



## MATHS

## **BOOKS - SHRI BALAJI MATHS (ENGLISH)**

# FUNCTION

**Single Choice Problems** 

1. Range of the function  $f(x) = \log_{\sqrt{2}} \bigl( 2 - \log_2 \bigl( 16 \sin^2 x + 1 \bigr) \bigr)$  is:

- A. [0, 1]
- B.  $(-\infty,2]$
- $\mathsf{C}.\,[\,-1,\,1]$
- D.  $(-\infty,\infty)$

### Answer: B

2. The values of lpha and eta for which  $\left|e^{|x-eta|}-lpha
ight|=2$  has four distinct solutions are

A. 
$$a\in(-2,\infty),b=0$$
  
B.  $a\in(2,\infty),b=0$   
C.  $a\in(3,\infty),b\in R$   
D.  $a\in(2,\infty)b=0$ 

### Answer: C

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3. The range of the function :

$$f(x) = an^{-1}x + rac{1}{2} {
m sin}^{-1}x$$

A. 
$$(\,-\pi/2,\pi/2)$$

B. 
$$[-\pi/2,\pi/2]-\{0\}$$
  
C.  $[-\pi/2,\pi/2]$   
D.  $(-3\pi/4,3\pi/4)$ 

### Answer: C

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4. Find the number of real ordered pair(s) (x, y) for which:  $16^{x^2+y} + 16^{x+y^2} = 1$ A.O B.1 C.2 D.3

### Answer: B

5. The conplete range of vlaues of 'a' such that  $\left(rac{1}{2}
ight)^{|x|}=x^2-a$  is

satisfied for maximum number of values of x is:

A. 
$$(-\infty, -1)$$

B.  $(-\infty,\infty)$ 

$$\mathsf{C.}\,(\,-1,1)$$

D.  $(-1,\infty)$ 

#### Answer: D

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6. For a real number x, let [x] denote the greatest integer less than or equal to x. Let f: R  $ightarrow\,$  R be defined as  $f(x)=2x+[x]+\sin x\cos x$  then f is

A. One-one but not onto

- B. onto but not one-one
- C. Both one-one and onto
- D. Neither one-one nor onto

### Answer: A

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7. The maximum value of 
$$\sec^{-1}\left(rac{7-5ig(x^2+3ig)}{2(x^2+2)}
ight)$$
 is:

A. 
$$\frac{5\pi}{6}$$
  
B.  $\frac{5\pi}{12}$   
C.  $\frac{7\pi}{12}$   
D.  $\frac{2\pi}{3}$ 

### Answer: D

8. Number of ordered pair (a,b) the set  $A = \{1, 2, 3, 4, 5\}$  so that the functon  $f(x) = \frac{x^3}{3} + \frac{a}{2}x^2 + bx + 10$  is an injective mapping  $\forall x \in R$ : A. `13 B. 14 C. 15 D. 16

### Answer: C

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9. let A be the greatest value of the function  $f(x) = \log_x[x]$ , (where [.] denotes gratest integer function) and B be the least value of the function  $g(x) = |\sin x| + |\cos x|$ , then :

A. A > B

 $\mathsf{B.}\, A < B$ 

 $\mathsf{C}.\, A=B$ 

D.2A + B = 4

Answer: C

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10. The function  $f:(a,\infty) o R$  where R denotes the range corresponding to the given domain, with rule  $f(x)=2x^3-3x^2+6$ , will have an inverse provided

A.  $a=1,B=[5,\infty)$ 

B.  $a = 2, B = [10, \infty)$ 

 $\mathsf{C}.\,a,0,B=[6,\infty)$ 

D. 
$$a=\,-1,B=[1,\infty)$$

Answer: A

11. Solution of the inequation  $\{x\}(\{x\}-1)(\{x\}+2)\geq 0$ 

where  $\{.\}$  denots fractin part function) is :

A.  $x\in(\,-2,1)$ 

B.  $x \in I$  (I denote set of integers)

 $\mathsf{C}.\,x\,\in\,[0,\,1)$ 

D.  $x\in [-2,0)$ 

#### Answer: B

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12. Let f(x), g(x) be two real valued functions then the function  $h(x) = 2 \max \{f(x) - g(x), 0\}$  is equal to :

A. 
$$f(x) - g(x) - |g(x) - f(x)|$$
  
B.  $f(x) + g(x) - |g(x) - f(x)|$ 

C. 
$$f(x)-g(x)+|g(x)-f(x)|$$
  
D.  $f(x)+g(x)+|g(x)-f(x)|$ 

Answer: C

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**13.** Let  $R = \{(1, 3), (4, 2), (2, 4), (2, 3), (3, 1)\}$  be a relation the set  $A = \{1, 2, 3, 4\}$ . The relation R is (a). a function (b). reflexive (c). not symmetric (d). transitive

A. a function

B. reflexive

C. not symmetric

D. transitive

Answer: C

14. The true set of valued of 'K' for which  $\sin^{-1} igg( rac{1}{1+\sin^2 x} igg) = rac{k\pi}{6}$  may

have a solution is :

A. 
$$\left[\frac{1}{4}, \frac{1}{2}\right]$$
  
B.  $[1, 2]$   
C.  $\left[\frac{1}{6}, \frac{1}{2}\right]$ 

D.[2, 4]

#### Answer: B



15. A real valued function f(x) satisfies the functional equation f(x - y) = f(x)f(y) - f(a - x)f(a + y), where a is a given constant and f(0)=1, f(2a-x) =?

A. -f(x)

 $\mathsf{B.}\,f(x)$ 

C. f(a) + f(a - x)D. f(-x)

#### Answer: A

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16. Let  $g \colon R o R$  be given by g(x) = 3 + 4x if  $g^n(x) = ext{ gogogo.....og}$  (x)

n times. Then inverse of  $g^n(x)$  is equal to :

A. 
$$(x + 1 - 4^n)$$
.  $4^{-n}$ 

B.  $(x - 1 + 4^n)4^{-n}$ 

C. 
$$(x + 1 + 4^n)4^{-n}$$

D. None of these

#### Answer: A

17. Let f:D o R bge defined as  $:f(x)=rac{x^2+2x+a}{x^2+4x+3a}$  where D and R denote the domain of f and the set of all the real numbers respectively. If

f is surjective mapping. Then the complete range of a is :

A.  $0 < a \le 1$ B.  $0 < a \le 1$ C.  $0 \le a < 1$ D. 0 < a < 1

#### Answer: D

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18. Let  $f\colon (-\infty,2] o (-\infty,4]$  be a function defined by  $f(x)=4x-x^2.$  Then,  $f^{-1}(x)$  is

A.  $2-\sqrt{4-x}$ 

B.  $2 + \sqrt{4-x}$ C.  $-2 + \sqrt{4-x}$ D.  $-2 - \sqrt{4-x}$ 

#### Answer: A

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**19.** IF  $\{5 \sin x\} + [\cos x] + 6 = 0$ , then range of  $f(x) = \sqrt{3} \cos x + \sin x$  corresponding to solution set of the given equation is: (where [.] denotes greatest integer function)

A. 
$$[-2, -1]$$
  
B.  $\left(-\frac{3\sqrt{3}+2}{5}, -1\right)$   
C.  $[-2, -\sqrt{3})$   
D.  $\left(-\frac{3\sqrt{3}+4}{5}, -1\right)$ 

Answer: D

**20.** If  $f: R \to R$  where  $f(x) = ax + \cos x$  is an invertible function, then (a).  $(-2, -1] \cup [1, 2);$  (b). [-1, 1]; (c).  $(-\infty, -1] \cup [1, \infty);$ (d).  $(-\infty, -2] \cup [2, \infty).$ A.  $(-2, -1] \cup [1, 2)$ B. [-1, 1]C.  $(-\infty, -1] \cup [1, \infty)$ D.  $(-\infty, -2] \cup [2, \infty)$ 

