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## MATHS

## BOOKS - KC SINHA ENGLISH

## CONIC SECTIONS - FOR BOARDS

## Solved Examples

1. Find the equation of the parabola whose: focus
is $(1,1)$ and the directrix is $x+y=1=0$

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2. Find the equation of the parabola whose focus
is $(1,-1)$ and whose vertex is 2,1 . Also, find its axis and latus-rectum.

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3. Find the focus and the equation of the parabola whose vertex is $(6,-3)$ and directrix is

$$
3 x-5 y+1=0
$$

4. Find the equation of the parabola whose focus is $(1,1)$ and equation of directrix is $x+y=1$.

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5. Find the equation of the parabola which is symmetric about the $y$-axis, and passes through the point $(2,-3)$.

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6. Find the equation of the parabola whose axis is parallel to $x$-axis and which passes through points
$(0,0),(1,1)$ and $(2,3)^{`}$

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7. Find the equation of the parabola whose latusrectum is 4units, axis is the line $3 x+4 y-4=0$ and the tangent at the vertex is the line $4 x-3+7=0$.
8. Find the equation of the parabola the extremities of whose latus rectum are (1,2) and (1, -4).

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9. The equation of the parabola whose vertex and
focus lie on the axis of $x$ at distances $a$ and $a_{1}$
from the origin, respectively, is

$$
\begin{align*}
& y^{2}-4\left(a_{1}-a\right) x \text { (b) } y^{2}-4\left(a_{1}-a\right)(x-a)  \tag{a}\\
& y^{2}-4\left(a_{1}-a\right)(x-a) \text { (d) none }
\end{align*}
$$

10. Find the axis, vertex, tangent at the vertex, focus, directrix and length of latus rectum of the parabola $x^{2}=-16 y$.

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11. Find the vertex, focus, directrix and length of the latus rectum of the parabola
$y^{2}-4 y-2 x-8=0$
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12. Find the vertex, axis, focus, directrix, tangent at the vertex, and length of the latus rectum of the parabola $2 y^{2}+3 y-4 x-3=0$.

## (D) Watch Video Solution

13. The focal distance of a point on the parabola $y^{2}=12 \xi s 4$. Find the abscissa of this point.
14. Find the axis, tangent at the vertex, vertex, focus, directrix and latus rectum of the parabola $9 y^{2}-16 x-12 y-57=0$

## D Watch Video Solution

15. Find the angle made by a double ordinate of
length $8 a$ at the vertex of the parabola $y^{2}=4 a x$.

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16. An equilateral trinalge is inscribed in the parabola $y^{2}=-8 x$, where one vertex is at the vertex of the parabola. Find the length of the side of the tringle.

## D Watch Video Solution

17. Find the area of the triangle formed by the lines joining the vertex of the parabola $x^{2}=-36 y$ to the ends of the latus rectum.

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18. If $y_{1}, y_{2}, y_{3}$ be the ordinates of a vertices of the triangle inscribed in a parabola $y^{3}=4 a x$, then show that the area of the triangle is $\frac{1}{8 a}\left|\left(y_{1}-y_{2}\right)\left(y_{2}-y_{3}\right)\left(y_{3}-y_{1}\right)\right|$.

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19. If a parabolic reflector is 20 cm in diameter and 5 cm deep, find the focus.

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20. An arc is in the form of a parabola with its axis
vertical. The arch is 10 m high and 5 m wide at the
base. How high is it 2 m from the vertex of the parabola?

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21. The cable of a uniformly loaded suspension bridge hangs in the form of a parabola. The roadway which is horizontal and 100 m long is supported by vertical wires attached to the cable,
the longest wire being 30 m and the shortest
being 6 m . Find the length of the supporting wire attached to the roadway 18 m from the middle.

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22. Obtain the equation of the ellipse whose
focus is the point ( $-1,1$ ), and the corresponding directrix is the line $x-y+3=0$, and the eccentricity is $\frac{1}{2}$.
23. Find the equation of the ellipse whose axes are parallel to the coordinate axes having its
centre at the point $(2,-3)$ one focus at $(3,-3)$ and vertex at $(4,-3)$.

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24. Find the equation of the ellipse, with major axis along the $x$-axis and passing through the points $(4,3)$ and ( $-1,4$ ).

