



MATHS

BOOKS - CENGAGE

LIMITS

Examples

1. Find the value of $\lim_{x \rightarrow 3^-} \frac{x - 2}{x - 3}$.

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2. Prove that $\left[\lim_{x \rightarrow 0} \frac{\tan^{-1} x}{x} \right] = 0$, where $[.]$ represents the greatest integer function.

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3. If $f(x) = \begin{cases} \frac{x - |x|}{x}, & x \neq 0 \\ x = 0, \end{cases}$ show that $(\lim)_{x \rightarrow 0} f(x)$ does not exist.

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4. Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be defined by $f(x) = \begin{cases} x & x \text{ is irrational} \\ 1 - x & x \text{ is rational} \end{cases}$ then f is

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5. Evaluate $\lim_{x \rightarrow 1^+} 2^{-2^{\frac{1}{1-x}}}$.

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6. Evaluate $\lim_{x \rightarrow 0^-} \frac{x^2 - 3x + 2}{x^3 - 2x^2}$.

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7. Evaluate $\lim_{x \rightarrow 0} \frac{\sin x - 2}{\cos x - 1}$.

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8. If $[.]$ denotes the greatest integer function, then $(\lim)_{x \rightarrow 0} \frac{x}{a} \left[\frac{b}{x} \right] \frac{b}{a}$
b. 0 c. $\frac{a}{b}$ d. does not exist

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9. For what value of a is this function $f(x) \begin{cases} \frac{x^4-1}{x-1} & \text{if } x \neq 1 \\ a & \text{if } x = 1 \end{cases}$
continuous at $x=1$?

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10. Evaluate the left-and right-hand limits of the function defined by $f(x) = \begin{cases} 1 + x^2, & \text{if } 0 \leq x < 1 \\ 2 - x, & \text{if } x > 1 \end{cases}$ at $x = 1$. Also, show that $(\lim)_{x \rightarrow 1} f(x)$ does not exist



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11. Let $f(x) = \begin{cases} \cos[x], & x \leq 0 \\ |x| + a, & x < 0 \end{cases}$. Then find the value of a , so that $\lim_{x \rightarrow 0} f(x)$ exists, where $[x]$ denotes the greatest integer function less than or equal to x .



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12. Evaluate $(\lim)_{x \rightarrow \frac{5\pi}{4}} [\sin x + \cos x]$, where $[.]$ denotes the greatest integer function.



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13.

Let

$$f(x) = \begin{cases} x + 1, & x > 0 \\ 2 - x, & x \leq 0 \end{cases} \text{ and } g(x) = \begin{cases} x + 3, & x < 1 \\ x^2 - 2x - 2, & 1 \leq x < 2 \\ x - 5, & x \geq 2 \end{cases}$$

Find the LHL and RHL of $g(f(x))$ at $x=0$ and, hence, find $\lim_{x \rightarrow 0} g(f(x))$.



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14. If $(\lim)_{x \rightarrow a} [f(x) + g(x)] = 2$ and $(\lim)_{x \rightarrow a} [f(x) - g(x)] = 1$, then find the value of $(\lim)_{x \rightarrow a} f(x)g(x)$.

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15. Find the following limits.

(i) $\lim_{x \rightarrow 2} \frac{4x}{x^3 - 3}$ (ii) $\lim_{x \rightarrow 1} \frac{\log_{10} x - 3}{3x - 2}$ (iii) $\lim_{x \rightarrow \pi} \frac{3 + \cos x}{2 - \sin x}$

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16. Evaluate $\lim_{x \rightarrow 0} \left(\frac{x + 4}{2 - x} \right)^{\frac{x^2 + 2x - 3}{x - 1}}$

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17. If $a_1 = 1$ and $a_n + 1 = \frac{4 + 3a_n}{3 + 2a_n}$, $n \geq 1$ and if $\lim_{n \rightarrow \infty} a_n = a$, then find the value of a .

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18. $\lim_{x \rightarrow \infty} \frac{\sin x}{x}$

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19. Find $\lim_{x \rightarrow 0} [x] \left(\frac{e^{1/x} - 1}{e^{1/x} + 1} \right)$, (where $[.]$ represents the greatest integer function).

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20. In the neighbourhood of $x = 0$ it is known that

$1 + |x| < \frac{e^x - 1}{x} < 1 - |x|$ then find $\lim_{x \rightarrow 0} \frac{e^x - 1}{x}$.

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21. If $0 < \log_e x < \sqrt{x}$ for all $x < 1$, then find the value of $\lim_{x \rightarrow \infty} \frac{\log_e x}{x}$.

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22. If $3 - \left(\frac{x^2}{12}\right) \leq f(x) \leq 3 + \left(\frac{x^3}{9}\right)$ for all $x \neq 0$, then find the value of $(\lim)_{x \rightarrow 0} f(x)$

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23. Evaluate $\lim_{x \rightarrow 2} \frac{x^2 - 5x + 6}{x^2 - 4}$.

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24. Evaluate $\lim_{x \rightarrow 1} \left(\frac{2}{1-x^2} - \frac{1}{1-x} \right)$.

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25. Evaluate $\lim_{x \rightarrow 1} \frac{x^2 + x \log_e x - \log_e x - 1}{(x^2) - 1}$

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26. The value of $\lim_{x \rightarrow \frac{3\pi}{4}} \frac{1 + \sqrt[3]{\tan x}}{1 - 2 \cos^2 x}$ is

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27. Evaluate $\lim_{x \rightarrow \infty} \frac{\log_e x}{x}$

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28. Evaluate $\lim_{n \rightarrow \infty} (4^n + 5^n)^{1/n}$

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29. Evaluate $\lim_{x \rightarrow 0} \frac{\sqrt{2+x} - \sqrt{2}}{x}$.

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30. Evaluate $\lim_{x \rightarrow a} \frac{\sqrt{a+2x} - \sqrt{3x}}{\sqrt{3a+x} - 2\sqrt{x}}$, ($a \neq 0$).

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31.

Evaluate

$$\lim_{x \rightarrow \pi/2} \tan^2 x \sqrt{2 \sin^2 x + 3 \sin x + 4} - \sqrt{\sin^2 x + 6 \sin x + 2}.$$

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32. Evaluate $\lim_{n \rightarrow \infty} \frac{1^3 + 2^3 + 3^3 + \dots + n^3}{\sqrt{4n^8 + 1}}$.

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33. If $f(x) = \frac{x^2 - 3x + 2}{x^2 - 7x + 12}$, then which of the following limits exists?

(i) $\lim_{x \rightarrow \infty} \sin^{-1} f(x)$ (ii) $\lim_{x \rightarrow \infty} \cos^{-1} f(x)$

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34. Evaluate $\lim_{x \rightarrow \infty} \frac{\sqrt{3x^2 - 1} - \sqrt{2x^2 - 1}}{4x + 3}$.

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35. Evaluate $\lim_{x \rightarrow \infty} \sqrt{x}(\sqrt{x+c} - \sqrt{x})$.

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36. Find the value of $\lim_{x \rightarrow 0^+} \frac{3(\log_e x)^2 + 5 \log_e x + 6}{1 + (\log_e x)^2}$.

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37. Evaluate $\lim_{x \rightarrow \infty} \frac{3^{\sin x} + 2x + 1}{\sin x - \sqrt{x^2 + 1}}$.

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38. Evaluate: $(\lim)_{x \rightarrow \infty} \frac{x + 7 \sin x}{-2x + 13}$ using sandwich theorem.

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39. Evaluate $\lim_{x \rightarrow \infty} \frac{\sqrt{x^2 + 1} - \sqrt[3]{x^3 + 1}}{\sqrt[4]{x^4 + 1} - \sqrt[5]{x^4 + 1}}$

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40. Evaluate $\lim_{x \rightarrow \infty} \left(\sqrt{25x^2 - 3x} + 5x \right)$.

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41. Evaluate $\lim_{x \rightarrow \infty} \left(\frac{x^2 + x - 1}{3x^2 + 2x + 4} \right)^{\frac{3x^2 + x}{x - 2}}$



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42. Evaluate $\lim_{n \rightarrow \infty} \sin^n \left(\frac{2\pi n}{3n+1} \right), n \in \mathbb{N}.$



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43. Evaluate: $(\lim)_{x \rightarrow \infty} ((x + 1)(x + 2)(x + 3) \dots - x)$



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44. Evaluate $\lim_{n \rightarrow \infty} \frac{1}{1+n^2} + \frac{2}{2+n^2} + \dots + \frac{n}{n+n^2}.$



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45. If $[x]$ denotes the greatest integer less than or equal to x , then evaluate $(\lim)_{n \rightarrow \infty} \frac{1}{n^2} ([1.x] + [2.x] + [3.x] + \dots + [n.x])$



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46. If $(\lim)_{x \rightarrow \infty} \left\{ \frac{x^2 + 1}{x + 1} - (ax + b) \right\} = 0$, then find the value of a and b .

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47. Evaluate $\lim_{n \rightarrow \infty} \frac{n^p \sin^2(n!)}{n + 1}$, where $0 < p < 1$.

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48. Evaluate $\lim_{n \rightarrow \infty} (-1)^{n-1} \sin\left(\pi \sqrt{n^2 + 0.5n + 1}\right)$, where $n \in \mathbb{N}$

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49. Evaluate $\lim_{x \rightarrow 2} \frac{x^{10} - 1024}{x^5 - 32}$.

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50. If $\lim_{x \rightarrow 2} \frac{x^n - 2^n}{x - 2} = 80$ and $n \in \mathbb{N}$, then find the value of n .

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51. Evaluate $\lim_{x \rightarrow 1} \frac{\sqrt{x} + \sqrt{\sqrt{x}} + \sqrt{\sqrt{\sqrt{x}}} + \sqrt{\sqrt{\sqrt{\sqrt{x}}}} - 4}{x - 1}$.

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52. Evaluate $\lim_{x \rightarrow a} \frac{(x + 2)^{5/3} - (a + 2)^{5/3}}{x - a}$.

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53. Evaluate: $(\lim)_{x \rightarrow 2} \frac{\sqrt{(x + 7)} - 3\sqrt{(2x - 3)}}{3\sqrt{x + 6} - 23\sqrt{3x - 5}}$

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54. If $\lim_{x \rightarrow 0} \frac{(4x - 1)^{\frac{1}{3}} + a + bx}{x} = \frac{1}{3}$ then find the values of a and b.

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55. Evaluate $\lim_{x \rightarrow 0} \frac{\sin x - x}{x^3}$.

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56. Evaluate $\lim_{x \rightarrow 0} \frac{5 \sin x - 7 \sin 2x + 3 \sin 3x}{x^2 \sin x}$.

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57. Evaluate $\lim_{x \rightarrow 0} \frac{\sin x + \log(1 - x)}{x^2}$.

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58. Evaluate $\lim_{x \rightarrow 0} \frac{e^{\sin x} - (1 + \sin x)}{(\tan(\sin x))^2}$

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59. Evaluate $\lim_{x \rightarrow 0} \left(\frac{1}{x^2} - \frac{1}{\sin^2 x} \right)$.

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60. If $(\lim)_{x \rightarrow 0} \frac{\cos 4x + a \cos 2x + b}{x^4}$ is finite, find a and b using expansion formula.

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61. Find the integral value of n for which

$(\lim)_{x \rightarrow 0} \frac{\cos^2 x - \cos x - e^x \cos x + e^x - \frac{x^3}{2}}{x^n}$ is a finite nonzero number

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62. Find the limits of the following:

$$(i) \lim_{x \rightarrow 0} \frac{\sin 3x}{x} \quad (ii) \lim_{x \rightarrow 0} \frac{\sin 7x}{\sin 4x} \quad (iii) \lim_{x \rightarrow 0} \frac{1 - \cos^2 x}{x^2}$$

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63. Find the following limits:

$$(i) \lim_{x \rightarrow 0} \frac{1}{x} \sin^{-1} \left(\frac{2x}{1+x^2} \right) \quad (ii) \lim_{x \rightarrow 0} \frac{1}{x} \sin^{-1} (3x - 4x^3)$$

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64. Evaluate $\lim_{x \rightarrow \infty} 2^{x-1} \tan \left(\frac{a}{2^x} \right)$.

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65. Evaluate $\lim_{x \rightarrow \frac{\pi}{2}} \frac{1 + \cos 2x}{(\pi - 2x)^2}$.

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66. Evaluate $\lim_{x \rightarrow 2} \frac{x^2 - x - 2}{x^2 - 2x - \sin(x - 2)}$.

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67. Find $\lim_{x \rightarrow 0} \frac{\sqrt{\frac{1}{2}(1 - \cos 2x)}}{x}$ if exists.

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68. Evaluate $\lim_{x \rightarrow 0} \frac{\sin(\pi \cos^2 x)}{x^2}$.

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69. Evaluate $\lim_{x \rightarrow \frac{\pi}{6}} \frac{2 - \sqrt{3} \cos x - \sin x}{(6x - \pi)^2}$.

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70. Evaluate $\lim_{x \rightarrow \pi} \frac{\sin^{-1}(1 + \cos x) \cdot \sec\left(\frac{x}{2}\right)}{(x - \pi)}$.

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71. Evaluate $\lim_{x \rightarrow \infty} \left[\frac{x^4 \sin\left(\frac{1}{x}\right) + x^2}{(1 + |x|^3)} \right]$.

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72. Evaluate $\lim_{x \rightarrow 0} \frac{\tan x - \sin x}{x^3}$.

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73. Evaluate $\lim_{x \rightarrow \infty} x \left(\tan^{-1} \frac{x+1}{x+4} - \frac{\pi}{4} \right)$.

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74. Evaluate $\lim_{n \rightarrow \infty} n \sin\left(2\pi\sqrt{1+n^2}\right)$, ($n \in N$).

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75. Evaluate $\lim_{x \rightarrow -1^+} \frac{\sqrt{\pi} - \sqrt{\cos^{-1} x}}{\sqrt{1+x}}$.

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76. Evaluate $\lim_{x \rightarrow 0} x \left[\tan^{-1}\left(\frac{x+1}{x+2}\right) - \tan^{-1}\left(\frac{x}{x+2}\right) \right]$.

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77. Evaluate $\lim_{x \rightarrow 0} \frac{1 - \cos(1 - \cos x)}{x^4}$.

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78. Using $(\lim)_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$ prove that the area of circle of radius R is πR^2 (Figure)

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79. Prove that $\left[\lim_{x \rightarrow 0} \frac{\sin x}{x} \right] = 0$, where $[.]$ represents the greatest integer function.

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80. Prove that $\left[\lim_{x \rightarrow 0} \frac{\tan^{-1} x}{x} \right] = 0$, where $[.]$ represents the greatest integer function.

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81. If $L = \lim_{x \rightarrow 0} \frac{\sin 2x + a \sin x}{x^3}$ is finite, then find the value of a and L .

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82. If $m, n \in I_0$ and $\lim_{x \rightarrow 0} \frac{\tan 2x - n \sin x}{x^3} = \text{some integer}$, then find the value of n and also the value of limit.

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83. Evaluate $\lim_{x \rightarrow 0} \frac{3^{2x} - 2^{3x}}{x}$.

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84. Evaluate $\lim_{x \rightarrow 0} \frac{10^x - 2^x - 5^x + 1}{x \tan x}$.

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85. Evaluate $\lim_{x \rightarrow 0} \frac{2^x - 1}{\sqrt{1+x} - 1}$.

