



## MATHS

### BOOKS - KC SINHA ENGLISH

### DETERMINANTS - FOR BOARDS

#### Solved Examples

1. Evaluate: 
$$\begin{vmatrix} 219 & 117 & 345 \\ 19 & 9 & 34 \\ 7 & 3 & 6 \end{vmatrix}$$



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2. Show that 
$$\begin{vmatrix} 1 & a & a^2 \\ 1 & b & b^2 \\ 1 & c & c^2 \end{vmatrix} = (a - b)(b - c)(c - a)$$



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3. Prove that 
$$\begin{vmatrix} 1 & a & a^3 \\ 1 & b & b^3 \\ 1 & c & c^3 \end{vmatrix} = (a - b)(b - c)(c - a)(a + b + c)$$

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4. 
$$\begin{vmatrix} x + 1 & x + 2 & x + a \\ x + 2 & x + 3 & x + b \\ x + 3 & x + 4 & x + c \end{vmatrix} = 0$$
 where  $a, b$  and  $c$  are in AP.

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5. Using properties of determinants, prove the following:

$$\begin{vmatrix} 3a & -a + b & -a + c \\ 3b & -b + c & -b + a \\ 3c & -c + a & -c + b \end{vmatrix} = 3(a + b + c)(a^2 + b^2 + c^2 + ab + bc + ca)$$

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6. Solve: 
$$\begin{vmatrix} a & xa & -xa & -xa & -xa & xa & -xa & -xa & -xa & xa \\ xa & a & -xa & -xa & -xa & xa & -xa & -xa & -xa & xa \\ -xa & xa & a & -xa & -xa & xa & a & -xa & -xa & xa \\ -xa & xa & xa & a & -xa & xa & xa & a & -xa & xa \\ -xa & xa & xa & xa & a & xa & xa & xa & a & xa \\ xa & -xa & -xa & -xa & xa & a & -xa & -xa & -xa & xa \\ -xa & -xa & -xa & -xa & xa & xa & a & -xa & -xa & xa \\ -xa & -xa & xa & xa & xa & xa & xa & a & -xa & xa \\ xa & a & xa \\ xa & a \end{vmatrix} = 0$$

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7. Prove the identities:

$$|abc - ab + ac + b| = a^3 + b^3 + c^3 - 3abc$$

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8. Prove that:

$$\begin{vmatrix} \alpha & \beta & \gamma \\ \alpha^2 & \beta^2 & \gamma^2 \\ \beta + \gamma & \gamma + \alpha & \alpha + \beta \end{vmatrix} = (\alpha - \beta)(\beta - \gamma)(\gamma - \alpha)(\alpha + \beta + \gamma).$$

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10. Prove that:  $|(1+a_1, 1, 1), (1, 1+a_2, 1), (1, 1, 1+a_3)| = a_1 a_2 a_3 (1 + 1/a_1 + 1/a_2 + 1/a_3)$

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11. Prove the following, using properties of determinants:

$$|a + b + 2c \quad abc \quad cb + c + 2abc \quad cac + a + 2b| = 2(a + b + c)^3$$

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12. Let  $a, b, c$  be positive and not all equal. Show that the value of the

determinant  $\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$  is negative.

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13. Prove that

$$|aa + ba + b + c \quad 2a \quad 3a + 2B \quad 4a + 3b + 2c \quad 3a \quad 6a + 3b \quad 10a + 6b + 3c| = a^3$$

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14. show that 
$$\begin{vmatrix} 1 & 1+p & 1+p+q \\ 2 & 3+2p & 1+3p+2q \\ 3 & 6+3p & 1+6p+3q \end{vmatrix} = 1$$

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15. Show that

$$|1 + a| |1 + b| |1 + c| = abc \left( 1 + \frac{1}{a} + \frac{1}{b} + \frac{1}{c} \right) = abc + bc + ca + ab$$