## 25. Find the equation of the ellipse whose foci are

 $(2,3),(-2,3)$ and whose semi-minor axes is $\sqrt{5}$
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26. Find the equation of the ellipse the extremities of whose minor axis are
$(3,1)$ and $(3,5)$ and whose eccentricity is $\frac{1}{2}$.

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27. The equation of the ellipse with its centre at
$(1,2)$, one focus at $(6,2)$ and passing through the point $(4,6)$ is-

## D Watch Video Solution

28. Find the equation of the ellipse whose axes
are along the coordinate axes, foci at $(0, \pm 4)$
and eccentricity $4 / 5$.

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29. Find the equation of an ellipse the distance between the foci is 8 units and the distance between the directrices is 18 units.

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30. Find the equation of the ellipse with foci at $( \pm 5,0) a n d x=\frac{36}{5}$ as one of the directrices.
31. Find the equation of the ellipse that passes through the origin and has the foci at the points $(-1,1)$ and $S^{\prime}(1,1)$.

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32. Find the length and equation of major and minor axes, centre, eccentricity, foci, equation of directrices, vertices and length of latus rectum of
the ellipses: $\frac{x^{2}}{225}+\frac{y^{2}}{289}=1$

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33. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the eccentricity and the length of the latus rectum of the ellipse. $16 x^{2}+y^{2}=16$

## (D) Watch Video Solution

34. For the ellipse
$12 x^{2}+4 y^{2}+24 x-16 y+25=0 \quad$ centries
$(-1,2) \mathrm{b}$. lengths of the axes are $\sqrt{3}$ and 1 c .
eccentricity $=\sqrt{\frac{2}{3}}$ d. all of these
35. Find the latus rectum, the eccentricity and coordinates of the foci of the ellipse $9 x^{2}+5 y^{2}+30 y=0$.

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36. A rod of length 12 cm moves with its ends always touching the coordinate axes. Determine the equation of the locus of a point $P$ on the rod, which is 3 cm from the end in contact with the x axis.
37. A rod $A B$ of length 15 cm rests in between two coordinate axes in such a way that the end point $A$ lies on $x-a \xi s$ and end point $B$ lies on $y-a \xi s$. A point is taken on the rod in such a way that $A P=6 \mathrm{~cm}$. Show that the locus of $P$ is an ellipse. Also find its eccentricity.

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38. An arch way is in the shape of a semi-ellipse,
the road level being the major axis. If the breadth
of the arch way is 30 feet and a man 6 feet tall just touches the top when 2 feet from the side, find the greatest height of the arch.

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39. An arc is in the form of a semi-ellipse. It is $8 m$
wide and $2 m$ high at the centre. Find the height of the arch at a point 1.5 cm from one end.

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40. A man running a racecourse notes that the sum of the distances from the two flag posts from him is always 10 m and the distance between the flag posts is 8 m . Find the equation of the posts traced by the man.

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41. Find the equation of the hyperbola whose one directrix is $2 x+y=1$, the corresponding focus is $(1,2)$ and eccentricity is $\sqrt{3}$
42. Find the equation of the hyperbola having $e=32$ and foci at $( \pm 3,0)$

## (D) Watch Video Solution

43. Find the equation of the hyperbola having eccentricity $e=\frac{4}{3}$ and vertices at $(0, \pm 7)$.

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44. Find the equation of the hyperbola, the length of whose latus rectum is 8 , eccentricity is 3 $\frac{3}{\sqrt{5}}$ and whose transverse and conjugate axes are along the $x$ and $y$ axes respectively.

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45. Find the equation of the hyperbola having
vertices at $( \pm 5,0)$ and foci at $( \pm 7,0)$

## D Watch Video Solution

46. Find the equation of the hyperbola whose eccentricity is $\sqrt{2}$ and the distance between the
foci is 16 , taking transverse and conjugate axes of
the hyperbola as $x$ and $y$-axes respectively.

## D Watch Video Solution

47. Referred to the principal axes as the axes of coordinates find the equation of the hyperbola whose foci are at $(0, \pm \sqrt{10})$ and which passes through the point $(2,3)$.
48. Find the equation of the hyperbola for which the distance between focie is $32, e=2 \sqrt{2}$ and transverse and conjugate axes are along $x$ and $y$-axes respectively.