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86. Evaluate $\lim_{x \rightarrow 1} \frac{a^{x-1} - 1}{\sin \pi x}$.

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87. Evaluate $\lim_{x \rightarrow 0} \frac{e^x - e^{x \cos x}}{x + \sin x}$.

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88. Evaluate $x \lim_{x \rightarrow 2} \frac{x - 2}{\log_a(x - 1)}$.

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89. Evaluate $\lim_{x \rightarrow a} \frac{\log x - \log a}{x - a}$.

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90. Evaluate $\lim_{x \rightarrow 0} \frac{\log(5 + x) - \log(5 - x)}{x}$.



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91. Evaluate $\lim_{h \rightarrow 0} \frac{\log_e(1 + 2h) - 2\log_e(1 + h)}{h^2}$.



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92. Let $p_n = a^{P_{n-1}} - 1, \forall n = 2, 3, \dots$, and let $P_1 = a^x - 1$, where $a \in R^+$. Then evaluate $(\lim_{x \rightarrow 0} \frac{P_n}{x})$



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93. If $\lim_{x \rightarrow 0} \frac{ae^x - b}{x} = 2$, then find the values of a and b.



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94. Find the following limits:

(i) $\lim_{x \rightarrow 0} (1 - x)^{\frac{1}{x}}$ (ii) $\lim_{x \rightarrow 1} (1 + \log_e x)^{\frac{1}{\log_e x}}$

$$(iii) \lim_{x \rightarrow 0} (1 + \sin x)^{\frac{1}{x}}$$

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95. Evaluate $\lim_{x \rightarrow 0} (\cos x)^{\cot x}$.

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96. The population of a country increases by 2% every year. If it increases k times in a century, then prove that $[k] = 7$, where $[.]$ represents the greatest integer function.

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97. If $\lim_{x \rightarrow 0} (1 + ax + bx^2)^{2/x} = e^3$, then find the values of a and b .

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98. Evaluate $\lim_{x \rightarrow 0} \left(\frac{\sin x}{x} \right)^{\left(\frac{\sin x}{x - \sin x} \right)}$.

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99. Evaluate $\lim_{x \rightarrow 0} \left(\frac{a^x + b^x + c^x}{3} \right)^{2/x}$, $(a, b, c > 0)$

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100. If $f(n) = (\lim)_{x \rightarrow 0} \left\{ \left(1 + s \in \frac{x}{2} \right) \left(1 + s \in \frac{x}{x^2} \right) \left(1 + s \in \frac{x}{x^n} \right) \right\}^{1/x}$

then find $(\lim)_{n \rightarrow \infty} f(n)$.

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101. Find the following using L'Hospital's rule

(i) $\lim_{x \rightarrow 0} \frac{(16 + 5x)^{1/4} - 2}{(32 + 3x)^{1/5} - 2}$

(ii) $\lim_{x \rightarrow \pi/2} [x \tan x - (\pi/2) \sec x]$

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102. Let $f(x)$ be a twice-differentiable function and $f''(0) = 2$. Then

evaluate $\lim_{x \rightarrow 0} \frac{2f(x) - 3f(2x) + f(4x)}{x^2}$.

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103. Let $f(a) = g(a) = k$ and their n th derivatives exist and be not equal for some n .

If $\lim_{x \rightarrow a} \frac{f(a)g(x) - f(a) - g(a)f(x) + g(a)}{g(x) - f(x)} = 4$ then find the value of

k .

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104. Evaluate $\lim_{x \rightarrow 0} (\log_{\tan^2 x} (\tan^2 2x))$.

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105. Evaluate: $(\lim)_{x \rightarrow 0} \frac{\sin^{-1} x - \tan^{-1} x}{x^3}$

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106. The graph of the function $y = f(x)$ has a unique tangent at the point $(a,0)$ through which the graph passes. Then evaluate

$$\lim_{x \rightarrow a} \frac{\log_e \{1 + 6f(x)\}}{3f(x)}.$$

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107. Evaluate $\lim_{x \rightarrow \infty} x \log_e \left\{ \frac{\sin\left(a + \frac{1}{x}\right)}{\sin a} \right\}, 0 < a < \frac{\pi}{2}.$

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108. Find the value of a so that $\lim_{x \rightarrow 0} (e^{ax} - e^x - x) = \frac{3}{2}.$

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109. Find the value of $\lim_{x \rightarrow 0} \frac{\sin x + \log_e \left(\sqrt{1 + \sin^2 x} - \sin x \right)}{\sin^3 x}$.

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110. Evaluate $\lim_{x \rightarrow \infty} x^{\frac{1}{x}}$.

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111. Evaluate $\lim_{x \rightarrow \frac{\pi}{2}^-} (\cos x)^{\cos x}$.

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112. Evaluate $\lim_{x \rightarrow 0^+} (x)^{\frac{1}{\log_e \sin x}}$.

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113. Evaluate: $(\lim)_{n \rightarrow \infty} n^2 \left\{ \left(1 - \frac{\cos 1}{n}\right) \left(1 - \frac{\cos 1}{n}\right) \left(1 - \frac{\cos 1}{n}\right) \dots \right\}$.

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114. Prove that $\sin x = 2^{10} \sin\left(\frac{x}{2^{10}}\right) \cos\left(\frac{x}{2}\right) \cos\left(\frac{x}{2^2}\right) \dots \cos\left(\frac{x}{2^{10}}\right)$.

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115. Evaluate: $(\lim)_{x \rightarrow 1} \sec\left(\frac{\pi}{2^x}\right) \log x$.

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116. Evaluate $\lim_{x \rightarrow 0^+} \frac{1}{x} \cos^{-1}\left(\frac{\sin x}{x}\right)$.

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117. If $f(x) = \frac{\tan x}{x}$, then find $\lim_{x \rightarrow 0} ([f(x)] + x^2)^{\frac{1}{[f(x)]}}$, where $[.]$ and $\{.\}$ denotes greatest integer and fractional part function respectively.

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118. Evaluate $\lim_{n \rightarrow \infty} \frac{1}{n^2(\log_e n - \log_e(n-1)) + n}$.

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119. Evaluate $\lim_{x \rightarrow 0} \frac{(1+x)^{1/x} - e + \frac{1}{2}ex}{x^2}$.

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120. Evaluate $\lim_{x \rightarrow 0^+} x^m(\log x)^n, m, n, \in N$.

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121. If $\alpha_1, \alpha_2, \dots, \alpha_n$ are the roots of equation $x^n + nax - b = 0$, show that $(\alpha_1 - \alpha_2)(\alpha_1 - \alpha_3) \dots (\alpha_1 - \alpha_n) = n(\alpha_1^{n-1} + a)$

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122. Evaluate $\lim_{x \rightarrow 0} \left\{ 1^{1/\sin^2 x} + 2^{1/\sin^2 x} + \dots + n^{1/\sin^2 x} \right\}^{\sin^2 x}$.

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123. Evaluate $\lim_{x \rightarrow \pi/2} \frac{\sin x - (\sin x)^{\sin x}}{1 - \sin x + \log_e \sin x}$.

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124. Evaluate: $(\lim_{n \rightarrow 0} \frac{e - (1+x)^{\frac{1}{x}}}{x})$

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125.

Evaluate:

$$(\lim)_{n \rightarrow \infty} n^{-n^2} \{ (n + 2^0)(n + 2^{-1})(n + 2^{-2}) \dots (n + 2^{-n+1}) \}^n$$


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126. ABC is an isosceles triangle inscribed in a circle of radius r . If $AB = AC$ and h is the altitude from A to BC , then triangle ABC has perimeter $P = 2(\sqrt{2hr - h^2} + \sqrt{2hr})$ and area $A =$ _____ and also

$$(\lim)_{h \rightarrow 0} \frac{A}{P^3} = _ _ _$$

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127. At the endpoint and midpoint of a circular arc AB , tangent lines are drawn, and the points A and B are joined with a chord. Prove that the ratio of the areas of the triangles thus formed tends to 4 as the arc AB decreases infinitely.


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Exercise 2.1

1. Evaluate: $(\lim)_{x \rightarrow 2^+} \frac{x^2 - 1}{2x + 4}$

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2. Evaluate : $(\lim)_{x \rightarrow 2^+} \frac{[x - 2]}{\log(x - 2)}$, where $[.]$ represents the greatest integer function.

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3. Evaluate: $(\lim)_{x \rightarrow 0} \frac{\sin[\cos x]}{1 + [\cos x]}$ ($[.]$ denotes the greatest integer function).

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4. If $f(x) = \begin{cases} \frac{x - |x|}{x}, & x \neq 0 \\ x = 0, \end{cases}$ show that $(\lim)_{x \rightarrow 0} f(x)$ does not exist.

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5. Show that $(\lim)_{x \rightarrow 0} (e^{(1/x)+1} / e^{(1/x)-1})$ does not exist

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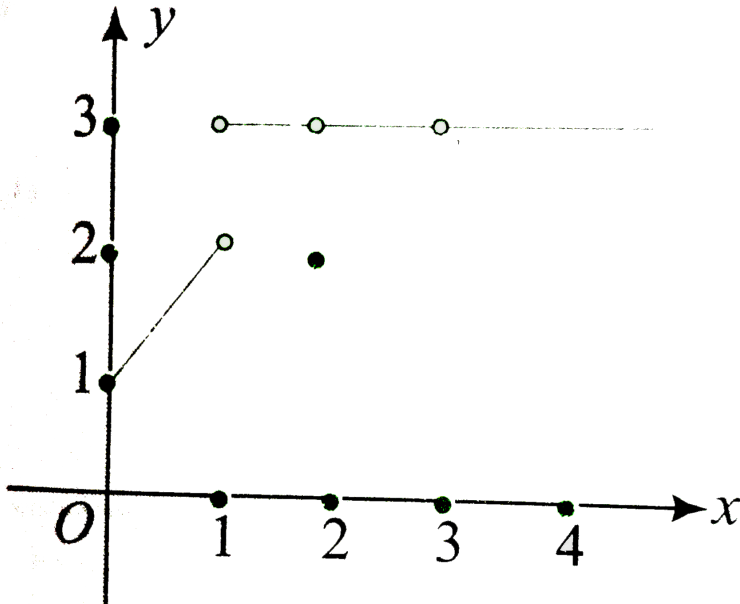
6. $\lim_{x \rightarrow 0} \frac{3x + |x|}{7x - 5|x|}$

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7. If $f(x) = \begin{cases} x, & x < 0 \\ 1, & x = 0 \\ x^2, & x > 0 \end{cases}$, then find $\lim_{x \rightarrow 0} f(x)$ if exists.

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8. Consider the following graph of the function $y=f(x)$. Which of the following is//are correct?



- (a) $\lim_{x \rightarrow 1} f(x)$ does not exist.
- (b) $\lim_{x \rightarrow 2} f(x)$ does not exist.
- (c) $\lim_{x \rightarrow 3} f(x) = 3$.
- (d) $\lim_{x \rightarrow 1.99} f(x)$ exists.

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9. Evaluate $\lim_{x \rightarrow 0} \frac{\tan(\operatorname{sgn}(x))}{\operatorname{sgn}(x)}$ if exists.

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10. If $f(x) = \begin{cases} \sin x & x \neq n\pi \text{ and } n \in \mathbb{Z} \\ 2 & x = n\pi \end{cases}$ and
 $g(x) = \begin{cases} x^2 + 1 & x \neq 0 \\ 4 & x = 0 \\ 5 & x = 2 \end{cases}$ then $\lim_{x \rightarrow 0} g\{f(x)\}$ is

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Exercise 2.2

1. If $|f(x)| \leq x^2$, then prove that $\lim_{x \rightarrow 0} \frac{f(x)}{x} = 0$.

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2. If $f(x) = \text{sgn}(x)$ and $g(x) = x^3$, then prove that $\lim_{x \rightarrow 0} f(x) \cdot g(x)$ exists though $\lim_{x \rightarrow 0} f(x)$ does not exist.

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3. If $f(x) = \begin{cases} \frac{\sin [x]}{[x]}, & \text{for } [x] \neq 0 \\ 0, & \text{for } [x] = 0 \end{cases}$ where $[x]$ denotes the greatest

integer less than or equal to x . Then find $\lim_{x \rightarrow 0} f(x)$.

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4. Find the value of $\lim_{x \rightarrow 0^+} (\sin x)^{\frac{1}{x}}$.

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5. Let the sequence $\{b_n\}$ real numbers satisfies the recurrence relation

$$b_{n+1} = \frac{1}{3} \left(2b_n + \frac{125}{(b_n)^2} \right), b_n \neq 0. \text{ Then find the } \left(\lim \right)_{n \rightarrow \infty} b_n.$$

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6. Let $f: (1, 2) \rightarrow R$ satisfy the inequality

$$\frac{\cos(2x - 4) - 33}{2} < f(x) < \frac{x^2 |4x - 8|}{x - 2} \forall x \in (1, 2).$$

Then find $\lim_{x \rightarrow 2^-} f(x)$.

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7. If $\frac{x^2 + x - 2}{x + 3} \leq \frac{f(x)}{x^2} \leq \frac{x^2 + 2x - 1}{x + 3}$ hold for a certain interval containing the point $x = -1$ and $(\lim)_{x \rightarrow 1} f(x)$ exists then find the value of $(\lim)_{x \rightarrow 1} f(x)$

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Exercise 2.3

1. Evaluate $\lim_{x \rightarrow 1} \frac{(2x - 3)(\sqrt{x} - 1)}{2x^2 + x - 3}$.

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2. Evaluate $\lim_{x \rightarrow 1} \frac{x^4 - 3x^4 + 2}{x^3 - 5x^2 + 3x + 1}$.

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3. Evaluate $\lim_{x \rightarrow \frac{\pi}{4}} \frac{1 - \sin 2x}{1 + \cos 4x}$.

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4. Evaluate $\lim_{x \rightarrow \pi/4} \frac{1 - \cot^3 x}{2 - \cot x - \cot^3 x}$.

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5. Evaluate $\lim_{x \rightarrow a} \frac{\sqrt{3x - a} - \sqrt{x + a}}{x - a}$.

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6. Evaluate $\lim_{x \rightarrow 0} \frac{\sqrt{2} - \sqrt{1 + \cos x}}{\sin^2 x}$.

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7. Evaluate $\lim_{x \rightarrow \sqrt{10}} \frac{\sqrt{7+2x} - (\sqrt{5} + \sqrt{2})}{x^2 - 10}$.

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8. Evaluate $\lim_{n \rightarrow \infty} \frac{(1^2 - 2^2 + 3^2 - 4^2 + 5^2 + \dots n \text{ terms})}{n^2}$.

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9. Evaluate $\lim_{x \rightarrow \infty} \left[\sqrt{a^2 x^2 + ax + 1} - \sqrt{a^2 x^2 + 1} \right]$.

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10. If $[x]$ denotes the greatest integer less than or equal to x , then evaluate $(\lim)_{n \rightarrow \infty} \frac{1}{n^2} ([1. x] + [2. x] + [3. x] + \dots + [n. x])$

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11. Evaluate $\lim_{x \rightarrow \infty} x^3 \left\{ \sqrt{x^2 + \sqrt{1 + x^4}} - x\sqrt{2} \right\}$.

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12. Evaluate $\lim_{x \rightarrow \infty} \left(\frac{7x^2 + 1}{5x^2 - 1} \right)^{\frac{x^5}{1-x^3}}$.

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13. Evaluate $\lim_{n \rightarrow \infty} \cos\left(\pi\sqrt{n^2 + n}\right)$ when n is an integer.

