



MATHS

JEE (MAIN AND ADVANCED MATHEMATICS) FOR BOARD AND COMPETITIVE EXAMS

COMPLEX NUMBERS AND QUADRATIC EQUATIONS

Example

1. Evaluate the followings :

(i) i^{23}

(ii) i^{-97}



Watch Video Solution

2. Evaluate $\frac{i^{81} + 1}{(i^{253})^9}$



Watch Video Solution

3. Plot the complex number $-6 + 7i$ on the Argand plane.



Watch Video Solution

4. write the complex numbers that are represented by the following points in the complex plane

(i) $0,3$ (ii) $(-1,0)$



Watch Video Solution

5. Find the values of x and y , if $2x + 3yi = 2 + 12i$, where $x, y \in R$



Watch Video Solution

6. If $Z_1 = 2 + 3i$ and $z_2 = -1 + 2i$ then find

(i) $z_1 + z_2$

(ii) $z_1 - z_2$

(iii) $z_1 \cdot z_2$

(iv) $\frac{z_1}{z_2}$



Watch Video Solution

7. If $z_1 = 3 - 2i$, $z_2 = 2 - i$ and $z_3 = 2 + 5i$ then find $z_1 + z_2 - 2z_3$



Watch Video Solution

8. If $z = 4 + 7i$ be a complex number, then find

(i) Additive inverser of z .

(ii) Multiplicative inverse of z .



Watch Video Solution

9. Express the following in the form of $a + ib$.

(i) $\left(\frac{1}{2} + 3i\right)^2$

(ii) $(2 + 3i)(2 - 3i)$



Watch Video Solution

10. Express the following in the form of $a + ib$.

(i) $\left(\frac{1}{4} + 4i\right)^2$

,



Watch Video Solution

11. Express the following in the form of $a + ib$

(i) $\frac{4 + 3i}{5 + 3i}$



Watch Video Solution

12. Prove that the complex number $\left(\frac{3+2i}{2-3i}\right) + \left(\frac{3-2i}{2+3i}\right)$ is purely real.



Watch Video Solution

13. Plot the conjugate of the complex number $-2 + 7i$ on the Argand plane



Watch Video Solution

14. Find the conjugate of

$$\frac{1}{2+5i}$$



Watch Video Solution

15. If $z_1 = 3 + 2i$ and $z_2 = 2 - i$ then verify that

$$(i)\overline{z_1 + z_2} = \bar{z}_1 + \bar{z}_2$$



Watch Video Solution

16. if $z_1 = 1 - i$ and $z_2 = -2 + 4i$ then find $Im\left(\frac{z_1 z_2}{\bar{z}_1}\right)$



Watch Video Solution

17. Find real values of x and y for which the complex numbers $-5 + ix^2y$ and $x^2 + y + 35i$ are conjugate of each other .



Watch Video Solution

18. If $\frac{p + iq}{r + is} = x + iy$, prove that $\frac{p - iq}{r - is} = x - iy$ and $\frac{p^2 + q^2}{r^2 + s^2} = x^2 + y^2$, where $p, q, r, s, x, y, \in R$



Watch Video Solution

19. Represent the modulus of $8 + 6i$ in the Argand plane .



Watch Video Solution

20. Find the modulus of the following complex number $(3 + 4i)(1 + 5i)$



Watch Video Solution

21. If $z_1 = 3 - 4i$ and $z_2 = 5 + 7i$, verify

(i) $|-z_1| = |z_1|$

(ii) $|z_1 + z_2| < |z_2|$



Watch Video Solution

22. Find the modulus and argument of the complex number $3\sqrt{2} - 3\sqrt{2}i$

.



Watch Video Solution

23. Find modulus of

(i) $\frac{2 + 4i}{2 - 6i}$



Watch Video Solution

24. Find the square roots of the following complex numbers.

(i) $-6 - 8i$



Watch Video Solution

25. Solve the following quadratic equations :

(i) $9x^2 - 8x + 2 = 0$

(ii) $\sqrt{7}x^2 + x + \sqrt{7} = 0$

(iii) $2\sqrt{3}x^2 - \sqrt{2}x + 3\sqrt{3} = 0$



Watch Video Solution

26. Solve $x^2 - (\sqrt{2} + i)x + \sqrt{2}i = 0$



Watch Video Solution

27. If $x_n = \frac{\cos \pi}{3^n} + i \frac{\sin(\pi)}{3^n}$, then $x_1, x_2, x_3, \dots \dots \dots x_\infty$ is equal to



Watch Video Solution

28. If $1, \alpha, \alpha^2, \alpha^3, \dots, \alpha^{n-1}$ are n n^{th} roots of unity, then find the value of $(2011 - \alpha)(2011 - \alpha^2) \dots (2011 - \alpha^{n-1})$



Watch Video Solution

29. If α is one of the non real imaginary seventh roots of unity, then form the quadratic equation whose roots are given by $\alpha + \alpha^2 + \alpha^4$ and $\alpha^3 + \alpha^5 + \alpha^6$

[Watch Video Solution](#)

30. Find the greatest and least value of

$$|z_1 + z_2| = \text{ if } z_1 = 24 + 7i \text{ and } |z_2| = 7$$

[Watch Video Solution](#)

31. about to only mathematics

[Watch Video Solution](#)

32. if $z_1, z_2, z_3, \dots, z_n$ are complex numbers such that

$$|z_1| = |z_2| = \dots = |z_n| = \left| \frac{1}{z_1} + \frac{1}{z_2} + \frac{1}{z_3} + \dots + \frac{1}{z_n} \right| = 1$$

Then show that $|z_1 + z_2 + z_3 + \dots + z_n| = 1$

[Watch Video Solution](#)

33. If z_1 and z_2 are two complex numbers such that $|z_1| < 1 < |z_2|$, then prove that $|(1 - z_1 \bar{z}_2) / (z_1 - z_2)| < 1$



Watch Video Solution

34. Find the complex number z if $z\bar{z} = 2$ and $z + \bar{z} = 2$



Watch Video Solution

35. If $iz^3 + z^2 - z + i = 0$, where $i = \sqrt{-1}$, then $|z|$ is equal to 1 (b) $\frac{1}{2}$
(c) $\frac{1}{4}$ (d) None of these



Watch Video Solution

36. If ω is a cube root of unity but not equal to 1, then minimum value of $|a + b\omega + c\omega^2|$, (where a, b and c are integers but not all equal), is



Watch Video Solution

37. If $\arg(z_1) = \frac{2\pi}{3}$ and $\arg(z_2) = \frac{\pi}{2}$, then find the principal value of $\arg(z_1 z_2)$ and also find the quadrant of $z_1 z_2$.



Watch Video Solution

38. If $\arg(z) < 0$, then find $\arg(-z) - \arg(z)$.



Watch Video Solution

39. If the complex numbers z_1, z_2 and z_3 represent the vertices of an equilateral triangle such that $|z_1| = |z_2| = |z_3|$ then relation among z_1, z_2 and z_3



Watch Video Solution

40. Find the condition in order that z_1, z_2, z_3 are vertices of an isosceles triangle right angled at z_2 .



Watch Video Solution

41. Show that the area of the triangle on the Argand diagram formed by the complex number z, iz and $z + iz$ is $\frac{1}{2}|z|^2$



Watch Video Solution

42. If $|z - 25i| \leq 15$, then find

(i) Maximum $|z|$ (2) Maximum $\arg(z)$

(3) minimum $|z|$ (4) Minimum $\arg(z)$



Watch Video Solution

43. Show that if $z_1 z_2 + z_3 z_4 = 0$ and $z_1 + z_2 = 0$, then the complex numbers z_1, z_2, z_3, z_4 are concyclic.



Watch Video Solution

44. Locate the points representing the complex number z on the Argand plane.

(a) $|z + 1 - 2i| = 2\sqrt{2}$

(b) $|z - 1|^2 + |z + 1|^2 = 4$

(c) $\left| \frac{z - 2008}{z + 2008} \right| = 2007$

(d) $|z - 2008| = |z - 2007i|$

(e) $|z - 2008| + |z + 2008| = 4018$



View Text Solution

45. If θ is real and z_1, z_2 are connected by $z_1^2 + z_2^2 + 2z_1 z_2 \cos \theta = 0$, then prove that the triangle formed by vertices O, z_1 and z_2 is isosceles.



Watch Video Solution

46. Show that there is no complex number such that

$$|z| \leq \frac{1}{2} \text{ and } z^n \sin \theta_0 + z^{n-1} \sin \theta_2 + \dots + z \sin \theta_{n-1} + \sin \theta_n = 2$$

where $\theta, \theta_1, \theta_2, \dots, \theta_{n-1}, \theta_n$ are reals and $n \in \mathbb{Z}^+$.



Watch Video Solution

47. If z is a complex number lying in the fourth quadrant of Argand plane

and $\left| \left[\frac{kz}{k+1} \right] + 2i \right| > \sqrt{2}$ for all real value of $k (k \neq -1)$, then range

of $\arg(z)$ is $\left(\frac{\pi}{8}, 0 \right)$ b. $\left(\frac{\pi}{6}, 0 \right)$ c. $\left(\frac{\pi}{4}, 0 \right)$ d. none of these



Watch Video Solution

48. If $z_1 = a + ib$ and $z_2 = c + id$ are complex numbers such that

$$|z_1| = |z_2| = 1 \text{ and } \operatorname{Re}(z_1 \bar{z}_2) = 0,$$

then the pair of complex numbers $w_1 = a + ic$ and $w_2 = b + id$ satisfies :



Watch Video Solution

49. if the roots of the equation $z^2 + (p + iq)z + r + is = 0$ are real when $p, q, r, s, \in \mathbb{R}$, then determine $s^2 + q^2 r$.



Watch Video Solution

50. Let P, Q, R be points represented by complex numbers z_1, z_2, z_3 and circumcentre of $\triangle PQR$ coincides with origin, Let the altitude, PL of the \triangle meets the circumcircle again at M , then find the complex number representing the point M .



Watch Video Solution

51. If the ratio $\frac{z - i}{z - 1}$ is purely imaginary, prove that the point z lies on the circle whose centre is the point $\frac{1}{2}(1 + i)$ and radius is $\frac{1}{\sqrt{2}}$



Watch Video Solution

52. Find the locus of complex number z , satisfying $(z + 1)^n = z^n$



Watch Video Solution

53. If $2 + \sqrt{3}i$ is a root of the equation $x^2 + px + 1 = 0$, then write the values of p and q .



Watch Video Solution

54. If α, β are the roots of the equation $(x - a)(x - b) = c, c \neq 0$. Find the roots of the equation $(x - \alpha)(x - \beta + c) = 0$



Watch Video Solution

55. Discuss the nature of roots of equation

$x^2 + ax + b = 0$ and $x^2 + cx + d = 0$, where a, b, c, d are real numbers and

$ac = 2(b + d)$



Watch Video Solution

56. Fill in the blanks If the quadratic equations $x^2 + ax + b = 0$ and $x^2 + bx + a = 0$ ($a \neq b$) have a common root, then the numerical value of $a + b$ is _____.



Watch Video Solution

57. Find a relation between a, b, c so that two quadratic equations $ax^2 + bx + c = 0$ and $1003x^2 + 1505x + 2007 = 0$ have a common root.



Watch Video Solution

58. If two equations $x^2 + ax + bc = 0$ and $x^2 + bx + ca = 0$ have a common root, then find the condition and the quadratic with other roots of the equations.



Watch Video Solution

59. Discuss the sign scheme of the expesion
$$\frac{(x^2 - 2011x + 2010)(x^2 + 2011x - 2012)}{(x^2 - 4x + 4)(x^2 - 8x + 15)(x^2 - 5x + 6)^2}$$



Watch Video Solution

60. for what values of m , the equation $2x^2 - 2(2m + 1)x + m(m + 1) = 0$ $m \in R$ has (i) Both roots smaller than 2 ? (ii) Both roots greater than 2 ? (iii) Both roots lie in the interval (2,3) ? (iv) Exactly one root lie in the interval (2,3) ? (v) One root is smaller than 1, and the other root is greater than 1 ? (vi) One root is greater than 3 and the other root is smaller than 2 ? (vii) Roots α and β are such that both 2 and 3 lie between α and β ?



View Text Solution

61. If the roots of the cubic equation $x^3 - 9x^2 + a = 0$ are in A.P., Then find one of roots and a

[Watch Video Solution](#)

62. Find the number of real roots of the equation

$$f(x) = x^3 + 2x^2 + x + 2 = 0$$

[Watch Video Solution](#)

63. If the equation $2x^3 - 6x + k = 0$ has three real and distinct roots, then find the value (s) of k .

[Watch Video Solution](#)

64. if α, β, γ are the roots of $x^3 + x^2 + x + 9 = 0$, then find the equation whose roots are $\frac{\alpha + 1}{\alpha - 1}, \frac{\beta + 1}{\beta - 1}, \frac{\gamma + 1}{\gamma - 1}$

[Watch Video Solution](#)

65. The equations $ax^2 + bx + c = 0$, $x^3 - 2x^2 + 2x - 1 = 0$ have two roots common, then find the value of $a+b$.



Watch Video Solution

66. find the condition that $px^3 + qx^2 + rx + s = 0$ has exactly one real root, where $p, q, r, s, \in R$



Watch Video Solution

67. if α, β be the roots of $x^2 - (a - 2)x - a - 1 = 0$ then the least value of $\alpha^2 + \beta^2$ is (1) 0 (2) 1 (3) 3 (4) 5



Watch Video Solution

68. If the quadratic equation $a^2(b^2 - c^2)x^2 + b^2(c^2 - a^2)x + c^2(a^2 - b^2) = 0$ has real and equal

roots, than a^2, b^2, c^2 are

(1) A.P. (2) (G.P. (3) H.P. (4) A.G.P.