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16. prove that 
$$\begin{vmatrix} a^2 + 1 & ab & ac \\ ab & b^2 + 1 & bc \\ ac & bc & c^2 + 1 \end{vmatrix} = 1 + a^2 + b^2 + c^2.$$

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17. Prove that: 
$$\begin{vmatrix} (b+c)^2 & a^2 & a^2 \\ b^2 & (c+a)^2 & b^2 \\ c^2 & c^2 & (a+b)^2 \end{vmatrix} = 2abc(a+b+c)^3$$

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18. If  $2s = a + b + c$  and  $A = \begin{vmatrix} a^2 & (s-a)^2 & (s-a)^2 \\ (s-b)^2 & b^2 & (s-b)^2 \\ (s-c)^2 & (s-c)^2 & c^2 \end{vmatrix}$  is equal to

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19. Prove that identities:

$$|-bc^2 + b^2 + bca^2 + ac - a^2 + aca^2 + a^2 + ab - ab| = (ab + bc + ca)^2$$

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20. Prove that  $\begin{vmatrix} -2a & a+b & a+c \\ b+a & -2b & b+c \\ c+a & c+b & -2c \end{vmatrix} = 4(a+b)(b+c)(c+a)$

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21. Show that: 
$$\begin{vmatrix} b+c & c+a & a+b \\ q+r & r+p & p+q \\ y+z & z+x & x+y \end{vmatrix} = 2 \begin{vmatrix} a & b & c \\ p & q & r \\ x & y & z \end{vmatrix}.$$

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22. Solve the equation: 
$$\begin{vmatrix} 15-x & 1 & 10 \\ 11-3x & 1 & 16 \\ 7-x & 1 & 13 \end{vmatrix} = 0$$

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23. Solve the equation 
$$\begin{vmatrix} a-x & c & b \\ c & b-x & a \\ b & a & c-x \end{vmatrix} = 0$$
 where  $a + b + c \neq 0$ .

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24. find the area of triangle whose vertices are (3,8),(-4,2)and (5,1)

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25. If the area of  $ABC$  formed by  $A(x, y)$ ,  $B(1, 2)$  and  $C(2, 1)$  is 7 square units, then prove that  $x + y = 15$  or  $x + y + 9 = 0$

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26. Examine whether points  $(-8, 3)$ ,  $(2, -2)$  and  $(-4, 1)$  are collinear or not.

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27. (i) Find the equation of line joining  $(1, 2)$  and  $(3, 4)$  using determinants,  
(ii) Find the equation of the line joining  $(3, 1)$  and  $(9, 3)$  using determinants.

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1. Evaluate the following:  $\begin{vmatrix} 7 & 5 \\ -2 & 3 \end{vmatrix}$

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2. Evaluate the following:  $\begin{vmatrix} \cos \alpha & \sin \alpha \\ \sin \alpha & \cos \alpha \end{vmatrix}$

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3. Evaluate the following:  $\begin{vmatrix} \tan \alpha & \sec \alpha \\ \sin \alpha & \cot \alpha \end{vmatrix}$

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4. Evaluate the following:  $|\cos \theta, -\sin \theta|, [\sin \theta, \cos \theta]$

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5. Evaluate the following:  $\begin{vmatrix} \frac{1}{2} & \frac{1}{5} \\ \frac{1}{2} & \frac{1}{7} \end{vmatrix}$



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6. Evaluate the following:  $\begin{vmatrix} x^2 - x & x - 1 \\ x + 1 & x + 1 \end{vmatrix}$



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7. Write the value of  $\begin{vmatrix} a + ib & c + id \\ -c + id & a - ib \end{vmatrix}$ .



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8. Evaluate the following:  $\begin{vmatrix} \frac{1}{2} & 8 \\ 4 & 2 \end{vmatrix}$



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9. If  $A = [1242]$ , then show that  $|2A| = 4|A|$ .



