



India's Number 1 Education App

## MATHS

### BOOKS - KC SINHA ENGLISH

#### COMPLEX NUMBERS - FOR BOARDS

##### Solved Examples

1. Write the complex number:  $5 - 7\sqrt{-21}$



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2. Write the complex number:  $\frac{\sqrt{3}}{2} - \frac{\sqrt{-2}}{7}$



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3. Write the complex number:  $\sqrt{x}$ , ( $x > 0$ )



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4. Write the complex number:  $-b + \sqrt{-4ac}$ , ( $a, c > 0$ )



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5. Write the real and imaginary part of the complex number:

$$\frac{\sqrt{17}}{2} + i \frac{2}{\sqrt{70}}$$



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6. Write the real and imaginary part of the complex number:

$$\sqrt{37} + \sqrt{-19}$$



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7. Find a and b such that  $2a + i4b$  and  $2i$  represent the same complex number.

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8. Find the multiplicative inverse of the following complex number:  $3 + 2i$

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9. Find Multiplicative Inverse of  $\frac{3 + 4i}{4 - 5i}$

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10. Find the sum and product of the complex numbers  $-\sqrt{3} + \sqrt{-2}$  and  $2\sqrt{3} - i$

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11. Explain the fallacy in the following:

$$-1 = i. \quad i = \sqrt{-1}. \quad \sqrt{-1} = \sqrt{(-1)(-1)} = \sqrt{1} = 1$$



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12. Evaluate:  $i^{80}$



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13. Evaluate:  $\frac{1}{i}$



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14. Evaluate:  $(-\sqrt{-1})^{31}$



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15. Evaluate:  $\frac{i^2 + i^4 + i^6 + i^7}{1 + i^2 + i^3}$



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16. Simplify:  $i^{n+100} + i^{n+50} + i^{n+48} + i^{n+46}$



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17. Simplify:  $\left(\frac{1+i}{1-i}\right)^{200}$



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18. Evaluate:  $\left[i^{19} + \left(\frac{1}{i}\right)^{25}\right]^2$



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19. Write the complex number in  $a+ib$  form:  $z = \frac{2+i}{(1+i)(1-2i)}$



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20. Express:  $\frac{(1+i)^3}{4+3i}$  in the form  $a+ib$



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21. Express each one of the following in the standard form

$$a+ib: \left( \frac{1}{1-2i} + \frac{3}{1+i} \right) \left( \frac{3+4i}{2-4i} \right)$$



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22. Express each one of the following in the standard form

$$a+ib: \frac{1}{1-\cos\theta+2i\sin\theta}$$



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23. If  $z_1$  and  $z_2$  are  $1 - i$  and  $-2 + 4i$  respectively find  $\operatorname{Im}\left(\frac{z_1 z_2}{\bar{z}_1}\right)$



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24. If  $Z = x^2 - 7x - 9yi$  such that  $\bar{Z} = y^2i + 20i - 12$  then the number of order pair  $(x,y)$  is :



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25. Find the real values of  $x$  and  $y$ , if :  $\frac{(1+i)x - 2i}{3+i} + \frac{(2-3i)y + i}{3-i} = i$



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26. solve  $z + 2 = \frac{1}{4 - 3i}$ , where  $z$  is a complex number



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27. Find real  $\theta$  such that  $\frac{3 + 2i \sin \theta}{1 - 2i \sin \theta}$  is purely real.



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28. If  $x = \frac{1}{2}(5 - 3i)$ , then find the value of  $x^4 - x^3 - 12x^2 + 23x + 12$



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29. Find the square root of  $7-24i$



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30. Find the square root of  $4 + 4\sqrt{3}i$



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31. Find square root of  $8 - 15i$



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32. Find the square root of  $7 - 30\sqrt{-2}$



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33. Find all possible values of  $\sqrt{i} + \sqrt{-i}$ .



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34. Find the square root of the following:

$$\frac{x^2}{y^2} + \frac{y^2}{x^2} - \frac{1}{i} \left( \frac{x}{y} - \frac{y}{x} \right) - \frac{9}{4}$$



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35. If  $\omega, \omega^2$  be imaginary cube root of unity then

$$(3 + 3\omega + 5\omega^2)^6 - (2 + 6\omega + 2\omega^2)^3$$
 is equal to



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36. If  $w$  is a complex cube root of unity then show that

$$(2 - w)(2 - w^2)(2 - w^{10})(2 - w^{11}) = 49?$$



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37. If  $\omega$  is an imaginary cube root of unity, then show that

$$(1 - \omega)(1 - \omega^2)(1 - \omega^4)(1 - \omega^5) = 9$$



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38. If  $\omega$  is an imaginary cube root of unity, then show that

$$(1 - \omega + \omega^2)^5 + (1 + \omega - \omega^2)^5 = 32$$



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**39.** Show that  $\left(\frac{-1 + \sqrt{3}i}{2}\right)^n + \left(\frac{-1 - \sqrt{3}i}{2}\right)^n$  is equal to 2 when n is a multiple of 3 and is equal to  $-1$  when n is any other positive integer.