Watch Video Solution

69. The number of solution of the equation

$$|x - x^2 - 1| = |2x - 3 - x^2| \text{ is}$$

(1) 0 (2) 1 (3) (4) Infinitely many



Watch Video Solution

70. Let $a, b, c \in R$ and $a > 0$. If the quadratic equation

$ax^2 + bx + c = 0$ has two real roots α and β such that

$\alpha > -1$ and $\beta > 1$, then show that $1 + \left| \frac{b}{a} \right| + \frac{c}{a} > 0$



Watch Video Solution

71. The equation $x^2 + px + q = 0$ has two roots α, β then

Choose the correct answer :

(1) The equation $qx^2 + (2q - p^2)x + q$ has roots

(1) $\frac{\alpha}{\beta}, \frac{\beta}{\alpha}$ (2) $\frac{1}{\alpha}, \frac{1}{\beta}$

(3) α^2, β^2 (4) None of these

(2) The equation whose roots are $\frac{1}{\alpha}, \frac{1}{\beta}$ is

(1) $px^2 + qx + 1 = 0$ (2) $qx^2 + px + 1 = 0$

(3) $x^2 + qx + p = 0$

(4) $qx^2 + x + p = 0$

3. the values of p and q when roots are -1,2

(1) $p = -1, q = -2$ (2) $p = -1, q = 2$

(3) $p=1, q = -2$ (4) None of these



Watch Video Solution

72. Match the following :

Column I

- (A) The total number of real solutions of the equation $(x^2 - 7x + 1)^{(x^2 - 7x + 1)}$
- (B) Total number of values of a so that $x^2 - x - a = 0$ has distinct integral roots
- (C) The least value of n such that $(n - 2)x^2 + 8x + n + 4 > 0 \forall x \in \mathbb{R}$
- (D) Total number of integral values of a such that $x^2 + ax + a + 1 = 0$ has integral roots

 [View Text Solution](#)

73. if α, β, γ are the roots of the equation $x^3 + 3x + 2 = 0$ then $\frac{\alpha^3 + \beta^3 + \gamma^3}{\alpha^2 + \beta^2 + \gamma^2}$

 [Watch Video Solution](#)

Try Yourself

1. Evaluate $2i^2 + 6i^3 + 3i^{16} - 6i^{19} + 4i^{25}$

 [Watch Video Solution](#)

2. Evaluate $\left[i^{14} - \left(\frac{1}{i} \right)^{34} \right]^2$



Watch Video Solution

3. Plot the complex number $-4 + 5i$ on the Argand plane.



Watch Video Solution

4. Plot the complex number $-3 + 7i$ on the Argand plane.



Watch Video Solution

5. Write the complex number represented by the point $(-2, 5)$



Watch Video Solution

6. Write the complex number represented by the point $(-6, -7)$



Watch Video Solution

7. Find the values of x and y , if $(3y - 2) + (5 - 4x)i = 0$, where $x, y \in \mathbb{R}$.



Watch Video Solution

8. Find the values of x and y , if $x + 4yi = ix + y + 3$ where $x, y \in \mathbb{R}$



Watch Video Solution

9. If $z_1 = 4 - i$ and $z_2 = -3 + 7i$ then find

(i) $z_1 + z_2$

(ii) $z_1 - z_2$



Watch Video Solution

10. If $z_1 = 6 + 9i$ and $z_2 = 5 + 2i$ then find $\frac{z_1}{z_2}$



Watch Video Solution

11. If $z_1 = 1 + i$, $z_2 = 2 - 3i$ and $z_3 = 5 + 2i$ then find $z_1 - z_2 + 3z_3$



Watch Video Solution

12. If $z_1 = 2 + 3i$, $z_2 = 1 - i$ and $z_3 = 3 + 4i$, then find $z_1 z_2 + z_3$



Watch Video Solution

13. If $z_1 = -1 + 3i$ and $z_2 = 2 + i$ then find $2(z_1 + z_2)$



Watch Video Solution

14. Find the multiplicative inverse of the complex number $2 + 9i$.

[Watch Video Solution](#)

15. Express $\left(4 - \frac{5}{2}i\right)^2$ in the form of $a + ib$.

[Watch Video Solution](#)

16. Express $(1 - i)^4$ in the form of $a + ib$.

[Watch Video Solution](#)

17. Express $\left(\frac{1}{3} + \frac{4}{3}i\right)^2$ in the form of $a + ib$.

[Watch Video Solution](#)

18. if $z_1 = 3i$ and $z_2 = 1 + 2i$, then find $z_1 z_2 - z_1$

[Watch Video Solution](#)

19. Express $\frac{1}{1 + \cos \theta - i \sin \theta}$ in the form of $a + ib$.



Watch Video Solution

20. Express $\left(\frac{1}{2 - 2i} + \frac{3}{1 + i}\right)\left(\frac{3 + 4i}{2 - 4i}\right)$ in the form of $a + ib$



Watch Video Solution

21. Show that the complex number $\left(\frac{4 + 3i}{3 + 4i}\right)\left(\frac{4 - 3i}{3 - 4i}\right)$ is purely real.



Watch Video Solution

22. Find real q such that $\frac{3 + 2i \sin \theta}{1 - 2i \sin \theta}$ is purely real.



Watch Video Solution

23. Plot the conjugate of the complex number $2 - 3i$ on the Argand plane.



[Watch Video Solution](#)

24. Plot the conjugate of the complex number $-7-4i$ on the Argand plane.]



[Watch Video Solution](#)

25. Mutiply ($5 + 2i$) by its conjugate.



[Watch Video Solution](#)

26. Find the conjugate of $\frac{(1 - 2i)^2}{2 + i}$



[Watch Video Solution](#)

27. if $z = 2 + i + 4i^2 - 6i^3$ then verify that

(i) $\left(\overline{z^2} = (\bar{z})^2\right)$



[Watch Video Solution](#)

28. if $z=3-2i$, then verify that

(i) $z + \bar{z} = 2\operatorname{Re}z$

(ii) $z - \bar{z} = 2i\operatorname{Im}z$



Watch Video Solution

29. if $z_1 = 3 - i$ and $z_2 = -3 + i$, then find $\operatorname{Re}\left(\frac{z_1 z_2}{\bar{z}_1}\right)$



Watch Video Solution

30. Let $z_1 = 2 - i$ and $z_2 = 2 + i$, then $\operatorname{Im}\left(\frac{1}{z_1 z_2}\right)$ is



Watch Video Solution

31. Find real values of x and y for which the complex numbers $7 + ix^2y$ and $x^2 + y + 18i$ are conjugate of each other.

[Watch Video Solution](#)

32. Find real number x and y if $(x - iy)(4 + 7i)$ is the conjugate of $29 - 2i$.

[Watch Video Solution](#)

33. Find the conjugate of $\frac{\sqrt{2} - i\sqrt{2}}{2\sqrt{5} - i\sqrt{2}}$

[Watch Video Solution](#)

34. If $\frac{(a + i)^2}{(2a - i)} = p + iq$, show that: $p^2 + q^2 = \frac{(a^2 + 1)^2}{(4a^2 + 1)}$.

[Watch Video Solution](#)

35. Represent the modulus of $3 + 4i$ in the Argand plane.

[Watch Video Solution](#)

36. Represent the modulus of $1+i$, in the Argand plane.



Watch Video Solution

37. Find the modulus of $\frac{2-3i}{4+i}$



Watch Video Solution

38. Find the modulus of $\frac{(3+2i)^2}{4-3i}$



Watch Video Solution

39. If $z_1 = 5 + 2i$ and $z_2 = 2 + i$, verify

$$(i) |z_1 z_2| = |z_1| |z_2|$$



Watch Video Solution

40. if $z_1 = 2 + 3i$ and $z_2 = 1 + i$ then find, $|z_1 + z_2|$



Watch Video Solution

41. Find the modulus and argument of $-4i$.



Watch Video Solution

42. Find the modulus and argument of -3 .



Watch Video Solution

43. Convert the complex number $\frac{1+i}{1-i}$ in the polar form



Watch Video Solution

44. Convert the complex number $\frac{4}{1-i\sqrt{3}}$ in the polar form.



[Watch Video Solution](#)

45. Find the square root of $-6+8i$.



[Watch Video Solution](#)

46. Find the square root of $5 - 12i$



[Watch Video Solution](#)

47. Solve $9x^2 - 12x + 25 = 0$



[Watch Video Solution](#)

48. Solve $16x^2 + 4 = 0$



[Watch Video Solution](#)

49. Solve $x^2 - x + (1 - i) = 0$



Watch Video Solution

50. Solve $x^3 + x^2 + x + 1$.



Watch Video Solution

51. If z_1, z_2, z_3, z_4 are complex numbers, show that they are vertices of a parallelogram in the Argand diagram if and only if $z_1 + z_3 = z_2 + z_4$



Watch Video Solution

52. If P, Q, R, S are represented by the complex number $4 + i, 1 + 6i, -4 + 3i, -1 - 2i$ respectively, then $PQRS$ is a (A) rectangle (B) square (C) rhombus (D) parallelogram



Watch Video Solution

53. The length of perpendicular from $P(2 - 3i)$ on the line $(3 + 4i)Z + (3 - 4i)\bar{Z} + 9 = 0$ is equal to



Watch Video Solution

54. If $z_1 = 7 + 6i$, $z_2 = 2 + 2i$ and $z_3 = 1 - 4i$ then find $z_1 - z_2 + z_3$



Watch Video Solution

55. The set of values of k for which the equation $z\bar{z} + (-3 + 4i)\bar{z} - (3 + 4i)z + k = 0$ represents a circle, is



Watch Video Solution

56. Locus of the point z satisfying the equation $|zi - i| + |z - i| = 2$ is

(1) A line segment (2) A circle

(3) An ellipse (4) A pair of straight line



Watch Video Solution

57. If $z=x+iy$ is a complex number satisfying $\left|z + \frac{i}{2}\right|^2 = \left|z - \frac{i}{2}\right|^2$, then the locus of z is



Watch Video Solution

58. If $|z^2 - 1| = |z|^2 + 1$, then z lies on (a) The Real axis (b) The imaginary axis (c) A circle (d) An ellipse



Watch Video Solution

59. If $w = z/[z - (1/3)i]$ and $|w| = 1$, then find the locus of z .



Watch Video Solution

60. If $z = x + iy$ and $\arg\left(\frac{z-2}{z+2}\right) = \frac{\pi}{6}$, then find the locus of z .



Watch Video Solution

Assignment (Section -A) (objective Type Questions (one option is correct))

1. The value of i^{-9999} is

A. $-i$

B. i

C. 1

D. -1

Answer: B



Watch Video Solution

2. If $z = \frac{1+i}{\sqrt{2}}$, then the value of z^{1929} is

A. $1+i$

B. -1

C. $\frac{1+i}{2}$

D. $\frac{1+i}{\sqrt{2}}$

Answer: D



Watch Video Solution

3. $(\sqrt{-3})(\sqrt{-5})$ is equal to

A. $\sqrt{15}$

B. $-\sqrt{15}$

C. $i\sqrt{15}$

D. $\sqrt{5}$

Answer: B



Watch Video Solution

4. the value of $\frac{(i^{11} + i^{12} + i^{13} + i^{14} + i^{15})}{(1 + i)}$ is

A. $\frac{-(1 + i)}{2}$

B. $\frac{(1 - i)}{2}$

C. $\frac{(1 + i)}{2}$

D. $\frac{1}{2}$

Answer: A



Watch Video Solution

5. if $z = \left(\frac{1 + i}{1 - i}\right)$ then z^2 equals

A. 1

B. -1

C. i

D. none

Answer: A



Watch Video Solution

6. If the multiplicative inverse of a complex number is $\frac{\sqrt{2} + 5i}{17}$, then the complex number is

A. $\frac{\sqrt{2} - 5i}{17}$

B. $\frac{\sqrt{2} + 5i}{29}$

C. $\frac{17}{27}(\sqrt{2} - 5i)$

D. $\frac{17}{27}(\sqrt{2} + 5i)$

Answer: C



Watch Video Solution

7. The additive inverse of $5+7i$ is

A. $5-7i$

B. $-5 + 7i$

C. $5+7i$

D. $-5 - 7i$

Answer: D



Watch Video Solution

8. The complex number $\frac{1+2i}{1-i}$ lies in the Quadrant number

A. First quadrant

B. Second quadrant

C. Thrid quadrant

D. Fourth quadrant

Answer: B



Watch Video Solution

9. If $\left(\frac{1+i}{1-i}\right)^3 - \left(\frac{1-i}{1+i}\right)^3 = a + ib$ find a and b

A. 0 and 2

B. 0 and -2

C. 2 and 0

D. 2 and 2

Answer: B



Watch Video Solution

10. If $x = -2 - \sqrt{3}i$, where $i = \sqrt{-1}$, find the value of $2x^4 + 5x^3 + 7x^2 - x + 41$

A. 1

B. 3

C. 6

D. 8

Answer: C



Watch Video Solution

11. $\left[i^{17} + \frac{1}{i^{315}} \right]^9$ is equal to

A. $32i$

B. -512

C. 512

D. $512i$

Answer: D



Watch Video Solution

12. If $z = 3 - 2i$ then the value s of $(\text{Re}z)(\text{Im}z)^2$ is

A. 6

B. 12

C. -6

D. -12

Answer: B



Watch Video Solution

13. If $z_1 = 4 - 3i$ and $z_2 = 3 + 9i$ then $z_1 - z_2$ is

A. $1 + 12i$

B. $-1 + 12i$

C. $1 - 12i$

D. $-1 - 12i$

Answer: C



Watch Video Solution

14. If $z_1 = 2 + 3i$ and $z_2 = 5 - 3i$ then $z_1 z_2$ is

A. $-9 - 19i$

B. $-9 + 19i$

C. $19 - 19$

D. $19 + i9$

Answer: D



Watch Video Solution

15. $\frac{1 + 2i}{1 + 3i}$ is equal to

A. $\frac{7}{10} - \frac{i}{10}$

B. $\frac{7}{10} + \frac{i}{10}$

C. $7 - i$

D. $\frac{7}{2} + \frac{i}{2}$

Answer: A



Watch Video Solution

16. $\frac{(1+i)^3}{2+i}$ is equal to

A. $\frac{2}{5} - \frac{6}{5}i$

B. 0

C. $-\frac{1}{5} + \frac{5}{6}i$

D. $-\frac{2}{5} + \frac{6}{5}i$

Answer: D



Watch Video Solution

17. $\left(\frac{2}{1-i} + \frac{3}{1+i}\right)\left(\frac{2+3i}{4+5i}\right)$ is equal to