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14. Evaluate $\lim_{x \rightarrow 1} \frac{\sum_{k=1}^{100} x^k - 100}{x - 1}$.

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15. Evaluate $\lim_{h \rightarrow 0} \left[\frac{1}{h^3 \sqrt{8+h}} - \frac{1}{2h} \right]$.



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Exercise 2.4

1. Evaluate $\lim_{x \rightarrow 0} \left\{ \frac{\sin x - x + \frac{x^3}{6}}{x^5} \right\}$.



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2. Evaluate $\lim_{x \rightarrow 0} \frac{e^x - 1 - x}{x^2}$.



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3. Evaluate $\lim_{x \rightarrow 0} \frac{e^x - e^{-x} - 2x}{x - \sin x}$.



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4. If $\lim_{x \rightarrow 0} \frac{1 - \cos x}{e^{ax} - bx - 1} = 2$ then find the values of a and b.

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5. Find the values of a and b in order that $(\lim)_{x \rightarrow 0} \frac{x(1 + a \cos x) - b \sin x}{x^3} = 1$ [us \in gL' $H\sigma\pi\tau al'$ sre].

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Exercise 2.5

1. Evaluate $\lim_{x \rightarrow \infty} \frac{\sin x^0}{x}$.

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2. Evaluate $\lim_{x \rightarrow 0} \frac{1 - \cos mx}{1 - \cos nx}$.

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3. Evaluate $\lim_{x \rightarrow 0} \frac{\cot 2x - \operatorname{cosec} 2x}{x}$.

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4. Evaluate $\lim_{x \rightarrow 0} \frac{\tan 2x - x}{3x - \sin x}$.

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5. Evaluate $\lim_{n \rightarrow \infty} n \cos\left(\frac{\pi}{4n}\right) \sin\left(\frac{\pi}{4n}\right)$.

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6. Evaluate $\lim_{x \rightarrow 0} \frac{\cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)}{\sin^{-1} x}$.

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7. Evaluate $\lim_{h \rightarrow 0} \frac{2 \left[\sqrt{3} \sin\left(\frac{\pi}{6} + h\right) - \cos\left(\frac{\pi}{6} + h\right) \right]}{\sqrt{3}h(\sqrt{3} \cosh - \sinh)}$.

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8. Evaluate $\lim_{x \rightarrow 0} \frac{8}{x^8} \left\{ 1 - \cos \frac{x^2}{2} - \cos \frac{x^2}{4} + \cos \frac{x^2}{2} \cos \frac{x^2}{4} \right\}$.

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9. Evaluate: $(\lim)_{x \rightarrow 0, y \rightarrow 0} \frac{y^2 + \sin x}{x^2 + \sin y^2}$ where $(x, y) \rightarrow 0$, along the curve $x = y^2$

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10. Evaluate $\lim_{x \rightarrow 1} (1 - x) \tan \frac{\pi x}{2}$.

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11. Evaluate $\lim_{x \rightarrow 0} \frac{x \tan 2x - 2x \tan x}{(1 - \cos 2x)^2}$.

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12. If $\lim_{x \rightarrow 2} \frac{\tan(x - 2) \cdot (x^2 + (k - 2)x - 2k)}{(x^2 - 4x + 4)} = 5$, then find the value of k.

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Exercise 2.6

1. Evaluate $\lim_{x \rightarrow \infty} \left[x \left(a^{1/x} - 1 \right) \right], a > 1$

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2. Evaluate $\lim_{x \rightarrow 0} \frac{x2^x - x}{1 - \cos x}$

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3. Evaluate: $\lim_{x \rightarrow 0} \frac{\sin(e^x - 1)}{\log(x - 1)}$

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4. Evaluate $\lim_{x \rightarrow 0} \frac{e^{x^2} - \cos x}{x^2}$

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5. Evaluate $\lim_{x \rightarrow 0} \frac{e^x + e^{-x} - 2}{x^2}$

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6. $\lim_{x \rightarrow a} \frac{\log(x - a)}{\log(e^x - e^a)}$

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7. Evaluate $\lim_{x \rightarrow 0} \frac{a^{\tan x} - a^{\sin x}}{\tan x - \sin x}, a > 0$

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8. $\lim_{x \rightarrow 0} \frac{(1 - 3^x - 4^x + 12^x)}{\sqrt{(2 \cos x + 7)} - 3}$

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9. $\lim_{x \rightarrow 0} \frac{(729)^x - (243)^x - (81)^x + 9^x + 3^x - 1}{x^3}$

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Exercise 2.7

1. Evaluate $\lim_{x \rightarrow \infty} \left(1 + \frac{2}{x}\right)^x$.

A. 0

B. 1

C. -1

D. does not exist

Answer: e^2



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2. Evaluate $\lim_{x \rightarrow \infty} (\log_3 3x)^{\log_x 3}$.

A. l exists but m does not

B. m exists but l does not

C. both l and m exist

D. neither l nor m exists

Answer: e



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3. Evaluate $\lim_{x \rightarrow \infty} \left(\frac{x+2}{x+1} \right)^{x+3}$.

A. 0

B. e

C. ∞

D. does not exist

Answer: B



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4. Evaluate $\lim_{x \rightarrow \infty} \left(1 + \frac{1}{a+bx} \right)^{c+dx}$, where a, b, c, and d are positive.

A. 4

B. 2

C. -1

D. 0

Answer: $e^{d/b}$



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5. Evaluate $\lim_{x \rightarrow 7/2} (2x^2 - 9x + 8)^{\cot(2x-7)}$.

A. both $\lim_{x \rightarrow a} f(x)$ and $\lim_{x \rightarrow a} g(x)$ must exist

B. $\lim_{x \rightarrow a} f(x)$ need not exist but $\lim_{x \rightarrow a} g(x)$ exists

C. neither $\lim_{x \rightarrow a} f(x)$ nor $\lim_{x \rightarrow a} g(x)$ may exist

D. $\lim_{x \rightarrow a} f(x)$ exists but $\lim_{x \rightarrow a} g(x)$ need not exist

Answer: $e^{5/2}$



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6. If x_1 and x_2 are the real and distinct roots of $ax^2 + bx + c = 0$ then

prove that $\lim_{x \rightarrow x_1} (1 + \sin(ax^2 + bx + c))^{\frac{1}{x-x_1}} = e^{a(x_1-x_2)}$.

A. does not exist

B. 1

C. ∞

D. $\frac{1}{2}$

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7. Evaluate: $(\lim)_{x \rightarrow 0} \left\{ \sin^2 \left(\frac{\pi}{2 - px} \right) \right\}^{\sec} \left(2 \left(\frac{\pi}{2 - qx} \right) \right)$

A. -1

B. 2

C. $\sqrt{5}$

D. e^{-p^2/q^2}

Answer: D

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Exercise 2.8

1. Evaluate $\lim_{x \rightarrow 1} \frac{\cos \frac{\pi}{2} x}{1 - \sqrt{x}}$

A. -1

B. 1

C. 0

D. does not exist

Answer: π



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2. Evaluate $\lim_{x \rightarrow 1} \frac{1 + \log x - x}{1 - 2x + x^2}$

A. 0

B. 1

C. $\frac{1}{3}$

D. $\frac{1}{2}$

Answer: $-1/2$



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3. Evaluate $\lim_{x \rightarrow \pi/2} \tan x \log \sin x$

A. -2

B. -1

C. $-\frac{2}{7}$

D. 0

Answer: 0



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4. Evaluate $\lim_{x \rightarrow 0} \frac{\log \cos x}{x}$

A. $1/3$

B. $2/3$

C. $-1/4$

D. $3/2$

Answer: 0



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5. Evaluate $\lim_{x \rightarrow 0} \frac{2^x - 1}{(1+x)^{1/2} - 1}$

A. $\frac{1}{8\sqrt{3}}$

B. $\frac{1}{4\sqrt{3}}$

C. 0

D. none of these

Answer: $\log 4$



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6. Evaluate $\lim_{x \rightarrow \pi/4} (2 - \tan x)^{1/\ln(\tan x)}$

A. 16

B. 8

C. 4

D. 2

Answer: e^{-1}



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7. Evaluate $\lim_{x \rightarrow 0^+} x^x$ and $\lim_{x \rightarrow 0^+} x^{x^x}$

A. $1/2$

B. 2

C. 1

D. None of these

Answer: 1 and 0



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8. If $\lim_{x \rightarrow a} \frac{a^x - x^a}{x^x - a^a} = -1$ and $a > 0$, then find the value of a .

A. 43529

B. 2

C. $\sin \frac{2}{5}$

D. $\sin \frac{1}{5}$

Answer: $a = 1$



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Exercise (Single)

1. $(\lim)_{x \rightarrow 0} \left[\frac{\sin(\operatorname{sgn}(x))}{(\operatorname{sgn}(x))} \right]$, where $[\cdot]$ denotes the greatest integer function, is equal to (a) 0 (b) 1 (c) -1 (d) does not exist

A. $\hat{\ } (2n)p_n$

B. $\hat{\ } (2n)C_n$

C. $(2n)!$

D. none of these

Answer: A



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2. Let $\lim_{x \rightarrow 0} \frac{[x]^2}{x^2} = l$ and $\lim_{x \rightarrow 0} \frac{[x^2]}{x^2} = m$, where $[\cdot]$ denotes greatest integer. Then (a) l exists but m does not (b) m exists but l does not (c) both l and m exist (d) neither l nor m exists

A. $-\frac{1}{\sqrt{2}}$

B. $\frac{1}{\sqrt{2}}$

C. $\sqrt{2}$

D. $-\sqrt{2}$

Answer: B



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3. $\lim_{x \rightarrow 1} \left[\cos ec \frac{\pi x}{2} \right]^{1/(1-x)}$ (where $[.]$ represents the greatest integer function) is equal to

A. (i) exists, (ii) does not exist

B. (i) does not exist, (ii) exists

C. both (i) and (ii) exist

D. neither (i) nor (ii) exists

Answer: B



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4. The value of the limit $(\lim)_{x \rightarrow 0} \frac{a\sqrt{x} - a\frac{1}{\sqrt{x}}}{a\sqrt{x} + a\frac{1}{\sqrt{x}}}$, $a > 1$, is 4 (b) 2 (c) -1 (d)

0

A. does not exist

B. $1/3$

C. 0

D. $2/9$

Answer: C



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5. If $\lim_{x \rightarrow a} \left\{ \frac{f(x)}{g(x)} \right\}$ exists, then

A. 0

B. 2

C. 4

D. ∞

Answer: C



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6. $(\lim)_{x \rightarrow 1} \frac{1}{\sqrt{|x| - \{-x\}}}$ (where $\{x\}$ denotes the fractional part of (x))
is equal to does not exist (b) 1∞ (d) $\frac{1}{2}$

A. 16

B. 24

C. 32

D. 8

Answer: A



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7. If $x_1 = 3$ and $x_{n+1} = \sqrt{2 + x_n}$, $n \geq 1$, then $(\lim)_{x \rightarrow \infty} x_n$ is -1 (b) 2 (c) $\sqrt{5}$ (d) 3

A. 0

B. $\frac{1}{2}$

C. $\log 2$

D. e^4

Answer: B



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8. $\lim_{x \rightarrow 0^+} \frac{\sum_{r=1}^{2n+1} [x^r] + (n+1)}{1 + [x] + |x| + 2x}$, where $n \in N$ and $[.]$ denotes the greatest integer function, equals

A. 0

B. 1

C. -1

D. does not exist

Answer: C



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9. $\lim_{x \rightarrow \infty} \frac{\sin^4 x - \sin^2 x + 1}{\cos^4 x - \cos^2 x + 1}$ is equal to

A. 0

B. 1

C. 10

D. 100

Answer: B



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10.

If

$f(x) = \frac{2}{x-3}$, $g(x) = \frac{x-3}{x+4}$, and $h(x) = -\frac{2(2x+1)}{x^2+x-12}$, then $\lim_{x \rightarrow 3} [f(x)g(x)h(x)]$ is

(a) -2 (b) -1 (c) $-\frac{2}{7}$ (d) 0

A. 1

B. ∞

C. $\sqrt{2}$

D. none of these

Answer: C



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11. The value of $\lim_{x \rightarrow \pi} \frac{1 + \cos^3 x}{\sin^2 x}$ is

A. $[2, 5)$

B. $(1, 5)$

C. $(-1, 5)$

D. $(-\infty, \infty)$

Answer: D



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12. The value of $(\lim)_{x \rightarrow 2} \frac{\sqrt{1 + \sqrt{2 + x}} - \sqrt{3}}{x - 2}$ is (a) $\frac{1}{8\sqrt{3}}$ (b) $\frac{1}{4\sqrt{3}}$ (c) 0

(d) none of these

A. 0

B. e^x

C. $\log_e x$

D. none of these

Answer: A



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13. The value of $(\lim)_{x \rightarrow 2} \frac{2^x + 2^{3-x} - 6}{\sqrt{2^{-x}} - 2^{1-x}}$ is 16 (b) 8 (c) 4 (d) 2

A. $|2x| > \sqrt{3}$

B. $|2x| < \sqrt{3}$

C. $|2x| \geq \sqrt{3}$

D. $|2x| \leq \sqrt{3}$

Answer: B



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14.

$$(\lim)_{x \rightarrow 2} \left(\left(\frac{x^3 - 4x}{x^3 - 8} \right)^{-1} - \left(\frac{x + \sqrt{2x}}{x - 2} - \frac{\sqrt{2}}{\sqrt{x} - \sqrt{2}} \right)^{-1} \right) \text{ is equal to } < 0$$

a) $\frac{1}{2}$ (b) 2 (c) 1 (d) none of these

A. 1

B. $1/2$

C. 2

D. none of these

Answer: A



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15. about to only mathematics

A. 1

B. -1

C. 0

D. none of these

Answer: C



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16. $\lim_{x \rightarrow 1} \frac{(1-x)(1-x^2)(1-x^{2n})}{\{(1-x)(1-x^2)(1-x^n)\}^2}, n \in N$, equals ${}^{2n}P_n$ (b)
 ${}^{2n}C_n$ (c) $(2n)!$ (d) none of these

A. 0

B. π

C. 2π

D. none of these

Answer: B



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17. The value of $\lim_{x \rightarrow \frac{1}{\sqrt{2}}} \frac{x - \cos(\sin^{-1} x)}{1 - \tan(\sin^{-1} x)}$ is

A. $-\frac{1}{\sqrt{2}}$

B. -1

C. non-existent

D. none of these

Answer: A

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18. evaluate (i) $\lim_{x \rightarrow \infty} \sec^{-1}\left(\frac{x}{\sin x}\right)$ and (ii) $\lim_{x \rightarrow \infty} \sec^{-1}\left(\frac{\sin x}{x}\right)$.