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10. If  $A = \begin{bmatrix} 2 & 4 \\ -5 & -1 \end{bmatrix}$  show that:  $|3A| = 9|A|$

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11. Write the minor and cofactor of each element of second column in the

following determinants and evaluate them:  $\begin{vmatrix} 4 & 9 & 7 \\ 3 & 5 & 7 \\ 5 & 4 & 5 \end{vmatrix}$

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12. Write the minor and cofactor of each element of second column in the

following determinants and evaluate them:  $\begin{vmatrix} 1 & 2 & 4 \\ 1 & 3 & 9 \\ 1 & 4 & 16 \end{vmatrix}$

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13. Write the cofactor of  $a_{12}$  in the matrix  $\begin{bmatrix} 2 & -3 & 5 \\ 6 & 0 & 4 \\ 4 & 5 & -7 \end{bmatrix}$

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14. Write the minor and cofactor of each element of the following determinants and also evaluate the determinant in each case:  $\begin{vmatrix} 5 & -10 \\ 0 & 3 \end{vmatrix}$

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15. Write the minor and cofactor of each element of the following determinants and also evaluate the determinant in each case:

$$\begin{vmatrix} 1 & 3 & -2 \\ 4 & -5 & 6 \\ 3 & 5 & 2 \end{vmatrix}$$

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16. Write the minor and cofactor of each element of the following determinants and also evaluate the determinant in each case:  $\begin{vmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{vmatrix}$

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17. Evaluate the following: 
$$\begin{vmatrix} 1 & 5 & 7 \\ 6 & 7 & 2 \\ 1 & 2 & 3 \end{vmatrix}$$

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18. Evaluate the following: 
$$\begin{vmatrix} 1^2 & 2^2 & 3^2 \\ 2^2 & 3^2 & 4^2 \\ 3^2 & 4^2 & 5^2 \end{vmatrix}$$

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19. Evaluate the following: 
$$\begin{vmatrix} a & h & g \\ h & b & f \\ g & f & c \end{vmatrix}$$

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20. Evaluate the following: 
$$\begin{vmatrix} 43 & 3 & 6 \\ 35 & 21 & 4 \\ 17 & 9 & 2 \end{vmatrix}$$





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21. Evaluate the following:

$$\begin{vmatrix} 9 & 9 & 12 \\ 1 & 3 & -4 \\ 1 & 9 & 12 \end{vmatrix}$$



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22. Evaluate the following:

$$\begin{vmatrix} 42 & 1 & 6 \\ 28 & 7 & 4 \\ 14 & 3 & 2 \end{vmatrix}$$



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23. Evaluate the following:

$$\begin{vmatrix} 3 & -4 & 5 \\ 1 & 1 & -2 \\ 2 & 3 & 1 \end{vmatrix}$$



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24. Evaluate the following:

$$\begin{vmatrix} 2 & -1 & -2 \\ 0 & 2 & -1 \\ 3 & -5 & 0 \end{vmatrix}$$



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26. Evaluate the following: 
$$\begin{vmatrix} 0 & 1 & 2 \\ -1 & 0 & -3 \\ -2 & 3 & 0 \end{vmatrix}$$



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27. Evaluate the determinant  $\Delta = \begin{vmatrix} 1 & 2 & 4 \\ -1 & 3 & 0 \\ 4 & 1 & 0 \end{vmatrix}$



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28. Evaluate the following: If  $A = \begin{bmatrix} 1 & 1 & -2 \\ 2 & 1 & -3 \\ 5 & 4 & -9 \end{bmatrix}$  find  $|A|$



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29. If  $A = [101012004]$ , then show that  $|3A| = 27|A|$



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30. Evaluate the following: 
$$\begin{vmatrix} 1 & 1 & 1 \\ 1 & 1+x & 1 \\ 1 & 1 & 1+y \end{vmatrix}$$



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31. Evaluate the following: 
$$\begin{vmatrix} 1 & a & bc \\ 1 & b & ca \\ 1 & c & ab \end{vmatrix}$$