A. $-\frac{117}{82} - \frac{13}{82}i$

B. $-\frac{117}{82} + \frac{13}{82}i$

C. $\frac{117}{82} - \frac{13i}{82}$

D. $\frac{117}{82} + \frac{13i}{82}$

Answer: C



Watch Video Solution

18. In the Argand plane, the conjugate of the complex number $3-7i$ will lie in

A. First quadrant

B. Second quadrant

C. Third quadrant

D. Fourth quadrant

Answer: A



Watch Video Solution

19. if $z = 4 - 9i$ then $z\bar{z}$ is

A. -92

B. -97

C. 92

D. 97

Answer: D



Watch Video Solution

20. The conjugate of $\frac{(1 + 2i)^2}{3 - i}$ is

A. $\frac{-13}{10} + \frac{9}{10}i$

B. $\frac{-13}{10} - \frac{9}{10}i$

C. $\frac{13}{10} + \frac{9}{10}i$

D. $\frac{13}{10} - \frac{9}{10}i$

Answer: B



Watch Video Solution

21. $\frac{3 - \sqrt{-16}}{1 - \sqrt{-25}}$ is equal to

A. $\frac{-1}{24}$

B. 0

C. $\frac{23}{26} + \frac{11}{26}i$

D. $23+5i$

Answer: C



Watch Video Solution

22. If $z_1 = 1 + i$ and $z_2 = -3 + 2i$ then $lm\left(\frac{z_1 z_2}{\bar{z}_1}\right)$ is

A. 2

B. -3

C. 3

D. -2

Answer: B



Watch Video Solution

23. The multiplicative inverse of $(3 + \sqrt{5}i)^2$ is

A. $\frac{1}{49} - \frac{3\sqrt{5}}{98}i$

B. $\frac{1}{49} + \frac{3\sqrt{5}}{98}i$

C. $4 + 6\sqrt{5}i$

D. $4 - 6\sqrt{5}i$

Answer: A



Watch Video Solution

24. if $z = 3 + i + 9i^2 - 6i^3$ then $(\overline{z^{-1}})$ is

A. $2+i$

B. $-\frac{3}{79} + \frac{4}{79}i$

C. $1 - i$

D. $-\frac{6}{85} + \frac{7}{85}i$

Answer: D



Watch Video Solution

25. The conjugate of the complex number represented by the point (6-5) is

- A. $6 - 5i$
- B. $6 + 5i$
- C. $-6 + 5i$
- D. $-6 - 5i$

Answer: B



Watch Video Solution

26. if $z_1 = 3 + i$ and $z_2 = 2 - i$, then $\left| \frac{z_1 + z_2 - 1}{z_1 - z_2 + i} \right|$ is

- A. $\frac{\sqrt{8}}{5}$
- B. $\sqrt{\frac{8}{5}}$
- C. $\frac{8}{5}$
- D. $\frac{8}{\sqrt{5}}$

Answer: A



Watch Video Solution

27. The modulus of $\frac{(2 + 3i)^2}{2 + i}$ is

A. $\frac{\sqrt{13}}{5}$

B. $\frac{\sqrt{147}}{5}$

C. $\frac{13}{\sqrt{5}}$

D. $\frac{\sqrt{185}}{5}$

Answer: C



Watch Video Solution

28. The value of $(1 + i)(1 - i^2)(1 + i^4)(1 - i^5)$ is

A. $2i$

B. 8

C. -8

D. $8i$

Answer: B



Watch Video Solution

29. If $z = \frac{1}{(1+i)(1-2i)}$, then $|z|$ is

A. $\frac{2}{10}$

B. $\frac{\sqrt{7}}{10}$

C. $\frac{9}{\sqrt{10}}$

D. $\frac{1}{\sqrt{10}}$

Answer: D



Watch Video Solution

30. The value of $\left| \frac{1}{2+i} - \frac{1}{2-i} \right|$ is

A. $-\frac{2}{5}$

B. $\frac{4}{25}$

C. $\frac{2}{5}$

D. 0

Answer: C



Watch Video Solution

31. Find the value of

$\tan 22.5^\circ$



Watch Video Solution

32. $(4 + 3i) + (7 - 4i) - (3 + 5i) + i^{25}$ is equal to

A. $2+7i$

B. $4+7i$

C. $8 - 5i$

D. $-8 + 2i$

Answer: C



Watch Video Solution

33. The conjugate of $\sqrt{-5} + 3^2$ is

A. $9 - \sqrt{5}i$

B. $9 + \sqrt{5}i$

C. $-9 + \sqrt{5}i$

D. $-9 - \sqrt{5}i$

Answer: A



Watch Video Solution

34. The modulus of $i^{25} + (i + 2)^3$ is

A. $\sqrt{47}$

B. $4\sqrt{15}$

C. $\sqrt{35}$

D. $2\sqrt{37}$

Answer: D



Watch Video Solution

35. If $z = a+ib$ is a complex numbers, then

A. $Re(z) = \frac{z + \bar{z}}{2}$

B. $Re(z) = \frac{z\bar{z}}{2}$

C. $Re(z) = \frac{z - \bar{z}}{2}$

D. $Re(z) = \frac{z + \bar{z}}{2}$

Answer: D



Watch Video Solution

36. The modulus of the complex number $z = a + ib$ is

A. $z \cdot \bar{z}$

B. $a + b$

C. $a^2 + b^2$

D. $\sqrt{z \cdot \bar{z}}$

Answer: D



Watch Video Solution

37. The argument of the complex number $(1 + i)^4$ is

A. 135°

B. 180°

C. 90°

D. 45°

Answer: C



Watch Video Solution

38. The amplitude of $\frac{1}{i}$ is equal to 0 b. $\frac{\pi}{2}$ c. $-\frac{\pi}{2}$ d. π

A. 0

B. $\frac{\pi}{2}$

C. $-\frac{\pi}{2}$

D. π

Answer: D



Watch Video Solution

39. Find the value of $\cos 75^\circ$



Watch Video Solution

40. If $z = \frac{-4 + 2\sqrt{3}i}{5 + \sqrt{3}i}$, then the value of $\arg(z)$ is

A. π

B. $\frac{\pi}{3}$

C. $\frac{2\pi}{3}$

D. $\frac{\pi}{4}$

Answer: C



Watch Video Solution

41. if $z = \cos \frac{\pi}{4} + i \sin \frac{\pi}{6}$ then

A. $|z| = 1, \arg(z) = \frac{\pi}{4}$

B. $|z| = 1, \arg(z) = \frac{\pi}{6}$

C. $|z| = \frac{\sqrt{3}}{2}, \arg(z) = \frac{5\pi}{24}$

D. $|z| = \frac{\sqrt{3}}{2}, \arg(z) = \frac{\tan^{-1} 1}{\sqrt{2}}$

Answer: D



Watch Video Solution

42. The square root of $-8i$ is

A. $\pm 2(1 - i)$

B. $2(1 + i)$

C. $\pm (1 - i)$

D. $\pm (1 + i)$

Answer: A



Watch Video Solution

43. Find the square root of the following complex numbers

$$3 + 4i$$

A. $\pm(2 - i)$

B. $\pm(2 + i)$

C. $\pm(3 + i)$

D. $\pm(3 - i)$

Answer: B



Watch Video Solution

44. If α and β are the roots of $4x^2 = 3x + 7 = 0$ then the value of

$$\frac{1}{\alpha} = \frac{1}{\beta} \text{ is } \frac{4}{7} \text{ b. } -\frac{3}{7} \text{ c. } \frac{3}{7} \text{ d. } -\frac{3}{4}$$

A. $\frac{4}{7}$

B. $-\frac{3}{7}$

C. $\frac{3}{7}$

D. $-\frac{3}{4}$

Answer: B



Watch Video Solution

45. If a, b are the roots of the equation ' $x^2+x+1=0$ ', then ' a^2+b^2 '=

a)1 b)2 c) -1 d)3

A. 1

B. 2

C. -1

D. 3

Answer : C



Watch Video Solution

46. if the difference of the roots of the equation $x^2 - px + q = 0$ is unity.

A. $p^2 + 4q = 1$

B. $p^2 - 4q = 1$

C. $p^2 - 4q^2 = (1 + 2q)^2$

D. $4p^2 + q^2 = (1 + 2p)^2$

Answer: B



Watch Video Solution

47. If α and β are the roots of the equation $x^2 - px + 16 = 0$, such that $\alpha^2 + \beta^2 = 9$, then the value of p is

A. $\pm\sqrt{6}$

B. $\pm\sqrt{41}$

C. ± 8

D. ± 7

Answer: B

[Watch Video Solution](#)

Assignment (Section -B) (objective Type Questions (one option is correct)

1. The solution of the equation $z(\overline{z - 3i}) = 2(2 + 3i)$ is/are

A. $2 + i, 3 - 2i$

B. $2 + 2i, 3i$

C. $3 + 2i, 2i$

D. $2, 2 + 3i$

Answer: D

[Watch Video Solution](#)

2. If $f(x) = x^4 - 8x^3 + 4x^2 + 4x + 39$ and $f(3 + 2i) = a + ib$ then $a : b$ is equal to

A. $\frac{1}{8}$

B. $-\frac{1}{4}$

C. $\frac{1}{4}$

D. $-\frac{1}{8}$

Answer: D



Watch Video Solution

3. If center of a regular hexagon is at the origin and one of the vertices on the Argand diagram is $1 + 2i$, then its perimeter is $2\sqrt{5}$ b. $6\sqrt{2}$ c. $4\sqrt{5}$ d. $6\sqrt{5}$

A. $6\sqrt{5}$

B. $4\sqrt{5}$

C. $6\sqrt{2}$

D. $2\sqrt{5}$

Answer: A



Watch Video Solution

4. The sum of principal arguments of complex numbers

$1 + i, -1 + i\sqrt{3}, -\sqrt{3} - i, \sqrt{3} - i, i, -3i, 2, -1$ is

A. $\frac{11\pi}{12}$

B. $\frac{13\pi}{12}$

C. $\frac{12\pi}{13}$

D. $\frac{\pi}{15}$

Answer: A



Watch Video Solution

5. If $z = \frac{\cos \pi}{4} + i \frac{\sin \pi}{6}$, then $|z| = 1, \arg(z) = \frac{\pi}{4}$ b.
 $|z| = 1, \arg(z) = \frac{\pi}{6}$ c. $|z| = \frac{\sqrt{3}}{2}, \arg(z) = \frac{25\pi}{24}$ d.

$$|z| = \frac{\sqrt{3}}{2}, \arg(z) = \frac{\tan^{-1} 1}{\sqrt{2}}$$

A. $|z| = 1, \arg(z) = \frac{\pi}{4}$

B. $|z| = 1, \arg|z| = \frac{\pi}{6}$

C. $|z| = \frac{\sqrt{3}}{2}, \arg z = \frac{5\pi}{24}$

D. $|z| = \frac{\sqrt{3}}{2}, \arg z = \tan^{-1} \left(\frac{1}{\sqrt{2}} \right)$

Answer: D



Watch Video Solution

6. Represent the complex numbers

$$\frac{1 + 7i}{(2 - i)^2} \text{ in polar form}$$

A. $\sqrt{2} \left(\cos(3\pi)/4 - i \sin \frac{3\pi}{4} \right)$

B. $\sqrt{2} \left(\cos(3\pi)/4 + i \sin \frac{3\pi}{4} \right)$

C. $\sqrt{2} \left(\cos(7\pi)/4 + i \sin \frac{7\pi}{4} \right)$

D. $\sqrt{2} \left(\cos(7\pi)/4 - i \sin \frac{7\pi}{4} \right)$

Answer: B



Watch Video Solution

7. In any $\triangle ABC$, if

$$\cos \theta = \frac{a}{b+c}, \cos \phi = \frac{b}{a+c}, \cos \psi = \frac{c}{a+b} \quad \text{where } \theta, \phi \text{ and } \psi \text{ lie}$$

between 0 and π , prove that

$$\tan^2 \frac{\theta}{2} + \tan^2 \frac{\phi}{2} + \tan^2 \frac{\psi}{2} = 1$$

A. 3

B. $-\frac{3}{2}$

C. 0

D. $\frac{3}{2}$

Answer: C



Watch Video Solution

8. The value of $(i + \sqrt{3})^{100} + (i - \sqrt{3})^{100} + 2^{100}$ is

- A. 1
- B. -1
- C. 0
- D. 2

Answer: C



Watch Video Solution

9. Which of the following is not true ?

A. The number whose conjugate is $\frac{1}{1-i}is\frac{1}{1+i}$

B. if $\sin x + i \cos 2x$ and $\cos x - i \sin 2x$ are conjugate to each other
then number of values of x is zero

C. if $x+1+iy$ and $2+3i$ are conjugate of each other then the value of $x+y$ is -2.

D. $2 + I > 3 + i$

Answer: D



Watch Video Solution

10. The complex numbers z_1, z_2 and z_3 satisfying $\frac{z_1 - z_3}{z_2 - z_3} = \frac{1 - i\sqrt{3}}{2}$ are the vertices of triangle which is (1) of area zero (2) right angled isosceles (3) equilateral (4) obtuse angled isosceles

A. Of area zero

B. Right angled isosceles

C. Equilateral

D. Obtuse angle isosceles

Answer: C

[Watch Video Solution](#)

11. Let $a = i^i$ and consider the following statements $S_1 : a = e^{-\frac{\pi}{2}}$, S_2 : The value of $\sin(\operatorname{Im} a) - 1$, $\operatorname{Im}(a) + \arg(a) = 0$ Now identify the correct combination of the true statements.