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49. The foci of a hyperbola coincide with the foci
of the ellipse $\frac{x^{2}}{25}+\frac{y^{2}}{9}=1$. Find the equation of the hyperbola, if its eccentricity is 2 .
50. Find the length of the transverse axis, conjugate axis, eccentricity, vertices, foci and directrices of the hyperbola $9 x^{2}-16 y^{2}=144$.

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51. Find the length of axes of the ellipse whose eccentricity is $4 / 5$ and whose foci coincide with those of the hyperbola $9 x^{2}-16 y^{2}+144=0$
52. Find the length of the transverse and conjugate axes, eccentricity, centre, foci and directrices of the hyperbola.
$9 x^{2}-16 y^{2}-72 x+96 y-144=0$

## (D) Watch Video Solution

53. Find the centre, eccentricity and foci of the hyperbola, $9 x^{2}-16 y^{2}-18 x-64 y-199=0$
54. If eande' the eccentricities of a hyperbola and its conjugate, prove that $\frac{1}{e^{2}}+\frac{1}{e^{n}}=1$.

## (D) Watch Video Solution

55. If $S$ and $S^{\prime \prime}$ are the foci, C is the centre, and $P$ is a point on a rectangular hyperbola, show that $S P \times S^{\prime} P=\left(C P_{2}\right)$.
56. Find the equation of the locus of all points such that difference of their distances from $(4,0)$ and $(-4,0)$ is always equal to 2.

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## Exercise

1. Find the equaiton of the parabola whose focus
is $(0,-2)$ and directrix is $y=2$.
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2. Find the equaiton of the parabola whose focus is $(0,-3)$ and directrixisy $=3^{\prime}$.

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3. Find the equaiton of the parabola whose focus
is $(4,0)$ and directrix is $x=-4$

## (D) Watch Video Solution

4. Find the equation of parabola whose focus is
$(6,0)$ and directrix $x=-6$.

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5. Find the equation of the parabola with focus (2,

0 ) and directrix $x=-2$.

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6. Find the equation of the parabola whose focus
is $(-1,2)$ and directrixis $\mathrm{x}-2 \mathrm{y}-15=0$ '.
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7. Find the equation of the parabola whose focus is $(2,3)$ and directrix is $x-2 y-6=0$.

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9. Find the equation of the parabola whose focus
is at $(-1,1)$ and the directrix is $x+y+1=0$.
10. Find the equation of the parabola whose focus
is $(5,3)$ and directrix is the line $3 x-4 y+1=0$.

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11. Find the equation of the parabola if the focus is the point $\left(\frac{5}{4},-1\right)$ and the directrix is $4 x-13=0$.
12. Find the equation of the parabola having ther vertex at $(0,1)$ and the focus at $(0,0)$.

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13. Find the equation of the parabola with vertex at $(0,0)$ and focus at $(0,2)$.

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14. about to only mathematics
15. Find the equation of the parabola whose focus is $(3,0)$ and vertex is $(0,0)$.

## D Watch Video Solution

16. Find the equation of the parabola having vertex at $(0,0)$ and focus at $(-2,0)$.
17. Find the equation of the parabola passing through $(5,2)$, having vertex at $(0,0)$ and symmetric about $y$-axis.

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18. about to only mathematics

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19. Find the equation of the parabola whose focus is at $(0,0)$ and vertex is at the intersection of the
line $x+y=1$ and $x-y=3$.

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20. Prove that the equation of the parabola whose focus is $(0,0)$ and tangent at the vertex is
$x-y+1=0$
$x^{2}+y^{2}+2 x y-4 x+4 y-4=0$.

## (D) Watch Video Solution

21. Find the equation of the parabola with vertex
is at $(2,1)$ and the directrix is $x=y-1$.

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22. Find the equatin to the parabola whose axis is parallel to the $y$-xis and which passes through the point $(0,4),(1.9), \quad$ and
its latus rectum.
determine its latus rectum.

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23. Equation of parabola which has its axis along $x$-axis and which passes through the points $(3,2)$ and $(-2,-1)$ is
24. Find the equation of a parabola whose end points of latus rectum are $(3,5)$ and $(3,-3)$.