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32. Evaluate the following: 
$$\begin{vmatrix} x+\lambda & x & x \\ x & x+\lambda & x \\ x & x & x+\lambda \end{vmatrix}$$



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33. Evaluate the following: 
$$\begin{vmatrix} 1 & a^2 - bc \\ 1 & b & b^2 - ac \\ 1 & c & c^2 - ab \end{vmatrix}$$



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34. Evaluate the following: 
$$\begin{vmatrix} 1 & 1 & 1 \\ \alpha & \beta & \gamma \\ \beta\gamma & \gamma\alpha & \alpha\beta \end{vmatrix}$$



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35. Prove that :  $|a^22a + 112a + 1a + 21331| = (a - 1)^3$



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36. Evaluate the following 
$$\begin{vmatrix} 1 & 1 & 1 \\ a^2 & b^2 & c^2 \\ a^3 & b^3 & c^3 \end{vmatrix}$$



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37. Evaluate the following: 
$$\begin{vmatrix} a & b & c \\ a^2 & b^2 & c^2 \\ a^3 & b^3 & c^3 \end{vmatrix}$$



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38. Show that 
$$\begin{vmatrix} 1 & a & b+c \\ 1 & b & c+a \\ 1 & c & a+b \end{vmatrix} = 0.$$



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39. Prove: 
$$\begin{vmatrix} 0 & b^2 & ac^2 & aa^2 & b0 & c^2 & ba^2 & cb^2 & c0 \end{vmatrix} = 2a^3b^3c^3$$



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40. Evaluate 
$$\begin{vmatrix} 1 & x & y \\ x & x+y & y \\ 1 & x & x+y \end{vmatrix}$$



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41. Evaluate the following:  $|[a, b + c, a^2], [b, c + a, b^2], [c, a + bc^2]|$



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$$42. \begin{vmatrix} b+c & a-b & a \\ c+a & b-c & b \\ a+b & c-a & c \end{vmatrix} =$$



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43. Write the value of the following determinant:

$$|a - - - ab - - aa - bc - aa - - c|$$



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44. Evaluate  $\begin{vmatrix} 1 & \omega & \omega^2 \\ \omega & \omega^2 & 1 \\ \omega^2 & \omega & \omega \end{vmatrix}$  where  $\omega$  is cube root of unity.



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45. If  $a, b, c$ , are in A.P, find value of  
 $|ay + 45y + 78y + a3y + 56y + 89y + b4y + 67y + 910y + c|$



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46. Evaluate  $|xyx + yyx + y \times + yxy|$ .



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47. Show that :  $\begin{vmatrix} x & y & z \\ x^2 & y^2 & z^2 \\ x^3 & y^3 & z^3 \end{vmatrix} = xyz(x - y)(y - z)(z - x)$ .



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48. For a fixed positive integer  $n$ , if  $n!(n+1)!(n+2)!(n+1)!(n+2)!(n+3)!(n+2)!(n+3)!(n+4)!$ , then show that  $\left[ \frac{(n!)^3}{n} - 4 \right]$  is divisible by  $n$ .



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49. Prove: 
$$\begin{vmatrix} 1 & a^2 + bc & a^3 \\ 1 & b^2 + ca & b^3 \\ 1 & c^2 + ab & c^3 \end{vmatrix} = -(a-b)(b-c)(c-a)(a^2 + b^2 + c^2)$$



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50. Q. 
$$\begin{vmatrix} x+y & x & x \\ 15x+4y & 4x & 2x \\ 10x+8y & 8x & 3x \end{vmatrix} = 51x^3$$
 Find the value of  $x$ .



