



## MATHS

### BOOKS - CENGAGE

#### LOGARITHM AND ITS PROPERTIES

##### Examples

1. Solve for  $x$ :  $4^x - 3^{x - \frac{1}{2}} = 3^{x + \frac{1}{2}} - 2^{2x - 1}$

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2. Solve  $e^{\sin x} - e^{-\sin x} - 4 = 0$ .

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3. Solve:  $|x - 3|^3 x^{2-10x+3} = 1$

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4. Solve  $(1/2)^{x^2-2x} < 1/2$ .

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5. Find the smallest integral value of  $x$  satisfying  $(x - 2)^x \wedge (2 - 6x + 8) > 1$

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6. Find the number of solutions of equation  $(2x - 3)2^x = 1$

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7. Find the value of  $(\log)_{2\sqrt{3}}1728$ .

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8. Prove that  $\frac{2}{5} < \log_{10} 3 < \frac{1}{2}$ .

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9. Arrange  $(\log)_2 5$ ,  $(\log)_{0.5} 5$ ,  $(\log)_7 5$ ,  $(\log)_3 5$  in decreasing order.

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10. Prove that number  $(\log)_2 7$  is an irrational number.

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11. Which of the following numbers are positive/negative : (i)  $\log_{\sqrt{3}} \sqrt{2}$   
(ii)  $\log_3(4)$

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12. Find the value of  $\log \tan 1^\circ \log \tan 2^\circ \dots \log \tan 89^\circ$ .

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13. If  $\log_a 3 = 2$  and  $\log_b 8 = 3$ , then prove that  $\log_a b = \log_3 4$ .

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14. If  $\log_3 y = x$  and  $\log_2 z = x$ , find  $72^x$  in terms of  $y$  and  $z$ .

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15. If

$$\frac{x(y+z-x)}{\log x} = \frac{y(z+x-y)}{\log y} = \frac{z(x+y-z)}{\log z}, \text{ provethat } x^y y^x = z^x y^z = x^z$$

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16. Suppose  $x, y, z \neq 0$  and are not equal to 1 and

$\log x + \log y + \log z = 0$ . Find the value of

$$\frac{1}{x^{\log y}} + \frac{1}{(\log z) y^{\log z}} + \frac{1}{(\log x) z^{\log x}} + \frac{1}{(\log y)}$$

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17. Solve :  $2(25)^x - 5(10^x) + 2(r^x) \geq 0$ .

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18. Find the number of solution to equation  $(\log)_2(x+5) = 6-x$  :

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19. Find the number of solutions of the following equations: 1.

$$x^{-\frac{1}{2}}(\log)_{0.5}x = 1, 2. x^2 - 4x + 3 - (\log)_{-2}x = 0$$

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20. Find the value of the following:

(i)  $\log_{10} 2 + \log_{10} 5$

(ii)  $\log_3(\sqrt{11} - \sqrt{2}) + \log_3(\sqrt{11} + \sqrt{2})$

(iii)  $\log_7 35 - \log_7 5$

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21. Find the value of  $\log_2(2\sqrt[3]{9} - 2) + \log_2(12\sqrt[3]{3} + 4 + 4\sqrt[3]{9})$ .

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22. What is logarithm of  $32^5\sqrt{4}$  to the base  $2\sqrt{2}$ ?



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23. If  $(\log)_e \left( \frac{a+b}{2} \right) = \frac{1}{2} ((\log)_e a + (\log)_e b)$ , then find the relation between  $a$  and  $b$ .



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24. Which of the following pairs of expression are defined for the same set of values of  $x$ ?  $f_1(x) = 2(\log)_2 x$  and  $f_2(x) = (\log)_{10} x^2$

$$f_1(x) = (\log)_x^2 \text{ and } f_2(x) = 2$$

$$f_1(x) = (\log)_{10}(x-2) + (\log)_{10}(x-3) \text{ and } f_2(x) = (\log)_{10}(x-2)(x-3)$$



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25. Find the value of  $7 \log \left( \frac{16}{15} \right) + 5 \log \left( \frac{25}{24} \right) + 3 \log \left( \frac{81}{80} \right)$ .



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26. If sum  $\log_2 x + \log_4 x + \log_{16} x + \log_{256} x + \dots = 6$ , then find the value of  $x$ .



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27. Suppose that  $a$  and  $b$  are positive real numbers such that  $\log_{27} a + \log_9(b) = \frac{7}{2}$  and  $\log_{27} b + \log_9 a = \frac{2}{3}$ . Then the value of the  $ab$  equals



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28. Solve for  $x$ :  $11^{4x-5} \cdot 3^{2x} = 5^{3-x} \cdot 7^{-x}$ .



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29. Which is greater:  $x = (\log)_3 5$  or  $y = (\log)_{17} 25$ ?

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30. If  $n > 1$ , then prove that

$$\frac{1}{(\log)_2 n} + \frac{1}{(\log)_3 n} + \frac{1}{(\log)_{53} n} = \frac{1}{(\log)_{53!} n}.$$

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31. Let  $a = \log_3 20$ ,  $b = \log_4 15$  and  $c = \log_5 12$ . Then find the value of

$$\frac{1}{a+1} + \frac{1}{b+1} + \frac{1}{c+1}.$$

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32. If  $\log_a(ab) = x$  then  $\log_b(ab)$  is equals to

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33. If  $(\log)_{12}27 = a$ , then find  $(\log)_6 16$  *ermsofa*

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34. If  $a^x = b$ ,  $b^y = c$ ,  $c^z = a$ , then find the value of  $xyz$ .

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35. Find the value of

$$((\log)_3 4) ((\log)_4 5) ((\log)_5 6) ((\log)_6 7) ((\log)_7 8) ((\log)_8 9).$$

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36. Simplify:  $\frac{1}{1 + (\log)_a bc} + \frac{1}{1 + (\log)_b ca} + \frac{1}{1 + (\log)_c ab}$

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37.

If

$$x = (\log)_{2a} a, y = (\log)_{3a} 2a, z = (\log)_{4a} 3a, \text{ prove that } 1 + xyz = 2yz.$$

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38. If  $(\log)_b a (\log)_c a + (\log)_a b (\log)_c b + (\log)_a c (\log)_c a = 3$  (where  $a, b, c$  are different positive real numbers  $\neq 1$ ), then find the value of  $ab \cdot$

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39. If  $y = 2^{\frac{1}{\log_x 4}}$  then prove that  $x = y^2$ .

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40. Find the value of  $81^{(1 / (\log)_5 3)} + 27^{\log 36} + 3^{\left(\frac{4}{(\log)_7 9}\right)}$

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41. Prove that  $\frac{2^{(\log)_2 \frac{1}{4}x} - 3^{\log} - (27)(x^2 + 1)^3 - 2x}{7^{4(\log)_{49}x} - x - 1} > 0$

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42. If  $60^a = 3$  and  $60^b = 5$  then  $12^{\frac{1-a-b}{2(1-b)}}$  is equal to

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43. Solve  $(\log)_4 8 + (\log)_{4(x+3)} - (\log)_4(x-1) = 2$ .

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44. Solve  $\log(-x) = 2\log(x+1)$ .