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**40.** If  $1; w; w^2$  are cube root of unity and n is a positive integer; then  $1 + w^n + w^{2n} = \{3; \text{ When } n \text{ is multiple of 3}; 0; \text{ when } n \text{ is not a multiple of 3}$



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**41.** If  $\omega$  be an imaginary cube root of unity, show that  $1 + \omega^n + \omega^{2n} = 0$ , for  $n=2,4$



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**42. (i)** If  $\alpha, \beta$  be the imaginary cube root of unity, then show that

$$\alpha^4 + \beta^4 + \alpha^{-1}\beta^{-1} = 0$$



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**43.** Show that  $\sqrt{\left[ -1\sqrt{\left\{ -1 - \sqrt{-1 + \dots \text{to} \infty} \right\}} \right]} = \omega, \text{ or } \omega^2$



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**44.** Prove that  $x^{3p} + x^{3q+1} + x^{3r+2}$  is exactly divisible by  $x^2 + x + 1$ , if  $p, q, r$  is integer.



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**45.** Prove that  $\left( \frac{i - \sqrt{3}}{i + \sqrt{3}} \right)^{100} + \left( \frac{i + \sqrt{3}}{i - \sqrt{3}} \right)^{100} = -1$



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**46.**  $x + \frac{1}{x} = -1$  then find the value of  $x^{2000} + \frac{1}{x^{2000}}$



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**47.** If the cube roots of unity are  $1, \omega, \omega^2$ , then the roots of the equation  $(x - 1)^3 + 8 = 0$  are a.  $-1, 1 + 2\omega, 1 + 2\omega^2$  b.  $-1, 1 - 2\omega, 1 - 2\omega^2$  c.  $-1, -1, -1$  d. none of these



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**48.** If  $\alpha, \beta$  and  $\gamma$  are the cube roots of  $P(p) < 0$ , then for any  $x, y$ , and  $z$ ,  $\frac{x\alpha + y\beta + z\gamma}{x\beta + y\gamma + z\alpha}$  is equal to



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**49.** The value of  $\frac{a + b\omega + c\omega^2}{b + c\omega + a\omega^2} + \frac{a + b\omega + c\omega^2}{c + a\omega + b\omega^2}$  (where ' $\omega$ ' is the imaginary cube root of unity), is (a)  $-\omega$  (b).  $\omega^2$  (c). 1 (d).  $-1$



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51. If  $x = a + b$ ,  $y = a\omega + b\omega^2$  and  $z = a\omega^2 + b\omega$ , prove that  $xyz = a^3 + b^3$



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52.

If

$x = a + b$ ,  $y = a\omega + b\omega^2$  and  $z = a\omega^2 + b\omega$ , prove that  $xyz = a^3 + b^3$



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53.  $\omega$  is an imaginary root of unity. Prove that

$$(a + b\omega + c\omega^2)^3 + (a + b\omega^2 + c\omega)^3$$

$$= (2a - b - c)(2b - a - c)(2c - a - b).$$



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**54.** Resolve into linear factors  $a^2 + b^2 + c^2 - ab - bc - ca$



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**55.** Find the complex conjugates of  $2 + i5$ ,  $-6 - i7$  and  $\sqrt{3}$



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**56.** Find the conjugate, modulus and argument of  $\sqrt{2} - \sqrt{2}i$



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**57.** Find the conjugate and modulus of the following complex number

$$(3 - 2i)(3 + 2i)(1 + i)$$



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58. Find the modulus and argument of the complex number

$$\frac{2+i}{4i+(1+i)^2}$$



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59. Find the modulus and principal argument of the following complex

number:  $\frac{5}{2}(\cos 30^\circ + i\sin 30^\circ)$



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60. Find the modulus and principal argument of the following complex

number:  $\cos 70^\circ + i\cos 20^\circ$



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**61.** about to only mathematics



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**62.** For any two complex numbers  $z_1$  and  $z_2$  prove that:

$$|z_1 + z_2|^2 + |z_1 - z_2|^2 = 2[|z_1|^2 + |z_2|^2]$$



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**63.** For any two complex numbers  $z_1$  and  $z_2$  prove that:

$$|z_1 + z_2|^2 = |z_1|^2 + |z_2|^2 + 2\operatorname{Re}\bar{z}_1 z_2$$



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**64.** If  $|z_1| = |z_2| = \dots = |z_n| = 1$ , then show that

$$|z_1| = |z_2| = \dots = |z_n| = \left| \frac{1}{z_1} + \frac{1}{z_2} + \frac{1}{z_3} + \dots + \frac{1}{z_n} \right|$$



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65. If  $z$  is a complex number such that  $|z| = 1$ , prove that  $\frac{z-1}{z+1}$  is purely imaginary, what will be your conclusion if  $z = 1$ ?



