### **MATHS**

### **BOOKS - CENGAGE**

### **DOT PRODUCT**

**Dpp 21** 

1. Let 
$$a,b>0$$
 and  $\overrightarrow{\alpha}=\left(\dfrac{\overrightarrow{i}}{a}+\dfrac{4\hat{j}}{b}+b\hat{k}\right)$  and  $\overrightarrow{\beta}=b\hat{i}+a\hat{j}+\dfrac{1}{b}\hat{k}$ , then the maximum value of  $\dfrac{30}{5+\overrightarrow{\alpha},\overrightarrow{\beta}}$  is

### Answer: A



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**2.** If a vector  $\overrightarrow{r}$  is equall inclined with the vectors

$$\overrightarrow{a} = \cos heta \hat{i} + \sin heta \hat{j}, \ \overrightarrow{b} = -\sin heta \hat{i} + \cos heta \hat{j}$$
 and

 $\overrightarrow{c}=\hat{k}$ , then the angle between  $\overrightarrow{r}$  and  $\overrightarrow{a}$  is

A. 
$$\cos^{-1}\left(\frac{1}{\sqrt{2}}\right)$$

B. 
$$\cos^{-1}\left(\frac{1}{\sqrt{3}}\right)$$
C.  $\cos^{-1}\left(\frac{1}{3}\right)$ 
D.  $\cos^{-1}\left(\frac{1}{2}\right)$ 



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**3.** Let G be the centroid of the  $\triangle ABC$ , whose sides are of lengths a,b,c. If P be a point in the plane of  $\triangle ABC$ , such that PA=1, PB=3, PC=4 and PG=2, then the value of  $a^2+b^2+c^2$  is

A. 42

- B. 40
- C. 36
- D. 28

### **Answer: A**



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**4.** If  $\overrightarrow{a}=3\hat{i}-\hat{j}+5\hat{k}$  and  $\overrightarrow{b}=\hat{i}+2\hat{j}-3\hat{k}$  are given vectors. A vector  $\overrightarrow{c}$  which is perpendicular to z-axis satisfying  $\overrightarrow{c}.\overrightarrow{a}=9$  and  $\overrightarrow{c}.\overrightarrow{b}=-4$ . If inclination of  $\overrightarrow{c}$  with x-axis and y-axis and y-axis is  $\alpha$  and  $\beta$  respectively, then which of the following is not true?

A. 
$$lpha>rac{\pi}{4}$$

B. 
$$eta>rac{\pi}{2}$$

C. 
$$lpha>rac{\pi}{2}$$

D. 
$$eta < rac{\pi}{2}$$

### **Answer: C**



**5.** If 
$$\overrightarrow{a}$$
,  $\overrightarrow{b}$ ,  $\overrightarrow{c}$  are unit vectors such that  $\overrightarrow{a}$  is perpendicular to the plane of  $\overrightarrow{b}$ ,  $\overrightarrow{c}$  and the angle between  $\overrightarrow{b}$ ,  $\overrightarrow{c}$  is  $\frac{\pi}{3}$ , then  $\left|\overrightarrow{a}+\overrightarrow{b}+\overrightarrow{c}\right|=$ 



**6.** A unit vector 
$$\overrightarrow{a}$$
 in the plane of  $\overrightarrow{b}=2\hat{i}+\hat{j}$  and  $\overrightarrow{c}=\hat{i}-\hat{j}+\hat{k}$  is such that angle between  $\overrightarrow{a}$  and  $\overrightarrow{d}$  where  $\overrightarrow{d}=\overrightarrow{j}+2\overrightarrow{k}$  is

A. 
$$\dfrac{\dfrac{\overrightarrow{i}+\dfrac{\overrightarrow{j}+\dfrac{\overrightarrow{k}}{k}}{\sqrt{3}}}{\sqrt{3}}$$
B.  $\dfrac{\dfrac{\overrightarrow{i}-\dfrac{\overrightarrow{j}+\dfrac{\overrightarrow{k}}{k}}{\sqrt{3}}}{\sqrt{3}}$ 

C. 
$$\dfrac{2~i~+~j}{\sqrt{5}}$$
D.  $\dfrac{2~i~-~j}{\sqrt{5}}$ 



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$$|OA| = |BC| = a, |OB| = |AC| = b, |OC| = |AB| = a$$

**7.** In a tetrahedron OABC, the edges are of lengths,

$$|OA| = |BC| = a, |OB| = |AC| = b, |OC| = |AB| = c.$$

Let  $G_1$  and  $G_2$  be the centroids of the triangle ABC

and AOC such that  $OG_1 \perp BG_2, \,\,$  then the value of  $rac{a^2+c^2}{b^2}$  is

- B. 3
- C. 6
- D. 9



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**8.** The vectors  $\overrightarrow{x}$  and  $\overrightarrow{y}$  satisfy the equation

$$p\overrightarrow{x}+q\overrightarrow{y}=\overrightarrow{a}$$
 (where p,q are scalar constants and  $\overrightarrow{a}$ 

is a known vector). It is given that  $\overrightarrow{x}$  .  $\overrightarrow{y} \geq \frac{\left|\overrightarrow{a}\right|^2}{4pq}$  , then

$$\dfrac{\left|\overrightarrow{x}
ight|}{\left|\overrightarrow{y}
ight|}$$
 is equal to  $(pq>0)$ 

