



# MATHS

# **BOOKS - CENGAGE**

# **INTRODUCTION TO VECTORS**

#### **Examples**

**1.** The vector  $\overrightarrow{a} + \overrightarrow{b}$  bisects the angle between the vectors  $\widehat{a}$  and  $\widehat{b}$  if (A)  $\left|\overrightarrow{a}\right| + \left|\overrightarrow{b}\right| = 0$  (B) angle between  $\overrightarrow{a}$  and  $\overrightarrow{b}$  is zero (C)  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are equal vector (D) none of these

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**2.** if  $\overrightarrow{A}o + \overrightarrow{O}B = \overrightarrow{B}O + \overrightarrow{O}C$ , than prove that B is the midpoint of AC.

**3.** ABCDE is pentagon, prove that  $\overrightarrow{A}B + \overrightarrow{B}C + \overrightarrow{C}D + \overrightarrow{D}E + \overrightarrow{E}A = \overrightarrow{0}$  $\overrightarrow{A}B + \overrightarrow{A}E + \overrightarrow{B}C + \overrightarrow{D}C + \overrightarrow{E}D + \overrightarrow{A}C = 3\overrightarrow{A}C$ 



**4.** Prove that the resultant of two forces acting at point O and represented by  $\overrightarrow{OB}$  and  $\overrightarrow{OC}$  is given by  $2\overrightarrow{OD}$ , where D is the midpoint of BC.

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5. Prove that the sum of three vectors determined by the medians of a

triangle directed from the vertices is zero.



**6.** ABC is a triangle and P any point on BC. if  $\overrightarrow{P}Q$  is the sum of  $\overrightarrow{A}P + \overrightarrow{P}B$ + $\overrightarrow{P}C$ , show that ABPQ is a parallelogram and Q, therefore, is a fixed point.

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7. Two forces  $\overrightarrow{A}B$  and  $\overrightarrow{A}D$  are acting at vertex A of a quadrilateral ABCD and two forces  $\overrightarrow{C}B$  and  $\overrightarrow{C}D$  at C prove that their resultant is given by 4  $\overrightarrow{E}F$ , where E and F are the midpoints of AC and BD, respectively.

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8. If  $O(\overrightarrow{0})$  is the circumcentre and O' the orthocentre of a triangle ABC, then prove that i.  $\overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC} = \overrightarrow{OO'}$ ii.  $\overrightarrow{O'A} + \overrightarrow{O'B} + \overrightarrow{O'C} = 2\overrightarrow{O'O}$ 

iii. 
$$AO^{'} + O^{'}\dot{B} + O^{'}\dot{C} = 2A\dot{O} = A\dot{P}$$

where AP is the diameter through A of the circumcircle.

**9.** A unit vector of modulus 2 is equally inclined to x - and y -axes angle at

an angle  $\pi/3$  . Find the length of projection of the vector on the z -axis.

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**10.** If the projections of vector  $\overrightarrow{a}$  on x -, y - and z -axes are 2, 1 and 2 units ,respectively, find the angle at which vector  $\overrightarrow{a}$  is inclined to the z -axis.

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11. Find a vector of magnitude 8 units in the direction of the vector  $\Bigl(5\hat{i}-\hat{j}+2\hat{k}\Bigr).$ 

12. सदिश  $\overline{PQ}$ , के अनुदिश मात्रक सदिश ज्ञात कीजिए जहाँ बिंदु P और Q क्रमश: (1,2,3) और

(4,5,6) है!

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**13.** If 
$$\overrightarrow{a} = \left(-\hat{i} + \hat{j} - \hat{k}\right)$$
 and  $\overrightarrow{b} = \left(2\hat{i} - 2\hat{j} + 2\hat{k}\right)$  then find the unit vector in the direction of  $\left(\overrightarrow{a} + \overrightarrow{b}\right)$ .

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14. Show that the points A,B and C with position vectors , $\overrightarrow{a} = 3\hat{i} - 4\hat{j} - 4\hat{k}, \overrightarrow{b} = 2\hat{i} - \hat{j} + \hat{k}$  and  $\overrightarrow{c} = \hat{i} - 3\hat{j} = 5\hat{k}$ 

,respectively form the vertices of a right angled triangle.

**15.** If  $2\overrightarrow{A}C = 3\overrightarrow{C}B$ , then prove that  $2\overrightarrow{O}A = 3\overrightarrow{C}B$  then prove that  $2\overrightarrow{O}A + 3\overrightarrow{O}B = 5\overrightarrow{O}C$  where O is the origin.



16. Prove that points  $\hat{i}+2\hat{j}-3\hat{k}, 2\hat{i}-\hat{j}+\hat{k}$  and  $2\hat{i}+5\hat{j}-\hat{k}$  form a

triangle in space.

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17. Find the position vector of a point R which divides the line joining two points P and Q whose position vectors are  $\hat{i} + 2\hat{j} - \hat{k}$  and  $-\hat{i} + \hat{j} + \hat{k}$ respectively, in the ratio 2 : 1

(i) internally (ii) externally



**18.** If  $\overrightarrow{a}, \overrightarrow{b}, \overrightarrow{c}, \overrightarrow{d}$  are the position vectors of points A, B, C and D, respectively referred to the same origin O such that no three of these points are collinear and  $\overrightarrow{a} + \overrightarrow{c} = \overrightarrow{b} + \overrightarrow{d}$ , then prove that quadrilateral ABCD is a parallelogram.

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**19.** Find the point of intersection of AB and A( 6,-7,0),B(16,-19,-4,) , C(0,3,-6)

and D(2,-5,10).

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**20.** Find the angle of vector  $\overrightarrow{a} = 6\hat{i} + 2\hat{j} - 3\hat{k}$  with x -axis.

**21.** The lines joining the vertices of a tetrahedron to the centroids of opposite faces are concurrent.



**22.** The midpoint of two opposite sides of a quadrilateral and the midpoint of the diagonals are the vertices of a parallelogram. Prove that using vectors.

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**23.** Check whether the three vectors 
$$2\hat{i} + 2\hat{j} + 3\hat{k}, \vec{b} = -3\hat{i} + 3\hat{j} + 2\hat{k}$$
 and  $\vec{c} = 3\hat{i} + 4\hat{k}$  form a triangle or not.

**24.** Find the resultant of vectors  $\vec{a} = \hat{i} - \hat{j} + 2\hat{k}$  and  $\vec{b} = \hat{i} + 2\hat{j} - 4\hat{k}$ . Find the unit vector in the direction of the resultant vector.

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**25.** If in parallelogram ABCD, diagonal vectors are  $\overrightarrow{A}C = 2\hat{i} + 3\hat{j} + 4\hat{k}$ and  $\overrightarrow{B}D = -6\hat{i} + 7\hat{j} - 2\hat{k}$ , then find the adjacent side vectors  $\overrightarrow{A}B$ and  $\overrightarrow{A}D$ 

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**26.** If two side of a triangle are  $\hat{i} + 2\hat{j}and\hat{i} + \hat{k}$  , then find the length of

the third side.

**27.** Three coinitial vectors of magnitudes a, 2a and 3a meet at a point and their directions are along the diagonals if three adjacent faces if a cube. Determined their resultant R. Also prove that the sum of the three vectors determinate by the diagonals of three adjacent faces of a cube passing through the same corner, the vectors being directed from the corner, is twice the vector determined by the diagonal of the cube.

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**28.** The axes of coordinates are rotated about the z-axis though an angle of  $\pi/4$  in the anticlockwise direction and the components of a vector are  $2\sqrt{2}$ ,  $3\sqrt{2}$ , 4. Prove that the components of the same vector in the original system are -1,5,4.

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**29.** If the resultant of two forces is equal in magnitude to one of the components and perpendicular to it direction, find the other components

using the vector method.

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**30.** A man travelling towards east at 8km/h finds that the wind seems to blow directly from the north On doubling the speed, he finds that it appears to come from the north-east. Find the velocity of the wind.

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**31.** OABCDE is a regular hexagon of side 2 units in the XY-plane in the first quadrant. O being the origin and OA taken along the x-axis. A point P is taken on a line parallel to the z-axis through the centre of the hexagon at a distance of 3 unit from O in the positive Z direction. Then find vector AP.

**32.** If  $\overrightarrow{a} = 7\hat{i} - 4\hat{j} - 4\hat{k}$  and  $\overrightarrow{b} = -2\hat{i} - \hat{j} + 2\hat{k}$ , determine vector  $\overrightarrow{c}$  along the internal bisector of the angle between vectors  $\overrightarrow{a}$  and  $\overrightarrow{b}$  such that  $\left|\overrightarrow{c}\right| = 5\sqrt{6}$ .

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**33.** Find a unit vector  $\overrightarrow{c}$  if  $-\hat{i} + \hat{j} - \hat{k}$  bisects the angle between vectors  $\overrightarrow{c}$  and  $3\hat{i} + 4\hat{j}$ .

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**34.** The vectors  $2i+3\hat{j},5\hat{i}+6\hat{j}$  and  $8\hat{i}+\lambda\hat{j}$  have initial points at (1, 1).

Find the value of  $\lambda$  so that the vectors terminate on one straight line.

**35.** If  $\overrightarrow{a}$ ,  $\overrightarrow{b}$  and  $\overrightarrow{c}$  are three non-zero vectors, no two of which are collinear,  $\overrightarrow{a} + 2\overrightarrow{b}$  is collinear with  $\overrightarrow{c}$  and  $\overrightarrow{b} + 3\overrightarrow{c}$  is collinear with  $\overrightarrow{a}$ , then find the value of  $\left|\overrightarrow{a} + 2\overrightarrow{b} + 6\overrightarrow{c}\right|$ .

