



## MATHS

### BOOKS - CENGAGE

# GRAPHICAL TRANSFORMATIONS

#### Illustrations

1. Plot  $y = |x|$ ,  $y + x - 2$ , and  $y = |x|2$



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2. Draw the graph of  $y = \sin^{-1}(x - 3)$ .



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3. Draw the graph of  $y = \log_e(x + 3)$ ,



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4. Draw the graph of

$$y = \cot^{-1} x + \sec^{-1} x + \operatorname{cosec}^{-1} x.$$



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5. Draw the graph of  $y = |x - 3| + 1$ .



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6. Solve  $3x + 2y > 12$  graphically



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7. For  $a \leq 0$ , determine all real roots of the equation

$$x^2 - 2a|x - a| - 3a^2 = 0$$



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8. Consider the function

$$f(x) = \begin{cases} x - [x] - \frac{1}{2}, & \text{if } x \notin I \\ 0, & \text{if } x \in I, \text{ where } I \end{cases}$$

denotes the fractional integral function and  $I$  is the set

of integers. Then find

$$g(x) = \max(x^2, f(x), |x|); \quad -2 \leq x \leq 2.$$



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9. If  $f(x) = 2x + 1$  and  $g(x) = x^2 - 2$ , then  $g \circ f(x)$

is



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10. Find angle between the vectors ,When

$$\vec{a} = \hat{i} - 2\hat{j} + 3\hat{k} \text{ and } \vec{b} = 3\hat{i} - 2\hat{j} + \hat{k}$$



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11. Draw the graph of  $y = 0.5(x - 1)^2$  and compare with  $y = (x - 1)^2$ .



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12. Plot  $y = \sin x$  and  $y = \sin 2x$ .



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13. Find  $f \circ g(x)$ , if  $f(x) = |x|$  and  $g(x) = |5x - 2|$

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14. Plot the curve  $y = (\log)_e(-x)$ .

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15. To draw the graph of  $y = \log_e(-x)$ , flip the graph of  $y = \log_e x$  over the y-axis shown in the following figure.

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**16.** Find the value of  $k$  for which the equation  $x^2 - 6x + k = 0$  has distinct roots.



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**17.** Draw the graph of  $y = -\cot^{-1} x$ .



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**18.** Draw the graph of  $y = -\log_e x$ .



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19. Draw the graph of  $y = 2 - |x - 1|$ .



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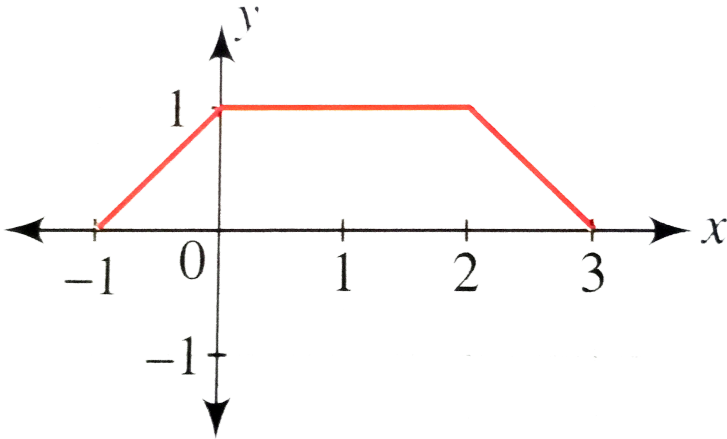
20. Draw the graph of  $y = \sin^{-1}(\cos x)$ .



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21. Given the graph of  $y = f(x)$ .



Draw the graphs of the following.

(a)  $y = f(1 - x)$  (b)  $y = -2f(x)$

(c)  $y = f(2x)$  (d)  $y = 1 - f(x)$

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22. Draw the graph for  $y = |\log x|$

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23. Draw the graph of  $y = |\sin x|$  and hence the graph of  $y = \sin^{-1}|\sin x|$ .

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24. Draw the graph of  $y = f(x) = \sqrt{1 - \cos x}$

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25. Draw the graph of  $y = |\sin x - 0.5|$ .