A. $-\frac{1}{2\sqrt{2}}$

B. $\frac{1}{2\sqrt{2}}$

C. $\frac{1}{\sqrt{2}}$

D. does not exist

Answer: A

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19. $\lim_{x \rightarrow \infty} \left(\frac{x^3}{3x^2 - 4} - \frac{x^2}{3x + 2} \right)$ is equal to

A. 2

B. -1

C. 0

D. $\frac{2}{9}$

Answer: D

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20. $(\lim)_{n \rightarrow \infty} \frac{n(2n+1)^2}{(n+2)(n^2+3n-1)}$ is equal to (a) < 0 (b) 2 (c) 4 (d) ∞

A. 1

B. 0

C. 2

D. none of these

Answer: C

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21. $(\lim)_{x \rightarrow \infty} \frac{(2x + 1)^{40} (4x - 1)^5}{(2x + 3)^{45}}$ is equal to (a) 16 (b) 24 (c) 32 (d) 8

A. $\frac{1}{2\pi}$

B. $\frac{-1}{\pi}$

C. $\frac{-2}{\pi}$

D. none of these

Answer: C



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22. $\lim_{x \rightarrow \infty} \left[\sqrt{x + \sqrt{x + \sqrt{x}}} - \sqrt{x} \right]$ is equal to

A. 1

B. 0

C. 2

D. none of these

Answer: B



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23. about to only mathematics

A. $\sec x(x \tan x + 1)$

B. $x \tan x + \sec x$

C. $x \sec x + \tan x$

D. none of these

Answer: D



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24. $\lim_{x \rightarrow \infty} \frac{(x+1)^{10} + (x+2)^{10} + \dots + (x+100)^{10}}{x^{10} + 10^{10}}$ is equal to

A. 0

B. 1

C. 2

D. 4

Answer: D



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25. $(\lim)_{x \rightarrow \infty} \frac{2\sqrt{x} + 3\sqrt{x} + 4\sqrt{x} + \dots + n\sqrt{n}}{\sqrt{(2x-3)} + (\sqrt{2x-3}) + \dots + (\sqrt{2x-3})}$ is equal to

1 (b) ∞ (c) $\sqrt{2}$ (d) none of these

A. 0

B. 1

C. $\sqrt{2}$.

D. $2\sqrt{2}$.

Answer: C



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26. If $\lim_{x \rightarrow \infty} \frac{f(x) \cdot (n \cdot 3^n)}{n(x-2)^n + n \cdot 3^{n+1} - 3^n} = \frac{1}{3}$, then the range of x is (where $n \in \mathbb{N}$). (a) (2,5) (b) (1,5) (c) $-5, 5$ (d) $(-\infty, \infty)$

A. 1

B. $(2/3)^{1/2}$

C. $(3/2)^{1/2}$

D. $e^{1/2}$

Answer: A



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27. $\lim_{n \rightarrow \infty} n^2 \left(x^{1/n} - x^{1/(n+1)} \right), x > 0$, is equal to

A. π

B. 2π

C. $\pi/2$

D. none of these

Answer: C



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28. Let $f(x) = (\lim)_{x \rightarrow \infty} \frac{1}{\left(\frac{3}{\pi} \tan^{-1} 2x\right)^{2n} + 5}$. Then the set of values of

x for which $f(x) = 0$ is $|2x| > \sqrt{3}$ (b) $|2x|$

A. 199

B. 198

C. 0

D. none of these

Answer: A



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29. $f(x) = \frac{\ln(x^2 + e^x)}{\ln(x^4 + e^{2x})}$. Then $\lim_{x \rightarrow \infty} f(x)$ is equal to

A. $\frac{2a}{\pi}$

B. $-\frac{2a}{\pi}$

C. $\frac{4a}{\pi}$

D. $-\frac{4a}{\pi}$

Answer: B



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30. The value of $(\lim)_{x \rightarrow \infty} \left[\frac{2n}{2n^2} \frac{\cos(n+1)}{2n-1} - \frac{n}{1-2n} \frac{n(-1)^n}{n^2+1} \right]$ is 1 (b)

- 1 (c) 0 (d) none of these

A. 5

B. 6

C. 7

D. none of these

Answer: C



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31. If $f(x) = 0$ is a quadratic equation such that $f(-\pi) = f(\pi) = 0$ and $f\left(\frac{\pi}{2}\right) = -\frac{3\pi^2}{4}$, then $(\lim)_{x \rightarrow \pi} \frac{f(x)}{\sin(\sin x)}$ is equal to 0 (b) π (c) 2π
(d) none of these

A. $-\frac{3}{2}\pi$

B. $-\frac{1}{2}$

C. (2π)

D. $\frac{3}{2}\pi$

Answer: C



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32. $(\lim)_{x \rightarrow 1} \frac{x \sin(x - [x])}{x - 1}$, where $[.]$ denotes the greatest integer function is equal to (a) 0 (b) -1 (c) not exist (d) none of these

A. $\frac{2}{\pi - 1}$

B. $\frac{\pi + 1}{2}$

C. $\frac{2}{\pi + 1}$

D. $\frac{2(\pi + 1)}{\pi - 1}$

Answer: C



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33. $\lim_{x \rightarrow \infty} \frac{x^2 \tan \frac{1}{x}}{\sqrt{8x^2 + 7x + 1}}$ is equal to

A. 4

B. $(1/2)$

C. 2

D. $1/4$

Answer: A



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34. $(\lim)_{x \rightarrow 0} \frac{x^a \sin^b x}{\sin(x^c)}$, where a, b, c in $\mathbb{R} \setminus \{0\}$, exists and has non-zero value. Then, (a) $a + c$ (b) 1 (c) -1 (d) none of these

A. 0

B. $\pi/2$

C. π

D. 2π

Answer: C



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35. $\lim_{x \rightarrow 0} \frac{x^4(\cot^4 x - \cot^2 x + 1)}{(\tan^4 x - \tan^2 x + 1)}$ is equal to

A. -1

B. 1

C. 0

D. none of these

Answer: A

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36. $(\lim)_{x \rightarrow 1} \frac{1 - x^2}{s \in 2\pi x} \text{ is equal to } < o \frac{1}{2\pi} \text{ (b) } -\frac{1}{\pi} \text{ (c) } \frac{-2}{\pi} \text{ (d) none of these}$

A. 0

B. ∞

C. -2

D. 2

Answer: B

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37. $\lim_{x \rightarrow 0} \frac{1}{x} \cos^{-1} \left(\frac{1 - x^2}{1 + x^2} \right)$ is equal to

- A. $f(x)f(y)$
- B. $f(x) + f(y)$
- C. $f(x) - f(y)$
- D. none of these

Answer: D

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38. $(\lim)_{x \rightarrow 0} \frac{(x + y)\sec(x + y) - x \sec x}{y} \text{ is equal to } < 0$ (a)

$\sec x(x \tan x + 1)$ (b) $x \tan x + \sec x$ (c) $x \sec x + \tan x$ (d) none of these

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39. $\lim_{x \rightarrow 0} (1 + x)^{\frac{1}{3x}}$

A. $\log n \left(\frac{2}{3} \right)$

B. 0

C. $n \log n \left(\frac{2}{3} \right)$

D. not defined

Answer: A



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40. $(\lim)_{n \rightarrow \infty} \sum_{x=1}^{20} \cos^{2n}(x - 10)$ is equal to (a) 0 (b) 1 (c) 19 (d) 20

A. 2

B. -2

C. 1

D. -1

Answer: B



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41. $\lim_{x \rightarrow -1} \left(\frac{x^4 + x^2 + x + 1}{x^2 - x + 1} \right)^{\frac{1 - \cos(x+1)}{(x+1)^2}}$ is equal to

A. 1

B. -1

C. $\frac{1}{2}$

D. $-\frac{1}{2}$

Answer: B



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42. $(\lim)_{x \rightarrow \infty} \{x + 5 \tan^{-1}(x + 5) - (x + 1) \tan^{-1}(x + 1)\}$ is equal to

(a) π (b) 2π (c) $\frac{\pi}{2}$ (d) none of these

A. $\frac{1}{m2^m} - \frac{1}{n2^n}$

B. $\frac{1}{m2^m} + \frac{1}{n2^n}$

C. $\frac{1}{m2^{m-1}} - \frac{1}{n2^{n-1}}$

D. $\frac{1}{m2^{m-1}} + \frac{1}{n2^{n-1}}$

Answer: B



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43. The value of $(\lim)_{x \rightarrow 0} \left(\left[\frac{100x}{\sin x} \right] + \left[\frac{99 \sin x}{x} \right] \right)$ (where $[.]$ represents the greatest integral function) is 199 (b) 198 (c) 0 (d) none of these

A. 1

B. 0

C. $e - 1$

D. $e + 1$

Answer: B



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44. The value of $\lim_{x \rightarrow a} \sqrt{a^2 - x^2} \cot \frac{\pi}{2} \sqrt{\frac{a-x}{a+x}}$ is

A. $\frac{5050}{\pi e}$

B. $100 \frac{)}{\pi e}$

C. $-\frac{5050}{\pi e}$

D. $-\frac{4950}{\pi e}$

Answer: C



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45. $(\lim)_{x \rightarrow 0} \left[\min (y^2 - 4y + 11) \frac{\sin x}{x} \right]$ (where $[\cdot]$ denotes the greatest integer function) is 5 (b) 6 (c) 7 (d) does not exist

A. -1

B. 1

C. 0

D. 2

Answer: B



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46. The value of $\lim_{x \rightarrow 0} \frac{1 - (\cos x)\sqrt{\cos 2x}}{x^2}$ is

A. $\frac{1}{3}$

B. $\frac{1}{2}$

C. $\frac{1}{6}$

D. $\frac{5}{12}$

Answer: D



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47. $\lim_{x \rightarrow \infty} \frac{1}{x+1} \tan\left(\frac{\pi x + 1}{2x + 2}\right)$ is equal to

A. $\frac{1}{2}$

B. $-\frac{1}{2}$

C. 0

D. none of these

Answer: A



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48. The value of $(\lim)_{x \rightarrow 1^-} \frac{1 - \sqrt{x}}{(1-x)^2}$ is 4 (b) $\frac{1}{2}$ (c) 2 (d) $\frac{1}{4}$

A. $1/6$

B. $-1/3$

C. $1/2$

D. 1

Answer: D



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49. $(\lim)_{x \rightarrow \frac{\pi}{2}} \left(\frac{\sin(x \cos x)}{\cos(x \sin x)} \right)$ is equal to $a < 0$ (b) $\frac{p}{2}$ (c) p (d) $2p$

A. $a = 3$ and $b = 9/2$

B. $a = 3$ and $b = 9/2$

C. $a = -3$ and $b = -9/2$

D. $a = 3$ and $b = -9/2$

Answer: B



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50. $(\lim)_{x \rightarrow 0} \left[(1 - e^x) \frac{\sin x}{|x|} \right]$ is (where $[.]$ represents the greatest integer function). -1 (b) 1 (c) 0 (d) does not exist

A. 1

B. 2

C. 3

D. none of these

Answer: A

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51. Evaluate $\lim_{x \rightarrow 0} \frac{x(e^x - 1)}{1 - \cos x}$ is equal to

A. e

B. $\frac{1}{e}$

C. 1

D. none of these

Answer: D

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52. If $f(x) = \lim_{n \rightarrow \infty} n \left(x^{\frac{1}{n}} - 1 \right)$, then f or $x > 0, y > 0, f(xy)$ is equal to : (a) $f(x)f(y)$ (b) $f(x) + f(y)$ (c) $f(x) - f(y)$ (d) none of these

A. $f(2x) + f(2y)$

B. $f(x) + f(y)$

C. $f(x+y)$

D. $f(x) - f(y)$

Answer: B

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53. $\lim_{x \rightarrow 0} \left\{ (1+x)^{\frac{2}{x}} \right\}$ (where $\{.\}$ denotes the fractional part of x) is equal to

A. 1

B. e

C. e^{-1}

D. none of these

Answer: A



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54. The value of $(\lim)_{x \rightarrow \infty} \frac{(2^x)^n / e^x - (3^x)^n / e^x}{x^n}$ (where $n \in \mathbb{N}$)

is $\log n \left(\frac{2}{3} \right)$ (b) 0 (c) $n \log n \left(\frac{2}{3} \right)$ (d) none of defined

A. e

B. e^2

C. e^{-1}

D. 1

Answer: B



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$$55. \lim_{x \rightarrow 0} \frac{\sin(x^2)}{\ln(\cos(2x^2 - x))} \text{ is equal to } \rightarrow 2 \text{ (b) } - 2 \text{ (c) } 1 \text{ (d) } - 1$$

A. e^a

B. $-a$

C. e^{1-a}

D. e^{1+a}

Answer: B



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$$56. \lim_{x \rightarrow \infty} \frac{e^{1/x^2} - 1}{2 \tan^{-1}(x^2) - \pi} \text{ is equal to } < 0 \text{ (b) } - 1 \text{ (c) } \frac{1}{2} \text{ (d) } - \frac{1}{2}$$

A. $e^{(1-e)}$

B. $e^{\left(\frac{1-e}{e}\right)}$

C. $e^{\left(\frac{e}{1-e}\right)}$

D. $e^{\frac{1+e}{e}}$

Answer: D



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57. $(\lim)_{x \rightarrow 0} \frac{(2^m + x)^{\frac{1}{m}} - (2^n + x)^{\frac{1}{n}}}{x}$ is equal to (a) 2

$\left(\frac{1}{m2^m} - \frac{1}{n2^n}\right)$ (b) $\frac{1}{(m2^m)+1/(n2^n)}$ (c) $\frac{1}{(m2^{-m})-1/(n2^{-n})}$ (d) $\frac{1}{(m2^{-m})+1/(n2^{-n})}$

A. $(n!)^n$

B. $(n!)^{1/n}$

C. $n!$

D. $\ln(n!)$

Answer: C



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58. The value of $\lim_{n \rightarrow \infty} \frac{1}{n} [e^{\frac{1}{n}} + e^{\frac{2}{n}} + \dots + e]$ is



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59. The value of $\lim_{n \rightarrow \infty} \left[\frac{1}{n} + 2 \right]$ is



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60. $(\lim)_{x \rightarrow 0} \frac{\log(1+x+x^2) + \log(1-x+x^2)}{\sec x - \cos x} = -1$ (b) 1 (c) 0 (d) 2

A. 2

B. 1

C. $\log_a 2$

D. 0

Answer: B



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61. The value of $\lim_{x \rightarrow 0} \frac{2^{3x} - 3^{2x}}{x}$ is

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62. The value of $\lim_{x \rightarrow 0} \frac{1 + \sin x - \cos x + \log(1 - x)}{x^3}$ is

A. 1

B. -1

C. 2

D. -2

Answer: B

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63. The value of $\lim_{n \rightarrow \infty} \left[\frac{1 + 2 + 3 + \dots + n}{n^2} \right]$ is

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64. If $(\lim)_{x \rightarrow 0} (x^{-3} \sin 3x + ax^{-2} + b)$ exists and is equal to 0, then

$$a = -3 \text{ and } b = \frac{9}{2} \qquad a = 3 \text{ and } b = \frac{9}{2} \qquad a = -3 \text{ and } b = -\frac{9}{2}$$

$$a = 3 \text{ and } b = -\frac{9}{2}$$

A. $a = 1$

B. $a = 0$

C. $b = 1$

D. $b = -1$

Answer: A



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65. If $\lim_{x \rightarrow 0} \frac{x^n - \sin x^n}{x - \sin^n x}$ is non-zero finite, then n must be equal to 4 (b) 1

(c) 2 (d) 3

A. 1, if $n = m$

B. 0, if $n > m$

C. ∞ , if $n < m$

D. n/m , if $n < m$

Answer: B



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66. $(\lim)_{x \rightarrow 0} \left(\frac{1 + \tan x}{1 + \sin x} \right)^{\cos e x}$ is equal to (a) e (b) $\frac{1}{e}$ (c) 1 (d) none of

these

A. $\lim_{x \rightarrow 0} f(x)$ exists for $n > 0$

B. $\lim_{x \rightarrow 0} f(x)$ does not exist for $n < 0$

C. $\lim_{x \rightarrow 0} f(x)$ does not exist for any value of n

D. $\lim_{x \rightarrow 0} f(x)$ exists for any value of n

Answer: C



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67. The value of $\lim_{x \rightarrow 1} (2 - x)^{\tan\left(\frac{\pi x}{2}\right)}$ is

A. $a = 1/4$

B. $b = 3/4$

C. $L = -1/32$

D. $L = 1/32$

Answer: C



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68. The value of $(\lim_{x \rightarrow \infty} \left(\frac{\cos x}{m}\right)^m)$ is 1 (b) e (c) e^{-1} (d) none of these

A. $\lim_{x \rightarrow \infty} \frac{\log_e x}{\{x\}} = \infty$

B. $\lim_{x \rightarrow 2^+} \frac{x}{x^2 - x - 2} = \infty$

C. $\lim_{x \rightarrow -1^-} \frac{x}{x^2 - x - 2} = \infty$

D. $\lim_{x \rightarrow \infty} \frac{\log_{0.5} x}{\{x\}} = \infty$

Answer: A



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69. $(\lim)_{x \rightarrow \infty} \left(\frac{n^2}{n^2} \right)^{n(n-1)}$ *isequa < o* e (b) e^2 (c) e^{-1} (d) 1

A. $\lim_{x \rightarrow 0} \frac{[x + |x|]}{x} = 0$, where $[x]$ denotes the greatest integer

functions.