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66. If  $z_1 = 2 - i$ ,  $z_2 = 1 + i$ , find  $\left| \frac{z_1 + z_2 + 1}{z_1 - z_2 + i} \right|$



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67. Find the number of non-zero integral solutions of the equation  $|1 - i|^x = 2^x$ .



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68. If  $\alpha$  and  $\beta$  are different complex numbers with  $|\beta| = 1$ , then find  $\left| \frac{\beta - \alpha}{1 - \bar{\alpha}\beta} \right|$ .



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69. If  $z = x + iy$  prove that  $|x| + |y| \leq \sqrt{2}|z|$



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70. If  $z = 2 - 3i$  show that  $z^2 - 4z + 13 = 0$  and hence find the value of  $4z^3 - 3z^2 + 169$ .



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71. If  $z_1$  and  $z_2$  are two complex numbers such that  $|z_1| = |z_2| + |z_1 - z_2|$  show that  $\operatorname{Im} \left( \frac{z_1}{z_2} \right) = 0$



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72. Show that for  $z \in C$ ,  $|z| = 0$  if and only if  $z = 0$



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73. Solve the equation  $2z = |z| + 2i$ , where  $z$  is a complex number.



74. Express  $\sin 30^\circ + i\cos 30^\circ$  in polar form



75. Write down the following complex number in polar form: Product of  $2(\cos 30^\circ + i\sin 30^\circ)$  and  $3(\cos 90^\circ + i\sin 90^\circ)$



76. Write down the following complex number in polar form: Quotient of  $12(\cos 150^\circ + i\sin 150^\circ)$  and  $3(\cos 60^\circ + i\sin 60^\circ)$



77. Express the following complex number in the polar form: (i)  $\frac{1 + 7i}{(2 - i)^2}$   
(ii)  $\frac{1 + 3i}{1 - 2i}$

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78. If  $\sqrt{a} + ib = x + iy$  prove that  $\sqrt{a} - ib = x - iy$

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79.  $(x + iy)^{\frac{1}{3}} = (a + ib)$  then prove that  $\left(\frac{x}{a} + \frac{y}{b}\right) = 4(a^2 - b^2)$

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80. If  $(x + iy) = \sqrt{\frac{a + ib}{c + id}}$  then prove that  $(x^2 + y^2)^2 = \frac{a^2 + b^2}{c^2 + d^2}$

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**81.** if  $\frac{3}{2 + \cos \theta + i \sin \theta} = a + ib$  then prove that  $a^2 + b^2 = 4a - 3$



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**82.** Show that:

$$(x^2 + y^2)^5 = (x^5 - 10x^3y^2 + 5xy^4)^2 + (5x^4y - 10x^2y^3 + y^5)^2$$



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**83.** Express  $(1 + a^2)(1 + b^2)(1 + c^2)$  as the sum of two squares.



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**84.** If  $(1 + x)^n = a_0 + a_1x + a_2x^2 + \dots + a_nx^n$ , then

$(a_0 - a_2 + \dots)^2 + (a_1 - a_3 + \dots)^2$  is equal to (A)  $3^n$  (B)  $2^n$  (C)

$\left(\frac{1 - 2^n}{1 + 2^n}\right)$  (D) none of these



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85. Show that the points representing the complex numbers  $(3 + 2i)$ ,  $(2 - i)$  and  $-7i$  are collinear



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86. Show that the points representing the complex numbers  $3 + 2i$ ,  $5i$ ,  $-3 + 2i$  and  $-i$  form a square



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87. Let  $z_1$ ,  $z_2$  and  $z_3$  be three distinct complex numbers , satisfying  $|z_1| = |z_2| = |z_3| = 1$ . Which of the following is/are true :



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**88.** Show that the area of the triangle on the Argand diagram formed by the complex number  $z$ ,  $iz$  and  $z + iz$  is  $\frac{1}{2}|z|^2$



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**89.** Complex numbers  $z_1, z_2, z_3$  are the vertices  $A, B, C$  respectively of an isosceles right angled triangle with right angle at  $C$  and  $(z_1 - z_2)^2 = k(z_1 - z_3)(z_3 - z_2)$ , then find  $k$ .