A. S_1, S_2 only

B. S_1, S_3 only

C. S_1, S_2, S_3

D. S_1 only

Answer: C

[Watch Video Solution](#)

12. If $z^2 + z + 1 = 0$ then the value of

$\left(z + \frac{1}{z}\right)^2 + \left(z^2 + \frac{1}{z^2}\right)^2 + \left(z^3 + \frac{1}{z^3}\right)^2 + \dots + \left(z^{21} + \frac{1}{z^{21}}\right)^2$ is equal to

A. 21

B. 42

C. 0

D. 11

Answer: B



Watch Video Solution

13. If ω is an imaginary fifth root of unity, then find the value of

$$\log_2 |1 + \omega + \omega^2 + \omega^3 - 1/\omega|.$$

A. 2

B. 0

C. 2

D. -1

Answer: A

14. If $1, \alpha_1, \alpha_2, \alpha_3, \dots, \alpha_{3n}$ be the roots of the equation $x^{3n+1} - 1 = 0$, and w be an imaginary cube root of unity, then

$$\frac{(w^2 - \alpha_1)(w^2 - \alpha_2) \dots (w^{3n} - \alpha_{3n})}{(w - \alpha_1)(w^2 - \alpha) \dots (w - \alpha_{3n})}$$

A. ω

B. $-\omega$

C. 1

D. ω^2

Answer: C

15. If z_1, z_2, z_3, z_4 are two pairs of conjugate complex numbers, then $\arg\left(\frac{z_1}{z_3}\right) + \arg\left(\frac{z_2}{z_4}\right)$ is

A. 0

B. $\frac{\pi}{2}$

C. $\frac{3\pi}{4}$

D. π

Answer: A



Watch Video Solution

16. If $|z - 4 + 3i| \leq 2$ then the least and the greatest values of $|z|$ are q

A. 3,7

B. 4,7

C. 3,9

D. 4,5

Answer: A



Watch Video Solution

17. If $|z_1| = 2$, $|z_2| = 3$, $|z_3| = 4$ and $|2z_1 + 3z_2 + 4z_3| = 4$ then the expression $|8z_2z_3 + 27z_3z_1 + 64z_1z_2|$ equals (A) 72 (B) 24 (C) 96 (D) 92

A. 72

B. 24

C. 96

D. 92

Answer: C



Watch Video Solution

18. If $z_1 = \cos \theta + i \sin \theta$ and $1, z_1, (z_1)^2, (z_1)^3, \dots, (z_1)^{n-1}$ are vertices of a regular polygon such that $\frac{\operatorname{Im}(z_1)^2}{\operatorname{Re} z_1} = \frac{\sqrt{5} - 1}{2}$, then the value n is

A. (a)20

B. (b)10

C. (c)18

D. (d)15

Answer: A



Watch Video Solution

19. The area of the triangle whose vertices are represented by the complex numbers O, z and \bar{z} where z is $(\cos \alpha + i \sin \alpha)$ is equal to -

A. $\frac{1}{2}|z|^2 \cos \theta$

B. $\frac{1}{2}|z|^2 \sin \alpha$

C. $\frac{1}{2}|z|^2 \sin \alpha \cos \alpha$

D. $\frac{1}{2}|z|^2$

Answer: B

[Watch Video Solution](#)

20. The maximum value of $|z|$ where z satisfies the condition

$$\left| z + \left(\frac{2}{z} \right) \right| = 2 \text{ is}$$

A. $\sqrt{3} - 1$

B. $\sqrt{3} + 1$

C. $\sqrt{3}$

D. $\sqrt{2} + \sqrt{3}$

Answer: B

[Watch Video Solution](#)

21. The value of $\frac{1 - \tan^2 15^\circ}{1 + \tan^2 15^\circ}$ is

[Watch Video Solution](#)

22. Both the roots of the equation $(x - b)(x - c) + (x - a)(x - c) + (x - a)(x - b) = 0$ are always a. positive b. real c. negative d. none of these

A. $a + b\omega + c\omega^2 = 0$

B. $a + b\omega^2 + c\omega = 0$

C. $a^2 + b^2 + c^2 - ab - bc - ca = 0$

D. $a+b+c=0$

Answer: D



Watch Video Solution

23. If $\log \sqrt{3} \left(\frac{|z|^2 - |z| + 1}{2 + |z|} \right) > 2$, then the locus of z is

A. $|z|=5$

B. $|z| \leq 5$

C. $|z| > 5$

D. $|z| = 0$

Answer: B



Watch Video Solution

24. If $\arg z = \frac{\pi}{4}$, then

A. $\operatorname{Re}(z^2) = 9\operatorname{Im}(z^2)$

B. $\operatorname{Im}(z^2) = 0$

C. $\operatorname{Re}(z^2) = 0$

D. $\operatorname{Re}(z) = 0$

Answer: C



Watch Video Solution

25. If $z^2 + z|z| + |z^2| = 0$, then the locus z is a. a circle b. a straight line
c. a pair of straight line d. none of these

A. Circle

B. Straight line

C. A pair of straight lines

D. None of these

Answer: C



Watch Video Solution

26. The least value of p for which the two curves $argz = \frac{\pi}{6}$ and $|z - 2\sqrt{3}i| = p$ intersect is

A. $p = \sqrt{3}$

B. $p=3$

C. $p = \frac{1}{\sqrt{3}}$

D. $P = \frac{1}{3}$

Answer: B



Watch Video Solution

27. $Re\left(\frac{z+4}{2z-1}\right) = \frac{1}{2}$, then z is represented by a point lying on

- A. A circle
- B. An ellipse
- C. A straight line
- D. No real locus

Answer: C



Watch Video Solution

28. If $f(x)$ and $g(x)$ are two polynomials such that the polynomial $h(x) = xf(x^3) + x^2g(x^6)$ is divisible by $x^2 + x + 1$, then $f(1) = g(1)$

(b) $f(1) = 1g(1)$ $h(1) = 0$ (d) all of these

A. $f(1)+g(1)=1$

B. $f(1)=-g(1)$

C. $f(1)=g(1) \neq 0$

D. $f(1) = \pm g(1)$

Answer: B



Watch Video Solution

29. If $\omega (\neq 1)$ is a cube root of unity, then $(1 - \omega + \omega^2)(1 - \omega^2 + \omega^4)(1 - \omega^4 + \omega^8) \dots$ upto $2n$ is factors, is

A. $(x - 1)^{2n}$

B. $(x - 1)^{2n+1}$

C. $(x - 1)^{2n-1}$

D. $(X - 1)^{2n+2}$

Answer: A



Watch Video Solution

30. If $z = \frac{\sqrt{3} - i}{2}$, where $i = \sqrt{-1}$, then $(i^{101} + z^{101})^{103}$ equals to

A. iz

B. z

C. \bar{z}

D. ωz , (ω is complex cube root of unity)

Answer: B



Watch Video Solution

31. The region of the complex plane for which

$$\left| \frac{z - a}{z + \overline{a}} \right| = 1, (Re(a) \neq 0) \text{ is}$$

- A. x-axis
- B. y-axis
- C. Straight line $x=a$
- D. The straight line $y=a$

Answer: B



Watch Video Solution

32. If the imaginary part of $\frac{2z + 1}{iz + 1}$ is -2 , then show that the locus of the point representing z in the argand plane is a straight line.

- A. A circle
- B. A straight line

C. A parabola

D. An ellipse

Answer: B



Watch Video Solution

33. In z is a complex number satisfying $|2008z-1|=2008|z-2|$, then locus z is

A. y-axis

B. x-axis

C. Circle

D. A line parallel to y-axis

Answer: D



Watch Video Solution

34. The locus of the points z satisfying the condition $\arg \left(\frac{z-1}{z+1} \right) = \frac{\pi}{3}$ is, a

A. A straight line

B. Circle

C. A parabola

D. Ellipse

Answer: B



Watch Video Solution

35. the locus of $z = i + 2 \exp \left(i \left(\theta + \frac{\pi}{4} \right) \right)$ is

A. A circle

B. An ellipse

C. A parabola

D. A hyperbola

Answer: A



Watch Video Solution

36. If one vertex and centre of a square are z and origin then which of the following cannot be the vertex of the square ?

A. iz

B. $-z$

C. $-iz$

D. $2z$

Answer: D



Watch Video Solution

37. if the complex no z_1, z_2 and z_3 represents the vertices of an equilateral triangle such that $|z_1| = |z_2| = |z_3|$ then relation among z_1, z_2 and z_3

A. $z_1 + z_2 = z_3$

B. $z_1 + z_2 + z_3 = 0$

C. $z_1 z_2 = \frac{1}{z_3}$

D. $z_1 - z_2 = z_3 - z_2$

Answer: B



Watch Video Solution

38. If $|z - 2 - 3i| + |z + 2 - 6i| = 4$ where $i = \sqrt{-1}$, then locus of P (z) is

A. An ellipse

B. A point

C. Segment joining the points $(2 + 3i)$ and $(-2 + 6i)$

D. Empty

Answer: D



Watch Video Solution

39. If z_1, z_2, z_3 and u, v, w are complex numbers representing the vertices of two triangles such that $z_3 = (1 - t)z_1 + tz_2$ and $w = (1 - u)u + tv$, where t is a complex number, then the two triangles

A. Have the same area

B. Are similar

C. Are congruent

D. Are equilateral

Answer: B



Watch Video Solution

40. If $|z - 25i| \leq 15$. then $|\text{maximum } \arg(z) - \text{minimum } \arg(z)|$ equals

A. $\sin^{-1}\left(\frac{3}{5}\right) - \cos^{-1}\left(\frac{3}{5}\right)$

B. $\frac{\pi}{2} + \cos^{-1}\left(\frac{3}{5}\right)$

C. $2\cos^{-1}(4/5)$

D. $\cos^{-1}\left(\frac{3}{5}\right)$

Answer: C



Watch Video Solution

41. For two complex numbers z_1 and z_2 , we have $\left| \frac{z_1 - z_2}{1 - \bar{z}_1 z_2} \right| = 1$, then

A. both z_1 and z_2 lie on circle $|z|=1$

B. $\arg\left(\frac{z_1}{z_2}\right) = \frac{\pi}{3}$

C. At least one of z_1 and z_2 lies on the circle $|z|=1$

D. $|z_1| = 2|z_2|$

Answer: A



Watch Video Solution

42. Let α , and β are the roots of the equation $x^2 + x + 1 = 0$ then

A. $\alpha^2 + \beta^2 = 4$

B. $(\alpha - \beta)^2 = 3$

C. $\alpha^3 + \beta^3 = 2$

D. $\alpha^4 + \beta^4 = 1$

Answer: C



Watch Video Solution

43. If the ratio of the roots of the equation $lx^2 + nx + n = 0$ is $p:q$

prove that $\sqrt{\frac{p}{q}} + \sqrt{\frac{q}{p}} + \sqrt{\frac{n}{l}} = 0$

A. $\sqrt{\frac{p}{q}} + \sqrt{\frac{q}{p}} + \sqrt{\frac{n}{1}} = 1$

B. $\sqrt{\frac{p}{q}} + \sqrt{\frac{q}{p}} + \sqrt{\frac{n}{l}} = 0$

C. $\sqrt{\frac{q}{p}} + \sqrt{\frac{p}{q}} + \sqrt{\frac{l}{n}} = 1$

D. $\sqrt{\frac{q}{p}} + \sqrt{\frac{p}{q}} + \sqrt{\frac{l}{n}} = 0$

Answer: B



Watch Video Solution

44. For the equation $|x^2| + |x| - 6 = 0$, the roots are

A. Real and equal

B. Real with sum 0

C. Real with sum 1

D. Real with product 0

Answer: B



Watch Video Solution

45. If $a + b + c = 0$ and a, b, c are rational. Prove that the roots of the equation

$$(b + c - a)x^2 + (c + a - b)x + (a + b - c) = 0 \text{ are rational.}$$

A. Rational

B. Irrational

C. Imaginary

D. Equal

Answer: A



Watch Video Solution

46. If $\sec \alpha$, $\tan \alpha$ are roots of $ax^2 + bx + c = 0$, then

A. $a^4 - b^4 + 4ab^2c = 0$

B. $a^4 + b^4 - 4ab^2c = 0$

C. $a^2 - b^2 = 4ac$

D. $a^2 + b^2 = ac$

Answer: A



Watch Video Solution

47. If x is real then the values of $\frac{x^2 + 34x - 71}{x^2 + 2x - 7}$ does not lie in the interval

A. Lies between 4 and 7

B. Lies between 5 and 9

C. Has no value between 4 and 7

D. Has no value between 5 and 9

Answer: D



Watch Video Solution

48. if α & β are the roots of the quadratic equation $ax^2 + bx + c = 0$, then the quadratic equation $ax^2 - bx(x - 1) + c(x - 1)^2 = 0$ has roots

A. $\frac{\alpha}{1 - \alpha}, \frac{\beta}{1 - \beta}$

B. $\frac{1 - \alpha}{\alpha}, \frac{1 - \beta}{\beta}$

C. $\frac{\alpha}{1 + \alpha}, \beta/(1 + \beta)$

D. $\frac{1 + \alpha}{\alpha}, \frac{1 + \beta}{\beta}$

Answer: C



Watch Video Solution

49. let α, β be roots of $ax^2 + bx + c = 0$ and γ, δ be the roots of $px^2 + qx + r = 0$ and D_1 and D_2 be the respective equations .if $\alpha, \beta, \gamma, \delta$ in A. P. then $\frac{D_1}{D_2}$ is

A. $\frac{a^2}{b^2}$

B. $\frac{a^2}{p^2}$

C. $\frac{b^2}{q^2}$

D. $\frac{c^2}{r^2}$

Answer: B



Watch Video Solution

50. The equation

$$\frac{a(x-b)(x-c)}{(a-b)(a-c)} + \frac{b(x-c)(x-a)}{(b-c)(b-a)} + \frac{c(x-a)(x-b)}{(c-a)(c-b)} = x$$

is

satisfied by

A. No value of x .

- B. Exactly two values of x .
- C. Exactly three values of x .
- D. All values of x

Answer: D



Watch Video Solution

51. If $z_1 = 3 - 2i$, $z_2 = 2 - i$ and $z_3 = 2 + 5i$ then find $z_1 + z_2 - 3z_3$



Watch Video Solution

52. If the equation $(k^2 - 3k + 2)x^2 + (k^2 - 5k + 4)x + (k^2 - 6k + 5) = 0$ is an identity then the value of k is

- A. 1
- B. 2

C. 3

D. 4

Answer: A



Watch Video Solution

53. The value of k if

A. The roots of $5x^2 + 13x + k = 0$ are let say a and b and they are reciprocal to each other is 5.

B. The roots of $x^2 + x + k = 0$ are consecutive integer is 1.

C. The roots of $x^2 - 6x + k = 0$ are in the ratio 2 : 1 is 7.

D. The roots of the equation $x^2 + kx - 1 = 0$ are real, equal in magnitude but opposite in sign is 1.

Answer: A



Watch Video Solution

54. if the difference of the roots of the equation $x^2 + ax + b = 0$ is equal to the difference of the roots of the equation $x^2 + bx + a = 0$, then

