



## MATHS

### BOOKS - OBJECTIVE RD SHARMA ENGLISH

### INCREASING AND DECREASING FUNCTIONS

#### Illustration

1. The function  $f(x) = 2\log(x - 2) - x^2 + 4x + 1$  increases on the interval (a) (1, 2) (b) (2, 3) (c) (1, 3) (d) (2, 4)

A. (1,2)

B. (2,3)

C. (1,3)

D. (2,4)

**Answer: B**



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2. The function  $f(x) = x^3 - 3x$  is

- A. increasing on  $(-\infty, -1) \cup [1, \infty)$  and decreasing on  $(-1, 1)$
- B. decreasing on  $(-\infty, -1] \cup [1, \infty)$  and increasing on  $(-1, 1)$
- C. increasing on  $(0, \infty)$  and decreasing on  $(-\infty, 0)$
- D. decreasing on  $(0, \infty)$  and increasing on  $(-\infty, 0)$

Answer: A



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3. The function  $f$  defined by  $f(x) = (x + 2)e^{-x}$  is

- A. decreasing in for all  $x$
- B. increasing in  $(-\infty, -1)$  and decreasing in  $(-1, \infty)$
- C. increasing for all  $x$

D. decreasing in  $(-1, \infty)$  and increasing in  $(-\infty, 0)$

**Answer: B**



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4. Let  $f(x) = x^3 + ax^2 + bx + 5\sin^2 x$  be an increasing function on the set  $R$ . Then find the condition on  $a$  and  $b$ .

A.  $a^2 + 3b + 15 > 0$

B.  $a^2 + 3b + 15 < 0$

C.  $a^2 - 3b - 15 > 0$

D.  $a^2 - 3b - 15 < 0$

**Answer: A**



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5. Let the function  $f(x) = \tan^{-1}(\sin x + \cos x)$  be defined on  $[0, 2\pi]$

Then  $f(x)$  is

A. increasing on  $[0, \pi/4) \cup [5\pi/4, 2\pi]$

B. decreasing on  $(\pi/4, 2\pi)$

C. increasing on  $(0, \pi/4, ) \cup (3\pi/4, 2\pi)$

D. decreasing on  $[\pi/4, 7\pi/4]$

**Answer: A**



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## Section I Solved Mcqs

1. Let  $h(x) = f(x) - (f(x))^2 + (f(x))^3$  for every real number  $x$ . Then  
(a)  $h$  is increasing whenever  $f$  is increasing (b)  $h$  is increasing whenever  $f$  is decreasing  
(c)  $h$  is decreasing whenever  $f$  is decreasing (d) nothing can be said in general

- A. h is increasing whenever f is increasing
- B. h is increasing whenever f is decreasing
- C. h is decreasing whenever f is decreasing
- D. nothing can be said in general

**Answer: A::C**

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2. If  $f(x) = \frac{x}{\sin x}$  and  $g(x) = \frac{x}{\tan x}$ , where  $0 < x \leq 1$ , then in this interval

- A. both  $f(x)$  and  $g(x)$  are increasing functions
- B. both  $f(x)$  and  $g(x)$  decreasing functions
- C.  $f(x)$  is an increasing function
- D.  $g(x)$  is an increasing function

**Answer: C**



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3. Find the interval to which  $b$  may belong so that the function  $f(x) = \left(1 - \frac{\sqrt{21 - 4b - b^2}}{b + 1}\right)x^3 + 5x + \sqrt{6}$  is increasing at every point of its domain.

A. (-7,-1)

B. (-6,-2)

C. (2,25)

D. all of the above

Answer:



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4. The interval of increase of the function  $f(x) = x - e^x + \tan(2\pi/7)$  is  
(a)  $(0, \infty)$  (b)  $(-\infty, 0)$  (c)  $(1, \infty)$  (d)  $(-\infty, 1)$

A.  $(0, \infty)$

B.  $(-\infty, 0)$

C.  $(1, \infty)$

D.  $(5, \infty)$

**Answer: B**



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5. The function  $f(x) = x^x$  decreases on the interval (a)  $(0, e)$  (b)  $(0, 1)$   
(c)  $(0, 1/e)$  (d)  $(1/e, e)$

A.  $(0, e)$

B.  $(0, 1)$

C.  $(0, 1/e)$

D. none of these

**Answer: C**

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6. The set of all  $x$  for which  $\log(1 + x) \leq x$  is equal to .....

A.  $(0, \infty)$

B.  $(-1, \infty)$

C.  $(-1, 0)$

D. none of these

**Answer: B**

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7. The function  $f(x) = \frac{x}{x \log x}$  increase on the interval

A.  $(1, \infty)$

B.  $(0, e)$

C.  $(e, \infty)$



D. none of these

**Answer: C**



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8. The function  $f(x) = \tan^{-1}(\sin x + \cos x)$  is an increasing function in

(a)  $\left(-\frac{\pi}{2}, \frac{\pi}{4}\right)$  (b)  $\left(0, \frac{\pi}{2}\right)$  (c)  $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$  (d)  $\left(\frac{\pi}{4}, \frac{\pi}{2}\right)$

A.  $\left(0, \frac{\pi}{2}\right)$

B.  $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$

C.  $\left(\frac{\pi}{4}, \frac{\pi}{2}\right)$

D.  $\left(-\frac{\pi}{2}, \frac{\pi}{4}\right)$

**Answer: D**



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9. The set of all  $x$  for which  $1 + \log x < x$ , is

A.  $(1, \infty)$

B.  $(0,1)$

C.  $(0, \infty)$

D. none of these

**Answer: C**



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10. For  $x > 1$  and  $y = \log x$  which one of the following is not true ?

A.  $x - 1 > y$

B.  $x^2 - 1 > y$

C.  $y > x - 1$

D.  $\frac{x - 1}{x} < y$

**Answer: C**



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11. If the function  $f(x) = 2x^2 - kx + 5$  is increasing on  $[1, 2]$ , then  $k$  lies in the interval (a)  $(-\infty, 4)$  (b)  $(4, \infty)$  (c)  $(-\infty, 8)$  (d)  $(8, \infty)$

A.  $(-\infty, 4)$

B.  $(4, \infty)$

C.  $(-\infty, 8)$

D.  $(8, \infty)$

**Answer: A**



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12. Let  $f(x) = x^3 + ax^2 + bx + 5\sin^2 x$  be an increasing function on the set  $R$ . Then find the condition on  $a$  and  $b$ .

