



MATHS

BOOKS - KC SINHA ENGLISH

CONIC SECTIONS - FOR BOARDS

Solved Examples

1. Find the equation of the parabola whose: focus

is (1,1) and the directrix is x+y=1=0

2. Find the equation of the parabola whose focus is (1, -1) and whose vertex is 2, 1. Also, find its axis and latus-rectum.



3. Find the focus and the equation of the parabola whose vertex is (6, -3) and directrix is

3x - 5y + 1 = 0

4. Find the equation of the parabola whose focus

is (1, 1) and equation of directrix is x + y = 1.



5. Find the equation of the parabola which is symmetric about the y-axis, and passes through the point (2, -3).



6. Find the equation of the parabola whose axis is parallel to x-axis and which passes through points (0,0), (1,1) and (2,3)

Watch Video Solution

7. Find the equation of the parabola whose latusrectum is 4units, axis is the line 3x + 4y - 4 = 0 and the tangent at the vertex is

the line 4x - 3 + 7 = 0.



8. Find the equation of the parabola the extremities of whose latus rectum are (1, 2) and (1, -4).

9. The equation of the parabola whose vertex and focus lie on the axis of x at distances a and a_1 from the origin, respectively, is (a) $y^2 - 4(a_1 - a)x$ (b) $y^2 - 4(a_1 - a)(x - a)$ (c) $y^2 - 4(a_1 - a)(x - a)$ (d) none

Watch Video Solution

10. Find the axis, vertex, tangent at the vertex, focus, directrix and length of latus rectum of the parabola $x^2 = -16y$.

Watch Video Solution

11. Find the vertex, focus, directrix and length of

the latus rectum of the parabola

$$y^2 - 4y - 2x - 8 = 0$$

12. Find the vertex, axis, focus, directrix, tangent at the vertex, and length of the latus rectum of the parabola $2y^2 + 3y - 4x - 3 = 0$.

Watch Video Solution

13. The focal distance of a point on the parabola

 $y^2 = 12\xi s4$. Find the abscissa of this point.



14. Find the axis, tangent at the vertex, vertex, focus, directrix and latus rectum of the parabola $9y^2 - 16x - 12y - 57 = 0$



15. Find the angle made by a double ordinate of length 8a at the vertex of the parabola $y^2 = 4ax$.



16. An equilateral trinalge is inscribed in the parabola $y^2 = -8x$, where one vertex is at the vertex of the parabola. Find the length of the side of the tringle.



17. Find the area of the triangle formed by the lines joining the vertex of the parabola $x^2 = -36y$ to the ends of the latus rectum.

18. If y_1, y_2, y_3 be the ordinates of a vertices of the triangle inscribed in a parabola $y^3 = 4ax$, then show that the area of the triangle is $rac{1}{8a}|(y_1 - y_2)(y_2 - y_3)(y_3 - y_1)|.$



19. If a parabolic reflector is 20 cm in diameter

and 5 cm deep, find the focus.



20. An arc is in the form of a parabola with its axis vertical. The arch is 10 m high and 5 m wide at the base. How high is it 2 m from the vertex of the parabola ?



21. The cable of a uniformly loaded suspension bridge hangs in the form of a parabola. The roadway which is horizontal and 100m long is supported by vertical wires attached to the cable, the longest wire being 30m and the shortest

being 6m. Find the length of the supporting wire

attached to the roadway 18m from the middle.



22. Obtain the equation of the ellipse whose focus is the point (-1, 1), and the corresponding directrix is the line x - y + 3 = 0, and the eccentricity is $\frac{1}{2}$.

23. Find the equation of the ellipse whose axes are parallel to the coordinate axes having its centre at the point (2, -3) one focus at (3, -3) and vertex at (4, -3).

Watch Video Solution

24. Find the equation of the ellipse, with major axis along the x-axis and passing through the points (4, 3) and (-1, 4).

25. Find the equation of the ellipse whose foci are (2, 3), (-2, 3) and whose semi-minor axes is $\sqrt{5}$

Watch Video Solution

26. Find the equation of the ellipse the extremities of whose minor axis are (3, 1) and (3, 5) and whose eccentricity is $\frac{1}{2}$.

27. The equation of the ellipse with its centre at (1, 2), one focus at (6, 2) and passing through the point (4, 6) is-

Watch Video Solution

28. Find the equation of the ellipse whose axes are along the coordinate axes, foci at $(0, \pm 4)$ and eccentricity 4/5.

