  $q$ th, and  $r$ th terms of a harmonic progression.



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**205.** let  $a > 0, d > 0$  find the value of the determinant

$$\begin{vmatrix} \frac{1}{a} & \frac{1}{a(a+d)} & \frac{1}{(a+d)(a+2d)} \\ \frac{1}{a+d} & \frac{1}{(a+d)(a+2d)} & \frac{1}{(a+2d)(a+3d)} \\ \frac{1}{a+2d} & \frac{1}{(a+2d)(a+3d)} & \frac{1}{(a+3d)(a+4d)} \end{vmatrix}$$



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206. For all values of A,B,C and P,Q,R show that

$$\begin{vmatrix} \cos(A - P) & \cos(A - Q) & \cos(A - R) \\ \cos(B - p) & \cos(B - Q) & \cos(B - R) \\ \cos(C - P) & \cos(C - Q) & \cos(C - R) \end{vmatrix} = 0$$



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207. Let  $\lambda$  and  $\alpha$  be real. Find the set of all values of  $\lambda$  for which the system of linear equations

$$\lambda x + (\sin \alpha)y + (\cos \alpha)z = 0, x + (\cos \alpha)y + (\sin \alpha)z = 0, -x + (\sin \alpha) have trivial solution$$


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208.

Prove

that

$$|ax - by - cz| + |ay + bx - cz| + |az + cx - bz| + |cy + bz - cx|$$



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**209.** If  $(x) = |\alpha + x\theta + x\lambda + x\beta + x\varphi + x\mu + x\gamma + x\psi + xv + x|$  show that  $\Delta^{\wedge}(x) = 0$  and  $\Delta(0) + Sx$ , where  $S$  denotes the sum of all the cofactors of all elements in  $\Delta(0)$  and dash denotes the derivative with respect of  $x$ .



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**210.** If  $\alpha, \beta, \gamma$  are different from 1 and are the roots of  $ax^3 + bx^2 + cx + d = 0$  and  $(\beta - \gamma)(\gamma - \alpha)(\alpha - \beta) = \frac{25}{2}$ , then prove that  $\left| \frac{\alpha}{1 - \alpha} \frac{\beta}{1 - \beta} \frac{\gamma}{1 - \gamma} \alpha\beta\gamma\alpha^2\beta^2\gamma^2 \right| = \frac{25d}{2(a + b + c + d)}$



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**211.** If  $p + q + r = 0 = a + b + c = 0$ , then the value of the determinant  $|paqbrcqcrapbrbpqqa|$  is a. 0 b.  $pa + qb + rc$  c. 1 d. none of these





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212.

Let

$$= |2a_1b_1a_1b_2 + a_2b_1a_1b_3 + a_3b_1a_1b_2 + a_2b_12a_2b_2a_2b_3 + a_3b_2a_1b_3 + a_3b_1a_3b_2|$$

. Expressing as the product of two determinants, show that = 0. Hence,

show

that

if

$$ax^2 + 2hxy + by^2 + 2gx + 2fy + c = (lx + my + n)(l'x + m'y + n), \text{ then}$$



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$$213. \text{ If } 2s = a + b + c \text{ and } A = \begin{vmatrix} a^2 & (s-a)^2 & (s-a)^2 \\ (s-b)^2 & b^2 & (s-b)^2 \\ (s-c)^2 & (s-c)^2 & c^2 \end{vmatrix} \text{ then}$$

det A



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$$214. \text{ Evaluate } |xC_1^x C_2^x C_3^y C_1^y C_2^y C_3^z C_1^z C_2^z C_3|$$



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215. Using factor theorem, show that

$$\begin{vmatrix} -2a & a+b & c+a \\ a+b & -2a & b+c \\ c+a & c+b & -2c \end{vmatrix} = 4(a+b)(b+c)(c+a)$$



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216. If a determinant of order  $3 \times 3$  is formed by using the numbers 1 or -1 then minimum value of determinant is :



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217. If  $z = | -53 + 4i5 - 7i3 - 4i68 + 7i5 + 7i8 - 7i9 |$ , then  $z$  is purely real purely imaginary  $a + ib$ , where  $a \neq 0$ ,  $b \neq 0$  d.  $a + ib$ , where  $b = 4$



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218. If  $\omega = cis \frac{2\pi}{3}$ , then number of distinct roots of

$$\begin{vmatrix} z+1 & \omega & \omega^2 \\ \omega & z+\omega^2 & 1 \\ \omega^2 & 1 & z+\omega \end{vmatrix} = 0.$$



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219. If  $\omega$  is the complex cube root of unity then

$$\begin{vmatrix} 1 & 1+i+\omega^2 & \omega^2 \\ 1-i & -1 & \omega^2-1 \\ -i & -i+\omega-1 & -1 \end{vmatrix} =$$



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220.

If

$$ax12 + by12 + cz12 = ax22 + by22 + cz22 = ax32 + by32 + cz32 = d, ax$$

then prove that  $|x_1y_1z_1x_2y_2z_2x_3y_3z_3| = (d-f) \left\{ \frac{(d+2f)}{abc} \right\}^{1/2}$



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**221.** If  $A$ ,  $B$ , and  $C$  are the angles of triangle, show that the system of equations

$x \sin 2A + y \sin C + z \sin B = 0$ ,  $\sin C + y \sin 2B + z \sin A = 0$ , and  $x \sin B + y \sin A + z \sin C = 0$  posses nontrivial solution. Hence, system has infinite solutions.



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**222.** Let  $\alpha, \beta, \gamma$  are the real roots of the equation  $x^3 + ax^2 + bx + c = 0$  ( $a, b, c \in R$  and  $a \neq 0$ ). If the system of equations  $(u, v, w)$  given by  $\alpha u + \beta v + \gamma w = 0$ ,  $\beta u + \gamma v + \alpha w = 0$ ,  $\gamma u + \alpha v + \beta w = 0$  has non-trivial solutions then the value of  $a^2/b$  is \_\_\_\_\_.



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**223.** If  $a_1, a_2, a_3, 54, a_6, a_7, a_8, a_9$  are in H.P., and  $D = |a_1 a_2 a_3 45 a_6 a_7 a_8 a_9|$ , then the value of  $[D]$  is where  $[.]$  represents the greatest integer function



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224. If  $f(x)$  is a polynomial of degree  $< 3$ , prove that

$$|1af(a)/(x-a)1bf(b)/(x-b)1cf(c)/(x-c)| \div |1aa^21^21^2| = \frac{1}{(x)}$$



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225.

Prove

that

$$= |acc - a + bcbb - cb + ca - bb - c0a - cxxyz1 + x + y| = 0 \text{ implies}$$

that  $a, b, c$  are in A.P. or  $a, c, b$  are in G.P.



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226.

Solve

for

$x \in R$

:

$$\begin{vmatrix} (x+a)(x-a) & (x+b)(x-b) & (x+c)(x-c) \\ (x-a)^3 & (x-b)^3 & (x-c)^3 \\ (x+a)^3 & (x+b)^3 & (x+c)^3 \end{vmatrix} = 0, \text{ a,b and c being}$$

distinct real numbers.



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227. Absolute value of sum of roots of the equation  $|x + 22x + 33x + 42x + 33x + 44x + 53x + 55c + 810x + 17| = 0$  is \_\_\_\_\_.



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228. Let  $\alpha_1, \alpha_2$  and  $\beta_1, \beta_2$  be the roots of the equation  $ax^2 + bx + c = 0$  and  $px^2 + qx + r = 0$  respectively. If the system of equations  $\alpha_1y + \alpha_2z = 0$  and  $\beta_1y - 2z = 0$  has a non trivial solution then prove that  $\frac{b^2}{q^2} = \frac{ac}{pr}$



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229. The product of all values of  $t$ , for which the system of equations  $(a - t)x + by + cz = 0, bx + (c - t)y + az = 0, cx + ay + (b - t)z = 0$

has non-trivial solution, is  $|a - c - b - cb - a - b - ac|$  (b)  $|abcbcacab|$

$|acaba|$  (d)  $|aa + + c + + a + aa + b|$



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230. Let  $\omega = -\frac{1}{2} + i\frac{\sqrt{3}}{2}$ , then value of the determinant

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & -1 & -\omega^2 \\ \omega^2 & \omega^2 & \omega \end{bmatrix}$$
 is (a)  $3\omega$  (b)  $3\omega(\omega - 1)$  (c)  $3\omega^2$  (d)  $3\omega(1 - \omega)$



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231. If  $= |-xa - xab - x|$ , then a factor is  $a + b + x$

$x^2 - (a - b) + x + a^2 + b^2 + ab$        $x^2 - (a + b) + x + a^2 + b^2 - ab$

$a + b - x$



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**232.** If  $g(x) = \left| a^{-x} e^{x \log_e a} x^2 a^{-3x} e^{3x \log_e a} x^4 a^{-5x} e^{5x \log_e a} 1 \right|$ , then graphs of  $g(x)$  is symmetrical about the origin graph of  $g(x)$  is symmetrical about the y-axis  $\left( \frac{d^4 g(x)}{dx^4} \Big|_{x=0} \right) = 0$   $f(x) = g(x) \times \log\left(\frac{a-x}{a+x}\right)$  is an odd function



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**233.** the sum of values of p for which the equations  $x+y+z=1$   $x+2y +4z=p$  and  $x+4y +10z =p^2$  have a solution is \_\_\_\_\_



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**234.** The value of  $|\alpha|$  for which the system of equation  
 $\alpha x + y + z = \alpha - 1$   
 $x + \alpha y + z = \alpha - 1$   
 $x + y + \alpha z = \alpha - 1$   
has no solution , is \_\_\_\_\_





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235. Let

$$D_1 = |aba + bc dc + d ab a - b| \text{ and } D_2 = |aca + cb db + da ca + b + c|$$

then the value of  $\left| \frac{D_1}{D_2} \right|$ , where  $b \neq 0$  and  $a \neq bc$ , is \_\_\_\_.



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236. If

$$|x + yx + y + z^2 x^3 x + 2y^4 x + 3y + 2z^3 x^6 x + 3y^10 x + 6y + 3z| = 64,$$

then the real value of  $x$  is \_\_\_\_\_.



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237. If  $= \left| 13 \cos \theta 1 s \int h \eta 13 \cos \theta 1 s \int h \eta 1 \right|$ , then the value of  $(\_ (\max)) / 2$



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**238.**

If

$$|x^n x^{n+2} x^{n+4} y^n y^{n+2} y^{n+4} z^n z^{n+2} z^{n+4}| = \left(\frac{1}{y^2} - \frac{1}{x^2}\right) \left(\frac{1}{z^2} - \frac{1}{y^2}\right) \left(\frac{1}{x^2} - \frac{1}{z^2}\right)$$

then  $n$  is \_\_\_\_\_.



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**239.**

The value of

$$|2x_1y_1x_1y_2 + x_2y_1x_1y_3 + x_3y_1x_1y_2 + x_2y_12x_2y_2x_2y_3 + x_3y_2x_1y_3 + x_3y_1x_2y_3|$$

is.



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**240.** Given  $A = |ab2cde2flm2n|$ ,  $B = |f2de2n4l2mc2ab|$  , then the

value of  $B/A$  is \_\_\_\_\_.



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**Examples**

1. find the value of

$$\begin{vmatrix} 1 & 2 & 4 \\ -1 & 3 & 0 \\ 4 & 1 & 0 \end{vmatrix}$$



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2. Prove that the determinant  $\Delta = \begin{vmatrix} x & \sin \theta & \cos \theta \\ -\sin \theta & -x & 1 \\ \cos \theta & 1 & x \end{vmatrix}$  is independent of  $\theta$ .



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3. The parameter on which the value of the determinant  
 $|1aa^2\cos(p-d)x\cos px\cos(p+d)x\sin(p-d)x\sin px\sin(p+d)x|$   
does not depend is a b. p c. d d. x



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4. Let  $a, b, c$  be positive and not all equal. Show that the value of the

determinant  $\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$  is negative



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5. If  $a, b, c \in R$ , then find the number of real roots of the equation

$$= |xc - b - cxab - ax| = 0$$



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6. If  $x + y + z = 0$ , prove that

$$\begin{vmatrix} ax & by & cz \\ cy & az & bx \\ bz & cx & ay \end{vmatrix} = xyz \begin{vmatrix} a & b & c \\ c & a & b \\ b & c & a \end{vmatrix}$$



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7. If  $p\lambda^4 + q\lambda^3 + r\lambda^2 + s\lambda + t = \begin{vmatrix} \lambda^2 + 3\lambda & \lambda - 1 & \lambda + 3 \\ \lambda^2 + 1 & 2 - \lambda & \lambda - 3 \\ \lambda^2 - 3 & \lambda + 4 & 3\lambda \end{vmatrix}$  then  $t =$



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8. The largest value of a third order determinant whose elements are equal to 1 or 0 is



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9. Prove that the value of the determinant

$$\begin{vmatrix} -7 & 5 + 3i & \frac{2}{3} - 4i \\ 5 - 3i & 8 & 4 + 5i \\ \frac{2}{3} + 4i & 4 - 5i & 9 \end{vmatrix} \text{ is real}$$



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10. Without expanding the determinants Prove that

$$\begin{vmatrix} 103 & 115 & 114 \\ 111 & 108 & 106 \\ 104 & 113 & 116 \end{vmatrix} + \begin{vmatrix} 113 & 116 & 104 \\ 108 & 106 & 111 \\ 115 & 114 & 103 \end{vmatrix} = 0$$



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11. Prove that

$$\begin{vmatrix} ax & by & cz \\ x^2 & y^2 & z^2 \\ 1 & 1 & 1 \end{vmatrix} = \begin{vmatrix} a & c & c \\ x & y & z \\ yz & xz & xy \end{vmatrix}$$



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12. for  $x, y, z > 0$  Prove that

$$\begin{vmatrix} 1 & \log_x y & \log_x z \\ \log_y x & 1 & \log_y z \\ \log_z x & \log_z y & 1 \end{vmatrix} = 0$$



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13. without expanding at any stage Prove that

$$\begin{vmatrix} 0 & a & -b \\ -a & 0 & -c \\ b & c & 0 \end{vmatrix} = 0$$



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**14.** consider the fourth -degree polynomial equation

$$\begin{vmatrix} a_1 + b_1x & a_1x^2 + b_1 & c_1 \\ a_2 + b_2x^2 & a_2x^2 + b_2 & c_2 \\ a_3 + b_3x^2 & a_3x^2 + b_3 & c_3 \end{vmatrix} = 0$$

Without expanding the determinant find all the roots of the equation.



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**15.** Let  $\Delta_r = |r - 1|n^6(r - 1)^22n^24n - 2(r - 1)^23n^33n^2 - 3n|$ . Show

that  $\sum_{r=1}^n \Delta_r$  is constant.



