



MATHS

BOOKS - CENGAGE

PROPERTIES AND SOLUTIONS OF TRIANGLE

Examples

1. In triangle ABC , D is on AC such that $AD=BC$ and $BD=DC$, $\angle DBC = 2x$ and $\angle BAD = 3x$ where each angle is in degree. Then find x

[View Text Solution](#)

2. In a circle of radius r , chords of length a and b cm subtend angles θ and 3θ , respectively, at the center. Show that $r = a\sqrt{\frac{a}{3a-b}} \text{ cm}$

[Watch Video Solution](#)

3. perpendiculars are drawn from the angles A, B and C of an acute-angled triangle on the opposite sides, and produced to meet the circumscribing circle. If these produced parts are α, β, γ , respectively, then show that $\frac{a}{\alpha} + \frac{b}{\beta} + \frac{c}{\gamma} = 2(\tan A + \tan B + \tan C)$.



Watch Video Solution

4. D, E, F are three points on the sides BC, CA, AB , respectively, such that $\angle ADB = \angle BEC = \angle CFA = \theta$. A', B', C' are the points of intersections of the lines AD, BE, CF inside the triangle. Show that area of $A'B'C' = 4 \cos^2 \theta$, where is the area of ABC .



Watch Video Solution

5. In ABC , a semicircle is inscribed, which lies on the side AB . If x is the length of the angle bisector through angle C , then prove that the radius of the semicircle is $x \sin\left(\frac{C}{2}\right)$.

[Watch Video Solution](#)

6. Given the base of a triangle, the opposite angle A , and the product k^2 of other two sides, show that it is not possible for a to be less than $2k \sin \frac{A}{2}$

[Watch Video Solution](#)

7. In a triangle of base a , the ratio of the other two sides is $r (< 1)$. Show that the altitude of the triangle is less than or equal to $\frac{ar}{1 - r^2}$

[Watch Video Solution](#)

8. Let ABC be a triangle with incentre at I . Also, let P and Q be the feet of perpendiculars from $A \rightarrow BI$ and CI , respectively. Then which of the following results are correct? $\frac{AP}{BI} = \frac{\frac{\sin B}{2} \frac{\cos C}{2}}{\frac{\sin A}{2}}$ (b) $\frac{AQ}{CI} = \frac{\frac{\sin C}{2} \frac{\cos B}{2}}{\frac{\sin A}{2}}$

$\frac{AP}{BI} = \frac{\frac{\sin C}{2} \frac{\cos B}{2}}{\frac{\sin A}{2}}$ (d) $\frac{AP}{BI} + \frac{AQ}{CI} = \sqrt{3}$ if $\angle A = 60^\circ$



Watch Video Solution

9. Let O be the circumcentre and H be the orthocentre of an acute angled triangle ABC . If $A > B > C$, then show that

$$Ar(\triangle BOH) = Ar(\triangle AOH) + Ar(\triangle COH)$$


Watch Video Solution

10. If I is the incenter of $\triangle ABC$ and R_1, R_2 , and R_3 are, respectively, the radii of the circumcircle of the triangle IBC , ICA , and IAB , then prove that $R_1 R_2 R_3 = 2rR^2$



Watch Video Solution

11. Show that the line joining the incenter to the circumcentre of triangle ABC is inclined to the side BC at an angle $\tan^{-1} \left(\frac{\cos B + \cos C - 1}{\sin C - \sin B} \right)$



Watch Video Solution

12. about to only mathematics



Watch Video Solution

13. about to only mathematics



Watch Video Solution

14. Let ABC be a triangle with incenter I and inradius r . Let D , E , and F be the feet of the perpendiculars from I to the sides BC , CA , and AB , respectively. If r_1 , r_2 and r_3 are the radii of circles inscribed in the quadrilaterals $AFIE$, $BDIF$, and $CEID$, respectively, prove that

$$\frac{r_1}{r - r_1} + \frac{r_2}{r - r_2} + \frac{r_3}{r - r_3} = \frac{r_1 r_2 r_3}{(r - r_1)(r - r_2)(r - r_3)}$$



Watch Video Solution

15. In convex quadrilateral $ABCD$, $AB = a$, $BC = b$, $CD = c$, $DA = d$. This quadrilateral is such that a circle can be inscribed in it and a circle can also be circumscribed about it. Prove that $\frac{\tan^2 A}{2} = \frac{bc}{ad}$.



Watch Video Solution

16. If in a triangle ABC , $b = 3c$ and $C - B = 90^\circ$, then find the value of $\tan B$



Watch Video Solution

17. In a triangle ABC if $BC = 1$ and $AC = 2$, then what is the maximum possible value of angle A ?



Watch Video Solution

18. The perimeter of a triangle ABC is six times the arithmetic mean of the sines of its angles. If the side a is 1 then find angle A .



Watch Video Solution

19. If $A = 75^\circ$, $b = 45^\circ$, then prove that $b + c\sqrt{2} = 2a$



Watch Video Solution

20. If the base angles of triangle are $\left(22\frac{1}{2}\right)^\circ$ and $\left(112\frac{1}{2}\right)^\circ$, then prove that the altitude of the triangle is equal to $\frac{1}{2}$ of its base.



Watch Video Solution

21. If a^2, b^2, c^2 are in A.P., then prove that $\tan A, \tan B, \tan C$ are in H.P.



Watch Video Solution

22. In any triangle ABC , prove that:

$$\frac{a^2 \sin(B - C)}{\sin B + \sin C} + \frac{b^2 \sin(C - A)}{\sin C + \sin A} + \frac{c^2 \sin(A - B)}{\sin A + \sin B} = 0$$



View Text Solution

23. In any triangle. if $\frac{a^2 - b^2}{a^2 + b^2} = \frac{\sin(A - B)}{\sin(A + B)}$, then prove that the triangle is either right angled or isosceles.



Watch Video Solution

24. ABCD is a trapezium such that $AB \parallel CD$ and CB is perpendicular to them. If $\angle ADB = \theta$, $BC = p$, and $CD = q$, show that

$$AB = \frac{(p^2 + q^2) \sin \theta}{p \cos \theta + q \sin \theta}$$



Watch Video Solution

25. In a ΔABC , $\angle C = 60^\circ$ & $\angle A = 75^\circ$. If D is a point on AC such that area of the ΔBAD is $\sqrt{3}$ times the area of the ΔBCD , then the $\angle ABD = 60^\circ$ (b) 30° (c) 90° (d) none of these



Watch Video Solution

26. In a scalene triangle ABC , D is a point on the side AB such that $CD^2 = AD \cdot DB$, $\sin \angle C \in AS \in B = \frac{\sin^2 C}{2}$ then prove that CD is internal bisector of $\angle C$.



Watch Video Solution

27. In a triangle ABC , $\angle A = 60^\circ$ and $b : c = (\sqrt{3} + 1) : 2$, then find the value of $(\angle B - \angle C)$.



Watch Video Solution

28. If the median AD of triangle ABC makes an angle $\frac{\pi}{4}$ with the side BC, then find the value of $|\cot B - \cot C|$.



Watch Video Solution

29. The base of a triangle is divided into three equal parts. If t_1, t_2, t_3 are the tangents of the angles subtended by these parts at the opposite vertex, prove that $\left(\frac{1}{t_1} + \frac{1}{t_2}\right)\left(\frac{1}{t_2} + \frac{1}{t_3}\right) = 4\left(1 + \frac{1}{t_2^2}\right)$.



Watch Video Solution

30. In $\triangle ABC$, prove that $(a - b)^2 \cos^2 \frac{C}{2} + (a + b)^2 \sin^2 \frac{C}{2} = c^2$



Watch Video Solution

31. In $\triangle ABC$, if $(a + b + c)(a - b + c) = 3ac$, then find $\angle B$.



Watch Video Solution

32. If $a = \sqrt{3}$, $b = \frac{1}{2}(\sqrt{6} + \sqrt{2})$ and $c = 2$, then find $\angle A$



Watch Video Solution

33. The sides of a triangle are $x^2 + x + 1$, $2x + 1$, and $x^2 - 1$. Prove that the greatest angle is 120° .



Watch Video Solution

34. If the angles A, B, C of a triangle are in A.P. and sides a, b, c, are in G.P., then prove that a^2, b^2, c^2 are in A.P.



Watch Video Solution

35. Let a, b and c be the three sides of a triangle, then prove that the equation $b^2x^2 + (b^2 = c^2 - a^2)x + c^2 = 0$ has imaginary roots.

[Watch Video Solution](#)

36. Let $a \leq b \leq c$ be the lengths of the sides of a triangle. If $a^2 + b^2$

[Watch Video Solution](#)

37. In a triangle ABC , if the sides a, b, c , are roots of $x^3 - 11x^2 + 38x - 40 = 0$, then find the value of

$$\frac{\cos A}{a} + \frac{\cos B}{b} + \frac{\cos C}{c}$$

[Watch Video Solution](#)

38. If in a triangle ABC , $\angle C = 60^\circ$, then prove that

$$\frac{1}{a+c} + \frac{1}{b+c} = \frac{3}{a+b+c}.$$

[Watch Video Solution](#)

39. In a triangle, if the angles $A, B, \text{ and } C$ are in A.P. show that

$$2 \frac{\cos 1}{2} (A - C) = \frac{a + c}{\sqrt{a^2 - ac + c^2}}$$



Watch Video Solution

40. If $a = 9, b = 4 \text{ and } c = 8$ then find the distance between the middle point of BC and the foot of the perpendicular from A.



Watch Video Solution

41. Three parallel chords of a circle have lengths 2,3,4 units and subtend angles $\alpha, \beta, \alpha + \beta$ at the centre, respectively



Watch Video Solution

42. In a cyclic quadrilateral PQRS, PQ= 2 units, QR= 5 units, RS=3 units and $\angle PQR = 60^\circ$, then what is the measure of SP?

[Watch Video Solution](#)

43. Show that $a(b \cos C - c \cos B) = b^2 - c^2$

[Watch Video Solution](#)

44. If in a triangle $a \frac{\cos^2 C}{2} + c \frac{\cos^2 A}{2} = \frac{3b}{2}$, then find the relation between the sides of the triangle.

[Watch Video Solution](#)

45. Prove that $(b + c)\cos A + (c + a)\cos B + (a + b)\cos C = 2s$.

[Watch Video Solution](#)

46. If $\cos\left(\frac{A}{2}\right) = \sqrt{\frac{b+c}{2c}}$, then prove that $a^2 + b^2 = c^2$.

[Watch Video Solution](#)

47. If the cotangents of half the angles of a triangle are in A.P., then prove that the sides are in A.P.



Watch Video Solution

48. If the sides a, b and c of ABC are in A.P.; prove that

$$2 \sin\left(\frac{A}{2}\right) \sin\left(\frac{C}{2}\right) = \sin\left(\frac{B}{2}\right)$$



Watch Video Solution

49. Prove that $\left(\frac{\cot A}{2} + \frac{\cot B}{2}\right) \left(a \frac{\sin^2 B}{2} + b \frac{\sin^2 A}{2}\right) = \cot \frac{C}{2}$



Watch Video Solution

50. Find the value of $\tan A/2$, if area of ΔABC is $a^2 - (b - c)^2$.



Watch Video Solution

51. Prove that $a^2 \sin 2B + b^2 \sin 2A = 4\Delta$



Watch Video Solution

52. Prove that $\frac{(a+b+c)(b+c-a)(c+a-b)(a+b-c)}{4b^2c^2} = \sin^2 A$



Watch Video Solution

53. If the sides of a triangle are 17, 25 and 28, then find the greatest length of the altitude.



Watch Video Solution

54. In equilateral triangle ABC with interior point D, if the perpendicular distances from D to the sides of 4, 5, and 6, respectively, are given, then find the area of ABC.

[Watch Video Solution](#)

55. If area of a triangle is 2 sq. units, then find the value of the product of the arithmetic mean of the lengths of the sides of a triangle and harmonic mean of the lengths of the altitudes of the triangle.

[Watch Video Solution](#)

56. A triangle has sides 6, 7, and 8. The line through its incenter parallel to the shortest side is drawn to meet the other two sides at P and Q. Then find the length of the segment PQ.

[Watch Video Solution](#)

57. Each side of triangle ABC is divided into three equal parts. Find the ratio of the area of hexagon $PQRSTU$ to the area of the triangle ABC.

[Watch Video Solution](#)

58. The two adjacent sides of a cyclic quadrilateral are 2 and 5 and the angle between them is 60° . If the area of the quadrilateral is $4\sqrt{3}$, find the remaining two sides.



Watch Video Solution

59. In triangle ABC , $a:b:c = 4:5:6$. The ratio of the radius of the circumcircle to that of the incircle is ____.



Watch Video Solution

60. Given a triangle ABC with sides $a=7$, $b=8$ and $c=5$. Find the value of expression $(\sin A + \sin B + \sin C) \left(\frac{\cot A}{2} + \frac{\cot B}{2} + \frac{\cot C}{2} \right)$



Watch Video Solution

61. If $b = 3$, $c = 4$, and $B = \frac{\pi}{3}$, then find the number of triangles that can be constructed.



Watch Video Solution

62. If $A = 30^\circ$, $a = 7$, and $b = 8$ in ABC , then find the number of triangles that can be constructed.



Watch Video Solution

63. If in triangle ABC , $(a = (1 + \sqrt{3})\text{ cm}, b = 2\text{ cm}, \text{ and } \angle C = 60^\circ)$, then find the other two angles and the third side.