29. Find the equation of an ellipse the distance between the foci is 8 units and the distance between the directrices is 18 units.



30. Find the equation of the ellipse with foci at $(\pm 5, 0)andx = \frac{36}{5}$ as one of the directrices.



31. Find the equation of the ellipse that passes through the origin and has the foci at the points (-1, 1) and S'(1, 1).

Watch Video Solution

32. Find the length and equation of major and minor axes, centre, eccentricity, foci, equation of directrices, vertices and length of latus rectum of the ellipses : $\frac{x^2}{225} + \frac{y^2}{289} = 1$

33. Find the coordinates of the foci, the vertices, the length of major axis, the minor axis, the eccentricity and the length of the latus rectum of the ellipse. $16x^2 + y^2 = 16$

Watch Video Solution

34. For the ellipse
$$12x^2 + 4y^2 + 24x - 16y + 25 = 0$$
 centries $(-1, 2)$ b. lengths of the axes are $\sqrt{3}$ and 1 c. eccentricity $= \sqrt{\frac{2}{3}}$ d. all of these

35. Find the latus rectum, the eccentricity and coordinates of the foci of the ellipse $9x^2 + 5y^2 + 30y = 0.$



36. A rod of length 12 cm moves with its ends always touching the coordinate axes. Determine the equation of the locus of a point *P* on the rod, which is 3cm from the end in contact with the xaxis.



37. A rod AB of length 15cm rests in between two coordinate axes in such a way that the end point A lies on $x - a\xi s$ and end point B lies on $y - a\xi s$. A point is taken on the rod in such a way that AP = 6cm. Show that the locus of P is an ellipse. Also find its eccentricity.



38. An arch way is in the shape of a semi-ellipse, the road level being the major axis. If the breadth

of the arch way is 30 feet and a man 6 feet tall just touches the top when 2 feet from the side, find the greatest height of the arch.

Watch Video Solution

39. An arc is in the form of a semi-ellipse. It is 8m wide and 2m high at the centre. Find the height of the arch at a point 1. 5cm from one end.

40. A man running a racecourse notes that the sum of the distances from the two flag posts from him is always 10 m and the distance between the flag posts is 8 m. Find the equation of the posts traced by the man.

Watch Video Solution

41. Find the equation of the hyperbola whose one directrix is 2x + y = 1, the corresponding focus is (1, 2) and eccentricity is $\sqrt{3}$

42. Find the equation of the hyperbola having e=32 and foci at $(\pm 3,0)$

Watch Video Solution

43. Find the equation of the hyperbola having eccentricity $e = \frac{4}{3}$ and vertices at $(0, \pm 7)$.



45. Find the equation of the hyperbola having

vertices at $(\ \pm\ 5, 0)$ and foci at $(\ \pm\ 7, 0)$

46. Find the equation of the hyperbola whose eccentricity is $\sqrt{2}$ and the distance between the foci is 16, taking transverse and conjugate axes of the hyperbola as x and y - axes respectively.



47. Referred to the principal axes as the axes of coordinates find the equation of the hyperbola whose foci are at $(0, \pm \sqrt{10})$ and which passes through the point (2, 3).



48. Find the equation of the hyperbola for which the distance between focie is $32, e = 2\sqrt{2}$ and transverse and conjugate axes are along x and y - axes respectively.

Watch Video Solution

49. The foci of a hyperbola coincide with the foci of the ellipse $\frac{x^2}{25} + \frac{y^2}{9} = 1$. Find the equation of the hyperbola, if its eccentricity is 2.

50. Find the length of the transverse axis, conjugate axis, eccentricity, vertices, foci and directrices of the hyperbola $9x^2 - 16y^2 = 144$.



Watch Video Solution

51. Find the length of axes of the ellipse whose eccentricity is 4/5 and whose foci coincide with those of the hyperbola $9x^2 - 16y^2 + 144 = 0$



52. Find the length of the transverse and conjugate axes, eccentricity, centre, foci and directrices of the hyperbola. $9x^2 - 16y^2 - 72x + 96y - 144 = 0$

Watch Video Solution

53. Find the centre, eccentricity and foci of the hyperbola, $9x^2 - 16y^2 - 18x - 64y - 199 = 0$

54. If *eande* ' the eccentricities of a hyperbola and its conjugate, prove that $\frac{1}{e^2} + \frac{1}{e^{\prime 2}} = 1$. Watch Video Solution

55. If S and S'' are the foci, C is the centre, and P is a point on a rectangular hyperbola, show that $SP \times S'P = (CP_2).$



56. Find the equation of the locus of all points such that difference of their distances from (4, 0) and (-4, 0) is always equal to 2.