A.  $a^2 - 3b - 15 > 0$

B.  $a^2 - 3b + 15 > 0$

C.  $a^2 - 3b + 15 < 0$

D.  $a > 0$  and  $b < 0$

**Answer: C**

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**13.** If  $a, b, c$  are real numbers, then find the intervals in which

$$f(x) = \begin{vmatrix} x + a^2 & ab & ac \\ ab & x + b^2 & bc \\ ac & bc & x + c^2 \end{vmatrix} \text{ is increasing or decreasing.}$$

A.  $\left( -\frac{2}{3}(a^2 + b^2 + c^2), 0 \right)$

B.  $0, \left( -\frac{2}{3}(a^2 + b^2 + c^2) \right)$

C.  $\left( \frac{a^2 + b^2 + c^2}{3} \right)$

D. none of these

**Answer: A**



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**14.** Let  $f(x)$  be the function given by

$$f(x) = 3x^5 - 5x^3 + 21x + 3 \sin x + \cos x + 5. \text{ Then ,}$$

- A.  $f(x)$  is increasing on  $\mathbb{R}$  and  $f(x) = 0$  has exactly one negative root
- B.  $f(x)$  is increasing on  $\mathbb{R}$  and  $f(x) = 0$  has exactly one positive root
- C.  $f(x)$  is an increasing and  $f(x) = 0$  has exactly one negative root
- D.  $f(x)$  is an increasing and  $f(x) = 0$  has exactly one positive root

**Answer: A::C**



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**15.** If the function  $f(x) = 2 \tan x + (2a + 1)(\log)_e |\sec x| + (a - 2)x$  is increasing on  $\mathbb{R}$  , then (a)  $a \in (1/2, \infty)$  (b)  $a \in (-1/2, 1/2)$  (c)

$$a = 1/2 \text{ (d) } a \in R$$

A.  $(a \in (1/2, \infty))$

B.  $(a \in (-1/2, 1/2))$

C.  $a = 1/2$

D.  $(a \in R)$

**Answer: C**



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16. If  $f'(x^2 - 4x + 3) > 0$  for all  $x \in (2, 3)$  then  $f(\sin x)$  is increasing on

A.  $\bigcup_{n \in Z} \left( 2n\pi, (4n + 1)\frac{\pi}{2} \right)$

B.  $\bigcup_{n \in Z} \left( (4n - 1)\frac{\pi}{2}, 2n\pi \right)$

C.  $R$

D. none of these

**Answer: A**



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17. Let  $f(x) = \tan^{-1}(g(x))$ , where  $g(x)$  is monotonically increasing for  $0 < x < \frac{\pi}{2}$ .

- A. increasing on  $(0, \pi/2)$
- B. decreasing on  $(0, \pi/2)$
- C. increasing on  $(0, \pi/4)$  and decreasing on  $(\pi/4, \pi/2)$
- D. none of these

**Answer: A**



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18. Let  $f(x) = \int e^x (x - 1)(x - 2) dx$ , then  $f(x)$  decrease in the interval

A.  $(-\infty, -2)$

B.  $(-2, -1)$

C.  $(1, 2)$

D.  $(2, \infty)$

**Answer: C**

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**19. Assertion** Consider the following statements in  $S$  and  $RS$ : Both  $\sin x$  and  $\cos x$  are decreasing function in the interval  $(\frac{\pi}{2}, \pi)$  *Reason* If a differentiable function decreases in an interval  $(a, b)$ , then its derivative also decrease in  $(a, b)$ . Which of the following is true? (a) Both  $S$  and  $R$  are wrong. (b) Both  $S$  and  $R$  are correct, but  $R$  is not the correct explanation of  $S$ . (c)  $S$  is correct and  $R$  is the correct explanation for  $S$ . (d)  $S$  is correct and  $R$  is wrong.

A. Both  $S$  and  $R$  are wrong



B. Both S and R are correct but R is not correct explanation for S

C. S is correct and R wrong

D. d

**Answer: D**



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20. The length of the longest interval, in which the function  $3 \sin x - 4 \sin^3 x$  is increasing is

A.  $\frac{\pi}{3}$

B.  $\frac{\pi}{2}$

C.  $3\frac{\pi}{2}$

D.  $\pi$

**Answer: A**



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21. If  $f(x) = x^3 + 4x^2 + ax + 5$  is a monotonically decreasing function of  $x$  in the largest possible interval  $(-\infty, -2/3)$ , then the value of  $a$  is

- A. 4
- B. 2
- C. -1
- D. none of these

**Answer: A**

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22. Let  $f(x) = 2 \sin^3 x - 3 \sin^2 x + 12 \sin x + 5$ ,  $0 \leq x \leq \frac{\pi}{2}$ . Then  $f(x)$  is

- A. decreasing on  $[0, \pi/2]$
- B. increasing on  $[0, \pi/2]$
- C. increasing on  $(0, \pi/4)$  and decreasing on  $(\pi/4, \pi/2)$

D. none of these

**Answer: B**



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**23.** Let  $f'(x) > 0$  and  $g'(x) < 0$  for all  $x \in R$  Then

A.  $f\{g(x) > f(g(X + 1))\}$

B.  $f\{g(x) > f(g(X - 1))\}$

C.  $g\{f(x) > g(f(X + 1))\}$

D.  $g\{f(x) > g(f(X - 1))\}$

**Answer: A::C**



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24. If  $f(x) = (ab + b^2 + 1)x + \int_0^x (\cos^4 \theta + \sin^4 \theta) d\theta$  is an increasing function of  $x$  for all  $x \in R$  and  $b \in R$ ,  $b$  being independent of  $x$  then

- A.  $a \in (0, \sqrt{6})$
- B.  $a \in (\sqrt{6}, \sqrt{6})$
- C.  $a \in (-\sqrt{6}, 0)$
- D. none of these

**Answer: B**



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25. If  $f(x) = \frac{P^2 - 1}{P^2 + 1}x^3 - 3x + \log 2$  is a decreasing function of  $x$  in  $R$  then the set of possible values of  $P$  (independent of  $x$ ) is

- A.  $[-1, 1]$
- B.  $[1, \infty]$

C.  $[-\infty, -1]$

D. none of these

**Answer: A**



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26. If  $g(x)$  is a continuous function at  $x=a$  such that  $g(a) > 0$  and  $f'(x) = g(x)(x^2 - ax + a^2)$  for all  $x \in K$  then  $f(x)$  is

A. increasing in the neighbourhood of  $x=a$

B. decreasing in the neighbourhood of  $x=a$

C. constant in the neighbourhood of  $x=a$

D. maximum at  $x=a$

**Answer: A**



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27. Let  $g(x) = 2f\left(\frac{x}{2}\right) + f(2-x)$  and  $f'(x) < 0 \forall x \in (0, 2)$ . Then  $g(x)$  increases in  $\left(\frac{1}{2}, 2\right)$  (b)  $\left(\frac{4}{3}, 2\right)$  (c)  $(0, 2)$  (d)  $\left(0, \frac{4}{3}\right)$