Watch Video Solution

64. In ABC , sides b, c and angle B are given such that a has two values a_1 and a_2 . Then prove that $|a_1 - a_2| = 2\sqrt{b^2 - c^2 \sin^2 B}$

[Watch Video Solution](#)

65. In ABC , a, c and A are given and b_1, b_2 are two values of the third side b such that $b_2 = 2b_1$. Then prove that $\sin A = \sqrt{\frac{9a^2 - c^2}{8c^2}}$

[Watch Video Solution](#)

66. O is the circumcenter of ABC and R_1, R_2, R_3 are respectively, the radii of the circumcircles of the triangle OBC, OCA and OAB . Prove that

$$\frac{a}{R_1} + \frac{b}{R_2} + \frac{c}{R_3} = \frac{abc}{R_3}$$

[Watch Video Solution](#)

67. In ABC , $C = 60^\circ$ and $B = 45^\circ$. Line joining vertex A of triangle and its circumcenter (O) meets the side BC at D . Find the ratio $BD:DC$. Find the ratio $AO:OD$.

[Watch Video Solution](#)

68. The diameters of the circumcircle of triangle ABC drawn from A,B and C meet BC, CA and AB, respectively, in L,M and N. Prove that

$$\frac{1}{AL} + \frac{1}{BM} + \frac{1}{CN} = \frac{2}{R}$$



Watch Video Solution

69. Find the lengths of chords of the circumcircle of triangle ABC, made by its altitudes



Watch Video Solution

70. Let ABC be a triangle with $\angle B = 90^\circ$. Let AD be the bisector of $\angle A$ with D on BC. Suppose $AC=6\text{cm}$ and the area of the triangle ADC is 10cm^2 . Find the length of BD.



Watch Video Solution

71. If the distances of the vertices of a triangle $\triangle ABC$ from the points of contacts of the incircle with sides are α, β and γ then prove that

$$r^2 = \frac{\alpha\beta\gamma}{\alpha + \beta + \gamma}$$



Watch Video Solution

72. If x, y and z are the distances of incenter from the vertices of the triangle ABC , respectively, then prove that $\frac{abc}{xyz} = \frac{\cot A}{2} \frac{\cot B}{2} \frac{\cot C}{2}$



Watch Video Solution

73. Prove that $\cos A + \cos B + \cos C = 1 + \frac{r}{R}$



Watch Video Solution

74. Prove that $\frac{a \cos A + b \cos B + c \cos C}{a + b + c} = \frac{r}{R}$.



Watch Video Solution

75. Incircle of ABC touches the sides BC , CA and AB at D , E and F , respectively. Let r_1 be the radius of incircle of BDF . Then prove that

$$r_1 = \frac{1}{2} \frac{s(-b)\sin B}{\left(1 + \frac{\sin B}{2}\right)}$$



Watch Video Solution

76. In an acute angle triangle ABC , a semicircle with radius r_a is constructed with its base on BC and tangent to the other two sides AB and AC . r_b and r_c are defined similarly. If r is the radius of the incircle of triangle ABC then prove that

$$\frac{2}{r} = \frac{1}{r_a} + \frac{1}{r_b} + \frac{1}{r_c}$$



Watch Video Solution

77. Let the incircle with center I of ABC touch sides BC , CA and AB at D , E , F , respectively. Let a circle is drawn touching ID , IF and incircle of ABC

having radius r_1 . similarly r_2 and r_3 are defined. Prove that

$$\frac{r_1}{r - r_1} \frac{r_2}{r - r_2} \frac{r_3}{r - r_3} = \frac{a + b + c}{8R}$$



Watch Video Solution

78. In ABC , the bisector of the angle A meets the side BC at D and the

circumscribed circle at E. Prove that $DE = \frac{a^2 \frac{\sec A}{2}}{2(b + c)}$



Watch Video Solution

79. Let I be the incentre of $\triangle ABC$ having inradius r. AI, BI and CI intersect

incircle at D, E and F respectively. Prove that area of

$\triangle DEF$ is $\frac{r^2}{2} \left(\cos. \frac{A}{2} + \cos. \frac{B}{2} + \cos. \frac{C}{2} \right)$



Watch Video Solution

80. In ABC , the three bisectors of the angle A, B and C are extended to

intersect the circumcircle at D, E and F respectively. Prove that

$$AD \frac{\cos A}{2} + BE \frac{\cos B}{2} + CF \frac{\cos C}{2} = 2R(\sin A + \sin B + \sin C)$$



Watch Video Solution

81. Given a right triangle ABC with $\angle A = 90^\circ$. Let D be the mid-point of BC . If the inradii of the triangle ABD and ACD are r_1 and r_2 then find the range of $\frac{r_1}{r_2}$.



Watch Video Solution

82. Prove that the distance between the circumcenter and the incenter of triangle ABC is $\sqrt{R^2 - 2Rr}$



Watch Video Solution

83. Prove that $a \cos A + b \cos B + c \cos C \leq s$.



Watch Video Solution

84. about to only mathematics



Watch Video Solution

85. If in ABC , the distances of the vertices from the orthocentre are x, y , and z , then prove that $\frac{a}{x} + \frac{b}{y} + \frac{c}{z} = \frac{abc}{xyz}$



Watch Video Solution

86. ABC is an acute angled triangle with circumcenter O and orthocentre H . If $AO=AH$, then find the angle A .



Watch Video Solution

87. In a acute angled triangle ABC , point D, E and F are the feet of the perpendiculars from A, B and C onto BC, AC and AB , respectively. H is orthocentre. If $\sin A = \frac{3}{5}$ and $BC = 39$, then find the length of AH

[Watch Video Solution](#)

88. Prove that the distance between the circumcenter and the orthocentre of triangle ABC is $R\sqrt{1 - 8 \cos A \cos B \cos C}$

[Watch Video Solution](#)

89. Let ABC be an acute angled triangle whose orthocentre is at H . If altitude from A is produced to meet the circumcircle of triangle ABC at D , then prove $HD = 4R \cos B \cos C$

[Watch Video Solution](#)

90. In ABC , let L, M, N be the feet of the altitudes. The prove that $\sin(\angle MLN) + \sin(\angle LMN) + \sin(\angle MNL) = 4 \sin A \sin B \sin C$

[Watch Video Solution](#)

91. The lengths of the medians through acute angles of a right-angled triangle are 3 and 4. Find the area of the triangle.

 [Watch Video Solution](#)

92. Two medians drawn from the acute angles of a right angled triangle intersect at an angle $\frac{\pi}{6}$. If the length of the hypotenuse of the triangle is 3units , then the area of the triangle (in sq. units) is $\sqrt{3}$ (b) 3 (c) $\sqrt{2}$ (d) 9

 [Watch Video Solution](#)

93. Prove that $r_1 + r_2 + r_3 - r = 4R$

 [Watch Video Solution](#)

94. If in a triangle $r_1 = r_2 + r_3 + r$, prove that the triangle is right angled.

 [Watch Video Solution](#)

95. Prove that $\frac{r_1 + r_2}{1} = 2R$



Watch Video Solution

96. Prove that

$$(r + r_1)\tan\left(\frac{B - C}{2}\right) + (r + r_2)\tan\left(\frac{C - A}{2}\right) + (r + r_3)\tan\left(\frac{A - B}{2}\right)$$



Watch Video Solution

97. If the distance between incenter and one of the excenter of an equilateral triangle is 4 units, then find the inradius of the triangle.



Watch Video Solution

98. If I_1, I_2, I_3 are the centers of escribed circles of ABC , show that are of $I_1 I_2 I_3 = \frac{abc}{2r}$.

[Watch Video Solution](#)

99. Prove that the sum of the radii of the circles, which are, respectively, inscribed and circumscribed about a polygon of n sides, whose side length is a , is $\frac{1}{2}a \frac{\cot \pi}{2n}$.

[Watch Video Solution](#)

100. If the area of the circle is A_1 and the area of the regular pentagon inscribed in the circle is A_2 , then find the ratio $\frac{A_1}{A_2}$.

[Watch Video Solution](#)

101. Prove that the area of a regular polygon having $2n$ sides, inscribed in a circle, is the geometric mean of the areas of the inscribed and circumscribed polygons of n sides.

[Watch Video Solution](#)

Exercise 5 1

1. Find the value of $\frac{a^2 + b^2 + c^2}{R^2}$ in any right-angled triangle.

 [View Text Solution](#)

2. Let the angles A, B and C of triangle ABC be in AP and let $b:c$ be $\sqrt{3}:\sqrt{2}$. Find angle A .

 [View Text Solution](#)

3. In a triangle ABC , if $(\sqrt{3} - 1)a = 2b$, $A = 3B$, then $\angle C$ is

 [View Text Solution](#)

4. In a triangle ABC , if $\frac{\cos A}{a} = \frac{\cos B}{b} = \frac{\cos C}{c}$ and the side $a = 2$, then area of triangle is

 [View Text Solution](#)

[Watch Video Solution](#)

5. In triangle ABC , if $\cos^2 A + \cos^2 B - \cos^2 C = 1$, then identify the type of the triangle

[Watch Video Solution](#)

6. Prove that $b^2 \cos 2A - a^2 \cos 2B = b^2 - a^2$

[Watch Video Solution](#)

7. In any triangle ABC , prove that following :

$$\frac{c}{a+b} = \frac{1 - \tan\left(\frac{A}{2}\right)\tan\left(\frac{B}{2}\right)}{1 + \tan\left(\frac{A}{2}\right)\tan\left(\frac{B}{2}\right)}$$

[Watch Video Solution](#)

8. For any triangle ABC, prove that

$$(b^2c^2)\cot A + (c^2a^2)\cot B + (a^2b^2)\cot C = 0$$



Watch Video Solution

9. In a triangle ABC, prove that $\frac{b+c}{a} \leq \sec \frac{A}{2}$



Watch Video Solution

10. In any triangle ABC, prove that: $\frac{1 + \cos(A - B)\cos C}{1 + \cos(A - C)\cos B} = \frac{a^2 + b^2}{a^2 + c^2}$



Watch Video Solution

11. In a triangle ABC, if a, b, c are in A.P. and

$$\frac{b}{c}\sin 2C + \frac{c}{b}\sin 2B + \frac{b}{a}\sin 2A + \frac{a}{b}\sin 2B = 2, \text{ then find the value of}$$

$\sin B$



View Text Solution

12. Prove that $a \cos A + b \cos B + c \cos C = 4R \sin A \sin B \sin C$.



Watch Video Solution

Exercise 5 2

1. If the sides of a triangle are a , b and $\sqrt{a^2 + ab + b^2}$, then find the greatest angle



Watch Video Solution

2. If the segments joining the points $A(a, b)$ and $B(c, d)$ subtends an angle θ at the origin, prove that : $\cos \theta = \frac{ac + bd}{\sqrt{(a^2 + b^2)(c^2 + d^2)}}$



Watch Video Solution

3. If $x, y > 0$, then prove that the triangle whose sides are given by $3x + 4y$, $4x + 3y$, and $5x + 5y$ units is obtuse angled.



[View Text Solution](#)

4. In $\triangle ABC$, angle A is 120° , $BC + CA = 20$, and $AB + BC = 21$

Find the length of the side BC



[Watch Video Solution](#)

5. In $\triangle ABC$, $AB = 1$, $BC = 1$, and $AC = 1/\sqrt{2}$. In

$\triangle MNP$, $MN = 1$, $NP = 1$, and $\angle MNP = 2\angle ABC$. Find the side

MP



[Watch Video Solution](#)

6. If in a triangle ABC , $\frac{bc}{2 \cos A} = b^2 + c^2 - 2bc \cos A$ then prove that the triangle must be isosceles



Watch Video Solution

7. With usual notation, if in triangle ABC ,
 $\frac{b+c}{11} = \frac{c+a}{12} = \frac{a+b}{13}$, then prove that $\frac{\cos A}{7} = \frac{\cos B}{19} = \frac{\cos C}{25}$



Watch Video Solution

8. The sides of a triangle are three consecutive natural numbers and its largest angle is twice the smallest one. Determine the sides of the triangle.



View Text Solution

1. In $\triangle ABC$, prove that $c \cos(A - \alpha) + a \cos(C + \alpha) = b \cos \alpha$



Watch Video Solution

2. Prove that $\frac{\cos C + \cos A}{c + a} + \frac{\cos B}{b} = \frac{1}{b}$



Watch Video Solution

3. Prove that

$$a(b^2 + c^2) \cos A + b(c^2 + a^2) \cos B + c(a^2 + b^2) \cos C = 3abc$$



View Text Solution

Exercise 5 4

1. In a triangle ABC if $b + c = 3a$ then find the value of

$$\cot\left(\frac{B}{2}\right) \cot\left(\frac{C}{2}\right)$$



Watch Video Solution

2. Prove that $bc \cos^2 \frac{A}{2} + ca \cos^2 \frac{B}{2} + ab \cos^2 \frac{C}{2} = s^2$



Watch Video Solution

3. If in $\triangle ABC$, $\tan \frac{A}{2} = \frac{5}{6}$ and $\tan \frac{C}{2} = \frac{2}{5}$, then prove that a , b , and c are in A.P.