B. $\lim_{x \rightarrow 0} \frac{x e^{\frac{1}{x}}}{1 + e^{\frac{1}{x}}} = 0$

C. $\lim_{x \rightarrow 3} (x - 3)^{\frac{1}{5}} \operatorname{sgn}(x - 3) = 0$, where sgn stands for signum

function.

D. $\lim_{x \rightarrow 0} \frac{\tan^{-1}|x|}{x} = 0$

Answer: B



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70. $(\lim)_{n \rightarrow \infty} \left\{ \left(\frac{n}{n+1} \right)^\alpha + \sin\left(\frac{1}{n}\right) \right\}^n$ (when $\alpha \in \mathbb{Q}$) is equal to (a) $e^{-\alpha}$
(b) $-\alpha$ (c) $e^{1-\alpha}$ (d) $e^{1+\alpha}$

A. $a = 1/3, b = 1$

B. $a = 1, b = -1$

C. $a = 9, b = -9$

D. $a = 2, b = 2/3$

Answer: C



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71. $(\lim)_{x \rightarrow \infty} \left[\left(\frac{e}{1-e} \right) \left(\frac{1}{e} - \frac{x}{1+x} \right) \right]^\xi$ (a) $e^{(1-e)}$ (b) $e^{\left(\frac{1-e}{e}\right)}$ (c) $e^{\left(\frac{e}{1-e}\right)}$
(d) $e^{\left(\frac{1+e}{e}\right)}$

A. limit does not exist when $a = \pi/6$

B. $L = -1$ when $a = \pi$

C. $L = 1$ when $a = \pi/2$

D. $L = 1$ when $a = 0$

Answer: C

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72. $(\lim_{x \rightarrow 0} \left(\frac{1^x + 2x + 3^x + \dots + n^x}{n} \right)^{1/x})$ is equal to (a) $(n!)^n$ (b) $(n!)^{\frac{1}{n}}$ (c) $n!$ (d) $\ln(n!)$

A. $f(1^+) + f(1^-) = 0$

B. $f(1^+) + f(1^-) + f(1) = 3/2$

C. $f(-1^+) + f(-1^-) = -1$

D. $f(1^+) + f(-1^-) = 0$

Answer: B

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73. If $p > q > 0$ and $r < -1$

A. $-\frac{3}{4}$

B. 0 if n is even

C. $-\frac{3}{4}$ if n is odd

D. none of these

Answer: C



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74. $(\lim)_{x \rightarrow \infty} \frac{x(\log x)^3}{1+x+x^2}$ equal 0 (b) -1 (c) 1 (d) none of these

A. $f(x) = 1$
 $x \rightarrow 0^+$

B. $\lim_{x \rightarrow 0^-} f(x) = \cot 1$

C. $\cot^{-1} \left(\lim_{x \rightarrow 0^-} f(x) \right) = 1$

D. $\tan^{-1} \left(\lim_{x \rightarrow 0^+} f(x) \right) = \frac{\pi}{4}$

Answer: A



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75. $(\lim)_{x \rightarrow \infty} \left(\frac{\cot^{-1}(x^{-a}(\log)_a x)}{\sec^{-1}(a^x(\log)_x a)}, (a > 1) \right)$ 2 (b) 1 (c) $(\log)_a 2$

(d) 0

A. $\lim_{x \rightarrow 1} f(x)$ exists $\Rightarrow a = -2$

B. $f(x)$ exists $\Rightarrow a = 13$
 $x \rightarrow -2$

C. $f(x) = 4/3$ if it exists
 $x \rightarrow 1$

D. $\lim_{x \rightarrow -2} f(x) = -1/3$ if it exists

Answer: B



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76. The value of $\lim_{n \rightarrow \infty} \frac{e^n}{\left(1 + \frac{1}{n}\right)^{n^2}}$ is

A. -1

B. 0

C. 1

D. ∞

Answer: C



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Exercise (Multiple)

1.

Let

$$f(x) = \begin{cases} 1 + \frac{2x}{a}, & 0 \leq x < 1 \\ ax, & 1 \leq x < 2 \end{cases}$$

If $\lim_{x \rightarrow 1} f(x)$ exists, then a is

1 (b) -1 (c) 2 (d) -2

A. $\lim_{x \rightarrow 5^-} f(x) = 0$

B. $\lim_{x \rightarrow 5^+} f(x) = 1$

C. $\lim_{x \rightarrow 5} f(x)$ does not exist

D. none of these

Answer: B::C

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2. If $f(x) = |x - 1| - [x]$, where $[x]$ is the greatest integer less than or equal to x , then $f(1 + 0) = 1$, $f(1 - 0) = 0$, $f(1 + 0) \neq 0 = f(1 - 0)$

$(\lim)_{x \rightarrow 1} f(x)$ exists $(\lim)_{x \rightarrow 1} f(x)$ does not exist

A. $\lim_{x \rightarrow 0} [f(x)] = 0$

B. $\lim_{x \rightarrow 0} [f(x)] = 1$

C. $\lim_{x \rightarrow 0} \left[\frac{f(x)}{x} \right]$ does not exist

D. $\lim_{x \rightarrow 0} \left[\frac{f(x)}{x} \right]$ exists

Answer: A::D

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3. $(\lim)_{x \rightarrow \infty} \left(an - \frac{1 + n^2}{1 + n} \right) = b$, where a is a finite number, then (a)

$a = 1$ (b) $a = 0$ (c) $b = 1$ (d) $b = -1$

A. $f(0) = 1$

B. $f\left(\frac{\pi}{2}\right) = 1$

C. $f(a) = (\cos a)^{\cos^2 a} \cdot (\sin a)^{\sin^2 a}$ if $a \in \left(0, \frac{\pi}{2}\right)$

D. $f(a) = \frac{(\sin a)^{\sin^2 a}}{(\cos a)^{\cos^2 a}}$ if $a \in \left(0, \frac{\pi}{2}\right)$

Answer: A:C

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4. If $m, n \in N$, $(\lim)_{x \rightarrow 0} \frac{\sin x^m}{(\sin x)^m}$ is 1, if $n = m$ (b) 0, if $n > m$

oo, ifn

A. $\frac{p}{2}$

B. $\frac{\pi}{2\sqrt{2}}$

C. $\frac{\pi}{\sqrt{2}}$

D. $\sqrt{2}\pi$

Answer: A::B::C



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5. If $f(x) = \begin{cases} x^n \sin\left(\frac{1}{x^2}\right), & x \neq 0 \\ 0, & x = 0 \end{cases}$, $(n \in I)$, then $(\lim)_{x \rightarrow 0} f(x)$ exists or $n > 1$ $(\lim)_{x \rightarrow 0} f(x)$ exists or $n < 0$ $(\lim)_{x \rightarrow 0} f(x)$ does not exist for any value of n $(\lim)_{x \rightarrow 0} f(x)$ cannot be determined

A. $\frac{\pi}{2}$

B. $\frac{\pi}{2\sqrt{2}}$

C. $\frac{\pi}{\sqrt{2}}$

D. $\sqrt{2}\pi$

Answer: A::B



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6. If $L = \lim_{x \rightarrow 0} \frac{1}{x^3} \left(\frac{1}{\sqrt{1+x}} - \frac{1+ax}{1+bx} \right)$ exists, then

A. $\cos L < \cos R$

B. $\tan(2L) < an < 2R$

C. $\sin L > \sin R$

D. None of these

Answer: A::B::C



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7. Which of the following is true?

A. always 1

B. always -1

C. $(-1)^{n-m+1}$

D. $(-1)^{n-m}$

Answer: A::B::C



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8. The value of $\lim_{n \rightarrow 0} \left[\frac{1 + 2 + 3 + \dots + n}{n^2} \right]$ is



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9. If $(\lim)_{x \rightarrow 1^-} (2 - x + a[x - 1] + b[1 + x])$ exists, then a and b can take the values of (where $[.]$ denotes the greatest integer function). (a) $a = \frac{1}{3}, b = 1$ (b) $a = 1, b = -1$ (c) $a = 9, b = -9$ (d) $a = 2, b = \frac{2}{3}$

A. is always equal to -1

B. is always equal to +1

C. does not exist None of these

D.

Answer: B::C



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10. $L = \lim_{x \rightarrow a} \frac{|2 \sin x - 1|}{2 \sin x - 1}$. Then limit does not exist when $a = \frac{\pi}{6}$
 $L = -1$ when $a = \pi$ $L = 1$ when $a = \frac{\pi}{2}$ $L = 1$ when $a = 0$

A. $1/2$

B. $-1/3$

C. $-1/6$

D. 3

Answer: A::B::C



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11. Let $f(x) = \lim_{n \rightarrow \infty} \frac{x}{x^{2n} + 1}$. Then

A. real and equal roots

B. complex roots

C. unequal positive real roots

D. unequal roots

Answer: B::C::D



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12. $\lim_{n \rightarrow \infty} \frac{-3n + (-1)^n}{4n - (-1)^n}$ is equal to ($n \in \mathbb{N}$)

A. $[-2, 2]$

B. $[0, 2]$

C. $[-1, 1]$

D. $[-2, 1]$

Answer: A::C



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13. Given a real valued function f such that

$$f(x) = \begin{cases} \frac{\tan^2[x]}{x^2 - [x]^2}, & x < 0 \text{ and } 1, \\ x = 0 \text{ and } \sqrt{\{x\}\cot\{x\}}, & x < 0 \end{cases}$$

where $[.]$ represents greatest integer function then

A. $p_1 \ln a_1 + p_2 \ln a_2 + \dots + p_n \ln a_n$

B. $a_1^{p_1} + a_2^{p_2} + \dots + a_n^{p_n}$

C. $a_1^{p_1} \cdot a_2^{p_2} \dots a_n^{p_n}$

D. $\sum_{r=1}^n a_r p_r$

Answer: A::B::C::D



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14. If $f(x) = \frac{3x^2 + ax + a + 1}{x^2 + x - 2}$, then which of the following can be correct

(a) $(\lim)_{x \rightarrow 1} f(x) \text{ exists } a = -2$ (b)

$(\lim)_{x \rightarrow -2} f(x) \text{ exists } a = 13$ (c) $(\lim)_{x \rightarrow 1} f(x) = \frac{4}{3}$ (d)

$(\lim)_{x \rightarrow -2} f(x) = -\frac{1}{3}$

A. $\ln a_1$

B. e^{a_n}

C. $a_{(1)}$

D. a_n

Answer: A::B::C::D



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15. The value of $\lim_{n \rightarrow \infty} \left[\frac{1}{n} + 2 \right]$ is

A. $\ln a_n$

B. e^{a_1}

C. a_1

D. a_n

Answer: B::C



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16. Let $f(x) = \frac{x^2 - 9x + 20}{x - [x]}$ where $[x]$ denotes greatest integer less than or equal to x , then

A. -1

B. $1/2$

C. 1

D. $3/2$

Answer: A::B::C

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17. Given $(\lim)_{x \rightarrow 0} \frac{f(x)}{x^2} = 2$, where $[.]$ denotes the greatest integer function, then (a) $(\lim)_{x \rightarrow 0} [f(x)] = 0$ (b) $(\lim)_{x \rightarrow 0} [f(x)] = 1$ (c) $(\lim)_{x \rightarrow 0} \left[\frac{f(x)}{x} \right]$ does not exist (d) $(\lim)_{x \rightarrow 0} \left[\frac{f(x)}{x} \right]$ exists

A. $\frac{1}{3}$

B. $\frac{1}{4}$

C. $\frac{1}{2}$

D. $\frac{2}{3}$

Answer: A::C



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18. If $f(a) = \lim_{x \rightarrow 2} (\sin^x a + \cos^x a)^{\frac{1}{(x-2)}}$ for $a \in \left[0, \frac{\pi}{2}\right]$, then

A. $-np$

B. np

C. n^2p

D. np^2

Answer: A::B::C



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Exercise (Comprehension)

1. Find the domain of $f(x) = \sqrt{|x| - \{x\}}$ (where $\{\cdot\}$ denotes the fractional part of x).

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2. Let $f(x) = \frac{\sin^{-1}(1 - \{x\}) \times \cos^{-1}(1 - \{x\})}{\sqrt{2}\{x\} \times (1 - \{x\})}$, where $\{x\}$ denotes the fractional part of x .

$R = \lim_{x \rightarrow 0^+} f(x)$ is equal to

A. $\frac{\pi}{2}$

B. $\frac{\pi}{2\sqrt{2}}$

C. (π)

D. $\frac{1}{2\sqrt{2}}$

Answer: B

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3. Integrate $\frac{\cos^{-1} x}{-\sqrt{1-x^2}}$

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4. $A_i = \frac{x - a_i}{|x - a_i|}$, $i = 1, 2, \dots, n$, and $a_1 < a_2 < a_3 < \dots < a_n$.

If $1 \leq m \leq n$, $\min N$, then the value of $L = \lim_{x \rightarrow a_m} (A_1 A_2 \dots A_n)$ is

A. 2

B. -1

C. not exist

D. 1

Answer: C

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5. $A_i = \frac{x - a_i}{|x - a_i|}$, $i = 1, 2, \dots, n$, and $a_1 < a_2 < a_3 < \dots < a_n$.

If $1 \leq m \leq n$, $\min N$, then the value of $R = \lim_{x \rightarrow a_m^+} (A_1 A_2 \dots A_n)$ is

A. $e^{-\frac{1}{4}}$

B. $e^{-\frac{1}{2}}$

C. e^{-2}

D. e^{-4}

Answer: D



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6. $A_i = \frac{x - a_i}{|x - a_i|}$, $i = 1, 2, \dots, n$, and $a_1 < a_2 < a_3 < \dots < a_n$.