A. $a + b = 4$

B. $a = b = -4$

C. $a - b = 4$

D. $a - b = -4$

Answer: B



Watch Video Solution

55. If the equations $px^2 + 2qx + r = 0$ and $px^2 + 2rx + q = 0$ have a common root then $p + q + 4r =$

A. 0

B. 1

C. 2

D. -2

Answer: A



Watch Video Solution

56. If the equations $ax^2 + bx + c = 0$ and $x^2 + x + 1 = 0$ has one common root then $a : b : c$ is equal to

A. 1 : 1 : 1

B. 1 : 2 : 3

C. 2 : 3 : 1

D. 3 : 2 : 1

Answer: A



Watch Video Solution

57. If 1,2,3 are the roots of the equation $x^3 + ax^2 + bx + c = 0$, then

A. $a=1, b=2, c=3$

B. $a=-6, b=11, c=-6$

C. $a=6, b=11, c=6$

D. $a=6, b=6, c=6$

Answer: B



Watch Video Solution

58. Consider that $f(x) = ax^2 + bx + c$, $D = b^2 - 4ac$, then which of the following is not true ?

A. If $a > 0$ then minimum value of $f(x)$ is $\frac{-D}{4a}$

B. If $a < 0$, then maximum value of $f(x)$ is $\frac{-D}{4a}$

C. if $a > 0, D < 0$, then $f(x) > 0$ for all $x \in \mathbb{R}$

D. If $a > 0$, $D > 0$, then $f(x) > 0$ for all $x \in R$

Answer: D



Watch Video Solution

59. If the minimum value of $x^2 + 2x + 3$ is m and maximum value of $-x^2 + 4x + 6$ is M then $m + M =$

A. 10

B. 11

C. 12

D. 13

Answer: C



Watch Video Solution

60. for all $x \in R$ if $mx^2 - 9mx + 5m + 1 > 0$ then m lies in the interval

A. $\left(-\frac{61}{4}, 0\right)$

B. $\left(\frac{4}{61}, \frac{61}{4}\right)$

C. $\left(0, \frac{4}{61}\right)$

D. $\left(\frac{-4}{61}, 0\right)$

Answer: C



Watch Video Solution

61. If one root of equation $(l - m)x^2 + lx + 1 = 0$ be double of the other

and if l be real, show that $m \leq \frac{9}{8}$

A. $\frac{9}{8}$

B. $\frac{7}{8}$

C. $\frac{8}{9}$

D. $\frac{5}{9}$

Answer: A



Watch Video Solution

62. if p, q, r are real numbers satisfying the condition $p + q + r = 0$, then the roots of the quadratic equation $3px^2 + 5qx + 7r = 0$ are

- A. positive
- B. negative
- C. Real and distinct
- D. Imaginary

Answer: C



Watch Video Solution

63. The roots of the equation $x^3 - 2x^2 - x + 2 = 0$ are

A. 1,2,3

B. $-1, 1, 2$

C. $-1, 0, 1$

D. $-1, -2, 3$

Answer: B



Watch Video Solution

64. IF α, β are the roots of the equation $x^2 + 2ax + b = 0$, then the quadratic equation with rational coefficient one of whose roots is $\alpha + \beta + \sqrt{\alpha^2 + \beta^2}$ is

A. $x^2 + 4ax - 2b = 0$

B. $x^2 + 4ax + 2b = 0$

C. $x^2 - 4ax + 2b = 0$

D. $x^2 - 4ax - 2b = 0$

Answer: B



Watch Video Solution

65. The set of all values of ' a ' for which the quadratic equation $3x^2 + 2(a^2 - 3a + 2) = 0$ possess roots of opposite sign, is
a. $(-\infty, 1)$ b. $(-\infty, 0)$ c. $(1, 2)$ d. $(3/2, 2)$

A. $1 < a < 2$

B. $a \in (2, \infty)$

C. $1 < a < 3$

D. $-1 < a < 0$

Answer: A



Watch Video Solution

66. Let $a, b, c \in R$ and $a \neq 0$ be such that $(a + c)^2 < b^2$, then the quadratic equation $ax^2 + bx + c = 0$ has

- A. Imaginary roots
- B. Real roots
- C. Exactly one real root lying in the interval $(-1, 1)$
- D. Exactly two roots in $(-1, 1)$

Answer: C



Watch Video Solution

67. If $p + iq$ be one of the roots of the equation $x^3 + ax + b = 0$, then $2p$ is one of the roots of the equation

- A. $x^3 + ax + b = 0$
- B. $x^3 - ax - b = 0$
- C. $x^3 + ax - b = 0$

D. $x^3 + bx + a = 0$

Answer: C



Watch Video Solution

68. If

$a_1, a_2, a_3, a_4, \dots, a_{n-1}, a_n$ are distinct non-zero real numbers such that
 $(a_2^2 + a_3^2 + a_4^2 + \dots + a_n^2) \leq 0$ then $a_1, a_2, a_3, \dots, a_{n-1}, a_n$
are in

A. A.P.

B. G.P.

C. H.P.

D. A.G.P.

Answer: B



Watch Video Solution

69. If coefficients of the equation $ax^2 + bx + c = 0$, $a \neq 0$ are real and roots of the equation are non-real complex and $a + c < b$, then

A. $4a + c > 2b$

B. $4a + c < 2b$

C. $4a + c = 2b$

D. None of these

Answer: B



Watch Video Solution

70. If the sum of the roots of the quadratic equation $ax^2 + bx + c = 0$ is equal to the sum of the squares of their reciprocals then prove that

$\frac{a}{c}, \frac{b}{a}$ and $\frac{c}{b}$ are in HP

A. A.P.

B. G.P.

C. H.P.

D. None of these

Answer: C



Watch Video Solution

71. The number of irrational roots of the equation

$$(x - 1)(x - 2)(3x - 2)(3x + 1) = 21 \text{ is}$$

A. 0

B. 2

C. 3

D. 4

Answer: B



Watch Video Solution

72. If $\alpha \in \left(0, \frac{\pi}{2}\right)$, then $\sqrt{x^2 + x} + \frac{\tan^2 \alpha}{\sqrt{x^2 + x}}$ is always greater than or equal to $2 \tan \alpha$ 1 $2 \sec^2 \alpha$

A. S_1 only

B. S_2 only

C. S_3 only

D. S_1, S_2, S_3, S_4

Answer: D



Watch Video Solution

73. If a, b are real, then the roots of the quadratic equation $(a - b)x^2 - 5(a + b)x - 2(a - b) = 0$ are

A. Real and equal

B. Non-real complex

C. Real and unequal

D. None of these

Answer: C



Watch Video Solution

74. If α, β are the roots of the equation $ax^2 - bx + c = 0$ then equation $(a + cy)^2 = b^2y$ has the roots

A. $\frac{1}{\alpha}, \frac{1}{\beta}$

B. α^2, β^2

C. $\frac{\alpha}{\beta}, \frac{\beta}{\alpha}$

D. $\frac{1}{\alpha^2}, \frac{1}{\beta^2}$

Answer: D



Watch Video Solution

75. If a, b, c are in GP, show that the equations $ax^2 + 2bx + c = 0$ and $dx^2 + 2ex + f = 0$ have a common root if $\frac{a}{d}, \frac{b}{e}, \frac{c}{f}$ are in HP

A. A.P.

B. G.P.

C. H.P.

D. $ab = cd$

Answer: A



Watch Video Solution

76. Find the least integral value of k for which the equation $x^2 - 2(k + 2)x + 12 + k^2 = 0$ has two different real roots.

A. 0

B. 2

C. 3

D. 4

Answer: C



Watch Video Solution

77. The roots x_1 and x_2 of the equation $x^2 + px + 12 = 0$ are such that their differences is 1. then the positive value of p is

A. 1

B. 2

C. 3

D. 7

Answer: D



Watch Video Solution

78. If $a < b < c < d$, then for any real non-zero λ , the quadratic equation $(x - a)(x - c) + \lambda(x - b)(x - d) = 0$, has real roots for

- A. All roots real and distinct
- B. All roots but not necessarily distinct
- C. All root and negative
- D. May be imaginary

Answer: A



Watch Video Solution

Assignment (Section -C) (objective Type Questions (more then a one options are correct)

1. If $|3z-1|=3|z-2|$, then z lies on

- A. $6\operatorname{Re}(z) = 7$

- B. On the perpendicular bisector of line joining $\left(\frac{1}{3}, 0\right)$ and $(2, 0)$
- C. A line parallel to x-axis
- D. A line parallel to y-axis

Answer: A::B::D



Watch Video Solution

2. If $S = \sum_{k=1}^{10} \left(\sin \frac{2\pi k}{11} + i \cos \frac{2\pi k}{11} \right)$ then

A. $S + \bar{S} = 0$

B. $S\bar{S} = 1$

C. $\sqrt{S} = \pm \frac{1}{\sqrt{2}}(1 + i)$

D. $S - \bar{S} = 0$

Answer: A::B::C



Watch Video Solution

3. Let $\cos A + \cos B + \cos C = 0$ and $\sin A + \sin B + \sin C = 0$ then which of the following statement(s) is/are correct?

A. $\sum \cos(2A - B - C) = 1$

B. $\sum \cos(2A - B - C) = 0$

C. $\sum \sin(2A - B - C) = 0$

D. $\sum (2A - B - C) = 3$

Answer: A::C



Watch Video Solution

4. The equation whose roots are n th power of the roots of the equation, $x^2 - 2x \cos \phi + 1 = 0$ is given by

A. $(x + \cos n\phi)^2 + \sin^2 n\phi = 0$

B. $(x - \cos n\phi)^2 + \sin^2 n\phi = 0$

C. $X^2 + 2x \cos n\phi + 1 = 0$

D. $x^2 - 2x \cos n\phi + 1 = 0$

Answer: B::D



Watch Video Solution

5. If $z(1+a) = b+ic$ and $a^2 + b^2 + c^2 = 1$, then

$[(1+iz)/(1-iz) = \frac{a+ib}{1+c}]$ b. $\frac{b-ic}{1+a}$ c. $\frac{a+ic}{1+b}$ d. none of these

A. $\frac{b-ic}{1-ia}$

B. $\frac{a+ib}{1+c}$

C. $\frac{1-c}{a+ib}$

D. $\frac{1+a}{b+ic}$

Answer: B::C



Watch Video Solution

6. z_1, z_2, z_3, z_4 are distinct complex numbers representing the vertices of a quadrilateral $ABCD$ taken in order. If $z_1 - z_4 = z_2 - z_3$ and $\arg[(z_4 - z_1)/(z_2 - z_1)] = \pi/2$, the quadrilateral is

- A. Rhombus
- B. Square
- C. Rectangle
- D. A cyclic quadrilateral

Answer: C::D



Watch Video Solution

7. If α, β, γ are cube roots of $p < 0$, then for any x, y, z

$$\frac{\alpha^2 x^2 + \beta^2 y^2 + \gamma^2 z^2}{\beta^2 x^2 + \gamma^2 y^2 + \alpha^2 z^2}$$

is

- A. 1

B. $\frac{\alpha}{\gamma}$

C. $\frac{\beta}{\alpha}$

D. $\frac{\gamma}{\beta}$

Answer: B::C::D



Watch Video Solution

8. If z is a complex number satisfying $z + z^{-1} = 1$ then $z^n + z^{-n}$, $n \in N$, has the value

A. $2(-1)^n$ when n is a multiple of 3

B. $(-1)^{n-1}$, when n is not a multiple of 3

C. $(-1)^{n+1}$, when n is a multiple of 3.

D. 0 when n is not a multiple of 3.

Answer: A::B



Watch Video Solution

9. If z satisfies $|z - 1| < |z + 3|$ then $\omega = 2z + 3 - i$ satisfies

A. $|\omega - 5 - i| < |\omega + 3 + i|$

B. $|\omega - 5| < |\omega + 3|$

C. $\text{Im}(i\omega) < 1$

D. $|\arg(\omega - 1)| < \frac{\pi}{2}$

Answer: B::D



Watch Video Solution

10. If $|z + \omega|^2 = |z|^2 + |\omega|^2$, where z and ω are complex numbers, then

A. $\frac{z}{\omega}$ is purely real

B. $\frac{z}{\omega}$ is purely imaginary

C. $z\bar{\omega} + \bar{z}\omega = 0$

D. $\text{amp}\left(\frac{z}{\omega}\right) = \frac{\pi}{2}$

Answer: B::C::D



Watch Video Solution

11. Let z_1 and z_2 be two complex numbers represented by points on circles $|z| = 1$ and $|z| = 2$ respectively, then

A. $\min |z_1 - z_2| = 1$

B. $\max |2z_1 + z_2| = 4$

C. $\left| z_2 + \frac{1}{z_1} \right| \leq 3$

D. $\min |z_1 - z_2| = 2$

Answer: A::B::C



Watch Video Solution

12. Let complex number z satisfy $\left| z - \frac{2}{z} \right| = 1$ then $|z|$ can take all values except

A. 1

B. 2

C. 3

D. 4

Answer: C::D



Watch Video Solution

13. If $z = x + iy$, then the equation $\left| \frac{2z - i}{z + 1} \right| = m$ does not represent a circle, when m is (a) $\frac{1}{2}$ (b). 1 (c). 2 (d). 3

A. $m = \frac{1}{2}$

B. $m=1$

C. $m = 2$

D. $m= 3$

Answer: A::B::D

14. If $\sqrt[3]{-1} = -1, -\omega, -\omega^2$, then roots of the equation $(x + 1)^3 + 64 = 0$ are

A. $-1 - 4\omega$

B. $-1 - 4\omega^2$

C. -5

D. -4

Answer: A::B::C

15. If $z_1 = p + iq$ and $z_2 = u + iv$ are complex numbers such that $|z_1| = |z_2| = 1$ and $\operatorname{Re}(z_1 \bar{z}_2) = 0$ then the pair of complex number, $\omega_1 = p + iu$ and $\omega_2 = q + iv$ satisfies.