1. Find the equaiton of the parabola whose focus

is (0, -2) and directrix is y = 2.

2. Find the equaiton of the parabola whose focus

is (0, -3) and *directrixisy=3*.

Watch Video Solution

3. Find the equaiton of the parabola whose focus

is (4,0) and directrix is x=-4

Watch Video Solution

4. Find the equation of parabola whose focus is (6, 0) and directrix x = -6.



7. Find the equation of the parabola whose focus

is (2, 3) and directrix is x - 2y - 6 = 0.



9. Find the equation of the parabola whose focus

is at (-1, 1) and the directrix is x + y + 1 = 0.

10. Find the equation of the parabola whose focus

is (5,3) and directrix is the line 3x-4y+1=0.



12. Find the equation of the parabola having ther

vertex at (0, 1) and the focus at (0, 0).



13. Find the equation of the parabola with vertex

at (0, 0) and focus at (0, 2).

Watch Video Solution

14. about to only mathematics



15. Find the equation of the parabola whose focus

is (3, 0) and vertex is (0, 0).



16. Find the equation of the parabola having vertex at (0, 0) and focus at (-2, 0).
17. Find the equation of the parabola passing through (5, 2), having vertex at (0, 0) and symmetric about y-axis.



19. Find the equation of the parabola whose focus is at (0, 0) and vertex is at the intersection of the

line x + y = 1 and x - y = 3.



20. Prove that the equation of the parabola whose focus is (0, 0) and tangent at the vertex is x - y + 1 = 0 is $x^2 + y^2 + 2xy - 4x + 4y - 4 = 0.$

Watch Video Solution

21. Find the equation of the parabola with vertex is at (2, 1) and the directrix is x = y - 1.



22. Find the equatin to the parabola whose axis is parallel to the y-xis and which passes through the point (0, 4), (1.9), and (-2, 6) and determine its latus rectum.

Watch Video Solution

23. Equation of parabola which has its axis along x-axis and which passes through the points (3, 2) and (-2, -1) is



25. Find the equation of the parabola with its axis parallel to x-axis and which passes through the points (1, 2), (-1, 3) and (-2, 1).

26. For each of that parabolas, find the coordinates of the focus, the equation of the directrix and the length of latus rectum : $x^2 = 6y$

Watch Video Solution

27. Find the coordinates of the focus, axis, the equation of the directrix and latus rectum of the parabola $y^2 = 8x$.

28. For the following parabola find the coordinates of the focus, the equation of the directrix and the length of the latus rectum. $y^2 = 12x$



29. For each of that parabolas, find the coordinates of the focus, the equation of the directrix and the length of latus rectum : $x^2 = -9y$

30. For each of that parabolas, find the coordinates of the focus, the equation of the directrix and the length of latus rectum : $y^2 = -12x$

Watch Video Solution

31. For each of that parabolas, find the coordinates of the focus, the equation of the directrix and the length of latus rectum : $y^2 = 10x$



32. For each of that parabolas, find the coordinates of the focus, the equation of the directrix and the length of latus rectum : $y^2 = -8x$

Watch Video Solution

Match Mideo Colution

33. Find the coordinates of the focus, axis of the parabola, the equation of the directrix and the length of the latus rectum. $x^2 = 6y$



35. Find the vertex, focus, axis, directrix and latus

rectum of that parabola : $\left(y-2
ight)^2=3(x+1)$



$$3x^2 + 12x + 8y = 0.$$





39. Find the equation of the parabola with focus

(5, 0), and directrix x = -5. Also, find the length

of the latus rectum.

Watch Video Solution

40. Find the equation of the circle described on the line segment as diameter joining the foci of the parabolas $x^2 = 4ay$ and $y^2 = 4a(x - a)$ as diameter.

41. An equilateral triangle is inscribed in the parabola $y^2 = 4ax$ whose vertex is at of the parabola. Find the length of its side.