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**36.** Let  $A=(1,2,3), B=(3,\ -1,5), C=(4,0,\ -3)$ , then  $\angle A$  is

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37. Check whether the given three vectors are coplanar or non-coplanar.

$$-2\hat{i}-2\hat{j}+4\hat{k},\ -2\hat{i}+4\hat{j},4\hat{i}-2\hat{j}-2\hat{k}$$





#### in space.



**39.** If  $\overrightarrow{a} and \overrightarrow{b}$  are two non-collinear vectors, show that points  $l_1\overrightarrow{a} + m_1\overrightarrow{b}, l_2\overrightarrow{a} + m_2\overrightarrow{b}$  and  $l_3\overrightarrow{a} + m_3\overrightarrow{b}$  are collinear if  $|l_1l_2l_3m_1m_2m_3111| = 0.$ 

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**40.** The vectors  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are non collinear. Find for what value of x the vectors  $\overrightarrow{c} = (x-2)\overrightarrow{a} + \overrightarrow{b}$  and  $\overrightarrow{d} = (2x+1)\overrightarrow{a} - \overrightarrow{b}$  are collinear.?

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41. The median AD of the triangle ABC is bisected at E and BE meets AC at

F. Find AF:FC.

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**42.** Prove that the necessary and sufficient condition for any four points in three-dimensional space to be coplanar is that there exists a liner relation connecting their position vectors such that the algebraic sum of the coefficients (not all zero) in it is zero.



**43.** If the four points with position vectors  $-2\hat{i}+\hat{j}+\hat{k},\,\hat{i}+\hat{j}+\hat{k},\,\hat{j}-\hat{k}$  and  $\lambda\hat{j}+\hat{k}$  are coplanar, then  $\lambda=$ 

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**44.** If  $\overrightarrow{a}$ ,  $\overrightarrow{b}$  and  $\overrightarrow{c}$  are non-coplanar vectors, prove that the four points  $2\overrightarrow{a} + 3\overrightarrow{b} - \overrightarrow{c}$ ,  $\overrightarrow{a} - 2\overrightarrow{b} + 3\overrightarrow{c}$ ,  $3\overrightarrow{a} + 4\overrightarrow{b} - 2\overrightarrow{c}$  and  $\overrightarrow{a} - 6\overrightarrow{b} + 6\overrightarrow{c}$  are coplanar.

**45.** Let P be an interior point of a triangle ABC and AP, BP, CP meet the sides BC, CA, AB in D, E, F, respectively. Show that  $\frac{AP}{PD} = \frac{AF}{FB} + \frac{AE}{EC}$ .

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**46.** Points 
$$A(\overrightarrow{a}), B(\overrightarrow{b}), C(\overrightarrow{c}) and D(\overrightarrow{d})$$
 are relates as  $x\overrightarrow{a} + y\overrightarrow{b} + z\overrightarrow{c} + w\overrightarrow{d} = 0$  and

x + y + z + w = 0, where x, y, z, and w are scalars (sum of any two of

x, y, znadw is not zero). Prove that if A, B, CandD are concylic, then

$$|xy| igg| ec{a} - ec{b} igg|^2 = |wz| igg| ec{c} - ec{d} igg|^2.$$

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### Exercise 11

1. Find the unit vector in the direction of the vector  $\overrightarrow{a} = \hat{i} + \hat{j} + 2\hat{k}.$ 





**3.** Find the direction cosines of the vector joining the points A(1, 2,3) and

B(-1, -2, 1) directed from A to B.

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**4.** The position vectors of PandQ are 5 $\hat{i}$  +  $4\hat{j}$  +  $a\hat{k}$  and  $-\hat{i}$  +  $2\hat{j}$  -  $2\hat{k}$  ,

respectively. If the distance between them is 7, then find the value of a.

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5. Given three points are A(-3, -2, 0), B(3, -3, 1) and C(5, 0, 2). Then find a vector having the same direction as that of  $\overrightarrow{AB}$  and magnitude equal to  $|\overrightarrow{A}C|$ .

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6. Find a vector of magnitude 5 units and parallel to the resultant of the

vectors 
$$\overrightarrow{a} = 2\hat{i} + 3\hat{j} - \hat{k}$$
 and  $\overrightarrow{b} = \hat{i} - 2\hat{j} + \hat{k}$ .

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7. Show that the points A(1, -2, -8) B (5, 0, -2) and C(11, 3, 7) are collinear

and find the ratio in which B divides AC.

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8. If ABCD is a rhombus whose diagonals cut at the origin O, then proved that  $\overrightarrow{O}A + \overrightarrow{O}B + \overrightarrow{O}C + \overrightarrow{O}D + \overrightarrow{O}$ .

**9.** Let D, EandF be the middle points of the sides BC, CAandAB, respectively of a triangle ABC. Then prove that  $\overrightarrow{A}D + \overrightarrow{B}E + \overrightarrow{C}F = \overrightarrow{0}$ .

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**10.** Let ABCD be a p[arallelogram whose diagonals intersect at P and let O be the origin. Then prove that  $\overrightarrow{O}A + \overrightarrow{O}B + \overrightarrow{O}C + \overrightarrow{O}D = 4\overrightarrow{O}P$ .

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**11.** If ABCD is quadrilateral and EandF are the mid-points of ACandBD respectively, prove that  $\overrightarrow{A}B + \overrightarrow{A}D + \overrightarrow{C}B + \overrightarrow{C}D = 4\overrightarrow{E}F$ .

**12.** If  $\overrightarrow{A}O + \overrightarrow{O}B = \overrightarrow{B}O + \overrightarrow{O}C$ , then A, BnadC are (where O is the origin) a. coplanar b. collinear c. non-collinear d. none of these

**13.** If the sides of an angle are given by vectors  $\vec{a} = \hat{i} - 2\hat{j} + 2\hat{k}$  and  $\vec{b} = 2\hat{i} + \hat{j} + 2\hat{k}$ , then find the internal bisector of the angle.

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14. ABCD is a parallelogram. If LandM are the mid-points of BCandDC respectively, then express  $\overrightarrow{A}Land\overrightarrow{A}M$  in terms of  $\overrightarrow{A}Band\overrightarrow{A}D$ . Also, prove that  $\overrightarrow{A}L + \overrightarrow{A}M = \frac{3}{2}\overrightarrow{A}C$ .

**15.** ABCD is a quadrilateral. E is the point of intersection of the line joining the midpoints of the opposite sides. If O is any point and  $\overrightarrow{O}A + \overrightarrow{O}B + \overrightarrow{O}C + \overrightarrow{O}D = x\overrightarrow{O}E$ , then x is equal to a. 3 b. 9 c. 7 d. 4

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**16.** What is the unit vector parallel to  $\vec{a} = 3\hat{i} + 4\hat{j} - 2\hat{k}$ ? What vector should be added to  $\vec{a}$  so that the resultant is the unit vector  $\hat{i}$ ?

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17. The position vectors of points AandB w.r.t. the origin are  $\vec{a} = \hat{i} + 3\hat{j} - 2\hat{k}$ , respectively. Determine vector  $\vec{O}P$  which bisects angle AOB, where P is a point on AB.

**18.** If  $\overrightarrow{r}_1, \overrightarrow{r}_2, \overrightarrow{r}_3$  are the position vectors off thee collinear points and scalar *pandq* exist such that  $\overrightarrow{r}_3 = p\overrightarrow{r}_1 + q\overrightarrow{r}_2$ , then show that p+q=1.

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**19.** If  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are two vectors of magnitude 1 inclined at  $120^{\circ}$ , then find the angle between  $\overrightarrow{b}$  and  $\overrightarrow{b} - \overrightarrow{a}$ .

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20. Find the vector of magnitude 3, bisecting the angle between the

vectors 
$$\overrightarrow{a} = 2\hat{i} + \hat{j} - \hat{k} \, ext{ and } \, \overrightarrow{b} = \hat{i} - 2\hat{j} + \hat{k}.$$



**1.** If  $\overrightarrow{a}$ ,  $\overrightarrow{b}$ ,  $\overrightarrow{c}$  and  $\overrightarrow{d}$  are four vectors in three-dimensional space with the same initial point and such that  $3\overrightarrow{a} + 2\overrightarrow{b} + \overrightarrow{c} - 2\overrightarrow{d} = 0$ , show that terminals A, B, CandD of these vectors are coplanar. Find the point at which ACandBD meet. Find the ratio in which P divides ACandBD.



$$\mathsf{ii.}\ 3\overrightarrow{i}+\overrightarrow{j}-\overrightarrow{k}, 2\overrightarrow{i}-\overrightarrow{j}+7\overrightarrow{k}, 7\overrightarrow{i}-\overrightarrow{j}+13\overrightarrow{k}$$

**4.** If  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are non-collinear vectors and  $\overrightarrow{A} = (p+4q)\overrightarrow{a} + (2p+q+1)\overrightarrow{b}$  and  $\overrightarrow{B} = (-2p+q+2)\overrightarrow{a} + (2p-3q)$ , and if  $3\overrightarrow{A} = 2\overrightarrow{B}$ , then determine p and q.