A. increasing on  $\left(\frac{4}{3}, 2\right)$  and increasing on  $\left(0, \frac{4}{3}\right)$

B. decreasing on  $\left(0, \frac{4}{3}\right)$  and decreasing on  $\left(\frac{4}{3}, 2\right)$

C. increasing  $\left(0, \frac{4}{3}\right)$  and decreasing on  $\left(\frac{4}{3}, 2\right)$

D. non of these

**Answer: C**

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28. The set of all values of  $a$  for which the function

$$f(x) = \left(\frac{a^2 - 1}{3}\right)x^3 + (a - 1)x^2 + 2x + 1$$

increases on  $\mathbb{R}$ , is

A.  $(-3, 1)$

B.  $\mathbb{R} - [-3, 1]$

C.  $(-\infty, -3)$

D.  $[1, \infty]$

**Answer: B**



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29. Let  $f(x) = \begin{cases} xe^{ax}, & x \leq 0 \\ x + ax^2 - x^3, & x > 0 \end{cases}$ , where  $a$  is a

positive constant. Then the interval in which  $f'(x)$  is increasing is

A.  $(0, a/3)$

B.  $(-2/a, 0)$

C.  $(-2/a, a/3)$

D. non of these

**Answer: C**



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30. Let  $f(x)$  be a function given by  $f(x) = \frac{x^2 + 1}{[x]}$

where  $[ ]$  denotes the greatest interger function .Then  $f(x)$  is monotonically

A. increasing on  $[1,4)$

B. decreasing  $[1,4)$

C. increasing on  $[1,2)$

D. decreasing on  $[2,3)$

**Answer: C**



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31. If the function  $f(x)=3 \cos |x| -6 ax +b$  increases for all  $x \in R$  then the range of value of a given by

A.  $\left( -\frac{1}{2}, \infty \right)$

B.  $(-\infty, -1/2)$



C.  $(-\infty, -2)$

D.  $(-2, \infty)$

**Answer: B**



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**32.** Let  $f$  and  $g$  be increasing and decreasing functions, respectively, from  $[0, \infty] \rightarrow [0, \infty]$ . Let  $h(x) = f(g(x))$ . If  $h(0) = 0$ , then  $h(x) - h(1)$  is  
(a) always zero (b) always negative (c) always positive (d) strictly increasing  
none of these

A. always 0

B. always positive

C. always negative

D. strictly increasing

**Answer: A**



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33. The interval in which  $f(x)$  increases less rapidly than  $g(x)$ ,  $f(x) = 2x^3 + 5$  and  $g(x) = 9x^2 - 12x$  is

A.  $(-\infty, 1)$

B.  $(1, 2)$

C.  $(2, \infty)$

D. none of these

Answer: B



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34. If  $f(x) = \begin{cases} 3x^2 + 12x - 1, & -1 \leq x \leq 2 \\ 37 - x, & 2 < x \leq 3 \end{cases}$  then

A.  $f(x)$  increasing on  $[-1, 2]$

B.  $f(x)$  is continuous on  $[-1, 3]$

C.  $f'(2)$  does not exist

D. all of these

**Answer: D**



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35. Given that  $f(x) > g(x)f$  or  $allx \in R$  and  $f(0) = g(0)$  then

A.

$$f(x) > g(x)f \text{ or } allx \in (0, \infty) \text{ and } f(x) > g(x)f \text{ or } allx \in (-\infty, 0)$$

B.

$$f(x) < g(x)f \text{ or } allx \in (0, \infty) \text{ and } f(x) > g(x)f \text{ or } allx \in (-\infty, 0)$$

C.

$$f(x) > g(x) > f \text{ or } allx \in (-\infty, 0) \text{ and } f(x) < g(x)f \text{ or } allx \in (0, \infty)$$

D. none of these

**Answer: A**



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36. The function  $f(x) = \frac{\sin x}{x}$  is decreasing in the interval

A.  $\left(-\frac{\pi}{2}, 0\right)$

B.  $(0, \pi/2)$

C.  $(0, \pi)$

D. none of these

Answer: B



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37. [ If  $0 < x < \frac{\pi}{2}$  then 1)  $\frac{2}{\pi} > \frac{\sin x}{x}$  (2)  $(\pi) < \frac{\sin x}{x}$  3)  $\frac{\sin x}{x} > 1$ , 4)  
 $2 < \frac{\sin x}{x}$

A.  $\frac{2}{\pi} < \frac{\sin x}{x}$

B.  $\frac{\sin x}{x} < 1$

C.  $\frac{\sin x}{x} > 1$

D.  $\frac{\sin x}{x} > 1$

**Answer: B::C**



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38. If  $0 < \alpha < \beta < \frac{\pi}{2}$  then

A.  $\frac{\tan \beta}{\tan \alpha} < \frac{\alpha}{\beta}$

B.  $\frac{\tan \beta}{\tan \alpha} > \frac{\alpha}{\beta}$

C.  $\frac{\tan \beta}{\tan \alpha} > \frac{\alpha}{\beta}$

D.  $\frac{\tan \alpha}{\tan \beta} \leq \frac{\alpha}{\beta}$

**Answer: B**



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39. If  $0 \leq x \leq \frac{\pi}{2}$  then

A.  $2 \sin x + \tan x < 3x$

B.  $2 \sin x + \tan x < 2x$

C.  $2 \sin x + \tan x \leq 3x$

D.  $2 \sin x + \tan x \leq 3x$

Answer: C



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40. If  $f(x) = x \cdot e^{x(1-x)}$ , then  $f(x)$  is

A. increasing on  $[-1/2, 1]$

B. decreasing on  $\mathbb{R}$

C. increasing on  $\mathbb{R}$

D. decreasing on  $[-1/2, 1]$

**Answer: A**



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41. If  $f(x) = \int_0^x e^{t^2}(t-2)(t-3)dt$  for all  $x \in (0, \infty)$ , then

A.  $e^x < 1 + x$

B.  $\log_e(1+x) < x$

C.  $\sin x > x$

D.  $\log x > x$

**Answer: B**



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42. If  $0 < x < \frac{\pi}{2}$  then

A.  $\cos x > 1 - \frac{2x}{\pi}$

B.  $\cos x < -\frac{2x}{\pi}$

C.  $\cos x > \frac{2x}{\pi}$

D.  $\cos x < \frac{2x}{x}$

**Answer: A**



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43. If  $0 < x < \frac{\pi}{2}$  then

A.  $\tan x < x < \sin x$

B.  $x < \sin x < \tan x$

C.  $\sin x < \tan x < x$

D. none of these

**Answer: D**



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44. Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be a function such that  $f(x) = ax + 3\sin x + 4\cos x$ .

Then  $f(x)$  is invertible if  $a \in (-5, 5)$  (b)  $a \in (-\infty, 5)$

$a \in (-5, +\infty)$  (d) none of these

A.  $a \in (-5, 5)$

B.  $a \in (-\infty, -5)$

C.  $a \in (5, \infty)$

D. none of these

**Answer: B**



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45. if the function  $f: \mathbb{R} \rightarrow \mathbb{R}$  given by  $f(x) = x^3 + ax^2 + 5x + \sin 2x$  is

invertible then

A.  $a \in (-\infty, -3)$

B.  $a \in (-3, 3)$

C.  $a \in (3, \infty)$

D. none of these

**Answer: C**



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**46.** If  $f(x) = \sin x$ ,  $x$  in  $[-\pi/2, \pi/2]$  then which one of the following is not correct ?