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25. Find the equation of the parabola with its axis parallel to $x$-axis and which passes through the points $(1,2),(-1,3)$ and $(-2,1)$.
26. For each of that parabolas, find the coordinates of the focus, the equation of the directrix and the length of latus rectum : $x^{2}=6 y$

## (D) Watch Video Solution

27. Find the coordinates of the focus, axis, the equation of the directrix and latus rectum of the parabola $y^{2}=8 x$.
28. For the following parabola find the coordinates of the focus, the equation of the directrix and the length of the latus rectum. $y^{2}=12 x$

## D Watch Video Solution

29. For each of that parabolas, find the coordinates of the focus, the equation of the directrix and the length of latus rectum : $x^{2}=-9 y$
30. For each of that parabolas, find the coordinates of the focus, the equation of the directrix and the length of latus rectum : $y^{2}=-12 x$

## D Watch Video Solution

31. For each of that parabolas, find the coordinates of the focus, the equation of the directrix and the length of laius rectum : $y^{2}=10 x$
32. For each of that parabolas, find the coordinates of the focus, the equation of the directrix and the length of latus rectum : $y^{2}=-8 x$

## D Watch Video Solution

33. Find the coordinates of the focus, axis of the parabola, the equation of the directrix and the length of the latus rectum. $x^{2}=6 y$
34. Find the vertex, focus, axis, directrix and latusrectum of the parabola
$4 y^{2}+12 x-20 y+67=0$.

## D Watch Video Solution

35. Find the vertex, focus, axis, directrix and latus rectum of that parabola : $(y-2)^{2}=3(x+1)$
36. Find the vertex, focus, axis, directrix and latus rectum of that parabola : $y^{2}-3 x-2 y+7=0$

## (D) Watch Video Solution

37. Find the vertex, focus, axis, directrix and latus rectum of that parabola : $y^{2}-3 x-2 y+7=0$

## (D) Watch Video Solution

38. Find the focus and directrix of the parabola $3 x^{2}+12 x+8 y=0$.
39. Find the equation of the parabola with focus
(5, 0), and directrix $x=-5$. Also, find the length of the latus rectum.

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40. Find the equation of the circle described on the line segment as diameter joining the foci of the parabolas $x^{2}=4 a y$ and $y^{2}=4 a(x-a)$ as diameter.
41. An equilateral triangle is inscribed in the parabola $y^{2}=4 a x$ whose vertex is at of the parabola. Find the length of its side.

## (D) Watch Video Solution

42. Find the area of the triangle formed by the
lines joining the vertex of the parabola $x^{2}=12 y$ to the ends of its latus-rectum.
43. $P Q$ is a double ordinate of a parabola $y^{2}=4 a x$. Find the locus of its points of trisection.

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44. The focus of a parabolic mirror as shown in the figure alongside is at a distance of 6 cm from its vertex. If the mirror is 20 cm deep, find the distance $B C$.
45. A water jet from a function reaches it maximum height of 4 m at a distance 0.5 m from the vertical passing through the point $O$ of water outlet. The height of the jet above the horizontal
$O X$ at a distance of 0.75 m from the point $O$ is 5 m (b) 6 m (c) 3 m (d) 7 m

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46. about to only mathematics
47. Obtain the equation of the ellipse whose
focus is the point $(-1,1)$, and the corresponding directrix is the line $x-y+3=0$, and the eccentricity is $\frac{1}{2}$.

## D Watch Video Solution

48. Find the equation of the ellipse whose: One focus is $(6,7)$, directrix is $x+y+2$ and eccentricity is $\frac{1}{\sqrt{3}}$
49. Find the equation to the ellipse whose one
focus is ( 2,1 ), the directrix is $2 x-y+3=0$ and
the eccentricity is $\frac{1}{\sqrt{2}}$

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50. Find the equation of the ellipse with centre at the origin, the length of the major axis 12 and one focus at (4, 0).
(D) Watch Video Solution
51. Find the equation of the ellipse whose centre is $(-2,3)$ and whose semi axis are 3 and 2 when major axis is i. parallel to $x$-axis ii. parallel to $y$-axis.