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5. If  $\overrightarrow{a}$ ,  $\overrightarrow{b}$  and  $\overrightarrow{c}$  are any three non-coplanar vectors, then prove that points  $l_1\overrightarrow{a} + m_1\overrightarrow{b} + n_1\overrightarrow{c}$ ,  $l_2\overrightarrow{a} + m_2\overrightarrow{b} + n_2\overrightarrow{c}$ ,  $l_3\overrightarrow{a} + m_3\overrightarrow{b} + n_3\overrightarrow{c}$ ,  $l_4\overrightarrow{a} + m_4$ are coplanar if  $\begin{vmatrix} l_1 & l_2 & l_3 & l_4 \\ m_1 & m_2 & m_3 & m_4 \\ n_1 & n_2 & n_3 & n_4 \\ 1 & 1 & 1 & 1 \end{vmatrix} = 0$ 

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**6.** If  $\overrightarrow{a}$ ,  $\overrightarrow{b}$  and  $\overrightarrow{c}$  are three non-zero, non-coplanar vectors, then find the linear relation between the following four vectors :

$$\overrightarrow{a} - 2\overrightarrow{b} + 3\overrightarrow{c}, 2\overrightarrow{a} - 3\overrightarrow{b} + 4\overrightarrow{c}, 3\overrightarrow{a} - 4\overrightarrow{b} + 5\overrightarrow{c}, 7\overrightarrow{a} - 11\overrightarrow{b} + 15\overrightarrow{c}$$

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7. Let a, b, c be distinct non-negative numbers and the vectors  $a\hat{i} + a\hat{j} + c\hat{k}$ ,  $\hat{i} + \hat{k}$ ,  $c\hat{i} + c\hat{j} + b\hat{k}$  lie in a plane, and then prove that the quadratic equation  $ax^2 + 2cx + b = 0$  has equal roots.

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#### **Exercise Subjective**

**1.** The position vectors of the vertices A, B and C of triangle are  $\hat{i} + \hat{j}, \hat{j} + \hat{k}$  and  $\hat{i} + \hat{k}$ , respectively. Find the unit vectors  $\hat{r}$  lying in the plane of ABC and perpendicular to IA, where I is the incentre of the triangle.

**2.** A ship is sailing towards the north at a speed of 1.25 m/s. The current is taking it towards the east at the rate of 1 m/s and a sailor is climbing a vertical pole on the ship at the rate of 0.5 m/s. Find the velocity of the sailor in space.

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**3.** A bag contains 2 red balls and 4 black balls. A ball is drawn at random

from the bag. What is the probability that the ball drawn is red?

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**4.** ABCD is a tetrahedron and O is any point. If the lines joining O to the vrticfes meet the opposite faces at P, Q, RandS, prove that  $\frac{OP}{AP} + \frac{OQ}{BQ} + \frac{OR}{CR} + \frac{OS}{DS} = 1.$ 

**5.** A pyramid with vertex at point P has a regular hexagonal bas ABCDEF, Positive vector  $\hat{i} + \hat{j} + \sqrt{3}\hat{k}$ . Altitude drawn from P on the base meets the diagonal AD at point G. find the all possible position vectors of G. It is given that the volume of the pyramid is  $6\sqrt{3}$  cubic units and AP is 5 units.

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**6.** A straight line L cuts the lines AB, ACandAD of a parallelogram

 $\begin{array}{ll} ABCD & \text{at} & \text{points} & B_1, C_1 and D_1, & \text{respectively.} & \text{If} \\ \left( \stackrel{\rightarrow}{A}B \right)_1, \lambda_1 \stackrel{\rightarrow}{A}B, \left( \stackrel{\rightarrow}{A}D \right)_1 = \lambda_2 \stackrel{\rightarrow}{A} Dand \left( \stackrel{\rightarrow}{A}C \right)_1 = \lambda_3 \stackrel{\rightarrow}{A}C, \text{ then prove} \\ \text{that} \ \frac{1}{\lambda_3} = \frac{1}{\lambda_1} + \frac{1}{\lambda_2} \,. \end{array}$ 

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7. The position vector of the points PandQ are  $5\hat{i} + 7\hat{j} - 2\hat{k}$  and  $-3\hat{i} + 3\hat{j} + 6\hat{k}$ , respectively. Vector  $\overrightarrow{A} = 2\hat{i} - \hat{j} + \hat{k}$  passes through point P and vector  $\overrightarrow{B} = 3\hat{i} + 2\hat{j} + 4\hat{k}$  passes through point Q. A third

vector  $2\hat{i}+7\hat{j}-5\hat{k}$  intersects vectors AandB Find the position vectors

of points of intersection.

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**8.** Sow that 
$$x_1\hat{i}+y_1\hat{j}+z_1\hat{k}, x_2\hat{i}+y_2\hat{j}+z_2\hat{k}, and x_3\hat{i}+y_3\hat{j}+z_3\hat{k},$$
 are

if

#### non-coplanar

 $|x_1|>|y_1|+|z_1|, |y_2|>|x_2|+|z_2| and |z_3|>|x_3|+|y_3|$  .

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**9.** If  $\overrightarrow{A} n d\overrightarrow{B}$  are two vectors and k any scalar quantity greater than zero, then prove that  $\left|\overrightarrow{A} + \overrightarrow{B}\right|^2 \leq (1+k)\left|\overrightarrow{A}\right|^2 + \left(1 + \frac{1}{k}\right)\left|\overrightarrow{B}\right|^2$ .

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 are different angles. If these vectors are coplanar, show that a is independent of  $\alpha, \beta, and\gamma$ .

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11. In a triangle PQR, SandT are points on QRandPR, respectively, such that QS = 3SRandPT = 4TR. Let M be the point of intersection of PSandQT. Determine the ratio QM:MT using the vector method.

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12. A boat moves in still water with a velocity which is k times less than the river flow velocity. Find the angle to the stream direction at which the boat should be rowed to minimize drifting.

**13.** If D, EandF are three points on the sides BC, CAandAB, respectively, of a triangle ABC such that the  $\frac{BD}{CD}$ ,  $\frac{CE}{AE}$ ,  $\frac{AF}{BF} = -1$ 

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14. In a quadrilateral PQRS,  $\overrightarrow{P}Q = \overrightarrow{a}$ ,  $\overrightarrow{Q}R$ ,  $\overrightarrow{b}$ ,  $\overrightarrow{S}P = \overrightarrow{a} - \overrightarrow{b}$ , M is the midpoint of  $\overrightarrow{Q}RandX$  is a point on SM such that  $SX = \frac{4}{5}SM$ . Prove that P, XandR are collinear.

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#### **Exercise Single**

**1.** Four non zero vectors will always be a. linearly dependent b. linearly independent c. either a or b d. none of these

A. linearly dependent

B. linearly independent

C. either a or b

D. none of these

Answer: A

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2. Let  $\overrightarrow{a}, \overrightarrow{b}, \overrightarrow{c}$  be three unit vectors such that  $3\overrightarrow{a} + 4\overrightarrow{b} + 5\overrightarrow{c} = \overrightarrow{0}$ . Then which of the following statements is true? (A)  $\overrightarrow{a}$  is parallel to vecb (B)vecaisperpendic<u>a</u> $r \rightarrow \overrightarrow{b}$  (C)  $\overrightarrow{a}$  is neither paralel nor perpendicular to  $\overrightarrow{b}$  (D)  $\overrightarrow{a}, \overrightarrow{b}, \overrightarrow{c}$  are copalanar A.  $\overrightarrow{a}$  is parallel to  $\overrightarrow{b}$ B.  $\overrightarrow{a}$  is perpendicular to  $\overrightarrow{b}$ 

C.  $\overrightarrow{a}$  is neither parallel nor perpendicular to  $\overrightarrow{b}$ 

D. none of these

Answer: D



**3.** Let ABC be a triangle the position vectors of whose vertices are respectively  $\hat{i} + 2\hat{j} + 4\hat{k}$ ,  $-2\hat{i} + 2\hat{j} + \hat{k}$  and  $2\hat{i} + 4\hat{j} - 3\hat{k}$ . Then the  $\triangle ABC$  is (A) isosceles (B) equilateral (C) righat angled (D) none of these

A. isosceles

B. equilateral

C. right angled

D. none of these

#### Answer: C

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**4.** If 
$$\left| \overrightarrow{a} + \overrightarrow{b} \right| < \left| \overrightarrow{a} - \overrightarrow{b} \right|$$
, then the angle between  $\overrightarrow{a}$  and  $\overrightarrow{b}$  can lie in

the interval

A. 
$$(-\pi/2, \pi/2)$$
  
B.  $(0, \pi)$   
C.  $(\pi/2, 3\pi/2)$   
D.  $(0, 2\pi)$ 

#### Answer: C

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5. A point O is the centre of a circle circunscribed about a triangle ABC. Then,  $\overrightarrow{O}A\sin 2A + \overrightarrow{bO}B\sin 2B + \overrightarrow{O}C\sin 2C$  is equal to

A. 
$$\left(\overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC}\right)\sin 2A$$

B.  $3\overrightarrow{OG}$ , where G is the centroid of triangle ABC

 $\mathsf{C}.\stackrel{\rightarrow}{0}$ 

D. none of these

#### Answer: C



7. If  $\overrightarrow{a}$  is a non zero vecrtor iof modulus  $\overrightarrow{a}$  and m is a non zero scalar such that ma is a unit vector, write the value of m.