(1) $|\omega_1| = 1$ (2) $|\omega_2| = 1$

(3) $Re(\omega_1, \bar{\omega}_2) = 0$ (4) None of these

A. $|\omega_1| = 1$

B. $|\omega_2| = 1$

C. $Re(\omega_1 \bar{\omega}_2) = 0$

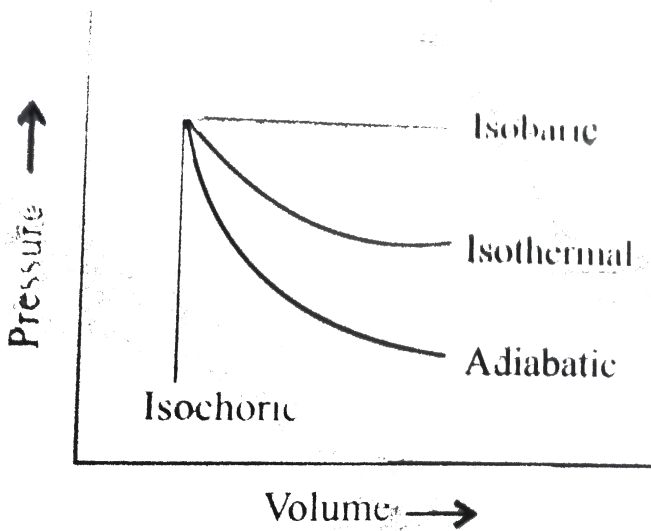
D. $|\omega_1| = 2|\omega_2|$

Answer: A::B::C



Watch Video Solution

16. The pressure-volume of various thermodynamic process is shown in graphs:



Work is the mole of transference of energy. It has been observed that reversible work done by the system is the maximum obtainable work.

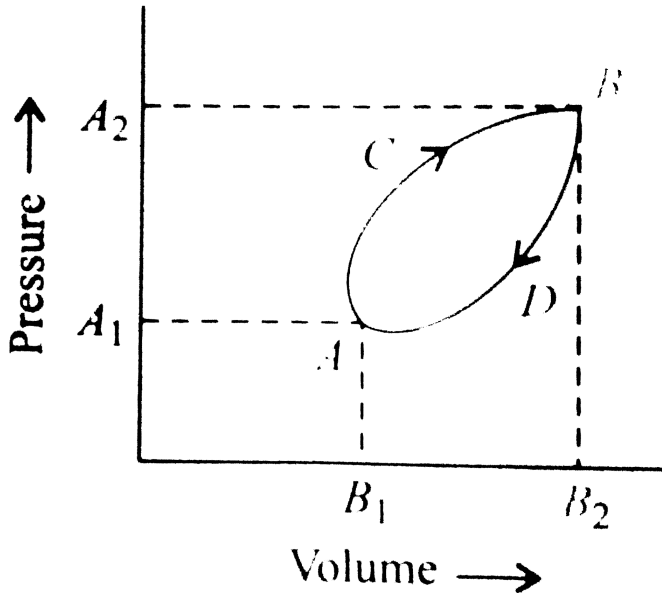
$$w_{rev} > w_{irr}$$

The works of isothermal and adiabatic processes are different from each other.

$$\begin{aligned} w_{\text{isothermal reversible}} &= 2.303nRT \log_{10} \left(\frac{V_2}{V_1} \right) \\ &= 2.303nRT \log_{10} \left(\frac{P_2}{P_1} \right) \end{aligned}$$

$$w_{\text{adiabatic reversible}} = C_V(T_1 - T_2)$$

A thermodynamic system goes in a cyclic process as represented in the following $P - V$ diagram:



The net work done during the complete cycle is given by the area

- A. $|z|=5$
- B. $|z| \leq 5$
- C. $|z| \geq 5$
- D. $2 \leq |z| \leq 3$

Answer: B::D



Watch Video Solution

17. If z_1, z_2 be two complex numbers satisfying the equation

$$\left| \frac{z_1 + z_2}{z_1 - z_2} \right| = 1, \text{ then}$$

A. $z_1 \bar{z} + z_2 \bar{z}_1 = 1$

B. $\left(\frac{\bar{z}_1}{\bar{z}_2} \right) = - \frac{z_1}{z_2}$

C. $z_1 \bar{z}_2 + z_2 \bar{z}_1 = 0$

D. $Re(z_1 \bar{z}_2) = 0$

Answer: B::C::D



Watch Video Solution

18. If $\sin \alpha, \cos \alpha$ are the roots of the equation $x^2 + bx + c = 0 (c \neq 0)$, then

A. $a^2 - b^2 + 2ac = 0$

B. $(a + c)^2 = b^2 + c^2$

C. $\frac{b}{a} \in | -\sqrt{2}, \sqrt{2} |$

D. $\frac{c}{a} \in \left[-\frac{1}{2}, \frac{1}{2} \right]$

Answer: A::B::C::D



Watch Video Solution

19. If α, β are the roots of the equation $ax^2 + 2bx + c = 0$ and $\alpha + h, \beta + h$ are the roots of the equation $Ax^2 + 2Bx + C = 0$ then

A. $h = \frac{b}{a} - \frac{B}{A}$

B. $\frac{b^2 - ac}{B^2 - AC} = \frac{a^2}{A^2}$

C. $h = \frac{Ac + aC}{A + a}$

D. $\frac{b^2 - aC}{B^2 - AC} = \frac{a}{A}$

Answer: A::B



Watch Video Solution

20. The solution set of the inequality $(x + 3)^5 - (x - 1)^5 \geq 244$ is

A. $(-\infty, 2]$

B. $[0, \infty)$

C. $(-2, -1)$

D. $(0,1)$

Answer: A::B



Watch Video Solution

21. Let a, b, c be real numbers in G.P. such that a and c are positive, then the roots of the equation $ax^2 + bx + c = 0$

A. Are real and in the ratio $b : ac$

B. Are real

C. Are imaginary and in ratio $1 : \omega$ is a non-real complex cubic root of constant

D. Are imaginary and are in the ration $\omega^2 : 1$ with usual notation

Answer: C::D



Watch Video Solution

22. Let $\cos \alpha$ be a root of the equation $25x^2 + 5x - 12 = 0 - 1 < x < 0$, then the value of $\sin^2 \alpha$ is

A. $\frac{20}{25}$

B. $-\frac{12}{25}$

C. $\frac{16}{25}$

D. $-\frac{24}{25}$

Answer: C



Watch Video Solution

23. If the quadratic equations $x^2 + pqx + r = 0$ and $z^2 + prx + q = 0$ have a common root then the equation containing their other roots is/are

A. $x^2 - p(q + r)x + p^2qr = 0$

B. $x^2p(q + r) + (q + r)x - pqr = 0$

C. $p(q + r)x^2 - (q + r)x + pqr = 0$

D. $x^2 + p(q + r)x - p^2qr = 0$

Answer: A::B



Watch Video Solution

24. The quadratic equation $x^2 - (m - 3)x + m = 0$ has

A. Real distinct roots if and only if $m \in (-\infty, 1) \cup (9, \infty)$

B. Both positive roots if and if and only if $m \in (9, \infty)$

C. Both negative roots if and only if $m \in (0, 1)$

D. No roots

Answer: A::B::C



Watch Video Solution

25. If both roots of the equation $x^2 - 2ax + a^2 - 1 = 0$ lie between -3 and 4 ,then [a] is/are , where [] represents the greatest ineger function

A. 1

B. - 1

C. 2

D. 0

Answer: A::B::C::D



Watch Video Solution

26.

Let

α, β the roots of $x^2 - 4x + A = 0$ and γ, δ be the roots of $x^2 - 36x + B = 0$. If $\alpha, \gamma, \beta, \delta$ forms an increasing G.P. Then

A. $B = 81A$

B. $A=3$

C. $B = 243$

D. $A + B = 251$

Answer: A::B::C



Watch Video Solution

27. For the equation $x^{\frac{3}{4}} (\log x)^2 + \log_2 x - \frac{5}{4} = \sqrt{2}$, which one of the following is true ?

A. Has at least one real solution

B. Has exactly three real solutions

C. Has exactly one irrational solutions

D. Has non-real complex roots

Answer: A::B::C



Watch Video Solution

28. If $f(x) = ax^2 + bx + c$, $g(x) = -ax^2 + bx + c$, where $ac \neq 0$, then prove that $f(x)g(x) = 0$ has at least two real roots.

A. At least three real roots

B. No real roots

C. At least two real roots

D. At most two imaginary roots

Answer: C::D



Watch Video Solution

29. Sum of the squares of all integral values of a for which the inequality

$x^2 + ax + a^2 + 6a < 0$ is satisfied for all $x \in (1, 2)$ must be equal to

A. 90

B. 89

C. 80

D. 91

Answer: A::B::C



Watch Video Solution

30. If the roots of the equation $\frac{1}{x+p} + \frac{1}{x+q} = \frac{1}{r}$ are equal in magnitude but opposite in sign and its product is α

A. $p + q = r$

B. $p + q = 2r$

C. $\alpha^2 = \frac{p^2 + q^2}{2}$

$$\text{D. } \alpha = \frac{-p^2 + q^2}{2}$$

Answer: B::C



Watch Video Solution

31. Find the integral values of a for which $(a + 2)x^2 + 2(a + 1)x + a = 0$ will have both roots integers

A. 0

B. -1

C. -2

D. -3

Answer: A::B::D



Watch Video Solution

32. If $(x - 1)^2$ is a factor of $ax^3 + bx^2 + c$ then roots of the equation $cx^3 + bx + a = 0$ may be

A. (a)1

B. (b)− 1

C. (c)− 2

D. (d)0

Answer: A::C



Watch Video Solution

33. If $b^2 \geq 4ac$ for the equation $ax^4 + bx^2 + c = 0$ then all the roots of the equation will be real if

A. $b > 0, a < 0, c < 0$

B. $b > 0, a > 0, c > 0$

C. $b < 0, a > 0, c > 0$

D. $b > 0, a < 0, c < 0$

Answer: C::D



Watch Video Solution

34. If the difference between the roots of the equation $x^2 + ax + 1 = 0$ is less than $\sqrt{5}$, then find the set of possible value of a .

A. $(-3, 0)$

B. $(0, 3)$

C. $(-3, 3)$

D. $(3, \infty)$

Answer: A::B::C



Watch Video Solution

35. The set of all real numbers a such that $a^2 + 2a$, $2a + 3$, and $a^2 + 3a + 8$ are the sides of a triangle is _____

A. $\left(6, \frac{13}{2}\right)$

B. $(5, 7)$

C. $(5, \infty)$

D. $(0, 5)$

Answer: A::B::C

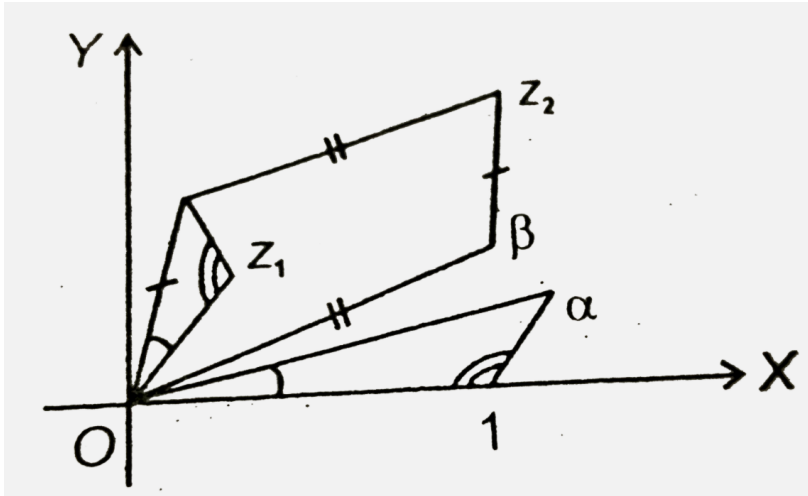


Watch Video Solution

Assignment (Section -D) Linked comprehension Type Questions

1. Let z_1, α, β be complex numbers of which α and β constants and z_1 varies. If z_2 is given in terms of z_1 by one of the following equations, it is required to find z_2 corresponding to z_1 then

In the given figure



A. $z_2 = \alpha z_1 + \beta$

B. $z_2 = \frac{\alpha z_1}{\beta}$

C. $z_2 = \alpha \beta z_1$

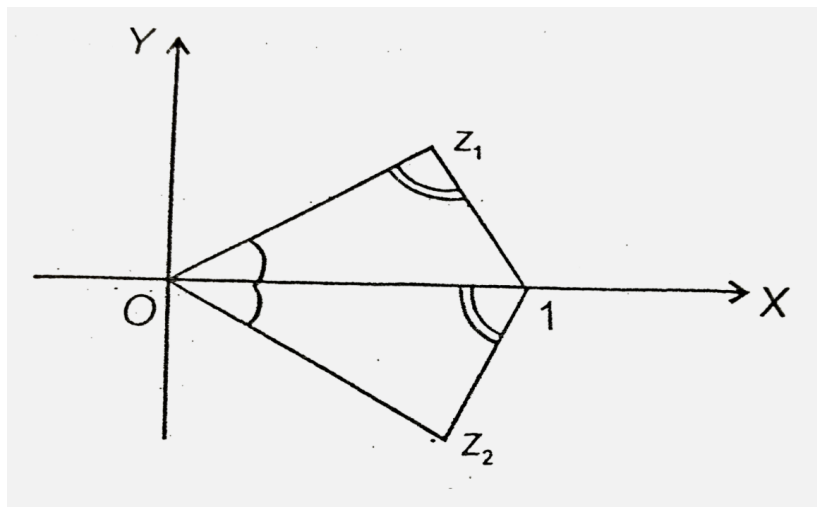
D. $z_2 = \beta z_1$

Answer: D



Watch Video Solution

2. Let z_1, α, β be complex numbers of which α and β constants and z_1 varies. If z_2 is given in terms of z_1 by one of the following equations, it is required to find z_2 corresponding to z_1 then The given figure illustrates



