

## MATHS

### BOOKS - KC SINHA ENGLISH

#### INVERSE CIRCULAR FUNCTIONS - FOR COMPETITION

##### Solved Examples

1. Find the angle  $\sin^{-1}(\sin 10)$



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2. The value of  $3\tan^{-1}\frac{1}{2} + 2\tan^{-1}\frac{1}{5} + \sin^{-1}\frac{142}{65\sqrt{5}}$  is :



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3. Evaluate :  $\cos(2\cos^{-1}x + \sin^{-1}x)atx = \frac{1}{5}$



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4. Show that  $\frac{1}{2}\cos^{-1}\left(\frac{3}{5}\right) = \tan^{-1}\left(\frac{1}{2}\right)$



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5.

If

$A = 2\tan^{-1}(2\sqrt{2} - 1)$  and  $B = 3\sin^{-1}\left(\frac{1}{3}\right) + \sin^{-1}\left(\frac{3}{5}\right)$ , then show

.



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6. If  $0 < a_1 < a_2 < \dots < a_n$ , then prove that  
 $\tan^{-1}\left(\frac{a_1x - y}{x + a_1y}\right) + \tan^{-1}\left(\frac{a_2 - a_1}{1 + a_2a_1}\right) + \tan^{-1}\left(\frac{a_3 - a_2}{1 + a_3a_2}\right) + \dots + t$



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7. Show that  $2 \tan^{-1} x + \frac{\sin^{-1}(2x)}{1+x^2}$  is constant for  $x \geq 1$ , find that constant.



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8. Prove the relation,  $s_t = u + at - \frac{1}{2}a$ .



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9. If the points  $(a_1, b_1)$ ,  $(a_2, b_2)$  and  $(a_1 + a_2, b_1 + b_2)$  are collinear, show that  $a_1 b_2 = a_2 b_1$ .



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10. Using mathematical induction, prove that  $\tan^{-1}\left(\frac{1}{3}\right) + \tan^{-1}\left(\frac{1}{7}\right) + \dots + \tan^{-1}\left(\frac{1}{n^2+n+1}\right) = \tan^{-1}\left(\frac{n}{n+1}\right)$



11. If  $x_1, x_2, x_3$  and  $x_4$  are the roots of the equations  $x^4 - x^3 \sin 2\beta + x^2 \cos 2\beta - x \cos \beta - \sin \beta = 0$ , prove that  $\tan^{-1} x_1 + \tan^{-1} x_2 + \tan^{-1} x_3 + \tan^{-1} x_4 = \left(\frac{\pi}{2}\right) - \beta$ .



12. If  $\cos^{-1} x + \cos^{-1} y + \cos^{-1} z = \pi$  and  $x + y + z = \frac{3}{2}$ , then prove that  $x = y = z$



13. If  $\sin^{-1} x = \sin^{-1} y + \sin^{-1} z = \pi$ , prove that  $x^4 + y^4 + z^4 + 4x^2y^2z^2 =$



14. Find all possible values of  $x$  and  $y$  for which

$$\cos^{-1} \sqrt{x} + \cos^{-1} \sqrt{1-x} + \cos^{-1} \sqrt{1-y} = \left(\frac{3\pi}{4}\right)$$



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15. The number of positive integral solutions of  $\tan^{-1} x + \cot^{-1} y = \tan^{-1} 3$  is :



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16. If  $a^2 + b^2 = c^2, c \neq 0$ , then find the non-zero solution of the equation:

$$\sin^{-1} \cdot \frac{ax}{c} + \sin^{-1} \cdot \frac{bx}{c} = \sin^{-1} x$$



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17. Convert the trigonometric function  $\sin[2\cos^{-1}\{\cot(2\tan^{-1}x)\}]$  into an algebraic function  $f(x)$ . Then from the algebraic function find all

the values of  $x$  for which  $f(x)$  is zero. Express the values of  $x$  in the form  $a \pm \sqrt{b}$  where  $a$  and  $b$  are rational numbers.



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18. The value(s) of  $\theta$  satisfying the equation  $\theta = \tan^{-1}(2 \tan^2 \theta) - \frac{1}{2} \left( \sin^{-1} \left( \frac{3 \sin 2\theta}{5 + 4 \cos 2\theta} \right) \right)$  is



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20. Solve :  $\tan^{-1} 2x + \tan^{-1} 3x = \frac{\pi}{4}$



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21. If  $\sin^{-1} \left( x - \frac{x^2}{2} + \frac{x^3}{4} - \dots \right) + \cos^{-1} \left( x^2 - \frac{x^4}{2} + \frac{x^6}{4} \right) = \frac{\pi}{2}$  for  $0 < |x|$

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22. The number of real solutions of  $\tan^{-1} \sqrt{x(x+1)} + \sin^{-1} \sqrt{x^2+x+1} = \frac{\pi}{2}$  is  
a. zero b. one c. two d. infinite

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23. If  $\sin \left( \sin^{-1} \frac{1}{5} + \cos^{-1} x \right) = 1$ , then find the value of x

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24. Solve  $\sin^{-1} x + \sin^{-1} (1-x) = \cos^{-1} x$

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25. A solution of  $\sin^{-1}(1) - \sin^{-1}\left(\frac{\sqrt{3}}{x^2}\right) - \frac{\pi}{6} = 0$  is (A)  $x = -\sqrt{2}$   
(B)  $x = \sqrt{2}$  (C)  $x = 2$  (D)  $x = \frac{1}{\sqrt{2}}$