A. 
$$m=\pm 1$$

B. 
$$a = |m|$$
  
C.  $a = 1/|m|$   
D.  $a = rac{1}{m}$ 

#### Answer: C

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8. ABCD a parallelogram, and  $A_1$  and  $B_1$  are the midpoints of sides BC and CD, respectively. If  $\overrightarrow{AA_1} + \overrightarrow{AB_1} = \lambda \overrightarrow{AC}$ , then  $\lambda$  is equal to `

A. 
$$\frac{1}{2}$$

**B**. 1

C. 
$$\frac{3}{2}$$

 $\mathsf{D.}\,2$ 

#### Answer: C

9. The position vectors of the points PandQ with respect to the origin Oare  $\overrightarrow{a} = \hat{i} + 3\hat{j} - 2\hat{k}$  and  $\overrightarrow{b} = 3\hat{i} - \hat{j} - 2\hat{k}$ , respectively. If M is a point on PQ, such that OM is the beisector of POQ, then  $\overrightarrow{O}M$  is a.  $2(\hat{i} - \hat{j} + \hat{k})$  b.  $2\hat{i} + \hat{j} - 2\hat{k}$  c.  $2(-\hat{i} + \hat{j} - \hat{k})$  d.  $2(\hat{i} + \hat{j} + \hat{k})$ A.  $2(\hat{i} - \hat{j} + \hat{k})$ B.  $2\hat{i} + \hat{j} - 2\hat{k}$ C.  $2(-\hat{i} + \hat{j} - \hat{k})$ D.  $2(\hat{i} + \hat{j} + \hat{k})$ 

#### Answer: B

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**10.** *ABCD* is a quadrilateral. *E* is the point of intersection of the line joining the midpoints of the opposite sides. If *O* is any point and  $\overrightarrow{O}A + \overrightarrow{O}B + \overrightarrow{O}C + \overrightarrow{O}D = x\overrightarrow{O}E$ , then *x* is equal to a. 3 b. 9 c. 7 d. 4
A. 3	
B. 9	
C. 7	

# Answer: D

D. 4

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**11.** The vector  $\overrightarrow{AB} = 3\hat{i} + 4\hat{k}$  and  $\overrightarrow{AC} = 5\hat{i} - 2\hat{j} + 4\hat{k}$  are sides of a triangle ABC. The length of the median through A is (A)  $\sqrt{18}$  (B)  $\sqrt{72}$  (C)  $\sqrt{33}$  (D)  $\sqrt{288}$ 

- A.  $\sqrt{14}$
- B.  $\sqrt{18}$

C.  $\sqrt{29}$ 

D. 5

## Answer: B



**12.** A, B, C and D have position vectors  $\overrightarrow{a}$ ,  $\overrightarrow{b}$ ,  $\overrightarrow{c}$  and  $\overrightarrow{d}$ , repectively, such that  $\overrightarrow{a} - \overrightarrow{b} = 2\left(\overrightarrow{d} - \overrightarrow{c}\right)$ . Then

A. AB and CD bisect each other

B. BD and AC bisect each other

C. AB and CD trisect each other

D. BD and AC trisect each other

## Answer: D



**13.** If  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are two unit vectors and  $\theta$  is the angle between them, then the unit vector along the angular bisector of  $\overrightarrow{a}$  and  $\overrightarrow{b}$  will be given by

A. 
$$\frac{\overrightarrow{a} - \overrightarrow{b}}{2\cos(\theta/2)}$$
  
B. 
$$\frac{\overrightarrow{a} + \overrightarrow{b}}{2\cos(\theta/2)}$$
  
C. 
$$\frac{\overrightarrow{a} - \overrightarrow{b}}{\cos(\theta/2)}$$

D. none of these

#### Answer: B

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14. let us define , the length of a vector as |a|+|b|+|c|. this definition coincides with the usual definition of the length of a vector  $a\hat{i}+b\hat{j}+c\hat{k}$  if

A. a = b = c = 0

B. any two of a, b and c are zero

C. any one of a, b and c is zero

D. 
$$a + b + c = 0$$

#### Answer: B

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15. Given three vectors  $\overrightarrow{a} = 6\hat{i} - 3\hat{j}, \ \overrightarrow{b} = 2\hat{i} - 6\hat{j}$  and  $\overrightarrow{c} = -2\hat{i} + 21\hat{j}$  such that  $\overrightarrow{\alpha} = \overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c}$ . Then the resolution of te vector  $\overrightarrow{\alpha}$  into components with respect to  $\overrightarrow{a}$  and  $\overrightarrow{b}$  is given by (A)  $3\overrightarrow{a} - 2\overrightarrow{b}$  (B)  $2\overrightarrow{a} - 3\overrightarrow{b}$  (C)  $3\overrightarrow{b} - 2\overrightarrow{a}$  (D) none of these

A. 
$$3\overrightarrow{a} - 2\overrightarrow{b}$$
  
B.  $3\overrightarrow{b} - 2\overrightarrow{a}$   
C.  $2\overrightarrow{a} - 3\overrightarrow{b}$   
D.  $\overrightarrow{a} - 2\overrightarrow{b}$ 

#### Answer: C

**16.** If  $\overrightarrow{\alpha} + \overrightarrow{\beta} + \overrightarrow{\gamma} = a \overrightarrow{\delta} and \overrightarrow{\beta} + \overrightarrow{\gamma} + \overrightarrow{\delta} = b \overrightarrow{\alpha}, \overrightarrow{\alpha} and \overrightarrow{\delta}$  are noncolliner, then  $\overrightarrow{\alpha} + \overrightarrow{\beta} + \overrightarrow{\gamma} + \overrightarrow{\delta}$  equals a.  $a \overrightarrow{\alpha}$  b.  $b \overrightarrow{\delta}$  c. 0 d.  $(a + b) \overrightarrow{\gamma}$ 

A.  $a \overrightarrow{\alpha}$ B.  $b \overrightarrow{\delta}$ C. 0 D.  $(a + b) \overrightarrow{\gamma}$ 

## Answer: C

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**17.** In triangle ABC,  $\angle A = 30^{\circ}$ , H is the orthocenter and D is the midpoint of BC. Segment HD is produced to T such that HD = DT. The length AT is equal to a. 2BC b. 3BC c.  $\frac{4}{2}BC$  d. none of these

B. 3 BC

C. 
$$\frac{4}{3}BC$$

D. none of these

## Answer: A

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18. If  $P(\operatorname{not} E) = 0.25$ , what is the probability of E?

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**19.** Given three non-zero, non-coplanar vectors 
$$\overrightarrow{a}, \overrightarrow{b}$$
 and  $\overrightarrow{c}$ .  
 $\overrightarrow{r}_1 = p\overrightarrow{a} + q\overrightarrow{b} + \overrightarrow{c}$  and  $\overrightarrow{r}_2 = \overrightarrow{a} + p\overrightarrow{b} + q\overrightarrow{c}$ . If the vectors  
 $\overrightarrow{r}_1 + 2\overrightarrow{r}_2$  and  $2\overrightarrow{r}_1 + \overrightarrow{r}_2$  are collinear, then  $(p, q)$  is

A. (0, 0)

B. (1, -1)

C.(-1,1)

D. (1, 1)

Answer: D

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20. If the vectors  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are linearly independent and satisfying  $\left(\sqrt{3} an heta+1
ight)\overrightarrow{a}+\left(\sqrt{3} ext{sec}\, heta-2
ight)\overrightarrow{b}=\overrightarrow{0}$  ,then the most general

values of  $\theta$  are:

A. 
$$2n\pi - rac{\pi}{6}, n \in Z$$
  
B.  $2n\pi \pm rac{11\pi}{6}, n \in Z$   
C.  $n\pi \pm rac{\pi}{6}, n \in Z$   
D.  $2n\pi + rac{11\pi}{6}, n \in Z$ 

Answer: D

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**21.** In a trapezium, vector  $\overrightarrow{B}C = \alpha \overrightarrow{A}D$ . We will then find that  $\overrightarrow{p} = \overrightarrow{A}C + \overrightarrow{B}D$  is collinear with  $\overrightarrow{A}D$ . If  $\overrightarrow{p} = \mu \overrightarrow{A}D$ , then which of the following is true? a)  $\mu = \alpha + 2$  b)  $\mu + \alpha = 2$  c)  $\alpha = \mu + 1$  d)  $\mu = \alpha + 1$ 

A.  $\mu = lpha + 2$ B.  $\mu + lpha = 1$ C.  $lpha = \mu + 1$ 

D.  $\mu = lpha + 1$ 

#### Answer: D

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**22.** Vectors  $\overrightarrow{a} = \hat{i} + 2\hat{j} + 3\hat{k}$ ,  $\overrightarrow{b} = 2\hat{i} - \hat{j} + \hat{k}$  and  $\overrightarrow{c} = 3\hat{i} + \hat{j} + 4\hat{k}$  are so placed that the end point of one vector is the starting point of the next vector. Then the vectors are

A. not coplanar

B. coplanar but cannot form a triangle

C. coplanar and form a triangle

D. coplanar and can form a right-angled triangle

#### Answer: B

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**23.** Vectors  $\overrightarrow{a} = -4\hat{i} + 3\hat{k}$ ;  $\overrightarrow{b} = 14\hat{i} + 2\hat{j} - 5\hat{k}$  are laid off from one point. Vector  $\hat{d}$ , which is being laid of from the same point dividing the angle between vectors  $\overrightarrow{a} and \overrightarrow{b}$  in equal halves and having the magnitude  $\sqrt{6}$ , is a.  $\hat{i} + \hat{j} + 2\hat{k}$  b.  $\hat{i} - \hat{j} + 2\hat{k}$  c.  $\hat{i} + \hat{j} - 2\hat{k}$  d.  $2\hat{i} - \hat{j} - 2\hat{k}$ 

A.  $\hat{i}+\hat{j}+2\hat{k}$ B.  $\hat{i}-\hat{j}+2\hat{k}$ C.  $\hat{i}+\hat{j}-2\hat{k}$ D.  $2\hat{i}-\hat{j}-2\hat{k}$ 

## Answer: A



24. If  $\hat{i} - 3\hat{j} + 5\hat{k}$  bisects the angle between  $\hat{a}$  and  $-\hat{i} + 2\hat{j} + 2\hat{k}$ , where  $\hat{a}$  is a unit vector, then

$$\begin{array}{l} \mathsf{A.}\,\widehat{a} = \frac{1}{150} \Big( 41 \hat{i} + 88 \hat{j} - 40 \hat{k} \Big) \\ \mathsf{B.}\,\widehat{a} = \frac{1}{105} \Big( 41 \hat{i} + 88 \hat{j} + 40 \hat{k} \Big) \\ \mathsf{C.}\,\widehat{a} = \frac{1}{105} \Big( -41 \hat{i} + 88 \hat{j} - 40 \hat{k} \Big) \\ \mathsf{D.}\,\widehat{a} = \frac{1}{105} \Big( 41 \hat{i} - 88 \hat{j} - 40 \hat{k} \Big) \end{array}$$