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52. Find the equation of an ellipse whose vertices
are $(0, \pm 10)$ and eccentricity $e=\frac{4}{5}$

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53. Find the equation for the ellipse that satisfies
the given conditions:Vertices $(0, \pm 13)$, foci
$(0, \pm 5)$

## D Watch Video Solution

54. Find the equation of ellipse whose vetices are
$(p, 5,0)$ and foci are $( \pm 4,0)$
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55. Find the equation of the ellipse whose vertices are $( \pm 13,0)$ and foci are $( \pm 5,0)$.

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56. Find the equation of the ellipse whose vetices
are $( \pm 6,0)$ and foci are $( \pm 4,0)$.
(D) Watch Video Solution
57. Find the equation of the ellipse having, length of major axis 26 and foci $( \pm 5,0)$

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58. Find the equation of the ellipse, whose length of the major axis is 20 and foci are $(0, \pm 5)$.

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59. Find the equation of the ellipse having, length of major axis 8 and foci $( \pm 3,0)$
(D) Watch Video Solution
60. Find the equation of the ellipse having, length of major axis 16 and foci $(0, \pm 6)$

## (D) Watch Video Solution

61. Find the equation of the ellipse passing through the point $(3,2)$, having centre at $(0,0)$ and major axis on $y$-axis.
62. Find the equation for the ellipse that satisfies the given conditions: Ends of major axis $(0, \pm \sqrt{5})$, ends of minor axis $( \pm 1,0)$

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63. If $a$ be the length of semi-major axis, $b$ the
length of semi-minor axis and $c$ the distance of one focus from the centre of an ellipse, then find the equation of the ellipse for which centre is ( 0 ,
$0)$, foci is on x -axis, $b=3$ and $c=4$.
64. The distance between the foci of an ellipse is

10 and its lactusrectum is 15 , find its equation reffered to its axes as axes of cordinates.

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65. find the equation of the ellipse refer refer to it

Centre whose major axis is equal to distance between the foci and latus rectum is 10 .

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66. The eccentricity of an ellipse is $\frac{1}{2}$ and the distance between its foci is 4 units. If the major and minor axes of the ellipse are respectively along the $x$ and $y$ axes, find the equation of the ellipse

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67. Find the equation of the ellipse passing through ( 6,4 ), foci on $y$-axis, centre at the origin and having eccentricity $\frac{3}{4}$.
68. Find the equation of the ellipse passing through $(4,1)$ with focus as $( \pm 3,0)$

## (D) Watch Video Solution

69. Find the equation of the set of all points
whose distance from $(0,4)$ are $\frac{2}{3}$ of their distance from the line $\mathrm{y}=9$.
(D) Watch Video Solution
70. Find the equation of the ellipse whose foci re $(4,0)$ and ( $-4,0$ ) eccentricity $=1 / 3$.

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71. Find the equation to the ellipse (referred to its axes as the axes of $x$ and $y$ respectively) which passes through the point $(-3,1)$ and has eccentricity $\sqrt{\frac{2}{5}}$
72. If the angle between the lines joining the foce of any ellipse to an extremity of the minor axis is $90^{\circ}$, find the accentricity. Find also the equation of the ellipse if the major axis is $2 \sqrt{2}$.

## D Watch Video Solution

73. For the ellipse $9 x^{2}+16 y^{2}=144$, find the length of the major and minor axes, the eccentricity, the coordinatse of the foci, the vertices and the equations of the directrices.
74. Find the lengths of the major and the minor axes, the coordinates of the foci, the vertices, the eccentricity, the length of latus rectum and the eqatuion of the directrices of that ellipses : $\frac{x^{2}}{169}+\frac{y^{2}}{25}=1$

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75. Find the lengths of the major and the minor axes, the coordinates of the foci, the vertices, the eccentricity, the length of latus rectum and the
eqatuion of the directrices of that ellipses :
$\frac{x^{2}}{25}+\frac{y^{2}}{169}=1$

## - Watch Video Solution

76. Find the lengths of the major and the minor axes, the coordinates of the foci, the vertices, the eccentricity, the length of latus rectum and the eqatuion of the directrices of that ellipses : $3 x^{2}+2 y^{2}=18$

## D Watch Video Solution

77. Find the lengths of the major and the minor axes, the coordinates of the foci, the vertices, the eccentricity, the length of latus rectum and the eqatuion of the directrices of that ellipses : $x^{2}+16 y^{2}=16$.