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51. Prove that

$$\begin{vmatrix} b+c & c+a & a+b \\ c+a & a+b & b+c \\ a+b & b+c & c+a \end{vmatrix} = 2(a+b+c)(ab+bc+ca-a^2-b^2-c^2).$$

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52. Using properties of determinant prove that:

$$\begin{vmatrix} 1 & x+y & x^2+y^2 \\ 1 & y+z & y^2+z^2 \\ 1 & z+x & z^2+x^2 \end{vmatrix} = (x-y)(y-z)(z-x)$$

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53. Prove: 
$$\begin{vmatrix} a-b-c & 2a & 2a \\ 2b & b-c-a & 2b \\ 2c & 2c & c-a-b \end{vmatrix} = (a+b+c)^3$$

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54. Using properties of determinant prove that

$$|a + b + c \quad c - b - ca \quad b + c - a - b - aa + b + c| = 2(a + b)(b + c)(c + a)$$

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55. show that

$$\begin{vmatrix} y + z & x & y \\ z + x & z & x \\ x + y & y & z \end{vmatrix} = (x + y + z)(x - z)^2$$

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56. Using properties of determinants, prove the following:

$$|1 \times^2 \quad x^2 1 \quad \times x^2 1| = (1 - x^3)^2$$

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57. Show that:

$$\begin{vmatrix} a & b - c & c + b \\ a + c & b & c - a \\ a - b & b + a & c \end{vmatrix} = (a + b + c)(a^2 + b^2 + c^2).$$

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58. show that 
$$\begin{vmatrix} y+z & x & y \\ z+x & z & x \\ x+y & y & z \end{vmatrix} = (x+y+z)(x-z)^2$$

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59.

Prove:

$$\left| (b+c)^2 a^2 bc (c+a)^2 b^2 ca (a+b)^2 c^2 ab \right| = (a-b)(b-c)(c-a)(a+b+c)$$

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60.

Prove:

$$\begin{vmatrix} a^2 & a^2 - (b-c)^2 & bc \\ b^2 & b^2 - (c-a)^2 & ca \\ c^2 & c^2 - (a-b)^2 & ab \end{vmatrix} = (a-b)(b-c)(c-a)(a+b+c)(a^2 + b^2 + c^2)$$

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61. Show that:  $|b^2 + c^2abacbac^2 + a^2bacba^2 + b^2| = 4a^2b^2c^2$

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62. Prove that:

$$|abax + bycbx + cyaax + bybx + cy0| = (b^2 - ac)(ax^2 + 2bxy + cy^2)$$

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63. Prove that:

$$2x^2 + 2b^2 + 2c^2 - 2ab - 2bc - 2ca = [(a - b)^2 + (b - c)^2 + (c - a)^2]$$

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64. Evaluate 
$$\begin{vmatrix} \cos \alpha \cos \beta & \cos \alpha \sin \beta & -\sin \alpha \\ -\sin \beta & \cos \beta & 0 \\ \sin \alpha \cos \beta & \sin \alpha \sin \beta & \cos \alpha \end{vmatrix}$$

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65. Without expanding, prove that

$$\begin{vmatrix} a + bx & c + dx & p + qx \\ ax + b & cx + d & px + q \\ u & v & w \end{vmatrix} = (1 - x^2) \begin{vmatrix} a & c & p \\ b & d & q \\ u & v & w \end{vmatrix}.$$



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66. Using properties of determinants. Prove that

$$|\sin \alpha \cos \alpha \cos(\alpha + \delta) \sin \beta \cos \beta \cos(\beta + \delta) \sin \gamma \cos \gamma \cos(\gamma + \delta)| = 0$$



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67. Prove that

$$\begin{vmatrix} \sin \alpha & \cos \alpha & \sin(\alpha + \delta) \\ \sin \beta & \cos \beta & \sin(\beta + \delta) \\ \sin \gamma & \cos \gamma & \sin(\gamma + \delta) \end{vmatrix} = 0.$$



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68. Prove that the determinant  $[x \sin \theta \cos \theta - \sin \theta - x \cos \theta \ 1 \ x]$  is independent of  $\theta$ .