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**16.** Find the value of  $\begin{vmatrix} 41 & 1 & 5 \\ 79 & 7 & 9 \\ 29 & 5 & 3 \end{vmatrix}$



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17. Find the value of determinant

$$\left| \sqrt{(13)} + \sqrt{3}2\sqrt{5}\sqrt{5}\sqrt{(15)} + \sqrt{(26)}5\sqrt{(10)}3 + \sqrt{(65)}\sqrt{(15)}5 \right|$$



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18. Find the value of the determinant

$$\begin{vmatrix} 1 & 1 & 1 & 1 \\ 1 & 2 & 3 & 4 \\ 1 & 3 & 6 & 10 \\ 1 & 4 & 10 & 20 \end{vmatrix}$$



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19. Prove that

$$\begin{vmatrix} \sin \alpha & \cos \alpha & \sin(\alpha + \delta) \\ \sin \beta & \cos \beta & \sin(\beta + \delta) \\ \sin \gamma & \cos \gamma & \sin(\gamma + \delta) \end{vmatrix} = 0$$



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20. Solve for  $x$

$$|x - 22x - 33 \times - 4x - 42x - 93x - 16x - 82x - 273x - 64| = 0.$$



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21. By using properties of determinants, prove the following:

$$|x + 42x^2 - 2x^2 \times + 42x^2 - 2x^2 \times + 4| = (5x + 4)(4 - x)^2$$



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22. prove that  $\begin{bmatrix} a - b - c & 2a & 2a \\ 2b & b - c - a & 2b \\ 2c & 2c & c - a - b \end{bmatrix} = (a + b + c)^3$



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23. if  $x_i = a_i b_i C_i, i = 1, 2, 3$  are three-digit positive integer such that

each  $x_i$  is a multiple of 19 then prove that  $\det \begin{Bmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{Bmatrix}$  is divisible by 19.



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**24.** If  $a, b$  and  $c$  are real numbers, and

$$\Delta = \begin{bmatrix} b+c & C+a & a+b \\ c+a & a+b & b+c \\ a+b & b+c & c+a \end{bmatrix} = 0$$

Show that either  $a + b + c = 0$  or  $a = b = c$ .



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**25.** Find the value of the determinant  $|baabpqrr111|$ , where  $a, b$ , and  $c$  are respectively, the  $p$ th,  $q$ th, and  $r$ th terms of a harmonic progression.



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**26.**

if  $a_1, a_2, a_3, \dots$  are in A.P, then find the value of the following determinants

$$\begin{array}{lll} a_p + a_{p+m} + a_{p+2m} & 2a_p + 3a_{p+m} + 4a_{p+2m} & 4a_p + 9a_{p+m} + 16a_{p+2m} \\ a_p + a_{q+m} + a_{q+2m} & 2a_q + 3a_{q+m} + 4a_{q+2m} & 4a_q + 9a_{q+m} + 16a_{q+2m} \\ a_r + a_{r+m} + a_{r+2m} & 2a_r + 3a_{r+m} + 4a_{r+2m} & 4a_r + 9a_{r+m} + 16a_{r+2m} \end{array}$$



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27.

Prove

that

$$\left| (1, , \beta\gamma + \alpha\delta, , \beta^2\gamma^2 + \alpha^2, \delta^2), (1, , \gamma\alpha + \beta\delta, , \gamma^2\alpha^2 + \beta^2\delta^2), (1, , \alpha\beta + \gamma\delta, , \alpha^2\beta^2 + \gamma^2\delta^2) \right| = - (a + b + c) \times (a - b)(b - c)(c - a).$$



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28.

Prove

that

$$\left| ab + ca^2bc + ab^2ca + bc^2 \right| = - (a + b + c) \times (a - b)(b - c)(c - a).$$



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29. Prove that

$$\begin{vmatrix} x^2 & x^2 - (y - z)^2 & yz \\ y^2 & y^2 - (z - x)^2 & zx \\ z^2 & z^2 - (x - y)^2 & xy \end{vmatrix}$$

$$= (x - y)(y - z)(z - x)(x + y + z)(x^2 + y^2 + z^2)$$



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30. If  $a, b, c$  are all distinct and  $\begin{vmatrix} a & a^3 & a^4 - 1 \\ b & b^3 & b^4 - 1 \\ c & c^3 & c^4 - 1 \end{vmatrix} = 0$ , show that

$$abc(ab+bc+ac) = a+b+c$$



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31. Prove that  $\begin{vmatrix} a^2 + 1 & ab & ac \\ ab & b^2 + 1 & bc \\ ac & bc & c^2 + 1 \end{vmatrix} = 1 + a^2 + b^2 + c^2$



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32. prove that  $\begin{vmatrix} (b+c)^2 & bc & ac \\ ba & (c+a)^2 & cb \\ ca & cb & (a+b)^2 \end{vmatrix}$

$$\begin{vmatrix} (b+c)^2 & a^2 & a^2 \\ b^2 & (c+a)^2 & b^2 \\ c^2 & c^2 & (a+b)^2 \end{vmatrix} = 2abc(a+b+c)^3$$



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**33.** Let  $a, b, c$  be real numbers with  $a^2 + b^2 + c^2 = 1$ . Show that the equation

$|ax - by - cbx - aycx + abx + ay - ax + by - y + bcx + acy + b - ax|$   
represents a straight line.



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**34.** If  $a^2 + b^2 + c^2 = 1$ , then prove that

$|a^2 + (b^2 + c^2) \cos \varphi ab(1 - \cos \varphi) ac(1 - \cos \varphi) ba(1 - \cos \varphi) b^2 + (c^2 + a^2)|$   
is independent of  $a, b, c$ .



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**35.** Find the area of a triangle having vertices  $A(3, 2)$ ,  $B(11, 8)$ , and  $C(8, 12)$ .



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**36.**

If

the

lines

$a_1x + b_1y + 1 = 0$ ,  $a_2x + b_2y + 1 = 0$  and  $a_3x + b_3y + 1 = 0$  are concurrent, show that the points  $(a_1, b_1)$ ,  $(a_2, b_2)$  and  $(a_3, b_3)$  are collinear.



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**37.** The number of values of  $a$  for which the lines  $2x + y - 1 = 0$ ,  $ax + 3y - 3 = 0$ , and  $3x + 2y - 2 = 0$  are concurrent is 0 (b) 1 (c) 2 (d) infinite



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**38.** If the lines  $ax + y + 1 = 0$ ,  $x + by + 1 = 0$  and  $x + y + c = 0$  ( $a, b, c$  being distinct and different from 1) are concurrent, then prove that

$$\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} = 1.$$


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39. Find the value of  $\lambda$  if  $2x^2 + 6xy + 3y^2 + 8x + 14y + \lambda = 0$  represent a pair of straight lines.

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40. show that the determinant

$$\begin{vmatrix} a^2 + b^2 + c^2 & bc + ca + ab & bc + ca + ab \\ bc + ca + ab & a^2 + b^2 + c^2 & bc + ca + ab \\ bc + ca + ab & bc + ca + ab & a^2 + b^2 + c^2 \end{vmatrix}$$

is always non-negative.

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41. Factorize the following

$$|3a + b + ca^3 + b^3 + c^3a + b + ca^2 + b^2 + c^2a^4 + b^4 + c^4a^2 + b^2 + c^2a^3 +$$

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42. prove that

$$\begin{vmatrix} (a-x)^2 & (a-y)^2 & (a-z)^2 \\ (b-x)^2 & (b-y)^2 & (b-z)^2 \\ (c-x)^2 & (c-y)^2 & (c-z)^2 \end{vmatrix}$$

$$\begin{vmatrix} (1+ax)^2 & (1+bx)^2 & (1+cx)^2 \\ (1+ay)^2 & (1+by)^2 & (1+cy)^2 \\ (1+az)^2 & (1+bx)^2 & (1+cz)^2 \end{vmatrix}$$

$$= 2(b-c)(c-a)(a-b) \times (y-z)(z-x)(x-y)$$



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43. If  $\alpha, \beta, \gamma$  are real numbers, then without expanding at any stage, show that

$$|1 \cos(\beta - \alpha) \cos(\gamma - \alpha) \cos(\alpha - \beta) 1 \cos(\gamma - \beta) \cos(\alpha - \gamma) \cos(\beta - \gamma) 1| = 1$$



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44. If

$$\begin{vmatrix} 1 & x & x^2 \\ x & x^2 & 1 \\ x^2 & 1 & x \end{vmatrix} = 3 \quad \text{then find the value of}$$

$$\begin{vmatrix} x^3 - 1 & 0 & x - x^4 \\ 0 & x - x^4 & x^3 - 1 \\ x - x^4 & x^3 - 1 & 0 \end{vmatrix}$$



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45.

Show

that

$$|bc - a^2ca - b^2ab - c^2ca - b^2ab - c^2bc - a^2ab - c^2bc - a^2ca - b^2| = |a^2c^2 -$$



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46. Let  $= \begin{vmatrix} \cos x & \sin x & \cos x \\ \cos 2x & \sin 2x & 2 \cos 2x \\ \cos 3x & \sin 3x & 3 \cos 3x \end{vmatrix}$  then find the values of  $f(0)$  and  $f'(\pi/2)$ .



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47. If  $f(x) = \left| x \cap !2 \cos x \frac{\cos(n\pi)}{2} 4 \sin x \frac{\sin(n\pi)}{2} 8 \right|$  then find the value of  $\frac{d^n}{dx^n} ([f(x)])_{x=0} n \in z$ .



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**48.** If  $f, g$ , and  $h$  are differentiable functions of

$x$  and  $(x) = |fgh(xf)'(xg)'(xh)'(x^{f^2}f)''(x^2g)''(x^2h)|'$  prove

$$\Delta' = |(fg'h f'g'h'(x^3f'')')(x^3g'')'(x^3h'')'|'$$



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**49.** Let  $\alpha$  be a repeated root of a quadratic equation

$f(x) = 0$  and  $A(x), B(x), C(x)$  be polynomials of degrees 3, 4, and 5,

respectively, then show that

$|A(x)B(x)C(x)A(\alpha)B(\alpha)C(\alpha)A'(\alpha)B'(\alpha)C'(\alpha)|$  is divisible by  $f(x)$

, where prime ( ') denotes the derivatives.



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**50.** if  $\Delta(x) = \begin{vmatrix} a_1 + x & b_1 + x & c_1 + x \\ a_2 + x & b_2 + x & c_2 + x \\ a_3 + x & b_3 + x & c_3 + x \end{vmatrix}$  then show that  $\Delta(x) = 0$

and that  $\Delta(x) = \Delta(0) + sx$ . where  $s$  denotes the sum of all the cofactors of all the elements in  $\Delta(0)$



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51. If  $\Delta(x) = \begin{vmatrix} 1 & x^2 & x^2 \\ 6 & 4x & 3 \\ 9 & x & -7 \end{vmatrix}$  then find the value of  $\int_0^1 \Delta(x) dx$  without expanding  $\Delta(x)$ .

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52. Find the value of  $a$  and  $b$  if the system of equation  $a^2x - by = a^2 - b$  and  $bx = b^2y = 2 + 4b$  (i) posses unique solution (ii) infinite solutions

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53. If a system of three linear equations  $x + 4ay + a = 0$ ,  $x + 3by + b = 0$ , and  $x + 2cy + c = 0$  is consistent, then prove that  $a, b, c$  are in H.P.

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54. Solve by Cramers rule  $x + y + z = 6$      $x - y + z = 2$

$$3x + 2y - 4z = -5$$



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55. For what values of p and q the system of equations

$2x + py + 6z = 8$ ,  $x + 2y + qz = 5$ ,  $x + y + 3z = 4$  has i no solution ii a unique solution iii in finitely many solutions.



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56. If  $2ax - 2y + 3z = 0$ ,  $x + ay + 2z = 0$ , and  $2 + az = 0$  have a

nontrivial solution, find the value of  $a$ .



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57. For what values of  $k$ , the following system of equations possesses a nontrivial solution over the set of rationals:  
 $c + ky + 3z = 0$ ,  $3c + ky - 2z = 0$ ,  $2c + 3y - 4x = 0$ . Also find the solution for this value of  $k$ .



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58. Using factor theorem, show that

$$\begin{vmatrix} -2a & a+b & c+a \\ a+b & -2a & b+c \\ c+a & c+b & -2c \end{vmatrix} = 4(a+b)(b+c)(c+a)$$



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59. If  $a, b$  and  $c$  are non-zero real numbers then prove that

$$\begin{vmatrix} b^2c^2 & bc & b+c \\ c^2a^2 & ca & c+a \\ a^2b^2 & ab & a+b \end{vmatrix} = 0$$



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**60.**

Prove

that

$$|ax - by - czay + bxcx + azay + bxby - cz - axbz + cycx + azbz + cycz|$$



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**61.** If  $f(x)$  is a polynomial of degree  $< 3$ , prove that

$$|1af(a)/(x-a)1bf(b)/(x-b)1cf(c)/(x-c)| \div |1aa^21^21^2| = \frac{1}{(x)}$$



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$$62. \begin{vmatrix} 2a_1b_1 & a_1b_2 + a_2b_1 & a_1b_3 + a_3b_1 \\ a_1b_2 + a_2b_1 & 2a_2b_2 & a_2b_3 + a_3b_2 \\ a_1b_3 + a_3b_1 & a_3b_2 + a_2b_3 & 2a_3b_3 \end{vmatrix} =$$



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$$63. \text{Find the value of } \begin{vmatrix} \cos\left(\frac{2\pi}{63}\right) & \cos\left(\frac{3\pi}{70}\right) & \cos\left(\frac{4\pi}{77}\right) \\ \cos\left(\frac{\pi}{72}\right) & \cos\left(\frac{\pi}{40}\right) & \cos\left(\frac{3\pi}{88}\right) \\ 1 & \cos\left(\frac{\pi}{90}\right) & \cos\left(\frac{2\pi}{99}\right) \end{vmatrix}$$



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64. Let  $f(t) = \begin{vmatrix} \cos t & t & 1 \\ 2 \sin t & t & 2t \\ \sin t & t & t \end{vmatrix}$ . Then find  $\lim_{t \rightarrow 0} \frac{f(t)}{t^2}$



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65.

it

$$x_1^2 + 2y_1^2 + 3z_1^2 = x_2^2 + 2y_2^2 + 3z_2^2 = x_3^2 + 2y_3^2 + 3z_3^2 = 2 \text{ and } x_2x_3 + 2y_2$$

Then find the value of  $\begin{vmatrix} x_1 & y_1 & z_1 \\ x_2 & y_2 & z_2 \\ x_3 & y_3 & z_3 \end{vmatrix}$



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66. about to only mathematics



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67. If  $bc + qr = ca + rp = ab + pq = -1$  and  $(abc, pqr \neq 0)$  then

$$\begin{vmatrix} ap & a & p \\ bq & b & q \\ cr & c & r \end{vmatrix}$$
 is (A) 1 (B) 2 (C) 0 (D) 3



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## Exercise 12.1

1.