View Text Solution

4. Prove that $(b + c - a) \left(\cot \frac{B}{2} + \cot \frac{C}{2} \right) = 2a \cot \frac{A}{2}$



Watch Video Solution

5. If $\sin^2 \left(\frac{A}{2} \right)$, $\sin^2 \left(\frac{B}{2} \right)$, and $\sin^2 \left(\frac{C}{2} \right)$ are in $H. P.$, then prove that the sides of triangle are in $H. P.$



Watch Video Solution

Exercise 5 5

1. If $c^2 = a^2 + b^2$, then prove that $4s(s - a)(s - b)(s - c) = a^2b^2$



Watch Video Solution

2. If the sides of a triangle are in the ratio 3 : 7 : 8, then find $R : r$



Watch Video Solution

3. In triangle ABC, if $a = 2$ and $bc = 9$, then prove that $R = 9/2\Delta$



Watch Video Solution

4. In $\triangle ABC$, if lengths of medians BE and CF are 12 and 9 respectively, find the maximum value of Δ



Watch Video Solution

5. Let the lengths of the altitudes drawn from the vertices of $\triangle ABC$ to the opposite sides are 2, 2 and 3. If the area of $\triangle ABC$ is Δ , then find the area of triangle



Watch Video Solution

6. A triangle with integral sides has perimeter 8 cm. Then find the area of the triangle



Watch Video Solution

7. The sides of a triangle are in A.P. and its area is $\frac{3}{5}$ th of the area of an equilateral triangle of the same perimeter, prove that its sides are in the ratio 3:5:7



Watch Video Solution

Exercise 5.6

1. In which of the following cases, there exists a triangle ABC?

(a) $b \sin A = a, A < \pi/2$

(b) $b \sin A > a, A > \pi/2$

(c) $b \sin A > a, A < \pi/2$

(d) $b \sin A < a, A < \pi/2, b > a$

(e) $b \sin A < a, A > \pi/2, b = a$



View Text Solution

2. If in $\triangle ABC$, $b = 3\text{cm}$, $c = 4\text{cm}$ and the length of the perpendicular from A to the side BC is 2 cm, then how many such triangle are possible ?



Watch Video Solution

3. In a triangle ABC , $\frac{a}{b} = \frac{2}{3}$ and $\sec^2 A = \frac{8}{5}$. Find the number of triangle satisfying these conditions



Watch Video Solution

4. In a triangle, the lengths of the two larger sides are 10 and 9, respectively. If the angles are in A.P., then the length of the third side can be $5 - \sqrt{6}$ (b) $3\sqrt{3}$ (c) 5 (d) $5 + \sqrt{6}$



View Text Solution

5. If a, b and A are given in a triangle and c_1, c_2 are possible values of the third side, then prove that $c_1^2 + c_2^2 - 2c_1c_2 \cos 2A = 4a^2 \cos^2 A$



[View Text Solution](#)

6. In $\triangle ABC$, a, b and A are given and c_1, c_2 are two values of the third side c . Prove that the sum of the area of two triangles with sides a, b, c_1 and a, b, c_2 is $\frac{1}{2}b^2 \sin 2A$



[View Text Solution](#)

Exercise 5.7

1. Let f, g and h be the lengths of the perpendiculars from the circumcenter of $\triangle ABC$ on the sides a, b , and c , respectively. Prove that

$$\frac{a}{f} + \frac{b}{g} + \frac{c}{h} = \frac{1}{4} \frac{abc}{fgh}$$



[Watch Video Solution](#)

2. If AD, BE, CF are the diameters of circumcircle of $\triangle ABC$, then prove that area of hexagon AFB DCE is 2Δ



[Watch Video Solution](#)

3. If the sides of triangle are in the ratio 3:5:7, then prove that the minimum distance of the circumcentre from the side of triangle is half the circumradius



[Watch Video Solution](#)

4. If circumradius of triangle ABC is 4 cm, then prove that sum of perpendicular distances from circumcentre to the sides of triangle cannot exceed 6 cm



[Watch Video Solution](#)

Exercise 5 8

1. If the incircle of the triangle ABC passes through its circumcenter, then

find the value of $4 \sin. \frac{A}{2} \sin. \frac{B}{2} \sin. \frac{C}{2}$



Watch Video Solution

2. In $\triangle ABC$, $a = 10$, $A = \frac{2\pi}{3}$, and circle through B and C passes through the incenter. Find the radius of this circle



Watch Video Solution

3. Let ABC be a triangle with $\angle BAC = 2\pi/3$ and $AB = x$ such that $(AB)(AC) = 1$. If x varies, then find the longest possible length of the angle bisector AD



Watch Video Solution

4. If the incircle of the $\triangle ABC$ touches its sides at L, M and N as shown in the figure and if x, y, z be the circumradii of the triangles MIN, NIL and LIM respectively, where I is the incentre, then the product xyz is equal to:

- (A) Rr^2 (B) rR^2
 (C) $\frac{1}{2}Rr^2$ (D) $\frac{1}{2}rR^2$

 [Watch Video Solution](#)

5. In a triangle ABC , CD is the bisector of the angle C . If $\cos\left(\frac{C}{2}\right)$ has the value $\frac{1}{3}$ and $1(CD) = 6$, then $\left(\frac{1}{a} + \frac{1}{b}\right)$ has the value equal to -

 [Watch Video Solution](#)

6. In $\triangle ABC$, $\angle A = \frac{\pi}{3}$ and its inradius of 6 units. Find the radius of the circle touching the sides AB, AC internally and the incircle of $\triangle ABC$ externally



 [Watch Video Solution](#)

7. In triangle ABC, prove that the maximum value of $\tan\left(\frac{A}{2}\right)\tan\left(\frac{B}{2}\right)\tan\left(\frac{C}{2}\right)$ is $\frac{R}{2s}$



[Watch Video Solution](#)

Exercise 5 9

1. Line joining vertex A of triangle ABC and orthocenter (H) meets the side BC in D. Then prove that

(a) $BD:DC = \tan C:\tan B$

(b) $AH:HD = (\tan B + \tan C):\tan A$



[Watch Video Solution](#)

2. In a triangle ABC, $\angle A = 30^\circ$, $BC = 2 + \sqrt{5}$, then find the distance of the vertex A from the orthocenter

[Watch Video Solution](#)

3. If the perimeter of the triangle formed by feet of altitudes of the triangle ABC is equal to four times the circumradius of $\triangle ABC$, then identify the type of $\triangle ABC$

[Watch Video Solution](#)

4. AD, BE and CF are the medians of triangle ABC whose centroid is G. If the points A, F, G and E are concyclic, then prove that $2a^2 = b^2 + c^2$

[Watch Video Solution](#)

5. In an acute angle triangle ABC, AD, BE and CF are the altitudes, then

$\frac{EF}{a} + \frac{FD}{b} + \frac{DE}{c}$ is equal to -

[Watch Video Solution](#)

Exercise 5 10

1. In $\triangle ABC$, if $r_1 < r_2 < r_3$, then find the order of lengths of the sides



Watch Video Solution

2. The exradii r_1, r_2 and r_3 of ABC are in H.P. Show that its sides a, b and c are in A.P.



Watch Video Solution

3. If in $\triangle ABC$, $(a - b)(s - c) = (b - c)(s - a)$, prove that r_1, r_2, r_3 are in A.P.



Watch Video Solution

4. Prove that $2R \cos A = 2R + r - r_1$



Watch Video Solution

5. If the lengths of the perpendiculars from the vertices of a triangle ABC on the opposite sides are p_1, p_2, p_3 then prove that

$$\frac{1}{p_1} + \frac{1}{p_2} + \frac{1}{p_3} = \frac{1}{r} = \frac{1}{r_1} + \frac{1}{r_2} + \frac{1}{r_3}.$$



Watch Video Solution

6. Prove that $\frac{1}{r^2} + \frac{1}{r_1^2} + \frac{1}{r_2^2} + \frac{1}{r_3^2} = \frac{a^2 + b^2 + c^2}{S^2}$



Watch Video Solution

7. In any triangle ABC, find the least value of $\frac{r_1 + r_2 + r_3}{r}$



Watch Video Solution

8. Prove that $\frac{r_1 - r}{a} + \frac{r_2 - r}{b} = \frac{c}{r_3}$



Watch Video Solution

Exercise 5 11

1. Regular pentagons are inscribed in two circles of radius 5 and 2 units respectively. The ratio of their areas is



Watch Video Solution

2. Let A be a point inside a regular polygon of 10 sides. Let p_1, p_2, \dots, p_{10} be the distances of A from the sides of the polygon. If each side is of length 2 units, then find the value of $p_1 + p_2 + \dots + p_{10}$



Watch Video Solution

3. about to only mathematics



Watch Video Solution

4. If I_n is the area of n – sided regular polygon inscribed in a circle of unit radius and O_n be the area of the polygon circumscribing the given circle, prove that $I_n = \frac{O_n}{2} \left(\sqrt{1 + \left(\frac{2I_n}{n} \right)^2} \right)$



Watch Video Solution

Exercise Single

1. In ΔABC , $\frac{\sin A(a - b \cos C)}{\sin C(c - b \cos A)} =$

A. -2

B. -1

C. 0

D. 1

Answer: D



Watch Video Solution

2. If in a triangle ABC,

$$\frac{1 + \cos A}{a} + \frac{1 + \cos B}{b} + \frac{1 + \cos C}{c} = \frac{k^2(1 + \cos A)(1 + \cos B)(1 + \cos C)}{abc}$$

, then k is equal to

A. $\frac{1}{2\sqrt{2}R}$

B. $2R$

C. $\frac{1}{R}$

D. none of these

Answer: B



Watch Video Solution

3. In triangle ABC, $2ac \sin\left(\frac{1}{2}(A - B + C)\right)$ is equal to $a^2 + b^2 - c^2$

(b) $c^2 + a^2 - b^2$ (c) $b^2 - c^2 - a^2$ (d) $c^2 - a^2 - b^2$

A. $a^2 + b^2 - c^2$

B. $c^2 + a^2 - b^2$

C. $b^2 - c^2 - a^2$

D. $c^2 - a^2 - b^2$

Answer: B



Watch Video Solution

4. If the angles of triangle are in the ratio 4 :1:1 , then the ratio of the longest side to the perimeter is

A. $\sqrt{3} : (2 + \sqrt{3})$

B. 1 : 6

C. $1 : 2 + \sqrt{3}$

D. 2 : 3

Answer: A



Watch Video Solution

5. Which of the following pieces of data does NOT uniquely determine an acute-angled triangle ABC (R being the radius of the circumcircle)?

(a) $a, \sin A, \sin B$ (b) a, b, c (c) $a, \sin B, R$ (d) $a, \sin A, R$

A. $a, \sin A, \sin B$

B. a, b, c

C. $a, \sin B, R$

D. $a, \sin A, R$

Answer: D



Watch Video Solution

6. The sides of a triangle are in the ratio $1 : \sqrt{3} : 2$. Then the angles are in the ratio

A. $1 : 3 : 5$

B. 2:3:4

C. 3:2:1

D. 1:2:3

Answer: D



Watch Video Solution

7. In ABC , $a = 5$, $b = 12$, $c = 90^\circ$ and D is a point on AB so that $\angle BCD = 45^\circ$. Then which of the following is not true? $CD = \frac{60\sqrt{2}}{17}$ (b)

$BD = \frac{65}{17}$ $AD = \frac{60\sqrt{2}}{17}$ (d) none of these

A. $CD = \frac{60\sqrt{2}}{17}$

B. $BD = \frac{65}{17}$

C. $AD = \frac{60\sqrt{2}}{17}$

D. none of these

Answer: C

[Watch Video Solution](#)

8. In $\triangle ABC$, $(a + b + c)(b + c - a) = kbc$ if

A. $k < 0$

B. $k > 0$

C. $0 < k < 4$

D. $k < 4$

Answer: C

[Watch Video Solution](#)

9. Let D be the middle point of the side BC of a triangle ABC . If the triangle ADC is equilateral, then $a^2 : b^2 : c^2$ is equal to 1:4:3 (b) 4:1:3 (c) 4:3:1 (d) 3:4:1

A. 1:4:3

B. 4: 1: 3

C. 4: 3: 1

D. 3: 4: 1

Answer: B



Watch Video Solution

10. In a triangle ABC , the altitude from A is not less than BC and the altitude from B is not less than AC . The triangle is right angled (b) isosceles obtuse angled (d) equilateral

A. right angled

B. isosceles

C. obtuse angled

D. equilateral

Answer: A

[Watch Video Solution](#)

11. In $\triangle ABC$, if $\frac{\sin A}{c \sin B} + \frac{\sin B}{c} + \frac{\sin C}{b} = \frac{c}{ab} + \frac{b}{ac} + \frac{a}{bc}$, then the value of angle A is

A. 120°

B. 90°

C. 60°

D. 30°

Answer: B

[Watch Video Solution](#)

12. If in ABC , side a, b, c are in A.P. then $B > 60^\circ$ (b) $B < 60^\circ$ $B \leq 60^\circ$
(d) $B = |A - C|$

A. $B > 60^\circ$

B. $B < 60^\circ$

C. $B \leq 60^\circ$

D. $B = |A - C|$

Answer: C



Watch Video Solution

13. In triangle ABC , AD is the altitude from A . If $b > c$, $\angle C = 23^\circ$, and $AD = \frac{abc}{b^2 - c^2}$, then $\angle B = _ _$

A. 83°

B. 97°

C. 113°

D. 127°

Answer: C



Watch Video Solution

14. If the sides a, b, c of a triangle ABC form successive terms of G.P. with common ratio $r (> 1)$ then which of the following is correct? $A > \frac{\pi}{3}$ (b)