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45. Solve  $(\log)_2(3x-2) = (\log)_{\frac{1}{2}}x$



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46. Solve  $2^{x+2}27^{x/(x-1)} = 9$



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47. Solve:  $(\log)_2(4x3^x - 6) - (\log)_2(9^x - 6) = 1.$



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48. Solve :  $6((\log)_x 2 - (\log)_4 x) + 7 = 0.$



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49. Solve:  $4^{(\log)_2 \log x} = \log x - (\log x)^2 + 1$  (*baseise*).



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50. Solve:  $4(\log)_{\frac{x}{2}}(\sqrt{x}) + 2(\log)_{4x}(x^2) = 3(\log)_{2x}(x^3)$ .

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51. Solve  $4^{(\log)_9 x} - 6^{(\log)_9 2} + 2^{(\log)_3 27} = 0$

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52. Solve:  $\frac{1}{4}x^{\log_2 \sqrt{x}} = \left(2 \cdot x^{(\log)_2 x}\right)^{\frac{1}{4}}$

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53. Solve:  $|x - 1|^{(\log)_{10} x} \wedge 2 - (\log)_{10} x^2 = |x - 1|^3$

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54. Solve  $(\log)_2(x - 1) > 4$ .



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55. Solve  $\log_3(x - 2) \leq 2$ .



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56. Solve :  $(\log)_{0.3}(x^2 - x + 1) > 0$



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57. Solve  $1 < (\log)_2(x - 2) \leq 2$ .



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58. Solve  $\log_2|x - 1| < 1$ .



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59. Solve  $(\log)_{0.2}|x - 3| \geq 0$ .

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60. Solve :  $(\log)_2 \frac{x - 1}{x - 2} > 0$

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61. Solve:  $(\log)_{0.5} \frac{3 - x}{x + 2} < 0$

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62. Solve:  $(\log)_3(2x^2 + 6x - 5) > 1$

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63. Solve  $(\log)_{0.04}(x - 1) \geq (\log)_{0.2}(x - 1)$





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64. Solve :  $(\log)_{(x+3)}(x^2 - x) < 1$



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65. Solve  $2 \log_3 x - 4 \log_x 27 \leq 5$ .



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66. Solve:  $(\log)_{x + \frac{1}{x}} \left( \frac{\log_2(x - 1)}{x + 2} \right) > 0$



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67. Solve:  $(\log)_{(\log)_2 \left( \frac{x}{2} \right)} (x^2 - 10x + 22) > 0$



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68. Solve:  $(\log)_{0.1} \left( (\log)_2 \left( \frac{x^2 + 1}{x - 1} \right) \right) < 0$

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69. Solve:  $\frac{x - 1}{(\log)_3(9 - 3^x)} \leq 1.$

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70. Solve:  $\left( \left( \frac{1}{2} \right)^{\log(10) a^2} + 2 > \frac{3}{2^{(\log)_{10}(-a)}} \right)$

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71. Write the characteristic of each of the following numbers by using their standard forms: (i) 1235.5      (ii) 346.41      (iii) 62.723      (iv) 7.12345 (v) 0.35792      (vi) 0.034239      (vii) 0.002385      (viii) 0.0009468

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72. Write the significant digits in each of the following numbers to compute the mantissa of their logarithms: 3.239 (ii) 8 (iii) 0.9 (iv) 0.02 0.0367 (vi) 89 (vii) 0.0003 (viii) 0.00075

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73. Find the mantissa of the logarithm of the number 5395

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74. Find the mantissa of the logarithm of the number 0.002359

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75. Use the logarithm tables to find the logarithm of the following numbers 25975 (ii) 25.795

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76. Find the antilogarithm of each of the following: 2.7523 (ii) 3.7523 (iii) 5.7523 (iv) 0.7523 1.7523 (vi) 2.7523 (vii) 3.7523

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77. Evaluate  $(72.3)^{\frac{1}{3}}$  if  $\log 0.723 = -1.8591$ .

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78. Using logarithms, find the value of  $6.45 \times 981.4$

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79. Let  $x = (0.15)^{20}$ . Find the characteristic and mantissa of the logarithm of  $x$  to the base 10. Assume  $(\log)_{10} 2 = 0.301$  and  $(\log)_{10} 3 = 0.477$ .

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**80.** If  $(\log)_{10}2 = 0.30103$ ,  $(\log)_{10}3 = 0.47712$ , then find the number of digits in  $3^{12} \times 2^8$ .



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**81.** In the 2001 census, the population of India was found to be  $8.7 \times 10^7$ . If the population increases at the rate of 2.5% every year, what would be the population in 2011?



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**82.** Find the compound interest on Rs. 12000 for 10 years at the rate of 12% per annum compounded annually.



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83. If  $P$  is the number of natural numbers whose logarithms to the base 10 have the characteristic  $p$  and  $Q$  is the number of natural numbers whose reciprocals to the base 10 have the characteristic  $-q$ , then find the value of  $\log_{10} P - (\log)_{10} Q$ .

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84. Let  $L$  denote  $\text{antilog}_{32} 0.6$  and  $M$  denote the number of positive integers which have the characteristic 4, when the base of log is 5, and  $N$  denote the value of  $49^{(1 - (\log)_7 2)} + 5^{-(\log)_5 4}$ . Find the value of  $\frac{LM}{N}$ .

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85. Find the number of solutions of equation  $2^x + 3^x + 4^x - 5^x = 0$

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86. Let  $a, b, c, d$  be positive integers such that  $(\log)_a b = \frac{3}{2}$  and  $(\log)_c d = \frac{5}{4}$ . If  $(a - c) = 9$ , then find the value of  $(b - d)$ .

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87. If  $a \geq b > 1$ , then find the largest possible value of the expression  $(\log)_a \left( \frac{a}{b} \right) + (\log)_b \left( \frac{b}{a} \right)$ .

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88. If  $y = a^{\frac{1}{1 - (\log)_a x}}$  and  $z = a^{\frac{1}{1 - (\log)_a y}}$ , then prove that  $x = a^{\frac{1}{1 - (\log)_a z}}$ .

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89. Solve  $\sqrt{\log(-x)} = \log \sqrt{x^2}$  (base is 10).

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90. Solve  $3^{(\log_9 x)^2 - \frac{9}{2}\log_9 x + 5} = 3\sqrt{3}$ .

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91. Solve for:  $x : (2x)^{(\log)_b 2} = (3x)^{(\log)_b 3}$ .

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92. Solve the equations for  $x$  and  $y$ :  $(3x)^{\log 3} = (4y)^{\log 4}$ ,  $4^{\log x} = 3^{\log y}$ .

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93. Solve  $(\log)_{2x} 2 + (\log)_4 2x = -3/2$ .

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94.

Solve:

$$(\log)_{(2x+3)}(6x^2 + 23 + 21) + (\log)_{(3x+7)}(4x^2 + 12x + 9) = 4$$

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### Exercise 1 1

1. For  $x \leq 2$ , solve  $x^3 3^{|x-2|} + 3^{x+1} = x^3 \cdot 3^{x-2} + 3^{|x-2|+3}$

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2. Solve  $\left(\frac{1}{2}\right)^{x^6 - 2x^4} < 2^{(x)^2}$ .