If $1 \leq m \leq n$, $\min N$, then $\lim_{x \rightarrow a_m} (A_1 A_2 \dots A_n)$



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7. If $L = \lim_{x \rightarrow 0} \frac{\sin x + ae^x + be^{-x} + c \log_e(1+x)}{x^3}$ exists finitely, then

The value of L is

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8. If $L = \lim_{x \rightarrow 0} \frac{\sin x + ae^x + be^{-x} + c \log_e(1+x)}{x^3}$ exists finitely, then

Equation $ax^2 + bx + c = 0$ has

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9. If $L = \lim_{x \rightarrow 0} \frac{\sin x + ae^x + be^{-x} + c \log_e(1+x)}{x^3}$ exists finitely, then

The solutions set of $||x + c| - 2a| < 4b$ is

A. $\begin{matrix} a & b & c & d \\ s & r & q & p \end{matrix}$

B. $\begin{matrix} a & b & c & d \\ q & s & r & p \end{matrix}$

C. $\begin{matrix} a & b & c & d \\ s & r & p & q \end{matrix}$

D. $\begin{matrix} a & b & c & d \\ s & p & q & r \end{matrix}$

Answer: C



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10. Let $a_1 > a_2 > a_3 > \dots > a_n > 1$.

$p_1 > p_2 > p_3 > \dots > p_n > 0$ such that $p_1 + p_2 + p_3 + \dots + p_n = 1$.

Also, $F(x) = (p_1 a_1^x + p_n a_n^x)^{1/x}$.

$\lim_{x \rightarrow 0^+} F(x)$ equals

A. $\begin{matrix} a & b & c & d \\ s & r & q & p \end{matrix}$

B. $\begin{matrix} a & b & c & d \\ q & p & s & p \end{matrix}$

C. $\begin{matrix} a & b & c & d \\ s & r & p & q \end{matrix}$

D. $\begin{matrix} a & b & c & d \\ p & p & q & r \end{matrix}$

Answer: C



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11. Let $a_1 > a_2 > a_3 > \dots > a_n > 1$.

$p_1 > p_2 > p_3 > \dots > p_n > 0$ such that $p_1 + p_2 + p_3 + \dots + p_n = 1$.

Also, $F(x) = (p_1 a_1^x + p_n a_n^x)^{1/x}$.

$\lim_{x \rightarrow \infty} F(x)$ equals

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12. Let $a_1 > a_2 > a_3 \dots a_n > 1$ $p_1 > p_2 > \dots p_n > 0$; such that $p_1 + p_2 + p_3 + p_n = 1$. Also $F(x) = (p_1 a_1^x + p_2 a_2^x + \dots + p_n a_n^x)^{\frac{1}{x}}$

Then $\lim_{x \rightarrow \infty} F(x)$ equals

A. $\ln a_1$

B. $\ln a_n$

C. a_1

D. a_n

Answer: D

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13. If $L = \lim_{x \rightarrow \infty} (x + 1 - \sqrt{ax^2 + x + 3})$ exists infinitely then

The value of a is

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14. If $L = \lim_{x \rightarrow \infty} (x + 1 - \sqrt{ax^2 + x + 3})$ exists finitely then

The value of L is

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15. The value of $\lim_{n \rightarrow \infty} \left[\frac{1 + 2 + 3 + \dots + n}{n^2 + 5n + 2} \right]$ is

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16. Evaluate $\lim_{n \rightarrow \infty} \left[\frac{1 + 2 + 3 + \dots + n}{5n^2 + 2n + 1} \right]$

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17. Let $f(x)$ be a polynomial satisfying

$$\lim_{x \rightarrow \infty} \frac{x^2 f(x)}{2x^5 + 3} = 6 \text{ and } f(1) = 3, f(3) = 7 \text{ and } f(5) = 11. \text{ Then}$$

The value of $f(0)$ is



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18. Let $f(x)$ be a polynomial satisfying

$$\lim_{x \rightarrow \infty} \frac{x^2 f(x)}{2x^5 + 3} = 6 \text{ and } f(1) = 3, f(3) = 7 \text{ and } f(5) = 11. \text{ Then}$$

$$\lim_{x \rightarrow 1} \frac{x - 1}{\sin(f(x) - 2x - 1)}$$
 is equal to



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19. If $\lim_{x \rightarrow 0} \frac{f(x)}{\sin^2 x} = 8$, $\lim_{x \rightarrow 0} \frac{g(x)}{2 \cos x - xe^x + x^3 + x - 2} = \lambda$ and

$$\lim_{x \rightarrow 0} (1 + 2f(x))^{\frac{1}{g(x)}} = \frac{1}{e}, \text{ then}$$

The value of λ is



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20. If $\lim_{x \rightarrow 0} \frac{f(x)}{\sin^2 x} = 8$, $\lim_{x \rightarrow 0} \frac{g(x)}{2 \cos x - xe^x + x^3 + x - 2} = \lambda$ and

$\lim_{x \rightarrow 0} (1 + 2f(x))^{\frac{1}{g(x)}} = \frac{1}{e}$, then

$\lim_{x \rightarrow 0} (1 + f(x))^{\frac{1}{2g(x)}}$ is equal to



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Exercise (Matrix)

1. Match the following lists:

| List I | List II |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------|
| a. If $L = \lim_{x \rightarrow -1} \frac{\sqrt[3]{(7-x)} - 2}{(x+1)}$, then $12L =$ | p. -2 |
| b. If $L = \lim_{x \rightarrow \pi/4} \frac{\tan^3 x - \tan x}{\cos\left(x + \frac{\pi}{4}\right)}$, then $-L/4 =$ | q. 2 |
| c. If $L = \lim_{x \rightarrow 1} \frac{(2x-3)(\sqrt{x}-1)}{2x^2+x-3}$, then $20L =$ | r. 1 |
| d. If $L = \lim_{x \rightarrow \infty} \frac{\log x^n - [x]}{[x]}$, where $n \in N$, $([x]$ denotes greatest integer less than or equal to x), then $-2L =$ | s. -1 |



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2. Match the following :

- | | |
|---------------------|------------------------------|
| A V_3O_5 | i. High density polyethylene |
| B Ziegler - Natta | ii. PAN |
| C Peroxide | iii. NH_3 |
| D Finely divided Fe | iv. H_2SO_4 |

A B C D

- (a) (iv) (i) (ii) (iii)
 (b) (i) (ii) (iv) (iii)
 (c) (ii) (iii) (iv) (i)
 (d) (iii) (iv) (ii) (i)



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3. Match the following lists:

| List I | List II |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------|
| a. If $\lim_{x \rightarrow \infty} (\sqrt{x^2 - x - 1} - ax - b) = 0$, where $a > 0$, then there exists at least one a and b for which point $(a, 2b)$ lies on the line. | p. $y = -3$ |
| b. If $\lim_{x \rightarrow \infty} \frac{(1 + a^3) + 8e^{1/x}}{1 + (1 - b^3)e^{1/x}} = 2$, then there exists at least one a and b for which point (a, b^3) lies on the line. | q. $3x - 2y - 5 = 0$ |
| c. If $\lim_{x \rightarrow \infty} (\sqrt{x^4 - x^2 + 1} - ax^2 - b) = 0$, then there exists at least one a and b for which point $(a, -4b)$ lies on the line. | r. $15x - 2y - 11 = 0$ |
| d. If $\lim_{x \rightarrow -a} \frac{x^7 + a^7}{x + a} = 7$, where $a < 0$, then there exists at least one a for which point $(-a, 2)$ lies on the line. | s. $y = 2$ |



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4. Match the following

| S.No. | Column-A | Column-B |
|-------|---------------------------------------------------------------------------------------------------------------|----------------|
| (a) | The parallelogram that is inscribed in a circle is a | (i) square |
| (b) | The parallelogram having all of its sides equal is called a | (ii) rectangle |
| (c) | The diagonals of a quadrilateral are unequal and bisect each other necessarily at right angles. It is a | (iii) kite |
| (d) | The diagonals of a parallelogram are equal and bisect each other at right angles. It is a | (iv) rhombus |



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5. Match the following lists (where $[x]$ represents the greatest integer function) and then choose the correct code.

| List I | List II |
|--------------------------------------------------------------------------------|-------------------|
| a. $\lim_{x \rightarrow 0} x(-1)^{[1/x]}$ | p. Does not exist |
| b. $\lim_{x \rightarrow 2} (-1)^{[x]}$ | q. is 0 |
| c. $\lim_{x \rightarrow \frac{3}{2}} (x - [x])$ | r. is 1 |
| d. $\lim_{x \rightarrow 0} [x] \left(\frac{e^{1/x} - 1}{e^{1/x} + 1} \right)$ | s. is 2 |

Codes :

a b c d

(1) s r q p

(2) q p s p

(3) s r p q

(4) p p q r



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Exercise (Numerical)

1. The reciprocal of the value of:

$$\left(\lim\right)_{n \rightarrow \infty} \left(1 - \frac{1}{2^2}\right) \left(1 - \frac{1}{3^2}\right) \left(1 - \frac{1}{4^2}\right) \left(1 - \frac{1}{n^2}\right) \text{ is}$$



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2. $\lim_{x \rightarrow \infty} f(x)$, where $\frac{2x-3}{x} < f(x) < \frac{2x^2+5x}{x^2}$, is



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3.

if

$$f(x) = \begin{cases} x - 1, & x \geq 1 \\ 2x^2 - 2, & x < 1 \end{cases}, g(x) = \begin{cases} x + 1, & x > 0 \\ -x^2 + 1, & x \leq 0 \end{cases}$$

$h(x) = |x|$, then $(\lim_{x \rightarrow 0} f(g(h(x))))$ is ___



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4. If $(\lim_{x \rightarrow \infty} f(x))$ exists and is finite and nonzero and if

$$(\lim_{x \rightarrow \infty} \left\{ f(x) + \frac{3f(x) - 1}{f^2(x)} \right\}) = 3, \text{ then the value of } (\lim_{x \rightarrow \infty} f(x)) \text{ is } _$$



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5. If $L = (\lim_{x \rightarrow 2} \frac{(10 - x)^{\frac{1}{3}} - 2}{x - 2})$, then the value of $|1 - 4L|$ is ___



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6. If $\lim_{x \rightarrow 0} \frac{p \sin 2x + (1 - \cos 2x)}{x + \tan x} = 1$, then the value of p is _____.



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7. The value of $\lim_{x \rightarrow \infty} \left(\frac{100}{1 - x^{100}} - \frac{50}{1 - x^{50}} \right)$ is _____.

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8. If $L = (\lim)_{x \rightarrow 2} \frac{(10 - x)^{\frac{1}{3}} - 2}{x - 2}$, then the value of $|1(4L)|$ is _ _

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9. The value of $\lim_{x \rightarrow \infty} \left(\frac{100}{1 - x^{100}} - \frac{50}{1 - x^{50}} \right)$ is _____.

A. 4

B. 1

C. $\frac{2}{3}$

D. $\frac{3}{2}$

Answer: (4)



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10. The value of $(\lim)_{x \rightarrow \infty} \left[3\sqrt{(n+1)^2} - 3\sqrt{(n-1)^2} \right]$ is _____

A. Equals $\frac{1}{\sqrt{2}}$

B. Does not exist

C. Equals $\sqrt{2}$

D. Equals $-\sqrt{2}$

Answer: (0)



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11. If $L = (\lim)_{n \rightarrow \infty} (2x3^2x2^3x3^4 \dots \cdot x2^{n-1}x3^n)^{\frac{1}{(n^2+1)}}$, then the value of L^4 is

A. $-\frac{1}{4}$

B. $\frac{1}{2}$

C. 1

D. 2

Answer: (6)



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12. The value of $(\lim)_{x \rightarrow \infty} \left((\log)_e \frac{(\log)_e x}{e^{\sqrt{x}}} \right)$ is _____ ,

A. $\frac{\pi}{2}$

B. 1

C. $-\pi$

D. π

Answer: (0)



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A. 4

B. 3

C. 2

D. 1/2

Answer: (6)



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14. The value of $\lim_{x \rightarrow \infty} \left(x - x^2 \log_e \left(1 + \frac{1}{x} \right) \right)$ is _____.

A. 1

B. $\frac{1}{2}$

C. $\frac{1}{4}$

D. 2

Answer: (0.5)

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15.

Let

$$S_n = 1 + 2 + 3 + \dots + n \text{ and } P_n = \frac{S_2}{S_2 - 1} \cdot \frac{S_3}{S_3 - 1} \cdot \frac{S_4}{S_4 - 1} \dots \frac{S_n}{S_n - 1}$$

, where $n \in N, (n \geq 2)$ Then $\lim_{n \rightarrow \infty} P_n =$ _____.

A. 1

B. 2

C. 3

D. 4

Answer: (3)

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16. If $(\lim)_{x \rightarrow 1} \frac{a \sin(x - 1) + b \cos(x - 1) + 4}{x^2 - 1} = -2$, then $|a + b|$ is _____

A. does not exist (in \mathbb{R})

B. is equal to 0

C. is equal to 15

D. is equal to 120

Answer: (8)



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17. Let $(\lim)_{x \rightarrow 1} \frac{x^a - ax + a - 1}{(x - 1)^2} = f(a)$. Then the value of $f(4)$ is _____

A. $\pm \frac{\pi}{4}$

B. $\pm \frac{\pi}{3}$

C. $\pm \frac{\pi}{6}$

D. $\pm \frac{\pi}{2}$

Answer: (6)



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18. Evaluate $\lim_{x \rightarrow 1} \left(\frac{2}{1-x^2} - \frac{1}{1-x} \right)$.



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19. If: $(\lim)_{x \rightarrow 1} (1 + ax + bx^2)^{\frac{c}{(x-1)}} = e^3$, then the value of abc is ___

A. $a = 2$

B. $a = 1$

C. $L = \frac{1}{64}$

D. $L = (1)/(32)$

Answer: (3)

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20. Let $f''(x)$ be continuous at $x = 0$. If $\lim_{x \rightarrow 0} \left(2f(x) - 3a \frac{f(2x) + bf(8x)}{\sin^2 x} \right)$ exists and $f(0) \neq 0$, $f'(0) \neq 0$, then the value of $\frac{3a}{b}$ is ----

- A. $\lim_{x \rightarrow 1^+} f(x) = 0$
- B. $\lim_{x \rightarrow 1^-} f(x)$ does not exist
- C.
- D.

Answer: (7)

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21. If $L = \lim_{x \rightarrow 0} \frac{e^{-\left(\frac{x^2}{2}\right)} - \cos x}{x^3 \sin x}$, then the value of $\frac{1}{(3L)}$ is --

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22. The integer n for which $(\lim)_{x \rightarrow 0} \left((\cos x - 1) \frac{\cos x - e^{\widehat{x}}}{x^n} \right)$ is finite nonzero number is _____

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23. If $(\lim)_{x \rightarrow 0} \left[1 + x + \frac{f(x)}{x} \right]^{\frac{1}{x}} = e^3$, then find the value of $1n \left((\lim)_{x \rightarrow 0} \left[1 + \frac{f(x)}{x} \right]^{\frac{1}{x}} \right)$ is _ _

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JEE Main Previous Year

1. Let $f: R \rightarrow R$ be a positive, increasing function with

$\lim_{x \rightarrow \infty} \frac{f(3x)}{f(x)} = 1$. Then $\lim_{x \rightarrow \infty} \frac{f(2x)}{f(x)}$ is equal to

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2. Show that the $\lim_{x \rightarrow 2} \left(\frac{\sqrt{1 - \cos\{2(x - 2)\}}}{x - 2} \right)$ does not exist.