$B \geq \frac{\pi}{3}$ (d) `A

A. $A > \pi/3$

B. $B \geq \pi/3$

C. $C < \pi/3$

D. $A < B < \pi/3$

Answer: D



Watch Video Solution

15. In triangle ABC , $b^2 \sin 2C + c^2 \sin 2B = 2bc$ where $b = 20, c = 21$, then inradius = (a) 4 (b) 6 (c) 8 (d) 9

A. 4

B. 6

C. 8

D. 9

Answer: B



Watch Video Solution

16. In a ABC , if $AB = x$, $BC = x + 1$, $\angle C = \frac{\pi}{3}$, then the least integer value of x is 6 (b) 7 (c) 8 (d) none of these

A. 6

B. 7

C. 8

D. none of these

Answer: B



Watch Video Solution

17. If one side of a triangle is double the other, and the angles on opposite sides differ by 60^0 , then the triangle is equilateral (b) obtuse angled (c) right angled (d) acute angled

A. equilateral

B. obtus angled

C. right angled

D. acute angled

Answer: C



Watch Video Solution

18. If the hypotenuse of a right-angled triangle is four times the length of the perpendicular drawn from the opposite vertex to it, then the difference of the two acute angles will be 60^0 (b) 15^0 (c) 75^0 (d) 30^0

A. 60°

B. 15°

C. 75°

D. 30°

Answer: A



Watch Video Solution

19. If P is a point on the altitude AD of the triangle ABC such the $\angle CBP = \frac{B}{3}$, then AP is equal to $2a \frac{\sin C}{3}$ (b) $2b \frac{\sin C}{3}$ $2c \frac{\sin B}{3}$ (d) $2c \frac{\sin C}{3}$

A. $2a \sin. \frac{C}{3}$

B. $2b \sin. \frac{C}{3}$

C. $2c \sin. \frac{B}{3}$

D. $2c \sin. \frac{C}{3}$

Answer: C



Watch Video Solution

20. With usual notations, in triangle

ABC , $a \cos(B - C) + b \cos(C - A) + c \cos(A - B)$ is equal to abc/R^2

(b) $\frac{abc}{4R^2}$ $\frac{4abc}{R^2}$ (d) $\frac{abc}{2R^2}$

A. $\frac{abc}{R^2}$

B. $\frac{abc}{4R^2}$

C. $\frac{4abc}{R^2}$

D. $\frac{abc}{2R^2}$

Answer: A



Watch Video Solution

21. If in $\triangle ABC$, $8R^2 = a^2 + b^2 + c^2$, then the triangle ABC is

- A. right angled
- B. isosceles
- C. equilateral
- D. none of these

Answer: A



Watch Video Solution

22. Let ABC be a triangle with $\angle A = 45^\circ$. Let P be a point on side BC with PB=3 and PC=5. If O is circumcenter of triangle ABC, then length OP is $\sqrt{18}$
(b) $\sqrt{17}$ (c) $\sqrt{19}$ (d) $\sqrt{15}$

- A. $\sqrt{18}$
- B. $\sqrt{17}$
- C. $\sqrt{19}$
- D. $\sqrt{15}$

Answer: B



Watch Video Solution

23. In any triangle ABC , $\frac{a^2 + b^2 + c^2}{R^2}$ has the maximum value of (a) 3
(b) 6 (c) 9 (d) none of these

A. 3

B. 6

C. 9

D. none of these

Answer: C



Watch Video Solution

24. In triangle ABC , $R(b + c) = a\sqrt{bc}$, where R is the circumradius of the triangle. Then the triangle is isosceles but not right or right but not

isosceles right isosceles equilateral

A. isosceles but not right

B. right but not isosceles

C. right isosceles

D. equilateral

Answer: C



Watch Video Solution

25. In ABC , if $b^2 + c^2 = 2a^2$, then value of $\frac{\cot A}{\cot B + \cot C}$ is $\frac{1}{2}$ (b) $\frac{3}{2}$

(c) $\frac{5}{2}$ (d) $\frac{5}{2}$

A. $\frac{1}{2}$

B. $\frac{3}{2}$

C. $\frac{5}{2}$

D. $\frac{5}{3}$

Answer: A



Watch Video Solution

26. If $\sin \theta$ and $-\cos \theta$ are the roots of the equation $ax^2 - bx - c = 0$, where a, b and c are the sides of a triangle ABC, then $\cos B$ is equal to

$1 - \frac{c}{2a}$ (b) $1 - \frac{c}{a}$ $1 + \frac{c}{ca}$ (d) $1 + \frac{c}{3a}$

A. $1 - \frac{c}{2a}$

B. $1 - \frac{c}{a}$

C. $1 + \frac{c}{2a}$

D. $1 + \frac{c}{3a}$

Answer: C



Watch Video Solution

27. If D is the mid-point of the side BC of triangle ABC and AD is perpendicular to AC , then (a) $3b^2 = a^2 - c^2$ (b) $3a^2 = b^2 + 3c^2$ (c) $b^2 = a^2 - c^2$ (d) $a^2 + b^2 = 5c^2$

A. $3b^2 = a^2 - c^2$

B. $3a^2 = b^2 - 3c^2$

C. $b^2 = a^2 - c^2$

D. $a^2 + b^2 = 5c^2$

Answer: A



Watch Video Solution

28. In a triangle ABC , if $\cot A : \cot B : \cot C = 30 : 19 : 6$ then the sides a, b, c are

A. in A.P.

B. in G.P.

C. in H.P.

D. none of these

Answer: A



Watch Video Solution

29. In ABC , P is an interior point such that $\angle PAB = 10^\circ$, $\angle PBA = 20^\circ$, $\angle PCA = 30^\circ$, $\angle PAC = 40^\circ$ then ABC is isosceles (b) right angled equilateral (d) obtuse angled

A. isosceles

B. right angled

C. equilateral

D. obtuse angled

Answer: A



Watch Video Solution

30. In $\triangle ABC$, if $AB = c$ is fixed, and $\cos A + \cos B + 2\cos C = 2$ then the locus of vertex C is

- A. ellipse
- B. hyperbola
- C. circle
- D. parabola

Answer: A



Watch Video Solution

31. If in ABC , $A = \frac{\pi}{7}$, $B = \frac{2\pi}{7}$, $C = \frac{4\pi}{7}$ then $a^2 + b^2 + c^2$ must be

- A. R^2
- B. $3R^2$
- C. $4R^2$

D. $7R^2$

Answer: D



Watch Video Solution

32. In $\triangle ABC$, $\cot \frac{A}{2} + \cot \frac{B}{2} + \cot \frac{C}{2}$ is equal to

A. $\frac{\Delta}{r^2}$

B. $\frac{(a+b+c)^2}{abc} 2R$

C. $\frac{\Delta}{r}$

D. $\frac{\Delta}{Rr}$

Answer: A



Watch Video Solution

33. In $\triangle ABC$, $\left(\cot \frac{A}{2} + \cot \frac{B}{2} \right) \left(a \frac{\sin^2(B)}{2} + b \frac{\sin^2(A)}{2} \right) =$

A. $\cot C$

B. $c \cot C$

C. $\cot. \frac{C}{2}$

D. $c \cot. \frac{C}{2}$

Answer: D



Watch Video Solution

34. In a right-angled isosceles triangle, the ratio of the circumradius and inradius is $2(\sqrt{2} + 1) : 1$ (b) $(\sqrt{2} + 1) : 1$ 2 : 1 (d) $\sqrt{2} : 1$

A. $2(\sqrt{2} + 1) : 1$

B. $(\sqrt{2} + 1) : 1$

C. 2 : 1

D. $\sqrt{2} : 1$

Answer: B



Watch Video Solution

35. In the given figure, what is the radius of the inscribed semicircle having base on AB ?



A. $3/2$

B. $5/2$

C. $7/5$

D. none of these

Answer: A



Watch Video Solution

36. In $\triangle ABC$, $A = \frac{2\pi}{3}$, $b - c = 3\sqrt{3} \text{ cm}$ and area of $\triangle ABC = \frac{9\sqrt{3}}{2} \text{ cm}^2$, then (a) 9 cm (b) 18 cm (c) 27 cm

A. $6\sqrt{3}cm$

B. 9 cm

C. 18 cm

D. 27 cm

Answer: B



Watch Video Solution

37. In triangle ABC , let $\angle C = \frac{\pi}{2}$. If r is the inradius and R is circumradius of the triangle, then $2(r + R)$ is equal to (a) $a + b$ (b) $b + c$ (c) $c + a$ (d) $a + b + c$

A. $a + b$

B. $b + c$

C. $c + a$

D. $a + b + c$

Answer: A



Watch Video Solution

38. In the given figure, AB is the diameter of the circle, centered at O . If $\angle COA = 60^\circ$, $AB = 2r$, $AC = d$, and $CD = l$, then l is equal to



A. $d\sqrt{3}$

B. $d / \sqrt{3}$

C. $3d$

D. $\sqrt{3}d / 2$

Answer: A



Watch Video Solution

39. In triangle ABC, if P, Q, R divides sides BC, AC, and AB, respectively, in the ratio $k:1$ (in order). If the ratio $\left(\frac{\text{area } \Delta PQR}{\text{area } \Delta ABC}\right)$ is $\frac{1}{3}$, then k is equal to

- A. $1/3$
- B. 2
- C. 3
- D. none of these

Answer: B



Watch Video Solution

40. If the angles of a triangle are 30° and 45° and the included side is $(\sqrt{3} + 1) \text{ cm}$ then the area of the triangle is _____.

- A. $\frac{\sqrt{3} + 1}{2}$ sq. units
- B. $(\sqrt{3} + 1)$ sq. units

C. $2(\sqrt{3} - 1)$ sq. units

D. $\frac{2\sqrt{3} - 1}{2}$ sq. units

Answer: A



Watch Video Solution

41. In triangle ABC , base BC and area of triangle are fixed. The locus of the centroid of triangle ABC is a straight line that is parallel to side BC right bisector of side BC perpendicular to BC inclined at an angle $\sin^{-1}\left(\frac{\sqrt{\Delta}}{BC}\right)$ to side BC

A. parallel to side BC

B. right bisector of side BC

C. perpendicular to BC

D. inclined at an angle $\sin^{-1}(\sqrt{\Delta}/BC)$ to side BC

Answer: A

[Watch Video Solution](#)

42. Let the area of triangle ABC be $(\sqrt{3} - 1)/2$, $b = 2$ and $c = (\sqrt{3} - 1)$, and $\angle A$ be acute. The measure of the angle C is

A. 15°

B. 30°

C. 60°

D. 75°

Answer: A

[Watch Video Solution](#)

43. In $\triangle ABC$, $\Delta = 6$, $abc = 60$, $r = 1$ Then the value of $\frac{1}{a} + \frac{1}{b} + \frac{1}{c}$ is nearly (a) 0.5 (b) 0.6 (c) 0.4 (d) 0.8

A. 0.5

B. 0.6

C. 0.4

D. 0.8

Answer: D



Watch Video Solution

44. Triangle ABC is isosceles with $AB = AC$ and $BC = 65\text{cm}$. P is a point on BC such that the perpendicular distances from P to AB and AC are 24cm and 36cm , respectively. The area of triangle ABC (in sq cm is)

A. 1254

B. 1950

C. 2535

D. 5070

Answer: C



Watch Video Solution

45. In an equilateral triangle, the inradius, circumradius, and one of the exradii are in the ratio a) 2:4:5 (b) 1:2:3 (c) 1:2:4 (d) 2:4:3

A. 2:4:5

B. 1:2:3

C. 1:2:4

D. 2:4:3

Answer: B



Watch Video Solution

46. In triangle ABC , if $\cos A + \cos B + \cos C = \frac{7}{4}$, then $\frac{R}{r}$ is equal to $\frac{3}{4}$ (b) $\frac{4}{3}$ (c) $\frac{2}{3}$ (d) $\frac{3}{2}$

A. $\frac{3}{4}$

B. $\frac{4}{3}$

C. $\frac{2}{3}$

D. $\frac{3}{2}$

Answer: B



Watch Video Solution

47. If two sides of a triangle are roots of the equation $x^2 - 7x + 8 = 0$ and the angle between these sides is 60° then the product of inradius and circumradius of the triangle is $\frac{8}{7}$ (b) $\frac{5}{3}$ (c) $\frac{5\sqrt{2}}{3}$ (d) 8

A. $\frac{8}{7}$

B. $\frac{5}{3}$

C. $\frac{5\sqrt{2}}{3}$

D. 8

Answer: B



Watch Video Solution

48. Given $b = 2$, $c = \sqrt{3}$, $\angle A = 30^\circ$, then inradius of ABC is $\frac{\sqrt{3} - 1}{2}$

(b) $\frac{\sqrt{3} + 1}{2}$ (c) $\frac{\sqrt{3} - 1}{4}$ (d) *none of these*

A. $\frac{\sqrt{3} - 1}{2}$

B. $\frac{\sqrt{3} + 1}{2}$

C. $\frac{\sqrt{3} - 1}{4}$

D. none of these

Answer: A



Watch Video Solution

49. In triangle ABC , if $A - B = 120^\circ$ and $R = 8r$, where R and r have their usual meanings, then $\cos C$ equal $\frac{3}{4}$ (b) $\frac{2}{3}$ (c) $\frac{5}{6}$ (d) $\frac{7}{8}$