## (D) Watch Video Solution

78. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the eccentricity and the length of the latus rectum of the ellipse. $4 x^{2}+9 y^{2}=36$
79. Find the coordinates of the foci, the vertices, the length of major axis, the minor axis, the eccentricity and the length of latus rectum of that ellipses: $9 x^{2}+4 y^{2}=36$

## (D) Watch Video Solution

80. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the
eccentricity and the length of the latus rectum of the ellipse. $36 x^{2}+4 y^{2}=144$

## (D) Watch Video Solution

81. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the eccentricity and the length of latus rectum of that ellipses: $25 x^{2}+4 y^{2}=100$

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82. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the eccentricity and the length of the latus rectum of
the ellipse. $\frac{x^{2}}{100}+\frac{y^{2}}{400}=1$

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83. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the eccentricity and the length of latus rectum of
that ellipses: $\frac{x^{2}}{25}+\frac{y^{2}}{9}=1$
84. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the eccentricity and the length of the latus rectum of
the ellipse. $\frac{x^{2}}{25}+\frac{y^{2}}{100}=1$

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85. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the
eccentricity and the length of the latus rectum of
the ellipse. $\frac{x^{2}}{49}+\frac{y^{2}}{36}=1$

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86. Find the coordinates of the foci, the vertices,
the length of major axis, the minor axis, the eccentricity and the length of latus rectum of
that ellipses: $\frac{x^{2}}{25}+\frac{y^{2}}{100}=1$

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87. Show that the following equation represents
an ellipse and find its centre and eccentricity :
$8 x^{2}+6 y^{2}-16 x+12 y+13=0$

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88. Find the centre, the length of the axes and the accentricity of the ellipse
$x^{2}+3 y^{2}-4 x-12 y+13=0$

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> 89. Eccentricity of the ellipse
> $4 x^{2}+y^{2}-8 x+2 y+1=0$ is

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90. Find the latus rectum, eccentricity, coordinates of the foci and the length of axes of that ellipses : $9 x^{2}+5 y^{2}-30 y=0$

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91. Find the latusrectum,eccentricity,coordinates
of the foci,coordinates of the vertices, the length of the axes and the centre of the ellipse

$$
4 x^{2}+9 y^{2}-8 x-36 y+4=0
$$

92. Find the eccentricity of an ellipse if its latus rectum is equal to one-half of its major axis.

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93. Find the eccentricity of the ellipse whose latus rectum is one third of the major axis.

## (D) Watch Video Solution

94. A rod $A B$ of length 15 cm rests in between
two coordinate axes in such a way that the end
point $A$ lies on $x-a \xi s$ and end point $B$ lies on $y-a \xi s$. A point is taken on the rod in such a way that $A P=6 \mathrm{~cm}$. Show that the locus of $P$ is an ellipse. Also find its eccentricity.

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95. Find the equation of the hyperbola whose :
focus is $(2,2)$ directrix is $x+y=9$ and eccentricity $=2$.

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96. The equation of the directrix of a hyperbola is $x-y+3=0$. Its focus is ( $-1,1$ ) and eccentricity
97. Find the equation of the hyperbola.

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97. Find the equation of the hyperbola whose
conjugate axis is 5 and the distance between the foci is 13 .

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98. Find the equation of the hyperbola having foci ( $0, \pm 4$ ) and transverse axis of length. 6 .

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99. Find the equation of the hyperbola with
vertices at $(0, \pm 6)$ and $e=\frac{5}{3}$

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100. In each of the following find the equations of the hyperbola satisfying he given condition:
vertices $(0, \pm 5)$ ficu $(0, \pm 8)$

## (D) Watch Video Solution

101. Find the equation of the hyperbola having :
vertices $(0, \pm 3)$ and foci $(0, \pm 5)$.

## D Watch Video Solution

102. Find the equation of the hyperbola with foci
$(0, \pm 3)$ and vertices $\left(0, \pm \frac{\sqrt{11}}{2}\right)$
103. find the equation of hyperbola having Vertices $( \pm 2,0)$ and $\operatorname{foci}( \pm 3,0)$

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104. Find the equations of the hyperbola satisfying the given conditions :Foci $( \pm 4,0)$, the latus rectum is of length 12
105. find the equation of hyperabola where foci are $(0,12)$ and $(0,-12)$ and the length of the latus rectum is 36

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106. Find the equations of the hyperbola satisfying the given conditions :Foci $( \pm 3 \sqrt{5}, 0)$, the latus rectum is of length 8 .