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26. Statement 1. If  $x, 0, \tan^{-1} x + \tan^{-1}\left(\frac{1}{x}\right) = \frac{\pi}{2}$ , Statement 2.  
 $\tan^{-1} x + \cot^{-1} x = \frac{\pi}{2}, \forall x \in R$  (A) Both Statement 1 and Statement 2  
are true and Statement 2 is the correct explanation of Statement 1 (B)  
Both Statement 1 and Statement 2 are true and Statement 2 is not the  
correct explanation of Statement 1 (C) Statement 1 is true but Statement  
2 is false. (D) Statement 1 is false but Statement 2 is true



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27. Statement 1. If  $\sin^{-1} x = \cos^{-1} x$ , then  $x = \frac{1}{\sqrt{2}}$ , Statement 2.  
 $\sin^{-1} x + \cos^{-1} x = \frac{\pi}{2}, 1 \leq x \leq 1$  (A) Both Statement 1 and

Statement 2 are true and Statement 2 is the correct explanation of Statement 1 (B) Both Statement 1 and Statement 2 are true and Statement 2 is not the correct explanation of Statement 1 (C) Statement 1 is true but Statement 2 is false. (D) Statement 1 is false but Statement 2 is true



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28. the value of  $\cos(\cos^{-1}x + \sin^{-1}(x - 2))$  is equal to (A) 0 (B) 1 (C) -1  
(D)  $\sqrt{1 - x^2} \cdot \sqrt{x^2 - 4x + 3} + x(x - 2)$



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29. The value of  $\sin\left(\sin^{-1}\left(\frac{1}{2}\right) + \cos^{-1}\left(\frac{1}{3}\right)\right)$  is equal to (A)  $\left(\frac{\sqrt{3} + \sqrt{8}}{6}\right)$  (B)  $\left(\frac{1 + 2\sqrt{6}}{6}\right)$  (C)  $-\left(\frac{1 + 2\sqrt{6}}{6}\right)$  (D) 0



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30. The minimum value of  $\frac{x}{(\log_e x)}$  is (a)  $e$  (b)  $1/e$  (c) 1 (d) none of these



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31.  $\sum_{i=1}^{\infty} \tan^{-1} \left( \frac{1}{2i^2} \right) = t$ , then  $\tan t =$



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32.

Let  $f(\theta) = \sin \left( \tan^{-1} \left( \frac{\sin \theta}{\sqrt{\cos 2\theta}} \right) \right)$ , where  $-\frac{\pi}{4} < \theta < \frac{\pi}{4}$ . Then the is -



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**Exercise**

1. Find the value of : $\cot^{-1}\left(\cot\left(\frac{5\pi}{4}\right)\right)$



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2. The value of  $\sin^{-1}(\sin 5)$  is  $5 - 2\pi$



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3. Write the value of  $\cos^{-1}\left(\cos\left(5\frac{\pi}{4}\right)\right)$ .



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4. evaluate  $\cos^{-1} \cos 10$



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5. Find the value of the expression:  $\sin\left(2 \frac{\tan^{-1} 1}{3}\right) + \cos(\tan^{-1} 2\sqrt{2})$



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6. Prove that :  $\cot^{-1} 7 + \cot^{-1} 8 + \cot^{-1} 18 = \cot^{-1} 3$



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7. Prove that:  $\sin^{-1}\left(\frac{3}{5}\right) + \cos^{-1}\left(\frac{12}{13}\right) + \cot^{-1}\left(\frac{56}{33}\right) = \frac{\pi}{2}$



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8. Prove that :  $2\cot^{-1} 5 + \cot^{-1} 7 + 2\cot^{-1} 8 = \frac{\pi}{4}$ .



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9. Prove that :  $\tan^{-1} 1 + \tan^{-1} 2 + \tan^{-1} 3 = \pi = 2(\tan^{-1} 1 + \tan^{-1} (1)/(2) + \tan^{-1} (1)/(3))$



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10. If  $\tan A = \frac{1}{7}$  and  $\tan B = \frac{1}{3}$ , show that  $\cos 2A = \sin 4B$ .



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11. Find the sum

$$\tan^{-1}\left(\frac{x}{1+1.2x^2}\right) + \tan^{-1}\left(\frac{x}{1+2.3x^2}\right) + \dots + \tan^{-1}\left(\frac{x}{1+n(n+1)x^2}\right)$$


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12. If  $a_1, a_2, a_3, a_n$  are in arithmetic progression with common difference  $d$ , then evaluate the following expression:

$$\tan\left\{\tan^{-1}\left(\frac{d}{1+a_1a_2}\right) + \tan^{-1}\left(\frac{d}{1+a^2a_3}\right) + \tan^{-1}\left(\frac{d}{1+a_3a_4}\right) + \dots\right\}$$



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13. The inequality  $\sin^{-1}(\sin 5) > x^2 - 4x$  holds for



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14. The value of  $\cos(\sin^{-1}(\tan(\cos^{-1}(\sin(\tan^{-1}(4/3))))))$



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15.

Prove

that:

$$\frac{\alpha^3}{2} \cos ec^2\left(\frac{1}{2} \frac{\tan^{-1} \alpha}{\beta}\right) + \frac{\beta^3}{2} \sec^2\left(\frac{1}{2} \frac{\tan^{-1} \beta}{\alpha}\right) = (\alpha + \beta)(\alpha^2 + \beta^2).$$



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17. If  $\sin^{-1} x + \sin^{-1} y + \sin^{-1} z = \pi$ , prove that:

$$x\sqrt{1-x^2} + y\sqrt{1-y^2} + z\sqrt{1-z^2} = 2xyz$$



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18.