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3. Solve for  $x$  and  $y$ :  $y^x = x^y$ ,  $x = 2y$ . Find the value of  $x + y$

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4. Solve  $2^{x+2} - 2^{x+3} - 2^{x+4} > 5^{x+1} - 5^{x+2}$ .

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5. Solve  $\left(\frac{3}{4}\right)^{6x+10-x^2} < \frac{27}{64}$ .

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6. Find the number of solutions of  $|x| \cdot 3^{|x|} = 1$ .

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## Exercise 12

1. Find the value of  $3^{2\log_9 3}$ .

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2. Find the value of  $\sqrt{(\log_{0.5} 4)^2}$ .

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3. If  $\log_{\sqrt{8}} b = 3\frac{1}{3}$ , then find the value of  $b$ .

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4. Find the value of  $\log_5 \log_2 \log_3 \log_2 512$ .

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5. If  $\log_5 x = a$  and  $\log_2 y = a$ , find  $100^{2a-1}$  in terms of  $x$  and  $y$ .

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6. Find the value of  $\log_{1/3} \sqrt[4]{729} \cdot \sqrt[3]{9^{-1} \cdot 27^{-4/3}}$ .

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7. Solve for  $x$ :  $\log_4 \log_3 \log_2 x = 0$ .

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8. Prove that  $\log_{10} 2$  lies between  $\frac{1}{4}$  and  $\frac{1}{3}$ .

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9. Find number of roots of the equation  $x^3 - \log_{0.5} x = 0$ .

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1. Write each of the following as single logarithm:

(a)  $1 + \log_2 5$                       (b)  $2 - \log_3 7$

(c)  $2\log_{10} x + 3\log_{10} y - 5\log_{10} z$

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2. Prove that  $\frac{2}{3} < (\log)_{10} 3 < \frac{1}{2}$ .

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3. Prove that  $\log_7 \log_7 \sqrt{7\sqrt{(7\sqrt{7})}} = 1 - 3\log_7 2$ .

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4. If  $\log_{10} x = y$ , then find  $\log_{1000} x^2$  in terms of  $y$ .

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5. If  $\log_7 2 = m$ , then find  $\log_{49} 28$  in terms of  $m$ .



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6. Find the value of  $\log_2 \left( \frac{1}{7^{\log_7 0.125}} \right)$ .



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7. Find the value of  $\left( \frac{4}{\log_2(2\sqrt{3})} + \frac{2}{\log_3(2\sqrt{3})} \right)^2$ .



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8. If  $x$  and  $y$  are positive real numbers such that  $2\log(2y - 3x) = \log x + \log y$ , then find the value of  $\frac{x}{y}$ .



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9. If  $a^2 + b^2 = 7ab$ , show that  $\log\left(\frac{a+b}{3}\right) = \frac{1}{2}(\log a + \log b)$ .

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10. If  $\log_b n = 2$  and  $\log_n 2b = 2$ , then find the value of  $b$ .

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11. If  $\log_2 x \times \log_3 x = \log_2 x + \log_3 x$ , then find  $x$ .

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12. If  $y^2 = xz$  and  $a^x = b^y = c^z$ , then prove that  $(\log)_6 a = (\log)_c b$ .

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13. Prove the following identities:

$$(a) \frac{\log_a n}{\log_{ab} n} = 1 + \log_a b \qquad (b) \log_{ab} x = \frac{\log_a x \log_b x}{\log_a x + \log_b x}.$$

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14. Compute  $\log_{ab}(\sqrt[3]{a}/\sqrt{b})$  if  $\log_{ab} a = 4$ .

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15. If  $a^x = b^y = c^z = d^w$ , show that  $\log_a(bcd) = x\left(\frac{1}{y} + \frac{1}{z} + \frac{1}{w}\right)$ .

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16. Find the value of  $\left(\frac{1}{49}\right)^{1+(\log)_7 2} + 5^{-1(\log)\left(\frac{1}{5}\right)(7)}$

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## Exercise 1 4

1. Solve  $\log_2(25^{x+3} - 1) = 2 + \log_2(5^{x+3} + 1)$ .

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2. Solve  $\log_4(2 \times 4^{x-2} - 1) + 4 = 2x$ .

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3. Solve:  $27^{\log_3 \sqrt[3]{x^2 - 3x + 1}} = \frac{\log_2(x - 1)}{|\log_2(x - 1)|}$ .

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4. Solve  $\log_4(x - 1) = \log_2(x - 3)$ .

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5. Solve  $\log_6 9 - \log_9 27 + \log_8 x = \log_{64} x - \log_6 4$ .

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6. Solve  $\log_2(2\sqrt{17-2x}) = 1 - \log_{1/2}(x-1)$ .

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7. Solve :  $3\log_x(4) + 2\log_{4x} 4 + 3\log_{16x} 4 = 0$

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8. Solve  $(\log_3 x)(\log_5 9) - \log_x 25 + \log_3 2 = \log_3 54$ .

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9. Solve  $(x^{\log_{10} 3})^2 - (3^{\log_{10} x}) - 2 = 0$ .



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10. Solve  $x^{\log_4 x} = 2^3(\log_4 x + 3)$ .



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11. Find the sum of the squares of all the real solution of the equation

$$2\log_{(2+\sqrt{3})}(\sqrt{x^2+1}+x) + \log_{(2-\sqrt{3})}(\sqrt{x^2+1}-x) = 3$$



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12. Prove that the equation  $x^{\log_{\sqrt{x}} 2x} = 4$  has no solution.



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1. Solve  $\log_3|x| > 2$ .

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2. Solve  $\log_2 \cdot \frac{x - 4}{2x + 5} < 1$ .

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3. Solve  $\log_{10}(x^2 - 2x - 2) \leq 0$ .

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4. Let  $f(x) = \sqrt{\log_{10} x^2}$ . Find the set of all values of  $x$  for which  $f(x)$  is real.

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5. Solve  $2^{\log_2(x-1)} > x + 5$ .

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6. Solve  $\log_2|4 - 5x| > 2$ .

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7. Solve  $\log_{0.2} \frac{x+2}{x} \leq 1$ .

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8. Solve  $\log_{1/2}(x^2 - 6x + 12) \geq -2$ .

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9. Solve  $(0.5)^{\log_3 \log_{(1/5)} \left(x^2 - \frac{4}{5}\right)} > 1$ .



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10. Find the values of  $x$  which the function  $f(x) = \sqrt{\log_{1/2}\left(\frac{x-1}{x+5}\right)}$  is defined.



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11. Solve  $\log_{1-x}(x-2) \geq -1$ .



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12. Solve  $\log_3(x+2)(x+4) + \log_{1/3}(x+2) < \frac{1}{2}\log_{\sqrt{3}}7$ .



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13. Solve  $(\log)_x(x^2 - 1) \leq 0$ .



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## Exercise 1 6

1. If  $\log_{10} 2 = 0.3010$  and  $\log_{10} 3 = 0.477$ , then find the number of digits in the following numbers:

(a)  $3^{40}$       (b)  $2^{22} \times 5^{25}$  (c)  $24^{24}$

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2. If characteristic of three numbers  $a$ ,  $b$  and  $c$  are  $5$ ,  $-3$  and  $2$ , respectively, then find the maximum number of digits in  $N = abc$ .