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**90.** If  $z_1, z_2, z_3$  are the vertices of an isosceles triangle right angled at  $z_2$ , then prove that  $(z_1)^2 + 2(z_2)^2 + (z_3)^2 = 2(z_1 + z_3)z_2$



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**Exercise**

1. Write the following as complex numbers :  $\sqrt{-27}$



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2. Write the complex number:  $\sqrt{-16}$



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3. Write the complex number:  $4 + \sqrt{-5}$



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4. Write the complex number:  $-1 - \sqrt{-5}$



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5. Write the complex number:  $1 + \sqrt{-1}$





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6. Write the real and imaginary parts of the complex number:  $2 - i\sqrt{2}$



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7. Write the real and imaginary parts of the complex number:  $-\frac{\frac{1}{5} + i}{i}$



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8. Write the real and imaginary parts of the complex number:  $\frac{\sqrt{5}}{7}i$



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9. Write the real and imaginary part of the complex number:

$$\sqrt{37} + \sqrt{-19}$$



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10. Write the real and imaginary parts of the complex number:

$$\frac{\sqrt{37}}{3} + \frac{3}{\sqrt{70}}i$$



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11. Find the additive inverse of the following:  $-5 + 7i$



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12. Find the additive inverse of the following:  $4 - 3i$



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13. Find the additive inverse of the following:  $10$



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14. Find the sum of the following numbers  
 $\frac{2}{3} + \frac{5}{3}i$ ,  $-\frac{2}{3}i$  and  $-\frac{5}{4} - i$

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15. Find the difference of the following complex number,  
 $-3 + 2i$  and  $13 - i$

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16. Find the difference of the complex numbers:  $1 - i$  and  $-1 + 6i$

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17. Find the product and quotient of the complex numbers  
 $1 + i$  and  $3 + i$ .

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18. Find multiplicative inverse of the following:  $2 + \sqrt{3}i$

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19. Find multiplicative inverse of the following:  $-3 + 4i$

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20. Find multiplicative inverse of the following:  $-i$

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21. Find the multiplicative inverse of the complex number  $4 + 3i$

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22. Find multiplicative inverse of the following:  $(\sqrt{5} + i3)$



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23. Find multiplicative inverse of the following:  $2 - 4i$



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24. For any two complex numbers  $z_1$  and  $z_2$ , prove that

$$\operatorname{Re}(z_1 z_2) = \operatorname{Re} z_1 \operatorname{Re} z_2 - |m z_1| m z_2.$$



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25. Let  $z_1 = 2 - i$ ,  $z_2 = -2 + i$ . Find (i)  $\operatorname{Re}\left(\frac{z_1 z_2}{\bar{z}_1}\right)$  (ii)  $\operatorname{Im}\left(\frac{1}{z_1 \bar{z}_1}\right)$



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**26.** Let  $z_1 = 2 - i$ ,  $z_2 = -2 + i$ . Find (i)  $\operatorname{Re}\left(\frac{z_1 z_2}{\bar{z}_1}\right)$  (ii)  $\operatorname{Im}\left(\frac{1}{z_1 \bar{z}_1}\right)$



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**27.** Express the following in the form  $a+ib$ :  $(3 + 2i)(3 - 2i)$



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**28.** Express the following in the form  $a+ib$ :  $(i - 2)^2$



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**29.** Express the following in the form  $a+ib$ :  $\frac{2-i}{4+3i}$



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**30.** Express the following in the form  $a+ib$ :  $\frac{1+2i+3i^2}{1-2i+3i^2}$



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31. Express the following in the form  $a+ib$ :  $\left(\frac{1+i}{1-i}\right)^2$



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32. Express the following in the form  $a+ib$ :  $\left(\frac{1+2i}{2+i}\right)^2$



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33. Express the following in the form  $a+ib$ :  $\frac{6+3i}{2-i}$



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34. Express the following complex numbers in the standard form

$$a + ib: \frac{5 + \sqrt{2}i}{1 - \sqrt{2}i}$$



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35. Evaluate  $2i^2 + 6i^3 + 3i^{16} - 6i^{19} + 4i^{25}$



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36.  $1 + i^{10} + i^{110} + i^{1000}$



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37. Find the value of  $i^n + i^{n+1} + i^{n+2} + i^{n+3}$  for all  $n \in N$ .



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38. If  $\left\{ i^{17} - \left( \frac{1}{i} \right)^{34} \right\}^2 = a + 2i$ , then the value of a is



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**39.**  $(-i)^{4n+3}$ , where n is a positive integer.

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**40.** Simplify:  $\left(\frac{1+i}{1-i}\right)^{4n+1}$  (n is a positive integer)

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**41.** Simplify the following:  $(2i)^3$

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**42.** Simplify the following:  $(8i)\left(-\frac{1}{8}i\right)$

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**43.** Express the following in the form  $a + ib$ :  $(5i)\left(-\frac{3}{5}i\right)$



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44. Simplify the following:  $( - 5i) \left( \frac{1}{8}i \right)$



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45. Simplify the following:  $( - i)(2i) \left( - \frac{1}{8}i \right)^3$



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46. Simplify the following:  $i^{-35}$



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47. Simplify the following:  $i^{-39}$



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**48.** Express in the form of complex number  $i^9 + i^{19}$



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**49.** Evaluate :  $\left[ i^{18} + \left( \frac{1}{i} \right)^{25} \right]^3$



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**50.** Simplify the following:  $i^6 + i^8$



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**51.**  $i + i^2 + i^3 + i^4$  Find the value of the given term.