Express:

$$\cot^{-1} \left( \frac{y}{(1 - x^2 - y^2)} \right) = 2 \tan^{-1} \sqrt{\frac{3 - 4x^2}{4x^2}} - \frac{\tan^{-1} \sqrt{3 - 4x^2}}{x^2} \text{ as a rational integral equation in } x \text{ and } y.$$



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$$19. \text{ If } \frac{m \tan(\alpha - \theta)}{\cos^2 \theta} = \frac{n \tan \theta}{\cos^2(\alpha - \theta)}$$

$$\text{Prove that : } \theta = \frac{1}{2} \left[ \alpha - \tan^{-1} \left( \frac{n-m}{n+m} \tan \alpha \right) \right]$$



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$$20. \text{ If } \sin^{-1} \left( \frac{x}{a} \right) + \sin^{-1} \left( \frac{y}{b} \right) = \sin^{-1} \left( \frac{c^2}{ab} \right) \text{ then prove that}$$
$$b^2 x^2 + 2xy\sqrt{a^2 b^2 - c^2} = c^4 - a^2 y^2 - 2x^2 y^2$$



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21.

Prove

that:

$$\tan^{-1}(t) + \tan^{-1}\left(\frac{2t}{1-t^2}\right) = \tan^{-1}\left(\frac{3t-t^3}{1-3t^2}\right), \quad \text{if } -\frac{1}{\sqrt{3}} < t < \frac{1}{\sqrt{3}}$$



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22.  $\cos^{-1}\left(\sqrt{\frac{a-x}{a-b}}\right) = \sin^{-1}\left(\sqrt{\frac{x-b}{a-b}}\right)$  is possible, if



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23. Prove that:  $\sin \cos^{-1} \tan \sec^{-1} x = \sqrt{2 - x^2}$



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24. Solve:  $\frac{\sin^{-1}(3x)}{5} + \frac{\sin^{-1}(4x)}{5} = \sin^{-1} x$



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**25.** Solve :  $\tan^{-1}(x - 1) + \tan^{-1} x + \tan^{-1}(x + 1) = \tan^{-1} 3$



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**26.** Solve  $\sin^{-1}(1 - x) - 2s \in^{-1} x = \frac{\pi}{2}$



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**27.** If  $k$  be a positive integer , show that the equation  $\tan^{-1} x + \tan^{-1} y = \tan^{-1} k$  has no positive integral solution.



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**28.** Solve the equation  $\frac{\tan^{-1}(x + 1)}{x - 1} + \frac{\tan^{-1}(x - 1)}{x} = \tan^{-1}(-7)$



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29. If  $\tan^{-1}\left(\frac{2x}{x^2 - 1}\right) + \cos^{-1}\left\{\frac{x^2 - 1}{x^2 + 1}\right\} = \frac{2\pi}{3}$  then  $x =$



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30. If  $A = \tan^{-1}\left(\frac{x\sqrt{3}}{2k - x}\right)$  and  $B = \tan^{-1}\left(\frac{2x - k}{k\sqrt{3}}\right)$ , then the value of  $A - B$  is :



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31. Find the number of positive integral solution of the equation  
$$\tan^{-1} x + \frac{\cos^{-1}(y)}{\sqrt{1 - y^2}} = \frac{\sin^{-1}(3)}{\sqrt{10}}$$



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32. Solve  $2\cos^{-1} x = \sin^{-1}\left(2x\sqrt{1 - x^2}\right)$



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**33.** Solve:  $\sin^{-1}(x) + \sin\left(\sqrt{1-x^2}\right) =$



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**34.** If  $x, y, z$  are in A.P. and  $\tan^{-1} x, \tan^{-1} y$  and  $\tan^{-1} z$  are also in A.P.  
then show that  $x=y=z$  and  $y \neq 0$



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**35.** Find  $\sum_{k=1}^n \frac{\tan^{-1}(2k)}{2+k^2+k^4}$



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**36.** Sum of infinite terms of the series

$\cos^{-1}\left(1^2 + \frac{3}{4}\right) + \cot^{-1}\left(2^2 + \frac{3}{4}\right) + \cot^{-1}\left(3^2 + \frac{3}{4}\right) + \dots$  is



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37. Solve  $(\tan^{-1} x)^2 + (\cot^{-1} x)^2 = \frac{5\pi^2}{8}$



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38. Find the number of solution of the equation  
 $|y| = \sin x$  and  $y = \cos^{-1} \cos x$  where  $-2\pi \leq x \leq 2\pi$



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39. The least and the greatest values of  $(\sin^{-1} x)^3 + (\cos^{-1} x)^3$  are  
 $-\frac{\pi}{2}, \frac{\pi}{2}$  (b)  $-\frac{\pi^3}{8}, \frac{\pi^3}{8}$  (c)  $\frac{\pi^3}{32}, \frac{7\pi^3}{8}$  (d) none of these



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40. Consider the system of equations  
 $\cos^{-1} x + (\sin^{-1} y)^2 = \frac{p\pi^2}{4}$  and  $(\cos^{-1} x)(\sin^{-1} y)^2 = \frac{\pi^4}{16}, p \in Z$

The value of p for which system has a solution is



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41. find the value  $\sec^{-1}[\sec(-30)] = ?$



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42. Solve for  $x$ :  $3 \frac{\sin^{-1}(2x)}{1+x^2} - 4 \frac{\cos^{-1}(1-x^2)}{1+x^2} + 2 \frac{\tan^{-1}(2x)}{1-x^2} = \frac{\pi}{3}$