### Answer: C

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**21.** The range of function  $f(x) = [1 + \sin x] + \left[2 + \sin \frac{x}{2}\right] + \left[3 + \sin \frac{x}{3}\right] + \ldots + \left[n + \sin \frac{x}{n}\right] \forall x$ denotes greatest integer function) is :

$$\begin{array}{l} \text{A.} \left\{ \frac{n^2 + n - 2}{2}, \frac{n(n+1)}{2} \right\} \\ \text{B.} \left\{ \frac{n(n+1)}{2} \right\} \\ \text{C.} \left\{ \frac{n(n+1)}{2}, \frac{n^2 + n + 2}{2}, \frac{n^2 + n + 4}{2} \right\} \\ \text{D.} \left\{ \frac{n(n+1)}{2}, \frac{n^2 + n - 2}{2} \right\} \end{array}$$

#### Answer: D



**22.** Find the number of values of  $f(x) = \left[\frac{x}{15}\right] \left[-\frac{15}{x}\right]$  can take where  $x \in (0, 90)$  where [.] =GIF

A. 5

B. 6

C. 7

D. Infinite

Answer: B

23. Which of the following function is homogeneous ?

A. 
$$f(x) = x \sin y + y \sin x$$

$$\mathsf{B.}\,g(x)=xz\frac{^{y}}{x}+ye\frac{x}{y}$$

C. 
$$h(x)=rac{xy}{x+y^2}$$
  
D.  $\phi(x)=rac{x-y\cos x}{y\sin x+y}$ 

### Answer: B



24. Let 
$$f(x)=egin{bmatrix} 2x+3 & x>1\ lpha^2x+1 & x\leq 1 \end{bmatrix}$$
 If range of  $f(x)=R$  (set of real

numbers) then number orf integral value(s), which lpha any take :

B. 3

C. 4

D. 5

### Answer: C

25. The maximum integral values of x in the domain of 
$$f(x) = \log_{10} \left( \log_{1/3} (\log_4 (x-5)) \text{ is : (a). 5 (b). 7 (c). 8 (d). 9} \right)$$

A. 5

B. 7

C. 8

D. 9

## Answer: C

**26.** Range of the function f(x)= $\log_2 \left( \sqrt{x-2} + \sqrt{4-x} \right)$  is

A.  $(0, \infty)$ B.  $\left[\frac{1}{2}, 1\right]$ C. [1, 2]D.  $\left[\frac{1}{4}, 1\right]$ 

### Answer: B



27. Number of integers stastifying the equation  $|x^2 + 5x| + |x - x^2| = |6x|$  is: A. 3 B. 5 C. 7

D. 9

### Answer: C



28. Which of the following is not an odd function ?

A. In 
$$\left(rac{x^4+x^2+1}{\left(x^2+x+1
ight)^2}
ight)$$

C. sin (tan x)

D. 
$$f(x)$$
, where

$$f(x)+figg(rac{1}{x}igg)=f(x)figg(rac{1}{x}igg) orall x\in R-\{0\} egin{array}{l} ext{and} \ f(2)=33 \end{array}$$

#### Answer: D



**29.** Which of the following function is periodic with fundamental period  $\pi$ 

A. 
$$f(x) = \cos x \left| \frac{\sin x}{2} \right|$$
, where [.] denotes greatest integer function  
B.  $g(x) = \frac{\sin x + \sin 7x}{\cos x + \cos 7x} + |\sin x|$   
C.  $h(x) = \{x\} + |\cos x|$ , where {.} denotes functional part function  
D.  $\phi(x) = |\cos x| + \ln(\sin x)$ 

#### Answer: B

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**30.** Let 
$$f: N \to Z$$
 and  $f(x) = \begin{bmatrix} \frac{x-1}{2} & \text{when x is odd} \\ -\frac{x}{2} & \text{when x is even} \end{bmatrix}$ , then:

(a). f (x) is bijective (b).f (x) is injective but not surjective (c).f (x) is not injective but surjective (d).f (x) is neither injective nor subjective

A. f (x) is bijective

B. f (x) is injective but not surjective

C. f (x) is not injective but surjective

D. f (x) is neither injective nor subjective

### Answer: A



**31.** Let 
$$g(x)$$
 be the inverse of  $f(x)=rac{2^{x+1}-2^{1-x}}{2^x+2^{-x}}$  then g (x) be :

A. 
$$\frac{1}{2}\log_2\left(\frac{2+x}{2-x}\right)$$
  
B. 
$$-\frac{1}{2}\log_2\left(\frac{2+x}{2-x}\right)$$
  
C. 
$$\log_2\left(\frac{2+x}{2-x}\right)$$
  
D. 
$$\log_2\left(\frac{2-x}{2+x}\right)$$

### Answer: C



**32.** Which of the following is the graph of the curve  $\sqrt{|y|} = x$  is ?











## Answer: B

**33.** Domain of  $f(x) = \log_{(x)} \left(9 - x^2 
ight)$  is :

A.  $\{1, 2\}$ B.  $(-\infty, 2)$ C.  $(-\infty, \log_2 5]$ D.  $[\log)_2 5, 3]$ 

### Answer: C

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**34.** if  $e^x + e^{f(x)} = e$  then for f(x)

- A. Domain is  $(\,-\infty,1)$
- B. Range is  $(-\infty, 1]$
- C. Domain is  $(\,-\infty,0]$
- D. Range is  $(-\infty, 0]$

### Answer: A



**35.** A lion moves in the region given by the graph y - |y| - x + |x| = 0. curve a person can move so that he does not encounter lion -

A. 
$$y=x^2$$
  
B.  $y=sgnig(-e^2ig)$   
C.  $y=\log_{1/3}x$   
D.  $y=-(m+|x|), m>3$ 

#### Answer: D



36. If  $\left|f(x)+6-x^2
ight|=\left|f(x)
ight|+\left|4-x^2
ight|+2$ , then f(x) is necessarily

### non-negaive for

A. 
$$x \in [-2, 2]$$
  
B.  $xn(-\infty, -2) \cup (2, \infty)$   
C.  $x \in [-\sqrt{6}, \sqrt{6}]$   
D.  $x \in [-5, -2] \cup [2, 5]$ 

#### Answer: A



**37.** Let  $f(x) = \cos(px) + \sin x$  be periodic, then p must be : a) Positive real number b) Negative real number c) Rational d) Prime

A. Positive real number

B. Negative real number

C. Rational

D. Prime

Answer: C

**38.** The domain of f(x)is(0,1) .Then the domain of  $(f(e^x) + f(1n|x|)$  is

$$(a)(\,-1,e)$$
 (b)  $(1,e)$  (c)  $(\,-e,\,-1)$  (d) $(\,-e,1)$ 

A.  $\left(\frac{1}{e}, 1\right)$ B. (-e, 1)C.  $\left(-1, -\frac{1}{e}\right)$ D.  $(-e, -1) \cup (1, e)$ 

#### Answer: B

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**39.** Let  $A = \{1, 2, 3, 4\}$  and  $f: A \to A$  satisfy f(1) = 2, f(2) = 3, f(3) = 4, f(4) = 1. Suppose  $g: A \to A$  satisfies g(1) = 3 and fog = gof, then g = A.  $\{(1, 3), (2, 1), (3, 2), (4, 4)\}$ B.  $\{(1, 3), (2, 4), (3, 1), (4, 2)\}$ C.  $\{(1, 3), (2, 2), (3, 4), (4, 3)\}$ D.  $\{(1, 3), (2, 4), (3, 2), (4, 1)\}$ 

#### Answer: B

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**40.** Number of solutions of the equation,  $[y + [y]] = 2\cos x$  is: (where  $y = 1/3)[\sin x + [\sin x + [\sin x]]]$  and [] = greatest integer function) 0 (b) 1 (c) 2 (d)  $\infty$ 