Watch Video Solution

42. Find the area of the triangle formed by the lines joining the vertex of the parabola $x^2 = 12y$ to the ends of its latus-rectum.

43. PQ is a double ordinate of a parabola $y^2 = 4ax$. Find the locus of its points of trisection.



44. The focus of a parabolic mirror as shown in the figure alongside is at a distance of 6cm from its vertex. If the mirror is 20cm deep, find the distance BC.



45. A water jet from a function reaches it maximum height of 4 m at a distance 0.5 m from the vertical passing through the point O of water outlet. The height of the jet above the horizontal OX at a distance of 0.75 m from the point O is 5 m (b) 6 m (c) 3 m (d) 7 m



46. about to only mathematics



47. Obtain the equation of the ellipse whose focus is the point (-1, 1), and the corresponding directrix is the line x - y + 3 = 0, and the eccentricity is $\frac{1}{2}$.

Watch Video Solution



focus is (6,7), directrix is x+y+2 and eccentricity is $\displaystyle rac{1}{\sqrt{3}}$



49. Find the equation to the ellipse whose one focus is (2, 1), the directrix is 2x - y + 3 = 0 and the eccentricity is $\frac{1}{\sqrt{2}}$ **Watch Video Solution**

50. Find the equation of the ellipse with centre at the origin, the length of the major axis 12 and one focus at (4, 0).



51. Find the equation of the ellipse whose centre is (-2,3) and whose semi axis are 3 and 2 when major axis is i. parallel to x-axis ii. parallel to y-axis.



52. Find the equation of an ellipse whose vertices are $(0, \pm 10)$ and eccentricity $e=rac{4}{5}$

53. Find the equation for the ellipse that satisfies the given conditions:Vertices $(0, \pm 13)$, foci $(0, \pm 5)$



54. Find the equation of ellipse whose vetices are (p,5,0) and foci are $(\pm4,0)$



55. Find the equation of the ellipse whose vertices

are $(\pm 13, 0)$ and foci are $(\pm 5, 0).$



56. Find the equation of the ellipse whose vetices

are $(\pm 6, 0)$ and foci are $(\pm 4, 0)$.

Watch Video Solution

57. Find the equation of the ellipse having, length of major axis 26 and foci $(\pm 5, 0)$



59. Find the equation of the ellipse having, length

of major axis 8 and foci $(~\pm~3,0)$

60. Find the equation of the ellipse having, length

of major axis 16 and foci $(0, \pm 6)$



61. Find the equation of the ellipse passing through the point (3, 2), having centre at (0, 0) and major axis on y-axis.



62. Find the equation for the ellipse that satisfies the given conditions: Ends of major axis $\left(0,\ \pm\sqrt{5}
ight)$, ends of minor axis $(\ \pm1,0)$



63. If *a* be the length of semi-major axis, *b* the length of semi-minor axis and *c* the distance of one focus from the centre of an ellipse, then find the equation of the ellipse for which centre is (0, 0), foci is on x-axis, b = 3 and c = 4.



64. The distance between the foci of an ellipse is 10 and its lactusrectum is 15, find its equation reffered to its axes as axes of cordinates.



Watch Video Solution

65. find the equation of the ellipse refer refer to it

Centre whose major axis is equal to distance

between the foci and latus rectum is 10.



66. The eccentricity of an ellipse is $\frac{1}{2}$ and the distance between its foci is 4 units. If the major and minor axes of the ellipse are respectively along the x and y axes, find the equation of the ellipse

Watch Video Solution

67. Find the equation of the ellipse passing through (6, 4), foci on y-axis, centre at the origin and having eccentricity $\frac{3}{4}$.

68. Find the equation of the ellipse passing through (4, 1) with focus as $(\pm 3, 0)$

Watch Video Solution

69. Find the equation of the set of all points whose distance from (0,4) are $\frac{2}{3}$ of their distance from the line y=9.

70. Find the equation of the ellipse whose foci re

(4,0) and (-4,0) eccentricity =1/3.



71. Find the equation to the ellipse (referred to its axes as the axes of x and y respectively) which passes through the point (-3,1) and has eccentricity $\sqrt{\frac{2}{5}}$

72. If the angle between the lines joining the foce of any ellipse to an extremity of the minor axis is 90^0 , find the accentricity. Find also the equation of the ellipse if the major axis is $2\sqrt{2}$.