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52. Find the value of  $i^{12} + i^{13} + i^{14} + i^{15}$

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53. Simplify the following:  $i^4 + i^8 + i^{12} + i^{16}$

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54. Write the following in the form  $a + ib$ :  $\frac{1}{(2+i)^2} - \frac{1}{(2-i)^2}$ .

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55. Express of the complex number in the form  $a + ib$ .

$$\left(\frac{1}{5} + i\frac{2}{5}\right) - \left(4 + i\frac{5}{2}\right)$$

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**56.** The from  $a + ib$  is given :  $(7 - i2) - (4 + i) + (-3 + i5)$  simplify it.



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**57.** Express each of the following in the form

$$a + ib: \left\{ \left( \frac{1}{3} + \frac{7}{3}i \right) + \left( 4 + \frac{1}{3}i \right) \right\} - \left( -\frac{4}{3} + i \right)$$



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**58.** Simplify:  $i^3 + (6 + i3) - (20 + i5) + (14 + i3)$



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**59.**  $(7 + i5)(7 - i5)$  find product



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60. Express the following in the form  $a+ib$ :  $3i^3(15i^6)$



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61. Express the following in the form  $a+ib$ :  $\sqrt{3} + (3 - i2) - (3 - i2)$



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62. Express the following in the form  $a + ib$ :  $(1 - i)^4$



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63. Express the following in the form  $a+ib$ :  $\left(\frac{1}{2} + i2\right)^3$



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**64.** Express the following in the form  $a+bi$

$$\left( -2 - \frac{1}{3}i \right)^3$$



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**65.** Express each of the following in the form

$$a + ib: 3(7 + 7i) + i(7 + 7i)$$



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**66.** Express the following in the form  $a+ib$ :  $(3 + 5i)(2 + 6i)$



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**67.** Express the following in the form  $a+ib$ :  $\left( \frac{1}{3} + 3i \right)^3$



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68. Express the following in the form  $a+ib$ :  $(5 - 3i)^3$

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69. Express the following in the form  $a + ib$ :  $(1 - i)^4$

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70. Find the following as a single complex number  $x + iy$

$$(\sqrt{6} + i5) \left( \sqrt{6} - i\frac{1}{5} \right)$$

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71. Find the following as a single complex number  $x+ iy =$

$$(5 + i9)( - 3 + i4)$$

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$$72. \left[ \left( \sqrt{5} + \frac{i}{2} \right) (\sqrt{5} - i2) \right] \div (6 + i5)$$

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$$73. \frac{\left[ (\sqrt{2} + i\sqrt{3}) + (\sqrt{2} - i\sqrt{3}) \right]}{\left[ (\sqrt{3} + 1\sqrt{2}) + (\sqrt{3} - 1\sqrt{2}) \right]}$$

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74. Express each one of the following in the standard form

$$a + ib: \frac{(3 + i\sqrt{5})(3 - i\sqrt{5})}{(\sqrt{3} + \sqrt{2}i) - (\sqrt{3} - i\sqrt{2})}.$$

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75. Express the following complex numbers in the standard form

$$a + ib: \left( \frac{1}{1 - 4i} - \frac{2}{1 + i} \right) \left( \frac{3 - 4i}{5 + i} \right)$$

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76. If  $\left(\frac{1+i}{1-i}\right)^m = 1$ , then find the least positive integral value of  $m$ .



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77. Find  $x$  and  $y$  if: (i)  $(x + iy) + (7 - 5i) = 9 + 4i$



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78. Find the real values of  $x$  and  $y$ , if :  $(x + iy)(2 - 3i) = 4 + i$



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79. Find  $x$  and  $y$  if:  $\left(\frac{3}{\sqrt{5}}x - 5\right) + i2\sqrt{5}y = \sqrt{2}$



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80. If  $4x + i(3x - y) = 3 + i(-6)$ , where x and y are real numbers, then find the values of x and y.