#### Answer: D



25. If  $4\hat{i}+7\hat{j}+8\hat{k}, 2\hat{i}+3\hat{j}+4\hat{k}$  and  $2\hat{i}+5\hat{j}+7\hat{k}$  are the position

vectors of the vertices A, B and C, respectively, of triangle ABC, then the

position vector of the point where the bisector of angle A meets BC is

A. 
$$rac{2}{3}\Big(-6\hat{i}-8\hat{j}-6\hat{k}\Big)$$
  
B.  $rac{2}{3}\Big(6\hat{i}+8\hat{j}+6\hat{k}\Big)$   
C.  $rac{1}{3}\Big(6\hat{i}+13\hat{j}+18\hat{k}\Big)$   
D.  $rac{1}{3}\Big(5\hat{j}+12\hat{k}\Big)$ 

### Answer: C

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**26.** If  $\overrightarrow{b}$  is a vector whose initial point divides the join of  $5\hat{i}and5\hat{j}$  in the ratio k:1 and whose terminal point is the origin and  $\left|\overrightarrow{b}\right| \leq \sqrt{37}$ , thenk lies in the interval a. [-6, -1/6] b.  $(-\infty, -6] \cup [-1/6, \infty)$  c. [0, 6] d. none of these

)

A. 
$$[\,-6,\ -1/16]$$
  
B.  $(\,-\infty,\ -6]\cup[\,-1/6,\infty]$   
C.  $[0,6]$ 

### D. none of these

#### Answer: B

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27. Find the value of  $\lambda$  so that the points P, Q, RandS on the sides OA, OB, OCandAB, respectively, of a regular tetrahedron OABC are coplanar. It is given that  $\frac{OP}{OA} = \frac{1}{3}, \frac{OQ}{OB} = \frac{1}{2}, \frac{OR}{OC} = \frac{1}{3}and\frac{OS}{AB} = \lambda$ . a.  $\lambda = \frac{1}{2}$  b.  $\lambda = -1$  c.  $\lambda = 0$  d. for no value of  $\lambda$ A.  $\lambda = \frac{1}{2}$ B.  $\lambda = -1$ 

 $\mathsf{C}.\,\lambda=0$ 

D. for no value of  $\lambda$ 

#### Answer: B

28. 'I' is the incentre of triangle 
$$ABC$$
 whose corresponding sides are  
 $a, b, c$ , rspectively.  $a\overrightarrow{I}A + b\overrightarrow{I}B + c\overrightarrow{I}C$  is always equal to  $a$ .  $\overrightarrow{0}$  b.  
 $(a + b + c)\overrightarrow{B}C$  c.  $(\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c})\overrightarrow{A}C$  d.  $(a + b + c)\overrightarrow{A}B$   
A.  $\overrightarrow{0}$   
B.  $(a + b + c)\overrightarrow{BC}$   
C.  $(\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c})\overrightarrow{AC}$   
D.  $(a + b + c)\overrightarrow{AB}$ 

#### Answer: A

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**29.** Let  $x^2 + 3y^2 = 3$  be the equation of an ellipse in the x - y plane. AandB are two points whose position vectors are  $-\sqrt{3}\hat{i}and - \sqrt{3}\hat{i} + 2\hat{k}$ . Then the position vector of a point P on the ellipse such that  $\angle APB = \pi/4$  is a.  $\pm \hat{j}$  b.  $\pm (\hat{i} + \hat{j})$  c.  $\pm \hat{i}$  d. none of these A.  $\pm \, \hat{j}$ 

 $\mathsf{B.}\pm\left(\hat{i}+\hat{j}
ight)$ 

 $\mathsf{C}.\pm\hat{i}$ 

D. none of these

## Answer: A

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**30.** Locus of the point P, for which  $\overrightarrow{OP}$  represents a vector with direction cosine  $\cos \alpha = \frac{1}{2}$  (where O is the origin) is

A. a circle parallel to the y-z plane with centre on the x-axis

B. a conic concentric with the positive x-axis having vertex at the

origin and slant height equal to the magnitude of the vector

C. a ray emanating from the origin and making an angle of  $60^{\,\circ}$  with



D. a dise parallel to the y-z plane with centre on the x-axis and radius

equal to  $\left| \overrightarrow{OP} \right| \sin 60^{\circ}$ .

Answer: B

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**31.** If  $\overrightarrow{x}$  and  $\overrightarrow{y}$  are two non-collinear vectors and ABC is a triangle with side lengths a,b and c satisfying (20a-15b) $\overrightarrow{x}$  + (15b-12c) $\overrightarrow{y}$  + (12c-20a)  $\overrightarrow{x} \times \overrightarrow{y} = 0$  is:

A. an acute-angled triangle

B. an obtuse-angled triangle

C. a right-angled triangle

D. an isosceles triangle

Answer: D

**32.** A uni-modular tangent vector on the curve  

$$x = t^2 + 2, y = 4t - 5, z = 2t^2 - 6t = 2$$
 is a.  $\frac{1}{3}(2\hat{i} + 2\hat{j} + \hat{k})$  b.  
 $\frac{1}{3}(\hat{i} - \hat{j} - \hat{k})$  c.  $\frac{1}{6}(2\hat{i} + \hat{j} + \hat{k})$  d.  $\frac{2}{3}(\hat{i} + \hat{j} + \hat{k})$   
A.  $\frac{1}{3}(2\hat{i} + 2\hat{j} + \hat{k})$   
B.  $\frac{1}{3}(\hat{i} - \hat{j} - \hat{k})$   
C.  $\frac{1}{6}(2\hat{i} + \hat{j} + \hat{k})$   
D.  $\frac{2}{3}(\hat{i} + \hat{j} + \hat{k})$ 

#### Answer: A

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**33.** If  $\overrightarrow{x}$  and  $\overrightarrow{y}$  are two non-collinear vectors and a, b and c represent the sides of a  $\Delta ABC$  satisfying  $(a-b)\overrightarrow{x} + (b-c)\overrightarrow{y} + (c-a)(\overrightarrow{\times} x\overrightarrow{y}) = 0$ , then  $\Delta ABC$  is (where  $\overrightarrow{x} \times \overrightarrow{y}$  is perpendicular to the plane of  $\overrightarrow{x}$  and  $\overrightarrow{y}$ ) A. an acute-angled triangle

- B. an obtuse-angled triangle
- C. a right-angled triangle
- D. a scalene triangle

#### Answer: A

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**34.**  $\overrightarrow{A}$  is a vector with direction cosines  $\cos \alpha$ ,  $\cos \beta$  and  $\cos \gamma$ . Assuming the y - z plane as a mirror, the directin cosines of the reflected image of  $\overrightarrow{A}$  in the plane are a.  $\cos \alpha$ ,  $\cos \beta$ ,  $\cos \gamma$  b.  $\cos \alpha$ ,  $-\cos \beta$ ,  $\cos \gamma$  c.  $-\cos \alpha$ ,  $\cos \beta$ ,  $\cos \gamma$  d.  $-\cos \alpha$ ,  $-\cos \beta$ ,  $-\cos \gamma$ 

A.  $\cos \alpha$ ,  $\cos \beta$ ,  $\cos \gamma$ 

B.  $\cos \alpha$ ,  $-\cos \beta$ ,  $\cos \gamma$ 

 $\mathsf{C}.-\coslpha,\coseta,\cos\gamma$ 

 $\mathsf{D.}-\coslpha,\ -\coseta,\ -\cos\gamma$ 

## Answer: C



**Exercise Multiple** 



Answer: A::B::C::D

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**2.** The sides of a parallelogram are  $2\hat{i}+4\hat{j}-5\hat{k}$  and  $\hat{i}+2\hat{j}+3\hat{k}$ . The

unit vector parallel to one of the diagonals is

A. 
$$rac{1}{7} \Big( 3 \hat{i} + 6 \hat{j} - 2 \hat{k} \Big)$$
  
B.  $rac{1}{7} \Big( 3 \hat{i} - 6 \hat{j} - 2 \hat{k} \Big)$   
C.  $rac{1}{\sqrt{69}} \Big( \hat{i} + 2 \hat{j} + 8 \hat{k} \Big)$   
D.  $rac{1}{\sqrt{69}} \Big( - \hat{i} - 2 \hat{j} + 8 \hat{k} \Big)$ 

#### Answer: A::D

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**3.** The vector  $\overrightarrow{a}$  has the components 2p and 1 w.r.t. a rectangular Cartesian system. This system is rotated through a certain angel about the origin in the counterclockwise sense. If, with respect to a new system,  $\overrightarrow{a}$  has components (p+1)and1, then p is equal to a. -4 b. -1/3 c. 1 d.