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43. If  $\cos^{-1} x + \cos^{-1} y + \cos^{-1} z = \pi$ , then  $x^2 + y^2 + z^2 + xyz = 0$

$$x^2 + y^2 + z^2 + 2xyz = 0$$

$$x^2 + y^2 + z^2 + xyz = 1$$

$$x^2 + y^2 + z^2 + 2xyz = 1$$



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44. The value of  $\sin^{-1}(-\sqrt{3}/2)$  is- a.  $-\pi/3$  b.  $-2\pi/3$  c.  $4\pi/3$  d.  $5\pi/3$



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45. If  $\alpha, \beta, \gamma$  are the roots of the equations  $x^3 + px^2 + 2x + p = 0$  then the general value of  $\tan^{-1}\alpha + \tan^{-1}\beta + \tan^{-1}\gamma$  is (A)  $n\pi$  (B)  $\frac{n\pi}{2}$  (C)  $(2n+1)\frac{\pi}{2}$  (D) dependent upon the value of p.



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46. Principal value (s) of  $\cos^{-1}\left(-\frac{1}{2}\right)$  is(are) (A)  $\frac{\pi}{6}$  radian (B)  $\left(2n\pi + \frac{2\pi}{3}\right)$  radian (C)  $\frac{2\pi}{3}$  radian (D)  $\frac{4\pi}{3}$  radian



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47. If  $\sin^{-1}\left(\frac{1}{3}\right) + \sin^{-1}\left(\frac{2}{3}\right) = \sin^{-1}x$  then x is equal to (A)  $\left(4 + \frac{\sqrt{5}}{9}\right)$  (B)  $\left(4\sqrt{2} + \frac{\sqrt{5}}{9}\right)$  (C)  $\frac{\sqrt{3} + 1}{6}$  (D) 1



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48. If  $\sin^{-1} x + \cot^{-1} \left( \frac{1}{2} \right) = \frac{\pi}{2}$ , then  $x$  is  
a.  $0$  b.  $\frac{1}{\sqrt{5}}$  c.  $\frac{2}{\sqrt{5}}$  d.  $\frac{\sqrt{3}}{2}$



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49. Solve :  $\tan^{-1} 2x + \tan^{-1} 3x = \frac{\pi}{4}$



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50.  $\tan^{-1} \left( \frac{1}{3} \right) + \tan^{-1} \left( \frac{1}{7} \right) + \tan^{-1} \left( \frac{1}{13} \right) + \dots \dots \infty =$



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51. If  $\frac{\cos^{-1} x}{2} + \frac{\cos^{-1} y}{3} = \theta$ , then  $9x^2 - 12xy \cos \theta + 4y^2$  is equal to  
(a) 36 (b)  $-36 \sin^2 \theta$  (c)  $36 \sin^2 \theta$  (d)  $36 \cos^2 \theta$



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52. If  $\cot^{-1}(\sqrt{\cos \alpha}) - \tan^{-1}(\sqrt{\cos \alpha}) = x$ , then  $\sin x$  is  $\frac{\tan^2 \alpha}{2}$  (b)  
 $\frac{\cot^2 \alpha}{2}$  (c)  $\tan^2 \alpha$  (d)  $\frac{\cot \alpha}{2}$

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53. The value of  $\sin(\cot^{-1} x) =$  (A)  $\sqrt{1+x^2}$  (B)  $x$  (C)  $(1+x^2)^{-\frac{3}{2}}$  (D)  
 $(1+x^2)^{-\frac{1}{2}}$

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54. The value of  $\sin^{-1}\left(\frac{\sqrt{3}}{2}\right) + \sin^{-1}\left(\frac{1}{\sqrt{2}}\right)$  is equal to (A)  
 $\sin^{-1}\left(\frac{\sqrt{3+1}}{2\sqrt{2}}\right)$  (B)  $\pi - \sin^{-1}\left(\frac{\sqrt{3+1}}{2\sqrt{2}}\right)$  (C)  $\pi + \sin^{-1}\left(\frac{\sqrt{3+1}}{2\sqrt{2}}\right)$   
(D) none of these

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55.  $\sin^{-1}(2x\sqrt{1-x^2}) = 2\sin^{-1}x$  is true if  $x \in [0, 1]$  b.  
[ $-\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}$ ] c. [ $-\frac{1}{2}, \frac{1}{2}$ ] d. [ $-\frac{\sqrt{3}}{2}, \frac{\sqrt{3}}{2}$ ]



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56. If  $\cot^{-1} \frac{n}{\pi} > \frac{\pi}{6}$ ,  $n \in N$ , then find the maximum value of n.



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57. If we consider only the principal values of the inverse trigonometric functions , then the value of  $\tan\left(\cos^{-1}\left(\frac{1}{5\sqrt{2}}\right) - \sin^{-1}\left(\frac{4}{\sqrt{17}}\right)\right)$  is  
(a)  $\frac{\sqrt{29}}{3}$  (b)  $\frac{29}{3}$  (c)  $\frac{\sqrt{3}}{29}$  (d)  $\frac{3}{29}$



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58. If  $\sum_{i=1}^{10} \sin^{-1} x_i = 5\pi$  then  $\sum_{i=1}^{10} x_i^2 =$  (A) 0 (B) 5 (C) 10 (D) none of these



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59. If  $x = \sin(2 \tan^{-1} 2)$  and  $y = \sin\left(\frac{1}{2} \tan^{-1} \cdot \frac{4}{3}\right)$ , then prove that  $y^2 = 1 - x$



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60.