A. 0

B. 1

C. 2

D. Infinite

### Answer: A



**41.** The function 
$$f(x)=iggl\{rac{(x^{2n})}{(x^{2n}sgnx)^{2n+1}}iggl(rac{e^{rac{1}{x}}-e^{-rac{1}{x}}}{e^{rac{1}{x}}+e^{-rac{1}{x}}}iggr)x
eq 0n\in N$$
 is:

A. Odd function

B. Even function

C. Neither odd nor even function

D. Constant function

### Answer: B

**42.** 
$$f(1) = 1$$
 and  $f(n) = 2\sum_{r=1}^{n-1} f(r)$ . Then  $\sum_{n=1}^{m} f(n)$  is equal to (A) $3^m - 1$ 

(B) $3^m$ 

(C) $3^{m-1}$ 

(D)none of these

A. 3 ^(m) -1

 $\mathsf{B.}\, 3^m$ 

 $\mathsf{C.}\, 3^{m-1}$ 

 $D. no \neq of these$ 

### Answer: C

**43.** Let 
$$f(x) = rac{x}{\sqrt{1+x^2}}$$
 then ubrace(fo fo fo .....of)(x)`is :

A. 
$$rac{x}{\sqrt{1+ig(\sum_{r=1}^n rig)x^2}}$$
  
B.  $rac{x}{\sqrt{1+ig(\sum_{r=1}^n 1ig)x^2}}$   
C.  $ig(rac{x}{\sqrt{1+x^2}}ig)^n$ 

D. 
$$rac{n\pi}{\sqrt{1+\pi x^2}}$$

### Answer: B



**44.** Let  $f \colon R \to R$ , then  $f(x) = 2x + |\cos x|$  is:

(a).One-one into (b).One-one and onto

(c).May-one and into (d).Many-one and onto

A. One-one into

B. One-one and onto

C. May-one and into

D. Many-one and onto

Answer: B

**45.** Let  $f \colon R o R$  be a function defined by  $f(x) = x^3 + x^2 + 3x + \sin x$ .

Then f is

A. One-one end into

B. One-one and onto

C. Many-one and into

D. many-one and onto

### Answer: B

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**46.** If  $f(x) = \{x\} + \{x+1\} + \{x+2\}$ ..... $\{x+99\}$ , then the value of  $\left[f(\sqrt{2})\right]$  is, where (.) denotes fractional part function & [.] denotes the greatest integer function

A. 5050

B. 4950

C. 41

D. 14

### Answer: C

47. If 
$$|\cot x + \cos ecx| = |\cot x| + |\cos ecx|, x \in [0, 2\pi], ext{ then complete}$$
 set of values of x is :

A. 
$$[0, \pi]$$
  
B.  $\left(0, \frac{\pi}{2}\right]$   
C.  $\left(0, \frac{\pi}{2}\right] \cup \left[\frac{3\pi}{2}, 2\pi\right)$   
D.  $\left(\pi, \frac{3\pi}{2}\right] \cup \left[\frac{7\pi}{4}, 2\pi\right]$ 

## Answer: C

48. The funcrtin f(x) = 0 has eight distinvt real solution and f also satisfy f(4+x) = f(4-x). The sum of all the eight solution of f(x) = 0 is :

A. 12

B. 32

C. 16

D. 15

Answer: B

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49. Let f(x) polynomial of degree 5 with leading coefficient unity such that

f(1)=5, f(2)=4,f(3)=3,f(4)=2,f(5)=1, then f(6) is equal to

A. 0

B. 24

C. 120

D. 720

Answer: C

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50. Let  $f\colon A o B$  be a function such that  $f(x)=\sqrt{x-2}+\sqrt{4-x,}$  is

invertible, then which of the following is not possible ?

A. 
$$A = [3, 4]$$
  
B.  $A = [2, 3]$   
C.  $A = \left[2, 2\sqrt{3}
ight]$ 

 $\mathsf{D}.\left\{2,2\sqrt{2}\right]$ 

### Answer: C

**51.** Find the number of positive integral values of x satisfying  $\left[\frac{x}{9}\right] = \left[\frac{x}{11}\right]$  is where [.] -=Gl.F) (a). 21 (b). 22 (c). 23 (d). 24

A. 21

B. 22

C. 23

D. 24

#### Answer: D

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**52.** The domain of function  $f(x) = \log_{\left[x+\frac{1}{2}\right]} (2x^2 + x - 1)$ , where [.] denotes the greatest integer function is :

A.  $\left[\frac{3}{2}, \infty\right)$ B.  $(2, \infty)$ C.  $\left(-\frac{1}{2}, \infty\right) - \left\{\frac{1}{2}\right\}$ 

$$\mathsf{D}.\left(\frac{1}{2},1\right)\cup(1,\infty)$$

### Answer: A



**53.** The solution set of the equation  $[x]^2 + [x + 1] - 3 = 0$ , where [.] represents greatest integeral function is :

- A.  $[\,-1,o)\cup[1,2)$ B.  $[\,-2,\,-1)\cup[1,2)$ C. [1,2]
- D.  $[-3, -2) \cup [2, 3)$

#### Answer: B
54. Which among the following relations is a function ?

A. 
$$x^2+y^2=r^2$$
  
B.  $rac{x^2}{a^2}+rac{y^2}{b^2}=r^2$   
C.  $y^2=4ax$   
D.  $x^2=dxy$ 

#### Answer: D

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55. A function  $f\colon R o R$  is defined as  $f(x)=3x^2+1.$  then  $f^{-1}(x)$  is :

A. 
$$rac{\sqrt{x-1}}{3}$$
  
B.  $\left(rac{1}{2}\sqrt{x}-1
ight)$ 

C.  $f^{-1}$  does not exist

D. 
$$\sqrt{rac{x-1}{3}}$$

# Answer: C



$$\begin{aligned} & \textbf{56. If } f(x) = \begin{cases} 2+x, \ x \geq 0 \\ 4-x, \ x < 0 \end{cases}, \text{ then } f(f(x)) \text{ is given by :} \\ & \textbf{A. } f(f(x)) = \begin{cases} 4+x, \ x \geq 0 \\ 6-x, \ x < 0 \end{cases} \\ & \textbf{B. } f(f(x)) = \begin{cases} 4+x, \ x \geq 0 \\ x, \ x < 0 \end{cases} \\ & \textbf{C. } f(f(x)) = \begin{cases} 4-x, \ x \geq 0 \\ x, \ x < 0 \end{cases} \\ & \textbf{D. } f(f(x)) = \begin{cases} 4-x, \ x \geq 0 \\ x+2x, \ x < 0 \end{cases} \end{aligned}$$

# Answer: A



57. The function  $f\!:\!R o R$  defined as  $f(x)=rac{3x^2+3x-4}{3+3x-4x^2}$  is :

A. One ot one buty not onto



- C. Both one to one and onto
- D. Neither one to one nor onto

#### Answer: B

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**58.** The number of solutions of the equation  $e^x - \log(x) = 0$  is :

A. 0

B. 1

C. 2

D. 5

Answer: B

**59.** If complete solution set of  $e^{-x} \leq 4-x$  is [lpha, eta] then [lpha]+[eta] is

equal to : (where [.] denotes greatest integer function )

A. 0 B. 2 C. 1 D. 4

# Answer: C

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60. Range of 
$$f(x) = \sqrt{\sin(\log_7(\cos(\sin x)))}$$
 is:

A. [0, 1]

B.  $\{0, 1\}$ 

 $\mathsf{C}.\left\{0\right\}$ 

D. [1, 7]

# Answer: C



**61.** If domain of y=f(x) is  $x\in [-3,2],$  then domain of  $y=f(\mid \mid x]\mid$  ):

(where[.] denotes greatest integer function)

