



MATHS

BOOKS - CENGAGE

METHODS OF DIFFERENTIATION

Question Bank

1. Let $f: (-5, 5) \rightarrow \mathbb{R}$ be a differentiable function with $f(4) = 1$, $f'(4) = 1$, $f(0) = -1$ and $f''(0) = 1$, If $g(x) = f(2f^2(x)+2)^2$, then $g''(0)$ equals

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2.

Let $e^y = \frac{\sqrt{1+\alpha} + \sqrt{1-\alpha}}{\sqrt{1+\alpha} - \sqrt{1-\alpha}}$ and $\tan \frac{x}{2} = \sqrt{\frac{1-\alpha}{1+\alpha}}$, $\alpha \in [-1, 0] \cup (0, 1]$

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3. If $y = y(x)$ and it follows the relation $4xe^{xy} = y + 5\sin^2 x$, then $y'(0)$ is equal to _____

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4.
$$\frac{1}{\sqrt{x+3} - \sqrt{x-4}}$$

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5. Let $x = f(t)$ and $y = g(t)$, where x and y are twice differentiable function If

$f'(0) = g'(0) = f''(0) = 2, g(0) = 6$, then the value of $\left(\frac{d^2y}{(dx^2)} \right)_{t=0}$

is equal to

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6. If $f(x)$ is twice differentiable and $f''(0) = 3$, then

$$\lim_{x \rightarrow 0} \frac{2f(x) - 3f(2x) + f(4x)}{x^2} \text{ is}$$

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7. If $f(x) = 2x^3 + 7x - 5$ and $g(x) = f^{-1}(x)$, then reciprocal of $g'(4)$ is equal to

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8. If $e^y = e^x \cdot x^{-y}$, the value of $\left. \frac{dy}{dx} \right|_{x=e}$ is

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9. Suppose the function $f(x)-f(2x)$ has the derivative 5 at $x=1$ and derivative 7 at $x=2$. The derivative of the function $f(x)-f(4x)$ at $x=1$, has the value equal to

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10. Let $h(x)$ be differentiable for all x and let $f(x) = (kx + e^x)h(x)$ where k is some constant. If $h(0) = 5$, $h'(0) = -2$ and $f'(0) = 18$ then the value of k is equal to

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11. If f and g are differentiable functions such that $g'(a) = 2$ and $g(a) = b$ and if $f \circ g$ is an identity function then $f'(b)$ has the value equal to

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12. If $\phi(x) = x \cdot \sin x$ then $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\phi(x) - \phi\left(\frac{\pi}{2}\right)}{x - \frac{\pi}{2}} =$

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13. If $(\cos x)^y = (\cos y)^x$, "then" $(dy)/(dx)$ is equal to



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