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**26.** The number of solution of  $2 \cos x = |\sin x|$  where  $x \in [0.4\pi]$  is/are

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**27.** Solve  $|x^2 + 4x + 3| + 2x + 5 = 0$ .

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**28.** Solve  $\cos 2x > |\sin x|$ ,  $x \in \left(-\frac{\pi}{2}, \pi\right)$

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29. Prove that the equation  $2s \in x|x| + a$  has not solution for  $a \in \left( \frac{3\sqrt{3} - \pi}{3} - \infty \right)$ .

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30. Solve  $|x^2 - 1| + |x^2 - 4| < 6$  graphically.

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31. Discuss the differentiability of  $f(x) = \min. \{|x|, |x - 2|, 2 - |x - 1|\}$ .

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32. If the equation  $|x^2 + bx + c| = k$  has four real roots, then  $b^2 - 4c > 0$  and  $0 < k < \frac{4c - b^2}{4}$  none of these



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33. Sketch the curve  $y = \log|x|$



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34. Draw the graph of  $y = \sin|x|$ .



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35. Draw the graph of  $y = [|x|]$ , where  $[.]$  denotes the greatest integer function.



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36. Draw the graph of  $y = \sin^{-1}|x|$ .



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37. Draw the graph of  $y = \tan^{-1}|x|$ .



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38. Draw the graph of  $y = \{|x|\}$ , where  $\{.\}$  represents the fractional part function.

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39. Draw the graph of the function:

$$f(x) = |x^2 - 3|x| + 2|$$

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40. Draw the graph of  $y = \left| 1 - \frac{1}{|x| - 2} \right|$ .

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41. Draw the graph of  $|y| = |2^{|x|} - 3|$ .



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42. Find the total number of solutions to  $\sin \pi x = |\ln|x||$ .



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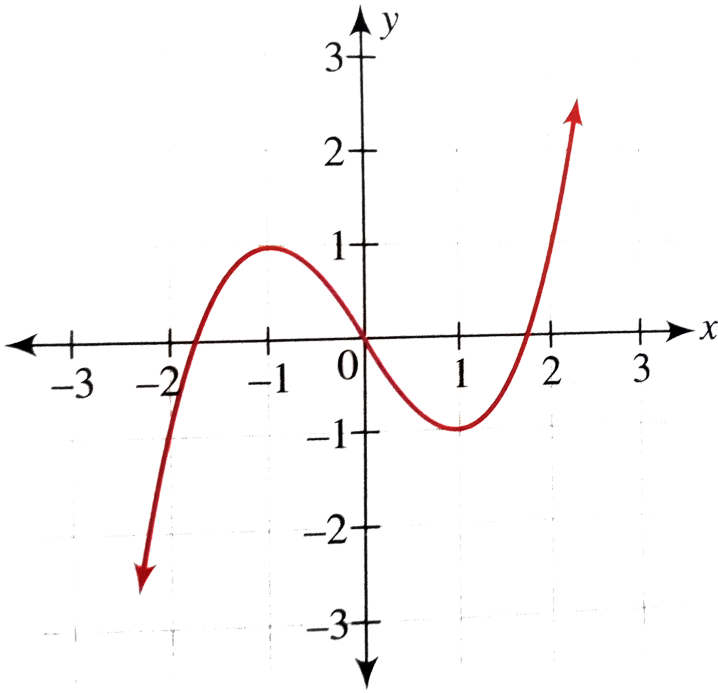
43. Find the number of solutions to  $7^{|x|} (|1 - |x||) = 1$ .



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44. The graph of the function  $y = f(x)$  is shown.



Find the number of solutions to the equation

$$||f(x)| - 1| = \frac{1}{2}.$$



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45. Consider the function  $f(x) = x^2 + bx + c$ , where  $D = b^2 - 4c > 0$ , then match the following columns.

Column I	Column II
Values of $b$ and $c$	Number of points of non-differentiability of $g(x) =  f(x) $
(a) $b < 0, c > 0$	(p) 1
(b) $c = 0, b < 0$	(q) 2
(c) $c = 0, b > 0$	(r) 3
(d) $b = 0, c < 0$	(s) 5



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46. Draw the graph of  $|y| = \sin x$ .