A. $\frac{3}{4}$

B. $\frac{2}{3}$

C. $\frac{5}{6}$

D. $\frac{7}{8}$

Answer: D



Watch Video Solution

50. ABC is an equilateral triangle of side 4cm . If R, r and h are the circumradius, inradius, and altitude, respectively, then $\frac{R + h}{h}$ is equal to 4 (b) 2 (c) 1 (d) 3

A. 4

B. 2

C. 1

D. 3

Answer: C



Watch Video Solution

51. A circle is inscribed in a triangle ABC touching the side AB at D such that $AD = 5$, $BD = 3$, if $\angle A = 60^\circ$ then length BC equals. 9

(b) $\frac{120}{13}$ (c) 13 (d) 12

A. 9

B. $\frac{120}{13}$

C. 13

D. 12

Answer: C



Watch Video Solution

52. The rational number which equals the number $\overline{2.357}$ with recurring decimal is a. $\frac{2355}{1001}$ b. $\frac{2379}{997}$ c. $\frac{2355}{999}$ d. none of these



Watch Video Solution

53. Let AD be a median of the ABC . If AE and AF are medians of the triangle ABD and ADC , respectively, and $AD = m_1$, $AE = m_2$, $AF = m_3$, then $\frac{a^2}{8}$ is equal to $m_1^2 + m_3^2 - 2m_2^2$, $m_1^2 + m_2^2 - 2m_3^2$, $m_1^2 + m_3^2 - 2m_2^2$, none of these

A. $m_2^2 + m_3^2 - 2m_1^2$

B. $m_1^2 + m_2^2 - 2m_3^2$

C. $m_1^2 + m_3^2 - 2m_2^2$

D. none of these

Answer: A



Watch Video Solution

54. For a triangle ABC , $R = \frac{5}{2}$ and $r = 1$. Let D, E and F be the feet of the perpendiculars from incentre I to BC, CA and AB, respectively. Then the value of $\frac{(IA)(IB)(IC)}{(ID)(IE)(IF)}$ is equal to ____

A. $\frac{5}{2}$

B. $\frac{5}{4}$

C. $\frac{1}{10}$

D. $\frac{1}{5}$

Answer: C



Watch Video Solution

55. In triangle ABC , $\angle A = 60^\circ$, $\angle B = 40^\circ$, and $\angle C = 80^\circ$. If P is the center of the circumcircle of triangle ABC with radius unity, then the radius of the circumcircle of triangle BPC is 1 (b) $\sqrt{3}$ (c) 2 (d) $\sqrt{3} 2$

A. 1

B. $\sqrt{3}$

C. 2

D. $\sqrt{3}/2$

Answer: A



Watch Video Solution

56. If H is the orthocenter of an acute angled triangle ABC whose circumcircle is $x^2 + y^2 = 16$, then circumdiameter of the triangle HBC is
(a) 1 (b) 2 (c) 4 (d) 8

A. 1

B. 2

C. 4

D. 8

Answer: D



Watch Video Solution

57. In triangle ABC, the line joining the circumcenter and incenter is parallel to side AC, then $\cos A + \cos C$ is equal to -1 (b) 1 (c) -2 (d) 2

A. $\frac{1}{2}$

B. 1

C. $\sqrt{3}$

D. 2

Answer: B



Watch Video Solution

58. In triangle ABC, line joining the circumcenter and orthocentre is parallel to side AC, then the value of $\tan A \tan C$ is equal to $\sqrt{3}$ (b) 3 (c)

$3\sqrt{3}$ (d) none of these

A. $\sqrt{3}$

B. 3

C. $3\sqrt{3}$

D. none of these

Answer: B



Watch Video Solution

59. In triangle ABC , $\angle C = \frac{2\pi}{3}$ and CD is the internal angle bisector of $\angle C$, meeting the side AB at D . If Length CD is 1, the H.M. of a and b is equal to: 1 (b) 2 (c) 3 (d) 4

A. 1

B. 2

C. 3

D. 4

Answer: B



Watch Video Solution

60. In the given figure $\triangle ABC$ is equilateral on side AB produced. We choose a point such that A lies between P and B. We now denote 'a' as the length of sides of $\triangle ABC$, r_1 as the radius of incircle $\triangle PAC$ and r_2 as the ex-radius of $\triangle PBC$ with respect to side BC. Then $r_1 + r_2$ is equal to

A. $\frac{1}{2}$

B. $\frac{3}{2}a$

C. $\frac{\sqrt{3}}{2}a$

D. $a\sqrt{2}$

Answer: C



View Text Solution

61. A variable triangle ABC is circumscribed about a fixed circle of unit radius. Side BC always touches the circle at D and has fixed direction. If B and C vary in such a way that $(BD)(CD)=2$, then locus of vertex A will be a straight line. a)parallel to side BC b)perpendicular to side BC c)making an angle $\left(\frac{\pi}{6}\right)$ with BC d)making an angle $\sin^{-1}\left(\frac{2}{3}\right)$ with BC

A. parallel to side BC

B. perpendicular to side BC

C. making an angle $(\pi/6)$ with BC

D. making an angle $\sin^{-1}(2/3)$ with BC

Answer: A



Watch Video Solution

62. In ABC , if $a = 10$ and $b \cot B + c \cot C = 2(r + R)$ then the maximum area of ABC will be (a) 50 (b) $\sqrt{50}$ (c) 25 (d) 5

A. 50

B. $\sqrt{50}$

C. 25

D. 5

Answer: C



Watch Video Solution

63. Let C be incircle of ABC . If the tangents of lengths t_1, t_2 and t_3 are drawn inside the given triangle parallel to sides a, b and c , respectively, the $\frac{t_1}{a} + \frac{t_2}{b} + \frac{t_3}{c}$ is equal to 0 (b) 1 (c) 2 (d) 3

A. 0

B. 1

C. 2

D. 3

Answer: B



Watch Video Solution

64. A park is in the form of a rectangle $120m \times 100m$. At the centre of the park there is a circular lawn. The area of park excluding lawn is $8700m^2$. Find the radius of the circular lawn. $\left(Use \pi \frac{22}{7}\right)$



Watch Video Solution

65. In triangle ABC, if $r_1 = 2r_2 = 3r_3$, then $a : b$ is equal to

A. $\frac{5}{4}$

B. $\frac{4}{5}$

C. $\frac{7}{4}$

D. $\frac{4}{7}$

Answer: A

[Watch Video Solution](#)

66. If in a triangle $\left(1 - \frac{r_1}{r_2}\right)\left(1 - \frac{r_1}{r_3}\right) = 2$ then the triangle is right angled (b) isosceles equilateral (d) none of these

- A. right angled
- B. isosceles
- C. equilateral
- D. none of these

Answer: A

[Watch Video Solution](#)

67. If in a triangle $\frac{r}{r_1} = \frac{r_2}{r_3}$, then

- A. $A = 90^\circ$
- B. $B = 90^\circ$

C. $C = 90^\circ$

D. none of these

Answer: C



Watch Video Solution

68. In $\triangle ABC$, I is the incentre, Area of $\triangle IBC$, $\triangle IAC$ and $\triangle IAB$ are, respectively, Δ_1 , Δ_2 and Δ_3 . If the values of Δ_1 , Δ_2 and Δ_3 are in A.P., then the altitudes of the $\triangle ABC$ are in

A. A.P.

B. G.P.

C. H.P.

D. none of these

Answer: C



Watch Video Solution

69. In an acute angled triangle ABC , $r + r_1 = r_2 + r_3$ and $\angle B > \frac{\pi}{3}$, then

$$b + 2c < 2a < 2b + 2c$$

$$b + 4c < 4a < 2b + 4c$$

$$b + 4c < 4a < 4b + 4c \quad b + 3c < 3a < 3b + 3c$$

A. $b + 2c < 2a < 2b + 2c$

B. $b + 4 < 4a < 2b + 4c$

C. $b + 4c < 4a < 4b + 4c$

D. $b + 3c < 3a < 3b + 3c$

Answer: D



Watch Video Solution

70. If in triangle ABC , $\sum \frac{\sin A}{2} = \frac{6}{5}$ and $\sum II_1 = 9$ (where

I_1, I_2 and I_3 are excenters and I is incenter, then circumradius R is equal

to $\frac{15}{8}$ (b) $\frac{15}{4}$ (c) $\frac{15}{2}$ (d) $\frac{4}{12}$

A. $\frac{15}{8}$

B. $\frac{15}{4}$

C. $\frac{15}{2}$

D. $\frac{4}{12}$

Answer: A



Watch Video Solution

71. The radii r_1, r_2, r_3 of the escribed circles of the triangle ABC are in H.P. If the area of the triangle is 24cm^2 and its perimeter is 24cm, then the length of its largest side is 10 (b) 9 (c) 8 (d) none of these

A. 10

B. 9

C. 8

D. none of these

Answer: A

[Watch Video Solution](#)

72. In ABC with usual notations, if $r = 1$, $r_1 = 7$ and $R = 3$, the ABC is (a) equilateral (b) acute angled which is not equilateral (c) obtuse angled (d) right angled

A. equilateral

B. acute angled which is not equilateral

C. obtuse angled

D. right angled

Answer: D

[Watch Video Solution](#)

73. Which of the following expresses the circumference of a circle inscribed in a sector OAB with radius R and $AB = 2a$? (a) $2\pi \frac{Ra}{R+a}$ (b) $\frac{2\pi R^2}{a}$ (c) $2\pi(r-a)^2$ (d) $2\pi \frac{R}{R-a}$

A. $2\pi \frac{Ra}{R+a}$

B. $\frac{2\pi R^2}{a}$

C. $2\pi(R-a)^2$

D. $2\pi \frac{R}{R-a}$

Answer: A



Watch Video Solution

74. In ABC , the median AD divides $\angle BAC$ such that $\angle BAD : \angle CAD = 2 : 1$. Then $\cos\left(\frac{A}{3}\right)$ is equal to $\frac{\sin B}{2\sin C}$ (b) $\frac{\sin C}{2\sin B}$ $\frac{2\sin B}{\sin C}$ (d) *none of these*

A. $\frac{\sin B}{2\sin C}$

B. $\frac{\sin C}{2\sin B}$

C. $\frac{2\sin B}{\sin C}$

D. none of these

Answer: A



Watch Video Solution

75. The area of the circle and the area of a regular polygon of n sides and of perimeter equal to that of the circle are in the ratio of (a) $\tan\left(\frac{\pi}{n}\right) : \frac{\pi}{n}$ (b) $\cos\left(\frac{\pi}{n}\right) : \frac{\pi}{n}$ (c) $\sin\left(\frac{\pi}{n}\right) : \frac{\pi}{n}$ (d) $\cot\left(\frac{\pi}{n}\right) : \frac{\pi}{n}$

A. $\tan\left(\frac{\pi}{n}\right) : \frac{\pi}{n}$

B. $\cos\left(\frac{\pi}{n}\right) : \frac{\pi}{n}$

C. $\sin. \frac{\pi}{n} : \frac{\pi}{n}$

D. $\cot\left(\frac{\pi}{n}\right) : \frac{\pi}{n}$

Answer: A



Watch Video Solution

76. The ratio of the area of a regular polygon of n sides inscribed in a circle to that of the polygon of same number of sides circumscribing the same is 3:4. Then the value of n is 6 (b) 4 (c) 8 (d) 12

A. 6

B. 4

C. 8

D. 12

Answer: A



Watch Video Solution

77. In any triangle, the minimum value of $r_1 r_2 r_3 / r^3$ is equal to 1 (b) 9 (c) 27 (d) none of these

A. 1

B. 9

C. 27

D. none of these

Answer: C



Watch Video Solution

78. If R_1 is the circumradius of the pedal triangle of a given triangle ABC , and R_2 is the circumradius of the pedal triangle of the pedal triangle formed, and so on R_3, R_4 then the value of $\sum_{i=1}^{\infty} R_i$, where R (circumradius) of ABC is 5 is 8 (b) 10 (c) 12 (d) 15

A. 8

B. 10

C. 12

D. 15

Answer: B

[Watch Video Solution](#)

79. A sector $OABO$ of central angle θ is constructed in a circle with centre O and of radius 6. The radius of the circle that is circumscribed about the triangle OAB , is (a) $6\frac{\cos \theta}{2}$ (b) $6\frac{\sec \theta}{2}$ (c) $3\frac{\sec \theta}{2}$ (d) $3\left(\frac{\cos \theta}{2} + 2\right)$

A. $6 \cos. \frac{\theta}{2}$

B. $6 \sec. \frac{\theta}{2}$

C. $3 \sec. \frac{\theta}{2}$

D. $3\left(\cos. \frac{\theta}{2} + 2\right)$

Answer: C

[Watch Video Solution](#)

80. There is a point P inside an equilateral ABC of side a whose distances from vertices A, B and C are 3, 4 and 5, respectively. Rotate the

triangle and P through 60° about C . Let A go to A' and $P \rightarrow P'$. Then the area of PAP' (in sq. units) is 8 (b) 12 (c) 16 (d) 6

A. 8

B. 12

C. 16

D. 6

Answer: D



Watch Video Solution

Exercise Multiple

1. The sides of ABC satisfy the equation $2a^2 + 4b^2 + c^2 = 4ab + 2a \cdot$

Then the triangle a) isosceles the triangle b) obtuse c) $B = \cos^{-1}\left(\frac{7}{8}\right)$ d)

$$A = \cos^{-1}\left(\frac{1}{4}\right)$$

A. the triangle is isosceles

B. the triangle is obtuse

C. $B = \cos^{-1}(7/8)$

D. $A = \cos^{-1}(1/4)$

Answer: A::C::D



Watch Video Solution

2. If sides of triangle ABC are a, b and c such that $2b = a + c$ then

$\frac{b}{c} > \frac{2}{3}$ (b) $\frac{b}{c} > \frac{1}{3}$ $\frac{b}{c} < 2$ (d) $\frac{b}{c} < \frac{3}{2}$