 $\mathsf{A.}-1$ 

 $\mathsf{B.}-1/3$ 

**C**. 1

 $\mathsf{D.}\,2$ 

## Answer: B::C

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**4.** If points 
$$\hat{i}+\hat{j},\,\hat{i}-\hat{j}\,\, ext{and}\,\,p\hat{i}+q\hat{j}+r\hat{k}$$
 are collinear, then

A. p=1

 $\mathsf{B.}\,r=0$ 

 $\mathsf{C}.\,q\in R$ 

D. q 
eq 1

## Answer: A::B::D

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5. If  $\overrightarrow{a}$ ,  $\overrightarrow{b}$ ,  $\overrightarrow{c}$  are non coplanar vectors and  $\lambda$  is a real number, then the vectors  $\overrightarrow{a} + 2\overrightarrow{b} + 3\overrightarrow{c}$ ,  $\lambda\overrightarrow{b} + 4c^{\rightarrow}$  and  $(2\lambda - 1)\overrightarrow{c}$  are non coplanar for

A.  $\lambda \in R$ B.  $\lambda = rac{1}{2}$ 

 $\mathsf{C}.\,\lambda=0$ 

D. no value of  $\lambda$ 

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## Answer: A::B::C

**6.** If the resultant of three forces  $\overrightarrow{F}_1 = p\hat{i} + 3\hat{j} - \hat{k}, \overrightarrow{F}_2 = 6\hat{i} - \hat{k}$  and  $\overrightarrow{F}_3 = -5\hat{i} + \hat{j} + 2\hat{k}$  acting on a particle has a magnitude equal to 5 units, then the value of p is

$$\mathsf{A.}-6$$

 $\mathsf{B.}-4$ 

D. 4

### Answer: B::C

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7. If the vectors  $\hat{i} - \hat{j}$ ,  $\hat{j} + \hat{k}$  and  $\overrightarrow{a}$  form a triangle then  $\overrightarrow{a}$  may be (A)  $-\hat{i} - \hat{k}$  (B)  $\hat{i} - 2\hat{j} - \hat{k}$  (C)  $2\hat{i} + \hat{j} + \hat{j}k$  (D) hati+hatk`

A.  $-\hat{i}-\hat{k}$ 

B.  $\hat{i}-2\hat{j}-\hat{k}$ 

C.  $2\hat{i}+\hat{j}+\hat{k}$ 

D.  $\hat{i}+\hat{k}$ 

Answer: A::B::D

8. The vector  $\hat{i} + x\hat{j} + 3\hat{k}$  is rotated through an angle  $\theta$  and doubled in magnitude, then it becomes  $4\hat{i} + (4x - 2)\dot{\hat{j}} + 2\hat{k}$ . Then value of x are  $-\frac{2}{3}$  (b)  $\frac{1}{3}$  (c)  $\frac{2}{3}$  (d) 2 A. 1

B. -2/3

C.2

D. 4/3

## Answer: B::C



**9.**  $\overrightarrow{a}, \overrightarrow{b}$  and  $\overrightarrow{c}$  are three coplanar unit vectors such that  $\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c} = 0$ . If three vectors  $\overrightarrow{p}, \overrightarrow{q}$  and  $\overrightarrow{r}$  are parallel to  $\overrightarrow{a}, \overrightarrow{b}$  and  $\overrightarrow{c}$ , respectively, and have integral but different magnitudes,

then among the following options,  $|\overrightarrow{p} + \overrightarrow{q} + \overrightarrow{r}|$  can take a value equal to A. 1 B. 0 C.  $\sqrt{3}$ D. 2 Answer: C::D

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**10.** If non-zero vectors  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are equally inclined to coplanar vector  $\overrightarrow{c}$ , then  $\overrightarrow{c}$  can be

A. 
$$\frac{\left|\overrightarrow{a}\right|}{\left|\overrightarrow{a}\right| + 2\left|\overrightarrow{b}\right|}\overrightarrow{a} + \frac{\left|\overrightarrow{b}\right|}{\left|\overrightarrow{a}\right| + \left|\overrightarrow{b}\right|}\overrightarrow{b}$$
  
B. 
$$\frac{\left|\overrightarrow{b}\right|}{\left|\overrightarrow{a}\right| + \left|\overrightarrow{b}\right|}\overrightarrow{a} + \frac{\left|\overrightarrow{a}\right|}{\left|\overrightarrow{a}\right| + \left|\overrightarrow{b}\right|}\overrightarrow{b}$$



#### Answer: B::D



11. If A(-4, 0, 3)andB(14, 2, -5), then which one of the following points lie on the bisector of the angle between  $\overrightarrow{O}Aand\overrightarrow{O}B(O$  is the origin of reference )? a. (2, 2, 4) b. (2, 11, 5) c. (-3, -3, -6) d. (1, 1, 2)

A. (2, 2, 4)B. (2, 11, 5)C. (-3, -3, -6)D. (1, 1, 2)

## Answer: A::C::D

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12. In a four-dimensional space where unit vectors along the axes are  $\hat{i}, \hat{j}, \hat{k}and\hat{l}, and\overrightarrow{a}_1, \overrightarrow{a}_2, \overrightarrow{a}_3, \overrightarrow{a}_4$  are four non-zero vectors such that no vector can be expressed as a linear combination of others and  $(\lambda - 1)(\overrightarrow{a}_1 - \overrightarrow{a}_2) + \mu(\overrightarrow{a}_2 + \overrightarrow{a}_3) + \gamma(\overrightarrow{a}_3 + \overrightarrow{a}_4 - 2\overrightarrow{a}_2) + \overrightarrow{a}_3 + \delta\overrightarrow{a}_4$ then a.  $\lambda = 1$  b.  $\mu = -2/3$  c.  $\gamma = 2/3$  d.  $\delta = 1/3$ 

- A.  $\lambda=1$
- $\mathsf{B.}\,\mu=\,-\,2\,/\,3$
- C.  $\gamma=2/3$
- D.  $\delta=1/3$

#### Answer: A::B::D

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**13.** Let ABC be a triangle, the position vectors of whose vertices are respectively

 $\hat{7j} + 10\hat{k}, \ -\hat{i} + 6\hat{j} + 6\hat{k} \ ext{ and } \ -4\hat{i} + 9\hat{j} + 6\hat{k}. \ ext{ Then, } \ \Delta ABC$  is

A. isosceles

B. equilateral

C. right angled

D. none of these

Answer: A::C

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**Exercise Reasoning Questions** 

**1.** Each question has four choices a, b, c, and d, out of which only one is correct. Each question contains STATEMENT 1 and STATEMENT 2. a. Both the statements are TRUE and statement 2 is the correct explanation for

Statement 1. b. Both the statements are TRUE but Statement 2 is NOT the correct explanation for Statement 1. c. Statement 1 is TRUE and Statement 2 is FALSE. d. Statement 1 is FALSE and Statement 2 is TRUE. A vector has components p and 1 with respect to a rectangular Cartesian system. The axes are rotted through an angel  $\alpha$  about the origin the anticlockwise sense. Statement 1: IF the vector has component p + 2 and 1 with respect to the new system, then p = -1. Statement 2: Magnitude of the origin vector and the new vector remains the same.

- A. Both the statements are true, and Statement 2 is the correct explanation for Statement 1.
- B. Both the statements are true, but Statement 2 is not the correct explanation for Statement 1.
- C. Statement 1 is true and Statement 2 is false.
- D. Statement 1 is false and Statement 2 is true.

## Answer: A

2. Statement 1: if three points P, QandR have position vectors  $\overrightarrow{a}, \overrightarrow{b}, and \overrightarrow{c}$ , respectively, and  $2\overrightarrow{a} + 3\overrightarrow{b} - 5\overrightarrow{c} = 0$ , then the points P, Q, andR must be collinear. Statement 2: If for three points  $A, B, andC, \overrightarrow{A}B = \lambda \overrightarrow{A}C$ , then points A, B, andC must be collinear.

A. Both the statements are true, and Statement 2 is the correct explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

C. Statement 1 is true and Statement 2 is false.

D. Statement 1 is false and Statement 2 is true.

## Answer: A



**3.** Statement 1: If  $\overrightarrow{u}$  and  $\overrightarrow{v}$  are unit vectors inclined at an angle  $\alpha$  and  $\overrightarrow{x}$  is a unit vector bisecting the angle between them, then  $\overrightarrow{x} = \left(\overrightarrow{u} + \overrightarrow{v}\right) / (2\sin(\alpha/2))$ . Statement 2: If Delta*ABC* is an isosceles triangle with AB = AC = 1, then the vector representing the bisector of angel A is given by  $\overrightarrow{A}D = \left(\overrightarrow{A}B + \overrightarrow{A}C\right)/2$ .

A. Both the statements are true, and Statement 2 is the correct explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct explanation for Statement 1.

C. Statement 1 is true and Statement 2 is false.

D. Statement 1 is false and Statement 2 is true.

## Answer: D

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**4.** Statement 1: If  $\cos \alpha$ ,  $\cos \beta$ , and  $\cos \gamma$  are the direction cosines of any line segment, then  $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$ . Statement 2: If cosalpha,cosbeta,a n dcosgamma are the direction cosines of any line segment, then cos2alpha+cos2beta+cos2gamma=1.

- A. Both the statements are true, and Statement 2 is the correct explanation for Statement 1.
- B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

C. Statement 1 is true and Statement 2 is false.

D. Statement 1 is false and Statement 2 is true.

## Answer: B



5. Statement 1: The direction cosines of one of the angular bisectors of two intersecting line having direction cosines as  $l_1, m_1, n_1 and l_2, m_2, n_2$ are proportional to  $l_1 + l_2, m_1 + m_2, n_1 + n_2$ . Statement 2: The angle between the two intersection lines having direction cosines as  $l_1, m_1, n_1 and l_2, m_2, n_2$  is given by  $\cos \theta = l_1 l_2 + m_1 m_2 + n_1 n_2$ .

A. Both the statements are true, and Statement 2 is the correct explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct explanation for Statement 1.