A. [-3, 2]B. [-2, 3]C. [-3, 3]D. [-2, 3]

#### Answer: B

62. Range of the function 
$$f(x) = \cot^{-1}\{-x\} + \sin^{-1}\{x\} + \cos^{-1}\{x\}$$
, where {.} denotes

# fractional part function:

A. 
$$\left(\frac{3\pi}{4},\pi\right)$$
  
B.  $\left[\frac{3\pi}{4},\pi\right)$   
C.  $\left[\frac{3\pi}{4},\pi\right]$   
D.  $\left(\frac{3\pi}{4},\pi\right]$ 

### Answer: D

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$$f{:}R-\left\{rac{3}{2}
ight\}
ightarrow R, f(x)=rac{3x+5}{2x-3}. \ Let f_1(x)=f(x), f_n(x)=f(f_{n-1}(x))$$

Let

for  $\pi\geq 2, n\in N,$  then  $f_{2008}(x)+f_{2009}(x)=$ 

A. 
$$rac{2x^2+5}{2x-3}$$

B. 
$$\frac{x^2 + 5}{2x - 3}$$
  
C.  $\frac{2x^2 - 5}{2x - 3}$   
D.  $\frac{x^2 - 5}{2x - 3}$ 

### Answer: A

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**64.** Find the range of the function  $f(x) = rac{ig(1+x+x^2ig)ig(1+x^4ig)}{x^3}$ 

- A.  $[0,\infty]$
- $\mathsf{B}.\left[2,\infty\right]$
- $\mathsf{C}.\,[4,\,\infty]$
- D.  $[6,\infty]$

# Answer: D

65. The function  $f:(-\infty, -1)\overrightarrow{0, e^5}$  defined by  $f(x) = e^x \hat{} (3 - 3x + 2)$  is many one and onto many one and into one-one and into A. Many one and onto

B. Many one and into

C. One to one and onto

D. One to one and into

# Answer: A

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66. If 
$$f(x)=\sin(\log)_eigg\{rac{\sqrt{4-x^2}}{1-x}igg\}$$
 , th

, then the domain of 
$$f(x)$$
 is \_\_\_

and its range is \_\_\_\_\_.

 $\mathsf{A}.\,[\,-1,1]$ 

B.[0,1]

 $\mathsf{C}.\,[\,-1,1)$ 

D. None of these

Answer: A

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67. Set of values of 'a' for which the function  $f\colon R o R,\,\,$  given by  $f(x)=x^3+(a+2)x^2+3ax+10$  is one-one is given by :

A. 
$$(\,-\infty,1]\cup[4,\infty)$$

B.[1, 4]

- $\mathsf{C}.\left[1,\infty\right]$
- D.  $[-\infty,4]$

#### Answer: B

**68.** If the range of the function  $F(x) = \tan^{-1}(3x^2 + bx + c)$  is  $\left[0, \frac{\pi}{2}\right)$ ; (domain in R) then :

A.  $b^2 = 3c$ B.  $b^2 = 4c$ C.  $b^2 = 12c$ 

D.  $b^2=8c$ 

## Answer: C

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69. Let  $f(x) = \sin^{-1}x - \cos^{-1}x$ , then the set of values of k for which of |f(x)| = k has exactly two distinct solutions is :

A.  $\left(0, \frac{\pi}{2}\right]$ B.  $\left(0, \frac{\pi}{2}\right]$ C.  $\left[\frac{\pi}{2}, \frac{3\pi}{2}\right)$ 

D. 
$$\left[\pi, \frac{3\pi}{2}\right]$$

# Answer: A



70.Let
$$f:R o R$$
isdefinedby $f(x) = \begin{cases} (x+1)^3 & x \leq 1 \\ \ln x + (b^2 - 3b + 10) & x > 1 \end{cases}$  If f (x) is invertible, then the

set of all values of 'b' is :

A.  $\{1,\,2\}$ 

 $\mathsf{B.}\,\phi$ 

 $C. \{2, 5\}$ 

D. None of these

# Answer: A

71. If f(x) is continuous such that  $|f(x)| \le 1, \ \forall x \in R ext{ and } g(x) = rac{e^{f(x)} - e^{-|f(x)|}}{e^{f(x)} + e^{-|f(x)|}},$  then range of g(x) is

A. 
$$[0, 1]$$
  
B.  $\left[0, \frac{e^2 + 1}{e^2 - 1}\right]$   
C.  $\left[0, \frac{e^2 - 1}{e^2 + 1}\right]$   
D.  $\left[\frac{e^2 + 1}{e^2 + 1}, 0\right]$ 

#### Answer: D



72. Consider all function  $f: \{1, 2, 3, 4\} \rightarrow \{1, 2, 3, 4\}$  which are one-one, onto and satisfy the following property :

If f(k) is odd then f(k+1) is even,K = 1, 2, 3. The number of such function is :

A. 4		
B. 8		
C. 12		
D. 16		

# Answer: C

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73. Consider the function  $f\colon R-\{1\} o R-\{2\}$  given by  $f\{x\}=rac{2x}{x-1}.$  Then

A. f is one-one but not onto

B. f is onto but not one-one

C. f is neither one-one nor onto

D. f is one-one and onto

Answer: D

74. If rang of fraction f(x) whose domain is set of all real numbers is [-2,4], then range of function $g(x)=rac{1}{2}f(2x+1)$  is equal to :

- A. [-2, 4]
- $\mathsf{B}.\,[\,-1,\,2]$
- $\mathsf{C}.[-3,9]$
- D.[-2,2]

### Answer: B

:

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75. Let 
$$f: R \to ext{ and } f(x) = rac{x \left(x^4 + 1 
ight) (x+1) + x^4 + 2}{x^2 + x + 1}, ext{ then } f(x) ext{ is }$$

A. one-one, inot

B. Many -one onto

C. One-one, onto

D. Mny one, into

## Answer: D

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$$f(x) = \left\{egin{array}{ccc} |x| & 0 \leq x < 1 \ |x-1| + |x-2| & 1 \leq x < 2 \ |x-3| & 2 \leq x < 3 \end{array}
ight.$$

The range of function  $g(x) = \sin(7(f(x)))$  is :

A. 
$$[0, 1]$$
  
B.  $[-1, 0]$   
C.  $\left[-\frac{1}{2}, \frac{1}{2}\right]$   
D.  $[-1, 1]$ 

## Answer: D



77. If 
$$\left[x
ight]^2-7[x]+10<0 ext{ and } 4[y]^2-16[y]+7<0, ext{ then } \left[x+y
ight]$$

cannot be ([.]` denotes greatest integer function):

A. 7

B. 8

C. 9

D. both (b) and (c)

#### Answer: C



78. Let  $f\colon R o R$  be a function defined by  $f(x)=rac{e^{\mid x\mid}-e^{-x}}{e^x+e^{-x}}$  . Then, f

is a bijection (b) f is an injection only (c) f is surjection on only (d) f is

neither an injection nor a surjection

- A. f (x) is many one, onto function
- B. f (x) is many one, into function
- C. f (x) is decreasing function  $\, orall \, n \in R$
- D. f(x) is bijective function

### Answer: B



```
79. The function f(x) satisfy the equation

f(1-x) + 2f(x) = 3x \forall x \in R, then f(0) =

A. -2

B. -1

C. 0

D. 1
```

### Answer: B



80. Let  $f:[0,5] \to [0,5)$  be an invertible function defined by  $f(x) = ax^2 + bx + C$ , where  $a, b, c \in R, abc \neq 0$ , then one of the root of the equation  $cx^2 + bx + a = 0$  is:

A. a B. b

C. c

 $\mathsf{D}.\,a+b+c$ 

Answer: A

**81.** Let  $f(x) = x^2$ ,  $\lambda x + \mu \cos x$ ,  $\lambda$  being an integer and  $\mu$  us a real number. The number of ordered pairs  $(\lambda, \mu)$  for which the equation f(x) = 0 and f(f(x)) = 0 have the same (non empty) set of real roots is:

