



## MATHS

### BOOKS - RESONANCE DPP ENGLISH

### DIFFERENTIAL EQUATIONS

#### Others

1. If  $F(x) = f(x)g(x)$  and  $f'(x)g'(x) = c$ , prove that

$$\frac{F''}{F} = \frac{f''}{f} + \frac{g''}{g} + \frac{2c}{fg} \quad \& \quad \frac{F'''}{F} = \frac{f'''}{f} + \frac{g'''}{g}$$

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2. The degree of the differential equation,  $e^{\left(\frac{d^3y}{dx^3}\right)^2} + x \frac{d^2y}{dx^2} + y = 0$  is 1

(b) 2 (c) 0 (d) not defined

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3. The order of the differential equation whose general solution is

$$y = c_1 \cos 2x + c_2 \cos^2 x + c_3 \sin^2 x + c_4$$

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4. The two curves  $x = y^2$ ,  $xy = a^3$  cut orthogonally at a point. Then  $a^2$  is equal to  $\frac{1}{3}$  (b) 3 (c) 2 (d)  $\frac{1}{2}$

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5. A curve  $C$  passes through  $(2,0)$  and the slope at  $(x, y)$  as  $\frac{(x+1)^2 + (y-3)}{x+1}$ . Find the equation of the curve. Find the area bounded by curve and x-axis in the fourth quadrant.

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6. Identify the statement(s) which is/are true. (a)

$$(b)(c) f((d)(e)x, y(f)) = (g)e^{(h)(i)(j)\frac{y}{k}x^{(l)(m)(n)}}(o) + \tan(p)\frac{y}{q}x^{(r)(s)}$$

(u) is a homogeneous of degree zero. (v) *[Math Processing Error]* (ww) is a homogeneous differential equation. (xx) *[Math Processing Error]* (iii) is a non-homogeneous. (jjj)

$$(kkk)(lll)\left((mmm)\left(\bigcap\right)(\infty o)x^{(ppp)2(qqq)}(rrr) + (sss)y^{(ttt)2(www)}(vvv)\right)$$

(gggg) is a homogeneous differential equation.



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7. The solution of the differential equation

$$\frac{x^2 dy}{dx} \cos\left(\frac{1}{x}\right) - y \sin\left(\frac{1}{x}\right) = -1, \text{ where } y \rightarrow 1 \text{ as } x \rightarrow \infty \text{ is (A)}$$

$$y = \sin\left(\frac{1}{x}\right) + \cos\left(\frac{1}{x}\right) \quad (B) \quad y = \frac{x+1}{x \sin\left(\frac{1}{x}\right)} \quad (C)$$

$$y = \sin\left(\frac{1}{x}\right) - \cos\left(\frac{1}{x}\right) \quad (D) \quad y = \frac{x}{x \cos\left(\frac{1}{x}\right)}$$



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8. The solution of differential equation

$$(1 + y^2) + \frac{(x - 2e^{\tan^{-1}((-1)y)})dy}{dx} = 0 \quad \text{is}$$

$$(x - 2) = ke^{\tan^{-1}((-1)y)} \quad xe^{\tan^{-1}((-1)y)} - 1y = e^2 \tan^{-1} y + k$$

$$xe^{\tan^{-1}((-1)y)} = \tan^{-1} y + k \quad xe^2 \tan^{-1} y = e^2 \tan^{-1} y + k$$

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9. The solution of the differential equation  $(x + y)^2 \frac{dy}{dx} = 1$ , satisfying

the condition  $y(1) = 0$  is (A)  $y + \frac{\pi}{4} = \tan^{-1}(x + y)$  (B)

$y - \frac{\pi}{4} = \tan^{-1}(x + y)$  (C)  $y = \tan^{-1} x$  (D)  $y = \tan^{-1}(\ln x) + 1$

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