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69. For any scalar  $p$  prove that

$$= \begin{vmatrix} x & x^2 & 1 + px^3 \\ y & y^2 & 1 + py^3 \\ z & z^2 & 1 + pz^3 \end{vmatrix} = (1 + pxyz)(x - y)(y - z)(z - x).$$



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70. Without expanding, show that the value of each of the determinants

is zero:  $\begin{vmatrix} \frac{1}{a}a^2bc & \frac{1}{b}b^2ac & \frac{1}{c}c^2ab \end{vmatrix}$



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71. Show that  $\begin{vmatrix} 1 & a & b + c \\ 1 & b & c + a \\ 1 & c & a + b \end{vmatrix} = 0.$



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72. Without expanding at any state, prove that

$$\begin{vmatrix} \frac{1}{a} & a & bc \\ \frac{1}{b} & b & ca \\ \frac{1}{c} & c & ab \end{vmatrix} = 0$$

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73. Without expanding at any state, prove that

$$\begin{vmatrix} 1 & bc & a(b+c) \\ 1 & ca & b(c+a) \\ 1 & ab & c(a+b) \end{vmatrix} = 0$$

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74. Without expanding prove that:

$$\begin{vmatrix} x+y & y+z & z+x \\ z & x & y \\ 1 & 1 & 1 \end{vmatrix} = 0.$$

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75. Using the property of determinants and without expanding, prove that:  $|xax + ayby + bzc + c| = 0$

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76. Using the property of determinants and without expanding, prove that:  $|276538754986| = 0$

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77. Show without expanding at any stage that:

$$\begin{vmatrix} a+b & b+c & c+a \\ b+c & c+a & a+b \\ c+a & a+b & b+c \end{vmatrix} = 2 \begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$$

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78. Evaluate  $\Delta = \begin{vmatrix} 0 & \sin \alpha & -\cos \alpha \\ -\sin \alpha & 0 & \sin \beta \\ \cos \alpha & -\sin \beta & 0 \end{vmatrix}$

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79. Prove that: 
$$\begin{vmatrix} 0 & a & -b \\ -a & 0 & -c \\ b & c & 0 \end{vmatrix} = 0.$$

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80. Show without expanding at any stage that:

$$\begin{vmatrix} 1 & \cos \alpha - \sin \alpha & \cos \alpha + \sin \alpha \\ 1 & \cos \beta - \sin \beta & \cos \beta + \sin \beta \\ 1 & \cos \gamma - \sin \gamma & \cos \gamma + \sin \gamma \end{vmatrix} = 2 \begin{vmatrix} 1 & \cos \alpha & \sin \alpha \\ 1 & \cos \beta & \sin \beta \\ 1 & \cos \gamma & \sin \gamma \end{vmatrix}$$

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81. Show without expanding at any stage that:

$$\begin{vmatrix} (a-1)^2 & a^2+1 & a \\ (b-1)^2 & b^2+1 & b \\ (c-1)^2 & c^2+1 & c \end{vmatrix} = 0$$

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82. Without expanding at any stage, find the value of :

$$\begin{vmatrix} a & b & c \\ a + 2x & b + 2y & c + 2z \\ x & y & z \end{vmatrix}$$

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83. Without expanding at any stage, prove that

$$\begin{vmatrix} 1 & a & a^2 \\ 1 & b & b^2 \\ 1 & c & c^2 \end{vmatrix} = \begin{vmatrix} 1 & a & bc \\ 1 & b & ca \\ 1 & c & ab \end{vmatrix}$$

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84. Without expanding the determinant, prove that

$$|aa^2bc - 2ca^2 - 2ab| = |1a^2a^31b^2b^31c^2c^3|$$

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85. Solve the equation:  $\begin{vmatrix} 2 & 4 \\ 5 & 1 \end{vmatrix} = \begin{vmatrix} 2x & 4 \\ 6 & x \end{vmatrix}$