A.  $f(x)$  is increasing on the  $[-\pi/2, \pi/2]$

B.  $f'(x)$  is increasing on  $[-\pi/2, \pi/2]$

C.  $f''(x)$  is increasing on  $[-\pi/2, \pi/2]$

D.  $f''(x)$  is decreasing on  $[-\pi/2, 0]$  and is increasing on  $[-\pi/2, \pi/2]$

**Answer: A**



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47. If  $f: \mathbb{R} \rightarrow \mathbb{R}$  defined by  $f(x) = 3x + 2a \cos x - 5$  is invertible then 'a' belongs to

A.  $[-3/2, 3/2]$

B.  $(-\infty, 3/2] \cup [3/2, \infty)$

C.  $(-4, 4)$

D.  $\mathbb{R}$

**Answer: A**



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48. Let  $f(x)$  be a function defined by

$$f(x) = (ab - a^2 - 2)x - \cos^4 t + \int_0^x \sin^2 t - 2dt$$

If  $f(x)$  is a decreasing function for all  $x \in \mathbb{R}$  and  $a$  in  $\mathbb{R}$  where  $a$  is independent of  $x$ , then

A.  $a \cdot b \in (1, \infty)$

B.  $b \in (-1, 1)$

C.  $b \in (-\infty, ]$

D. non of these

**Answer: C**



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**49.** Let  $f(x)$  and  $g(x)$  be defined and differentiable for all  $x \geq x_0$  and  $f(x_0) = g(x_0)$   $f(x) \geq (x)f$  or  $x > x_0$  then

A.  $f(x) < g(x) \text{ for } x > x_0$

B.  $f(x) = g(x) \text{ for } x = x_0$

C.  $f(x) > g(x), x \leq x_0$

D. none of these

**Answer: C**

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50. If  $a < 0$  and  $f(x) = e^{ax} + e^{-ax}$  is monotonically decreasing . Find the interval to which  $x$  belongs.

A.  $f\{x : x > 0\}$

B.  $\{x : x < 0\}$

C.  $\{x : x < 1\}$

D.  $\{x : x < 1\}$

**Answer: A**

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51. If  $f(x) = \int_x^{x^2} \frac{1}{(\log t)^2} dt$ ,  $x \neq 1$  then  $f(x)$  is monotonically

A. increasing on  $(2, \infty)$

B. increasing on (1,2)

C. decreasing on  $2(\infty)$

D. decreasing on (0,3)

**Answer: A**



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**52.** The interval in which the function

$$f(x) = \int_0^x \left( \frac{t}{t+2} - \frac{1}{t} \right) dt \text{ will be non-increasing is}$$

A.  $(-2, -1] \cup (0, 3]$

B.  $(-2, -1] \cup [0, 3]$

C.  $(-2, -1] \cup [0, 2]$

D.  $(-2, -1] \cup (0, 2]$

**Answer: D**



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53. If  $f(x) = x^3 + bx^2 + cx + d$  and  $0 < b^2 < c$ , then

- A.  $f(x)$  is strictly increasing function
- B.  $f(x)$  has a local maxima
- C.  $f(x)$  is a strictly decreasing function
- D.  $f(x)$  is unbounded

**Answer: A**



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54. For the function  $f(x) = x \cos \frac{1}{x}$ ,  $x \geq 1$  which one of the following is incorrect ?

- A. for at least one  $x$  in the interval  $[1, \infty)$ ,  $f(x + 2) - f(x) < 2$
- B.  $\lim_{x \rightarrow \infty} f'(x) = 1$

C. for all  $x$  in the interval  $[1, \infty)$ ,  $f(x + 2) - f(x) > 2$

D.  $f(x)$  is strictly decreasing in the interval  $[1, \infty)$

**Answer: A**



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55. If the function  $g: (-\infty, \infty) \rightarrow \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$  is given by

$g(u) = 2 \tan^{-1}(e^u) - \frac{\pi}{2}$ . Then  $g$  is

A. even and is strictly increasing in  $(0, \infty)$

B. odd and is strictly decreasing  $(-\infty, \infty)$

C. odd and is strictly increasing in  $(-\infty, \infty)$

D. neither even nor odd, but is strictly increasing in  $(-\infty, \infty)$

**Answer: C**



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56. Consider the function  $f: (-\infty, \infty) \rightarrow (-\infty, \infty)$  defined by

$$f(x) = \frac{x^2 - ax + 1}{x^2 + ax + 1}; 0 < a < 2. \text{ Which of the following is true?}$$

- A.  $f'(x)$  is positive on  $(-\infty, 0)$  and negative on  $(0, \infty)$
- B.  $f'(x)$  is negative on  $(-\infty, 0)$  and positive on  $(0, \infty)$
- C.  $f'(x)$  changes sign on both  $(-\infty, 0)$  and  $(0, \infty)$
- D.  $f'(x)$  does not change sign on  $(-\infty, \infty)$

**Answer: B**



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57. Consider the polynomial  $f(x) = 1 + 2x + 3x^2 + 4x^3$  for all  $x \in \mathbb{R}$ . So

$f(x)$  has exactly one real root in the interval

- A.  $(-1/4, 0)$
- B.  $(-11, -3/4)$
- C.  $(-3/4, -1/2)$

D.  $(0, 1/4)$

**Answer: C**



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**58.** Consider the polynomial

$$f(x) = 1 + 2x + 3x^2 + 4x^3$$

Let  $s$  be the sum of all distinct real roots of  $f(x)$  and let  $t = |s|$

The real number  $s$  lies in the interval.

A. increasing in  $(-t, -1/4)$  and decreasing in  $(-1/4, t)$

B. decreasing  $(-t, -1/4)$  and increasing in  $(-1/4, t)$

C. increasing in  $(-t, t)$

D. decreasing  $(-t, t)$

**Answer: B**



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59. If  $f(x) = x^{\frac{3}{2}}(3x - 10)$ ,  $x \geq 0$ , then  $f(x)$  is increasing in \_\_\_\_.