If

$$\tan^{-1}(x + h) = \tan^{-1}(x) + (h \sin y)(\sin y) - (h \sin y)^2 \cdot \frac{\sin^2 y}{2} + (h \sin y)$$

then (A)  $y = \tan^{-1} x$  (B)  $y = \sin^{-1} x$  (C)  $y = \cot^{-1} x$  (D)  $y = \cos^{-1} x$



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61. Solutions set of  $[\sin^{-1} x] > [\cos^{-1} x]$ , where  $[\cdot]$  denotes the greatest integer function, is



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62. The number of real solutions  $(x, y)$ , where

$|y| = \sin x, y = \cos^{-1}(\cos x), -2\pi \leq x \leq 2\pi$ , is :



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63.

If

$\sin^{-1} x + \sin^{-1} y + \sin^{-1} z = \frac{3\pi}{2}$  and  $f(1) = 2, f(p+q) = f(p) \cdot f(q)$ ,  
, then the value of  $x^{f(1)} + x^{f(2)} + z^{f(3)} - \left( \frac{x+y+z}{x^{f(1)} + y^{f(2)} + z^{f(3)}} \right)$

is :



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64. If  $\tan^{-1} x + \tan^{-1} 2x + \tan^{-1} 3x = \pi$ , then (A)  $x = 0$  (B)  $x = 1$  (C)

$x = -1$  (D)  $x \in \phi$



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65. The real solutions of the equation

$$\tan^{-1} \sqrt{x(x+1)} + \sin^{-1} \sqrt{x^2 + x + 1} = \frac{\pi}{2}$$



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66. The complete solution set of the inequality

$$(\cos^{-1} x)^2 - (\sin^{-1} x)^2 > 0 \text{ is :}$$



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67. The least and the greatest values of  $(\sin^{-1} x)^3 + (\cos^{-1} x)^3$  are

$$-\frac{\pi}{2}, \frac{\pi}{2} \quad (\text{b}) \quad -\frac{\pi^3}{8}, \frac{\pi^3}{8} \quad \frac{\pi^3}{32}, \frac{7\pi^3}{8} \quad (\text{d}) \text{ none of these}$$



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68.  $\sin^{-1}(\sin 5) > x^2 - 4x$  hold if  $x = 2 - \sqrt{9 - 2\pi}$   $x = 2 + \sqrt{9 - 2\pi}$

$$x > 2 + \sqrt{9 - 2\pi} \quad x \in (2 - \sqrt{9 - 2\pi}, 2 + \sqrt{9 - 2\pi})$$



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69.  $\sum_{n=1}^{\infty} \sin^{-1} \left( \frac{\sqrt{n} - (\sqrt{n-1})}{\sqrt{(n)(n+1)}} \right) =$  (A)  $\frac{\pi}{4}$  (B)  $\frac{\pi}{2}$  (C)  $-\frac{\pi}{3}$  (D)  $\frac{\pi}{3}$



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70.  $\sin^{-1} \left( \sin \left( \frac{7\pi}{6} \right) \right) =$  (A)  $\frac{7\pi}{6}$  (B)  $\frac{\pi}{6}$  (C)  $-\frac{\pi}{6}$  (D) none of these



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71.  $\cos^{-1} \left\{ -\sin \left( \frac{5\pi}{6} \right) \right\} =$  (A)  $-\frac{5\pi}{6}$  (B)  $\frac{5\pi}{6}$  (C)  $\frac{2\pi}{3}$  (D)  $-\frac{2\pi}{3}$



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72.  $\sin^{-1} \left( \cos \left( \sin^{-1} \left( \frac{\sqrt{3}}{2} \right) \right) \right) =$  (A)  $\frac{\pi}{3}$  (B)  $\frac{\pi}{6}$  (C)  $-\frac{\pi}{6}$  (D) none of these



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73.  $\sin^{-1}\left(-\frac{1}{2}\right) + \tan^{-1}(\sqrt{3}) =$  (A)  $-\frac{\pi}{6}$  (B)  $\frac{\pi}{3}$  (C)  $\frac{\pi}{6}$  (D) none of these



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74.  $\sum_{i=1}^{2n} \sin^{-1}(x_i) = n\pi$  then the value of  
 $\sum_{i=1}^n \cos^{-1} x_i + \sum_{i=1}^n \tan^{-1} x_i =$  (A)  $\frac{n\pi}{4}$  (B)  $\left(\frac{2}{3}\right)n\pi$  (C)  $\left(\frac{5}{4}\right)n\pi$  (D)  
 $2n\pi$



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75. The greater of the two angles  $A = 2\tan^{-1}(2\sqrt{2} - 1)$  and  $B = 3\sin^{-1}\left(\frac{1}{3}\right) + \sin^{-1}\left(\frac{3}{5}\right)$  is \_\_\_\_.



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76. If  $\cos^{-1} \sqrt{p} + \cos^{-1} \sqrt{1-p} + \cos^{-1} \sqrt{1-q} = \frac{3\pi}{4}$ , then the value of  $q$  is

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77. If the mapping  $f(x) = mx + c, m > 0$  maps  $[-1, 1]$  onto  $[0, 2]$ , then  $\tan\left(\tan^{-1}\frac{1}{7} + \cot^{-1} 8 + \cot^{-1} 18\right)$  is equal to

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78. If  $e^{\log_2 [\sin^2 \alpha + \sin^4 \alpha + \sin^6 \alpha + \dots \rightarrow \infty]}$  is a root of equation  $x^2 - 9x + 8 = 0$  where  $0 < \alpha < \frac{\pi}{2}$  then the principal value of  $\sin^{-1}\left(\frac{2\pi}{3}\right)$  is