73. For the ellipse $9x^2 + 16y^2 = 144$, find the length of the major and minor axes, the eccentricity, the coordinates of the foci, the vertices and the equations of the directrices.



74. Find the lengths of the major and the minor axes, the coordinates of the foci, the vertices, the eccentricity, the length of latus rectum and the eqatuion of the directrices of that ellipses : $\frac{x^2}{169} + \frac{y^2}{25} = 1$



75. Find the lengths of the major and the minor axes, the coordinates of the foci, the vertices, the eccentricity, the length of latus rectum and the

eqatuion of the directrices of that ellipses :

$$rac{x^2}{25} + rac{y^2}{169} = 1$$

Watch Video Solution

76. Find the lengths of the major and the minor axes, the coordinates of the foci, the vertices, the eccentricity, the length of latus rectum and the eqatuion of the directrices of that ellipses : $3x^2 + 2y^2 = 18$

77. Find the lengths of the major and the minor axes, the coordinates of the foci, the vertices, the eccentricity, the length of latus rectum and the eqatuion of the directrices of that ellipses : $x^2 + 16y^2 = 16$.

Watch Video Solution

78. Find the coordinates of the foci, the vertices, the length of major axis, the minor axis, the eccentricity and the length of the latus rectum of the ellipse. $4x^2 + 9y^2 = 36$

79. Find the coordinates of the foci, the vertices, the length of major axis, the minor axis, the eccentricity and the length of latus rectum of that ellipses: $9x^2 + 4y^2 = 36$



80. Find the coordinates of the foci, the vertices,

the length of major axis, the minor axis, the

eccentricity and the length of the latus rectum of

the ellipse. $36x^2 + 4y^2 = 144$



81. Find the coordinates of the foci, the vertices, the length of major axis, the minor axis, the eccentricity and the length of latus rectum of that ellipses: $25x^2 + 4y^2 = 100$

82. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the
eccentricity and the length of the latus rectum of
the ellipse.
$$\frac{x^2}{100} + \frac{y^2}{400} = 1$$

Watch Video Solution

83. Find the coordinates of the foci, the vertices, the length of major axis, the minor axis, the eccentricity and the length of latus rectum of that ellipses: $\frac{x^2}{25} + \frac{y^2}{9} = 1$

84. Find the coordinates of the foci, the vertices, the length of major axis, the minor axis, the eccentricity and the length of the latus rectum of the ellipse. $\frac{x^2}{25} + \frac{y^2}{100} = 1$

Watch Video Solution

85. Find the coordinates of the foci, the vertices, the length of major axis, the minor axis, the eccentricity and the length of the latus rectum of the ellipse. $\frac{x^2}{49} + \frac{y^2}{36} = 1$



86. Find the coordinates of the foci, the vertices, the length of major axis, the minor axis, the eccentricity and the length of latus rectum of that ellipses: $\frac{x^2}{25} + \frac{y^2}{100} = 1$

Watch Video Solution

87. Show that the following equation represents an ellipse and find its centre and eccentricity : $8x^2 + 6y^2 - 16x + 12y + 13 = 0$



89. Eccentricity of the ellipse

$$4x^2+y^2-8x+2y+1=0$$
 is
90. Find the latus rectum, eccentricity, coordinates of the foci and the length of axes of that ellipses : $9x^2 + 5y^2 - 30y = 0$

Watch Video Solution

91. Find the latusrectum, eccentricity, coordinates of the foci, coordinates of the vertices, the length of the axes and the centre of the ellipse $4x^2 + 9y^2 - 8x - 36y + 4 = 0$

92. Find the eccentricity of an ellipse if its latus

rectum is equal to one-half of its major axis.



93. Find the eccentricity of the ellipse whose latus

rectum is one third of the major axis.

Watch Video Solution

94. A rod AB of length 15cm rests in between two coordinate axes in such a way that the end

point A lies on $x - a\xi s$ and end point B lies on $y - a\xi s$. A point is taken on the rod in such a way that AP = 6cm. Show that the locus of P is an ellipse. Also find its eccentricity.