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3. There are 3 numbers  $a$ ,  $b$  and  $c$  such that  $\log_{10} a = 5.71$ ,  $\log_{10} b = 6.23$  and  $\log_{10} c = 7.89$ . Find the number of digits before decimal in  $\frac{ab^2}{c}$ .



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4. Rupees 10,000 is invested at 6% interest compounded annually. How long will it take to accumulate Rs. 20,000 in the account?



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5. An initial number of bacteria presented in a culture is 10000. This number doubles every 30 minutes. How long will it take to bacteria to reach the number 100000 ?



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6. Charles Richter defined the magnitude of an earthquake to be  $M = \frac{\log_{10} I}{S}$ , where  $I$  is the intensity of the earthquake (measured by the amplitude of a seismograph reading taken 100 km from the epicentre of the earthquake) and  $S$  is the intensity of a "standard earthquake" (whose amplitude is 1 micron =  $10^{-1}$  cm).



Each number increase on the Richter scale indicates an intensity ten times stronger. For example, an earthquake of magnitude 5. An earthquake of magnitude 7 is 100 times stronger than an earthquake of magnitude 5. An earthquake of magnitude 8 is 1000 times stronger than an earthquake of magnitude 5.

The earthquake in city A registered 8.3 on the Richter scale. In the same year, another earthquake was recorded in city B that was four times stronger. What was the magnitude of the earthquake in city B ?



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## Exercise Single

1.  $\log_4 18$  is

- A. a rational number
- B. an irrational number
- C. a prime number

D. none of these

**Answer: B**



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2. The number of  $N - 6 = 6(\log)_{10}2 + (\log)_{10}31$  lies between two successive integers whose sum is equal to 5 (b) 7 (c) 9 (c) 10

A. 5

B. 7

C. 9

D. 10

**Answer: B**



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3. Given that  $\log(2) = 0.3010$ , the number of digits in the number  $2000^{2000}$  is 6601 (b) 6602 (c) 6603 (d) 6604

A. 6601

B. 6602

C. 6603

D. 6604

**Answer: C**



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4. If  $(21.4)^a = (0.00214)^b = 100$ , then the value of  $\frac{1}{a} - \frac{1}{b}$  is 0 (b) 1 (c) 2 (d) 4

A. 0

B. 1

C. 2

D. 4

**Answer: C**



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5. The value of  $\log ab - \log|b| = \log a$  (b)  $\log|a|$  (c)  $-\log a$  (d) none of these

A.  $\log a$

B.  $\log|a|$

C.  $-\log a$

D. none of these

**Answer: B**



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6. If  $a, b, c$  are consecutive positive integers and  $\log(\log(1 + ac)) = 2K$ , then the value of  $K$  is  $\log b$  (b)  $\log a$  (c) 2 (d) 1

A.  $\log b$

B.  $\log a$

C. 2

D. 1

**Answer: A**



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7. If  $\frac{a + (\log)_4 3}{a + (\log)_2 3} = \frac{a + (\log)_8 3}{a + (\log)_4 3} = b$ , then  $isequa < o \frac{1}{2}$  (2)  $\frac{2}{3}$  (c)  $\frac{1}{3}$  (d)  $\frac{3}{2}$

A.  $\frac{1}{2}$

B.  $\frac{2}{3}$

C.  $\frac{1}{3}$

D.  $\frac{3}{2}$

**Answer: C**



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8. If  $p > 1$  and  $q > 1$  are such that  $\log(p + q) = \log p + \log q$ , then the value of  $\log(p - 1) + \log(q - 1)$  is equal to 0 (b) 1 (c) 2 (d) none of these

A. 0

B. 1

C. 2

D. none of these

**Answer: A**



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9. The value of  $\frac{1 + 2(\log)_3 2}{(1 + (\log)_3 2)^2} + ((\log)_6 2)^2$  is 2 (b) 3 (c) 4 (d) 1

A. 2

B. 3

C. 4

D. 1

**Answer: D**



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10. If  $(\log)_4 5 = a$  and  $(\log)_5 6 = b$ , then  $(\log)_3 2$  is equal to  $\frac{1}{2a + 1}$  (b)  $\frac{1}{2b + 1}$  (c)  $2ab + 1$  (d)  $\frac{1}{2ab - 1}$

A.  $\frac{1}{2a + 1}$

B.  $\frac{1}{2b + 1}$

C.  $2ab + 1$

$$D. \frac{1}{2ab - 1}$$

**Answer: D**



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11. If  $(\log)_{10}2 = a$ ,  $(\log)_{10}3 = b$  then  $(\log)_{0.72}(9.6)$  in terms of  $a$  and  $b$  is equal to  $\frac{2a + 3b - 1}{5a + b - 2}$  (b)  $\frac{5a + b - 1}{3a + 2b - 2}$  (c)  $\frac{3a + b - 2}{2a + 3b - 1}$   $\frac{2a + 5b - 2}{3a + b - 1}$

A.  $\frac{2a + 3b - 1}{5a + b - 2}$

B.  $\frac{5a + b - 1}{3a + 2b - 2}$

C.  $\frac{3a + b - 2}{2a + 3b - 1}$

D.  $\frac{2a + 5b - 2}{3a + b - 1}$

**Answer: B**



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12. There exists a natural number  $N$  which is 50 times its own logarithm to the base 10, then  $N$  is divisible by 5 (b) 7 (c) 9 (d) 11

A. 5

B. 7

C. 9

D. 11

**Answer: A**



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13. The value of  $\frac{(\log)_2 24}{(\log)_{96} 2} - \frac{(\log)_2 192}{(\log)_{12} 2}$  is 3 (b) 0 (c) 2 (d) 1

A. 3

B. 0

C. 2

D. 1

**Answer: A**



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14.  $(\log)_{x-1} x (\log)_{x-2} (x-1) (\log)_{x-12} (x-11) = 2$ ,  $x$  is equal to: 9 (b)

16 (c) 25 (d) none of these

A. 9

B. 16

C. 25

D. none of these

**Answer: B**



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15. If  $f(x) = \log\left(\frac{1+x}{1-x}\right)$ , then  $f(x_1)f(x_2) = f(x_1 + x_2)$   
 $f(x+2) - 2f(x+1) + f(x) = 0$        $f(x) + f(x+1) = f(x^2 + x)$   
 $f(x_1) + f(x_2) = f\left(\frac{x_1 + x_2}{1 + x_1x_2}\right)$

A.  $f(x_1) \cdot f(x_2) = f(x_1 + x_2)$

B.  $f(x+2) - 2f(x+1) + f(x) = 0$

C.  $f(x) + f(x+1) = f(x^2 + x)$

D.  $f(x_1) + f(x_2) = f\left(\frac{x_1 + x_2}{1 + x_1x_2}\right)$

**Answer: D**



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16. about to only mathematics

A.  $9/5$

B. 4

C. 5

D.  $8/5$

**Answer: A**



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17. The value of  $3^{(\log)_4 5} - 5^{(\log)_4 3}$  is 0 (b) 1 (c) 2 (d) none of these