A. $z_2 = 1 + z_1$

B. $z_2 = 2z_1$

C. $z_2 = \frac{1}{z_1}$

D. $z_2 = \frac{1}{z_1^2}$

Answer: C



Watch Video Solution

3. If x is the root of the equation $x^2 - ix - 1 = 0$, then

The value of x^{51} is

A. 1

B. -1

C. i

D. $-i$

Answer: C



Watch Video Solution

4. If x is the root of the equation $x^2 - ix - 1 = 0$, then

The value of $x^{20} + \frac{1}{x^{20}}$ may be

A. -1

B. 1

C. i

D. $-i$

Answer: A



Watch Video Solution

5. If x is the root of the equation $x^2 - ix - 1 = 0$, then

$x^{2013} - \frac{1}{x^{2013}}$ may be

A. -1

B. 1

C. $-2i$

D. $-i$

Answer: C



Watch Video Solution

6. $(1 + x)^n = a_0 + a_1x + a_2x^2 + \dots + a_nx^n$ then

Find the sum of the series $a_0 + a_2 + a_4 + \dots$

A. 2^n

B. 2^{n-1}

C. 2

D. 2^{n-2}

Answer: B



Watch Video Solution

7. The sum of the series $a_0 + a_4 + a_8 + a_{12} + \dots$ is

A. $2^n \cos \frac{n\pi}{4}$

B. $2^{n-1} \cos \frac{n\pi}{4}$

C. $2^{n-1} \cos \frac{n\pi}{4}$

D. $2^{\frac{n}{2}} \cos \frac{n\pi}{4}$

Answer: D



Watch Video Solution

8. If $(1 + x)^n = a_0 + a_1x + a_2x^2) \dots + a_nx^n$ The sum of the series $a_0 + a_4 + a_8 + a_{12} + \dots$ is

A. $2^{n-1} \cos \frac{n\pi}{4}$

B. $2^{n-2} + 2^{\frac{n}{2}-1} \cos \frac{n\pi}{4}$

C. $2^{n-1} + 2^{\frac{n}{2}} \sin \frac{n\pi}{4}$

D. $2^{n-1} \sin \frac{n\pi}{4}$

Answer: B



Watch Video Solution

9. Let us consider an equation $f(x) = x^3 - 3x + k = 0$. then the values of k for which the equation has

Exactly one root which positive , then k belongs to

A. $(-\infty, -2)$

B. $(2, \infty)$

C. $(0,2)$

D. $(-2, 0)$

Answer: A



Watch Video Solution

10. Let us consider an equation $f(x) = x^3 - 3x + k = 0$. then the values of k for which the equation has

Exactly one root which is negative, then k belong

A. $(2, \infty)$

B. $(0,2)$

C. $(-2,0)$

D. $(-\infty, -2)$

Answer: A



Watch Video Solution

11. Let us consider an equation $f(x) = x^3 - 3x + k = 0$. then the values of k for which the equation has

One negative and two positive root if k belongs to

A. $(2, \infty)$

B. $(0, 2)$

C. $(-2, 0)$

D. $(2, 3)$

Answer: B



Watch Video Solution

12. Exactly two real roots, when k belongs to

A. $(-1, 1)$

B. $\left(-1, \frac{5}{4}\right)$

C. $(-\infty, -1) \cup \left(\frac{5}{4}, \infty\right)$

D. \mathbb{R}

Answer: C



Watch Video Solution

13. The values of 'K' for which the equation $|x|^2(|x|^2 - 2k + 1) = 1 - k^2$,
has No root, when k belongs to

A. $(-\infty, -1)$

B. $(-1, 1)$

C. $\left(1, \frac{5}{4}\right)$

D. \mathbb{R}

Answer: B



Watch Video Solution

14. Exactly two real roots, when k belongs to

A. $\{1, -1\}$

B. $\{0, 1\}$

C. $\{0, -1\}$

D. $\{2, 3\}$

Answer: A



Watch Video Solution

Assertion -Reason Type Questions

1. Statement-1 : let z_1 and z_2 be two complex numbers such that $\arg(z_1) = \frac{\pi}{3}$ and $\arg(z_2) = \frac{\pi}{6}$ then $\arg(z_1 z_2) = \frac{\pi}{2}$
and

Statement -2 : $\arg(z_1 z_2) = \arg(z_1) + \arg(z_2) + 2k\pi, k \in \{0, 1, -1\}$

A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -1

B. Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -1

C. Statement -1 is True, Statement -2 is False

D. Statement -1 is False, Statement -2 is True

Answer: A



Watch Video Solution

2. Statement-1 : The locus of z , if $\arg\left(\frac{z-1}{z+1}\right) = \frac{\pi}{2}$ is a circle.

and

Statement -2 : $\left|\frac{z-2}{z+2}\right| = \frac{\pi}{2}$, then the locus of z is a circle.

A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -2

B. Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -2

C. Statement -1 is True, Statement -2 is False

D. Statement -1 is False, Statement -2 is True

Answer: D



Watch Video Solution

3. Statement-1 : If $e^{i\theta} = \cos \theta + i \sin \theta$ and the value of $e^{iA} \cdot e^{iB} \cdot e^{iC}$ is equal to -1, where A,B,C are the angles of a triangle.

and

Statement -2 : In any $\triangle ABC$, $A + B + C = 180^\circ$

- A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -1
- B. Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -1
- C. Statement -1 is True, Statement -2 is False
- D. Statement -1 is False, Statement -2 is True

Answer: A



Watch Video Solution

4. Statement-1 : $z_1^2 + z_2^2 + z_3^2 + z_4^2 = 0$ where z_1, z_2, z_3 and z_4 are the fourth roots of unity

and

Statement -2 : $(1)^{\frac{1}{4}} = (\cos 0^\circ + i\sin 0^\circ)^{\frac{1}{4}}$

- A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -4
- B. Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -4
- C. Statement -1 is True, Statement -2 is False
- D. Statement -1 is Flase, Statement -2 is True

Answer: A



Watch Video Solution

5. Statement -1 : For any four complex numbers z_1, z_2, z_3 and z_4 , it is given that the four points are concyclic, then $|z_1| = |z_2| = |z_3| = |z_4|$

Statement -2 : Modulus of a complex number represents the distance form origin.

- A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -5

- B. Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -5
- C. Statement -1 is True, Statement -2 is False
- D. Statement -1 is False, Statement -2 is True

Answer: D



Watch Video Solution

6. Statement -1 : The expression $\left(\frac{2i}{1+i}\right)^n$ is a positive integer for all the values of n.

and

Statement -2 : Here n=8 is the least positive for which the above expression is a positive integer.

- A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -6

- B. Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -6
- C. Statement -1 is True, Statement -2 is False
- D. Statement -1 is False, Statement -2 is True

Answer: D



Watch Video Solution

7. Statement -1 : if $1 - i, 1 + i, z_1$ and z_2 are the vertices of a square taken in order in the anti-clockwise sense then z_1 is $i - 1$ and Statement -2 : If the vertices are z_1, z_2, z_3, z_4 taken in order in the anti-clockwise sense, then $z_3 = iz_1 + (1 + i)z_2$

- A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -7
- B. Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -7

C. Statement -1 is True, Statement -2 is False

D. Statement -1 is False, Statement -2 is True

Answer: A

 **Watch Video Solution**

8. Statement-1 : IF $\left| z + \frac{1}{z} \right| = a$, where z is a complex number and a is a real number, the least and greatest values of $|z|$ are $\frac{\sqrt{a^2 + 4} - a}{2}$ and $\frac{\sqrt{a^2 + 4} + a}{2}$

and Statement -2 : For a equal to zero the greatest and the least values of $|z|$ are equal .

A. (a) Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -1

B. (b) Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -1

C. (c) Statement -1 is True, Statement -2 is False

D. (d) Statement -1 is False, Statement -2 is True

Answer: B



Watch Video Solution

9. Statement-1 : The locus of complex number z , satisfying $(z - 2)^n = z^n$ is a straight line .

and

Statement -2 : The equation of the form $ax + by + c = 0$ in $x - y$ plane is the general equation of straight line.

A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -1

B. Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -1

C. Statement -1 is True, Statement -2 is False

D. Statement -1 is False, Statement -2 is True

Answer: A



Watch Video Solution

10. Statement -1 : A root of the equation

$$(2^{10} - 3)x^2 - 2^{11}x + 2^{10} + 3 = 0 \text{ is } 1$$

and

Statement-2 : The sum of the coefficients of a quadratic equation is zero, then 1 is a root of the equation.

- A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -1
- B. Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -1
- C. Statement -1 is True, Statement -2 is False
- D. Statement -1 is False, Statement -2 is True

Answer: A



Watch Video Solution

11. Statement -1: The equation whose roots are reciprocal of the roots of the equation $10x^2 - x - 5 = 0$ is $5x^2 + x - 10 = 0$

and

Statement -2 : To obtain a quadratic equation whose roots are reciprocal of the roots of the given equation $ax^2 + bx + c = 0$ change the coefficients a, b, c to c, b, a . ($c \neq 0$)

A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -1

B. Statement -1 is True, Statement -2 is True, Statement -2 is NOT a correct explanation for Statement -1

C. Statement -1 is True, Statement -2 is False

D. Statement -1 is False, Statement -2 is True

Answer: A



Watch Video Solution

12. Statement-1 : The equation $x^2 - 2009x + 2008 = 0$ has rational roots

.

and

Statement -2 : The quadratic equation $ax^2 + bx + c = 0$ has rational roots iff $b^2 - 4ac$ is a perfect square.

A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -12

B. Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -12

C. Statement -1 is True, Statement -2 is False

D. Statement -1 is False, Statement -2 is True

Answer: C



Watch Video Solution

13. Statement -1 : one root of the equation $x^2 + 5x - 7 = 0$ lie in the interval (1,2).

and

Statement -2 : For a polynomial $f(x)$, if $f(p)f(q) < 0$, then there exists at least one real root of $f(x) = 0$ in (p,q)

A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -1

B. Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -1

C. Statement -1 is True, Statement -2 is False

D. Statement -1 is False, Statement -2 is True

Answer: A



Watch Video Solution

14. Statement -1 : The quadratic equation $ax^2 + bx + c = 0$ has real roots if $(a + c)^2 > b^2$, $\forall, a, b, c \in R$.

and

Statement -2 : The quadratic equation $ax^2 + bx + c = 0$ has real roots if $b^2 - 4ac \geq 0$

A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -14

B. Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -14

C. Statement -1 is True, Statement -2 is False

D. Statement -1 is False, Statement -2 is True

Answer: D



Watch Video Solution

15. Statement -1 : There is just one quadratic equation with real coefficients, one of whose roots is $\frac{1}{3 + \sqrt{7}}$

and

Statement -2 : In a quadratic equation with rational coefficients the irrational roots occur in pair.

A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -1

B. Statement -1 is True, Statement -2 is True, Statement -2 is NOT a correct explanation for Statement -1

C. Statement -1 is True, Statement -2 is False

D. Statement -1 is False, Statement -2 is True

Answer: D



Watch Video Solution

16. Statement -1 : The roots of $x^2 + 2\sqrt{2008}x + 501 = 0$ are irrational .
and

Statement -2: If the discriminant of the equation $ax^2 + bx + c = 0, a \neq 0, (a, b, c, \in R)$ is a perfect square, then the roots are rational.

- A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -16
- B. Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -16
- C. Statement -1 is True, Statement -2 is False
- D. Statement -1 is False, Statement -2 is True

Answer: C



Watch Video Solution

17. Statement -1 : if a, b, c not all equal and $a \neq 0, a^3 + b^3 + c^3 = 3abc$, then the equation $ax^2 + bx + c = 0$ has two real roots of opposite sign.
and

Statement -2 : If roots of a quadratic equation $ax^2 + bx + c = 0$ are real and of opposite sign then $ac < 0$.

- A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -17
- B. Statement -1 is True, Statement -2 is True, Statement -2 is NOT a correct explanation for Statement -17
- C. Statement -1 is True, Statement -2 is False
- D. Statement -1 is False, Statement -2 is True

Answer: D



Watch Video Solution

18. Statement -1 : There is just one quadratic equation with real coefficient one of whose roots is $\frac{1}{\sqrt{2} + 1}$

and

Statement -2 : In a quadratic equation with rational coefficients the irrational roots are in conjugate pairs.