A. $\frac{b}{c} > \frac{2}{3}$

B. $\frac{b}{c} > \frac{1}{3}$

C. $\frac{b}{c} < 2$

D. $\frac{b}{c} < \frac{3}{2}$

Answer: A::C



Watch Video Solution

3. If the sines of the angles A and B of a triangle ABC satisfy the equation $c^2x^2 - c(a+b)x + ab = 0$, then the triangle a) acute angled b) right angled c) obtuse angled d) $\sin A + \cos A = \frac{(a+b)}{c}$

A. is acute angled

B. is right angled

C. is obtuse angled

D. satisfies the equation $\sin A + \cos A = \frac{(a+b)}{c}$

Answer: B::D



Watch Video Solution

4. There exists a triangle ABC satisfying the conditions $\sin A = a$, $A > \pi/2$, $\sin A > a$, $A > \pi/2$, $b = a$

A. $\tan A + \tan B + \tan C = 0$

B. $\frac{\sin A}{2} = \frac{\sin B}{3} = \frac{\sin C}{7}$

C. $(a + b)^2 = c^2 + ab$ and $\sqrt{2}(\sin A + \cos A) = \sqrt{3}$

D. $\sin A + \sin B = \frac{\sqrt{3} + 1}{2}$, $\cos A \cos B = \frac{\sqrt{3}}{4} = \sin A \sin B$

Answer: C::D



Watch Video Solution

5. In triangle, ABC if $2a^2b^2 + 2b^2c^2 = a^2 + b^4 + c^4$, then angle B is equal to 45° (b) 135° 120° (d) 60°

A. 45°

B. 135°

C. 120°

D. 60°

Answer: A::B



Watch Video Solution

6. If in triangle ABC, a, c and angle A are given and $c \sin A < a < c$, then (b_1 and b_2 are values of b)

A. $b_1 + b_2 = 2c \cos A$

B. $b_1 + b_2 = c \cos A$

C. $b_1 b_2 = c^2 - a^2$

D. $b_1 b_2 = c^2 + a^2$

Answer: A::C



Watch Video Solution

7. If area of $ABC()$ and angle C are given and if the side c opposite to given angle is minimum, then $a = \sqrt{\frac{2}{\sin C}}$ (b) $b = \sqrt{\frac{2}{\sin C}}$
 $a = \sqrt{\frac{4}{\sin C}}$ (d) $b = \sqrt{\frac{4}{\sin C}}$

A. $a = \sqrt{\frac{2\Delta}{\sin C}}$

$$\text{B. } b = \sqrt{\frac{2\Delta}{\sin C}}$$

$$\text{C. } a = \frac{4\Delta}{\sin C}$$

$$\text{D. } b = \frac{4\Delta}{\sin^2 C}$$

Answer: A::B



Watch Video Solution

8. If Δ represents the area of acute angled triangle ABC, then

$$\sqrt{a^2b^2 - 4^2} + \sqrt{b^2c^2 - 4^2} + \sqrt{c^2a^2 - 4^2} = a^2 + b^2 + c^2 \frac{a^2 + b^2 + c^2}{2}$$

$$ab \cos C + bc \cos A + ca \cos B \quad ab \sin C + bc \sin A + ca \sin B$$

$$\text{A. } a^2 + b^2 + c^2$$

$$\text{B. } \frac{a^2 + b^2 + c^2}{2}$$

$$\text{C. } ab \cos C + bc \cos A + ca \cos B$$

$$\text{D. } ab \sin C + bc \sin A + ca \sin B$$

Answer: B::C

[Watch Video Solution](#)

9. Sides of $\triangle ABC$ are in A.P. If $a < \min\{b, c\}$, then $\cos A$ may be equal to

A. $\frac{4b - 3c}{2b}$

B. $\frac{3c - 4b}{2c}$

C. $\frac{4c - 3b}{2b}$

D. $\frac{4c - 3b}{2c}$

Answer: A::D

[Watch Video Solution](#)

10. If the angles of a triangle are 30° and 45° and the included side is $(\sqrt{3} + 1)cm$ then the area of the triangle is ____.

A. area of the triangle is $\frac{1}{2}(\sqrt{3} + 1)$ sq. units

B. area of the triangle is $\frac{1}{2}(\sqrt{3} - 1)$ sq. units

C. ratio of greater side to smaller side is $\frac{\sqrt{3} + 1}{\sqrt{2}}$

D. ratio of greater side to smaller side is $\frac{1}{4\sqrt{3}}$

Answer: A::C



Watch Video Solution

11. Lengths of the tangents from A,B and C to the incircle are in A.P., then

A. $r_1, r_2 r_3$ are in H.P

B. r_1, r_2, r_3 are in AP

C. a, b, c are in A.P

D. $\cos A = \frac{4c - 3b}{2c}$

Answer: A::C::D



Watch Video Solution

12. CF is the internal bisector of angle C of ABC , then CF is equal to

$\frac{2ab}{a+b} \frac{\cos C}{2}$ (b) $\frac{a+b}{2ab} \frac{\cos C}{2}$ (c) $\frac{b \sin A}{\sin\left(B + \frac{C}{2}\right)}$ (d) none of these

A. $\frac{2ab}{a+b} \cos. \frac{C}{2}$

B. $\frac{a+b}{2ab} \cos. \frac{C}{2}$

C. $\frac{b \sin A}{\sin\left(B + \frac{C}{2}\right)}$

D. none of these

Answer: A::C



Watch Video Solution

13. The incircle of $\triangle ABC$ touches side BC at D . The difference between

BD and CD (R is circumradius of $\triangle ABC$) is

A. $\left| 4R \sin. \frac{A}{2} \sin. \frac{B-C}{2} \right|$

B. $\left| 4R \cos. \frac{A}{2} \sin. \frac{B-C}{2} \right|$

C. $|b - c|$

D. $\left| \frac{b - c}{2} \right|$

Answer: A::C



Watch Video Solution

14. A circle of radius 4 cm is inscribed in $\triangle ABC$, which touches side BC at

D. If $BD = 6$ cm, $DC = 8$ cm then

A. the triangle is necessarily acute angled

B. $\tan. \frac{A}{2} = \frac{4}{7}$

C. perimeter of the triangle ABC is 42 cm

D. area of $\triangle ABC$ is $84cm^2$

Answer: A::B::C::D



Watch Video Solution

15. If H is the orthocentre of triangle ABC , $R =$ circumradius and $P = AH + BH + CH$, then $P = 2(R + r)$ (b) max of P is $3R$
min of P is $3R$ (d) $P = 2(R - r)$

A. $P = 2(R + r)$

B. max. of P is $3R$

C. min. of P is $3R$

D. $P = 2(R - r)$

Answer: A::B



Watch Video Solution

16. Let ABC be an isosceles triangle with base BC . If r is the radius of the circle inscribed in ΔABC and r_1 is the radius of the circle escribed opposite to the angle A , then the product $r_1 r$ can be equal to (where R is the radius of the circumcircle of ΔABC)

A. $R^2 \sin^2 A$

B. $R^2 \sin^2 2B$

C. $\frac{1}{2}a^2$

D. $\frac{a^2}{4}$

Answer: A::B::D



Watch Video Solution

17. If inside a big circle exactly $n(n \leq 3)$ small circles, each of radius r , can be drawn in such a way that each small circle touches the big circle and also touches both its adjacent small circles, then the radius of big

circle is $r \left(1 + \cos ec \frac{\pi}{n} \right)$ (b) $\left(\frac{1 + \frac{\tan \pi}{n}}{\frac{\cos \pi}{\pi}} \right) r \left[1 + \cos ec \frac{2\pi}{n} \right]$ (d)

$$\frac{r \left[\frac{\sin \pi}{2n} + \frac{\cos \pi}{2n} \right]^2}{\frac{\sin \pi}{n}}$$

A. $r \left(1 + \cos ec. \frac{\pi}{n} \right)$

B. $\left(\frac{1 + \tan \pi / n}{\cos \pi / n} \right)$

C. $r \left[1 + \cos ec. \frac{2\pi}{n} \right]$

$$D. \frac{r \left[\sin. \frac{\pi}{2n} + \cos. \frac{2\pi}{n} \right]^2}{\sin \pi / n}$$

Answer: A::D



Watch Video Solution

18. The area of a regular polygon of n sides is (where r is inradius, R is circumradius, and a is side of the triangle) $\frac{nR^2}{2} \sin\left(\frac{2\pi}{n}\right)$ (b)

$$nr^2 \tan\left(\frac{\pi}{n}\right) \frac{na^2}{4} \cot \frac{\pi}{n} \text{ (d) } nR^2 \tan\left(\frac{\pi}{n}\right)$$

$$A. \frac{nR^2}{2} \sin\left(\frac{2\pi}{n}\right)$$

$$B. nr^2 \tan\left(\frac{\pi}{n}\right)$$

$$C. \frac{na^2}{4} \cot. \frac{\pi}{n}$$

$$D. nR^2 \tan\left(\frac{\pi}{n}\right)$$

Answer: A::B::C



Watch Video Solution

19. In acute angled triangle ABC , AD is the altitude. Circle drawn with AD as its diameter cuts AB and AC at P and Q , respectively. Length of PQ is equal to $\frac{\Delta}{2R}$ (b) $\frac{abc}{4R^2}$ (c) $2R \sin A \sin B \sin C$ (d) $\frac{\delta}{R}$

A. $\frac{\Delta}{2R}$

B. $\frac{abc}{4R^2}$

C. $2R \sin A \sin B \sin C$

D. $\frac{\Delta}{R}$

Answer: C::D



Watch Video Solution

20. If A is the area and $2s$ is the sum of the sides of a triangle, then (a)

$A \leq \frac{s^2}{4}$ (b) $A \leq \frac{s^2}{3\sqrt{3}}$ (c) $2R \sin A$ (d) none of these

A. $A \leq \frac{s^2}{4}$

B. $A \leq \frac{s^2}{3\sqrt{3}}$

C. $A < \frac{s^2}{\sqrt{3}}$

D. none of these

Answer: A::B



Watch Video Solution

21. In ABC , internal angle bisector of $\angle A$ meets side BC in D . $DE \perp AD$ meets AC in E and AB in F . Then AE is H.M. of b and c and $AD = \frac{2bc}{b+c} \cos \frac{A}{2}$ $EF = \frac{4bc}{b+c} \sin \frac{A}{2}$ (d) $\triangle AEF$ is isosceles

A. AE is H.M of b and c

B. $AD = \frac{2bc}{b+c} \cos \frac{A}{2}$

C. $EF = \frac{4bc}{b+c} \sin \frac{A}{2}$

D. $\triangle AEF$ is isosceles

Answer: A::B::C::D



Watch Video Solution

22. In triangle ABC , $a = 4$ and $b = c = 2\sqrt{2}$. A point P moves within the triangle such that the square of its distance from BC is half the area of rectangle contained by its distance from the other two sides. If D be the centre of locus of P , then

- A. is $\frac{12\sqrt{6} - 28}{7}$ when P is inside the triangle
- B. may be $\frac{12\sqrt{6} - 8}{7}$ when P is outside the triangle
- C. may be $\frac{12\sqrt{6} + 14}{7}$ when P is inside the triangle
- D. may be $\frac{12\sqrt{6} + 14}{7}$ when P is outside the triangle

Answer: A::B::C



Watch Video Solution

23. BC is the base of the $\triangle ABC$ is fixed and the vertex A moves, satisfying the condition $\cot. \frac{B}{2} + \cot. \frac{C}{2} = 2 \cot. \frac{A}{2}$, then

A. $b + c = a$

B. $b + c = 2a$

C. vertex A moves along a straight line

D. vertex A moves along an ellipse

Answer: B::D



Watch Video Solution

24. If D, E and F be the middle points of the sides BC, CA and AB of the $\triangle ABC$, then $AD + BE + CF$ is



Watch Video Solution

Exercise Comprehension

1. Given that $\Delta = 6, r_1 = 2, r_2 = 3, r_3 = 6$

Circumradius R is equal to

A. 2.5

B. 3.5

C. 1.5

D. none of these

Answer: A



Watch Video Solution

2. Given that $\Delta = 6$, $r_1 = 3$, $r_2 = 2$, $r_3 = 6$

Inradius is equal to

A. 2

B. 1

C. 1.5

D. 2.5

Answer: B

3. Given that $\Delta = 6, r_1 = 2, r_2 = 3, r_3 = 6$ Difference between the greatest and the least angles is

A. $\cos^{-1} \cdot \frac{4}{5}$

B. $\tan^{-1} \cdot \frac{3}{4}$

C. $\cos^{-1} \cdot \frac{3}{5}$

D. none of these

Answer: C

4. Let $a = 6, b = 3$ and $\cos(A - B) = \frac{4}{5}$

Area (in sq. units) of the triangle is equal to

A. 9

B. 12

C. 11

D. 10

Answer: A



Watch Video Solution

5. Let $a = 6$, $b = 3$ and $\cos(A - B) = \frac{4}{5}$

Angle C is equal to

A. $\frac{3\pi}{4}$

B. $\frac{\pi}{4}$

C. $\frac{\pi}{2}$

D. none of these

Answer: C



Watch Video Solution

6. Let $a = 6$, $b = 3$ and $\cos(A - B) = \frac{4}{5}$

Value of $\sin A$ is equal to

A. $\frac{1}{2\sqrt{5}}$

B. $\frac{1}{\sqrt{3}}$

C. $\frac{1}{\sqrt{5}}$

D. $\frac{2}{\sqrt{5}}$

Answer: D



Watch Video Solution

7. Let ABC be an acute angled triangle with orthocenter H . D , E , and F are the feet of perpendicular from A , B , and C , respectively, on opposite sides.