Evaluate

$$|\cos \alpha \cos \beta \cos \alpha \sin \beta - \sin \alpha - \sin \beta \cos \beta|$$



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2. If A,B,C are the angles of a non right angled triangle ABC. Then find the

value of:  $\begin{vmatrix} \tan A & 1 & 1 \\ 1 & \tan B & 1 \\ 1 & 1 & \tan C \end{vmatrix}$



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3. If  $e^{i\theta} = \cos \theta + i \sin \theta$ , find the value of  
 $|1e^{i\pi/3}e^{i\pi/4}e^{-i\pi/3}1e^{i2\pi/3}e^{-i\pi/4}e^{-i2\pi/3}1|$



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4. Find the number of real root of the equation  
 $|0x - ax - bx + a0x - cx + bx + c0| = 0, a \neq b \neq c \text{ and } b(a + c) > ac$



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5. If  $\alpha, \beta, \gamma$  are the roots of  
 $ax^3 + bx^2 + cx + d = 0$  and  $|\alpha\beta\gamma\beta\gamma\alpha\gamma\alpha\beta| = 0, \alpha \neq \beta \neq \gamma$  then find the equation whose roots are  $\alpha + \beta - \gamma, \beta + \gamma - \alpha, \text{ and } \gamma + \alpha - \beta$ .



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6. A triangle has vertices  $A_i(x_i, y_i)$  for  $i=1,2,3$ . If the orthocenter of triangle is  $(0,0)$  then prove that

$$\begin{vmatrix} x_2 - x_3 & y_2 - y_3 & y_1(y_2 - y_3) + x_1(x_2 - x_3) \\ x_3 - x_1 & y_3 - y_1 & y_2(y_3 - y_1) + x_2(x_3 - x_1) \\ x_1 - x_2 & y_1 - y_2 & y_3(y_1 - y_2) + x_3(x_1 - x_2) \end{vmatrix} = 0$$



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7. if  $\omega \neq 1$  is cube root of unity and  $x+y+z \neq 0$  then

$$\begin{vmatrix} \frac{x}{1+\omega} & \frac{y}{\omega+\omega^2} & \frac{z}{\omega^2+1} \\ \frac{y}{\omega+\omega^2} & \frac{z}{\omega^2+1} & \frac{x}{1+\omega} \\ \frac{z}{\omega^2+1} & \frac{x}{1+\omega} & \frac{y}{\omega+\omega^2} \end{vmatrix} = 0 \text{ if}$$



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## Exercise 12.2

1. Prove that the value of determinant  $\begin{vmatrix} 1 & \omega & \omega^2 \\ \omega & \omega^2 & 1 \\ \omega^2 & 1 & \omega \end{vmatrix} = 0$

where  $\omega$  is complex cube root of unity .



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2. Prove that  $\begin{vmatrix} a & a^2 & bc \\ b & b^2 & ac \\ c & c^2 & ab \end{vmatrix} \begin{vmatrix} 1 & 1 & 1 \\ a^2 & b^2 & c^2 \\ a^3 & b^3 & c^3 \end{vmatrix}$



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3. if  $\Delta = \begin{vmatrix} abc & a_2 & c^2b \\ abc & c^2a & ca^2 \\ abc & a^2b & b^2a \end{vmatrix} = 0$ , ( $a, b, c \in R$  and are all different and non-zero) then prove that  $a + b + c = 0$



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4. if  $a_r = (\cos 2r\pi + i \sin 2r\pi)^{1/9}$  then prove that

$$\begin{vmatrix} a_1 & a_2 & a_3 \\ a^4 & a^5 & a_6 \\ a_7 & a_8 & a_9 \end{vmatrix} = 0$$



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5. Given  $A = |ab2cde2flm2n|$ ,  $B = |f2de2n4l2mc2ab|$ , then the value of  $B/A$  is \_\_\_\_\_.



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### Exercise 12.3

1. Prove that the value of each the following determinants zero:

$$(a) \begin{vmatrix} a_1 & la_1 + mb_1 & b_1 \\ a_2 & la_2 + mb_2 & b_2 \\ a_3 & la_3 + mb_3 & b_3 \end{vmatrix}$$



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2. using properties of determinants evaluate

$$\begin{vmatrix} 18 & 40 & 89 \\ 40 & 89 & 198 \\ 89 & 198 & 440 \end{vmatrix}$$



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3. Prove that  $\begin{vmatrix} 18 & 40 & 89 \\ 40 & 89 & 198 \\ 89 & 198 & 440 \end{vmatrix} = 3abc - a^3 - b^3 - c^3$



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4.  $\begin{bmatrix} 1 & 1+p & 1+p+q \\ 2 & 3+2p & 4+3p+2q \\ 3 & 6+3p & 10+6p+3q \end{bmatrix} = 1$



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5. Show that  $\begin{vmatrix} a-x & c & b \\ c & b-x & a \\ b & a & c-x \end{vmatrix} = 0$

where  $a + b + c \neq 0$



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6. Show that:

$$|3a - a + b - a + c - b + a3b - b + c - c + a - c + b3c| = 3(a + b + c)($$

7. Using properties of determinants Prove that

$$\begin{vmatrix} a+b+c & -c & -b \\ -c & a+b+c & -a \\ -b & -a & a+b+c \end{vmatrix} = 2(a+b)(b+c)(c+a)$$



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8. Solve  $\begin{vmatrix} x^2 - 1 & x^2 + 2x + 1 & 2x^2 + 3x + 1 \\ 2x^2 + x - 1 & 2x^2 + 5x - 3 & 4x^2 + 4x - 3 \\ 6x^2 - x - 2 & 6x^2 - 7x + 2 & 12x^2 - 5x - 2 \end{vmatrix} = 0$



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9. By using properties of determinants , show that :

$$\begin{bmatrix} 1 + a^2 - b^2 & 2ab & -2b \\ 2ab & 1 - a^2 + b^2 & 2a \\ 2b & -2a & 1 - a^2 - b^2 \end{bmatrix} = (1 + a^2 + b^2)^3$$



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**10.** Show that if  $x_1, x_2, x_3 \neq 0$

$$\begin{vmatrix} x_1 + a_1 b_1 & a_1 b_2 & a_1 b_3 \\ a_2 b_1 & x_2 + a_2 b_2 & a_2 b_3 \\ a_3 b_1 & a_3 b_2 & x_3 + a_3 b_3 \end{vmatrix} = x_1 x_2 x_3 \left( 1 + \frac{a_1 b_1}{x_1} + \frac{a_2 b_2}{x_2} + \frac{a_3 b_3}{x_3} \right)$$



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**11.** If  $A, B$  and  $C$  are the angles of a triangle, show that

$$| -1 + \cos B \cos C + \cos B \cos B \cos C + \cos A - 1 + \cos A \cos A - 1 + \cos A |$$



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**12.** If  $\begin{vmatrix} a^2 & b^2 & c^2 \\ (a+b)^2 & (b+1)^2 & (c+1)^2 \\ (a-1)^2 & (b-1)^2 & (c-1)^2 \end{vmatrix} = k(a-b)(b-c)(c-a)$  then the

value of  $k$  is a. 4 b. -2 c. -4 d. 2



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$$13. \text{ Prove that } \Delta = \begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ bc + 1^2 & ac + b^2 & ab + c^2 \end{vmatrix}$$
$$= 2(a - b)(b - c)(c - 1)$$



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$$14. \text{ Evaluate } \begin{vmatrix} .^x C_1 & .^x C_2 & .^x C_3 \\ .^y C_1 & .^y C_2 & .^y C_3 \\ .^z C_1 & .^z C_2 & .^z C_3 \end{vmatrix}$$



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$$15. \text{ if } \Delta_r = \begin{vmatrix} 2^{r-1} & 2 \times 3^{r-1} & 4 \times 5^{r-1} \\ \alpha & \beta & \gamma \\ 2^n - 1 & 3^n - 1 & 5^n - 1 \end{vmatrix}$$

then find the value of  $\sum_{r=1}^n \Delta_r$ .



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16.

Prove

that

$$|1 + a11111 + b11111 + c11111 + d| = abcd \left( a + \frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d} \right).$$

Hence find the value of the determinant if  $a, b, c, d$  are the roots of the equation  $px^4 + qx^3 + rx^2 + sx + t = 0$ .



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17. Prove that  $\begin{vmatrix} 1 & ab & \frac{1}{a} + \frac{1}{b} \\ 1 & bc & \frac{1}{b} + \frac{1}{c} \\ 1 & ca & \frac{1}{c} + \frac{1}{a} \end{vmatrix} = 0$



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18. Prove the identities:  $|b^2 + c^2abacbac^2 + a^2bacba^2 + b^2| = 4a^2b^2c^2$



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19. Show that  $\begin{vmatrix} a & b - c & c + b \\ a + c & b & c - a \\ a - b & b + a & c \end{vmatrix} = (a + b + c)(a^2 + b^2 + c^2)$



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## Exercise 12.4

1. If  $x_1, x_2, x_3$  as well as  $y_1, y_2, y_3$  are in G.P. with same common ratio, then prove that the points  $(x_1, y_1), (x_2, y_2),$  and  $(x_3, y_3)$  are collinear.



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2. If lines  $px + qy + r = 0, qx + ry + p = 0$  and  $rx + py + q = 0$  are concurrent, then prove that  $p + q + r = 0$  (where  $p, q, r$  are distinct).



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3.

if

$$(x_1, x_2)^2 + (y_1 - y_2)^2 = a^2, (x_2 - x_3)^2 + (y_2 - y_3)^2 = b^2 (x_3 - x_1)^2 + (y_3 - y_1)^2 = c^2$$

where a,b,c are positive then prove that

$$4 \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix} = (a + b + c)(b + c - a)(c + a - b)(a + b - c)$$



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4. it is known that the equation of hyperbola and that of its pair of asymptotes differ by constant . If equation of hyperbola is  $x^2 + 4xy + 3y^2 - 4x + 2y + 1 = 0$  then find the equation of its pair of asymptotes.



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Exercise 12.5

1.

Prove

that

$$|(b+x)(c+x)(v+x)(a+x)(a+x)(b+x)(b+y)(c+y)(c+x)(a+t)|$$



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$$2. \Delta = \begin{vmatrix} 1 + a^2 + a^4 & 1 + ab + a^2b^2 & 1 + ac + a^2c^2 \\ 1 + ab + a^2b^2 & 1 + b^2 + b^4 & 1 + bc + b^2c^2 \\ 1 + ac + a^2c^2 & 1 + bc + b^2c^2 & 1 + c^2c^4 \end{vmatrix} \text{ is equal to}$$



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3.

Prove

that

$$|2\alpha + \beta + \gamma + \delta\alpha\beta + \gamma\delta\alpha + \beta + \gamma + \delta| 2(\alpha + \beta)(\gamma + \delta)\alpha\beta(\gamma + \delta) + \gamma\delta(\alpha + \beta)(\gamma + \delta)$$



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4. For all values of  $A, B, C$  and  $P, Q, R$  show that

$$|\cos(A - P)\cos(A - Q)\cos(A - R)\cos(B - P)\cos(B - Q)\cos(B - R)\cos(C - P)\cos(C - Q)\cos(C - R)|$$



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5. Show that:  $|b^2 + c^2abacbac^2 + a^2bacba^2 + b^2| = 4a^2b^2c^2$



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6. Express  $= |2bc - a^2c^2b^2c^22ca - b^2a^2b62a^22ab - c^2|$  as square of a determinant of hence evaluate if.



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## Exercise 12.6

1. Let  $f(x) = \begin{vmatrix} \cos(x + x^2) & \sin(x + x^2) & -\cos(x + x^2) \\ \sin(x - x^2) & \cos(x - x^2) & \sin(x - x^2) \\ \sin 2x & 0 & \sin(2x^2) \end{vmatrix}$ .

Find the value of  $f'(0)$ .



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2. If  $f(x)$ ,  $g(x)$  and  $h(x)$  are three polynomial of degree 2, then prove that  $\varphi(x) = |f(x)g(x)h(x)f'(x)g'(xh'(x))f''(x)g''(xh''(x))|$  is a constant polynomial.



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3. If  $g(x) = \frac{f(x)}{(x-a)(x-b)(x-c)}$ , where  $f(x)$  is a polynomial of degree  $< 3$ , then prove that

$$\frac{dg(x)}{dx} = \left| 1af(a)(x-a)^{-2} 1bf(b)(x-b)^{-2} 1cf(c)(x-c)^{-2} \right| + \left| a^2a1b^2b1c \right|$$



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4. If  $f(x) = \begin{vmatrix} \cos(x+\alpha) & \cos(x+\beta) & \cos(x+\gamma) \\ \sin(x+\alpha) & \sin(x+\beta) & \sin(x+\gamma) \\ \sin(\beta-\gamma) & \sin(\gamma-\alpha) & \sin(\alpha-\beta) \end{vmatrix}$  and

$$f(0) = 2 \text{ then find the value of } \sum_{r=1}^{30} |f(r)|.$$



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$$5. f(x) = \begin{vmatrix} \cos x & x & 1 \\ 2 \sin x & x^2 & 2x \\ \tan x & x & 1 \end{vmatrix} \text{ then find the value of } \lim_{x \rightarrow 0} \frac{f(x)}{x}$$

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## Exercise 12.7

1. Find the following system of equations is consistent,  
 $(a + 1)^3x + (a + 2)^3y = (a + 3)^3$     $(a + 1)x + (a + 2)y = a + 3$  +1,  
then find the value of  $a$ .

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2. Solve the system of the equations:  $ax + by + cz = d$   
 $a^2x + b^2y + c^2z = d^2$     $a^3x + b^3y + c^3z = d^3$  Will the solution always exist and be unique?

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3. consider the system of equations : Itbr.  $3x - y + 4z = 3$

$$x + 2y - 3z = -2$$

$$6x + 5y + \lambda z = -3$$

Prove that system of equation has at least one solution for all real values of  $\lambda$ . also prove that infinite solutions of the system of equations satisfy

$$\frac{7x - 4}{-5} = \frac{7y + 9}{13} = z$$



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4. If the equation

$2x + 3y + 1 = 0, 3x + y - 2 = 0, \text{ and } ax + 2y - b = 0$  are consistent, then prove that  $a - b = 2$ .