A. 0

B. 1

C. 2

D. none of these

**Answer: A**



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18. If  $2^{x+y} = 6^y$  and  $3^{x-1} = 2^{y+1}$ , then the value of  $(\log 3 - \log 2)(x - y)$  is 1 (b)  $(\log)_2 3 - (\log)_3 2$   $\log\left(\frac{3}{2}\right)$  (d) none of these

A. 1

B.  $\log_2 3 - \log_3 2$

C.  $\log(3/2)$

D. none of these

**Answer: C**



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19. The value of x satisfying  $\sqrt{3}^{-4+2\log_{\sqrt{5}} x} = 1/9$  is

A. 2

B. 3

C. 4

D. none of these

**Answer: D**



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20. The value of  $x$  satisfying the equation

$$3\sqrt{5}^{\log_5 55} \left( (\log_5)_5 (\log_5)_5 \log_5 \left( \frac{x}{2} \right) \right) = 1 \quad \text{(b) 3 (c) 18 (d) 54}$$

A. 1

B. 3

C. 18

D. 54

**Answer: D**



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21. If  $\sqrt{(\log)_2 x - 0.5} = (\log)_2 \sqrt{x}$ , then  $x$  equals odd integer (b) prime number composite number (d) irrational

A. odd integer

B. prime number

C. composite number

D. irrational

**Answer: B**



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22. If  $(\log)_y x + (\log)_x y = 1$ ,  $x^2 + y = 12$ , the value of  $xy$  is 9 (b) 12 (c)

15 (d) 30

A. 9

B. 12

C. 15

D. 21

**Answer: A**



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23.  $4^{\log_9 3} + 9^{\log_2 4} = 10^{\log_x 83}$ , then  $x$  is equal to

A. 2

B. 3

C. 10

D. 30

**Answer: C**



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24. If  $(x + 1)^{(\log)_{10}(x+1)} = 100(x + 1)$ , then



A. all the roots are positive real numbers.

B. all the roots lie in the interval (0, 100)

C. all the roots lie in the interval [-1, 99]

D. none of these

**Answer: C**

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25. If  $\log_2 x + \log_x 2 = \frac{10}{3} = \log_2 y + \log_y 2$  and  $x \neq y$ , then  $x + y =$

A. 2

B.  $65/8$

C.  $37/6$

D. none of these

**Answer: D**

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26. If  $(\log)_{10} \left[ \frac{1}{2^x + x - 1} \right] = x [(\log)_{10} 5 - 1]$ , then  $x =$  4 (b) 3 (c) 2 (d)

1

A. 4

B. 3

C. 2

D. 1

**Answer: D**



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27. If  $(\log)_3 \{ 5 + 4(\log)_3(x - 1) \} = 2$ , then  $x$  is equal to 4 (b) 3 (c) 8 (d)

$(\log)_2 16$

A. 2

B. 4

C. 8

D. 16

**Answer: B**



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28. If  $2x^{(\log)_4 3} + 3^{(\log)_4 x} = 27$ , then  $x$  is equal to 2 (b) 4 (c) 8 (d) 16

A. 2

B. 4

C. 8

D. 16

**Answer: D**



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29. The equation

$$\log_4(2 - x) + \log_{0.25}(2 + x) = \log_4(1 - x) + \log_{0.25}(2x + 1)$$
 has

- A. only one prime solution
- B. two real solutions
- C. no real solution
- D. none of these

**Answer: D**



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30. The value of  $b$  for which the equation

$$2(\log)_{\frac{1}{25}}(bx + 28) = -(\log)_5(12 - 4x - x^2)$$
 has coincident roots is

$$b = -12 \quad (b) \quad b = 4 \text{ or } b = -12 \quad b = 4 \text{ or } b = -12 \quad (d)$$

$$b = -4 \text{ or } b = 12$$

A.  $b = -12$

B.  $b = 4$

C.  $b = 4$  or  $b = -12$

D.  $b = -4$  or  $b = 12$

**Answer: C**



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31. If the equation  $2^x + 4^y = 2^y$  is solved for  $y$  in terms of  $x$  where  $x < 0$ , then the sum of the solution is  $x(\log)_2(1 - 2^x)$  (b)  $x + (\log)_2(1 - 2^x)$  (c)  $(\log)_2(1 - 2^x)$  (d)  $x(\log)_2(2^x + 1)$

A.  $x \log_2(1 - 2^x)$

B.  $x + \log_2(1 - 2^x)$

C.  $\log_2(1 - 2^x)$

D.  $x \log_2(2^x + 1)$

**Answer: B**



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32. The number of solution of  $x^{\log x}(x + 3)^2 = 16$  is a) 0 (b) 1 (c) 2 (d)  $\infty$

A. 0

B. 1

C. 2

D.  $\infty$

Answer: A



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33. The product of roots of the equation  $\frac{\log_8\left(\frac{8}{x^2}\right)}{(\log_8 x)^2} = 3$  is 1 (b) (c)  $1/3$  (d)

$1/4$

A. 1

B.  $1/2$

C.  $1/3$

D.  $1/4$

**Answer: D**



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**34.** Let  $a > 1$  be a real number. Then the number of roots equation

$$a^{2(\log)_2 x} = 15 + 4x^{(\log)_2 a} \text{ is 2 (b) infinite (c) 0 (d) 1}$$

A. 2

B. infinite

C. 0

D. 1

**Answer: D**



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35. The number of roots of the equation  $(\log)_{3\sqrt{x}}x + (\log)_{3x}\sqrt{x} = 0$  is 1

(b) 2 (c) 3 (d) 0

A. 1

B. 2

C. 3

D. 0

**Answer: B**



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36. The set of all  $x$  satisfying the equation

$$x^{\log} - 3x^2 + ((\log)_3 x)^{2-10} = \frac{1}{x^2}$$

is 1 (b) 2 (c) 3 (d) 0

A.  $\{1, 9\}$

B.  $\{1, 9, 1/81\}$

C.  $\{1, 4, 1/81\}$



D.  $\{9, 1/81\}$

**Answer: B**



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**37.** Number of real values of  $x$  satisfying the equation

$$(\log)_2(x^2 - x)(\log)_2\left(\frac{x-1}{x}\right) + ((\log)_2x)^2 = 4, \text{ is } 0 \text{ (b) } 2 \text{ (c) } 3 \text{ (d) } 7$$

A. 0

B. 2

C. 3

D. 7

**Answer: B**



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38. Find the value of  $x$  satisfying the equations

$$\log_3(\log_2 x) + \log_{1/3}(\log_{1/2} y) = 1 \text{ and } xy^2 = 9$$

A. 4

B. 8

C. 16

D. 64

**Answer: D**



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39. If  $x_1$  and  $x_2$  are the roots of the equation  $e^{2x \ln x} = x^3$  with  $x_1 > x_2$ ,

then  $x_1 = 2x_2$  (b)  $x_1 = x_2^2$   $2x_1 = x_2^2$  (d)  $x_1^2 = x_2^3$

A.  $x_1 = 2x_2$

B.  $x_1 = x_2^2$

C.  $2x_1 = x_2^2$

D.  $x_1^2 = x_2^3$

**Answer: B**



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**40.** The number of real values of the parameter  $k$  for which  $(\log_{16} x)^2 - (\log)_{16}x + (\log)_{16}k = 0$  with real coefficients will have exactly one solution is 2 (b) 1 (c) 4 (d) none of these