A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -18

B. Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -18

C. Statement -1 is True, Statement -2 is False

D. Statement -1 is False, Statement -2 is True

Answer: D



Watch Video Solution

19. Statement-1 : Let a quadratic equation has a root $3 - 9i$ then the sum of roots is 6.

and

Statement -2 : If one root of $ax^2 + bx + c = 0, a \neq 0, a, b, c \in R$ is $\alpha + i\beta, \alpha, \beta \in R$ then the other roots must be $\alpha - i\beta$

A. Statement -1 is True, Statement -2 is True, Statement -2 is a correct explanation for statement -19

B. Statement -1 is True, Statement -2 is True , Statement -2 is NOT a correct explanation for Statement -19

C. Statement -1 is True, Statement -2 is False

D. Statement -1 is False, Statement -2 is True

Answer: A



Watch Video Solution

Section-F (Matrix -Match type Question)

1. Match the following :

Column - I

- (A) The smallest positive integer for which $(1+i)^n = (1-i)^n$ is
- (B) If $\sqrt[3]{a+ib} = x+iy$ and $\frac{b}{y} - \frac{a}{x} = k(x^2+y^2)$ then k is equal to
- (C) If $x = \frac{1+i}{\sqrt{2}}$, then the value of $1+x^2+x^4+x^6+x^8+x^{10}+\dots$ +
- (D) If the minimum value of $|z+1+i| + |z-1-i| + |2-z| + |3-z|$



Watch Video Solution

2. Let z_1 and z_2 be two given complex numbers. The locus of z such that

Column -I

- (A) $|z-z_1| + |z-z_2| = \text{constant} = k$, where $k \neq |z_1-z_2|$
- (B) $|z-z_1| - |z-z_2| = k$ where $k \neq |z_1-z_2|$
- (C) $\arg\left(\frac{z-z_1}{z-z_2}\right) = \pm \frac{\pi}{2}$
- (D) If ω lies on $|\omega| = 1$ then

Column-II

- (p) Circle
- (q) Circle
- (r) Hyperbola
- (s) Ellipse



Watch Video Solution

3. Match the following :

Column-I

(A) $|z - 6i| + |z - 8| = k$ will represent an ellipse for k equals to

(B) $||z - 12i + 3| - |z - 2|| = k$ will represent hyperbola if k equals to

(C) $|z = ki| + |z - 4| = \sqrt{10k}$ will represent line segment if k equals to

(D) $\frac{z - k + 2ki}{|z - 2 + 4i|} = k$ will represent circle if k equals to



Watch Video Solution

4. Match the following

Column-I

(A) if the roots of the equation $x^2 - 2ax + a^2 + a - 3 = 0$ are real and less than

(B) If the roots of the equation $x^2 - 2ax + a^2 + a - 3 = 0$ are real and

(C) If exactly one root of the above equation lies in the interval $(1, 3)$ then a

(D) IF the roots of the above equation are such that one root is greater than



Watch Video Solution

5. Let $f(x) = |x - 1| + |x - 2| + |x - 3|$, match the column I for the value of k column II.

Column - I

Column -II

- | | |
|--|-------|
| (A) $f(x) = k$ has no solution | (p) 1 |
| (B) $f(x) = k$ has only one solution | (q) 2 |
| (C) $f(x) = k$ has two solution of same sign | (r) 4 |
| (D) $f(x) = k$ has two solution of opposite sign | (s) 5 |
| | (t) 8 |



Watch Video Solution

6. For given equation $x^2 - ax + b = 0$, match conditions in column I with possible values in column II

column -I

- (A) If roots differ by unity then a^2 is equal to
- (B) If roots differ by unity then $1 + a^2$ is equal to
- (C) If one of the root be twice the other then $2a^2$ is equal to
- (D) If the sum of roots of the equation equal to the sum of squares of their



Watch Video Solution

7. If α, β, γ be the roots of the equation $x(1 + x^2) + x^2(6 + x) + 2 = 0$ then match the entries of column-I with those of column-II.

column-I

(A) $\alpha^{-1} + \beta^{-1} + \gamma^{-1}$ is equal to

(B) $\alpha^2 + \beta^2 + \gamma^2$ equals

(C) $(\alpha^{-1} + \beta^{-1} + \gamma^{-1}) - (\alpha + \beta + \gamma)$ is equal to

(D) $[\alpha^{-1} + \beta^{-1} + \gamma^{-1}]$ equals where $[\cdot]$ denotes the greatest integer equal to or less than \cdot



Watch Video Solution

section-G(Integer Answer type Questions)

1. P is a point satisfying $\arg z = \pi/4$, such that sum of its distance from two given point (0,1) and (0,2) is minimum, then P must be $\frac{k}{2}(1+i)$ then numerical value of k should be _____.



Watch Video Solution

2. $\sum_{r=1}^{2002 + (2k-1)} \cos\left(\frac{2r\pi}{7}\right) + i \sin\left(\frac{2r\pi}{7}\right) = 0$ then the non negative integral values of k less than 10 may be



Watch Video Solution

3. If $z = x + iy$ and roots $z\bar{z}^3 + \bar{z}z^3 = 30$ are the vertices of a rectangle and z_0 is centre of rectangle. Let d be distance of z_0 from the point on circle $|z-3| \leq 2$ then maximum value of d is _____



Watch Video Solution

4. If the complex number $A(z_1), B(z_2)$ and origin forms an isosceles triangle such that $\angle(AOB) = \frac{2\pi}{3}$, then $\frac{z_1^2 + z_2^2 + 4z_1z_2}{z_1z_2}$ equals _____



Watch Video Solution

5. The area of the triangle formed by three point $\sqrt{3} + i, -1 + \sqrt{3}i$ and $(\sqrt{3} - 1) + (\sqrt{3} + 1)i$ is _____



Watch Video Solution

6. The number of values (s) of k , for which both the roots of the equation $x^2 - 6kx + 9(k^2 - k + 1) = 0$ are real, distinct and have values atmost 3 is _____



Watch Video Solution

7. The possible greatest integral value of a for which the expression $\frac{ax^2 + 3x + 4}{x^2 + 2x + 2}$ is less than 5 for all real x is _____



Watch Video Solution

8. Let $f(x) = ax^2 + bx + c$ where a, b, c are real numbers. If the numbers $2a$, $a + b$ and c are all integers, then the number of integral values between 1 and 5 that $f(x)$ can take is _____



Watch Video Solution

1. Let A,B and C be three sets of complex numbers as defined below:

$$A = \{z: \operatorname{Im}(z) \geq 1\}$$

$$B = \{z: |z - 2 - i| = 3\}$$

$$C = \{z: \operatorname{Re}(1 - i)z) = 3\sqrt{2} \text{ where } i = \sqrt{-1}\}$$

Let z be any point in $A \cap B \cap C$. Then, $|z + 1 - i|^2 + |z - 5 - i|^2$ lies between

A. TTT

B. TTF

C. TFT

D. FFF

Answer: A



Watch Video Solution

2. If $\alpha = e^{i2\pi/7}$ and $f(x) = a_0 + \sum_{k=0}^{20} a_k x^k$, then prove that the value of $f(x) + f(\alpha x) + \dots + f(\alpha^6 x)$ is independent of α .

A. F T T

B. F T F

C. F F F

D. T F T

Answer: A



Watch Video Solution

3. Statement -1 : Two regular polygons are inscribed in the same circle.

The first polygon has 1982 sides and second has 2973 sides. If the polygons have a common vertex, then the number of vertex common to both of them is 991.

Statement -2 : The total number of complex numbers z , satisfying $|z-1| = |z+1| = |z|$ is one

Statement -3 : The locus represented by $|2011z+1| = 2011|z+1|$ is a straight line

A. (a) T T T

B. (b) T F T

C. (c) F T T

D. (d) F F F

Answer: B



Watch Video Solution

4. Statement -1 : If x is real and $y = \frac{x^2 - x + 3}{x + 2}$, then $y \in (-\infty, \infty) - (-11, 1)$

Statement -2 : If $[\]$ represents the greatest integer function and $f(x) = x - [x]$ then number of real roots of the equation $f(x) + f\left(\frac{1}{x}\right) = 1$ are infinite.

Statement -3 : if the difference of the roots of the equation $x^2 + hx + 7 = 0$ is 6, then , possible value (s) of h are -8 and 8.

A. T T T

B. T T F

C. T F F

D. F F F

Answer: A



Watch Video Solution

5. The solution of the equation $(3|x| - 3)^2 = |x| + 7$ which belongs to the domain of $\sqrt{x(x - 3)}$ are given by

A. F F T

B. T T F

C. T F F

D. T T T

Answer: D



Watch Video Solution

1. If α, β and γ are the roots of $X^3 - 3X^2 + 3X + 7 = 0$, find the value of $\frac{\alpha - 1}{\beta - 1} + \frac{\beta - 1}{\gamma - 1} + \frac{\gamma - 1}{\alpha - 1}$.



Watch Video Solution

2. A man walks a distance of 3 units from the origin towards the North-East ($N45^\circ E$) direction. From there, he walks a distance of 4 units towards the North-West ($N45^\circ W$) direction to reach a point P . Then, the position of P in the Argand plane is (a) $3e^{\frac{i\pi}{4}} + 4i$ (b) $(3 - 4i)e^{\frac{i\pi}{4}}$ (c) $(4 + 3i)e^{\frac{i\pi}{4}}$ (d) $(3 + 4i)e^{\frac{i\pi}{4}}$



Watch Video Solution

3. Let z_1 and z_2 be two given complex numbers such that $\frac{z_1}{z_2} + \frac{z_2}{z_1} = 1$ and $|z_1| = 3$, then $|z_1 - z_2|^2$ is equal to



Watch Video Solution

4. The locus of the centre of a circle which touches the given circles $|z - z_1| = |3 + 4i|$ and $|z - z_2| = |1 + i\sqrt{3}|$ is a hyperbola, then the length of its transverse axis is



Watch Video Solution

5. If $|z| = 1$ and $z \neq \pm 1$, then all the values of $\frac{z}{1 - z^2}$ lie on a line not passing through the origin $|z| = \sqrt{2}$ the x-axis (d) the y-axis



Watch Video Solution

6. If $|z_1 + z_2|^2 = |z_1|^2 + |z_2|^2$ the $\frac{6}{\pi} \arg\left(\frac{z_1}{z_2}\right)$ is equal to



Watch Video Solution

7. For every real number $a \geq 0$, find all the complex numbers z that satisfy the equation $2|z| - 4az + 1 + ia = 0$



Watch Video Solution

8. Let z_1, z_2 be complex numbers with $|z_1| = |z_2| = 1$ prove that $|z_1 + 1| + |z_2 + 1| + |z_1 z_2 + 1| \geq 2$.



Watch Video Solution

9. If one root of the quadratic equation $ax^2 + bx + c = 0$ is equal to the n^{th} power of the other root, then show that $(ac^n)^{\frac{1}{n+1}} + (a^n c)^{\frac{1}{n+1}} + b = 0$



Watch Video Solution

10. Let α and β be the roots of the equation $x^2 - px + q = 0$ and $V_n = \alpha^n + \beta^n$, Show that $V_{n+1} = pV_n - qV_{n-1}$
find V_5



Watch Video Solution

11. If p, q are roots of the quadratic equation $x^2 - 10rx - 11s = 0$ and r, s are roots of $x^2 - 10px - 11q = 0$ then find the value of $p+q+r+s$.



Watch Video Solution

12. Solve for x : $4^{x+1.5} + 9^{x+0.5} = 10.6^x$.



Watch Video Solution

13. Let α and β be the values of x obtained from the equation $\lambda^2(x^2 - x) + 2\lambda x + 3 = 0$ and if λ_1, λ_2 be the two values of λ for which α and β are connected by the relation $\frac{\alpha}{\beta} + \frac{\beta}{\alpha} = \frac{4}{3}$. then find the value of $\frac{\lambda_1^2}{\lambda_2} + \frac{\lambda_2^2}{\lambda_1}$ and $\frac{\lambda_1^2}{\lambda_2^2} + \frac{\lambda_2^2}{\lambda_1^2}$



Watch Video Solution

14. The twice of the product of real roots of the equation $(2x + 3)^2 - 3|2x + 3| + 2 = 0$ is _____



Watch Video Solution

15. The equation $ax^2 + bx + c = 0$ and $x^3 - 4x^2 + 8x - 8 = 0$ have two roots in common. Then $2b + c$ is equal to _____.



Watch Video Solution

16. If $x = 3 + 3^{1/3} + 3^{2/3}$, then the value of the expression $x^3 - 9x^2 + 8x - 12$ is equal to _____



Watch Video Solution

1. All complex numbers ' z ' which satisfy the relation $|z - |z + 1|| = |z + |z - 1||$ on the complex plane lie on the



Watch Video Solution

2. Suppose p is a polynomial with complex coefficients and all even degree. If all the roots of p are complex non-real numbers with modulus 1, prove that $p(1) \in \mathbb{R} \Leftrightarrow p(-1) \in \mathbb{R}$



Watch Video Solution

3. The point A_1, A_2, \dots, A_{10} are equally distributed on a circle of radius R (taken in order). Prove that $A_1 A_4 - A_1 A_2 = R$



Watch Video Solution

4. Let a and b be positive real numbers with $a^3 + b^3 = a - b$ and $k = a^2 + 4b^2$, then (1) $k < 1$ (2) $k > 1$ (3) $k = 1$ (4) $k > 2$



Watch Video Solution

5. Let k be a real number such that the inequality $\sqrt{x-3} + \sqrt{6-x} \geq k$ has a solution then the maximum value of k is

$\sqrt{3}$ (2) $\sqrt{6} - \sqrt{3}$

(3) $\sqrt{6}$ (4) $\sqrt{6} + \sqrt{3}$



Watch Video Solution

6. If α and β be the roots of the equation $x^2 + px - 1/(2p^2) = 0$, where $p \in \mathbb{R}$. Then the minimum value of $\alpha^4 + \beta^4$ is



Watch Video Solution

7. If the roots of the quadratic equation $x^2 - ax + 2b = 0$ are prime numbers, then the value of (a-b) is



Watch Video Solution

8. The number of real solutions of the equation $\sqrt[4]{97-x} + \sqrt[4]{x} = 5$

(1) 0 (2) 1

(3) 2 (4) 4



Watch Video Solution

9. If $f(x)$ is a polynomial of degree at least two with integral co-efficients then the remainder when it is divided by $(x-a)(x-b)$ is , where $a \neq b$

$$(1) \quad x \left[\frac{f(a) - f(b)}{b - a} \right] + \frac{af(b) - bf(a)}{a - b} \quad (2)$$

$$x \left[\frac{f(a) - f(b)}{a - b} \right] + \frac{af(b) - bf(a)}{a - b}$$

$$(3) \quad x \left[\frac{f(b) - f(a)}{a - b} \right] + \frac{af(b) - bf(a)}{a - b} \quad (4)$$

$$x \left[\frac{f(b) - f(a)}{a - b} \right] + \frac{bf(a) - af(b)}{a - b}$$



Watch Video Solution

10. Let $p(x)$ be a polynomial with real coefficient and $p(x) = x^2 + 2x + 1$. Find $P(1)$.



Watch Video Solution

11. If x, y, z are three real numbers such that $x + y + z = 4$ and $x^2 + y^2 + z^2 = 6$, then

(1) $\frac{2}{3} \leq x, y, z \leq 2$ (2) $0 \leq x, y, z \leq 2$

(3) $1 \leq x, y, z \leq 3$ (4) $2 \leq x, y, z \leq 3$



Watch Video Solution

12. If unity is double repeated root of $px^3 + g(x^2 + x) + r = 0$, then



Watch Video Solution

13. The number of real solutions of the equation $4x^{99} + 5x^{98} + 4x^{97} + 5x^{96} + \dots + 4x + 5 = 0$ is (1) 1 (2) 5 (3) 7 (4) 97



Watch Video Solution