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5. if  $x, y$  and  $z$  are not all zero and connected by the equations

$$a_1x + b_1y + c_1z = 0, a_2x + b_2y + c_2z = 0$$

and

$(p_1 + \lambda q_1)x + (p_2 + \lambda q_2)y + (p_3 + \lambda q_3)z = 0$  show that

$$\lambda = - \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ p_1 & p_2 & p_3 \end{vmatrix} \div \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ q_1 & q_2 & q_3 \end{vmatrix}$$



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## Exercise (Single)

1. if  $\theta \in R$  then maximum value of  $\Delta = \begin{vmatrix} 1 & 1 & 1 \\ 1 & 1 + \sin \theta & 1 \\ 1 & 1 & 1 + \cos \theta \end{vmatrix}$  is

A.  $\sqrt{3}/2$ )

B.  $1/2$

C.  $1/\sqrt{2}$

D. None of these

Answer: B



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2. If  $p + q + r = a + b + c = 0$ , then the determinant  $\begin{vmatrix} pa & qb & rc \\ qc & ra & pb \\ rb & pc & qa \end{vmatrix}$  equals

- A. 0
- B.  $pa + qb + rc$
- C. 1
- D. none of these

**Answer: A**



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3. If  $\alpha, \beta, \gamma$  are the roots of  $px^2 + qx^2 + r = 0$ , then the value of the determinant  $|\alpha\beta\beta\gamma\gamma\alpha\beta\gamma\gamma\alpha\alpha\beta\gamma\alpha\alpha\beta\beta\gamma|$  is p b. q c. 0 d. r

- A. p
- B. q
- C. 0

D. r

**Answer: C**



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4. If  $f(x) = a = bx + cx^2$  and  $\alpha, \beta, \gamma$  are the roots of the equation  $x^3 = 1$ , then  $|abcbcacab|$  is equal to  $f(\alpha) + f(\beta) + f(\gamma)$   
 $f(\alpha)f(\beta) + f(\beta)f(\gamma) + f(\gamma)f(\alpha)$   $f(\alpha)f(\beta)f(\gamma) - f(\alpha)f(\beta)f(\gamma)$

A.  $f(\alpha) + f(\beta) + f(\gamma)$

B.  $f(\alpha)f(\beta) + f(\beta)f(\gamma) + f(\gamma)f(\alpha)$

C.  $f(\alpha)f(\beta)f(\gamma)$

D.  $-f(\alpha)f(\beta)f(\gamma)$

**Answer: D**



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5. If  $[.]$  denotes the greatest integer less than or equal to the real number under consideration, and  $-1 \leq x < 0, 0 \leq y < 1, 1 \leq z < 2$ , then the

value of the determinant  $\begin{vmatrix} [x] + 1 & [y] & [z] \\ [x] & [y] + 1 & [z] \\ [x] & [y] & [z] + 1 \end{vmatrix}$  is

- a.  $[x]$
- b.  $[y]$
- c.  $[z]$
- d. none of these

A.  $[x]$

B.  $[y]$

C.  $[z]$

D. none of these

**Answer: C**



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6. if  $a = \cos \theta + i \sin \theta$ ,  $b = \cos 2\theta - i \sin 2\theta$ ,  $c = \cos 3\theta + i \sin 3\theta$  and if

$$\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix} = 0 \text{ then}$$

- A.  $\theta = 2k\pi, k \in \mathbb{Z}$
- B.  $\theta = (2k+1)\pi, k \in \mathbb{Z}$
- C.  $\theta = (4k+1)\pi, k \in \mathbb{Z}$
- D. none of these

**Answer: A**



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7. If  $\begin{vmatrix} x^n & x^{n+2} & x^{n+3} \\ y^n & y^{n+2} & y^{n+3} \\ z^n & z^{n+2} & z^{n+3} \end{vmatrix} = (x-y)(y-z)(z-x) \left( \frac{1}{x} + \frac{1}{y} + \frac{1}{z} \right)$ , then

$n$  equals

A. 1

B. -1

C. 2

D. -2

**Answer: B**



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8. If the determinant  $\begin{vmatrix} \cos 2x & \sin^2 x & \cos 4x \\ \sin^2 x & \cos 2x & \cos^2 x \\ \cos 4x & \cos^2 x & \cos 2x \end{vmatrix}$  is expanded in powers of  $\sin x$ , then the constant term is

A. 1

B. 0

C. -1

D. 2

**Answer: C**



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**9. about to only mathematics**

A. -2

B. -4

C. 0

D. -8

**Answer: B**



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**10.** If  $A + B + C = \pi$  and  $e^{i\theta} = \cos \theta + i \sin \theta$  and

$$z = \begin{vmatrix} e^{2iA} & e^{-iC} & e^{-iB} \\ e^{-iC} & e^{2iB} & e^{-iA} \\ e^{-iB} & e^{-iA} & e^{2iC} \end{vmatrix}, \text{ then}$$

A. 1

B. -1

C. -2

**Answer: D****Watch Video Solution**

11. If  $a, b, c$  are different, then the value of  $x$  for which

$$\begin{vmatrix} 0 & x^2 - a & x^3 - b \\ x^2 + a & 0 & x^2 + c \\ x^4 + b & x - c & 0 \end{vmatrix} = 0 \text{ is}$$

A. a

B. c

C. b

D. 0

**Answer: D****Watch Video Solution**

12. If the value of determinant  $|(a,1,1),(1,b,1)(1,1,c)|$  is positive , then

- A.  $abc > 1$
- B.  $abc > -8$
- C.  $abc > -8$
- D.  $abc > -2$

**Answer: B**



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13. if  $A_1, B_1, C_1 \dots \dots$  are respectively the cofactors of the elements  $a_1, b_1, c_1 \dots \dots$  of the determinant

$$\Delta = \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}, \Delta \neq 0 \text{ then the value of } \begin{vmatrix} B_2 & C_2 \\ B_3 & C_3 \end{vmatrix} \text{ is equal to}$$

- A.  $a_1^2 \Delta$
- B.  $a_1 \Delta$

C.  $a_1 \Delta^2$

D.  $a_1^2 \Delta^2$

**Answer: B**



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14. If  $a, b, c, d, e, \text{ and } f$  are in G.P. then the value of  $|a^2d^2xb^2e^2yc^2f^2z|$

depends on  $x$  and  $y$  b.  $x$  and  $z$  c.  $y$  and  $z$  d. independent of  $x, y, \text{ and } z$

A.  $x$  and  $y$

B.  $x$  and  $z$

C.  $y$  and  $z$

D. independent of  $x, y$  and  $z$

**Answer: D**



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**15.** Let  $x < 1$ , then value of  $|x^2 + 22x + 112x + 1x + 21331|$  is a. none-negative b. none-positive c. negative d. positive

A. non-negative

B. non-positive

C. negative

D. positive

**Answer: C**



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**16.** The value of  $|-1213 + 2\sqrt{22} + 2\sqrt{213} - 2\sqrt{22} - 2\sqrt{21}|$  is equal to

a. zero b.  $-16\sqrt{2}$  c.  $-8\sqrt{2}$  d. none of these

A. 0

B.  $-16\sqrt{2}$

C.  $-8\sqrt{2}$

D. none of these

**Answer: B**



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17. Let  $\{D_1, D_2, D_3, D_n\}$  be the set of third order determinant that can be made with the distinct non-zero real numbers  $a_1, a_2, a_q$ . Then

a.  $\sum_{i=1}^n D_i = 1$  b.  $\sum_{i=1}^n D_i = 0$  c.  $D_i = D_j, \forall i, j$  d. none of these

A.  $\sum_{i=1}^n D_i = 1$

B.  $\sum_{i=1}^n D_i = 0$

C.  $D_i D_j, \forall I, j$

D. None of these

**Answer: B**



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**18.** if  $w$  is a complex cube root to unity then value of

$$\Delta = \begin{vmatrix} a_1 + b_1w & a_1w^2 + b_1 & c_1 + b_1\bar{w} \\ a_2 + b_2w & a_2w^2 + b_2 & c_2 + b_2\bar{w} \\ a_3 + b_3w & a_3w^2 + b_3 & c_3 + b_3\bar{w} \end{vmatrix} \text{ is}$$

A. 0

B. -1

C. 2

D. none of these

**Answer:** A



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**19.** If  $a + b + c = 0$ , one root of  $|a - xcbcb - xabac - x| = 0$  is  $x = 1$

b.  $x = 2$  c.  $x = a^2 + b^2 + c^2$  d.  $x = 0$

A.  $x = 1$

B.  $x = 2$

C.  $x = a^2 + b^2 + c^2$

D.  $x = 0$

**Answer: D**



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20. If  $x, y, z$  are in A.P., then the value of the determinant are in A.P., then

the value of the determinant

$|a + 2a + 3a + 2xa + 3a + 4a + 2ya + 4a + 5a + 2z|$  is a. 1 b. 0 c. 2a d.

a

A. 1

B. 0

C. 2a

D. a

**Answer: B**



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21. If  $a_1, a_2, a_3, \dots, a_n, \dots$  are in G.P., then the determinant  $\Delta =$

$$\begin{vmatrix} \log a_n & \log a_{n+1} & \log_{n+2} \\ \log a_{n+3} & \log a_{n+4} & \log_{n+5} \\ \log a_{n+6} & \log a_{n+7} & \log_{n+8} \end{vmatrix} \text{ is equal to}$$

A. 1

B. 0

C.  $2a$

D.  $a$

**Answer: B**



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22. Value of  $|x + yzzxy + zxyyz + x|$ , where  $x, y, z$  are nonzero real numbers, is equal to  
a.  $xyz$  b.  $2xyz$  c.  $3xyz$  d.  $4xyz$

A.  $xyz$

B.  $2xyz$

C.  $3xyz$

D.  $4xyz$

**Answer: D**



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**23.** Which of the following is not the root of the equation

$$|x - 6 - 12 - 3x - 3 - 32x + 2| = 0?$$

- a. 2 b. 0 c. 1 d. -3

A. 2

B. 0

C. 1

D. -3

**Answer: B**



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24. The value of the determinant  $|kak^2 + a^2 1 kbk^2 + b^2 1 kck^2 + c^2 1|$  is

$$k(a+b)(b+c)(c+a) - kabc(a^2 + b^2 + c^2) - k(a-b)(b-c)(c-a)$$

$$k(a+b-c)(b+c-a)(c+a-b)$$

A.  $k(a+b)(b+c)(c+a)$

B.  $kabc(a^2 + b^2 + c^2)$

C.  $k(a-b)(b-c)(c-a)$

D.  $k(a+b-c)(b+c-a)(c+a-b)$

**Answer: C**



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25. If  $\begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^3 & b^3 & c^3 \end{vmatrix} = (a-b)(b-c)(c-a)(a+b+c)$

where  $a, b, c$  are all different, then the determinant

$$\begin{vmatrix} 1 & 1 & 1 \\ (x-a)^2 & (x-b)^2 & (x-c)^2 \\ (x-b)(x-c) & (x-c)(x-a) & (x-a)(x-b) \end{vmatrix} \text{ vanishes when}$$

A.  $a + b + c = 0$

B.  $x = \frac{1}{3}(a + b + c)$

C.  $x = \frac{1}{2}(a + b + c)$

D.  $x = a + b + c$

**Answer: B**



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**26.**

If

$f'(x) = |mxm - pmx + p \cap + pn - pmx + 2nmx + 2n + pmx + 2n -$ , then  $y = f(x)$  represents a straight line parallel to x-axis a straight line parallel to y-axis parabola a straight line with negative slope

A. a straight line parallel to x-axis

B. a straight line parallel to y-axis

C. parabola

D. a straight line with negative slope

**Answer: B**



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27. If  $|x3636x6x3| = |2x7x7272x| = |45x5x4x45| = 0$ , then  $x$  is equal to  
a. 0 b. -9 c. 3 d. none of these

A. 0

B. -9

C. 3

D. none of these

**Answer: B**



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28. If  $\begin{vmatrix} x^n & x^{n+2} & x^{2n} \\ 1 & x^a & a \\ x^{n+5} & x^{a+6} & x^{2n+5} \end{vmatrix} = 0$ ,  $\forall x \in R$ , where  $n \in N$ , then value of

$a$  is

- (a)  $n$
- (b)  $n - 1$
- (c)  $n + 1$
- (d) none of these

A.  $n$

B.  $n-1$

C.  $n+1$

D. none of these

**Answer: C**



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29. for the equation  $\begin{vmatrix} 1 & x & x^2 \\ x^2 & 1 & x \\ x & x^2 & 6 \end{vmatrix} = 0$

- A. There are exactly two distinct roots
- B. there is one pair of equation real roots
- C. There are three pairs of equal roots
- D. Modulus of each root is 2

**Answer: C**



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30. If  $a^2 + b^2 + c^2 = -2$  and  $f(x) = |a + a^2x(1 + b^2)x(1 + c^2)x(1 + a^2)x| + b^2x(1 + c^2)x(1 + a^2)x(1 + b^2)x$ , then  $f(x)$  is a polynomial of degree

- a. 0
- b. 1
- c. 2
- d. 3

A. 0

B. 1

C. 2

D. 3

**Answer: C**



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31. The value of the determinant  $\begin{vmatrix} 1 & 1 & 1 \\ .^m C_1 & .^{m+1} C_1 & .^{m+2} C_1 \\ .^m C_2 & .^{m+1} C_2 & .^{m+2} C_2 \end{vmatrix}$  is equal to

A. 1

B. -1

C. 0

D. none of these

**Answer: A**



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32.