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81. Find x and y if:  $(3y - 2) + i(7 - 2x) = 0$



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82. If  $a = \frac{1+i}{\sqrt{2}}$  find the value of  $a^6 + a^4 + a^2 + 1$



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83. If  $x = \sqrt{-2} - 1$  find the value of  $x^4 + 4x^3 + 6x^2 + 4x + 9$



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84. If  $x = 3 + 4i$  (where,  $i = \sqrt{-1}$ , the value of  $x^2 - 12x^3 + 70x^2 - 204x + 225$ , is

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85. If  $x = 3 + 2i$  find the value of  $x^4 - 4x^3 + 4x^2 + 8x + 39$

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86. Find the square root of  $7-24i$

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87. Find the square roots of the following:  $15\backslash 8i$

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**88.** Find the square root of the following:  $i$



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**89.** Find the square roots of the following:  $1\sqrt{-1} + i$



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**90.** Find the square root of the following complex number:  $1 - i$



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**91.** Find the square root of the following complex number:

$$-11 - 60\sqrt{-1}$$



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92. Find the square root of the following complex number:  $-8 - 6i$



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93. Find the square root of the following complex number:  $-5 + 12i$



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94. Find the square root of  $12 + 4\sqrt{5}i$



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95. find the square roots of following :  $(6\sqrt{-2} - 7)$



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96. Find the square roots of :  $4ab - 2i(a^2 - b^2)$



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97. Find the square root of  $\frac{x^2}{y^2} + \frac{y^2}{x^2} + \frac{1}{2}i\left(\frac{x}{y} + \frac{y}{x}\right) + \frac{31}{16}$



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98. Square root of  $\left(x^2 + \frac{1}{x^2}\right) - \frac{4}{i}\left(x - \frac{1}{x}\right) - 6$  is



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99. Find the square root of the following:  $a^2 - 1 + 2a\sqrt{-1}$



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100. Find the square root of the following:  $a^2 - 1 + 2a\sqrt{-1}$



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101. Find  $\sqrt{2 + 3\sqrt{-5}} + \sqrt{2 - 3\sqrt{-5}}$



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102. Find the value of  $(i)\omega^{21}(ii)\omega^{18}$



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103. Find the value of:  $\omega^{768}$



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104. Find the value of:  $\omega^{-105}$



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105. Find the value of:  $\omega^{-105}$



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106. Find the value of:  $\omega^{-364}$



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107. Find the value of:  $\omega^{-30}$



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108. if  $\alpha = \frac{-1 + \sqrt{-3}}{2}, \beta = \frac{-1 - \sqrt{-3}}{2}$  then prove that

$$\frac{\alpha}{\beta} + \frac{\beta}{\alpha} + 1 = 0$$



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109. If  $\omega$  be an imaginary cube root of unity, show that

$$(1 + \omega - \omega^2)(1 - \omega + \omega^2) = 4$$



110. If  $1, \omega, \omega^2$  be three roots of 1, show that:  $(3 + \omega + 3\omega^2)^6 = 64$



111. If  $\omega$  be an imaginary cube root of unity, show that  
 $(1 + \omega - \omega^2)(1 - \omega + \omega^2) = 4$



112. If  $1, \omega, \omega^2$  be three roots of 1, show that:  
 $(1 - \omega + \omega^2)^2 + (1 + \omega - \omega^2)^2 = -4$



113. If  $1, \omega, \omega^2$  be three roots of 1, show that:  $(1 + \omega)^3 - (1 + \omega^2)^3 = 0$



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114. evaluate  $\sqrt{-2 + 2\sqrt{-2 + 2\sqrt{-2 + \dots \dots \dots \infty}}}$



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115. show that  $\left(\frac{\sqrt{3} + i}{2}\right)^6 + \left(\frac{i - \sqrt{3}}{2}\right)^6 = -2$



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116. If  $1, \omega, \omega^2$  be the three cube roots of 1, then show that:

$$(1 + \omega)(1 + \omega^2)(1 + \omega^4)(1 + \omega^5) = 1$$



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117. If  $1, \omega, \omega^2$  be the three cube roots of 1, then show that:

$$(1 + \omega)(1 + \omega^2)(1 + \omega^4)(1 + \omega^8) = 1$$



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$$118. (2 + \omega + \omega^2)^3 + (1 + \omega - \omega^2)^8 - (1 - 3\omega + \omega^2)^4 = 1$$



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119. If  $\omega$  is complex cube root of unity

$$(1 - \omega + \omega^2)(1 - \omega^2 + \omega^4)(1 - \omega^4 + \omega^8)(1 - \omega^8 + \omega^{16})$$



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120. If  $a + b + c = 0$  and  $\omega, \omega^2$  are imaginary cube roots of unity, then

$$(a + b\omega + c\omega^2)^3 + (a + b\omega^2 + c\omega)^3 = 3abc$$
 (b) 6abc (c) 9 abc (d) 27 abc



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121. If  $\omega$  be an imaginary cube root of unity, show that

$$\frac{a + b\omega + c\omega^2}{a\omega + b\omega^2 + c} = \omega^2$$



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122. If  $\omega$  be an imaginary cube root of unity, show that  $1 + \omega^n + \omega^{2n} = 0$ ,

for  $n=2,4$



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123. Resolve into linear factors:  $a^2 - ab + b^2$



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124. Resolve into the linear factor:  $a^2 + ab + b^2$



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**125.** Resolve into the linear factor:  $a^3 + b^3$

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**126.** Resolve into linear factors:  $a^3 - b^3$

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**127.** Resolve into the linear factor:  $a^3 + b^3 + c^3 - 3abc$

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**128.** If  $x = a + b$ ,  $y = a\omega + b\omega^2$  and  $z = a\omega^2 + b\omega$  where  $\omega$  is an imaginary cube root of unity, prove that  $x^2 + y^2 + z^2 = 6ab$ .