- A. 2
- B. 3
- C. 1
- D. 6

# Answer: C

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82. Consider all function  $f: \{1, 2, 3, 4\} \rightarrow \{1, 2, 3, 4\}$  which are one-one, onto and satisfy the following property :

If f(k) is odd then f(k+1) is even, $K=1,\,2,\,3.$  The number of such

function is :

A. 4		
B. 8		
C. 12		
D. 16		

# Answer: C



83. Which of the following is closest to the graph of  $y = an(\sin x), x > 0$ ?







### Answer: B





A. f is one-one but not onto

B. f is onto but not one-one

C. f is one-one nor onto

D. f is both one-one and onto

Answer: D

85. If range of function f(x) whose domain is set of all real numbers is [-2,4], then range of function  $g(x)=rac{1}{2}f(2x+1)$  is equal to

- A. [-2, 4]
- $\mathsf{B}.\,[\,-1,\,.2]$
- $\mathsf{C}.\,[\,-3,\,9]$
- $\mathsf{D}.\,[\,-2,\,2]$

### Answer: B

:

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**86.** Let 
$$f: R \to \text{ and } f(x) = rac{x \left(x^4 + 1 
ight) (x + 1) + x^4 + 2}{x^2 + x + 1}, ext{ then } f(x) ext{ is }$$

# A. One-one, into

B. Many one, onto

C. One-one, onto

D. Many one, into

## Answer: D

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$$f(x) = \left\{egin{array}{ccc} |x| & 0 \leq x < 1 \ |x-1| + |x-2| & 1 \leq x < 2 \ |x-3| & 2 \leq x < 3 \end{array}
ight.$$

The range of function  $g(x) = \sin(7(f(x)))$  is :

A. 
$$[0, 1]$$
  
B.  $[-1, 0]$   
C.  $\left[-\frac{1}{2}, \frac{1}{2}\right]$   
D.  $[-1, 1]$ 

# Answer: D



. **c** 

• •

88. Number of integral values of x in the domain of function 
$$f(x) = \sqrt{\ln(|\ln|x| + 1)} + \sqrt{7|x| - (|x|)^2 - 10}$$
 is equal to  
A. 5  
B. 6  
C. 7  
D. 8

- --- **- -** ---

±1. .

- **C** 

**C**....

#### Answer: B



89. The number of integral ordered pair (x,y) that satisfy the system of

equatin |x + y - 4| = 5 and |x - 3| + |y - 1| = 5 is/are:

A. 2	
B. 4	
C. 6	
D. 12	

## Answer: D

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90. 
$$f\!:\!R o R$$
, where  $f(x)=rac{x^2+ax+1}{x^2+x+1}$  Complete set of values of 'a'

such that f(x) is onto, is

A.  $(\,-\infty,\infty)$ 

B.  $(-\infty, 0)$ 

 $\mathsf{C}.\left(0,\infty
ight)$ 

D. Empty set

#### Answer: D

**91.** If A={1,2,3,4} and f : A->A, then total number of invertible functions, 'f', such that  $f(2) \neq 2$ ,  $f(4) \neq 4$ , f(1) = 1 is equal to:

A. 1	
B. 2	
C. 3	
D. 4	

# Answer: C

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92. The domian of definition of  $f(x) = \log_{\left(x^2 - x + 1
ight)}\left(2x^2 - 7x + 9
ight)$  is :

A. R

B.  $R - \{0\}$ 

C.  $R - \{0, 1\}$ 

 $\mathsf{D}.\,R-\{1\}$ 

Answer: C

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**93.** Let 
$$f(x) = x^2 - 2x - 3, x \ge 1$$
 and  $g(x) = 1 + \sqrt{x+4}, x \ge -4$ 

then the number of real solution os equation f(x)=g(x) is/are

A. 0

B. 1

C. 2

D. 4

## Answer: B

1. f (x) is an even periodic function with period 10 in  

$$[0, 5], f(x) = \begin{cases} 2x & 0 \le x < 2\\ 3x^2 - 8 & 2 \le x < 4 \\ 10x & 4 \le x \le 5 \end{cases}$$
A.  $f(-4) = 40$   
B.  $\frac{f(-13) - f(11)}{f(13) + f(-11)} = \frac{17}{21}$   
C.  $f(5)$  is not defined  
D. Range of  $f(x)$  is  $[0, 50]$ 

#### Answer: A::B::D

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2. Let  $f(x) = \left| \left| x^2 - 4x + 3 \right| - 2 \right|$ . Which of the following is/are correct ?

A. f(x) = m has exactly two real solutios of different sign  $\, orall \, m > 2$ 

B. f(x)=m has exactly two real solution  $\,orall\,m\in(2,\infty)\cup\{0\}$ 

C. f(x) = m has no solutions  $\forall m < 0$ 

D. f(x) = m has four distinct real solution  $\forall m \in (0, 1)$ 

#### Answer: A::B::C::D

Watch Video Solution  $(1 - \tan^2(x/2))$ 

3. Let 
$$f(x) = \cos^{-1} igg( rac{1 - an^2(x/2)}{1 + an^2(x/2)} igg)$$
 . Solve for f(x).

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4.  $|\log_e |x|| = |k-1| - 3$  has four distict roots then k satisfies : (where $|x| < d^2, x 
eq 0$ )

A. (-4, -2)

**B**. (4, 6)

C. 
$$\left( e^{-1}, e 
ight)$$
  
D.  $\left( d^{-2}, e^{-1} 
ight)$ 

Answer: A::B

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5. Which of the following functions are defined for all  $x \in R$ ? (Where[. ] =

denotes greatest integer function)

A. 
$$f(x) = \sin[x] + \cos[x]$$
  
B.  $f(x) = \sec^{-1}(1 + \sin^2 x)$   
C.  $f(x) = \sqrt{\frac{9}{8} + \cos x + \cos 2x}$   
D.  $f(x) = \tan(ln(1 + |x|))$ 

### Answer: A::B::C

6. Let  $f(x)=egin{cases} x^2&0< x<2\\ 2x-3&2\leq x<3 \ ext{then the tuue equations:}\\ x+2&x\geq 3 \end{cases}$ 

A. 
$$f\left(f\left(f\left(\frac{3}{2}\right)\right) = f\left(\frac{3}{2}\right)$$
  
B.  $1 + f\left(f\left(f\left(\frac{5}{2}\right)\right)\right) = f\left(\frac{5}{2}\right)$ 

$$\mathsf{C}.\,f(f(f(2)))=f(1)$$

D. 
$$f(f(f(....,f(4))...)) = 2012$$

#### Answer: A::B::C

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7. Let 
$$f: \left[ -\frac{\pi}{3}, \frac{2\pi}{3} \right] \to [0, 4]$$
 be a function defined as  
 $f(x) = \sqrt{3} \sin x - \cos x + 2$ . Then  $f^{-1}(x)$  is given by  
 $(a) \sin^{-1}\left(\frac{x-2}{2}\right) - \frac{\pi}{6}$   
 $(b) \sin^{-1}\left(\frac{x-2}{2}\right) + \frac{\pi}{6}$   
 $(c) \frac{2\pi}{3} + \cos^{-1}\left(\frac{x-2}{2}\right)$ 

(d) none of these

A. 
$$f^{-1}(1) = rac{4\pi}{3}$$
  
B.  $f^{-1}(1) = \pi$   
C.  $f^{-1}(2) = rac{5\pi}{6}$   
D.  $f^{-1}(2) = rac{7\pi}{6}$ 

#### Answer: A::D



8. Let f(x) be invertible function and let  $f^{-1}(x)$  be is inverse. Let equation  $f(f^{-1}(x)) = f^{-1}(x)$  has two real roots  $\alpha$  and  $\beta$  (with in domain of f(x)), then :