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79. If  $1 \tan^{-1} x + \sin^{-1} \frac{2x}{1+x^2}$  is independent of  $x$ , then





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80. Prove that  $\tan^{-1} 1 + \tan^{-1} 2 + \tan^{-1} 3 = \pi$



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81. Prove that :  $\tan\left(2\tan^{-1}\frac{1}{5} - \frac{\pi}{4}\right) + \frac{7}{17} = 0$



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82. Which one of the following is correct? (A)  $\tan 1 > \tan^{-1}(1)$  (B)  
 $\tan < \tan^{-1}(1)$  (C)  $\tan 1 = \tan^{-1}(1)$  (D) none of these



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83. Evaluate :  $\cos(2\cos^{-1}x + \sin^{-1}x) \text{ at } x = \frac{1}{5}$



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**84.** The value of  $x$  for which  $\sin(\cot^{-1}(1+x)) = \cos(\tan^{-1}x)$  is  $\frac{1}{2}$  (b)

1 (c) 0 (d)  $-\frac{1}{2}$



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**85.** If  $\alpha, \beta$  and  $\gamma$  are the three angles with

$$\alpha = 2\tan^{-1}(\sqrt{2}-1); \beta = 3\sin^{-1}\left(\frac{1}{\sqrt{2}}\right) + \sin^{-1}\left(-\frac{1}{2}\right) \quad \text{and}$$

$$\gamma = \cos^{-1}\left(\frac{1}{3}\right), \text{ find the relation between alpha ,beta and gamma}$$

A.  $\alpha < \gamma$

B. null

C. null

D. null

**Answer:** null



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86. If  $0 < x < 1$ , then  $\tan^{-1} \frac{\sqrt{1-x^2}}{1+x}$  is equal to

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87. Which of the following is/are the value of  $\cos\left[\frac{1}{2}\cos^{-1}\left(\cos\left(-\frac{14\pi}{5}\right)\right)\right]$ ? (a)  $\cos\left(-\frac{7\pi}{5}\right)$  (b)  $\sin\left(\frac{\pi}{10}\right) \cos\left(\frac{2\pi}{5}\right)$  (d)  $-\cos\left(\frac{3\pi}{5}\right)$

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88. The value of  $\tan\left\{\frac{1}{2}\sin^{-1}\left(\frac{2x}{1+x^2}\right) + \frac{1}{2}\cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)\right\}$  is (A)  $\frac{2x}{1-x^2}$  (B)  $\frac{2x}{1-x^2}$  (C) not defined if  $x \geq 1$  (D) 0

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89. The sum  $\sum_{n=1}^{\infty} \tan^{-1}\left(\frac{4n}{n^4 - 2n^2 + 2}\right)$  is equal to

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90. Indicate the relation which can hold in their respective domain for infinite values of  $x$ .  $\tan|\tan^{-1} x| = |x|$  (b)  $\cot|\cot^{-1} x| = |x|$   
 $\tan^{-1}|\tan x| = |x|$  (d)  $\sin|\sin^{-1} x| = |x|$



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91. If  $\cos^{-1}\left(\frac{x^2 - 1}{x^2 + 1}\right) + \tan^{-1}\left(\frac{2x}{x^2 - 1}\right) = \frac{2\pi}{3}$ , then  $x$  equal to (A)  $\sqrt{3}$   
(B)  $2 + \sqrt{3}$  (C)  $2 - \sqrt{3}$  (D)  $-\sqrt{3}$



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92.  $2 \cot^{-1} 7 + \cos^{-1}\left(\frac{3}{5}\right)$  is equal to (A)  $\cot^{-1}\left(\frac{44}{117}\right)$  (B)  
 $\cos ec^{-1}\left(\frac{125}{117}\right)$  (C)  $\tan^{-1}\left(\frac{44}{117}\right)$  (D)  $\cos^{-1}\left(\frac{44}{125}\right)$



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**93.**  $\sin^{-1} x > \cos^{-1} x$  holds for

(A) all value of x

(B)  $x \in \left(0, \frac{1}{\sqrt{2}}\right)$

(C)  $x \in \left(\frac{1}{\sqrt{2}}, 1\right)$

(D)  $x = 0.75$



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**94.** Consider  $f(x) = \sin^{-1}(\sec(\tan^{-1} x)) + \cos^{-1}(\cosec(\cot^{-1} x))$  Statement-1:

Domain of  $f(x)$  is a singleton. Statement-2: Range of the function  $f(x)$  is a singleton.



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**95.** Statement 1.  $\tan \left[ \cos^{-1} \left( \frac{1}{\sqrt{82}} \right) - \sin^{-1} \left( \frac{5}{\sqrt{26}} \right) \right]$  is equal to  $\frac{29}{3}$ ,

Statement 2.  $\{x \cos(\cot^{-1} x) + \sin(\cot^{-1} x)\}^2 = \frac{51}{50}$ , when  $x = \frac{1}{5\sqrt{2}}$

(A) Both Statement 1 and Statement 2 are true and Statement 2 is the

## correct explanation of Statement 1

- (B) Both Statement 1 and Statement 2 are true and Statement 2 is not the correct explanation of Statement 1
- (C) Statement 1 is true but Statement 2 is false.
- (D) Statement 1 is false but Statement 2 is true



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96. Statement I  $\cos ec^{-1} \left( \frac{1}{2} + \frac{1}{\sqrt{2}} \right) > \sec^{-1} \left( \frac{1}{2} + \frac{1}{\sqrt{2}} \right)$

Statement II  $\cos ec^{-1} x > \sec^{-1} x$ , if  $1 \leq x < \sqrt{2}$



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97.