C. Statement 1 is true and Statement 2 is false.

D. Statement 1 is false and Statement 2 is true.

## Answer: B

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6. Statement 1: In DeltaABC,  $\overrightarrow{A}B + \overrightarrow{A}B + \overrightarrow{C}A = 0$  Statement 2: If  $\overrightarrow{O}A = \overrightarrow{a}$ ,  $\overrightarrow{O}B = \overrightarrow{b}$ ,  $then\overrightarrow{A}B = \overrightarrow{a} + \overrightarrow{b}$ 

A. Both the statements are true, and Statement 2 is the correct explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

- C. Statement 1 is true and Statement 2 is false.
- D. Statement 1 is false and Statement 2 is true.

### Answer: C

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7. Statement 1:  $\overrightarrow{a} = 3\overrightarrow{i} + p\overrightarrow{j} + 3\overrightarrow{k}$  and  $\overrightarrow{b} = 2\overrightarrow{i} + 3\overrightarrow{j} + q\overrightarrow{k}$  are parallel vectors if p = 9/2 and q = 2.

### Statement

:

$$\overrightarrow{a} = a_1 \overrightarrow{i} + a_2 \overrightarrow{j} + a_3 \overrightarrow{k}$$
 and  $\overrightarrow{b} = b_1 \overrightarrow{i} + b_2 \overrightarrow{j} + b_3 \overrightarrow{k}$  are parallel,  
then  $\frac{a_1}{b_1} = \frac{a_2}{b_2} = \frac{a_3}{b_3}$ .

A. Both the statements are true, and Statement 2 is the correct explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

C. Statement 1 is true and Statement 2 is false.

D. Statement 1 is false and Statement 2 is true.

## Answer: A

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8. Statement 1 : If 
$$\left| \overrightarrow{a} + \overrightarrow{b} \right| = \left| \overrightarrow{a} - \overrightarrow{b} \right|$$
, then  $\overrightarrow{a}$  and  $\overrightarrow{b}$  are

perpendicular to each other.

Statement 2 : If the diagonals of a parallelogram are equal in magnitude, then the parallelogram is a rectangle. A. Both the statements are true, and Statement 2 is the correct

explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

- C. Statement 1 is true and Statement 2 is false.
- D. Statement 1 is false and Statement 2 is true.

#### Answer: A

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**9.** Statement 1 : Let  $A(\overrightarrow{a}), B(\overrightarrow{b})$  and  $C(\overrightarrow{c})$  be three points such that  $\overrightarrow{a} = 2\hat{i} + \hat{k}, veb = 3\hat{i} - \hat{j} + 3\hat{k}$  and  $\overrightarrow{c} = -\hat{i} + 7\hat{j} - 5\hat{k}$ . Then OABC is tetrahedron.

Statement 2 : Let  $A(\overrightarrow{a}), B(\overrightarrow{b})$  and  $C(\overrightarrow{c})$  be three points such that vectors  $\overrightarrow{a}, \overrightarrow{b}$  and  $\overrightarrow{c}$  are non-coplanar. Then OABC is a tetrahedron, where O is the origin.

A. Both the statements are true, and Statement 2 is the correct

explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

- C. Statement 1 is true and Statement 2 is false.
- D. Statement 1 is false and Statement 2 is true.

#### Answer: A

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10. Statement 1: Let  $\overrightarrow{a}, \overrightarrow{b}, \overrightarrow{c} and \overrightarrow{d}$  be the position vectors of four points A, B, CandD and  $3\overrightarrow{a} - 2\overrightarrow{b} + 5\overrightarrow{c} - 6\overrightarrow{d} = 0$ . Then points A, B, C, andD are coplanar. Statement 2: Three non-zero, linearly dependent coinitial vector  $\left(\overrightarrow{P}Q, \overrightarrow{P}Rand\overrightarrow{P}S\right)$  are coplanar. Then  $\overrightarrow{P}Q = \lambda \overrightarrow{P}R + \mu \overrightarrow{P}S$ , where  $\lambda and \mu$  are scalars.
A. Both the statements are true, and Statement 2 is the correct

explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

- C. Statement 1 is true and Statement 2 is false.
- D. Statement 1 is false and Statement 2 is true.

#### Answer: A

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**11.** Statement 1 : If 
$$\left| \overrightarrow{a} \right| = 3$$
,  $\left| \overrightarrow{b} \right| = 4$  and  $\left| \overrightarrow{a} + \overrightarrow{b} \right| = 5$ , then  $\left| \overrightarrow{a} - \overrightarrow{b} \right| = 5$ .

Statement 2 : The length of the diagonals of a rectangle is the same.

A. Both the statements are true, and Statement 2 is the correct

explanation for Statement 1.

B. Both the statements are true, but Statement 2 is not the correct

explanation for Statement 1.

C. Statement 1 is true and Statement 2 is false.

D. Statement 1 is false and Statement 2 is true.

#### Answer: A

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**Exercise Comprehension** 

1. ABCD is a parallelogram. L is a point on BC which divides BC in the ratio

1:2. AL intersects BD at P.M is a point on DC which divides DC in the ratio

1:2 and AM intersects BD in Q.

Point P divides AL in the ratio

A. 1:2

B. 1:3

C.3:1

D. 2:1

Answer: C

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2. ABCD is a parallelogram. L is a point on BC which divides BC in the ratio

1:2. AL intersects BD at P.M is a point on DC which divides DC in the ratio

 $1\!:\!2$  and AM intersects BD in Q.

Point Q divides DB in the ratio

A. 1:2

 $B.\,1:3$ 

C.3:1

 $\mathsf{D}.\,2\!:\!1$ 

Answer: B



3. ABCD is a parallelogram. L is a point on BC which divides BC in the ratio

1:2. AL intersects BD at P.M is a point on DC which divides DC in the ratio

 $1\!:\!2$  and AM intersects BD in Q.

PQ:DB is equal to

A. 2/3

B.1/3

C.1/2

D. 3/4

Answer: C

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**4.** If ABCDEF is a regular hexagon then  $\overrightarrow{AD} + \overrightarrow{EB} + \overrightarrow{FC}$  equals :

A. 2 
$$\overrightarrow{AB}$$

B. 3  $\overrightarrow{AB}$ 

C. 4 $\overrightarrow{AB}$ 

D. none of these

Answer: C

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5. Consider the regular hexagon ABCDEF with centre at O (origin).

Five forces  $\overrightarrow{AB}$ ,  $\overrightarrow{AC}$ ,  $\overrightarrow{AD}$ ,  $\overrightarrow{AE}$ ,  $\overrightarrow{AF}$  act at the vertex A of a regular hexagon ABCDEF. Then their resultant is

A. 
$$\overrightarrow{AO}$$
  
B.  $\overrightarrow{AO}$   
C.  $\overrightarrow{AO}$ 

D.  $\overrightarrow{6AO}$ 

### Answer: D



**6.** Let A, B, C, D, E represent vertices of a regular pentagon ABCDE. Given the position vector of these vertices be  $\overrightarrow{a}, \overrightarrow{a} + \overrightarrow{b}, \overrightarrow{b}, \lambda \overrightarrow{a}$  and  $\lambda \overrightarrow{b}$ , respectively.

The ratio  $\frac{AD}{BC}$  is equal to

A. 
$$1 - \cos \frac{3\pi}{5} : \cos \frac{3\pi}{5}$$
  
B.  $1 + 2\cos \frac{2\pi}{5} : \cos \frac{\pi}{5}$ 

C. 
$$1 + 2\cos{\frac{\pi}{5}}: 2\cos{\frac{\pi}{5}}$$

D. None of these

#### Answer: C

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7. Let A, B, C, D, E represent vertices of a regular pentagon ABCDE. Given the position vector of these vertices be  $\overrightarrow{a}, \overrightarrow{a} + \overrightarrow{b}, \overrightarrow{b}, \lambda \overrightarrow{a}$  and  $\lambda \overrightarrow{b}$ , respectively.

AD divides EC in the ratio

A. 
$$\cos \frac{2\pi}{5} : 1$$
  
B.  $\cos \frac{3\pi}{5} : 1$   
C. 1:  $2 \cos \frac{2\pi}{5}$   
D. 1: 2

#### Answer: C

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**8.** In a parallelogram OABC, vectors  $\overrightarrow{a}, \overrightarrow{b}, \overrightarrow{c}$  are, respectively, tehe position vectors of vertices A, B, C with reference to O as origin. A point E is taken on the side BC which divides it in the ratio 2:1. Also, the line segment AE intersects the line bisecting the angle  $\angle AOC$  internally at point P. If CP when extended meets AB in point F, then The position vector of point P is



D. None of these

#### Answer: B

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**9.** In a parallelogram OABC, vectors  $\overrightarrow{a}, \overrightarrow{b}, \overrightarrow{c}$  are, respectively, tehe position vectors of vertices A, B, C with reference to O as origin. A point E is taken on the side BC which divides it in the ratio 2:1. Also, the line segment AE intersects the line bisecting the angle  $\angle AOC$  internally at point P. If CP when extended meets AB in point F, then The ratio in which F divides AB is

A. 
$$\frac{2\left|\overrightarrow{a}\right|}{\left|\left|\overrightarrow{a}-3\right|\overrightarrow{c}\right|\right|}$$



### Answer: D



Linked Comprehension Type

1. Let OABCD be a pentagon in which the sides OA and CB are parallel and

the sides OD and AB are parallel. Also OA: CB = 2:1 and OD: AB = 1:3. The ratio  $\frac{OX}{XC}$  is A. 3/4 B. 1/3

C.2/5

D. 1/2

## Answer: C

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2. Let OABCD be a pentagon in which the sides OA and CB are parallel and

the sides OD and AB are parallel. Also OA: CB = 2:1 and OD: AB = 1:3. The ratio  $\frac{AX}{XD}$  is A. 5/2B. 6 C. 7/3D. 4

 $\mathsf{D.}\,4$ 



# **Exercise Numerical**

**1.** Let ABC be a triangle whose centroid is G, orhtocentre is H and circumcentre is the origin 'O'. If D is any point in the plane of the triangle such that no three of O, A, C and D are collinear satisfying the relation  $\overrightarrow{AD} + \overrightarrow{BD} + \overrightarrow{CH} + 3\overrightarrow{HG} = \lambda \overrightarrow{HD}$ , then what is the value of the scalar ' $\lambda$ '?