The value of determinant

$$\wedge nC_{r-1}^n C_r(r+1)^{n+2} C_{r+1}^n C_r^n C_{r+1}(r+2)^{n+2} C_{r+2}^n C_{r+1}^n C_{r+2}(r+3)^{n+2} C$$

is  $n^2 + n - 2$  b. 0 c.  $\wedge n + 3C_{r+3}$  d.  $\wedge nC_{r-1} + ^n C_r + ^n C_{r+1}$

A.  $n^2 + n - 1$ )

B. 0

C.  $.^{n+3} C_{r+3}$

D.  $.^n C_{r-1} + ^n C_r + ^n C_{r+1}$

**Answer: B**



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33. if  $f(x) = \begin{vmatrix} x & a & a \\ a & x & a \\ a & a & x \end{vmatrix} = 0$  then

A.  $f(x) = 0$  and  $f(x) = 0$  has one common root

B.  $f(x) = 0$  and  $f(x) = 0$  has one common root

C. sum of roots of  $f(x) = 0$  is  $-3a$

D. none of these

**Answer: B**



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34. If  $x \neq y \neq z$  and  $\begin{vmatrix} x & x^2 & 1+x^3 \\ y & y^2 & 1+y^3 \\ z & z^2 & 1+z^3 \end{vmatrix} = 0$ , then  $xyz =$

A. 1

B. 2

C. -1

D. -2

**Answer: C**



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35. if  $x \neq 0, y \neq 0, z \neq 0$  and  $\begin{vmatrix} 1+x & 1 & 1 \\ 1+y & 1+2y & 1 \\ 1+z & 1+z & 1+3z \end{vmatrix} = 0$  then

$x^{-1} + y^{-1} + z^{-1}$  is equal to

A. -1

B. -2

C. -3

D. none of these

**Answer: C**



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36. if  $a_1b_1c_1, a_2b_2c_2$  and  $a_3b_3c_3$  are three-digit even natural numbers

and  $\Delta = \begin{vmatrix} c_1 & a_1 & b_1 \\ c_2 & a_2 & b_2 \\ c_3 & a_3 & b_3 \end{vmatrix}$  then  $\Delta$  is

A. divisible by 2 but not necessarily by 4

B. divisible by 4 but not necessarily by 8

C. divisible by 8

D. none of these

**Answer: A**



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37. if  $\begin{vmatrix} b+c & c+a & a+b \\ a+b & b+c & c+a \\ c+a & a+b & b+c \end{vmatrix} = k \begin{vmatrix} a & b & c \\ c & a & b \\ b & c & a \end{vmatrix}$  then the value of

k is

A. 1

B. 2

C. 3

D. 4

**Answer: B**



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38. suppose  $D = \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}$  and

$$D' = \begin{vmatrix} a_1 + pb_1 & b_1 + qc_1 & c_1 + ra_1 \\ a_2 + pb_2 & b_2 + qc_2 & c_2 + ra_2 \\ a_3 + pb_3 & b_3 + qc_3 & c_3 + ra_3 \end{vmatrix}. \text{ Then}$$

A.  $D' = D$

B.  $D' = D(1 - pqr)$

C.  $D = D(1 + p + q + r)$

D.  $D' = D(1 + pqr)$

**Answer: D**



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39. The value of the determinant  $\begin{vmatrix} \log_a\left(\frac{x}{y}\right) & \log_a\left(\frac{y}{z}\right) & \log_a\left(\frac{z}{x}\right) \\ \log_b\left(\frac{y}{z}\right) & \log_b\left(\frac{z}{x}\right) & \log_b\left(\frac{x}{y}\right) \\ \log_c\left(\frac{z}{x}\right) & \log_c\left(\frac{x}{y}\right) & \log_c\left(\frac{y}{z}\right) \end{vmatrix}$

A. 1

B. -1

C. 0

D.  $\frac{1}{6} \log_a xyz$

**Answer: C**



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**40.** If  $a > 0, b > 0, c > 0$  are respectively the pth, qth, rth terms of a G.P., then the value of the determinant

$$\begin{vmatrix} \log a & p & 1 \\ \log b & q & 1 \\ \log c & r & 1 \end{vmatrix}, \text{ is}$$

A. 0

B.  $\log(abc)$

C.  $-(p + q + r)$

D. none of these

**Answer: A**



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41. If  $a > 0$  and discriminant of  $ax^2 + 2bx + c$  is negative, then  
= abax + cbx + cax + x + c0 is +ve b.  $(ac - b)^2(ax^2 + 2bx + c)$  c.  
- ve d. 0

A. +ve

B.  $(ac - b)^2(ax^2 + 2bx + c)$

C. - ve

D. 0

**Answer: C**



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42. The number of distinct real roots of  $\begin{vmatrix} \sin x & \cos x & \cos x \\ \cos x & \sin x & \cos x \\ \cos x & \cos x & \sin x \end{vmatrix} = 0$  in the  
interval  $-\frac{\pi}{4} \leq x \leq t\frac{\pi}{4}$  is

A. 0

B. 2

C. 1

D. 3

**Answer: C**



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**43.**

if

$$D_k = \begin{vmatrix} 1 & n & n \\ 2k & n^2 + n + 1 & n^2 + n \\ 2k - 1 & n^2 & n^2 + n + 1 \end{vmatrix} \text{ and } \sum_{k=1}^n D_k = 56$$

then  $n$  equals

A. 4

B. 6

C. 8

D. 7

**Answer: D**



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**44.** the value of  $\sum_{r=2}^n (-2)^r \begin{vmatrix} n-2 C_{r-2} & n-2 C_{r-1} & n-2 C_r \\ -3 & 1 & 1 \\ 2 & -1 & 0 \end{vmatrix}$  ( $n > 2$ )

A.  $2n - 1 + (-1)^n$

B.  $2n + 1 + (-1)^{n-1}$

C.  $2n - 3 + (-1)^n$

D. none of these

**Answer: A**



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**45.** if  $\Delta = \begin{vmatrix} 3 & 4 & 5 & x \\ 4 & 5 & 6 & y \\ 5 & 6 & 7 & z \\ x & y & z & 0 \end{vmatrix} = 0$  then

A.  $x, y, z$  are in A.P.

B.  $x, y, z$  are in G.P

C.  $x, y, z$  are in H.P

D. none of these

**Answer: A**



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46. Roots of the equations  $\begin{vmatrix} x & m & n & 1 \\ a & x & n & 1 \\ a & b & x & 1 \\ a & b & c & 1 \end{vmatrix} = 0$  are

A. independent of  $m$  and  $n$

B. independent of  $a,b$  and  $c$

C. depend on  $m,n$  and  $a,b,c$

D. inedependent of  $m,n$  and  $a,b,c$

**Answer: A**



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47. If  $x, y, z$  are different from zero and

$\Delta = ab - yc - za - xbc - za - xb - yc = 0$ , then the value of the

expression  $\frac{a}{x} + \frac{b}{y} + \frac{c}{z}$  is  
a. 0 b. -1 c. 1 d. 2

A. 0

B. -1

C. 1

D. 2

Answer: D



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48. about to only mathematics

A. 0

B. 3

C. 6

D. 12

**Answer: B**



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49. In triangle ABC, if

$$\begin{vmatrix} 1 & 1 & 1 \\ \cot\left(\frac{A}{2}\right) & \cot\left(\frac{B}{2}\right) & \cot\left(\frac{C}{2}\right) \\ \tan\left(\frac{B}{2}\right) + \tan\left(\frac{C}{2}\right) & \tan\left(\frac{C}{2}\right) + \tan\left(\frac{A}{2}\right) & \tan\left(\frac{A}{2}\right) + \tan\left(\frac{B}{2}\right) \end{vmatrix} \text{ then}$$

the triangle must be (A) Equilateral (B) Isosceles (C) Right Angle (D) none

of these

A. equilateral

B. isosceles

C. obtuse angled

D. none of these

**Answer: B**



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50. If  $\begin{vmatrix} a & b - c & b + c \\ a + c & b & c - a \\ a - b & a + b & c \end{vmatrix} = 0$  then the line  $ax + by + c = 0$  passes

through the fixed point which is

A. (1, 2)

B. (1, 1)

C. (-2, 1)

D. (1, 0)

**Answer: B**



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51. The determinant  $\begin{vmatrix} y^2 & -xy & x^2 \\ a & b & c \\ a' & b' & c' \end{vmatrix}$  is equal to

- A.  $\begin{vmatrix} bx + ay & cx + by \\ b'x + a'y & c'x + b'y \end{vmatrix}$
- B.  $\begin{vmatrix} ax + by & bx + cy \\ a'x + b'y & b'x + c'y \end{vmatrix}$
- C.  $\begin{vmatrix} bx + cy & ax + by \\ b'x + c'y & a'x + b'y \end{vmatrix}$
- D.  $\begin{vmatrix} ax + by & bc + cy \\ a'x + b'y & b'x + c'y \end{vmatrix}$

**Answer: D**



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52. Let  $\vec{a}_r = x_r \hat{i} + y_r \hat{j} + z_r \hat{k}$ ,  $r = 1, 2, 3$  three mutually perpendicular

unit vectors then the value of  $\begin{vmatrix} x_1 & -x_2 & x_3 \\ y_1 & y_2 & y_3 \\ z_1 & z_2 & z_3 \end{vmatrix}$  is equal to

- A. zero
- B.  $\pm 1$
- C.  $\pm 2$
- D. none of these

**Answer: B**



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**53.** Let

$$\begin{vmatrix} y^5 z^6(z^3 - y^3) & x^4 z^6(x^3 - z^3) & x^4 y^5(y^3 - x^3) \\ y^2 z^3(y^6 - z^6) & x z^3(z^6 - x^6) & x y^2(x^6 - y^6) \\ y^2 \wedge (3)(z^3 - y^3) & x z^3(x^3 - z^3) & x y^2(y^3 - x^3) \end{vmatrix} \text{ and } \Delta_2 = \begin{vmatrix} x \\ x^4 \\ x^7 \end{vmatrix}$$

. Then  $\Delta_1 \Delta_2$  is equal to

A.  $\Delta_2^6$

B.  $\Delta_2^4$

C.  $\Delta_2^3$

D.  $\Delta_2^2$

**Answer: C**



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**54. the value of the determinant**

$$\begin{vmatrix} (a_1 - b_1)^2 & (a_1 - b_2)^2 & (a_1 - b_3)^2 & (a_1 - b_4)^2 \\ (a_2 - b_1)^2 & (a_2 - b_2)^2 & (a_2 - b_3)^2 & (a_3 - b_4)^2 \\ (a_3 - b_1)^2 & (a_3 - b_2)^2 & (a_3 - b_3)^2 & (a_3 - b_4)^2 \\ (a_4 - b_1)^2 & (a_4 - b_2)^2 & (a_4 - b_3)^2 & (a_4 - b_4)^2 \end{vmatrix} \text{ is}$$

- A. dependant on  $a_i, i = 1, 2, 3, 4$
- B. dependant on  $b_i, i = 1, 2, 3, 4$
- C. dependant on  $a_{ij}, b_i, i = 1, 2, 3, 4$
- D. 0

**Answer: D**



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55. if  $\Delta(x) = \begin{vmatrix} \tan x & \tan(x + h) & \tan(x + 2h) \\ \tan(x + 2h) & \tan x & \tan(x + h) \\ \tan(x + h) & \tan(x + 2h) & \tan x \end{vmatrix}$ , then

The value of  $\lim_{h \rightarrow 0} \cdot \frac{\Delta(\pi/3)}{\sqrt{3}h^2}$  is

B. 81

C. 64

D. 36

**Answer: A**



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56. Value of  $\begin{vmatrix} 1+x_1 & 1+x_1x & 1+x_1x^2 \\ 1+x_2 & 1+x_2x & 1+x_2x^2 \\ 1+x_3 & 1+x_3x & 1+x_3x^2 \end{vmatrix}$  depends upon

A.  $x$  only

B.  $x_1$  only

C.  $x_2$  only

D. none of these

**Answer: D**



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57. If  $\begin{vmatrix} a^2 + \lambda^2 & ab + c\lambda & ca - b\lambda \\ ab - c\lambda & b^2 + \lambda^2 & bc + a \\ ca + b\lambda & bc - a\lambda & c^2 + \lambda^2 \end{vmatrix}$

$$\begin{vmatrix} \lambda & c & -b \\ -c & \lambda & a \\ b & -a & \lambda \end{vmatrix} = (1 + a^2 + b^2 + c^2)^3, \text{ then the value of } \lambda \text{ is}$$

a. 8

b. 27

c. 1

d. -1

A. 8

B. 27

C. 1

D. -1

**Answer: C**



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58. Let  $\begin{vmatrix} x & 2 & x \\ x^2 & x & 6 \\ x & x & 6 \end{vmatrix} = ax^4 + bx^3 + cx^2 + dx + e$  Then, the value of  $5a + 4b + 3c + 2d + e$  is equal to

A. zero

B. -16

C. 16

D. -11

**Answer: D**



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59.  $\Delta_1 = \begin{vmatrix} x & b & b \\ a & x & b \\ a & a & x \end{vmatrix}$  and  $\Delta_2 = \begin{vmatrix} x & b \\ a & x \end{vmatrix}$  are the given determinants  
then

A.  $\Delta_1 = 3(\Delta_2)^2$

B.  $\frac{d}{dx}(\Delta_1) = 3\Delta_2$

C.  $\frac{d}{dx}(\Delta_1) = 3(\Delta_2)^2$

D.  $\Delta_1 = 3\Delta_2^{3/2}$

**Answer: B**



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60. if  $y = \sin mx$ , then the value of the determinant

$$\begin{vmatrix} y & y_1 & y_2 \\ y_3 & y_4 & y_5 \\ y_6 & y_7 & y_8 \end{vmatrix} \quad \text{Where } y_n = \frac{d^n y}{dx^n} \text{ is}$$

A.  $m^9$

B.  $m^2$

C.  $m^3$

D. 0

**Answer: D**



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61. Let  $f(x) = \begin{vmatrix} 2\cos^2 x & \sin 2x & -\sin x \\ \sin 2x & 2\sin^2 x & \cos x \\ \sin x & -\cos x & 0 \end{vmatrix}$ , then the value of

$$\int_0^{\pi/2} \{f(x) + f'(x)\} dx$$
 is

A.  $\pi$

B.  $\pi/2$

C.  $2\pi$

D.  $3\pi/2$

**Answer: A**



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62.  $a, b, c$  are distinct real numbers not equal to one. If  $ax + y + z = 0, x + by + z = 0$ , and  $x + y + cz = 0$  have nontrivial solution, then the value of  $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c}$  is equal to  
a. 1 b. -1  
c. zero d. none of these

A.  $-1$

B.  $1$

C. zero

D. none of these

**Answer: B**



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**63.** If the system of linear equation

$x + y + z = 6$ ,  $x + 2y + 3z = 14$ , and  $2x + 5y + \lambda z = \mu(\lambda, \mu R)$  has a unique solution, then a.  $\lambda = 8$  b.  $\lambda = 8, \mu = 36$  c.  $\lambda = 8, \mu \neq 36$  d. none of these

A.  $\lambda \neq 8$

B.  $\lambda = 8, \mu \neq 36$

C.  $\lambda = 8, \mu = 36$

D. none of these

**Answer: A**



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64. If  $\alpha, \beta, \gamma$  are the angles of a triangle and system of equations  
 $\cos(\alpha - \beta)x + \cos(\beta - \gamma)y + \cos(\gamma - \alpha)z = 0$   
 $\cos(\alpha + \beta)x + \cos(\beta + \gamma)y + \cos(\gamma + \alpha)z = 0$   
 $\sin(\alpha + \beta)x + \sin(\beta + \gamma)y + \sin(\gamma + \alpha)z = 0$  has non-trivial solutions,  
then triangle is necessarily a. equilateral b. isosceles c. right angled d.  
acute angled

A. equiliateral

B. isosocoles

C. right angled

D. acute angled

**Answer: B**



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**65.**

Given

$a = x/(y - z)$ ,  $b = y/(z - x)$ , and  $c = z/(x - y)$ , where  $x, y, z$  and  $z$  are not all zero, then the value of  $ab + bc + ca$  is  
a. 0 b. 1 c. -1 d. none of these

A. 0

B. 1

C. -1

D. none of these

**Answer: C**



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**66.** If  $pqr \neq 0$  and the system of equation  $(p + a)x + by - cz = 0$ ,  
 $ax + (q + b)y + cz = 0$ ,  $ac + by + (r + c)z = 0$  has nontrivial solution,  
then value of  $\frac{1}{p} + \frac{b}{q} + \frac{c}{r}$  is  
a. -1 b. 0 c. 0 d. -2

A. -1

B. 0

C. 1

D. 2

**Answer: A**



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**67.** The value of  $|\alpha|$  for which the system of equation

$$\alpha x + y + z = \alpha - 1$$

$$x + \alpha y + z = \alpha - 1$$

$$x + y + \alpha z = \alpha - 1$$

has no solution , is \_\_\_\_\_

A. either -2 or 1

B. -2

C. 1

D. not-2

**Answer: B**



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68. the set of equations  $\lambda x - y + (\cos \theta)z = 0$ ,  $3x + y + 2z = 0$  ,  
 $(\cos \theta)x+y+2z=0$  , $\theta \leq 0 < 2\pi$  has non-trivial solution (s)

- A. for no value of  $\lambda$  and 0
- B. for all values of  $\lambda$  and 0
- C. for all values of  $\lambda$  and only tow values of 0
- D. for only one value of  $\lambda$  and all values of 0

**Answer: A**



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**69.** If  $c < 1$  and the system of equations

$x + y - 1 = 0$ ,  $2x - y - c = 0$ , and  $bx + 3by - c = 0$  is consistent,

then the possible real values of  $b$  are  $b \left( -3\frac{3}{4} \right)$  b.  $b \left( -\frac{3}{2}, 4 \right)$  c.