A. 2

B. 1

C. 4

D. none of these

**Answer: A**



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41.  $x^{(\log)_5 x} > 5$  implies  $x \in (0, \infty)$  (b)  $[2, 2.5]$  (c)  $(2, 2.5)$  (d)  $(0, 2.5)$

A.  $x \in (0, \infty)$

B.  $x \in (0, 1/5) \cup (5, \infty)$

C.  $x \in (1, \infty)$

D.  $x \in (1, 2)$

**Answer: B**



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42. If  $S = \left\{ x \in N : 2 + (\log)_2 \sqrt{x+1} > 1 - (\log)_{\frac{1}{2}} \sqrt{4-x^2} \right\}$ , then

$S = \{1\}$  (b)  $S = Z$  (d)  $S = N$  (d) none of these

A.  $S = \{1\}$

B.  $S = Z$

C.  $S = N$

D. none of these

**Answer: A**



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43. If  $S = \{x \in R : ((\log)_{0.6} 0.216)(\log)_5(5 - 2x) \leq 0\}$ , then  $S$  is equal to (a)  $(2.5, \infty)$  (b)  $(2, 2.5)$  (c)  $(2, 2.5)$  (d)  $(0, 2.5)$

A.  $[2.5, \infty)$

B.  $[2, 2.5)$

C.  $(2, 2.5)$

D.  $(0, 2.5)$

**Answer: B**



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44. Solution set of the inequality  $\frac{1}{2^x - 1} > \frac{1}{1 - 2^{x-1}}$  is (a)  $(1, \infty)$  (b)  $(0, (\log)_2 \left(\frac{4}{3}\right))$  (c)  $(-1, \infty)$  (d)  $(0, (\log)_2 \left(\frac{4}{3}\right)) \cup (1, \infty)$

A.  $(1, \infty)$

B.  $(0, \log_2(4/3))$

C.  $(-1, \infty)$

D.  $(0, \log_2(4/3)) \cup (1, \infty)$

**Answer: D**



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**45.** If  $(\log)_2x + (\log)_2y \geq 6$ , then the least value of  $x + y$  is 4 (b) 8 (d) 16

(d) 32

A. 4

B. 8

C. 16

D. 32

**Answer: C**

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46. Which of the following is not the solution

$$\log_x \left( \frac{5}{2} - \frac{1}{x} \right) > \left( \frac{5}{2} - \frac{1}{x} \right) ?$$

A.  $\left( \frac{2}{5}, \frac{1}{2} \right)$

B.  $(1, 2)$

C.  $\left( \frac{2}{5}, 1 \right)$

D. none of these

**Answer: A :: B**

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47. The solution set of the inequality

$$(\log)_{10}(x^2 - 16) \leq (\log)_{10}(4x - 11) \text{ is } (a) (4, \infty) \text{ (b) } (4, 5) \text{ (c) } \left( \frac{11}{4}, \infty \right) \text{ (d)}$$

$$\left( \frac{11}{4}, 5 \right)$$

A.  $(4, \infty)$

B.  $(4, 5]$

C.  $(11/4, \infty)$

D.  $\left(\frac{11}{4}, 5\right)$

**Answer: B**

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48. Solution set of the inequality  $(\log)_{0.8} \left( (\log)_6 \frac{x^2 + x}{x + 4} \right) < 0$  is

A.  $(-4, -3)$

B.  $(-3, 4) \cup (8, \infty)$

C.  $(-3, \infty)$

D.  $(-4, -3) \cup (8, \infty)$

**Answer: D**

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49. Which of the following is not the solution of  $(\log)_3(x^2 - 2) < (\log)_3\left(\frac{3}{2}|x| - 1\right)$  is  $(\sqrt{2}, 2)$  (b)  $(-2, -\sqrt{2})$   $(-\sqrt{2}, 2)$  (d) none of these

A.  $(-\sqrt{2}, 2)$

B.  $(-2, -\sqrt{2})$

C.  $(-\sqrt{2}, 2)$

D. none of these

Answer: C



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50. The true solution set of inequality  $(\log)_{(x+1)}(x^2 - 4) > 1$  is equal to  $2, \infty)$  (b)  $\left(2, \frac{1 + \sqrt{21}}{2}\right)$   $\left(\frac{1 - \sqrt{21}}{2}, \frac{1 + \sqrt{21}}{2}\right)$  (d)  $\left(\frac{1 + \sqrt{21}}{2}, \infty\right)$

A.  $(2, \infty)$

B.  $\left(2, \frac{1 + \sqrt{21}}{2}\right)$

C.  $\left(\frac{1 - \sqrt{21}}{2}, \frac{1 + \sqrt{21}}{2}\right)$

D.  $\left(\frac{1 + \sqrt{21}}{2}, \infty\right)$

**Answer: D**



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## Exercise Multiple

1. For  $a > 0, \neq 1$ , the roots of the equation  $(\log)_{ax} a + (\log)_x a^2 + (\log)_{a^2a} a^3 = 0$  are given  $a^{-\frac{4}{3}}$  (b)  $a^{-\frac{3}{4}}$  (c)  $a$  (d)  $a^{-\frac{1}{2}}$

A.  $a^{-4/3}$

B.  $a^{-3/4}$

C.  $a$

D.  $a^{-1/2}$

**Answer: A::D**



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2. The real solutions of the equation  $2^{x+2} \cdot 5^{6-x} = 10^x \cdot 2$  is/are 1 (b) 2

(c)  $(\log)_{10}(250)$  (d)  $(\log)_{10}4 - 3$

A. 1

B. 2

C.  $-\log_{10}(250)$

D.  $\log_{10}4 - 3$

**Answer: B::C::D**



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3. If  $\frac{\log x}{b-c} = \frac{\log y}{c-a} = \frac{\log z}{a-b}$ , then which of the following is/are true?

A.  $xyz = 1$

B.  $x^a y^b z^c = 1$

C.  $x^{b+c} y^{c+a} z^{a+b} = 1$

D.  $xyz = x^a y^b z^c$

Answer: A::B::C::D



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4. If  $(\log)_k x \log_5 k = (\log)_x 5$ ,  $k \neq 1$ ,  $k > 0$ , then  $x$  is equal to  $k$  (b)  $1/5$

(c) 5 (d) none of these

A.  $k$

B.  $1/5$

C. 5

D. none of these

**Answer: B::C**

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5. If  $p, q \in \mathbb{N}$  satisfy the equation  $x^x = (\sqrt{x})^2$ , then  $p$  and  $q$  are relatively prime (b) twin prime (c) coprime if  $(\log)_q p$  is defined, then  $(\log)_p q$  is not and vice versa

A.  $p+q=5$

B.  $|p - q| = 4$

C.  $pq=4$

D. if  $\log_q p$  is defined, then  $\log_p q$  is not and vice versa

**Answer: A::C::D**

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6. Which of the following, when simplified, reduces to unity?