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**2.** If the resultant of three forces  

$$\overrightarrow{F}_1 = p\hat{i} + 3\hat{j} - \hat{k}, \overrightarrow{F}_2 = -5\hat{i} + \hat{j} + 2\hat{k}$$
 and  $\overrightarrow{F}_3 = 6\hat{i} - \hat{k}$  acting on  
a particle has a magnitude equal to 5 units, then what is difference in the  
values of  $p$ ?

**3.** Let  $\overrightarrow{a}$ ,  $\overrightarrow{b}$  and  $\overrightarrow{c}$  be unit vector such that  $\overrightarrow{a} + \overrightarrow{b} - \overrightarrow{c} = 0$ . If the area of triangle formed by vectors  $\overrightarrow{a}$  and  $\overrightarrow{b}$  is A, then what is the value of  $4A^2$ ?



**4.** Find the least positive integral value of x form which the angle between

vectors 
$$\overrightarrow{a} = x\hat{i} - 3\hat{j} - \hat{k}$$
 and  $\overrightarrow{b} = 2x\hat{i} + x\hat{j} - \hat{k}$  is acute.

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5. Vectors along the adjacent sides of parallelogram are  $\vec{a} = \hat{i} + 2\hat{j} + \hat{k}$  and  $\vec{b} = 2\hat{i} + 4\hat{j} + \hat{k}$ . Find the length of the longer diagonal of the parallelogram.

6. If vectors  $\overrightarrow{a} = \hat{i} + 2\hat{j} - \hat{k}$ ,  $\overrightarrow{b} = 2\hat{i} - \hat{j} + \hat{k}$  and  $\overrightarrow{c} = \lambda\hat{i} + \hat{j} + 2\hat{k}$ are coplanar, then find the value of  $(\lambda - 4)$ . Watch Video Solution Jee Previous Year the values of  $\lambda$  such that Find 1.  $x,y,z
eq (0,0,0) and ig(\hat{i}+\hat{j}+3\hat{k}ig)x+ig(3\hat{i}-3\hat{j}+\hat{k}ig)y+ig(-4\hat{i}+5\hat{j}ig)z=$ 

are unit vector along coordinate axes.

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**2.** A vector a has components  $a_1, a_2, a_3$  in a right handed rectangular cartesian coordinate system OXYZ the coordinate axis is rotated about z axis through an angle  $\frac{\pi}{2}$ . The components of a in the new system

**3.** The position vectors of the point A, B, C and D are  $3\hat{i} - 2\hat{j} - \hat{k}, 2\hat{i} + 3\hat{j} - 4\hat{k}, -\hat{i} + \hat{j} + 2\hat{k}$  and  $4\hat{i} + 5\hat{j} + \lambda\hat{k}$ ,

respectively. If the points A, B, C and D lie on a plane, find the value of  $\lambda$ .



**4.** Let OACB be a parallelogram with O at the origin and OC a diagonal. Let D be the midpoint of OA. using vector methods prove that BDandCO intersect in the same ratio. Determine this ratio.



5. In a triangle ABC, DandE are points on BCandAC, respectivley, such that BD = 2DCandAE = 3EC. Let P be the point of intersection of ADandBE. Find BP/PE using the vector method.

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**6.** Prove, by vector method or otherwise, that the point of intersection of the diagonals of a trapezium lies on the line passing through the midpoint of the parallel sides (you may assume that the trapezium is not a parallelogram).

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**7.** Show, by vector methods, that the angularbisectors of a triangle are concurrent and find an expression for the position vector of the point of concurrency in terms of the position vectors of the vertices.

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8.

Let

$$A(t) = f_1(t)\overrightarrow{i} + f_2(t)\overrightarrow{j}$$
 and  $\overrightarrow{B}(t) = g_1(t)\overrightarrow{i} + g_2(t)\overrightarrow{j}, t\varepsilon[0,1]$  where  $f_1$ ,  
are continuous functions. If  $\overrightarrow{A}(t)$  and  $\overrightarrow{B}(t)$  are non zero for all  
 $t\varepsilon[0,1]$  and  $\overrightarrow{A}(0) = 2\overrightarrow{i} + 3\overrightarrow{j}, \overrightarrow{A}(1) = 6\overrightarrow{i} = 2\overrightarrow{j}, \overrightarrow{B}(0) = 3\overrightarrow{i} + 2\overrightarrow{j}$  as  
prove that  $\overrightarrow{A}(t)$  and  $\overrightarrow{B}(t)$  are parallel for some  $t\varepsilon(0,1)$ 

9. about to only mathematics



$$egin{array}{lll} {f 10.} & {f If} egin{array}{ccc} a & a^2 & 1+a^3 \ b & b^2 & 1+b^3 \ c & c^2 & 1+c^3 \end{array} igg| = 0 ext{ and the vectors} \ ec{A} & = igg(1,a,a^2), ec{B} & = ig(1,b,b^2), ec{C}igg(1,c,c^2) \end{array}$$

are non-coplanar then the product abc = ....

**11.** If the vectors  

$$a\hat{i} + \hat{j} + \hat{k}, \hat{i} + b\hat{j} + \hat{k}, \hat{i} + \hat{j} + c\hat{k}(a \neq 1, b \neq 1, c \neq 1)$$
 are coplanat  
then the value of  $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c}$  is (A) 0 (B) 1 (C) -1 (D) 2  
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**12.** The points with position vectors  $\overrightarrow{a} + \overrightarrow{b}$ ,  $\overrightarrow{a} - \overrightarrow{b}$  and  $\overrightarrow{a} + k\overrightarrow{b}$  are

collinear for all real values of k.



**13.** The points with position vectors  $60\hat{i} + 3\hat{j}, 40\hat{i} - 8\hat{j}, a\hat{i} - 52\hat{j}$  are collinear iff (A) a = -40 (B) a = 40 (C) a = 20 (D) none of these

A. a = -40

 $\mathsf{B.}\,a=40$ 

 $\mathsf{C.}\,a=20$ 

D. none of these

Answer: A

14. Let a, b and c be distinct non-negative numbers. If vectos  $a\hat{i} + a\hat{j} + c\hat{k}, \hat{i} + \hat{k}$  and  $c\hat{i} + c\hat{j} + b\hat{k}$  are coplanar, then c is

A. the arithmetic mean of a and b

B. the geometric mean of a and b

C. the harmonic mean of a and b

D. equal to zero

### Answer: B

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15. Let  

$$\vec{a} = \hat{i} - \hat{k}, \vec{b} = x\hat{i} + \hat{j} + (1 - x)\hat{k} \text{ and } \vec{c} = y\hat{i} + x\hat{j} + (1 + x - y)\hat{k}$$
  
. Then  $\vec{a}, \vec{b}$  and  $\vec{c}$  are non-coplanar for

A. some values of x

B. some values of y

C. no values of x and y

D. for all values of x and y

Answer: D

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16. about to only mathematics

A. are collinear

B. form an equilateral triangle

C. form a scalene triangle

D. form a right-angled triangle

Answer: B

17. The number of distinct values of  $\lambda$ , for which the vectors  $-\lambda^2 \hat{i} + \hat{j} + \hat{k}, \, \hat{i} - \lambda^2 \hat{j} + \hat{k}$  and  $\hat{i} + \hat{j} - \lambda^2 \hat{k}$  are coplanar, is

A. zero

B. one

C. two

D. three

# Answer: C

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**18.** If 
$$\overrightarrow{a} = \hat{i} + \hat{j} + \hat{k}$$
,  $\overrightarrow{b} = 4\hat{i} + 3\hat{j} + 4\hat{k}$  and  $\overrightarrow{c} = \hat{i} + \alpha\hat{j} + \beta\hat{k}$   
are linearly dependent vectors and  $\left|\overrightarrow{c}\right| = \sqrt{3}$  then

A. 
$$\alpha = 1, \beta = -1$$

 $\texttt{B.}\,\alpha=1,\beta=~\pm\,1$ 

 $\mathsf{C}.\,\alpha=\,-\,1,\beta=\,\pm\,1$ 

$$\mathsf{D}.\,\alpha=\,\pm\,1,\beta=1$$

#### Answer: D



19. Consider the set of eight vector 
$$V = \left\{a\hat{i} + b\hat{j} + c\hat{k}; a, bc \in \{-1, 1\}
ight\}$$
. Three non-coplanar vectors can be chosen from  $V$  is  $2^p$  ways. Then  $p$  is\_\_\_\_\_.

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**20.** Suppose that  $\overrightarrow{p}$ ,  $\overrightarrow{q}$  and  $\overrightarrow{r}$  are three non-coplaner in  $R^3$ , Let the components of a vector  $\overrightarrow{s}$  along  $\overrightarrow{p}$ ,  $\overrightarrow{q}$  and  $\overrightarrow{r}$  be 4,3, and 5, respectively, if the components this vector  $\overrightarrow{s}$  along  $\left(-\overrightarrow{p}+\overrightarrow{q}+\overrightarrow{r}\right)$ ,  $\left(\overrightarrow{p}-\overrightarrow{q}+\overrightarrow{r}\right)$  and  $\left(-\overrightarrow{p}-\overrightarrow{q}+\overrightarrow{r}\right)$  are x, y

and z , respectively , then the value of 2x + y + z is