B. 
$$\frac{p^2}{q^2}$$

C. 
$$\frac{p}{q}$$

D. 
$$\frac{q}{p}$$

### **Answer: D**



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**9.** If  $\overrightarrow{a}$ ,  $\overrightarrow{b}$ ,  $\overrightarrow{c}$  non-zero vectors such that  $\overrightarrow{a}$  is perpendicular to  $\overset{
ightarrow}{b}$  and  $\overset{
ightarrow}{c}$  and  $\left|\overrightarrow{a}
ight|=1,\left|\overrightarrow{b}
ight|=2,\left|\overrightarrow{c}
ight|=1,\overrightarrow{b}.\overrightarrow{c}=1$ . There is a non-zero vector coplanar with  $\overrightarrow{a} + \overrightarrow{b}$  and  $2\overrightarrow{b} - \overrightarrow{c}$ and  $\overrightarrow{d}$  .  $\overrightarrow{a}=1$ , then the minimum value of  $|\overrightarrow{d}|$  is

A. 
$$\frac{2}{\sqrt{13}}$$

A. 
$$\dfrac{2}{\sqrt{13}}$$
B.  $\dfrac{3}{\sqrt{3}}$ 
C.  $\dfrac{4}{\sqrt{5}}$ 

$$\therefore \frac{4}{\sqrt{5}}$$

$$\text{D.}~\frac{4}{\sqrt{13}}$$

### **Answer: D**



# **View Text Solution**

**10.** Let two non-collinear vectors  $\overrightarrow{a}$  and  $\overrightarrow{b}$  inclined at an angle  $\dfrac{2\pi}{3}$  be such that  $\left|\overrightarrow{a}\right|=3$  and  $\left|\overrightarrow{b}\right|=2$ . If a point P moves so that at any time t its position vector  $\overrightarrow{OP}$  (where O is the origin) is given as

$$\overrightarrow{OP}=\left(t+rac{1}{t}
ight)\overrightarrow{a}+\left(t-rac{1}{t}
ight)\overrightarrow{b}$$
 then least distance of P from the origin is

B. 
$$\sqrt{2\sqrt{133}+10}$$

A.  $\sqrt{2\sqrt{133}-10}$ 

C.  $\sqrt{5 + \sqrt{133}}$ 

**Answer: B** 

**11.** Four vectors 
$$\overrightarrow{a}$$
,  $\overrightarrow{b}$ ,  $\overrightarrow{c}$  and  $\overrightarrow{x}$  satisfy the relation  $\left(\overrightarrow{a}.\overrightarrow{x}\right)\overrightarrow{b}=\overrightarrow{c}+\overrightarrow{x}$  where  $\overrightarrow{b}.\overrightarrow{a}\neq 1$ . The value of

 $\overrightarrow{x}$  in terms of  $\overrightarrow{a}$  ,  $\overrightarrow{b}$  and  $\overrightarrow{c}$  is equal to

A. 
$$\dfrac{\left(\overrightarrow{a}.\overrightarrow{c}\right)\overrightarrow{b}-\overrightarrow{c}\left(\overrightarrow{a}.\overrightarrow{b}-1\right)}{\left(\overrightarrow{a}.\overrightarrow{b}-1\right)}$$

B. 
$$\frac{\overrightarrow{c}}{\overrightarrow{a}.\overrightarrow{b}-1}$$
C.  $\frac{2(\overrightarrow{a}.\overrightarrow{c})\overrightarrow{b}+\overrightarrow{c}}{\overrightarrow{a}.\overrightarrow{b}-1}$ 

D. 
$$\frac{2\left(\overrightarrow{a} \cdot \overrightarrow{c}\right)\overrightarrow{c} + \overrightarrow{c}}{\left(\overrightarrow{a} \cdot \overrightarrow{b}\right) - 1}$$

**Answer: A** 



iew Text Solution

12. If area of a triangular face BCD of a regular tetrahdedron ABCD is  $4\sqrt{3}$  sq. units, then the area of a triangle whose two sides are represented by vectors  $\overrightarrow{AB}$  and  $\overrightarrow{CD}$  is

- A. 6 sq. units
- B. 8 sq.units
- C. 12 sq. units
- D. 16 sq.units

### **Answer: B**



**13.** If OABC is a tetrahedron such that

$$OA^2+BC^2=OB^2+CA^2=OC^2+AB^2$$
 then

A. 
$$OA \perp BC$$

B. 
$$OB \perp AC$$

C. 
$$OC \perp AB$$

D. 
$$AB \perp AC$$

### **Answer: C**



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**14.** If  $\overrightarrow{a}$ ,  $\overrightarrow{b}$  and  $\overrightarrow{c}$  are three units vectors equally inclined to each other at an angle  $\alpha$ . Then the angle

between  $\overrightarrow{a}$  and plane of  $\overrightarrow{b}$  and  $\overrightarrow{c}$  is

A. 
$$heta = \cos^{-1}\left(\frac{\coslpha}{\cos\left(rac{lpha}{2}
ight)}
ight)$$

$$\mathsf{B.}\,\theta = \sin^{-1}\!\left(\frac{\cos\alpha}{\cos\left(\frac{\alpha}{2}\right)}\right)$$

$$\mathsf{C.}\,\theta = \cos^{-1}\left(\frac{\sin\left(\frac{\alpha}{2}\right)}{\sin\alpha}\right)$$

D. 
$$heta = \sin^{-1} \left( rac{\sin \left( rac{lpha}{2} 
ight)}{\sin lpha} 
ight)$$

### **Answer: A**



**15.** If a,b,c and A,B,C 
$$\in$$
 R-{0} such that  $aA+bB+cC-\sqrt{\left(a^2+b^2+c^2
ight)\left(A^2+B^2+C^2
ight)}=0$ 

, then value of 
$$\dfrac{aB}{bA}+\dfrac{bC}{cB}+\dfrac{cA}{aC}$$
 is

A. 3

### **Answer: A**