Also, let R be the circumradius of $\triangle ABC$. Given

$$AH \cdot CH = 3 \text{ and } (AH)^2 + (BH)^2 + (CH)^2 = 7$$

Then answer the following

Value of $\frac{\cos A \cdot \cos B : \cos C}{\cos^2 A + \cos^2 B + \cos^2 C}$ is

A. $\frac{3}{14R}$

B. $\frac{3}{7R}$

C. $\frac{7}{3R}$

D. $\frac{14}{3R}$

Answer: A



Watch Video Solution

8. Let ABC be an acute angled triangle with orthocenter H . D , E , and F are the feet of perpendicular from A , B , and C , respectively, on opposite sides.

Also, let R be the circumradius of $\triangle ABC$. Given

$$AH \cdot BH \cdot CH = 3 \text{ and } (AH)^2 + (BH)^2 + (CH)^2 = 7$$

Then answer the following

Value of R is

A. 1

B. $\frac{3}{2}$

C. $\frac{5}{2}$

D. none

Answer: B



Watch Video Solution

9. Let ABC be an acute angled triangle with orthocenter H . D , E , and F are the feet of perpendicular from A , B , and C , respectively, on opposite sides.

Also, let R be the circumradius of $\triangle ABC$. Given

$$AH \cdot CH = 3 \text{ and } (AH)^2 + (BH)^2 + (CH)^2 = 7$$

Then answer the following

Value of $HD \cdot HF$ is

A. $\frac{9}{64R^3}$

B. $\frac{9}{8R^3}$

C. $\frac{8}{9R^3}$

D. $\frac{64}{9R^3}$

Answer: B



Watch Video Solution

10. Let O be a point inside $\triangle ABC$ such that

$$\angle OAB = \angle OBC = \angle OCA = \theta$$

$\cot A + \cot B + \cot C$ is equal to

A. $\tan^2 \theta$

B. $\cot^2 \theta$

C. $\tan \theta$

D. $\cot \theta$

Answer: D



View Text Solution

11. Let O be a point inside $\triangle ABC$ such that

$$\angle OAB = \angle OBC = \angle OCA = \theta$$

$\cos ec^2 A + \cos ec^2 B + \cos ec^2 C$ is equal to

A. $\cot^2 \theta$

B. $\cos ec^2 \theta$

C. $\tan^2 \theta$

D. $\sec^2 \theta$

Answer: B



Watch Video Solution

12. Let O be a point inside $\triangle ABC$ such that

$$\angle OAB = \angle OBC = \angle OCA = \theta$$

Area of $\triangle ABC$ is equal to

A. $\left(\frac{a^2 + b^2 + c^2}{4} \right) \tan \theta$

B. $\left(\frac{a^2 + b^2 + c^2}{4}\right) \cot \theta$

C. $\left(\frac{a^2 + b^2 + c^2}{2}\right) \tan \theta$

D. $\left(\frac{a^2 + b^2 + c^2}{2}\right) \cot \theta$

Answer: A



Watch Video Solution

13. Given an isosceles triangle with equal side of length b and angle $\alpha < \pi/4$, then

the circumradius R is given by

A. $\frac{1}{2}b \sec \alpha$

B. $b \sec \alpha$

C. $2b$

D. none of these

Answer: A

[Watch Video Solution](#)

14. Given an isosceles triangle with equal side of length b and angle

$\alpha < \pi/4$, then

the inradius r is given by

A. $\frac{b \sin 2\alpha}{2(1 - \cos \alpha)}$

B. $\frac{b \sin 2\alpha}{2(1 + \cos \alpha)}$

C. $\frac{b \sin \alpha}{2}$

D. $\frac{b \sin \alpha}{2(1 + \sin \alpha)}$

Answer: B

[Watch Video Solution](#)

15. Given an isosceles triangle with equal side of length b and angle

$\alpha < \pi/4$, then

the distance between circumcenter O and incenter I is

A. $\left| \frac{b \cos(3\alpha/2)}{2 \sin \alpha \cos(\alpha/2)} \right|$

B. $\left| \frac{b \cos 3\alpha}{\sin 2\alpha} \right|$

C. $\left| \frac{b \cos 3\alpha}{\cos \alpha \sin(\alpha/2)} \right|$

D. $\left| \frac{b}{\sin \alpha \cos \alpha / 2} \right|$

Answer: A



Watch Video Solution

16. In Fig. the incircle of $\triangle ABC$, touches the sides BC, CA and AB at D, E respectively. Show that : $AF + BD + CE = AE + BF + CD = \frac{1}{2}$ (Perimeter of $\triangle ABC$).



Watch Video Solution

17. Incircle of ABC touches the sides BC, CA and AB at D, E and F, respectively. Let r_1 be the radius of incircle of BDF . Then prove that

$$r_1 = \frac{1}{2} \frac{s(-b)\sin B}{\left(1 + \frac{\sin B}{2}\right)}$$

A. $2r^2 \sin(2A)\sin(2B)\sin(2C)$

B. $2r^2 \cos. \frac{A}{2} \cos. \frac{B}{2} \cos. \frac{C}{2}$

C. $2r^2 \sin(A - B)\sin(B - C)\sin(C - A)$

D. none of these

Answer: B



Watch Video Solution

18. Incircle of $\triangle ABC$ touches the sides BC, AC and AB at D, E and F, respectively. Then answer the following question

The length of side EF is

A. $r \sin. \frac{A}{2}$

B. $2r \sin. \frac{A}{2}$

C. $r \cos. \frac{A}{2}$

D. $2r \cos. \frac{A}{2}$

Answer: D



Watch Video Solution

19. Internal bisectors of $\triangle ABC$ meet the circumcircle at point D, E, and F

Length of side eF is

A. $2R \cos. \frac{A}{2}$

B. $2R \sin\left(\frac{A}{2}\right)$

C. $R \cos\left(\frac{A}{2}\right)$

D. $2R \cos\left(\frac{B}{2}\right) \cos\left(\frac{C}{2}\right)$

Answer: A



Watch Video Solution

20. Internal bisectors of $\triangle ABC$ meet the circumcircle at point D, E, and F

Area of $\triangle DEF$ is

A. $2R^2 \cos^2\left(\frac{A}{2}\right) \cos^2\left(\frac{B}{2}\right) \cos^2\left(\frac{C}{2}\right)$

B. $2R^2 \sin\left(\frac{A}{2}\right) \sin\left(\frac{B}{2}\right) \sin\left(\frac{C}{2}\right)$

C. $2R^2 \sin^2\left(\frac{A}{2}\right) \sin^2\left(\frac{B}{2}\right) \sin^2\left(\frac{C}{2}\right)$

D. $2R^2 \cos\left(\frac{A}{2}\right) \cos\left(\frac{B}{2}\right) \cos\left(\frac{C}{2}\right)$

Answer: D



Watch Video Solution

21. Internal bisectors of $\triangle ABC$ meet the circumcircle at point D, E, and F

Ratio of area of triangle ABC and triangle DEF is

A. ≥ 1

B. ≤ 1

C. $\geq 1/2$

D. $\leq 1/2$

Answer: B



Watch Video Solution

22. The area of any cyclic quadrilateral ABCD is given by

$$A^2 = (s - a)(s - b)(s - c)(s - d), \quad \text{where}$$

$2s = a + b + c + d$, a, b, c and d are the sides of the quadrilateral

Now consider a cyclic quadrilateral ABCD of area 1 sq. unit and answer the following question

The minimum perimeter of the quadrilateral is

A. 4

B. 2

C. 1

D. none of these

Answer: A

[Watch Video Solution](#)

23. The area of any cyclic quadrilateral ABCD is given by

$$A^2 = (s - a)(s - b)(s - c)(s - d), \quad \text{where}$$

$2s = a + b + c + d$, a, b, c and d are the sides of the quadrilateral

Now consider a cyclic quadrilateral ABCD of area 1 sq. unit and answer the following question

The minimum value of the sum of the lengths of diagonals is

A. $2\sqrt{2}$

B. 2

C. $\sqrt{2}$

D. none of these

Answer: A

[Watch Video Solution](#)

24. The area of any cyclic quadrilateral ABCD is given by

$$A^2 = (s - a)(s - b)(s - c)(s - d), \quad \text{where}$$

$2s = a + b + c + d$, a, b, c and d are the sides of the quadrilateral

Now consider a cyclic quadrilateral ABCD of area 1 sq. unit and answer the following question

When the perimeter is minimum, the quadrilateral is necessarily

- A. a square
- B. a rectangle but not a square
- C. a rhombus but not a square
- D. none of these

Answer: A



Watch Video Solution

25. In $\triangle ABC$, R, r, r_1, r_2, r_3 denote the circumradius, inradius, the exradii opposite to the vertices A, B, C respectively. Given that

$$r_1:r_2:r_3 = 1:2:3$$

The sides of the triangle are in the ratio

A. $1:2:3$

B. $3:5:7$

C. $1:5:9$

D. $5:8:9$

Answer: D



Watch Video Solution

26. In $\triangle ABC$, R, r, r_1, r_2, r_3 denote the circumradius, inradius, the exradii opposite to the vertices A, B, C respectively. Given that

$$r_1:r_2:r_3 = 1:2:3$$

The value of $R:r$ is

A. $5:2$

B. $5:4$

C. 5:3

D. 3:2

Answer: A



Watch Video Solution

27. In $\triangle ABC$, R, r, r_1, r_2, r_3 denote the circumradius, inradius, the exradii opposite to the vertices A, B, C respectively. Given that $r_1:r_2:r_3 = 1:2:3$

The greatest angle of the triangle is given by

A. $\cos^{-1}\left(\frac{1}{30}\right)$

B. $\cos^{-1}\left(\frac{1}{3}\right)$

C. $\cos^{-1}\left(\frac{1}{10}\right)$

D. $\cos^{-1}\left(\frac{1}{5}\right)$

Answer: C



Watch Video Solution

28. In $\triangle ABC$, P, Q, R are the feet of angle bisectors from the vertices to their opposite sides as shown in the figure. $\triangle PQR$ is constructed



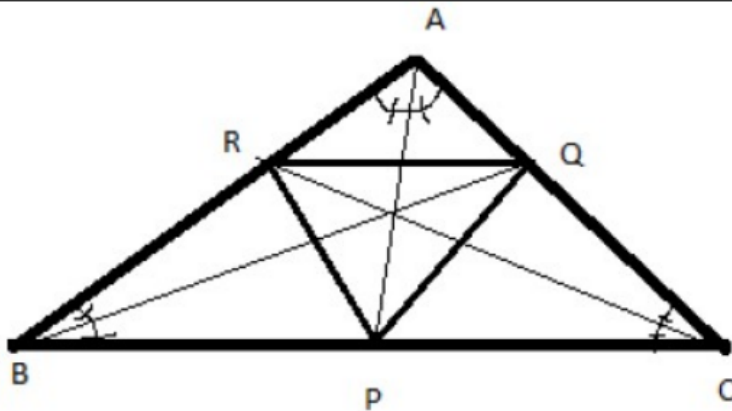
If $\angle BAC = 120^\circ$, then measured of $\angle RPQ$ will be

- A. 60°
- B. 90°
- C. 120°
- D. 150°

Answer: B

[Watch Video Solution](#)

29. In $\triangle ABC$, P, Q, R are the feet of angle bisectors from the vertices to their opposite sides as shown in the figure. $\triangle PQR$ is constructed



If $AB = 7$ units, $BC = 8$ units, $AC = 5$ units, then the side PQ will be

- A. $\frac{\sqrt{28}}{3}$ units
- B. $\frac{\sqrt{88}}{3}$ units
- C. $\frac{\sqrt{78}}{3}$ units
- D. $\frac{\sqrt{84}}{3}$ units

Answer: D



Watch Video Solution

30. Let G be the centroid of triangle ABC and the circumcircle of triangle AGC touches the side AB at A

If $BC = 6$, $AC = 8$, then the length of side AB is equal to

A. $\frac{1}{2}$

B. $\frac{2}{\sqrt{3}}$

C. $5\sqrt{2}$

D. none of these

Answer: C



Watch Video Solution

31. Let G be the centroid of triangle ABC and the circumcircle of triangle

AGC touches the side AB at A

If $\angle GAC = \frac{\pi}{3}$ and $a = 3b$, then $\sin C$ is equal to

A. $\frac{3}{4}$

B. $\frac{1}{2}$

C. $\frac{2}{\sqrt{3}}$

D. none of these

Answer: B



Watch Video Solution

32. Let G be the centroid of triangle ABC and the circumcircle of triangle AGC touches the side AB at A

If $AC = 1$, then the length of the median of triangle ABC through the vertex A is equal to