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129. If  $\omega$  be an imaginary cube root of unity, show that:

$$\frac{1}{1+2\omega} + \frac{1}{2+\omega} - \frac{1}{1+\omega} = 0.$$



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130. Find the cube roots of following: 8 and  $-8$



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131. Find the cube roots of following: 8 and  $-8$



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132. Find the modulus of the following :  $\frac{1-i\sqrt{3}}{2+2i}$



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133. Find the modulus and amplitude of  $\frac{2+i}{4i+(1+i)^2}$ .



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134. Find the modulus of  $\frac{1+i}{1-i} - \frac{1-i}{1+i}$



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135. Find the modulus and argument of each of the following complex number:  $-\sqrt{3} - i$



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136. Find the argument of the following:  $\frac{1+i}{-\sqrt{3}i}$



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137. Find the modulus and the arguments of the complex number

$$z = 1 - i\sqrt{3}$$



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138. Find the modulus of the following complex number:  $z = -\sqrt{3} + i$



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139. Find the modulus and argument of the following complex number:

$$z = \frac{(1+i)^{13}}{(1-i)^7}$$



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140. Find the modulus and argument of the following complex number:

$$\frac{1}{1+i}$$



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**141.** Find the modulus and argument of the following complex number:

$$\frac{1+i}{1-i}$$



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**142.** Find the modulus and argument of the complex number  $\frac{1+2i}{1-3i}$ .



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**143.** Find the conjugate of  $\frac{(3-2i)(2+3i)}{(1+2i)(2-i)}$ .



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**144.** Find the real numbers  $x$  and  $y$  if  $(x-iy)(3+5i)$  is the conjugate of  $-6-24i$ .



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**145.** If  $|2z - 1| = |z - 2|$  prove that  $|z| = 1$  where  $z$  is a complex



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**146.** If  $z = x + iy$  and  $w = \frac{1 - iz}{z - i}$ , show that  $|w| = 1$   $z$  is purely real.



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**147.** If  $|z - 5i| = |z + 5i|$ , then the locus of  $z$ .



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**148.** If  $|z| \leq 4$ , then find the maximum value of  $|iz + 3 - 4i|$ .



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**149.** If  $|z| \leq 4$ , then find the maximum value of  $|iz + 3 - 4i|$ .



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**151.** For any two complex numbers  $z_1$  and  $z_2$  prove that:

$$|z_1 + z_2|^2 + |z_1 - z_2|^2 = 2[|z_1|^2 + |z_2|^2]$$



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**152.** Solve the equation  $|z| + z = 2 + i$



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153. Change the following complex numbers to Cartesiasn form:

$$2(\cos 0^0 + i\sin 0^0)$$



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154. Change the following complex numbers to Cartesiasn form:

$$5(\cos 270^0 + i\sin 270^0)$$



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155. Change the following complex numbers to Cartesiasn form:

$$4(\cos 300^0 + i\sin 300^0)$$



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156. Write the number  $z = (i - \sqrt{3})^{13}$  in algebraic form.



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157. Write the following complex numbers in the polar form:  $1 + i$



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158. Put the following numbers in the polar form:  $-1 - \sqrt{3}i$



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159. Write the following complex numbers in the polar form:  $1 - i$



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160. Put the following numbers in the polar form:  $-3$



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161. Convert of the complex number in the polar form:  $1 + i$



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162. Write the following complex numbers in the polar form:  $-1 - i$



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163. Convert of the complex number in the polar form:  $\sqrt{3} + i$



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164. Put the following numbers in the polar form:  $-4 + i4\sqrt{3}$



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165. Convert of the complex number in the polar form:  $i$



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166. Represent the complex number  $z = 1 + i\sqrt{3}$  in the polar form.



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167. Convert  $\frac{1 + 3i}{1 - 2i}$  into the polar form.