A.  $(-\infty, -1) \cup (1, \infty)$

B.  $[2, \infty)$

C.  $(-\infty, -1) \cup [1, \infty)$

D.  $(-\infty, 0] \cup (2, \infty)$

**Answer: B**



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60. Let  $f(x) = \log(\sin x + \cos x)$ ,  $x$  in  $x \in (-\pi/4, (3\pi)/4)$

Then  $f$  is strictly increasing in the interval

A.  $\left(-\frac{\pi}{4}, \frac{\pi}{4}\right)$

B.  $\left(0, \frac{3\pi}{8}\right)$

C.  $\left(\frac{\pi}{2}, \frac{3\pi}{4}\right)$

D.  $\left(-\frac{\pi}{8}, \frac{\pi}{8}\right)$

**Answer: A**



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**61.** Let  $f(x) = (1 - x)^2 \sin^2 x + x^2$  for all  $x \in \mathbb{R}$  and let

$$g(x) = \int_1^x \left( \frac{2(t-1)}{t+1} - \ln t \right) f(t) dt \text{ for all } x \in (1, \infty).$$

Consider the statements :

P : There exists some  $x \in \mathbb{R}$  such that  $f(x) + 2x = 2(1 + x^2)$

Q : There exist some  $x \in \mathbb{R}$  such that  $2f(x) + 1 = 2x(1 + x)$

Then



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**62.**  $f(x) = x|\log_e x|$ ,  $x > 0$  is monotonically decreasing in

A.  $(e, \infty)$

B.  $(0, 1/e)$

C.  $(1/e, 1)$

D.  $(1, e)$

**Answer: C**



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**63.** Let  $F: \mathbb{R} \rightarrow \mathbb{R}$  be a thrice differentiable function. Suppose that  $F(1) = 0$ ,  $F(3) = -4$  and  $F'(x) < 0$  for all  $x \in (1/2, 3)$ . Let  $f(x) = xF(x)$  for all  $x \in \mathbb{R}$ . Then the correct statement(s) is (are)

A.  $f(1) < 0$

B.  $f(2) < 0$

C.  $f(x) \neq 0$  or *all*  $x \in (1, 3)$

D.  $f(x) = 0$  or *some*  $x \in$

**Answer: A::B::C**



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64. Let  $f(x) = 1 - x - x^3$ . Then, the real values of  $x$  satisfying the inequality,

$1 - f(x) - f^3(x) > f(1 - 5x)$ , are

A. (0,2)

B. (-2,2)

C.  $(-2, 1) \cup (1, \infty)$

D.  $(-\infty, -2) \cup (0, 2)$

**Answer: D**



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65. Let  $g(x) = f(\sin x) + f(\cos x)$ , then  $g(x)$  is decreasing on:

A.  $\left(\frac{\pi}{4}, \frac{\pi}{2}\right)$

B.  $\left(0, \frac{\pi}{4}\right)$

C.  $\left(0, \frac{\pi}{2}\right)$

D.  $\left(\frac{\pi}{2}, \frac{\pi}{2}\right)$

**Answer: B**



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66. Let  $f(x)$  be a monotonic polynomial of  $(2m-1)$  degree where  $m \in \mathbb{N}$ , then the equation

$f(x)+f(3x)+f(5x)+\dots+f(2m-1)x=(2m-1)$  has ..... roots.

A. at least one real root

B.  $(2m - 1)$  real roots

C. exactly one real root

D. none of these

**Answer: C**



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67. Let  $f(x) = \sin^4 x + \cos^4 x$ . Then  $f$  is increasing function in the interval

- A.  $\left(\frac{\pi}{4}, \frac{\pi}{2}\right)$
- B.  $\left(\frac{5\pi}{8}, \frac{3\pi}{4}\right)$
- C.  $\left(0, \frac{\pi}{4}\right)$
- D.  $\left(\frac{\pi}{2}, \frac{5\pi}{8}\right)$

**Answer: A**



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68. If  $f: R \rightarrow R$  is a twice differentiable function such that  $f''(x) > 0$  for all  $x \in R$ , and  $f\left(\frac{1}{2}\right) = \frac{1}{2}$  and  $f(1) = 1$ , then

- A.  $f(1) \leq 0$
- B.  $0 \leq f'(1) \leq \frac{1}{2}$



C.  $\frac{1}{2} < f'(1) \leq 1$

D.  $f(1) > 1$

**Answer: D**

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69. If  $f: \mathbb{R}$  is a differentiable function such that  $f(x) > 2f(x)$  for all  $x \in \mathbb{R}$  and  $f(0) = 1$  then

A.  $f(x)$  is increasing in  $(0, \infty)$

B.  $f(x)$  is decreasing in  $(0, \infty)$

C.  $f(x) < e^{2x}$  in  $(0, \infty)$

D.  $f(x) < e^{2x} \in (0, \infty)$

**Answer: A::C**

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## Section II Assertion Reason Type

1. Statement-1  $e^\pi > \pi^e$

Statement -2 The function  $x^{1/x}$  ( $x > 0$ ) is strictly decreasing in  $[e, \infty)$

- A. Statement-1 True statement -1 is True, Statement -2 is True  
statement -2 is a correct explanation for Statement-1
- B. Statement-1 True statement -1 is True, Statement -2 is True  
statement -2 is not a correct explanation for Statement-1
- C. Statement-1 True statement -1 is True, Statement -2 is False
- D. Statement-1 is False, Statement -2 is True

**Answer: A**



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2. Let  $f(x) = \tan^{-1} x - x + \frac{x^3}{6}$

Statement -1:  $f(x) < g(x)$  or  $0 < x \leq 1$

Statement -2:  $h(x) = \tan^{-1} x - x + \frac{x^3}{6}$  decreases on  $[-1,1]$

- A. Statement-1 True statement -1 is True, Statement -2 is True  
statement -2 is a correct explanation for Statement-2
- B. Statement-1 True statement -1 is True, Statement -2 is True  
statement -2 is not a correct explanation for Statement-2
- C. Statement-1 True statement -1 is True, Statement -2 is False
- D. Statement-1 is False, Statement -2 is True

**Answer: A**

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3. Statement-1  $e^x + e^{-x} > 2 + x^2$  is an increasing function on  $\mathbb{R}$ .

- A. Statement-1 True statement -1 is True, Statement -2 is True  
statement -2 is a correct explanation for Statement-3

B. Statement-1 True statement -1 is True, Statement -2 is True

statement -2 is not a correct explanation for Statement-3

C. Statement-1 True statement -1 is True, Statement -2 is False

D. Statement-1 is False, Statement -2 is True

**Answer: A**

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4. Statement-1  $f(x) = \frac{\sin x}{x} < 1$  for  $0 < x < \frac{\pi}{2}$

Statement -2  $f(x) = \frac{\sin x}{x}$  is decreasing function on  $(0, \pi/2)$

A. Statement-1 True statement -1 is True, Statement -2 is True

statement -2 is a correct explanation for Statement-4

B. Statement-1 True statement -1 is True, Statement -2 is True

statement -2 is not a correct explanation for Statement-4

C. Statement-1 True statement -1 is True, Statement -2 is False

D. Statement-1 is False ,Statement -2 is True

**Answer: A**

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5. Let  $f(x) = 2 \tan^{-1} \left( \frac{1-x}{1+x} \right)$

A. Statement-1 True statement -1 is True,Statement -2 is True

statement -2 is a correct explanation for Statement-5

B. Statement-1 True statement -1 is True,Statement -2 is True

statement -2 is not a correct explanation for Statement-5

C. Statement-1 True statement -1 is True,Statement -2 is False

D. Statement-1 is False ,Statement -2 is True

**Answer: A**

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6. Let  $f(x) = \frac{20}{4x^2 - 9x^2 + 6x}$

Statement -1 : Range of  $f = [6, 20]$

Statement -2  $f(x)$  increases on  $(1/2, 1)$  and decreases on  $(1, \infty) \cup (-\infty, 0) \cup (0, 1/2)$