Statement

1.

$\cos^{-1} x - \sin^{-1} \left( \frac{x}{2} + \frac{\sqrt{(3-3x^2)}}{2} \right) = -\frac{\pi}{3}$ , where  $\frac{1}{2} \leq x \leq 1$ ,

Statement 2.  $2 \sin^{-1} x = \sin^{-1} 2x\sqrt{1-x^2}$ , where  $-\frac{1}{\sqrt{2}} \leq x \leq \frac{1}{\sqrt{2}}$ .

- (A) Both Statement 1 and Statement 2 are true and Statement 2 is the correct explanation of Statement 1

- (B) Both Statement 1 and Statement 2 are true and Statement 2 is not the correct explanation of Statement 1
- (C) Statement 1 is true but Statement 2 is false.
- (D) Statement 1 is false but Statement 2 is true

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98. Statement 1. If  $x, 0, \tan^{-1} x + \frac{\tan^{-1} 1}{x} = \frac{\pi}{2}$ , Statement 2.  $\tan^{-1} x + \cot^{-1} x = \frac{\pi}{2}, \forall x \in R$  (A) Both Statement 1 and Statement 2 are true and Statement 2 is the correct explanation of Statement 1 (B) Both Statement 1 and Statement 2 are true and Statement 2 is not the correct explanation of Statement 1 (C) Statement 1 is true but Statement 2 is false. (D) Statement 1 is false but Statement 2 is true

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99.  $\text{Let } \alpha = \tan^{-1}\left(\frac{1}{2}\right) + \tan^{-1}\left(\frac{1}{3}\right),$   
 $\beta = \cos^{-1}\left(\frac{2}{3}\right) + \cos^{-1}\left(\frac{\sqrt{5}}{3}\right),$

$$\gamma = \sin^{-1} \left( \sin \left( \frac{2\pi}{3} \right) \right) + \frac{1}{2} \cos^{-1} \left( \cos \left( \frac{2\pi}{3} \right) \right)$$

The value of  $\cos(\alpha + \beta + \gamma)$  is equal to

- (A)  $\cos \left( \frac{5\pi}{12} \right)$  (B)  $\cos \left( \frac{7\pi}{12} \right)$  (C)  $-\cos \left( \frac{\pi}{12} \right)$  (D)  $-\cos \left( \frac{7\pi}{12} \right)$



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100.

$$\text{Let } \alpha = \tan^{-1} \left( \frac{1}{2} \right) + \tan^{-1} \left( \frac{1}{3} \right),$$

$$\beta = \cos^{-1} \left( \frac{2}{3} \right) + \cos^{-1} \left( \frac{\sqrt{5}}{3} \right),$$

$$\gamma = \sin^{-1} \left( \sin \left( \frac{2\pi}{3} \right) \right) + \frac{1}{2} \cos^{-1} \left( \cos \left( \frac{2\pi}{3} \right) \right)$$

then  $\sin \cot^{-1} \tan \cos^{-1} (\sin \gamma)$  is equal to

- (A)  $2 \sin \gamma$  (B)  $\sin \left( \frac{\gamma}{2} \right)$  (C)  $\frac{1}{2} \sin \gamma$  (D)  $\cos \gamma$



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101.

Let

$$\alpha = \tan^{-1} \left( \frac{1}{2} \right) + \tan^{-1} \left( \frac{1}{3} \right),$$

$$\beta = \cos^{-1} \left( \frac{2}{3} \right) + \cos^{-1} \left( \frac{\sqrt{5}}{3} \right),$$

$$\gamma = \sin^{-1} \left( \sin \left( \frac{2\pi}{3} \right) \right) + \frac{1}{2} \cos^{-1} \left( \cos \left( \frac{2\pi}{3} \right) \right)$$

then  $\cos \alpha + \cos \beta + \cos \gamma$  is equal to

- (A)  $\frac{\sqrt{2} - 1}{2}$  (B)  $\frac{\sqrt{2} + 1}{2}$  (C)  $\frac{\sqrt{2} + \sqrt{3}}{2}$  (D)  $\left( \frac{\sqrt{3} - \sqrt{2}}{2} \right)$



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102. If  $\frac{\cos^{-1} x}{a} + \frac{\cos^{-1} y}{b} = \alpha$ , prove that

$$\frac{x^2}{a^2} - 2\frac{xy}{ab} \cos \alpha + \frac{y^2}{b^2} = \sin^2 \alpha$$



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103. Let  $\cos^{-1}\left(\frac{x}{a}\right) + \cos^{-1}\left(\frac{y}{b}\right) = \alpha$ . Given equation represents and ellipse if (A)  $\alpha = 0$  (B)  $\alpha = \frac{\pi}{4}$  (C)  $\alpha = \frac{\pi}{2}$  (D)  $\alpha = \pi$



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104. Express:

$$\cot^{-1}\left(\frac{y}{(1-x^2-y^2)}\right) = 2\tan^{-1}\sqrt{\frac{3-4x^2}{4x^2}} - \frac{\tan^{-1}\sqrt{3-4x^2}}{x^2} \text{ as a}$$

rational integral equation in x and y.