$b \left( -\frac{3}{4}, 3 \right)$  d. none of these

A.  $b \in \left( -3\frac{3}{4} \right)$

B.  $b \in \left( -\frac{3}{2}, 4 \right)$

C.  $b \in \left( -\frac{3}{4}, 3 \right)$

D. none of these

**Answer: C**



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**70.** If  $a, b, c$  are in G.P. with common ratio  $r_1$  and  $\alpha, \beta, \gamma$  are in G.P. with

common ratio  $r_2$  and equations

$ax + \alpha y + z = 0$ ,  $bx + \beta y + z = 0$ ,  $cx + \gamma y + z = 0$  have only zero

solution, then which of the following is not true? a.  $a + b + c$  b.  $abc$  c. 1 d.

none of these

A.  $r_1 \neq 1$

B.  $r_2 \neq 1$

C.  $r_1 \neq r_2$

D. none of these

**Answer: D**



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71. The product of all values of  $t$ , for which the system of equations

$$(a - t)x + by + cz = 0, bx + (c - t)y + az = 0, cx + ay + (b - t)z = 0$$

has non-trivial solution, is | $a - c - b - cb - a - b - ac$ | (b) | $abcbcacab$ |

| $acaba$ | (d) | $aa + + c + + a + aa + b$ |

A.  $\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$

B.  $a + b + c$

C.  $a^2 + b^2 + c^2$

D. 1

**Answer: A**



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72. Let  $\lambda$  and  $\alpha$  be real. Then the numbers of intergral values  $\lambda$  for which the system of linear equations

$$\lambda x + (\sin \alpha)y + (\cos \alpha)z = 0$$

$$x + (\cos \alpha)y + (\sin \alpha)z = 0$$

$-x + (\sin \alpha)y - (\cos \alpha)z = 0$  has non-trivial solutions is

A. 0

B. 1

C. 2

D. 3

**Answer: D**



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### **Exercise (Multiple)**

1. Which of the following has / have value equal to zero ?

- A. 
$$\begin{vmatrix} 8 & 2 & 7 \\ 12 & 3 & 5 \\ 16 & 4 & 3 \end{vmatrix}$$
- B. 
$$\begin{vmatrix} 1/a & a^2 & bc \\ 1/b & b^2 & ac \\ 1/c & c^2 & ab \end{vmatrix}$$
- C. 
$$\begin{vmatrix} a+b & 2a+b & 3a+b \\ 2a+b & 3a+b & 4a+b \\ 4a+b & 5a+b & 6a+b \end{vmatrix}$$
- D. 
$$\begin{vmatrix} 2 & 43 & 6 \\ 7 & 35 & 4 \\ 3 & 17 & 2 \end{vmatrix}$$

**Answer: A::B::C**



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2. If  $f(\alpha, \beta) = \begin{vmatrix} \cos \alpha & -\sin \alpha & 1 \\ \sin \alpha & \cos \alpha & 1 \\ \cos(\alpha + \beta) & -\sin(\alpha + \beta) & 1 \end{vmatrix}$ , then

A.  $f(300,200) = f(400,200)$

B.  $f(200,400) = f(200,600)$

C.  $f(100,200) = f(200,200)$

D. none of these

**Answer: A::C**



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3. if  $f(0) = \begin{vmatrix} \sin 0 & \cos 0 & \sin 0 \\ \cos 0 & \sin 0 & \cos 0 \\ \cos 0 & \sin 0 & \sin 0 \end{vmatrix}$  then

A.  $f(0) = 0$  has exactly 2 real solutions in  $[0, \pi]$

B.  $f(0) = 0$  has exactly 3 real solutions in  $[0, \pi]$

C. range of function  $\frac{f(0)}{1 - \sin 20}$  is  $[-\sqrt{2}, \sqrt{2}]$

D. range of function  $\frac{f(0)}{\sin 20 - 1}$  is  $[-3, 3]$  is  $[-3, 3]$

**Answer: A::C**



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4. If  $f(x) = |ax^2 - 10ax - 1|$ , then  $f(2x) - f(x)$  is divisible by a

b. b c.c, d, e d. none of these

A. x

B. a

C.  $2a + 3x$

D.  $x^2$

**Answer: A::B::C**



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$$5. \Delta = \begin{vmatrix} 1 & 1+ac & 1+bc \\ 1 & 1+ad & 1+bd \\ 1 & 1+ae & 1+be \end{vmatrix} \text{ is independent of}$$

- A. a
- B. b
- C. c,d,e
- D. none of these

**Answer: A::B::C**



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$$6. \text{ if } \Delta = \begin{vmatrix} -x & a & b \\ b & -x & a \\ a & b & -x \end{vmatrix} \text{ then a factor of } \Delta \text{ is}$$

- A.  $a + b + x$
- B.  $x^2 - (a - b)x + a^2 + b^2 + ab$
- C.  $x^2 + (a + b)x + a^2 + b^2 - ab$

D.  $a + b - x$

**Answer: C::D**



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7. the determinant  $\Delta = \begin{vmatrix} a^2 + x & ab & ac \\ ab & b^2 + x & bc \\ ac & bc & c^2 + x \end{vmatrix}$  is divisible by

A.  $x$

B.  $x^2$

C.  $x^3$

D. none of these

**Answer: A::B**



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8.  $= |aa^2012a + b(a + b)012a + 3b|$  is divisible by a.  $a + b$  b.  $a + 2b$  c.  $2a + 3b$  d.  $a^2$

A.  $a + b$

B.  $a + 2b$

C.  $2a + 3b$

D.  $a^2$

**Answer: A::B**



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9. the roots of the equations  $\begin{vmatrix} .^x C_r & .^{n-1} C_r & .^{n-1} C_{r-1} \\ .^{x+1} C_r & .^n C_r & .^n C_{r-1} \\ .^{x+2} C_r & .^{n+1} C_r & .^{n+1} C_{r-1} \end{vmatrix} = 0$

A.  $x = n$

B.  $x = n + 1$

C.  $x = n - 1$

D.  $x = n - 2$

**Answer: A::C**



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10. If  $f(x) = \begin{vmatrix} 3 & 3x & 3x^2 + 2a^2 \\ 3x & 3x^2 + 2a^2 & 3x^3 + 6a^2x \\ 3x^2 + 2a^2 & 3x^3 + 6a^2x & 3x^4 + 12a^2x^2 + 2a^4 \end{vmatrix}$

then

A.  $f'(x)=0$

B.  $y=f(x)$  is a straight line parallel to x-axis

C.  $\int_0^2 f(x)dx = 32a^4$

D. none of these

**Answer: A::B**



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11. Let  $f(n) = \begin{vmatrix} n & n+1 & n+1 \\ .^n P_n & .^{n+1} P_{n+1} & .^{n+2} P_{n+2} \\ .^n C_n & .^{n+1} C_{n+1} & .^{n+2} C_{n+2} \end{vmatrix}$  where the symbols have their usual meanings .then f(n) is divisible by

A.  $n^2 + n + 1$

B.  $(n + 1)!$

C.  $n!$

D. none of these

**Answer: A::C**



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12. If  $\begin{vmatrix} a & b & a\alpha + b \\ b & c & b\alpha + c \\ a\alpha + b & b\alpha + c & 0 \end{vmatrix} = 0$ , prove that a,b,c, are in G.P. or  $\alpha$  is a

root of  $ax^2 + 2bx+c=0$

A. a,b,c are in A.P

B. a,b,c are in G.P.

C.  $\alpha$  is a root of the equation  $ax^2 + bx + c = 0$

D.  $(x - \alpha)$  is a factor of  $ax^2 + 2bx + c$

**Answer: B::D**



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13. if  $\begin{vmatrix} \sin x & \sin y & \sin z \\ \cos x & \cos y & \cos z \\ \cos^3 x & \cos^3 y & \cos^3 z \end{vmatrix} = 0$  then which of the following is /

are possible ?

A.  $x = y$

B.  $y = z$

C.  $x = z$

D.  $x + y + z = \pi/2$

**Answer: A::B::C::D**



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14. If  $\begin{vmatrix} x^2 + x & x + 1 & x - 2 \\ 2x^2 + 3x - 1 & 3x & 3x - 3 \\ x^2 + 2x + 3 & 2x - 1 & 2x - 1 \end{vmatrix} = xA + B$  then

- A.  $\begin{vmatrix} 1 & 1 & 1 \\ -1 & -3 & 3 \\ 4 & 0 & 0 \\ 0 & 1 & 2 \end{vmatrix}$
- B.  $\begin{vmatrix} 1 & -2 & 3 \\ -4 & 0 & 0 \\ 1 & 1 & -2 \end{vmatrix}$
- C.  $\begin{vmatrix} -3 & -2 & 3 \\ 4 & 0 & 1 \\ 0 & 1 & -2 \end{vmatrix}$
- D.  $\begin{vmatrix} -1 & -3 & 3 \\ 4 & 0 & 0 \end{vmatrix}$

**Answer: A::D**



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15. if  $\begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ bc & ca & ab \end{vmatrix} = \begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^3 & b^3 & c^3 \end{vmatrix}$  where a,b,c are distinct positive reals then the possible values of abc is / are

A.  $\frac{1}{18}$

B.  $\frac{1}{63}$

C.  $\frac{1}{27}$

D.  $\frac{1}{9}$

**Answer: A::B**



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16. 
$$\begin{vmatrix} .^x C_r & .^x C_{r+1} & .^x C_{r+2} \\ .^y C_r & .^y C_{r+1} & .^y C_{r+2} \\ .^z C_r & .^z C_{r+1} & .^z C_{r+2} \end{vmatrix}$$
 is equal to



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17. If 
$$\begin{vmatrix} \sin \theta \cos \phi & \sin \theta \sin \phi & \cos \theta \\ \cos \theta \cos \phi & \cos \theta \sin \phi & -\sin \theta \\ -\sin \theta \sin \phi & \sin \theta \cos \phi & \theta \end{vmatrix}$$
 then

A.  $\Delta$  is independent of theta

B.  $\Delta$  is independent of  $\phi$

C.  $\Delta$  is a constant

D.  $\left[ \frac{d\Delta}{d}(\theta) \right]_{\theta=\pi/2} = 0$

**Answer: B::D**



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18. If  $f(\theta) = |\sin^2 A \cot A + \sin^2 B \cos B + \sin^2 C \cos C|$ , then

$$\tan A + \tan B + \tan C = \cot A \cot B \cot C \sin^2 A + \sin^2 B + \sin^2 C = 0$$

A.  $\tan A + \tan B + \tan C$

B.  $\cot A \cot B \cot C$

C.  $\sin^2 A + \sin^2 B + \sin^2 C$

D. 0

**Answer: D**



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19. if determinant  $\begin{vmatrix} \cos(\theta + \phi) & -\sin(\theta + \phi) & \cos 2\phi \\ \sin \theta & \cos \theta & \sin \phi \\ -\cos \theta & \sin \theta & \cos \phi \end{vmatrix}$  is

- A. non-negative
- B. independent of theta
- C. independent of  $\phi$
- D. none of these

**Answer: A::B**



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20. If  $g(x) = \begin{vmatrix} a^{-x} & e^{x \log_e a} & x^2 \\ a^{-3x} & e^{3x \log_e a} & x^4 \\ a^{-5x} & e^{5x \log_e a} & 1 \end{vmatrix}$  then

- A. graphs of  $g(x)$  is symmetrical about the origin
- B. graphs of  $g(x)$  is symmetrical about the y-axis
- C.  $\frac{d^4 g(x)}{dx^4} |_{x=0} = 0$

D.  $f(x) = g(x) \times \log_e \left( \frac{a-x}{a+x} \right)$  is an odd function

**Answer: A::C**



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21. If  $\Delta(x) = \begin{vmatrix} x^2 + 4x - 3 & 2x + 4 & 13 \\ 2x^2 + 5x - 9 & 4x + 5 & 26 \\ 8x^2 - 6x + 1 & 16x - 6 & 104 \end{vmatrix} = ax^3 + bx^2 + cx + d$ ,

then

A.  $a = 3$

B.  $b = 0$

C.  $c = 0$

D. None of these

**Answer: B::C**



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22. if  $\begin{vmatrix} yz - x^2 & zx - y^2 & xy - z^2 \\ xz - y^2 & xy - z^2 & yz - x^2 \\ xy - z^2 & yz - x^2 & zx - y^2 \end{vmatrix} = \begin{vmatrix} r^2 & u^2 & u^2 \\ u^2 & r^2 & u^2 \\ u^2 & u^2 & r^2 \end{vmatrix}$  then

- A.  $r^2 = x + y + z$
- B.  $r^2 = x^2 = y^2 + z^2$
- C.  $u^2 = yz + zx + xy$
- D.  $u^2 = xyz$

**Answer: B::C**



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23. which of the following is / are true for

$$\Delta = \begin{vmatrix} a^2 & 1 & a+c \\ 0 & b^2+1 & b+c \\ 0 & b+c & c^2+1 \end{vmatrix} ?$$

- A.  $\Delta \geq 0$  for real values of a,b,c

- B.  $\Delta \leq 0$  for real values of a,b,c

$$C. \Delta = \begin{vmatrix} bc - 1 & 0 & 0 \\ 1 & ac & -a \\ -b & -a & ab \end{vmatrix}$$

D.  $\Delta = 0$  if  $bc = 1$  where  $a, b, c$  are non-zero

**Answer: A::C::D**



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24. The values of  $k \in R$  for which the system of equations  $x + ky + 3z = 0, kx + 2y + 2z = 0, 2x + 3y + 4z = 0$  admits of nontrivial solution is  
a. 2 b.  $5/2$  c. 3 d.  $5/4$

A. 2

B.  $5/2$

C. 3

D.  $5/4$

**Answer: A::B**



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25. The system of equations  $-2x + y + z = a$ ,  $x - 2y + z = b$ ,  $x + y - 2z = c$  has

- A. no solution if  $a + b + c \neq 0$
- B. unique solution if  $a + b + c = 0$
- C. infinite number of solutions if  $a + b + c = 0$
- D. None of these

**Answer: A::C**



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26. Let  $\alpha, \beta$  and  $\gamma$  be the roots of the equations  $x^3 + ax^2 + bx + c = 0$ , ( $a \neq 0$ ). If the system of equations  $\alpha x + \beta y + \gamma z = 0$ ,  $\beta x + \gamma y + \alpha z = 0$  and  $\gamma x + \beta y + \alpha z = 0$  has non-trivial solution then

A.  $a^2 = 3b$

B.  $a^3 = 27c$

C.  $b^3 = 27c^2$

D.  $\alpha + \beta + \gamma = 0$

**Answer: A::B::C**



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### Exercise (Comprehension)

1. Consider the function  $f(x) = \begin{vmatrix} a^2 + x & ab & ac \\ ab & b^2 + x & bc \\ ac & bc & c^2 + x \end{vmatrix}$

Which of the following is true ?