A. f(x) = x also have same two rreal roots

B.  $f^{-1}(x) = x$  also have same two real roots

C.  $f(x) = f^{-1}(x)$  also have same two real roots

D. Area of triangle formed by  $(0, 0), (\alpha, f(\alpha)), \text{ and } (\beta, f(\beta))$  is 1

unit

# Answer: A::B::C



**9.** In function 
$$f(x) = \cos^{-1} x + \cos^{-1} \left( \frac{x}{2} + \frac{\sqrt{3 - 3x^2}}{2} \right)$$
, then Range  
of  $f(x)$  is  $\left[ \frac{\pi}{3}, \frac{10\pi}{3} \right] \right]$  Range of  $f(x)$  is  $\left[ \frac{\pi}{3}, 5\pi \right] f(x)$  is one-one for  
 $x \in \left[ -1, \frac{1}{2} \right] f(x)$  is one-one for  $x \in \left[ \frac{1}{2}, 1 \right]$   
A. Range of  $f(x)is \left[ \frac{\pi}{3}, \frac{10\pi}{3} \right]$   
B. Rang  $f(x)is \left[ \frac{\pi}{3}, \frac{5\pi}{3} \right]$   
C. f (x) is one-one for  $x \in \left[ -1, \frac{1}{2} \right]$   
D. f (x) is one-one for  $x \in \left[ \frac{1}{2}, 1 \right]$ 

# Answer: B::C

10. Which option (s) is/are ture ?

A. 
$$f: R \to R, f(x) = e^{|x|} - e^{-x}$$
 is many-one into function  
B.  $f: R \to R, f(x) = 2x + |\sin x|$  is one-one onto  
C.  $f: R \to R, f(x) = \frac{x^2 + 4x + 30}{x^2 - 8x + 18}$  is many-one onto  
D.  $f: R \to R, f(x) = \frac{2x^2 - x + 5}{7x^2 + 2x + 10}$  is many-one into

#### Answer: A::B::D

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11. If  $f(x) = \left[ \frac{\ln(x)}{e} \right] + \left[ \frac{\ln(e)}{x} \right]$ , where [.] denotes greatest interger

function, the which of the following are ture ?

A. range of 
$$h(x)is\{-1,0\}$$

B. If h(x) = -1, then x can be rational as well as irractional

C. If  $h(x)=\,-\,1,\,$  then x can be rational as well as irrational

D. h(x) is periodic function

# Answer: A::C

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12. If 
$$f(x) = egin{cases} x^3 & x = Q \ -x^3 & x 
eq Q \end{pmatrix}$$
, then :

A. f (x) is periodic

B.f (x) is many-one

C. f (x) is one-one

D. range of the function is R

# Answer: C::D

13. Let f(x) be a real valued function such that  $f(0) = \frac{1}{2}$  and  $f(x+y)=f(x)f(a-y)+f(y)f(a-x), \forall x, y \in R$ , then for some real a,

A. f (x) is perodic function

B. f (x) is a constant function

C. 
$$f(x)=rac{1}{2}$$
  
D.  $f(x)=rac{\cos x}{2}$ 

# Answer: A::B::C

**14.** 
$$f(x)$$
 is an even periodic function with period 10. In  
 $[0,5]f(x) = \begin{cases} 2x & 0 \le x < 2\\ 3x^2 - 8 & 2 \le x < 4 \end{cases}$  Then :  
 $10x & 4 \le x \le 5$   
A  $f(-4) = 40$ 

B. 
$$rac{f(-13)-x(11)}{f(13)+f(-11)}=rac{17}{21}$$
C. f(5) is not defined

D. Range of f(x) is [0, 50]

Answer: A::B::D

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**15.** For the equation  $\frac{e^{-x}}{x+1}$  which of the following statement(s) is/are correct ?

A. when  $\lambda \in (0,\infty)$  equation has 2 real and distinct roots

B. when  $\lambda \in ig(-\infty, \ -e^2ig)$  equation has 2 real and distinct roots

C. when  $\lambda \in (0,\infty)$  equatio has 1 real root

D. when  $\lambda \in (-e,0)$  equation has no real root

#### Answer: B::C::D

**16.** For  $x \in R^+$ , if  $x, [x], \{x\}$  are in harmonic progression then the value of x can not be equal to (where [\*] denotes greatest integer function, {\*} denotes fractional part function)

A. 
$$\frac{1}{\sqrt{2}} \tan \frac{\pi}{8}$$
  
B. 
$$\frac{1}{\sqrt{2}} \cot \frac{\pi}{8}$$
  
C. 
$$\frac{1}{\sqrt{2}} \tan \frac{\pi}{12}$$
  
D. 
$$\frac{1}{\sqrt{2}} \cot \frac{\pi}{12}$$

### Answer: A::C::D

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17. The equation  $| \mid x-1 \mid +a \mid = 4$  can have real solutions for x if a

belongs to the interval.



**18.** If the domain of  $f(x) = \frac{1}{\pi} \cos^{-1} \left[ \log_3 \left( \frac{x^2}{3} \right) \right]$  where, x > 0 is [a,b] and the range of f(x) is [c,d], then :

A. a,b are the roots of the equation  $x^4 - 3x^4 - 3xc^3 - x + 3 = 0$ 

B. a,b are the roots of the equatin  $x^4-x^3+x^2-2x+1=0$ 

 $C. a^3 + d^3 = 1$ 

D. 
$$a^2 + b^2 + c^2 = 11$$

#### Answer: A::D

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**19.** The number of real values of x satisfying the equation  $\left[\frac{2x+1}{3}\right] + \left[\frac{4x+5}{6}\right] = \frac{3x-1}{2}$  are greater than or equal to {[\*] denotes greatest integer function}:

A. 7

B. 8

C. 9

D. 10

### Answer: A::B::C

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20. Let 
$$f\Big(x=\sin^6\Big(rac{x}{4}\Big)+\cos^6\Big(rac{x}{4}\Big).$$
  $Iff^n(x)$  denotes  $n^{th}$  derivative of f

evaluated at x. Then which of the following hold ?

A. 
$$f^{2014}(0) = -\frac{3}{8}$$
  
B.  $f^{2015}(0) = \frac{3}{8}$   
C.  $f^{2010}\left(\frac{\pi}{2}\right) = 0$   
D.  $f^{2011}\left(\frac{\pi}{2}\right) = \frac{3}{8}$ 

### Answer: A::C::D

21. Which of the following is (are) incorrect ?

A. If 
$$f(x) = \sin x$$
 and  $g(x) = \sin x$  then range of  $g(f(x))$  is $[-1,1]$ 

Β.

C. If 
$$f(x) = \left(2011 - x^{2012}
ight)^{rac{1}{2012}}$$
 then  $f(f(2)) = rac{1}{2}$ 

D. The function  $f\!:\!R o R$  defined as  $f(x)=rac{x^2+4x+30}{x^2-8x+18}$  is not

surjective.

### Answer: A::B

**22.** If [x] denotes the integral part of x for real x, and 
$$S = \left[\frac{1}{4}\right] + \left[\frac{1}{4} + \frac{1}{200}\right] + \left[\frac{1}{4} + \frac{1}{100}\right] + \left[\frac{1}{4} + \frac{3}{200}\right] \dots + \left[\frac{1}{4} + \frac{199}{200}\right]$$
then S is

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23. Let 
$$f(x) = \log_{\{x\}} [x]$$
  
 $g(x) = \log_{\{x\}} - \{x\}$   
 $h(x) \log_{\{x\}} \{x\}$ 

where  $[], \{\}$  denotes the greatest integer function and fractional part function respectively.

For  $x \in (1,5) thef(x)$  is not defined at how many points :

A. 5 B. 4 C. 3

D. 2

Answer: C



**Comprehension Type Problems** 

1. Let 
$$f(x) = \log_{\{x\}} [x]$$
 $g(x) = \log_{\{x\}} - \{x\}$  $h(x) \log_{\{x\}} \{x\}$ 

where  $[], \{\}$  denotes the greatest integer function and fractional part function respectively.