$$(\log)_{10} 5 \log_{10} 20 + ((\log)_{10} 2)^2 \cdot (c) - (\log)_5 (\log)_3 \sqrt{5\sqrt{9}} \frac{1}{6} (\log)_{\frac{\sqrt{3}}{2}} \left( \frac{64}{27} \right)$$

A.  $\log_{10} 5 \cdot \log_{10} 20 + (\log_{10} 2)^2$

B.  $\frac{2 \log 2 + \log 3}{\log 48 - \log 4}$

C.  $-\log_5 \log_3 \sqrt{\sqrt[5]{9}}$

D.  $\frac{1}{6} \log_{\sqrt{3}/2} \left( \frac{64}{27} \right)$

**Answer: A::B::C**



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7. If  $(\log)_a x = b$  for permissible values of  $a$  and  $x$ , then identify the statement(s) which can be correct. If  $a$  and  $b$  are two irrational numbers, then  $x$  can be rational. If  $a$  is rational and  $b$  is irrational, then  $x$  can be rational. If  $a$  is irrational and  $b$  is rational, then  $x$  can be rational. If  $a$  and  $b$  are rational, then  $x$  can be rational.

A. If  $a$  and  $b$  are two irrational numbers, then  $x$  can be rational.

B. If a is rational and b is irrational, then x can be rational.

C. If a is irrational and b is rational, then x can be rational.

D. If a and b are rational, then x can be rational.

**Answer: A::B::C::D**



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8. The number of solutions of the equation

$$\log_{x+1}(x - 0.5) = \log_{x-0.5}(x + 1) \text{ is}$$

A. two real solutions

B. no prime solution

C. one integral solution

D. no irrational solution

**Answer: B::C::D**



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9. The equation  $\sqrt{1 + \log_x \sqrt{27}} \log_3 x + 1 = 0$  has

- A. no integral solution
- B. one irrational solution
- C. two real solutions
- D. no prime solution

**Answer: A::D**



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10. If  $\log_{1/2}(4 - x) \geq \log_{1/2} 2 - \log_{1/2}(x - 1)$ , then  $x$  belongs to

- A.  $(1, 2]$
- B.  $[3, 4)$
- C.  $(1, 3]$
- D.  $[1, 4)$



**Answer: A::B**



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11. If the equation  $x^{\log_a x^2} = \frac{x^{k-2}}{a^k}$ ,  $a \neq 0$  has exactly one solution for  $x$ , then the value of  $k$  is/are

A.  $6 + 4\sqrt{2}$

B.  $2 + 6\sqrt{3}$

C.  $6 - 4\sqrt{2}$

D.  $2 - 6\sqrt{3}$

**Answer: A::C**



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12. The set of real values of  $x$  satisfying the equation

$$|x - 1|^{\log_3(x^2) - 2\log_x(9)} = (x - 1)^7$$

A.  $\frac{1}{\sqrt{3}}$

B. 1

C. 2

D. 81

**Answer: C::D**

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13. If  $x = 9$  is one of the solutions of

$$\log_e(x^2 + 15a^2) - \log_e(a - 2) = \log_e\left(\frac{8ax}{a - 2}\right), \text{ then}$$

A.  $a = \frac{3}{5}$

B.  $a = 3$

C.  $x = 15$

D.  $x = 2$

**Answer: B**



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14. In which of the following,  $m > n$  ( $m, n \in R$ )?

A.  $m = (\log_2 5)^2$  and  $n = \log_2 20$

B.  $m = \log_{10} 2$  and  $n = \log_{10} \sqrt[3]{10}$

C.  $m = \log_{10} 5 \cdot \log_{10} 20$  and  $n = 1$

D.  $m = \log_{1/2} \left( \frac{1}{3} \right)$  and  $n = \log_{1/3} \left( \frac{1}{2} \right)$

Answer: A:D



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15. if  $\log_{10} 5 = a$  and  $\log_{10} 3 = b$  then:

A.  $\log_{30} 8 = \frac{3(1-a)}{b+1}$

B.  $\log_{40} 15 = \frac{a+b}{3-2a}$

C.  $\log_{243} 32 = \frac{1-a}{b}$

D. none of these

**Answer: A::B::C**



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16. The value of  $\frac{6a^{\log_e b}(\log_{a^2} b)(\log_{b^2} a)}{e^{\log_e a \cdot \log_e b}}$  is

A. independent of a

B. independent of b

C. dependent on a

D. dependent on b

**Answer: A::B**



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17. The inequality  $\sqrt{x^{(\log)_2 \sqrt{x}}} \geq 2$  is satisfied by (A) only one value of  $x$   
(B)  $x \in \left[0, \left(\frac{1}{4}\right)\right]$  (C)  $x \in [4, \infty]$  (d)  $x \in (1, 2)$

A. only one value of  $x$

B.  $x \in \left(0, \frac{1}{4}\right]$

C.  $x \in [4, \infty)$

D.  $x \in (1, 2)$

**Answer: B::C**



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## Exercise Comprehension

1. Find the value of  $x$  satisfying the equations  
 $\log_3(\log_2 x) + \log_{1/3}(\log_{1/2} y) = 1$  and  $xy^2 = 9$

A. (200, 300)

B. (400, 500)

C. (700, 800)

D. none of these

**Answer: C**



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2. Find the value of  $x$  satisfying the equations

$$\log_3(\log_2 x) + \log_{1/3}(\log_{1/2} y) = 1 \text{ and } xy^2 = 9$$

A. (5, 7)

B. (7, 10)

C. (11, 15)

D. (25, 30)

**Answer: B**



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3. Consider equations  $x^{\log_y x} = 2$  and  $y^{\log_x y} = 16$ .

The value of  $x$  is

A.  $2^{\sqrt[3]{2}}$

B.  $2^{\sqrt[3]{4}}$

C.  $2^{\sqrt[3]{64}}$

D.  $2^{\sqrt[3]{256}}$

**Answer: B**



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4. Solve  $x^{(\log)_y x} = 2$  and  $y^{(\log)_x y} = 16$

A.  $2^{\sqrt[3]{2}}$

B.  $2^{\sqrt[3]{4}}$

C.  $2^{\sqrt[3]{128}}$

D.  $2^{\sqrt[3]{16}}$

**Answer: D**



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5. Prove that:  $2^{\sqrt{(\log_a \sqrt{a/b}) + (\log_b \sqrt{a/b})}} - (\log_a \sqrt{2/b}) + (\log_b \sqrt{a/b}) \geq \sqrt{(\log_a \sqrt{a/b}) + (\log_b \sqrt{a/b})} - 1$  if  $b \geq a > 1$

A. 1

B. 2

C.  $2^{\log_a b}$

D.  $2^{\log_b a}$

**Answer: B**



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6. Prove that:  $2^{\sqrt{(\log_a a) + (\log_b a)}} \cdot 2^{\sqrt{(\log_a b) + (\log_b a)}} = 2^{\sqrt{(\log_a a) + (\log_b a)}}$

A. 1

B. 2

C.  $2^{\log_a b}$

D.  $2^{\log_b a}$

**Answer: C**



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**Exercise Matrix**

List I	List II
a. The smallest integer greater than $\frac{1}{\log_3 \pi} + \frac{1}{\log_4 \pi}$ is	p. 10
b. Let $3^a = 4$ , $4^b = 5$ , $5^c = 6$ , $6^d = 7$ , $7^e = 8$ , and $8^f = 9$ . Then the value of the product $(abcdef)$ is	q. 3
c. Characteristic of the logarithm of 2008 to the base 2 is	r. 1
d. If $\log_2(\log_2(\log_3 x)) = \log_2(\log_3(\log_2 y)) = 0$ , then the value of $(x - y)$ is	s. 2

1.