A.  $f(x) = 0$  and  $f(x) = 0$  have one positive common root

B.  $f(x)=0$  and  $f(x)=0$  have one negative common root

C.  $f(x) = 0$  and  $f(x) = 0$  have no common root

D. None of these

**Answer: D**



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2. Consider the function  $f(x) = \begin{vmatrix} a^2 + x & ab & ac \\ ab & b^2 + x & bc \\ ac & bc & c^2 + x \end{vmatrix}$

which of the following is true ?

A.  $f(x)$  has one +ve point of maxima.

B.  $f(x)$  has one -ve point of minima

C.  $f(x)=0$  has three distinct roots

D. Local minimum value of  $f(x)$  is zero

**Answer: D**



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3. Consider the function  $f(x) = \begin{vmatrix} a^2 + x & ab & ac \\ ab & b^2 + x & bc \\ ac & bc & c^2 + x \end{vmatrix}$

In which of the following interval  $f(x)$  is strictly increasing

A.  $(-\infty, \infty)$

B.  $(-\infty, 0)$

C.  $(0, \infty)$

D. None of these

**Answer: C**



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4. Let  $\Delta = \begin{vmatrix} -bc & b^2 + bc & c^2 + bc \\ a^2 + ac & -ac & c^2 + ac \\ a^2 + ab & b^2 + ab & -ab \end{vmatrix}$  and the equation

$px^3 + qx^2 + rx + s = 0$  has roots a,b,c where  $a, b, c \in R^+$

the value of  $\Delta$  is

A.  $r^2/p^2$

A.  $r^3/p^3$

C.  $-s/p$

D. none of these

**Answer: B**



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5. Let  $\Delta = \begin{vmatrix} -bc & b^2 + bc & c^2 + bc \\ a^2 + ac & -ac & c^2 + ac \\ a^2 + ab & b^2 + ab & -ab \end{vmatrix}$  and the equation

$px^3 + qx^2 + rx + s = 0$  has roots a,b,c where  $a, b, c \in R^+$

The value of  $\Delta$  is

A.  $\leq 9r^2/p^2$

B.  $\geq 27s^2/p^2$

C.  $\leq 27s^3/p^3$

D. none of these

**Answer: B**



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6. Let  $\Delta = \begin{vmatrix} -bc & b^2 + bc & c^2 + bc \\ a^2 + ac & -ac & c^2 + ac \\ a^2 + ab & b^2 + ab & -ab \end{vmatrix}$  and the equation

$px^3 + qx^2 + rx + s = 0$  has roots a,b,c where  $a, b, c \in R^+$

if  $\Delta = 27$  and  $a^2 + b^2 + c^2 = 3$  then

A.  $3p + 2q = 0$

B.  $4p + 3q = 0$

C.  $3p + q = 0$

D. none of these

**Answer: C**



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7. if  $x > m, y > n, z > r$  ( $x, y, z > 0$ ) such that  $\begin{vmatrix} x & n & r \\ m & y & r \\ m & n & z \end{vmatrix} = 0$

The value of  $\frac{x}{x-m} + \frac{y}{y-n} + \frac{z}{z-r}$  is

A. 1

B. -1

C. 2

D. -2

**Answer: C**



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8. if  $x > m, y > n, z > r$  ( $x, y, z > 0$ ) such that  $\begin{vmatrix} x & n & r \\ m & y & r \\ m & n & z \end{vmatrix} = 0$

the value of  $\frac{m}{x-m} + \frac{n}{y-n} + \frac{r}{z-r}$  is

A. -2

B. -4

C. 0

D. -1

**Answer: D**



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9. if  $x > m, y > n, z > r (x, y, z > 0)$  such that  $\begin{vmatrix} x & n & r \\ m & y & r \\ m & n & z \end{vmatrix} = 0$

the value  $\frac{xyz}{(x-m)(y-n)(z-r)}$  is

A. 27

B.  $\frac{8}{27}$

C.  $\frac{64}{27}$

D. None of these

**Answer: B**



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10.

$$f(x) = \begin{vmatrix} x + c_1 & x + a & x + a \\ x + b & x + c_2 & x + a \\ x + b & x + b & x + c_3 \end{vmatrix} \text{ and } g(x) = (C_1 - x)(c_3 - x)$$

Coefficient of  $x$  in  $f(x)$  is

A.  $\frac{g(a) - f(b)}{b - a}$

B.  $\frac{g(-a) - g(-b)}{b - a}$

C.  $\frac{g(a) - g(b)}{b - a}$

D. none of these

Answer: C



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11.

$$f(x) = \begin{vmatrix} x + c_1 & x + a & x + a \\ x + b & x + c_2 & x + a \\ x + b & x + b & x + c_3 \end{vmatrix} \text{ and } g(x) = (C_1 - x)(c_3 - x)$$

Which of the following is not a constant term in  $f(x)$  ?

A.  $\frac{bg(a) - ag(b)}{(b - a)}$

B.  $\frac{bf(a) - af(-b)}{(b - a)}$

C.  $\frac{bf(-a) - ag(b)}{(b - a)}$

D. none of these

**Answer: D**



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**12.**

$$f(x) = \begin{vmatrix} x + c_1 & x + a & x + a \\ x + b & x + c_2 & x + a \\ x + b & x + b & x + c_3 \end{vmatrix} \text{ and } g(x) = (C_1 - x)(c_3 - x)$$

Which of the following is not true ?

A.  $f(-a) = g(a)$

B.  $f(-a) = g(-a)$

C.  $f(-b) = g(b)$

D. none of these

**Answer: B**



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13. Suppose  $f(x)$  is a function satisfying the following conditions:

$f(0) = 2, f(1) = 1$   $f$  has a minimum value at  $x = \frac{5}{2}$  For all

$x, f'(x) = |2ax^2 - 12ax + b + 1| + 1 - 12(ax + b)|$

where  $a, b$  are some constants. Determine the constants  $a, b$ , and the function  $f(x)$

A.  $1/4$

B.  $1/2$

C.  $-1$

D.  $3$

**Answer: B**



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**14.** Suppose  $f(x)$  is a function satisfying the following conditions :

(i)  $f(0)=2, f(1)=1$

(ii)  $f$  has a minimum value at  $x = 5/2$

(iii) for all  $x$ ,  $f(x) = \begin{vmatrix} 2ax & 2ax - 1 & 2ax + b + 1 \\ b & b + 1 & -1 \\ 2(ax + b) & 2ax + 2b + 1 & 2ax + b \end{vmatrix}$

$f(x)=0$  has

A. both roots positive

B. both roots negative

C. roots of opposite sign

D. imaginary roots

**Answer: D**



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**15.** Suppose  $f(x)$  is a function satisfying the following conditions :

(i)  $f(0)=2, f(1)=1$

(ii)  $f$  has a minimum value at  $x = 5/2$

$$(iii) \text{ for all } x, f(x) = \begin{vmatrix} 2ax & 2ax - 1 & 2ax + b + 1 \\ b & b + 1 & -1 \\ 2(ax + b) & 2ax + 2b + 1 & 2ax + b \end{vmatrix}$$

Range of  $f(x)$  is

A.  $[7/16, \infty)$

B.  $(-\infty, 15/16]$

C.  $[3/4, \infty)$

D. none of these

**Answer: A**



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16. Consider the polynomial function

$$f(x) = \begin{vmatrix} (1+x)^a & (1+2x)^b & 1 \\ 1 & (1+x)^a & (1+2x)^b \\ (1+2x)^b & 1 & (1+x)^a \end{vmatrix} \quad a, b \text{ being positive integers.}$$

The constant term in  $f(x)$  is

A. 2

B. 1

C. -1

D. 0

**Answer: D**



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**17.** Consider the polynomial function

$$f(x) = \begin{vmatrix} (1+x)^2 & (1+2x)^b & 1 \\ 1 & (1+x)^a & (1+2x)^b \\ (1+2x)^b & 1 & (1+x)^a \end{vmatrix}$$

a,b being positive integers.

the coefficient of x in f(x) is

A.  $2^a$

B.  $2^a - 3 \times 2^b + 1$

C. 0

D. none of these

**Answer: C**



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**18.** Consider the polynomial function

$$f(x) = \begin{vmatrix} (1+x)^2 & (1+2x)^b & 1 \\ 1 & (1+x)^a & (1+2x)^b \\ (1+2x)^b & 1 & (1+x)^a \end{vmatrix}$$

a,b being positive integers.

Which of the following is true ?

- A. All the roots of the equation  $f(x)=0$  are positive
- B. All the roots of the equation  $f(x)=0$  are negative
- C. At least one of the equation  $f(x)=0$  is repeating one .
- D. None of these

**Answer: C**



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19. Given that the system of equations

$x = cy + bz$ ,  $y = az + cx$ ,  $z = bx + ay$  has nonzero solutions and and

at least one of the a,b,c is a proper fraction.

$a^2 + b^2 + c^2$  is

A.  $> 2$

B.  $> 3$

C.  $< 3$

D.  $< 2$

**Answer: C**



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20. Given that the system of equations

$x = cy + bz$ ,  $y = az + cx$ ,  $z = bx + ay$  has nonzero solutions and and

at least one of the a,b,c is a proper fraction.

abc is

A.  $> -1$

B.  $> 1$

C.  $< 2$

D.  $< 3$

**Answer: A**



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21. Given that the system of equations

$x = cy + bz$ ,  $y = az + cx$ ,  $z = bx + ay$  has nonzero solutions and at least one of the  $a, b, c$  is a proper fraction.

System has solution such that

A.  $x, y, z \equiv (1 - 2a^2) : (1 - 2b^2) : (1 - 2c^2)$

B.  $x, y, z \equiv \frac{1}{1 - 2a^2} : \frac{1}{1 - 2b^2} : \frac{1}{1 - 2c^2}$

C.  $x, y, z \equiv \frac{a}{1 - a^2} : \frac{b}{1 - b^2} : \frac{c}{1 - c^2}$

D.  $x, y, z \equiv \sqrt{1 - a^2} : \sqrt{1 - b^2} : \sqrt{1 - c^2}$

**Answer: D**



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**22.** Consider the system of equations

$$x + y + z = 6$$

$$x + 2y + 3z = 10$$

$$x + 2y + \lambda z = \mu$$

the system has unique solution if

A.  $\lambda \neq 3$

B.  $\lambda = 3, \mu = 10$

C.  $\lambda = 3, \mu \neq 10$

D. none of these

**Answer: A**



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**23.** Consider the system of equations

$$x + y + z = 6$$

$$x + 2y + 3z = 10$$

$$x + 2y + \lambda z = \mu$$

the system has infinite solutions if

A.  $\lambda \neq 3$

B.  $\lambda = 3, \mu = 10$

C.  $\lambda = 3, \mu \neq 10$

D.  $\lambda = 3, \mu \neq 10$

**Answer:** B



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**24.** Consider the system of equations

$$x + y + z = 6$$

$$x + 2y + 3z = 10$$

$$x + 2y + \lambda z = \mu$$

The system has no solution if

A.  $\lambda \neq 3$

B.  $\lambda = 3, \mu = 10$

C.  $\lambda = 3, \mu \neq 10$

D. none of these

**Answer: C**



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### Matrix Match Type

1. Match the following lists :



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**2.** Match the following lists:



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**3.** If  $\alpha, \beta, \gamma$  are the roots of  $x^3 - 3x^2 + 3x - 1 = \begin{vmatrix} 1^2 & 2^2 & 3^2 \\ 2^2 & 3^2 & 4^2 \\ 3^2 & 4^2 & 5^2 \end{vmatrix}$

then match the list I with list II



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**4.** consider the system of equations

$$\lambda x + y + z = 1$$

$$x + \lambda y + z = \lambda :$$

$$x + y + \lambda z = \lambda^2$$

Now match the following lists:



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5. consider determinant  $\Delta = |a_{ij}|$  of order 3. If  $\Delta = 2$  the match the following lists.



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### Exercise (Numerical)

1. If  $a_1, a_2, a_3, 54, a_6, a_7, a_8, a_9$  are in H.P., and  $D = |a_1a_2a_354a_6a_7a_8a_9|$ , then the value of  $[D]$  is where  $[.]$  represents the greatest integer function



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2. the sum of values of p for which the equations  $x+y+z=1$ ,  $x+2y+4z=p$  and  $x+4y+10z=p^2$  have a solution is \_\_\_\_\_



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**3. The sum of roots of the equations**

$$\begin{vmatrix} x+2 & 2x+3 & 3x+4 \\ 2x+3 & 3x+4 & 4x+5 \\ 3x+5 & 5x+8 & 10x+17 \end{vmatrix} = 0 \text{ is } \underline{\hspace{2cm}}$$



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**4.**

**Prove**

**that**

$$\begin{vmatrix} (\beta + \gamma - \alpha - \delta)^4 & (\beta + \gamma - \alpha - \delta)^2 & 1 \\ (\gamma + \alpha - \beta - \delta)^4 & (\gamma + \alpha - \beta - \delta)^2 & 1 \\ (\alpha + \beta - \gamma - \delta)^4 & (\alpha + \beta - \gamma - \delta)^2 & 1 \end{vmatrix} = -64(\alpha - \beta)(\alpha - \gamma)(\alpha - \delta)$$



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**5. If**  $f(x) = \begin{vmatrix} 1 & x & x+1 \\ 2x & x(x-1) & (x+1)x \\ 3x(x-1) & x(x-1)(x-2) & (x+1)x(x-1) \end{vmatrix}$  **then**

the value of  $f(500)$  \_\_\_\_\_



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6.