A. $\frac{\sqrt{3}}{2}$

B. $\frac{1}{2}$

C. $\frac{2}{\sqrt{3}}$

D. $\frac{5}{\sqrt{2}}$

Answer: A



Watch Video Solution

33. The inradius in a right angled triangle with integer sides is r

If $r = 4$, the greatest perimeter (in units) is

A. 96

B. 90

C. 60

D. 48

Answer: B



Watch Video Solution

34. The inradius in a right angled triangle with integer sides is r

If $r = 5$, the greatest area (in sq. units) is

A. 150

B. 210

C. 330

D. 450

Answer: C



Watch Video Solution

Exercise Matrix

1. Find the derivative of $y = \sin^{-1}(2 - x^4)$.



Watch Video Solution

2. Prove that $\frac{1}{\sec A - 1} + \frac{1}{\sec A + 1} = 2 \cos ec A \cdot \cot A$



Watch Video Solution

3. Evaluate $\int \frac{2^x}{\sqrt{1 - 4^x}} dx$



Watch Video Solution

4. Evaluate $\int_1^5 \sqrt{x-2}\sqrt{x-1}dx$.



Watch Video Solution

5. Prove: $\sin\theta(1 + \tan\theta) + \cos\theta(1 + \cot\theta) = (\sec\theta + \csc\theta)$.



Watch Video Solution

6. In a triangle ABC, $a = 7, b = 8, c = 9$, BD is the median and BE the altitude from the vertex B. Match the following lists

- a. $BD =$ p. 2
- b. $BE =$ q. 7
- c. $ED =$ r. $\sqrt{45}$
- d. $AE =$ s. 6

A. a) $\begin{matrix} a & b & c & d \\ p & r & q & q \end{matrix}$

B. b) $\begin{matrix} a & b & c & d \\ r & q & s & p \end{matrix}$

C. c) $\begin{matrix} a & b & c & d \\ q & r & p & s \end{matrix}$

D. d) $\begin{matrix} a & b & c & d \\ s & p & q & r \end{matrix}$

Answer: C



Watch Video Solution

Exercise Numerical

1. Suppose α, β, γ and δ are the interior angles of regular pentagon, hexagon, decagon, and dodecagon, respectively, then the value of $|\cos \alpha \sec \beta \cos \gamma \cos \delta|$ is _____



Watch Video Solution

2. Let ABCDEFGHIJKL be a regular dodecagon. Then the value of $\frac{AB}{AF} + \frac{AF}{AB}$ is equal to ____



Watch Video Solution

3. In a $\triangle ABC$, $b = 12$ units, $c = 5$ units and $\Delta = 30$ sq. units. If d is the distance between vertex A and incentre of the triangle then the value of d^2 is _____



Watch Video Solution

4. In $\triangle ABC$, if $r = 1$, $R = 3$, and $s = 5$, then the value of $a^2 + b^2 + c^2$ is _____



Watch Video Solution

5. Consider a $\triangle ABC$ in which the sides are $a = (n + 1)$, $b = (n + 2)$, $c = n$ with $\tan C = 4/3$, then the value of Δ is _____



Watch Video Solution

6. In $\triangle AEX$, T is the midpoint of XE and P is the midpoint of ET . If $\triangle APE$ is equilateral of side length equal to unity, then the value of $(AX)^2$ is ____



Watch Video Solution

7. In $\triangle ABC$, the incircle touches the sides BC , CA and AB , respectively, at D , E , and F . If the radius of the incircle is 4 units and BD , CE , and AF are consecutive integers, then the value of s , where s is a semi-perimeter of triangle, is ____



Watch Video Solution

8. The altitudes from the angular points A , B , and C on the opposite sides BC , CA and AB of $\triangle ABC$ are 210, 195 and 182 respectively. Then the value of a is ____



Watch Video Solution

9. In $\triangle ABC$, If $\angle C = 3\angle A$, $BC = 27$, and $AB = 48$. Then the value of AC is _____



Watch Video Solution

10. The area of a right triangle is 6864 sq. units. If the ratio of its legs is 143 : 24, then the value of r is _____



Watch Video Solution

11. In $\triangle ABC$, if $\cos A + \sin A - \frac{2}{\cos B + \sin B} = 0$, then the value of $\left(\frac{a+b}{c}\right)^4$ is



Watch Video Solution

12. In $\triangle ABC$, $\angle C = 2\angle A$, and $AC = 2BC$, then the value of $\frac{a^2 + b^2 c^2}{R^2}$ (where R is circumradius of triangle) is _____



Watch Video Solution

13. In $\triangle ABC$, if $b(b+c) = a^2$ and $c(c+a) = b^2$, then $|\cos A \cdot \cos B \cdot \cos C|$ is _____



Watch Video Solution

14. The sides of triangle ABC satisfy the relations $a+b-c=2$ and $2ab-c^2=4$, then the square of the area of triangle is _____



Watch Video Solution

15. The lengths of the tangents drawn from the vertices A, B and C to the incircle of $\triangle ABC$ are 5, 3 and 2, respectively. If the lengths of the parts of tangents within the triangle which are drawn parallel to the sides BC, CA and AB of the triangle to the incircle are α , β and γ , respectively,

then the value of $[\alpha + \beta + \gamma]$ (where $[\cdot]$ represents the greatest integer function) is _____



Watch Video Solution

16. If a , b and c represent the lengths of sides of a triangle then the possible integral value of $\frac{a}{b+c} + \frac{b}{c+a} + \frac{c}{a+b}$ is _____



Watch Video Solution

17. In triangle ABC , $\sin A \sin B + \sin B \sin C + \sin C \sin A = 9/4$ and $a = 2$, then the value of $\sqrt{3}\Delta$, where Δ is the area of triangle, is _____



Watch Video Solution

18. In a $\triangle ABC$, $AB = 52$, $BC = 56$, $CA = 60$. Let D be the foot of the altitude from A and E be the intersection of the internal angle bisector

of $\angle BAC$ with BC. Find the length DE.



Watch Video Solution

19. Point D,E are taken on the side BC of an acute angled triangle ABC,,

such that $BD = DE = EC$. If

$\angle BAD = x$, $\angle DAE = y$ and $\angle EAC = z$ then the value of

$\frac{\sin(x+y)\sin(y+z)}{\sin x \sin z}$ is _____



Watch Video Solution

20. For a triangle ABC , $R = \frac{5}{2}$ and $r = 1$. Let D, E and F be the feet of

the perpendiculars from incentre I to BC, CA and AB, respectively. Then

the value of $\frac{(IA)(IB)(IC)}{(ID)(IE)(IF)}$ is equal to _____



Watch Video Solution

21. Circumradius of $\triangle ABC$ is 3 cm and its area is 6cm^2 . If DEF is the triangle formed by feet of the perpendicular drawn from A, B and C on the sides BC, CA and AB, respectively, then the perimeter of $\triangle DEF$ (in cm) is _____



Watch Video Solution

22. The distance of incentre of the right-angled triangle ABC (right angled at A) from B and C are $\sqrt{10}$ and $\sqrt{5}$, respectively. The perimeter of the triangle is _____



Watch Video Solution

Jee Main Previous Year

1. For a regular polygon, let r and R be the radii of the inscribed and the circumscribed circles. A false statement among the following is There is a

regular polygon with $\frac{r}{R} = \frac{1}{\sqrt{2}}$ (17) There is a regular polygon with $\frac{r}{R} = \frac{2}{3}$ (30) There is a regular polygon with $\frac{r}{R} = \frac{\sqrt{3}}{2}$ (47) There is a regular polygon with $\frac{r}{R} = \frac{1}{2}$ (60)

A. There is a regular polygon with $\frac{r}{R} = \frac{\sqrt{3}}{2}$

B. There is a regular polygon with $\frac{r}{R} = \frac{1}{2}$

C. There is a regular polygon with $\frac{r}{R} = \frac{1}{\sqrt{2}}$

D. There is a regular polygon with $\frac{r}{R} = \frac{2}{3}$

Answer: D



Watch Video Solution

2. ABCD is trapezium with $AB \parallel DC$. The diagonal AC and BD intersect at E .

If $\triangle AED \sim \triangle BEC$. Prove that $AD = BC$.

A. $\left(\frac{p^2 + q^2 \sin \theta}{p \cos \theta + q \sin \theta} \right)$

B. $\frac{(p^2 + q^2) \cos \theta}{p \cos \theta + q \sin \theta}$

C. $\frac{p^2 + q^2}{p^2 \cos \theta + q^2 \sin \theta}$

D. $\frac{(p^2 + q^2) \sin \theta}{(p \cos \theta + q \sin \theta)}$

Answer: A



Watch Video Solution

Jee Advanced Previous Year

1. Let ABC be a triangle such that $\angle ACB = \frac{\pi}{6}$ and let a, b and c denote the lengths of the side opposite to A, B , and C respectively. The value(s) of x for which $a = x^2 + x + 1, b = x^2 - 1$, and $c = 2x + 1$ is(are)

– $(2 + \sqrt{3})$ (b) $1 + \sqrt{3}$ 2 + $\sqrt{3}$ (d) $4\sqrt{3}$

A. $-(2 + \sqrt{3})$

B. $1 + \sqrt{3}$

C. $2 + \sqrt{3}$

D. $4\sqrt{3}$

Answer: B



Watch Video Solution

2. If the angles A, B and C of a triangle are in an arithmetic progression and if a, b and c denote the lengths of the sides opposite to A, B and C respectively, then the value of the expression $\frac{a}{c}\sin 2C + \frac{c}{a}\sin 2A$ is

A. $\frac{1}{2}$

B. $\frac{\sqrt{3}}{2}$

C. 1

D. $\sqrt{3}$

Answer: D



Watch Video Solution

3. Let PQR be a triangle of area with $a = 2, b = \frac{7}{2}, \text{ and } c = \frac{5}{2}$, where $a, b, \text{ and } c$ are the lengths of the sides

of the triangle opposite to the angles at $P, Q, \text{ and } R$ respectively. Then

$$\frac{2 \sin P - \sin 2P}{2 \sin P + \sin 2P} \text{ equals } \frac{3}{4} \text{ (b) } \frac{45}{4} \text{ (c) } \left(\frac{3}{4}\right)^2 \text{ (d) } \left(\frac{45}{4}\right)^2$$

A. $\frac{3}{4\Delta}$

B. $\frac{45}{4\Delta}$

C. $\left(\frac{3}{4\Delta}\right)^2$

D. $\left(\frac{45}{4\Delta}\right)^2$

Answer: C



Watch Video Solution

4. a triangle ABC with fixed base BC , the vertex A moves such that

$$\cos B + \cos C = 4 \sin^2 \left(\frac{A}{2} \right).$$

If $a, b, \text{ and } c$, denote the length of the sides

of the triangle opposite to the angles $A, B, \text{ and } C$, respectively, then (a)

$b + c = 4a$ (b) $b + c = 2a$ (c) the locus of point A is an ellipse (d) the locus of point A is a pair of straight lines

A. $b + c = 4a$

B. $b + c = 2a$

C. locus of point A is an ellipse

D. locus of point A is a pair of straight lines

Answer: B::C



Watch Video Solution

5. about to only mathematics

A. 16

B. 18

C. 24

D. 22

Answer: B::D



Watch Video Solution

6. In a triangle XYZ, let x, y, z be the lengths of sides opposite to the angles X, Y, Z, respectively, and $2s = x + y + z$. If $\frac{s-x}{4} = \frac{s-y}{3} = \frac{s-z}{2}$ of incircle of the triangle XYZ is $\frac{8\pi}{3}$

A. area of the triangle XYZ is $6\sqrt{6}$

B. the radius of circumcircle of the triangle XYZ is $\frac{35}{6}\sqrt{6}$

C. $\sin. \frac{X}{2} \sin. \frac{Y}{2} \sin. \frac{Z}{2} = \frac{4}{35}$

D. $\sin^2\left(\frac{X+Y}{2}\right) = \frac{3}{5}$

Answer: A::C::D



Watch Video Solution

7. In a triangle PQR, let $\angle PQR = 30^\circ$ and the sides PQ and QR have lengths $10\sqrt{3}$ and 10, respectively. Then, which of the following statement(s) is (are) TRUE ?

A. $\angle QPR = 45^\circ$

B. The area of the triangle PQR is $25\sqrt{3}$ and $\angle QRP = 120^\circ$

C. The radius of the incircle of the triangle PQR is $10\sqrt{3} - 15$

D. The area of the circumcircle of the triangle PQR is 100π

Answer: B::C::D



Watch Video Solution

8. Prove the following trigonometric identities:

$$(\cos ec A - \sin A)(\sec A - \cos A)(\tan A + \cot A) = 1$$



Watch Video Solution

9. Let ABC and ABC' be two non-congruent triangles with sides $AB = 4$, $AC = AC' = 2\sqrt{2}$ and angle $B = 30^\circ$. The absolute value of the difference between the areas of these triangles is

 [Watch Video Solution](#)

10. Two parallel chords of a circle of radius 2 are at a distance $\sqrt{3+1}$ apart. If the chord subtend angles $\frac{\pi}{k}$ and $\frac{2\pi}{k}$ at the center, where $k > 0$, then the value of $[k]$ is

 [Watch Video Solution](#)

11. Consider a triangle ABC and let a, b and c denote the lengths of the sides opposite to vertices A, B , and C , respectively. Suppose $a = 6$, $b = 10$, and the area of triangle is $15\sqrt{3}$. If $\angle ACB$ is obtuse and if r denotes the radius of the incircle of the triangle, then the value of r^2 is

 [Watch Video Solution](#)