Watch Video Solution

96. The equation of the directrix of a hyperbola is

x-y+3=0. Its focus is (-1,1) and eccentricity

3. Find the equation of the hyperbola.



97. Find the equation of the hyperbola whose conjugate axis is 5 and the distance between the foci is 13.

98. Find the equation of the hyperbola having foci

 $(0, \pm 4)$ and transverse axis of length. 6.



vertices at $(0, \ \pm 6)$ and $e=rac{5}{3}$

Watch Video Solution

100. In each of the following find the equations of

the hyperbola satisfying he given condition:



103. find the equation of hyperbola having Vertices ($\pm 2, 0$) and $foci(\pm 3, 0)$

Watch Video Solution

104. Find the equations of the hyperbola satisfying the given conditions :Foci (\pm 4, 0), the latus rectum is of length 12

105. find the equation of hyperabola where foci are (0,12) and (0,-12)and the length of the latus rectum is 36



106. Find the equations of the hyperbola satisfying the given conditions :Foci $(\pm 3\sqrt{5}, 0)$, the latus rectum is of length 8.

107. Foci $(0, \pm 13)$ the conjugate axis is length

24.



108. Find the equations of the hyperbola satisfying the given conditions :Foci (\pm 5, 0), the transverse axis is of length 8.



109. Find the equation of the hyperbola having vertices $(\pm 7, 0)$ and $e = \frac{4}{3}$.

Watch Video Solution

110. Find the equation of the hyperbola whose vertices are $(\pm 7, 0)$ and $e = \frac{4}{3}$.

Watch Video Solution

111. if in a hyperbola the eccentricity is $\sqrt{3}$ and the distance between the foci is 9 then the equation



the equation of the hyperbola.





114. Find the equation to the hyperbola referred to its axes as coordinate axes whose conjugate axis is 7 and passes through the point (3, -2).



115. In the hyperbola $4x^2 - 9y^2 = 36$, find the axes, the coordinates of the foci, the eccentricity, and the latus rectum.

116. Find the coordinates of the vertices, the foci,

the eccentricity and the equations of directrices

of the hyperbola $4x^2 - 25y^2 = 100$.



117. Find the coordinates to the vertices, the foci, the eccentricity and the equation of the directrices of the hyperbola : $3x^2 - 2y^2 = 1$

118. Find the eccentricity, coordinates of the foci equations of directrices and length of the latus rectum of the hyperbola $16x^2 - 9y^2 = 144$

Watch Video Solution

119. Find the coordinates to the vertices, the foci, the eccentricity and the equation of the directrices of the hyperbola : $16y^2 - 4x^2 = 1$

120. Find the coordinates to the vertices, the foci, the eccentricity and the equation of the directrices of the hyperbola : $y^2 - 16x^2 = 16$.

Watch Video Solution

121. Find the coordinates of the foci and the vertices, the eccentricity and the length of the latus rectum of the hyperbolas. $16x^2 - 9y^2 = 576$

122. Find the coordinates of the foci and the vertices, the eccentricity and the length of the latus rectum of the hyperbolas. $49y^2 - 16x^2 = 784$

Watch Video Solution

123. Find the foci, vertices, eccentricity and length

of latus rectum of the hyperbola : $3y^2 - x^2 = 27$.

124. Find the coordinates of the foci and the vertices, the eccentricity and the length of the latus rectum of the hyperbolas. $5y^2 - 9x^2 = 36$



125. Find the foci, vertices, eccentricity and length

of latus rectum of the hyperbola : $rac{y^2}{4} - rac{x^2}{9} = 1.$

126. Find the centre, eccentricity, foci and directrices of the hyperbola : $16x^2 - 9y^2 + 32x + 36y - 164 = 0$

Watch Video Solution

127. Show that the equation $9x^2 - 16y^2 - 18x - 64y - 199 = 0$ represents a hyperbola. Fof this hyperbola, find the length of axes, eccentricity, centre, foci, vertices, latus rectum and directrices.



128. Find the length of axes, eccentricity, centre, foci and latus rectum of the hyperbola $16x^2 - 3y^2 - 32x - 12y - 44 = 0.$



129. Foot of perpendicular from point P on hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ to its transverse axis is N. If A and A' are vartices of hyperbola and Q divides AP in the ratio $a^2 : b^2$, then prove that NQ is perpendicular to A'P. Vertix A is near to point P.



130. Prove that the locus of the point of intersection of the lines $\sqrt{3}x - y - 4\sqrt{3}k = 0$ and $\sqrt{3}kx + ky - 4\sqrt{3} = 0$, for different values of k, is a hyperbola whose eccentricity is 2.