If  $A=\{x\!:\!x\in ext{ domine of } f(x)))$  and  $B\{x\!:\!x ext{ domine of } g(x)\}$  then  $orall x\in (1,5), A-B$  will be :

A. (2, 3)

- B.(1,3)
- C.(1,2)

D. None of these

### Answer: D

2. Let 
$$f(x) = \log_{\{x\}} [x]$$
  
 $g(x) = \log_{\{x\}} - \{x\}$   
 $h(x) = \log_{[x]} \{x\}$ 

where  $[], \{\}$  denotes the greatest integer function and fractional part function respectively.

Domine of h(x) is :

A.  $[2,\infty)$ 

 $\mathsf{B}.\left[1,\infty\right)$ 

 $\mathsf{C}.\left[2,\infty
ight)-\left\{I
ight\}$ 

$$\mathsf{D}.\,R^+-\{I\}$$

Answer: C



**3.**  $\theta$  is said to be well behaved if it lies in interval  $\left[0, \frac{\pi}{2}\right]$ . They are intelligent if they make domain of f + g and g equal. The value of  $\theta$  for

which  $h(\theta)$  is defined are handosome. Let

$$f(x) = \sqrt{ heta x^2 - 2( heta^2 - 3)x - 12 heta,} g(x) = \ln(x^2 - 49),$$
 $h( heta) \ln \left[ \int_0^ heta 4 \cos^2 t dt - heta^2 
ight], ext{ where } heta ext{ is in radians.}$ 

Complete set of vlaues of  $\theta$  which are well behaved as well as intellignent

is:

A. 
$$\left[\frac{3}{4}, \frac{\pi}{2}\right]$$
  
B.  $\left[\frac{3}{5}, \frac{7}{8}\right]$   
C.  $\left[\frac{5}{6}, \frac{\pi}{2}\right]$   
D.  $\left[\frac{6}{7}, \frac{\pi}{2}\right]$ 

### Answer: D



**4.**  $\theta$  is said to be well behaved if it lies in interval  $\left[0, \frac{\pi}{2}\right]$ . They are intelligent if they make domain of f + g and g equal. The value of  $\theta$  for which  $h(\theta)$  is defined are handosome. Let

$$f(x) = \sqrt{ heta x^2 - 2( heta^2 - 3)x - 12 heta,} g(x) = \ln(x^2 - 49),$$
  
 $h( heta) \ln \left[ \int_0^ heta 4 \cos^2 t dt - heta^2 
ight], ext{ where } heta ext{ is in radians.}$ 

Complete set of vlaues of heta which are well behaved as well as intellignent

is:

A. 
$$\left[\frac{6}{7}, \frac{7}{2}\right]$$
  
B.  $\left(0, \frac{\pi}{3}\right]$   
C.  $\left[\frac{1}{4}, \frac{6}{7}\right]$   
D.  $\left[\frac{1}{2}, \frac{\pi}{2}\right]$ 

#### Answer: A

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**5.**  $\theta$  is said to be well behaved if it lies in interval  $\left[0, \frac{\pi}{2}\right]$ . They are intelligent if they make domain of f + g and g equal. The value of  $\theta$  for which  $h(\theta)$  is defined are handosome. Let

$$f(x)=\sqrt{ heta x^2-2ig( heta^2-3ig)x-12 heta,g(x)}=\lnig(x^2-49ig),$$

$$h( heta) {
m ln} iggl[ \int_0^ heta 4 \cos^2 t dt - heta^2 iggr], ext{ where } heta ext{ is in radians.}$$

Complete set of alues of  $\theta$  which are intelligent is :

A. 
$$\left(0, \frac{\pi}{2}\right]$$
  
B.  $\left[\frac{6}{7}, \frac{\pi}{2}\right]$   
C.  $\left[\frac{3}{4}, \frac{\pi}{2}\right]$   
D.  $\left[\frac{3}{5}, \frac{\pi}{2}\right]$ 

#### Answer: B

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**6.** Let  $f(x)=2-|x-3|, 1\leq x\leq 5 \,\, {
m and} \,\,$  for rest of the values f (x) can

be obtained by unsing the relation  $f(5x) = lpha f(x) \, orall x \in R.$ 

The vlaue of f (2007), taking  $lpha=5,\;$  is :

A. 1118

B. 2007

C. 1250

D. 132

Answer: A

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7. An even periodic functin  $f\colon R o R$  with period 4 is such that

$$f(x) = egin{bmatrix} \max \ . \ ig( ert x ert, x^2 ig) & 0 \leq x < 1 \ x & 1 \leq x \leq 2 \ \end{pmatrix}$$

The value of  $\{f(5.12)\}$  (where  $\{.\}$  denotes fractional part function), is :

A.  $\{f(3.26)\}$ B.  $\{f(7.88)\}$ C.  $\{f(2.12)\}$ D.  $\{f(5.88)\}$ 

Answer: B

**8.** An even periodic functin  $f \colon R o R$  with period 4 is such that

$$f(x) = egin{bmatrix} \max \ . \ ig(|x|, x^2ig) & 0 \leq x < 1 \ x & 1 \leq x \leq 2 \end{cases}$$

The number of solution of  $f(x)|3\sin x|$  for  $x\in(-6,6)$  are :

. .

### Answer: C

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9. Let 
$$f(x)=rac{2|x|-1}{x-3}$$

Range of f(x):

A.  $R-\{3\}$ 

B. 
$$\left(-\infty, \frac{1}{3}\right] \cup (2, \infty)$$
  
C.  $\left(-2, \frac{1}{3}\right]$  uu (2,00)`

D. R

### Answer: B

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10. Let 
$$f(x)=rac{2|x|-1}{x-3}$$

Range of the values of 'k' for which f(x) = k has exactly two distinct solutions:

A.  $\left(-2, \frac{1}{3}\right)$ B. (-2, 1]C.  $\left(0, \frac{2}{3}\right]$ D.  $(-\infty, -2)$ 

### Answer: A

11. Let f(x) be a continuous function (define for all x) which satisfies  $f^3(x) - 5f^2(x) + 10f(x) - 12 \ge 0, f^2(x) + 3 \ge 0$  and  $f^2(x) - 5f(x) + 4$ If distinct positive number  $b_1, b_2$  and  $b_3$  ar in G.P. then  $f(1) + \ln b_1), f(2) + \ln b_2, f(3) + \ln b_3$  are in :

A. A.P.

B. G.P.

C. H. P.

D. A. G. P.

Answer: A



12. Let f(x) be a continuous function (define for all x) which satisfies  $f^3(x)-5f^2(x)+10f(x)-12\geq 0, f^2(x)+3\geq 0$  and  $f^2(x)-5f(x)+10f(x)-12\geq 0$ 

The equation of tangent that can be drawn from (2,0) on the curve $y=x^2f(\sin x)$  is :

A. y = 24(x + 2)

B. y = 12(x + 2)

C. y = 24(x - 2)

D. 
$$y = 12(x - 2)$$

### Answer: C

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**13.** Let 
$$f:[2,\infty) \to \{1,\infty)$$
 defined by  $f(x) = 2^{x^4-4x^3}$  and  $g:\left[\frac{\pi}{2},\pi\right] \to A$  defined by  $g(x) = \frac{\sin x + 4}{\sin x - 2}$  be two invertible functions, then

The set "A" equals to

A. [5, 2]

B.[-2,5]

 $\mathsf{C}.\,[\,-5,\,2]$ 

D. [-5, -2]

Answer: D

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**Matching Type Problems** 

1. If  $x, y, z \in R$  satisfies the system of equations  $x + (y) + (s) = 12.7, [x] + \{y\} + z = 4.1$  and  $\{x\} + y + [z] = 2$ where  $\{.\}$  and [.] denotes the fractional and integral parts respectively) then match the following

	Column-I		Column-li	
(A)	${x} + {y} =$	<b>(P</b> )	7.7	
<b>(B</b> )	[z] + [x] =	(Q)	1.1	
(C)	$x + \{z\} =$	(R)	1	
(D)	$z + [y] - \{x\} =$	(\$)	3	
	Marine and the second	(T)	4	



**2.** Given the graph of y = f(x)







	Column-l		Column-li
(A)	If $ x^2 - x  \ge x^2 + x$ , then complete set of values of x is	(P)	(0,∞)
<b>(B)</b>	If $ x+y  > x-y$ , where $x > 0$ , then complete set of values of y is	(Q)	(–∞, 0]
(C)	If $\log_2 x \ge \log_2(x^2)$ , then complete set of values of x is	(R)	[−1,∞)

4.