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3. $\lim_{x \rightarrow 0} \frac{(1 - \cos 2x)(3 + \cos x)}{x \tan 4x}$ is equal to

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4. $(\lim)_{x \rightarrow 0} \left(\frac{\sin(\pi \cos^2 x)}{x^2} \right)$ is equal to (a) $\frac{\pi}{2}$ (b) π (c) $\frac{\pi}{2}$ (d) 1

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5. $\lim_{x \rightarrow 0} \frac{(1 - \cos 2x)(3 + \cos x)}{x \tan 4x}$ is equal to

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6. Let $p = \lim_{x \rightarrow 0^+} (1 + \tan^2 \sqrt{x})^{\frac{1}{2x}}$. Then $\log_e p$ is equal to

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7. The $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\cot x - \cos x}{(\pi - 2x)^3}$ equals

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8. For each $t \in R$, let $[t]$ be the greatest integer less than or equal to

t. Then $\lim_{x \rightarrow 0^+} x \left(\left[\frac{1}{x} \right] + \left[\frac{2}{x} \right] + \dots + \left[\frac{15}{x} \right] \right)$

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JEE Advanced Previous Year

1.

If

$$\lim_{x \rightarrow 0} [1 + x \ln(1 + b^2)]^{1/x} = 2b \sin^2 \theta, b > 0, \text{ and } \theta \in (-\pi, \pi],$$

then the value of θ is

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2. If $(\lim)_{x \rightarrow \infty} \left(\frac{x^2 + x + 1}{x + 1} - ax - b \right) = 4$, then $a = 1, b = 4$ (b)

$a = 1, b = -4$ $a = 2, b = -3$ (d) $a = 2, b = 3$

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3. Let $L = \lim_{x \rightarrow 0} \frac{a - \sqrt{a^2 - x^2} - \frac{x^2}{4}}{x^4}$, $a > 0$. If L is finite, then

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4. Let $f(x) = \left(\frac{1 - x(1 + |1 - x|)}{|1 - x|} \right) \cos \left(\frac{1}{1 - x} \right)$ for $x \neq 1$

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7. Let $\alpha, \beta \in R$ be such that $\lim_{x \rightarrow 0} \frac{x^2 \sin(\beta x)}{\alpha x - \sin x} = 1$. Then $6(\alpha + \beta)$ equals _____.



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Single Correct Answer Type

1. If $f: R \rightarrow R$ is defined by $f(x) = [x - 3] + |x - 4|$ for $x \in R$, then

$\lim_{x \rightarrow 3^-} f(x)$ is equal to (where $[.]$ represents the greatest integer

function)

A. -2

B. -1

C. 0

D. 1

Answer: C



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2. $\lim_{x \rightarrow \frac{\pi}{2}} \left[\frac{[\sin x] - [\cos x] + 1}{3} \right] =$ (where $[\cdot]$ denotes the greatest integer function)

A. 0

B. 1

C. -1

D. does not exist

Answer: A



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3. $(\lim_{x \rightarrow \frac{-1}{3}}) \frac{1}{x} \left[\frac{-1}{x} \right] =$ (where $[.]$ denotes the greatest integer function) a. -9 b. -12 c. -6 d. 0

A. -9

B. -12

C. -6

D. 0

Answer: C



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4. If $f(x) = \begin{cases} x + \frac{1}{2}, & x < 0 \\ 2x + \frac{3}{4}, & x > 0 \end{cases}$, then $(\lim_{x \rightarrow 0} f(x)) =$ (where $[.]$ denotes the greatest integer function) a.

b. c. does not exist d. none of these

A. $\frac{1}{2}$

B. $\frac{3}{4}$

C. does not exist

D. none of these

Answer: C



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5. $\lim_{x \rightarrow -7} \frac{[x]^2 + 15[x] + 56}{\sin(x + 7)\sin(x + 8)} =$ (where $[.]$ denotes the greatest integer function)

A. is 0

B. is 1

C. is -1

D. does not exist

Answer: A



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6. Which of the following limits exists finitely?

A. $\lim_{x \rightarrow 0^+} (x)^{\log_e x}$

B. $\lim_{x \rightarrow 1^+} \frac{x^2 - 9 - \sqrt{x^2 - 6x + 6}}{|x - 1| - 2}$

C. $\lim_{x \rightarrow 1^+} ([x])^{\frac{1}{x-1}} =$ (where $[.]$ denotes the greatest integer function)

D. none of these

Answer: C



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7. Let $L_1 = \lim_{x \rightarrow 4} (x - 6)^x$ and $L_2 = \lim_{x \rightarrow 4} (x - 6)^4$.

Which of the following is true?

- A. Both L_1 and L_2 exists
- B. Neither L_1 nor L_2 exists
- C. L_1 exists but L_2 does not exist
- D. L_2 exists but L_1 does not exist

Answer: D

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8. Set of all values of x such that $\lim_{n \rightarrow \infty} \frac{1}{1 + \left(\frac{4 \tan^{-1}(2\pi x)}{\pi}\right)^{4n}}$ is non-zero and finite number when $n \in \mathbb{N}$ is

- A. $\left(0, \frac{1}{2\pi}\right)$
- B. $\left(-\frac{1}{\pi}, \frac{1}{\pi}\right)$
- C. $\left[-\frac{1}{2\pi}, \frac{1}{2\pi}\right]$
- D. $\left(-\frac{1}{2\pi}, 0\right)$

Answer: C



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9. $\lim_{x \rightarrow \infty} \left[x - \log_e \left(\frac{e^x + e^{-x}}{2} \right) \right] =$

A. $\log_e 4$

B. 0

C. $\log_e 2$

D. ∞

Answer: C



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10. $\lim_{x \rightarrow \infty} \left\{ (e^x + \pi^x)^{\frac{1}{x}} \right\} =$ (where $\{.\}$ denotes the fractional part of x) is equal to

A. $\pi - e$

B. $\pi - 3$

C. $e - 2$

D. $3 - e$

Answer: B



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11. If $\frac{\cos x}{\sin ax}$ is periodic function, then

$\lim_{m \rightarrow \infty} (1 + \cos^{2m} n! \pi a)$ is equal to

A. 0

B. 1

C. 2

D. -1

Answer: C

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12. The value of $\lim_{x \rightarrow 0} \frac{\sqrt{1 - \cos x^2}}{1 - \cos x}$ is

A. $\frac{1}{2}$

B. 2

C. $\sqrt{2}$

D. none of these

Answer: C

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13. $\lim_{x \rightarrow \frac{\pi}{2}} (1 - \sin x)\tan x =$

A. $\frac{\pi}{2}$

B. 1

C. 0

D. ∞

Answer: C



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14. The value of $\lim_{x \rightarrow \infty} x^2 \left(1 - \cos. \frac{1}{x} \right)$ is

A. 0

B. $1/4$

C. $1/2$

D. 1

Answer: C



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15. $\lim_{x \rightarrow \infty} \sqrt[3]{x} \left(\sqrt[3]{(x+1)^2} - \sqrt[3]{(x-1)^2} \right) =$

A. $\frac{1}{3}$

B. $\frac{2}{3}$

C. 1

D. $\frac{4}{3}$

Answer: D



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16. $\lim_{n \rightarrow \infty} \frac{3 \cdot 2^{n+1} - 4 \cdot 5^{n+1}}{5 \cdot 2^n + 7 \cdot 5^n} =$

A. 0

B. 43529

C. $-4/7$

D. $-20/7$

Answer: D



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17. $\lim_{x \rightarrow 2^+} \{x\} \frac{\sin(x-2)}{(x-2)^2} =$ (where $\{ \}$ denotes the fractional part function)

A. 0

B. 2

C. 1

D. does not exist

Answer: C



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18. $\lim_{x \rightarrow \infty} \frac{\cot^{-1}(\sqrt{x+1} + \sqrt{x})}{\sec^{-1}\left\{\left(\frac{2x+1}{x-1}\right)^x\right\}} =$

A. 1

B. 0

C. $\pi/2$

D. non existent

Answer: A



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19.
$$\lim_{x \rightarrow 0} \frac{3 \tan 3x - 4 \tan 2x - \tan x}{4x^2 \tan x}$$

A. a) 0

B. b) 1

C. c) 3

D. d) 4

Answer: D



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20. $\lim_{x \rightarrow 0} \left[\frac{\sin^{-1} x}{\tan^{-1} x} \right] =$ (where $[.]$ denotes the greatest integer function)

A. 0

B. 1

C. -1

D. none of these

Answer: B



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21. The value of $\lim_{x \rightarrow \frac{\pi}{4}} \frac{\sqrt{1 - \sqrt{\sin 2x}}}{\pi - 4x}$ is

A. $\frac{1}{4}$

B. $-\frac{1}{4}$

C. 1

D. does not exist

Answer: D



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22. The value of $\lim_{x \rightarrow \infty} \left(e^{\sqrt{x^4+1}} - e^{(x^2+1)} \right)$ is

A. 0

B. e

C. 1/e

D. $-\infty$

Answer: D



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23. The value of $\lim_{x \rightarrow \pi/4} \frac{\tan^3 x - \tan x}{\cos\left(x + \frac{\pi}{4}\right)}$ is

A. 8

B. 4

C. -8

D. -2

Answer: C



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24. $\lim_{x \rightarrow \frac{\pi}{2}} \frac{(1 - \sin x)(8x^3 - \pi^3)(\cos x)}{(\pi - 2x)^4}$

A. $-\frac{\pi^2}{16}$

B. $\frac{3\pi^2}{16}$

C. $\frac{\pi^2}{16}$

D. $-\frac{3\pi^2}{16}$

Answer: D



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$$25. \lim_{x \rightarrow \infty} \frac{\sum_{r=1}^{10} (x+r)^{2010}}{(x^{1006} + 1)(2x^{1004} + 1)} =$$

A. 5

B. 2010

C. $\frac{502}{1005}$

D. 0

Answer: A



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$$26. \text{ If } \lim_{x \rightarrow 0} \frac{f(x)}{x^2} = a \text{ and } \lim_{x \rightarrow 0} \frac{f(1 - \cos x)}{g(x)\sin^2 x} = b \text{ (where } b \neq 0),$$

then $\lim_{x \rightarrow 0} \frac{g(1 - \cos 2x)}{x^4}$ is

A. $\frac{4a}{b}$

B. $\frac{a}{4b}$

C. $\frac{a}{b}$

D. none of these

Answer: C

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27.

If

$$f(x) = \begin{cases} \frac{x}{\sin x}, & x > 0 \\ 2 - x, & x \leq 0 \end{cases} \text{ and } g(x) = \begin{cases} x + 3, & x < 1 \\ x^2 - 2x - 2, & 1 \leq x < 2 \\ x - 5, & x \geq 2 \end{cases}$$

Then the value of $\lim_{x \rightarrow 0} g(f(x))$

A. is -2

B. is -3

C. is 1

D. does not exist

Answer: B



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28. If $k \in I$ such that $\lim_{x \rightarrow \infty} \left(\cos \frac{k\pi}{4} \right)^{2n} - \left(\cos - \frac{k\pi}{6} \right)^{2n} = 0$,

then k must not be divisible by 24 k is divisible by 24 of k is divisible
neither by 4 nor by 6 k must be divisible by 12 but not necessarily by 24
none of these

A. k must not be divisible by 24

B. k is divisible by 24 or k is divisible neither by 4 nor by 6

C. k must be divisible by 12 but not necessarily by 24

D. none of these

Answer: B



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29. If a_n and b_n are positive integers and $a_n + \sqrt{2}b_n = (2 + \sqrt{2})^n$, then

$$\lim_{n \rightarrow \infty} \left(\frac{a_n}{b_n} \right) =$$

A. $\sqrt{2}$

B. 2

C. $e^{\sqrt{2}}$

D. e^2

Answer: A



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30. The value of $\left(\lim_{x \rightarrow 0} \frac{\tan x^{\frac{1}{5}}}{(\tan^{-1} \sqrt{x})^2} \frac{\log(1 + 5x)}{e^{3\sqrt[5]{x}} - 1} \right)$ is

A. $\frac{3}{5}$

B. $\frac{5}{3}$

C. 1

D. none of these

Answer: B



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31. The value of $\lim_{x \rightarrow 3} \frac{(x^3 + 27) \log_e (x - 2)}{x^2 - 9}$ is

A. 9

B. 18

C. 27

D. $5/3$

Answer: A



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32. The value of $\lim_{x \rightarrow 0^+} \left(\frac{1 - \cos(\sin^2 x)}{x^2} \right)^{\frac{\log_e(1-2x^2)}{\sin^2 x}}$ is

A. 0

B. e

C. -1

D. ∞

Answer: D



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33. $\lim_{x \rightarrow 0} \frac{1}{x^2} \left| \frac{1 - \cos 3x}{\sin^{-1}(x^x -)} \frac{\log_e(1 + 4x)}{\tan^{-1}(2x)} \right|$ is equal to

A. 2

B. -4

C. 6

D. 4

Answer: B



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34. If graph of the function $y = f(x)$ is continuous and passes through

point $(3, 1)$ then $\lim_{x \rightarrow 3} \frac{\log_e(3f(x) - 2)}{2(1 - f(x))}$ is equal

A. $\frac{3}{2}$

B. $\frac{1}{2}$

C. $-\frac{3}{2}$

D. $-\frac{1}{2}$

Answer: C



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35. Let $f(x)$ be defined for all $x \in R$ such that

$\lim_{x \rightarrow 0} \left[f(x) + \log \left(1 - \frac{1}{e^{f(x)}} \right) - \log(f(x)) \right] = 0$. Then $f(0)$ is

A. 0

B. 1

C. 2

D. 3

Answer: A

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36. $\lim_{x \rightarrow \infty} x^2 \sin \left(\log_e \sqrt{\frac{\cos(\pi)}{x}} \right)$

A. 0

B. $-\frac{\pi^2}{2}$

C. $-\frac{\pi^2}{4}$

D. $-\frac{\pi^2}{8}$

Answer: C

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37. If $\lim_{x \rightarrow \infty} \left(\frac{x+c}{x-c} \right)^x = 4$ then the value of e^c is

A. $1/4$

B. $1/2$

C. 1

D. 2

Answer: D



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38. If $(\lim)_{x \rightarrow 0} \left[1 + x + \frac{f(x)}{x} \right]^{\frac{1}{x}} = e^3$, then find the value of $\ln \left((\lim)_{x \rightarrow 0} \left[1 + \frac{f(x)}{x} \right]^{\frac{1}{x}} \right)$ is --

A. e

B. e^2

C. e^3

D. none of these

Answer: B



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39. $\lim_{x \rightarrow \frac{\pi^-}{2}} [1 + (\cos x)^{\cos x}]^2 =$

A. Does not exist

B. 1

C. e

D. 4

Answer: D



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40. If $a > 0, b > 0$ then $\lim_{n \rightarrow \infty} \left(\frac{a - 1 + b^{\frac{1}{n}}}{a} \right)^n =$

A. $b^{\frac{1}{a}}$

B. $a^{\frac{1}{b}}$

C. a^b

D. b^a

Answer: A



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41. If $f(x) = \lim_{n \rightarrow \infty} \left(\frac{\cos(x)}{\sqrt{n}} \right)^n$, then the value of $\lim_{x \rightarrow 0} \frac{f(x) - 1}{x}$ is

A. 0

B. 1

C. 2

D. $3/2$

Answer: A



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42. $\lim_{x \rightarrow 0} \frac{\log(x^{x^2} + 2\sqrt{x})}{\tan \sqrt{x}}$ is equal to

A. 0

B. 1

C. e^2

D. 2

Answer: D



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43. Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be such that $f(a) = 1, f(a) = 2$. Then

$$\lim_{x \rightarrow 0} \left(\frac{f^2(a+x)}{f(a)} \right)^{1/x} \text{ is}$$

A. e^2

B. e^4

C. e^{-4}

D. $1/e$

Answer: B



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44. The value of $\lim_{n \rightarrow \infty} \left(\frac{n^2 - n + 1}{n^2 - n - 1} \right)^{n(n-1)}$ is

A. e

B. $1/e$

C. e^2

D. e^{-2}

Answer: B



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45. If $f(n) = (\lim)_{x \rightarrow 0} \left\{ \left(1 + s \in \frac{x}{2} \right) \left(1 + s \in \frac{x}{x^2} \right) \left(1 + s \in \frac{x}{x^n} \right) \right\}^{1/x}$

then find $(\lim)_{n \rightarrow \infty} f(n)$.