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86. Solve the equation:  $\begin{vmatrix} 3 & x \\ x & 1 \end{vmatrix} = \begin{vmatrix} 3 & 2 \\ 4 & 1 \end{vmatrix}$

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87. Solve the equation:  $\begin{vmatrix} 2 & 3 \\ 4 & 5 \end{vmatrix} = \begin{vmatrix} x & 3 \\ 2x & 5 \end{vmatrix}$

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88. Solve the equation:  $\begin{vmatrix} a & a & x \\ a & a & a \\ b & x & b \end{vmatrix} = 0$

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89. Solve the equation:  $\begin{vmatrix} x & 2 & 3 \\ 4 & x & 1 \\ x & 2 & 5 \end{vmatrix} = 0$

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90. Solve the following determinant equation:

$$\begin{vmatrix} x+a & b & c \\ c & x+b & a \\ a & b & x+c \end{vmatrix} = 0$$

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91. Solve the equation:  $\begin{vmatrix} x & 1 & 1 \\ 1 & x & 1 \\ 1 & 1 & x \end{vmatrix} = 0$

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92. Find the area of the triangle whose vertices are:

$$(-2, 4), (2, -6), (5, 4)$$

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93. Find the area of the triangle whose vertices are:  $(2, 7), (1, 1), (10, 8)$



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94. Find the area of the triangle whose vertices are:  $(1, 0)$ ,  $(6, 0)$ ,  $(4, 3)$



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95. Find the area of the triangle whose vertices are:

$(-2, -3)$ ,  $(3, 2)$ ,  $(-1, -8)$



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96. Find the area of the triangle whose vertices are:

$(-3, 2)$ ,  $(5, 4)$ ,  $(7, -6)$



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97. Find the area of the triangle whose vertices are:

$(1, 4), (2, 3), (-5, -3)$



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98. Find the area of the triangle whose vertices are:

$(3, 1), (4, 3), (-5, 4)$



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99. Find the area of the triangle whose vertices are:

$(2, 8), (-4, 2), (5, 1)$



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100. Find the value of  $x$  if the area of triangle is 35 sq. units whose vertices are  $(x, 4), (2, -6), (5, 4)$ .



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**101.** Prove that the area of the triangle whose vertices are  $(t, t - 2)$ ,  $(t + 2, t + 2)$  and  $(t + 3, t)$  is independent of  $t$ .



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**102.** Find the values of  $k$  if area of triangle is 9 sq. units and vertices are:  $(-2, 0)$ ,  $(0, 4)$ ,  $(0, k)$



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**103.** Find the values of  $k$  if area of triangle is 4 sq. units and vertices are:  $(k, 0)$ ,  $(0, 2)$ ,  $(4, 0)$



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104. Examine whether the points are collinear or not:  $(2,5), (-5,-2), (-1,2)$

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105. Examine whether the points are collinear or not:  $(-3,2), (-5,-4), (7,-6)$

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106. Examine whether the points are collinear or not:  $(1,5), (2,-4), (3,3)$

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107. Prove that the points  $(a, b + c), (b, c + a)$  and  $(c, a + b)$  are collinear.

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**108.** Prove that the points  $(a, b)$ ,  $(a_1, b_1)$  and  $(a - a_1, b - b_1)$  are collinear if  $ab_1 = a_1b$ .

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**109.** Show that the points  $(a, 0)$ ,  $(0, b)$  and  $(x, y)$  are collinear if  $x/a + y/b = 1$ .

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**110.** For what values of  $k$ , the points  $(1, 4)$ ,  $(k, 2)$ , and  $(-3, 16)$  are collinear?

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**111.** Find the value of  $t$  for which the points  $(1, -1)$ ,  $(3, -3)$  and  $(t, 2)$  lie on the same line (using determinants).

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**112.** Find the equation of the line joining A( 1,3) and B (0,0) using determinants and find k if D(k, 0) is a point such that area of triangle ABD is  $3\text{sq units}$ .



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