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6. Let 
$$f(x) = egin{cases} 1+x, & 0 \leq x \leq 2 \ 3-x, & 2 < x \leq 3 \end{cases}$$

find (fof) (x).

**1.** Let f(x) be a polynomial of degree 6 with leading coefficient 2009,Supposefurther,that

 $f(1),\ =1,\,f(2)=3=5,\,f(4)=7,\,f(5)=9,\,f(2)=2,\,$  then the sum

of all the digits of f(6) is

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2. Let  $f(x) = x^3 - 3x + 1$ . Then number of different real solutions of f(f(x)) = 0

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3. If 
$$f(x+y+1) = \left\{\sqrt{f(x)} + \sqrt{f(y)}
ight\}^2$$
 and

 $f(0)=1\,orall x,y\in R,determ\in ef(n),n\in N_{1}$ 

**4.** If the domain of 
$$f(x)=\sqrt{12-3^x-3^{3-x}}+\sin^{-1}iggl(rac{2x}{3}iggr)is[a,b],$$

then  $a = \ldots$ 

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5. The number of elements in the range of the function :

$$y=\sin^{-1}igg[x^2+rac{5}{9}igg]+\cos^{-1}igg[x^2-rac{4}{9}igg]$$
 where [.] denotes the greatest

integer function is

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6. The number of integers in the range of function  $f(x) = [\sin x] + [\cos x] + [\sin x + \cos x]$  is (where [.]= denotes greatest integer function)

7. If P(x) is polynomial of degree 4 such than P(-1) = P(1) = 5 and P(-2) = P(0) = P(2) = 2 find the maximum vaue of P (x).

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8. The number of integral vlaue (s) of k for which the curve  

$$y = \sqrt{-x^2 - 2x}$$
 and  $x + y - k = 0$  intersect at 2 distinct points is/are  
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9. Let the solution set of the equation

 $\sqrt{\left[x + \left[\frac{x}{2}\right]\right] + \left[\sqrt{\left\{x\right\}} + \left[\frac{x}{3}\right]\right]} = 3$  is [a, b). Find the product ab. (where  $[\cdot]$  and  $\{\cdot\}$  denote greatest integer and fractional part function, respectively).

10. For the real number x, let  $f(x)=rac{1}{2011\sqrt{1-x^{2011}}}.$  Find the number of

real roots of the equation

$$f(f(....\,(f(x))....\,) = (\{-x\}$$

where f is applies 2013 times and {.} denotes fractional part function.

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11. Find the number of elements contained in the range of the function

$$f(x) = \Big[rac{x}{6}\Big] \Big[rac{-6}{x}\Big] orall x \in (0,30)] where [.]`$$
 denotes greatest integer

function)

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12. Let 
$$f(x, y) = x^2 - y^2$$
 and  $g(x, y) = 2xy$ . such that  $(f(x, y))^2 - (g(x, y))^2 = \frac{1}{2}$  and  $f(x, y)$ .  $G(x, y) = \frac{\sqrt{3}}{4}$  Find the number of ordered pairs  $(x, y)$ ?

13. Let  $f(x) = rac{x+5}{\sqrt{x^2+1}}, ext{ then the smallest integral value of k for which} f(x) \leq k orall x \in R$  is

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15. Let  $f(x) = x^2 - bx + c$ , b is an odd positive integer. Given that f(x) = 0 has two prime numbers an roots and b + c = 35. If the least value of  $f(x) \forall x \in Ris\lambda$ , then  $\left|\frac{\lambda}{3}\right|$  is equal to (where [.] denotes greatest integer functio)

16. Let f(x) be a continuous function such that f(0) = 1 and  $f(x) = f\left(\frac{x}{7}\right) = \frac{x}{7} \forall x \in R$ , then f(42) is Watch Video Solution

17. If 
$$x = 10 \sum_{r=3}^{100} rac{1}{(r^2-4)},$$
 then  $[x] =$ 

(where [.] denotes gratest integer function)

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**18.** Let f(x) = cx+d/ax+b. Then fof(x) = x provided that.

B. d=a

C. a=b=c=d=1

D. a=b=1

### Answer:



19. Let 
$$A = \{x \mid x^2 - 4x + 3 < 0, x \in R\}$$
  
 $B = \{x \mid 2^{1-x} + p \le 0; x^2 - 2(p+7)x + 5 \le 0\}$  If  $A \subset B$ , then the range of real number  $p \in [a, b]$  where, a,b are integers. Find the value of  $(b-a)$ .

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20. Let the maximum value of expression  $y=rac{x^4-x^2}{x^6+2x^3-1}$  for  $x>1israc{p}{q},$  where p and q are relatively prime natural numbers, then p+q=

**21.** If f(x) is an even function then find the number of distinct real

numbers x such that 
$$f(x) = f \bigg( rac{x+1}{x+2} \bigg).$$

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22. The least integral value of m, m  $\,\in R$  for which the range of function

 $f(x)=rac{x+m}{x^2+1}$  contains the interval [0,1] is :

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**23.** Let  $x_1, x_2, x_3$  satisfying the equation  $x^3 - x^2 + \beta x + \gamma = 0$  are in GP where  $(x_1, x_2, x_3 > 0)$ , then the maximum value of  $[\beta] + [\gamma] + 2$  is, [.] is greatest integer function.

**24.** Let  $A = \{1, 2, 3, 4\}$  and  $B = \{0, 1, 2, 3, 4, 5\}$ . If 'm' is the number of strictly increasing function f,  $f: A \to B$  and n is the number of onto functions  $g: B \to A$ . Then the last digit of n-m is.

25. The value of 
$$\sum_{r=1}^{1024} [\log_2 r]$$
 is equal to, ([.] denotes the greatest integer

function)

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26. Let 
$$f(x) = \frac{ax+b}{xc+d}$$
, where a,b,c d are non zero If  $f(7) = 7, f(11) = 11$  and  $f(f(x)) = x$  for all x expect  $-\frac{d}{c}$ . The

unique number which is not is the range of f is

**27.** It is pouring down rain and the amount of rain hitting point (x, y) is given by  $f(x, y) = |x^3 + 2x^2y - 5xy^2 - 6y^3|$ . If Mr. 'A' starts at (0, 0), find number of possible value (s) for 'm' such that y= mx is a line along which Mr.' A could walk without any rain falling on him.

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**28.** Let P (x) be a cubic polynomical with leading co-efficient unity. Let the remainder when P (x) is divided by  $x^2 - 5x + 6$  equals 2 times the remainder when P (x) is divided by  $x^2 - 5x + 4$ . If P(0) = 100, find the sum of the digits of P(5),

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**29.** Let  $f(x) = x^2 + 10x + 20$ . Find the number of real solution of the equation f(f(f(f(x)))) = 0



**31.** Polynomial P(x) contains only terms of aodd degree. when P(x) is divided by (x - 3), the ramainder is 6. If P(x) is divided by  $(x^2 - 9)$  then remainder is g(x). Then find the value of g(2).

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**32.** The equation  $2x^3 - 3x^2 + p = 0$  has three real roots. Then find the minimum value of p.