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105. Absolute value of sum of all integers in the domain of

$$f(x) = \cot^{-1} \sqrt{(x+3)x} + \cos^{-1} \sqrt{x^2 + 3x + 1} \text{ is } \underline{\hspace{2cm}}$$

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106. If  $(\sin^{-1} x)^2 + (\sin^{-1} y)^2 + (\sin^{-1} z)^2 = \frac{3\pi^2}{4}$ , then find the minimum value of  $x + y + z$

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107. Prove the following:

$$\tan \left[ \frac{\pi}{4} + \frac{1}{2} \cos^{-1} \left( \frac{a}{b} \right) \right] + \tan \left[ \frac{\pi}{4} - \frac{1}{2} \cos^{-1} \left( \frac{a}{b} \right) \right] = \frac{2b}{a}$$

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**108.** If  $\sum_{i=1}^{200} \sin^{-1} x_i = 100\pi$ , then  $\sum_{i=1}^{200} x_i^2$  is equal to



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**109.** Greatest value of  $(\sin^{-1} x)^3 + (\cos^{-1} x)^3$  is  $\frac{m}{n}\pi^3$ , where m and n are relatively prime, then the value of mn is



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**110.** Find the value of  $\cos(2\cos^{-1} x + \sin^{-1} x)$  at  $x = \frac{1}{5}$ , where  $0 \leq \pi$  and  $-\frac{\pi}{2} \leq \sin^{-1} x \leq \frac{\pi}{2}$ .



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**111.** The value of  $\tan\left[\cos^{-1}\left(\frac{4}{5}\right) + \tan^{-1}\left(\frac{2}{3}\right)\right]$  is (a)  $\frac{6}{17}$  (b)  $\frac{7}{16}$  (c)  $\frac{16}{7}$  (d) none of these



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112. Evaluate: (i)  $\tan\left(2 \frac{\tan^{-1} 1}{5} - \frac{\pi}{4}\right)$  (ii)  $\tan\left\{\frac{1}{2} \frac{\cos^{-1}(\sqrt{5})}{3}\right\}$



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113. The principal value of  $\sin^{-1}\left(s \in \frac{2\pi}{3}\right)$  is (a)  $-\frac{2\pi}{3}$  (b)  $\frac{2\pi}{3}$  (c)  $\frac{4\pi}{3}$  (d)  $\frac{5\pi}{3}$   
(e) none of these



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114. The greater of the two angles  $A = 2\tan^{-1}(2\sqrt{2} - 1)$  and  $B = 3\sin^{-1}\left(\frac{1}{3}\right) + \sin^{-1}\left(\frac{3}{5}\right)$  is \_\_\_\_.



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**115.** If we consider only the principal values of the inverse trigonometric functions , then the value of  $\tan\left(\cos^{-1}\left(\frac{1}{5\sqrt{2}}\right) - \sin^{-1}\left(\frac{4}{\sqrt{17}}\right)\right)$  is

(a)  $\frac{\sqrt{29}}{3}$  (b)  $\frac{29}{3}$  (c)  $\frac{\sqrt{3}}{29}$  (d)  $\frac{3}{29}$



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**116.** The number of real solutions of  $\tan^{-1} \sqrt{x(x+1)} + \sin^{-1} \sqrt{x^2 + x + 1} = \frac{\pi}{2}$  is

a. zero b. one c. two d. infinite



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**117.** If  $\sin^{-1}\left(x - \frac{x^2}{2} + \frac{x^3}{4} - \dots\right) + \cos^{-1}\left(x^2 - \frac{x^4}{2} + \frac{x^6}{4}\right) = \frac{\pi}{2}$  for  $0 < |x|$



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118. Prove that  $\cos \tan^{-1} \sin \cot^{-1} x = \sqrt{\frac{x^2 + 1}{x^2 + 2}}$



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119. The domain of definition of the function  $f(x) = \sqrt{\sin^{-1}(2x) + \frac{\pi}{6}}$  for real-valued  $x$  is  
(a)  $\left[ -\frac{1}{4}, \frac{1}{2} \right]$  (b)  $\left[ -\frac{1}{2}, \frac{1}{2} \right]$  (c)  $\left( -\frac{1}{2}, \frac{1}{9} \right)$  (d)  
 $\left[ -\frac{1}{4}, \frac{1}{4} \right]$



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120. about to only mathematics



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121. The sum of the roots of the equation  $\tan^{-1}(x+3) - \tan^{-1}(x-3) = \sin^{-1} \frac{3}{5}$  is



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**122.**

Let  $f(\theta) = \sin\left(\tan^{-1}\left(\frac{\sin \theta}{\sqrt{\cos 2\theta}}\right)\right)$ , where  $-\frac{\pi}{4} < \theta < \frac{\pi}{4}$ . Then the is -

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**123.** If  $\cot^{-1}(\sqrt{\cos \alpha}) - \tan^{-1}(\sqrt{\cos \alpha}) = x$ , then  $\sin x$  is  $\frac{\tan^2 \alpha}{2}$  (b)  
 $\frac{\cot^2 \alpha}{2}$  (c)  $\tan^2 \alpha$  (d)  $\frac{\cot \alpha}{2}$

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**124.** The trigonometric equation  $\sin^{-1} x = 2 \sin^{-1} a$  has a solution for

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**125.** If  $\cos^{-1} x - \cos^{-1} \frac{y}{2} = \alpha$ , then  $4x^2 - 4xy \cos \alpha + y^2$  is equal to



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**126.** If  $\sin^{-1} \left( \frac{x}{5} \right) + \cos^{-1} \left( \frac{5}{4} \right) = \frac{\pi}{2}$  then a value of x is: (1) 1 (2) 3 (3) 4 (4) 5



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**127.** The value of  $\cot \left( \cos^{-1} \frac{5}{3} + \frac{\tan^{-1} 2}{3} \right)$  is: (1)  $\frac{6}{17}$  (2)  $\frac{3}{17}$  (2)  $\frac{4}{17}$  (4)  $\frac{5}{17}$



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