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List I	List II
a. $2^{\log_{(2\sqrt{2})} 15}$ is	p. rational
b. $\sqrt[3]{\left(5^{1/\log_7 5} + \frac{1}{\sqrt{(-\log_{10} 0.1)}}\right)}$ is	q. irrational
c. $\log_3 5 \cdot \log_{25} 27$ is	r. composite
d. Product of roots of equation $x^{\log_{10} x} = 100x$ is	s. prime

2.



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List I	List II
a. The value of $\log_2 \log_2 \log_4 256 - \log_{\sqrt{2}} 4$ is	p. 1
b. If $\log_3 (5x - 2) - 2 \log_3 \sqrt{3x + 1} = 1 - \log_3 4$ , then $x =$	q. 6
c. Product of roots of the equation $7x^2 + x^2 - 4x - 5 = (x - 1)$ is	r. 3
d. Number of integers satisfying $\log_2 (\sqrt{x} - 2) (\log_{\frac{1}{4}} x)^2 - 1 > 0$ are	s. 5

3.

- A.  $a \ b \ c \ d$   
 $s \ p \ q \ r$
- B.  $a \ b \ c \ d$   
 $s \ p \ q \ r$
- C.  $a \ b \ c \ d$   
 $q \ r \ p \ s$
- D.  $a \ b \ c \ d$   
 $r \ p \ q \ s$

Answer: A



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Exercise Numerical

1. If  $\log_a b = 2$ ,  $\log_b c = 2$ , and  $\log_3 c = 3 + \log_3 a$ , then the value of  $c/(ab)$  is \_\_\_\_\_.

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2. The value of  $(\log_{10} 2)^3 + \log_{10} 8 \log_{10} 5 + (\log_{10} 5)^3$  is .....

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3. If  $(\log)_4 A = (\log)_6 B = (\log)_9 (A + B)$ , then  $[4(B/A)]$  (where  $[ ]$  represents the greatest integer function) equals .....

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4. Integral value of  $x$  which satisfies the equation  $= \log_6 54 + (\log)_x 16 = (\log)_{\sqrt{2}} x - (\log)_{36} \left(\frac{4}{9}\right)$  is..

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5. If  $a = \log_{245} 175$  and  $b = \log_{1715} 875$ , then the value of  $\frac{1 - ab}{a - b}$  is \_\_\_\_\_.

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6. The difference of roots of the equation  $((\log)_{27} x^3)^2 = (\log)_{27} x^6$  is .....

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7. Sum of all integral values of  $x$  satisfying the inequality  $\left(3^{\left(\frac{5}{2}\right)^{\log(123)}}\right) - \left(3^{\log}\right) > 32$  is.....

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8. The least integer greater than  $(\log)_2 15 (\log)_{\frac{1}{6}} 2 (\log)_3 \frac{1}{6}$  is .....

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9. The reciprocal of  $\frac{2}{(\log)_4(2000)^6} + \frac{3}{(\log)_5(2000)^6}$  is .....

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10. Sum of integers satisfying  $\sqrt{(\log)_2 x - 1} - \frac{1}{2}(\log)_2(x^3) + 2 > 0$  is.....

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11. Number of integers satisfying the inequality  $(\log)_{\frac{1}{2}}|x - 3| > 1$  is.....

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12. Number of integers  $\leq 10$  satisfying the inequality  $2(\log)_{\frac{1}{2}}(x - 1) \leq \frac{1}{3} - \frac{1}{(\log)_{x^2 - x} 8}$  is.....

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13. The value of  $\left(\sqrt{3+2\sqrt{2}} + \sqrt{3-2\sqrt{2}}\right)^{2^9}$  is \_\_\_\_\_.

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14. The value of  $5^{(\log)_{\frac{1}{5}}\left(\frac{1}{2}\right)} + (\log)_{\sqrt{2}}\frac{4}{\sqrt{7}+\sqrt{3}} + (\log)_{\frac{1}{2}}\frac{1}{10+2\sqrt{21}}$   
is.....

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15. The value of  $N = \frac{(\log)_5 250}{(\log)_{50} 5} - \frac{(\log)_5 10}{(\log)_{1250} 5}$  is.....

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16. if  $x + \log_{10}(1 + 2^x) = x \log_{10} 5 + \log_{10} 6$  then  $x$

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17. The  $x, y, z$  are positive real numbers such that  $(\log)_{2x}z = 3$ ,  $(\log)_{5y}z = 6$ , and  $(\log)_{xy}z = \frac{2}{3}$ , then the value of  $\left(\frac{1}{2z}\right)$  is .....

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18. If  $a = (\log)_{12}18$ ,  $b = (\log)_{24}54$ , then find the value of  $ab + 5(a - b)$ .

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Jee Previous Year

1. Show that the equation  $e^{\sin x} - e^{-\sin x} - 4 = 0$  has no real solution.

A. infinite number of real roots

B. no real roots

C. exactly one real root



D. exactly four real roots

**Answer: B**



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2. Let  $(x_0, y_0)$  be the solution of the following equations:

$$(2x)^{1n2} = (3y)^{1n3} \quad 3^{1nx} = 2^{1ny}$$

The  $x_0$  is  $\frac{1}{6}$  (b)  $\frac{1}{3}$  (c)  $\frac{1}{2}$  (d) 6

A.  $\frac{1}{6}$

B.  $\frac{1}{3}$

C.  $\frac{1}{2}$

D. 6

**Answer: C**



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3. If  $3^x = 4^{x-1}$ , then  $x = \frac{2(\log)_3 2}{2(\log)_3 2 - 1}$  (b)  $\frac{2}{2 - (\log)_2 3}$   $\frac{1}{1 - (\log)_4 3}$

(d)  $\frac{2(\log)_2 3}{2(\log)_2 3 - 1}$

A.  $\frac{2\log_3 2}{2\log_3 2 - 1}$

B.  $\frac{2}{2 - \log_2 3}$

C.  $\frac{1}{1 - \log_4 3}$

D.  $\frac{2\log_2 3}{2\log_2 3 - 1}$

Answer: A::B::C

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4. The value of

$6 + (\log)_{3/2} \left( \frac{1}{3\sqrt{2}} \sqrt{\sqrt{4 - \frac{1}{3\sqrt{2}} \sqrt{4 - \frac{1}{\sqrt{2}} \sqrt{4 - \frac{1}{3\sqrt{2}}}}} \right)$  is .....

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5. The value of  $\left((\log_2 9)^2\right)^{\frac{1}{\log_2 (\log_2 9)}} \times (\sqrt{7})^{\frac{1}{\log_4 7}}$  is \_\_\_\_\_.



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