A. 1

B. e

C. 0

D. ∞

Answer: B



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46. $\lim_{n \rightarrow \infty} (1 - x + x \cdot \sqrt[n]{e})^n$ is equal to

A. e^x

B. e^{-x}

C. e^{2x}

D. none of these

Answer: A



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47. $\lim_{x \rightarrow 1} \frac{\sqrt[13]{x} - \sqrt[7]{x}}{\sqrt[5]{x} - \sqrt[3]{x}}$ is

A. $\frac{44}{91}$

B. $\frac{45}{89}$

C. $\frac{45}{89}$

D. $\frac{40}{93}$

Answer: B



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48. $\lim_{x \rightarrow 1} \frac{\sqrt[13]{x} - \sqrt[7]{x}}{\sqrt[5]{x} - \sqrt[3]{x}}$ is

- A. 1
- B. -1
- C. 0
- D. -1/2

Answer: D

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49. The value of $\lim_{x \rightarrow 0} \frac{1 - \cos 2x}{e^{x^2} - e^x + x}$ is

- A. 0
- B. 2
- C. 4
- D. 8

Answer: C



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50. If $f(a) = \frac{1}{4}$, then $\lim_{h \rightarrow 0} \frac{f(a + 2h^2) - f(a - 2h^2)}{f(a + h^3 - h^2) - f(a - h^3 + h^2)} =$

A. 0

B. 1

C. -2

D. none of these

Answer: C



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51. $\left(\lim_{x \rightarrow 0^+} \frac{1}{x\sqrt{x}} \left(a \tan^{-1} \frac{\sqrt{x}}{a} - b \frac{\tan^{-1}(\sqrt{x})}{b} \right) \right)$ has the value equal to $\frac{a-b}{3}$ b. 0 c. $\frac{(a^2 - b^2)}{6a^2b^2}$ d. $\frac{a^2 - b^2}{3a^2b^2}$

A. $\frac{a - b}{3}$

B. 0

C. $\frac{(a^2 - b^2)}{6a^2b^2}$

D. $\frac{a^2 - b^2}{3a^2b^2}$

Answer: D



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52. The value of $\lim_{x \rightarrow 0} \left(\frac{1 + 2x}{1 + 3x} \right)^{\frac{1}{x^2}} \cdot e^{\frac{1}{e^x}}$ is

A. $e^{\left(\frac{5}{2}\right)}$

B. e^2

C. e^{-2}

D. 1

Answer: A



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53. If $F: R \rightarrow R$ be a differentiable function at $x = 0$ satisfying $f(0) = 0$ and $f'(0) = 1$, then the value of

$$\lim_{x \rightarrow 0} \frac{1}{x} \sum_{n=1}^{\infty} (-1)^n f\left(\frac{x}{n}\right) =$$

- A. 0
- B. $-\log 2$
- C. 1
- D. e

Answer: B



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54. The value of $\lim_{x \rightarrow \frac{3\pi}{4}} \frac{1 + \sqrt[3]{\tan x}}{1 - 2 \cos^2 x}$ is

- A. $-1/2$

B. $-2/3$

C. $-3/2$

D. $-1/3$

Answer: D

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55. Let $g(x) = \frac{(x-1)^n}{\log \cos^m(x-1)}$, $0 < x < 2$ m and n integers, $m \neq 0$, $n > 0$ and. If $\lim_{x \rightarrow 1^+} g(x) = -1$, then

A. $n = 1, m = 1$

B. $n = 1, m = -1$

C. $n = 2, m = 2$

D. $n > 2, m = n$

Answer: C

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56. Number of integral values of λ for which

$\lim_{x \rightarrow 1} \sec^{-1} \left(\frac{\lambda^2}{\log_e x} - \frac{\lambda^2}{x-1} \right)$ does not exist is

A. 1

B. 2

C. 3

D. 4

Answer: C



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57. If $\lim_{x \rightarrow 0} \frac{e^{ax} - e^x - x}{x^2} = b$ (finite), then

A. $a = 2, b = 0$

B. $a = 0, b = \frac{3}{2}$

C. $a = 2, b = \frac{3}{2}$

D. $a = 0, b = 2$

Answer: C



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58. If $\lim_{x \rightarrow 0} \frac{x^3}{\sqrt{a + x}(bx - \sin x)} = 1, a > 0$, then $a + b$ is equal to

A. 36

B. 37

C. 38

D. 40

Answer: B



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59. If $\lim_{x \rightarrow \infty} x \log_e \left(\begin{vmatrix} \alpha/x & 1 & \gamma \\ 0 & 1/x & \beta \\ 1 & 0 & 1/x \end{vmatrix} \right) = -5$. where α, β, γ are

finite real numbers, then

A. $\alpha = 2, \beta = 1, \gamma \in R$

B. $\alpha = 2, \beta = 2, \gamma = 5$

C. $\alpha \in R, \beta = 1, \gamma \in R$

D. $\alpha \in R, \beta = 1, \gamma = 5$

Answer: D

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Multiple Correct Answers Type

1. If $A = \lim_{x \rightarrow 0} \frac{\sin^{-1}(\sin x)}{\cos^{-1}(\cos x)}$ and $B = \lim_{x \rightarrow 0} \frac{[|x|]}{x}$, then

A. $A = 1$

B. A does not exist

C. B = 0

D. B = 1

Answer: B::C



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2. If $f(x) = x \left(\frac{e^{|x| + [x]} - 2}{|x| + [x]} \right)$ then (where $[.]$ represent the greatest integer function)

A. $\lim_{x \rightarrow 0^+} f(x) = -1$

B. $\lim_{x \rightarrow 0^-} f(x) = 0$

C. $\lim_{x \rightarrow 0} f(0) = -1$

D. $\lim_{x \rightarrow 0} f(x) = 0$

Answer: A::B



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3. Assume that $(\lim)_{\theta \rightarrow 1} f(\theta)$ exists and $\frac{\theta^2 + \theta - 2}{\theta + 3} \leq \frac{f(\theta)}{\theta^2} \leq \frac{\theta^2 + 2\theta - 1}{\theta + 3}$ holds for certain interval containing the point $\theta = -1$ then $(\lim)_{\theta \rightarrow 1} f(\theta)$ is equal to $f(-1)$ b. is equal to 1 c. is non-existent d. is equal to -1

A. is equal to $f(-1)$

B. is equal to 1

C. is non-existent

D. is equal to -1

Answer: A::D



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4. Let $f(x) = \lim_{n \rightarrow \infty} \frac{\tan^{-1}(\tan x)}{1 + (\log_x x)^n}$, $x \neq (2n + 1)\frac{\pi}{2}$ then

A. $\forall 1 < x < \frac{\pi}{2}$, $f(x)$ is an identity function

- B. $\forall \frac{\pi}{2} < x < \pi$, the graph of $f(x)$ is a straight line having y intercept of $-\pi$
- C. $\forall \frac{\pi}{2} < x < e$, the graph of $f(x)$ is a straight line having y intercept of $-\pi$
- D. $\forall x > e$, $f(x)$ is a constant function

Answer: A::C::D

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ComprehensionType

1. Let $f(x)$ be the fourth degree polynomial such that $f'(0) = -6$, $f(0) = 2$ and $\lim_{x \rightarrow 1} \frac{f(x)}{(x-1)^2} = 1$

The value of $f(2)$ is

- A. 1
- B. 0

C. 2

D. 3

Answer: C



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2. Let $f(x)$ be the fourth degree polynomial such that $f'(0) = 6$, $f(0) = 2$ and $\lim_{x \rightarrow 1} \frac{f(x)}{(x-1)^2} = 1$. The value of $f(2)$ is 3 b.

1 c. 0 d. 2

A. 4

B. 5

C. 6

D. 7

Answer: C



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Multiple Correct Answer Type

1. If $\lim_{x \rightarrow \infty} x \log_e \left(\begin{vmatrix} \alpha/x & 1 & \gamma \\ 0 & 1/x & \beta \\ 1 & 0 & 1/x \end{vmatrix} \right) = -5$. then where α, β, γ are

finite real numbers, then a) $\alpha = 2, \beta = 1, \gamma \in \mathbb{R}$ b) $\alpha = 2, \beta = 2, \gamma = 5$

c) $\alpha \in \mathbb{R}, \beta = 1, \gamma \in \mathbb{R}$ d) $\alpha \in \mathbb{R}, \beta = 1, \gamma = 5$

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2. If $a \in I$, then value of a for which $\lim_{x \rightarrow a} \frac{\tan([x^3] - [x]^3)}{(x - a)^3}$ exists

finitely, is /are

A. 0

B. 1

C. -1

D. 2

Answer: A::B



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Comprehension Type

$$1. L = \lim_{x \rightarrow 0} \frac{\sin(\sin x) - \sin x}{ax^5 + bx^3 + c} = -\frac{1}{12}$$

The value/values of a is

A. $\in \mathbb{R}$

B. 2

C. 0

D. 1

Answer: A



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$$2. L = \lim_{x \rightarrow 0} \frac{\sin(\sin x) - \sin x}{ax^5 + bx^3 + c} = -\frac{1}{12}$$

The value/values of b is

A. $\in \mathbb{R}$

B. 2

C. 0

D. 1

Answer: B



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3.

If

$$f(x) = \left(\lim_{x \rightarrow \infty} \frac{(x^2 + ax + 1) + x^{2n}(2x^2 + x + b)}{1 + x^{2n}} \right) \text{ and } \left(\lim_{x \rightarrow \pm 1} f(x) \right)$$

exist, then The value of b is -1 b. 1 c. 0 d. 2

A. -1

B. 1

C. 0

D. 2

Answer: B



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4.

If

$$f(x) = \left(\lim_{x \rightarrow \infty} \frac{(x^2 + ax + 1) + x^{2n}(2x^2 + x + b)}{1 + x^{2n}} \right) \text{ and } \left(\lim_{x \rightarrow 1} f(x) \right)$$

exist, then The value of b is -1 b. 1 c. 0 d.2

A. -1

B. 1

C. 0

D. 2

Answer: C



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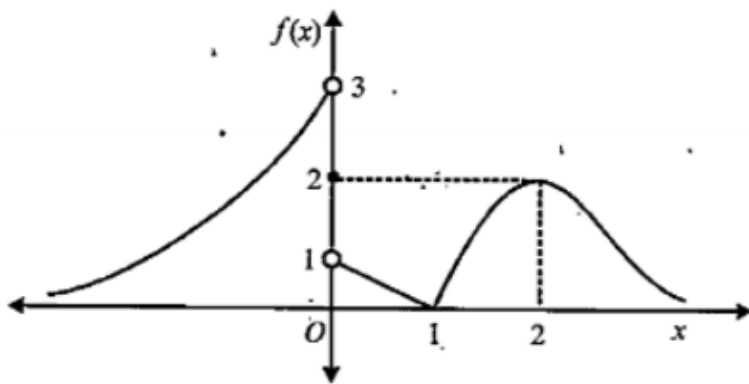
Question Bank

1. If $\lim_{x \rightarrow 0} \frac{1 - \cos x}{e^{ax} - bx - 1}$ exist and is equal to 1, then $(a^2 + b^2)$ equals

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2. If graph of a function $f(x)$ is shown in the adjacent figure, then

$\lim_{x \rightarrow 0^-} \left[\frac{4f(x) - 6[f(x)]}{\tan(2f(x) - 6)} \right]$ is equal to



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3. Let $f(x) = (\sec x)^{\cos ecx} + (\cot x)^{\sin x}$. Then the value of $\lim_{x \rightarrow 0^+} f(x)$ is equal to

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4.

$$\lim_{z \rightarrow 0} \left\{ \left\{ \max \left((\sin^{-1} x + \cos^{-1} x)^2, \min (x^2 + 4x + 7) \right) \right\} \cdot \frac{\sin^{-1} z}{z} \right\}$$

is equal to (where $[\cdot]$ denotes greatest integer function)

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5. The reciprocal of the value of:

$$(\lim)_{n \rightarrow \infty} \left(1 - \frac{1}{2^2} \right) \left(1 - \frac{1}{3^2} \right) \left(1 - \frac{1}{4^2} \right) \left(1 - \frac{1}{n^2} \right) \text{ is}$$

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6. The value of $\lim_{x \rightarrow 0} \frac{\sum_{k=1}^{2016} \left\{ \frac{\sin x}{x} + 2015k \right\}}{2016}$ is [where $\{x\}$ represents fractional part of x]

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7. $\lim_{x \rightarrow \infty} \frac{30 + 4\sqrt{x} + 7\sqrt[3]{x}}{2 + \sqrt{4x - 7} + \sqrt[3]{6x - 2}}$ equals

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8. If $\lim_{x \rightarrow 0} \left(\frac{a \sin x + b \tan x}{x^3} \right) = \frac{3}{2}$ then $|a+2b|$ is equal to

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9. $\lim_{n \rightarrow 0} \left(\frac{1}{1+n^2} + \frac{2}{1+n^2} + \frac{3}{1+n^2} + \dots + \frac{n}{1+n^2} \right)$ is equal to

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10. Find the value of $\lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{k^2 + k - 1}{(k + 1)!}$.

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11. The value of $\lim_{x \rightarrow 0} \left((\tan x)^{\frac{1}{x}} + (1 + \sin x)^x \right)$ where $x > 0$ is equal to

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12. If $\lim_{x \rightarrow 0} (a \sin x + b e^{(x)} + 3x^2) / (\sin x - 2x + \tan x)$ exists and has value equal to L , then the value of $(a+L)/b$ is equal to

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13. If $\lim_{x \rightarrow a} \frac{\sqrt{x-b} - \sqrt{a-b}}{x^2 - a^2} (a > b) = \frac{1}{64}$ and

$\lim_{x \rightarrow \infty} \left(\sqrt{x^2 + ax} - \sqrt{x^2 + bx} \right) = 2$ then the value of a/b , is`

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14. If $\lim_{x \rightarrow 0} \frac{k + \cos lx}{x^2}$ exists and has the value equal to -4 then find l^2

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15. $\lim_{x \rightarrow 0} \frac{(3 \sin x - \sin 3x)^4}{(\sec x - \cos x)^6}$ is equal to

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16. $\lim_{x \rightarrow 0} \frac{\tan x \sqrt{\tan x} - \sin x \sqrt{\sin x}}{x^3 \cdot \sqrt{x}}$ equals

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17. $f(x) = \frac{\ln(x^2 + e^x)}{\ln(x^4 + e^{2x})}$. Then $\lim_{x \rightarrow \infty} f(x)$ is equal to

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