- A. Statement-1 True statement -1 is True, Statement -2 is True  
statement -2 is a correct explanation for Statement-1
- B. Statement-1 True statement -1 is True, Statement -2 is True  
statement -2 is not a correct explanation for Statement-1
- C. Statement-1 True statement -1 is True, Statement -2 is False
- D. Statement-1 is False, Statement -2 is True

**Answer: D**



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7. Statement-1 : For  $0 \leq p < 1$  and for any positive  $a$  and  $b$  the inequality  $(a + b)^p < a^p + b^p$  is valid

Statement - 2: For  $0 \leq p \leq 1$  the function  $f(x) = 1 + x^p - (1 + x)^p$  decreases on  $[0, \infty)$

A. Statement-1 True statement -1 is True, Statement -2 is True

statement -2 is a correct explanation for Statement-1

B. Statement-1 True statement -1 is True, Statement -2 is True

statement -2 is not a correct explanation for Statement-1

C. Statement-1 True statement -1 is True, Statement -2 is False

D. Statement-1 is False, Statement -2 is True

**Answer: C**



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8. Statement-1: Let  $f(x)$  and  $g(x)$  be two real functions connected by the relation

$$g(x) = f(x) - 2(f(x))^2 + 4(f(x))^3$$

Then  $f(x)$  and  $g(x)$  increase or decrease together .

Statement-2:

if

$b^2 - 4ac < 0$  and  $a > 0$  then  $ax^2 + bx + c > 0$  for all  $x \in R$

A. Statement-1 True statement -1 is True, Statement -2 is True

statement -2 is a correct explanation for Statement-1

B. Statement-1 True statement -1 is True, Statement -2 is True

statement -2 is not a correct explanation for Statement-1

C. Statement-1 True statement -1 is True, Statement -2 is False

D. Statement-1 is False , Statement -2 is True

**Answer: A**



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1. If  $f$  and  $g$  are two increasing function such that  $f \circ g$  is defined then

- A.  $f \circ g$  is an increasing functions
- B.  $f \circ g$  is a decreasing function
- C.  $f \circ g$  is neither inceasing nor decreasing
- D. none of these

**Answer: A**



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2. If  $f$  is decreasing and  $g$  is increasing functions such that  $f \circ g$  exists then  $f \circ g$  is

- A. an increasing function
- B. a decreasing function

C. neither increasing nor decreasing

D. none of these

**Answer: A**



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3. If  $f$  is an increasing function and  $g$  is a decreasing function on an interval  $I$  such that  $fg$  exists, then :

A.  $fg$  is an increasing function on  $I$

B.  $fg$  is a decreasing function on  $I$

C.  $fg$  is neither increasing nor decreasing on  $I$

D. none of these

**Answer: B**



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4. Let  $y = x^2 e^{-x}$  then the interval in which  $y$  increases with respect to  $x$  is

A.  $(-\infty, \infty)$

B.  $(-2, 0)$

C.  $(2, \infty)$

D.  $(0, 2)$

**Answer: D**



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5. The interval in which the function  $f(x) = x^{e^{2-x}}$  increases is

A.  $(-\infty, 0)$

B.  $(2, \infty)$

C.  $(0, 2)$

D. none of these

**Answer: D**



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6. The function  $f(x) = \cos\left(\frac{\pi}{x}\right)$ , ( $x \neq 0$ ) is increasing in the interval

A.  $(2n + 1, 2n)$ ,  $n \in \mathbb{N}$

B.  $\left(\frac{1}{2n + 1}, 2n\right)$ ,  $n \in \mathbb{N}$

C.  $\left(\frac{1}{2n + 2}, \frac{1}{2n + 1}\right)$

D. none of these

**Answer: D**



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7. The value of  $b$  for which the function  $f(x) = \sin x - bx + c$  is decreasing in the interval  $(-\infty, \infty)$  is given by

A.  $b < 1$

B.  $b \geq 1$

C.  $b > 1$

D.  $b \leq 1$

**Answer: C**

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8. For what values of  $a$ , the function

$$f(x) = \left\{ \left( \frac{\sqrt{a+4}}{1-a} \right) x^5 - 3x + \log(5) \right\} \text{ decreases for all real } x.$$

A.  $(\infty, \infty)$

B.  $\left[ -4, \frac{3 - \sqrt{21}}{2} \right] \cup [1, \infty)$

C.  $\left( -3, 5 - \frac{\sqrt{27}}{2} \right) \cup (2, \infty) \cup [1, \infty)$

D.  $(1, \infty)$

**Answer: B**



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9. Find the least value of ' $a$ ' such that the function  $f(x) = x^2 + ax + 1$  is increasing on  $[1, 2]$ . Also, find the greatest value of ' $a$ ' for which  $f(x)$  is decreasing on  $[1, 2]$ .

A.  $(-2, \infty)$

B.  $[-4, \infty)$

C.  $[-\infty, -2)$

D.  $(-\infty, 2]$

**Answer: A**



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10. On which of the following intervals is the function  $f(x) = x^{100} + \sin x - 1$  increasing? (i)  $(0, \pi/2)$  (ii)  $(\pi/2, \pi)$  (iii)  $(0, 1)$  (iv)  $(-1, 1)$ .

A.  $(0, \frac{\pi}{2})$

B.  $(0, 1)$

C.  $(\pi/2, \pi)$

D. none of these

**Answer: D**



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11. Which of the following functions is not decreasing on  $(0, \pi/2)$ ?

A.  $\cos x$

B.  $\cos 2x$

C.  $\cos^2 x$

D.  $\tan x$

**Answer: D**



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12. Let  $f'(x) = f(x)(x - a)^2$ , where  $g(a) \neq 0$  and  $g$  is continuous at  $x=a$  then

A.  $f$  is increasing in the nbd of  $a$

B.  $f$  is decreasing in the nbd

C.  $f$  increases or decreases in the nbd of  $a$  according as  $g(a) > 0$  or  $g(a) < 0$

D. none of these

**Answer: C**



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13. Show that  $f(x) = 2x + \cot^{-1} x + \log(\sqrt{1+x^2} - x)$  is increasing in  $\mathbb{R}$ .

- A. increases on  $\mathbb{R}$
- B. decreases in  $[0, \infty)$
- C. neither increasing nor decreasing in  $(0, \infty)$
- D. none of these

**Answer: A**



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14. The function  $f(x) = \log(1+x) - (2+x)$  is increasing in

- A.  $(0, \infty)$
- B.  $(-\infty, 0)$
- C.  $(-\infty, \infty)$
- D. none of these

**Answer: D**

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15. On which of the following intervals in the function  $f(x) = 2x^2 - \log|x|$ ,  $x \neq 0$  increasing ?