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47. Draw the graph of  $|y| = \tan x$ .



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48. Sketch the curve  $|y| = (x - 1)(x - 2)$ .



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49. Draw the graph of  $|y| = \{x\}$ , where  $\{.\}$  represents the fractional part function.



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50. Draw the graph of  $|x| + |y| = 1 + x$ .



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51. Draw the graph of  $|x| - |y| = 2$  using graphical transformation.



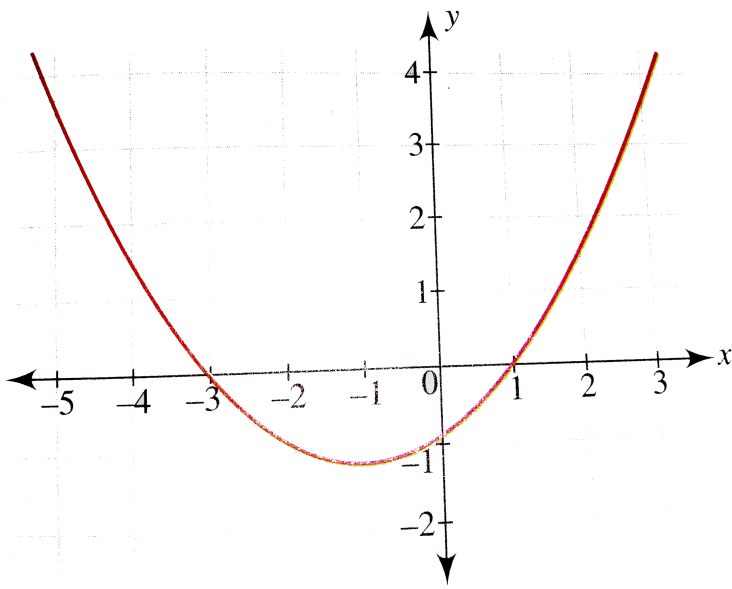
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52. Draw the graph of  $y = |2^{|x|} - 3|$ .



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53. Given the graph of the function  $y = f(x)$ , draw the graph of  $y = \operatorname{sgn} f(x)$ .



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54. about to only mathematics



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55. Draw the graph and discuss the continuity of  $f(x) = [\sin x + \cos x]$ ,  $x \in [0, 2\pi]$ , where  $[.]$  represents the greatest integer function.



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56. Let  $f: \mathbb{R} \rightarrow \mathbb{R}: f(x) = (x + 1)$  and  $g: \mathbb{R} \rightarrow \mathbb{R}: g(x) = (x^2 - 4)$ . Write down the formulae for  $(f \circ g)$ .



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Exercise

1. Draw the graph of  $y = \tan^{-1} x - \cot^{-1} x$ .



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2. Draw the graph of  $y = |x|$ .



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3. Draw the graph of

$$y = \tan^{-1} x + \cos^{-1} x + \sin^{-1} x.$$



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4. Draw the graph of  $|y| = (x - 1)(x - 2)(x - 3)$ .



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5. Draw the graph of  $y = \sin^{-1}(x - 3)$ .



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6. Draw the graph of  $y = \cot^{-1} x$ .



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7. Draw the graph of  $y = |\log_e(x + 3)|$ .





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8. Draw the graph of  $y = |\{x\} - 0.5|$ , where  $\{.\}$  represents the fractional part function.



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9. The number of real solution of the equation  $\sqrt{1 + \cos 2x} = \sqrt{2} \sin^{-1}(\sin x)$ ,  $-\pi < x < \pi$  is



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**10.** Find the number of real solutions to the equation

$$\log_{0.5} x = |x|.$$



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**11.** Find the number of points where the function

$$f(x) = \max \{|\tan x|, \cos|x|\}$$
 is non-differentiable in

the interval  $(-\pi, \pi)$ .



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**12.** Find the number of points of non-differentiability for

$$f(x) = \max \{||x| - 1|, 1/2\}.$$



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13. Let  $f(x) = \max . \{ |x^2 - 2|x||, |x| \}$  then number of points where  $f(x)$  is non derivable, is :



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14. Draw the graph of  $|y| = [x]$ , where  $[.]$  represents the greatest integer function.



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