If

$$|(x, x + y, x + y + z), (2x + 3x + 2y, 4x + 3y + 2z), (3x + 6x + 3y, 10x -$$

then the real value of x is



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7.

Let

$$D_1 = |aba + bc dc + d a b a - b| \text{ and } D_2 = |aca + cb db + d a c a + b + c|$$

then the value of  $\left| \frac{D_1}{D_2} \right|$ , where  $b \neq 0$  and  $a \neq bc$ , is \_\_\_\_.



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8. if  $a_1, a_2, a_3, \dots, a_{12}$  are in A.P and

$$\Delta_1 = \begin{vmatrix} a_1 a_5 & a_1 & a_2 \\ a_2 a_6 & a_2 & a_3 \\ a_3 a_7 & a_3 & a_4 \end{vmatrix} \Delta_3 = \begin{vmatrix} a_2 b_{10} & a_2 & a_3 \\ a_3 a_{11} & a_3 & a_4 \\ a_3 a_{12} & a_4 & a_5 \end{vmatrix}$$

then  $\Delta_2 : \Delta_2 = \text{_____}$



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9. if  $(1 + ax + bx^2)^4 = a_0 + a_1x + a_2x^2 + \dots + a_8x^8$ , where

$a, b, a_0, a_1, \dots, a_8 \in R$  such that  $a_0 + a_1 + a_2 \neq 0$  and

$$\begin{vmatrix} a_0 & a_1 & a_2 \\ a_1 & a_2 & a_0 \\ a_2 & a_0 & a_1 \end{vmatrix} = 0 \text{ then the value of } 5 \cdot \frac{a}{b} \text{ is } \underline{\hspace{2cm}}$$



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10.  $\begin{vmatrix} 5\sqrt{\log_e 3} & 5\sqrt{\log_e 3} & 3\sqrt{\log_e 3} \\ 3^{-\log_{1/3} 4} & (0.1)^{\log_{0.01} 4} & 7^{\log_7 3} \\ 7 & 3 & 5 \end{vmatrix}$  is equal to  $\underline{\hspace{2cm}}$



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11. Let  $a+b+c=s$  and  $\begin{vmatrix} s+c & a & b \\ c & s+a & b \\ c & a & s+b \end{vmatrix} = 532$  then the value of  $s$

is  $\underline{\hspace{2cm}}$



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12. Let  $a, b, c \in R$  not all are equal and  $\Delta_1 = \begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$

$$\Delta_2 = \begin{vmatrix} a + 2b & b + 3c & c + 4a \\ b + 2c & c + 3a & a + 4b \\ c + 2a & a + 3b & b + 4c \end{vmatrix} \text{ then } \frac{\Delta_2}{\Delta_1} = \underline{\hspace{2cm}}$$



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13. Three distinct points  $P(3u^2, 2u^3); Q(3v^2, 2v^3)$  and  $R(3w^2, 2w^3)$  are collinear then



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14. if  $\Delta_r = \begin{vmatrix} r & 612 & 915 \\ 101r^2 & 2r & 3r \\ r & \frac{1}{r} & \frac{1}{r^2} \end{vmatrix}$  then the value of

$$\lim_{n \rightarrow \infty} \cdot \frac{1}{n^3} (\sum_{r=1}^n \Delta_r) \text{ is } \underline{\hspace{2cm}}$$



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15. if  $x=31, y=32$  and  $z=33$  then the value of

$$\begin{vmatrix} (x^2 + 1)^2 & (xy + 1)^2 & (xz + 1)^2 \\ (xy + 1)^2 & (y^2 + 1)^2 & (yz + 1)^2 \\ (xz + 1)^2 & (yz + 1)^2 & (z^2 + 1)^2 \end{vmatrix} \text{ is } \underline{\hspace{2cm}}$$



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16. Let  $\alpha, \beta, \gamma$  are the real roots of the equation  $x^3 + ax^2 + bx + c = 0$  ( $a, b, c \in R$  and  $a \neq 0$ ). If the system of equations  $(\in u, v, \text{ and } w)$  given by  $\alpha u + \beta v + \gamma w = 0$ ,  $\beta u + \gamma v + \alpha w = 0$ ,  $\gamma u + \alpha v + \beta w = 0$  has non-trivial solutions then the value of  $a^2/b$  is \_\_\_\_\_.



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17. The value of  $|\alpha|$  for which the system of equation

$$\alpha x + y + z = \alpha - 1$$

$$x + \alpha y + z = \alpha - 1$$

$$x + y + \alpha z = \alpha - 1$$

has no solution , is \_\_\_\_\_



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18. Number of values of  $\theta$  lying in  $[0, 100\pi]$  for which the system of equations  $(\sin 3\theta) x - y + z = 0$ ,  $(\cos 2\theta) x + 4y + 3z = 0$ ,  $2x + 7y + 7z = 0$  has non-trivial solution is \_\_\_\_\_



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## JEE Main Previous Year

1. Let  $a, b, c$  be such that  $b(a+c) \neq 0$ . If

$$\begin{vmatrix} a & a+1 & a-1 \\ -b & b+1 & b-1 \\ c & c-1 & c+1 \end{vmatrix} + \begin{vmatrix} a+1 & b+1 & c-1 \\ a-1 & b-1 & c+1 \\ (-1)^{n+2}a & (-1)^{n+1}b & (-1)^nc \end{vmatrix} = 0,$$

Then the value of 'n' is:

A. zero

B. any even integer

C. any odd integer

D. any integer

**Answer: 3**



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**2.** Consider the system of linear equations:

$$x_1 + 2x_2 + x_3 = 3$$

$$2x_1 + 3x_2 + x_3 = 3$$

$$3x_1 + 5x_2 + 2x_3 = 1$$

The system has

A. no solution

B. infinite number of solutions

C. exactly three solutions.

D. a unique solution

**Answer: 1**



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3. The number of values of  $k$  for which the linear equations  $4x + ky + 2z = 0$   $kx + 4y + z = 0$   $2x + 2y + z = 0$  posses a non-zero solution is : (1) 3 (2) 2 (3) 1 (4) zero

A. zero

B. 3

C. 2

D. 1

**Answer: 3**



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**4.** The number of values of  $k$  for which the system of equations:

$$kx + (3k + 2)y = 4k$$

$(3k - 1)x + (9k + 1)y = 4(k + 1)$  has no solution, are

A. infinite

B. 1

C. 2

D. 3

**Answer:** 2



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**5.** If  $\alpha, \beta \neq 0$ , and  $f(n) = \alpha^n + \beta^n$  and

$$|31 + f(1)1 + f(2)1 + f(1)1 + f(2)1 + f(3)1 + f(2)1 + f(3)1 + f(4)| = .$$

, then K is equal to (1)  $\alpha\beta$  (2)  $\frac{1}{\alpha\beta}$  (3) 1 (4)  $-1$

A.  $\alpha\beta$

B.  $\frac{1}{\alpha\beta}$

C. 1

D. -1

**Answer:** 3



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**6.** The set of all values of  $\lambda$  for which the system of linear equations

$$x - 2y - 2z = \lambda x$$

$$x + 2y + z = \lambda y$$

$$-x - y = \lambda z$$

has a non-trivial solution

A. is an empty set

B. is a singleton set

C. contains two elements

D. contains more than two elements

**Answer: 3**



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7. The system of linear equations  $x + \lambda y - z = 0$   $\lambda x - y - z = 0$   $x + y - \lambda z = 0$  has a non-trivial solution for : (1) infinitely many values of  $\lambda$  . (2) exactly one value of  $\lambda$  . (3) exactly two values of  $\lambda$  . (4) exactly three values of  $\lambda$  .

- A. Exactly one value of  $\lambda$
- B. Exactly two values of  $\lambda$
- C. Exactly three values of  $\lambda$
- D. Infinitely many values of  $\lambda$

**Answer: 3**



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8. If  $S$  is the set of distinct values of ' $b$ ' for which the following system of linear equations  $x + y + z = 1$   $x + ay + z = 1$   $ax + by + z = 0$  has no solution, then  $S$  is : a finite set containing two or more elements (2) a singleton an empty set (4) an infinite set

A. a singleton set

B. an empty set

C. an infinite set

D. a finite set containing two or more elements

**Answer: 1**



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9. Let  $\omega$  be a complex number such that  $2\omega + 1 = z$  where  $z = \sqrt{-3}$ .

If  $|1111 - \omega^2 - 1\omega^2 1\omega^2 \omega^7| = 3k$ , then  $k$  is equal to : -1 (2) 1 (3)  $-z$  (4)

$z$

A. 1

B.  $-z$

C.  $z$

D. -1

**Answer: 2**



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**10.** If the system of linear equations  $x+ky+3z=0$   $3x+ky-2z=0$   $2x+4y-3z=0$  has a non-zero solution  $(x,y,z)$  then  $\frac{xz}{y^2}$  is equal to

A. 30

B. -10

C. 10

D. -30

**Answer: 3**



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11. If  $\begin{vmatrix} x - 4 & 2x & 2x \\ 2x & x - 4 & 2x \\ 2x & 2x & x - 4 \end{vmatrix} = (A + Bx)(x - A)^2$  then the ordered pair (A,B) is equal to

- A. (4, 5)
- B. (-4, -5)
- C. (-4, 3)
- D. (-4, 5)

Answer: D



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JEE Advanced Previous Year

1. Which of the following values of  $\alpha$  satisfying the equation  
$$|(1 + \alpha)^2(1 + 2\alpha)^2(1 + 3\alpha)^2(2 + \alpha)^2(2 + 2\alpha)^2(2 + 3\alpha)^2(3 + \alpha)^2(3 + 2\alpha)| = 4$$
b. 9 c. -9 d. 4

A. -4

B. 9

C. -9

D. 4

**Answer:** 2,3



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2. Let  $a, \lambda, \mu \in R$ , Consider the system of linear equations  
$$\begin{aligned} ax + 2y &= \lambda \\ 3x - 2y &= \mu \end{aligned}$$
 Which of the following statement(s) is (are) correct?

- A. If  $\alpha = -3$  then the system has infinitely many solutions for all values of  $\lambda$  and  $\mu$
- B. If  $\alpha \neq -3$  then the system has a unique solution for all values of  $\lambda$  and  $\mu$
- C. If  $\lambda + \mu = 0$  then the system has infinitely many solutions for  $\alpha = -3$
- D. if  $\lambda + \mu \neq 0$  then the system has no solution for  $\alpha = -3$

**Answer: 2,3,4**



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3. Let  $\omega$  be the complex number  $\cos\left(\frac{2\pi}{3}\right) + i \sin\left(\frac{2\pi}{3}\right)$ . Then the number of distinct complex numbers  $z$  satisfying

$$\Delta = \begin{vmatrix} z+1 & \omega & \omega^2 \\ \omega & z+\omega^2 & 1 \\ \omega^2 & 1 & z+\omega \end{vmatrix} = 0 \text{ is}$$



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4. The total number of distinct  $x \in R$  for which

$$\begin{vmatrix} x & x^2 & 1+x^3 \\ 2x & 4x^2 & 1+8x^3 \\ 3x & 9x^2 & 1+27x^3 \end{vmatrix} = 10$$
 is (A) 0 (B) 1 (C) 2 (D) 3



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5. For a real number  $\alpha$ , if the system  $[1\alpha\alpha^2\alpha 1\alpha\alpha^2\alpha 1][xyz] = [1 - 1 1]$  of linear equations, has infinitely many solutions, then  $1 + \alpha + \alpha^2 =$



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6. Let  $P$  be a matrix of order  $3 \times 3$  such that all the entries in  $P$  are from the set  $\{-1, 0, 1\}$ . Then, the maximum possible value of the determinant of  $P$  is \_\_\_\_.



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## Question Bank

1. Number of real roots of the equation  $[[1, x, x], [x, 1, x], [x, x, 1]] + [[1 - x, 1, 1], [1, 1 - x, 1], [1, 1, 1 - x]] = 0$  is

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2. If  $\begin{vmatrix} \sqrt{3}x - x^2 & x - 1 & x - \sqrt{3} \\ \sqrt{3}x & x & \sqrt{3} - 1 \\ x - 1 & \sqrt{3} - x & x - 1 \end{vmatrix} = ax^4 + bx^3 + cx^2 + dx + e$  and  $a + c = p + \sqrt{q}$ , then  $(p - q)$  is equal to

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3. If  $f(x) = [\cos(x + \alpha), \cos(x + \beta), \cos(x + \gamma)], [\sin(x + \alpha), \sin(x + \beta), \sin(x + \gamma)]$  and  $f(0) = -2$  then  $\sum_{r=1}^{30} |f(r)|$  equals

$$f(0) = -2 \text{ then } \sum_{r=1}^{30} |f(r)| \text{ equals}$$



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4. Let  $f(x) = \begin{vmatrix} 1 + \sin^2 x & \cos^2 x & 4 \sin 2x \\ \sin^2 x & 1 + \cos^2 x & 4 \sin 2x \\ \sin^2 x & \cos^2 x & 1 + 4 \sin 2x \end{vmatrix}$ , the maximum value of  $f(x)$  is



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5. Given  $2x - y + 2z = 1$ ,  $x - 2y + z = -4$ , and  $x + y + \lambda z = 4$ . Then the value of  $\lambda$  such that the given system of equation has no solution is



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6. If  $M$  and  $m$  are maximum and minimum value, respectively of  $\begin{vmatrix} 1 & \cos \theta & 1 \\ \cos \theta & 1 & \cos \theta \\ -1 & \cos \theta & 1 \end{vmatrix}$ , then value of  $(M + m)$  is



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7. The value of  $\begin{vmatrix} \log_3 512 & \log_4 3 \\ \log_3 8 & \log_4 9 \end{vmatrix} \begin{vmatrix} \log_2 3 & \log_8 3 \\ \log_3 4 & \log_3 4 \end{vmatrix}$  is



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8. If  $|[1, x, x^2], [x, x^2, 1], [x^2, 1, x]| = 3$ , then the value of  $|[x^{(3)-1}, 0, x-x^4], [0, x-x^{(4)}, x^{(3)-1}], [x-x^{(4)}, x^{(3)-1}, 0]|$



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9. If  $a, b, c$  are the sides of a scalene triangle such that  $|[a, a^2, a^{(3)-1}], [b, b^2, b^{(3)-1}], [c, c^2, c^{(3)-1}]| = 0$ , then the geometric mean of  $a, b, c$  is



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10. Let  $a + b + c = s$  and  $|[s+c, a, b], [c, s+a, b], [c, a, s+b]|$  is equal  $\rightarrow 54$  then the value of  $s$  is



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