A.  $\left(\frac{1}{2}, \infty\right)$

B.  $(-\infty, -1/2) \cup (0, 1/2)$

C.  $(-\infty, -1/2) \cup (1/2, \infty)$

D.  $(-1/2, 0) \cup (1/2, \infty)$

**Answer: D**

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16. If the function  $f(x) = \frac{K \sin x + 2 \cos x}{\sin x + \cos x}$  is strictly increasing for all values of  $x$ , then  $K < 1$  (b)  $K > 1$   $K < 2$  (d)  $K > 2$

A.  $K < 1$

B.  $K > 1$

C.  $K < 2$

D.  $K > 2$

**Answer: D**

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17. The function  $f(x) = \frac{a \sin x + b \cos x}{c \sin x + d \cos x}$  is decreasing, if

A.  $ad - bc > 0$

B.  $ad - bc < 0$

C.  $ab - cd > 0$

D.  $ab - cd < 0$

**Answer: B**

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18. If  $f(x) = kx^3 - 9x^2 + 9x + 3$  monotonically increasing in  $R$ , then

$k < 3$  (b)  $k \leq 2$   $k \geq 3$  (d) none of these

A.  $K < 3$

B.  $K > 3$

C.  $k \leq 3$

D. none of these

**Answer: B**



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19. Find the value of  $a$  for which the function

$(a + 2)x^3 - 3ax^2 + 9ax - 1$  decreases monotonically for all real  $x$ .

A.  $a < -2$

B.  $a > -2$

C.  $-3 < a < 0$

D.  $-\infty < a \leq -3$

**Answer: D**



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20. The function  $y = x^3 - 3x^2 + 6x - 17$

A. increases everywhere

B. decreases everywhere

C. increases for positive  $x$  and decreases for negative  $x$

D. increases for negative  $x$  and decreases for positive  $x$

**Answer: A**



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21. The interval in which the function  $x^3$  increases less rapidly than  $6x^2 + 15x + 5$  is :

A.  $(-\infty, -1)$

B.  $(-5, 1)$

C.  $(-1, 5)$

D.  $(5, \infty)$

**Answer: C**



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22. The interval in which the function  $f(x) = \sin x - \cos x - ax + b$  decreases for all real values of  $x$  is given by

A.  $a \geq \sqrt{2}$

B.  $a \leq 1$

C.  $a < \sqrt{2}$

D.  $a < 1$

**Answer: A**



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23. The function  $y = \cot^{-1} x - \log(x + \sqrt{x^2 + 1})$  is decreasing in

A.  $(-\infty, 0)$

B.  $(-\infty, 0)$

C.  $(0, \infty)$

D.  $(-\infty, \infty)$

**Answer: D**



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24. the function  $\frac{|x - 1|}{x^2}$  is monotonically decreasing at the point

A.  $(2, \infty)$

B.  $(0, 1)$

C.  $(-\infty, 1)$

D.  $(\infty, \infty)$

**Answer: C**



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25. Find the value of  $a$  in order that  $f(x) = \sqrt{3}\sin x - \cos x - 2ax + b$  decreases for all real values of  $x$ .

A.  $a < 1$

B.  $a \leq 1$

C.  $a \leq \sqrt{2}$

D.  $a < \sqrt{2}$

**Answer: B**



26. A function is matched below against an interval where it is supposed to be increasing. Which of the following parts is incorrectly matched?

Interval, Function  $[2, \infty)$  ,  $2x^3 - 3x^2 - 12x + 6$   $(-\infty, \infty)$  ,  
 $x^3 = 3x^2 + 3x + 3$   $(-\infty, -4)$  ,  $x^3 + 6x^2 + 6$   $\left(-\infty, \frac{1}{3}\right)$  ,  
 $3x^2 - 2x + 1$

- A. interval      Function  
(a)  $(-\infty, -4]$   $f(x) = x^3 + 6x^2 + 6$
- B. interval      Function  
(a)  $(-\infty, 1/3]$   $g(x) = 3x^3 - 2x + 1$
- C. interval      Function  
(a)  $(2, \infty]$   $h(x) = 2x^3 - 3x^2 + 12x + 6$
- D. interval      Function  
(a)  $(-\infty, \infty]$   $q(x) = x^3 - 3x^2 + 3x + 3$

Answer: B

27. A condition for a function  $y=f(x)$  to have an inverse is that it should be

A. defined for all  $x$

B. continuous for all  $x$

C. strictly monotone and continuous in the domain

D. an even function

**Answer: C**

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**28.** Let  $g(x) = f(x) + f(1 - x)$  and  $f''(x) < 0$ , when  $x \in (0, 1)$ . Then  $f(x)$  is

A.  $g(x)$  increases on  $[0,1]$

B.  $g(x)$  increases on  $[0,1]$

C.  $g(x)$  increases on  $[0,1]$

D.  $g(x)$  increases on  $[0,1/2]$  and decreases on  $[1/2,1]$

**Answer: B**

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29. The function  $f(x) = \frac{\ln(\pi + x)}{\ln(e + x)}$  is

- A. increasing function on  $[0, \infty)$
- B. decreases on  $[1/2, 1]$
- C. increasing on  $[0, \pi/e]$  and increasing on  $[\pi/e, \infty)$
- D. decreasing on  $[0, \pi/e]$  and increasing on  $[\pi/e, \infty)$

**Answer: B**

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30. Column I, Column II

$\int \frac{e^{2x} - 1}{e^{2x} + 1} dx$	$\int \frac{1}{(e^x + e^{-x})^2} dx$	$\int \frac{e^{-x}}{1 + e^x} dx$	$\int \frac{1}{\sqrt{1 - e^{2x}}} dx$
$\log(e^x + 1) - x - e^{-x} + c$	$\log(e^x + 1) - x + c$	$\log(e^x + 1) - x - e^{-x} + c$	$\log(e^x + 1) - x + c$

$\int \frac{e^{2x} - 1}{e^{2x} + 1} dx$  is equivalent to  $o$ , p.  
 $\int \frac{1}{(e^x + e^{-x})^2} dx$  is equivalent to  $o$ , q.  
 $\int \frac{e^{-x}}{1 + e^x} dx$  is equivalent to  $o$ , r.  
 $\int \frac{1}{\sqrt{1 - e^{2x}}} dx$  is equivalent to  $o$ , s.  $-\frac{1}{2(e^{2x} + 1)} + c$

- A. an increasing function  $\mathbb{R}$
- B. a decreasing function on  $\mathbb{R}$
- C. an even function on  $\mathbb{R}$
- D. none of these

**Answer: A**

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31.  $y = \{x(x - 3)^2\}$  increases for all values of  $x$  lying in the interval

- A.  $0 < x < \frac{3}{2}$
- B.  $0 < x < \infty$
- C.  $-\infty < x < 0$
- D.  $1 < x < 3$

**Answer: A**

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32. If  $a < 0$  and  $f(x) = e^{ax} + e^{-ax}$  is monotonically decreasing . Find the interval to which  $x$  belongs.