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168. Find the modulus and argument of the following complex number

and hence express each of them in the polar form:  $\frac{-16}{1 + i\sqrt{3}}$



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169. Write down the following complex number in polar form:

$Product of 2(\cos 30^\circ + i\sin 30^\circ)$  and  $3(\cos 90^\circ + i\sin 90^\circ)$



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170. Give the following products in polar form:

$$[3(\cos 225^\circ + i\sin 225^\circ)][6(\cos 45^\circ + i\sin 45^\circ)]$$



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171. Give the following products in polar form:

$$[2(\cos 210^\circ + i\sin 210^\circ)][4(\cos 120^\circ + i\sin 120^\circ)]$$



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172. Convert it into  $a+ib$  form:

$$\frac{7(\cos 135^\circ + i\sin 135^\circ)}{14(\cos 90^\circ + i\sin 90^\circ)}.$$



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173. Give the following quotients in polar form:  $\frac{9(\cos 90^\circ + i\sin 90^\circ)}{3(\cos 45^\circ + i\sin 45^\circ)}$



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174. Write the complex number  $z = \frac{1-i}{\cos \frac{\pi}{3} + i \sin \frac{\pi}{3}}$  " in polar form.



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175. If  $\frac{a+ib}{c+id} = x+iy$ , prove that (i)  $\frac{a-ib}{c-id} = (x-iy)$  (ii)  
 $\frac{a^2+b^2}{c^2+d^2} = (x^2+y^2)$



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176. If  $\frac{a+ib}{c+id} = x+iy$ , prove that (i)  $\frac{a-ib}{c-id} = (x-iy)$  (ii)  
 $\frac{a^2+b^2}{c^2+d^2} = (x^2+y^2)$



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177. Show that a real value of  $x$  will satisfy the equation

$$\frac{1 - ix}{1 + ix} = a - ib \quad \text{if } a^2 + b^2 = 1, \text{ when } a, b \text{ are real.}$$



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178. If  $x + iy = \frac{a + ib}{a - ib}$  prove that  $x^2 + y^2 = 1$



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179.

If

$$(a + ib)(c + id)(e + if)(g + ih) = A$$

$$\text{, then show that } (a^2 + b^2)(c^2 + d^2)(e^2 + f^2)(g^2 + h^2) = A^2 + B^2$$



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180. If  $a + ib = \frac{(x + i)^2}{2x^2 + 1}$ , prove that  $a^2 + b^2 = \frac{(x^2 + 1)^2}{(2x^2 + 1)^2}$



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**181.** If  $\frac{1}{m+in} - \frac{x-iy}{x+iy} = 0$ , where  $x, y, m, n$  are real and  $x+iy \neq 0$  and  $m+in \neq 0$ , prove that  $m^2 + n^2 = 1$ .



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**182.** if  $\left(1 + i\frac{x}{a}\right)\left(1 + i\frac{x}{b}\right)\left(1 + i\frac{x}{c}\right)\dots = A + iB$  then prove that  $\left(1 + \frac{x^2}{a^2}\right)\left(1 + \frac{x^2}{b^2}\right)\left(1 + \frac{x^2}{c^2}\right)\dots = A^2 + B^2$



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**183.** If  $\frac{a-ib}{a+ib} = \frac{1+i}{1-i}$ , then show that  $a+b=0$



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**184.** Express  $(1+a^2)(1+b^2)$  as the sum of two squares.



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**185.** Express  $(x^2 + a^2)(x^2 + b^2)(x^2 + c^2)$  as the sum of two squares



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**186.** Show that  $(x^2 + y^2)^4 = (x^4 - 6x^2y^2 + y^4)^2 + (4x^3y - 4xy^3)^2$ .



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**187.** Plot the following numbers and their complex conjugates on a complex number plane  $4 - 3i$



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**188.** Plot the following numbers and their complex conjugates on a complex number plane : 1



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**189.** Represent the following complex numbers in the complex plane

i



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**190.** Plot the following numbers and their complex conjugates on a complex number plane —  $\frac{4}{3}i$



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**191.** Plot the following numbers and their complex conjugates on a complex number plane :  $\sqrt{-3}$



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192. Plot the following numbers and their complex conjugates on a complex number plane :  $\frac{\sqrt{3}}{2} + \frac{i}{2}$



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193. Plot all the complex numbers in the complex number plane whose absolute value is 5.



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194. Show that the points representing the complex numbers  $3 + 4i$ ,  $8 - 6i$  and  $13 + 9i$  are the vertices of a right angled triangle.



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195. Prove that the points representing the complex numbers  $4 + 3i$ ,  $6 + 4i$ ,  $5 + 6i$ ,  $3 + 5i$  are the vertices of a square.



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196. Prove that the points  $(4, 5)$ ,  $(7, 6)$ ,  $(6, 3)$ ,  $(3, 2)$  are the vertices of a parallelogram. Is it a rectangle.



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197. A variable complex number  $z = x + iy$  is such that  $\arg \frac{z - 1}{z + 1} = \frac{\pi}{2}$ .

Show that  $x^2 + y^2 - 1 = 0$ .



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198. Prove that locus of  $z$  is a circle and find its centre and radius if  $\frac{z - i}{z - 1}$  is purely imaginary.



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**199.** If the points  $(2, 1)$  and  $(1, -2)$  are equidistant from the point  $(x, y)$ , show that  $x + 3y = 0$ .



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