# 107. Foci $(0, \pm 13)$ the conjugate axis is length 

 24.
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108. Find the equations of the hyperbola satisfying the given conditions :Foci $( \pm 5,0)$, the transverse axis is of length 8.

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109. Find the equation of the hyperbola having
vertices $( \pm 7,0)$ and $e=\frac{4}{3}$.

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110. Find the equation of the hyperbola whose vertices are $( \pm 7,0)$ and $e=\frac{4}{3}$.

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111. if in a hyperbola the eccentricity is $\sqrt{3}$ and the
distance between the foci is 9 then the equation
of hyperbola in the standard form is:

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112. The equation of the hyperbola, whose foci are
$(6,4)$ and $(-4,4)$ and eccentricity is 2 , is

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113. The coordinates of the foci of a hyperbola are
$( \pm 6,0)$ and its latus rectum is of 10 units. Find the equation of the hyperbola.
114. Find the equation to the hyperbola referred to its axes as coordinate axes whose conjugate axis is 7 and passes through the point $(3,-2)$.

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115. In the hyperbola $4 x^{2}-9 y^{2}=36$, find the axes, the coordinates of the foci, the eccentricity, and the latus rectum.
116. Find the coordinates of the vertices, the foci, the eccentricity and the equations of directrices of the hyperbola $4 x^{2}-25 y^{2}=100$.

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117. Find the coordinates to the vertices, the foci, the eccentricity and the equation of the directrices of the hyperbola : $3 x^{2}-2 y^{2}=1$

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118. Find the eccentricity, coordinates of the foci equations of directrices and length of the latus rectum of the hyperbola $16 x^{2}-9 y^{2}=144$

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119. Find the coordinates to the vertices, the foci, the eccentricity and the equation of the directrices of the hyperbola : $16 y^{2}-4 x^{2}=1$

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120. Find the coordinates to the vertices, the foci, the eccentricity and the equation of the directrices of the hyperbola : $y^{2}-16 x^{2}=16$.

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121. Find the coordinates of the foci and the vertices, the eccentricity and the length of the latus rectum of the hyperbolas. $16 x^{2}-9 y^{2}=576$

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122. Find the coordinates of the foci and the vertices, the eccentricity and the length of the latus rectum of the hyperbolas.
$49 y^{2}-16 x^{2}=784$
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123. Find the foci, vertices, eccentricity and length of latus rectum of the hyperbola : $3 y^{2}-x^{2}=27$.

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124. Find the coordinates of the foci and the vertices, the eccentricity and the length of the latus rectum of the hyperbolas. $5 y^{2}-9 x^{2}=36$

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125. Find the foci, vertices, eccentricity and length
of latus rectum of the hyperbola : $\frac{y^{2}}{4}-\frac{x^{2}}{9}=1$.
126. Find the centre, eccentricity, foci and directrices of the hyperbola $16 x^{2}-9 y^{2}+32 x+36 y-164=0$

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127. Show that the equation
$9 x^{2}-16 y^{2}-18 x-64 y-199=0$ represents a hyperbola. Fof this hyperbola, find the length of axes, eccentricity, centre, foci, vertices, latus rectum and directrices.
128. Find the length of axes, eccentricity, centre, foci and latus rectum of the hyperbola $16 x^{2}-3 y^{2}-32 x-12 y-44=0$.

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129. Foot of perpendicular from point $P$ on hyperbola $\frac{x^{2}}{a^{2}}-\frac{y^{2}}{b^{2}}=1$ to its transverse axis is $N$. If $A$ and $A$ are vartices of hyperbola and $Q$ divides AP in the ratio $a^{2}: b^{2}$, then prove that NQ is perpendicular to $A^{\prime} P$. Vertix $A$ is near to point $P$.
130. Prove that the locus of the point of intersection of the lines
$\sqrt{3} x-y-4 \sqrt{3} k=0$ and $\sqrt{3} k x+k y-4 \sqrt{3}=0$,
for different values of $k$, is a hyperbola whose eccentricity is 2.

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