A.  $x > 0$

B.  $x < 0$

C.  $x < 1$

D.  $x < 1$

**Answer: B**



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33. The function  $f(x) = \tan x - x$

A. always increases

B. always decreases

C. neverdecreases

D. some times increases and some time decreases

**Answer: A**



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**34.** The function  $f(x) = \cot^{-1} x + x$  increases in the interval (a)  $(1, \infty)$   
(b)  $(-1, \infty)$  (c)  $(-\infty, \infty)$  (d)  $(0, \infty)$

A.  $(1, \infty)$

B.  $(-1, \infty)$

C.  $(-\infty, \infty)$

D.  $(0, \infty)$

**Answer: A**



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35. The function  $f(x) = (\log)_e \left( x^3 + \sqrt{x^6 + 1} \right)$  is of the following types: (a) even and increasing (b) odd and increasing (c) even and decreasing (d) odd and decreasing

A. even and increasing

B. odd and increasing

C. even and decreasing

D. odd and decreasing

**Answer: B**



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36. Let  $f(x) = x^3 - 6x^2 + 15x + 3$ . Then, (a)  $f(x) > 0$  for all  $x \in R$  (b)  $f(x) > f(x + 1)$  for all  $x \in R$  (c)  $f(x)$  is invertible (d)  $f(x) < 0$  for all  $x \in R$

A.  $f(x) < 0$  for all  $x \in R$

B.  $f(x) > f(x + 1)$  or  $\forall x \in \mathbb{R}$

C.  $f(x)$  is invertible

D. none of these

**Answer: C**



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## Chapter Test

1. the function  $f(x) = \frac{\log x}{x}$  is increasing in the interval

A.  $(1, 2e)$

B.  $(0, e)$

C.  $(2, 2e)$

D.  $(1/e, 2e)$

**Answer: B**





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2. If the function  $f(x) = \cos|x| - 2ax + b$  increases along the entire number scale, then (a)  $a = b$  (b)  $a = \frac{1}{2}b$  (c)  $a \leq -\frac{1}{2}$  (d)  $a > \frac{3}{2}$

A.  $a \leq b$

B.  $a = \frac{b}{2}$

C.  $a < -\frac{1}{2}$

D.  $a > -\frac{3}{2}$

Answer: C



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3. If  $f(x) = kx - \sin x$  is monotonically increasing then

A.  $k > 1$

B.  $k > -1$

C.  $k < 1$

D.  $k < -1$

**Answer: A**

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4. The function  $f(x) = x\sqrt{ax - x^2}$ ,  $a < 0$

A. increases on the interval  $(0, 3a/4)$

B. decreases on the interval  $(, 3a/4)$

C. decreases on the interval  $(0, 3a/4)$

D. increases on the interval  $(3a/4, a)$

**Answer: A**

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5. The function  $f(x) = \sin^4 x + \cos^4 x$  increasing if

- A.  $0 < x < \pi/8$
- B.  $\pi/4 < x < 3\pi/8$
- C.  $3\pi/8 < x < 5\pi/8$
- D.  $5\pi/8 < x < 3\pi/4$

**Answer: B**



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6. Let  $f(x) = \cot^{-1} g(x)$  where  $g(x)$  is an increasing function on the interval  $(0, \pi)$  Then  $f(x)$  is

- A. increasing on  $(0, \pi)$
- B. decreasing on  $(0, \pi)$
- C. increasing on  $(0, \pi/2)$  and decreasing on  $(\pi/2, \pi)$
- D. none of these

**Answer: B**



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7. The values of  $x$  for which

$$1 + x \log_e \left( x + \sqrt{x^2 + 1} \right) \leq \sqrt{x^2 + 1} \text{ are}$$

A.  $x \leq 0$

B.  $0 \leq x \leq 1$

C.  $x \geq 0$

D. none of these

**Answer: C**



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8. Let  $g(x) = f(x) - 2\{f(x)\}^2 + 9\{f(x)\}^3$  for all  $x \in R$  Then

- A.  $g(x)$  and  $f(x)$  increase and decrease together
- B.  $g(x)$  increases whenever  $f(x)$  decreases and vice-versa
- C.  $g(x)$  increases for all  $x \in R$
- D.  $g(x)$  decreases for all  $x \in R$

**Answer: A**

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9. The function  $f(x) = x^{1/x}$  is increasing in the interval

- A.  $(e, \infty)$
- B.  $(-\infty, e)$
- C.  $(-e, e)$
- D. none of these

**Answer: B**

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10. If  $\phi(x)$  is continuous at  $x = a$  such that

$f(x) = (ax - a^2 - x^2)\phi(x)$  for all  $x$ , then  $f(x)$  is

- A. increasing in the neighbourhood of  $x = \alpha$
- B. decreasing in the neighbourhood of  $x = \alpha$
- C. constant in the neighbourhood of  $x = \alpha$
- D. minimum at  $x = \alpha$

**Answer: A**



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11. The function  $f(x)$  given by  $f(x) = \begin{vmatrix} x+1 & 1 & 1 \\ 1 & x+1 & 1 \\ 1 & 1 & x+1 \end{vmatrix}$  is increasing on

- A.  $\mathbb{R}$
- B.  $(-2, 0)$

C.  $\mathbb{R} - [-2, 0]$

D. none of these

**Answer: C**



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12. If  $f(x) = 2x^3 + 9x^2 + \lambda x + 20$  is a decreasing function for  $x$  in the largest possible interval  $(-2, -1)$  then  $\lambda =$

A. 12

B. -12

C. 6

D. none of these

**Answer: A**



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13. The set of values of  $a$  for which the function

$f(x) = 2e^x - ae^{-x} + (2a + 1)x - 3$  is increasing on  $\mathbb{R}$ , is

- A.  $[0, \infty)$
- B.  $(-\infty, 0)$
- C.  $(-\infty, \infty)$
- D. none of these

**Answer: A**



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14. The function  $f(x) = xe^{1-x}$  strictly

- A. increases in interval  $(0, \infty)$
- B. decreases in the interval  $(0, 2)$
- C. increases in the interval  $(1/2, 2)$
- D. decreases in the interval  $(1, \infty)$



**Answer: D**



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15. The function  $f(x) = \tan^{-1} x - x$  is decreasing on the set

A.  $\mathbb{R}$

B.  $(0, \infty)$

C.  $\mathbb{R} - [0]$

D. none of these

**Answer: A**



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16. If  $0 < x < \frac{\pi}{2}$  then

A.  $\cos(\sin x) > \cos x$

B.  $\cos(\sin x) < \cos x$

C.  $\cos(\sin x) = \sin(\cos x)$

D.  $\cos(\sin x) < \sin(\cos x)$

**Answer: A**



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17. If  $f$  is real-valued differentiable function such that  $f(x)f'(x) < 0$  for all real  $x$ , then

A.  $f(x)$  is increasing

B.  $f(x)$  is decreasing

C.  $|f(x)|$  is increasing

D.  $|f(x)|$  is decreasing

**Answer: D**



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18. For what value of  $a$ ,  $f(x) = -x^3 + 4ax^2 + 2x - 5$  decreasing for all  $x$ .

A. (1,2)

B. (3,4)

C. R

D. no value of  $a$

**Answer: D**



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