



## MATHS

### BOOKS - SHRI BALAJI MATHS (ENGLISH)

#### LIMIT

#### Exercise Single Choice Problems

1.  $\lim_{x \rightarrow 0} \frac{\cos(\tan x) - \cos x}{x^4}$  is equal to

A.  $\frac{1}{6}$

B.  $-\frac{1}{3}$

C.  $-\frac{1}{6}$

D.  $\frac{1}{3}$

Answer: B



2. The value of  $\lim_{x \rightarrow 0} \frac{(\sin x - \tan x)^2 - (1 - \cos 2x)^4 + x^5}{7(\tan^{-1} x)^7 + (\sin^{-1} x)^6 + 3 \sin^5 x}$  equal to :

A. 0

B. 1

C. 2

D.  $\frac{1}{3}$

**Answer: D**

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3. Let  $a = \lim_{x \rightarrow 0} \frac{\ln(\cos 2x)}{3x^2}$ ,  $b = \lim_{x \rightarrow 0} \frac{\sin^2 2x}{x(1 - e^x)}$ ,  $c = \lim_{x \rightarrow 1} \frac{\sqrt{x} - x}{\ln x}$

A.  $a < b < c$

B.  $b < c < a$

C.  $a < c < b$

$$D. b < a < c$$

**Answer: D**



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4. If  $f(x) = \cot^{-1}\left(\frac{3x - x^3}{1 - 3x^2}\right)$  and  $g(x) = \cos^{-1}\left(\frac{1 - x^2}{1 + x^2}\right)$  then

$$\lim_{x \rightarrow a} \frac{f(x) - f(a)}{g(x) - g(a)}$$

A.  $\frac{3}{2(1 + a^2)}$

B.  $\frac{3}{2}$

C.  $\frac{-3}{2(1 + a^2)}$

D.  $-\frac{3}{2}$

**Answer: D**



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5.  $\lim_{x \rightarrow 0} \left( \frac{(1+x)^{\frac{2}{x}}}{e^2} \right)^{\frac{4}{\sin x}}$  is :

A.  $e^4$

B.  $e^{-4}$

C.  $e^8$

D.  $e^{-8}$

**Answer: B**



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6.  $\lim_{x \rightarrow \infty} \frac{3}{x} \left[ \frac{x}{4} \right] = \frac{p}{q}$  where  $[.]$  denotes greatest integer function, then  $p + q$  (where  $p, q$  are relative prime) is:

A. 2

B. 7

C. 5

**Answer: B**


7.  $f(x) = \frac{x^n + \left(\frac{\pi}{3}\right)^n}{x^{n-1} + \left(\frac{\pi}{3}\right)^{n-1}}$ , (n is an even number, then which of the

following is correct

A. If  $f, \left[\frac{\pi}{3}, \infty\right) \rightarrow \left[\frac{\pi}{3}, \infty\right)$ , then function is invertible

B.  $f(x) = f(-x)$  has infinite number of solutions

C.  $f(x) = |f(x)|$  has infinite number of solutions

D.  $f(x)$  is one-one function for all  $x \in \mathbb{R}$

**Answer: D**


8.  $\lim_{x \rightarrow 0} \frac{\sin(\pi \cos^2(\tan(\sin x)))}{x^2}$  is equal to

A.  $\pi$

B.  $\frac{\pi}{4}$

C.  $\frac{\pi}{2}$

D. none of these

**Answer: A**



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9.  $\lim_{x \rightarrow \frac{\pi}{3}} \frac{\sin\left(\frac{\pi}{3} - x\right)}{2 \cos x - 1}$  is equal to:

A.  $\frac{2}{\sqrt{3}}$

B.  $\frac{1}{\sqrt{3}}$

C.  $\sqrt{3}$

D.  $\frac{1}{2}$

**Answer: B**



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10.  $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\sin x}{\cos^{-1} \left[ \frac{1}{4} (3 \sin x - \sin 3x) \right]}$  where  $[\ ]$  denotes greatest integer

function id:

A.  $\frac{2}{\pi}$

B. 1

C.  $\frac{4}{\pi}$

D. does not exist

**Answer: A**



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11. Let  $f$  be a continuous function on  $\mathbb{R}$  such that

$$f\left(\frac{1}{4n}\right) = \frac{\sin e^n}{e^{n^2}} + \frac{n^2}{n^2 + 1}$$

Then the value of  $f(0)$  is

A. 1

B. 0

C. -1

D.  $\frac{1}{6}$

**Answer: A**



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12.  $\lim_{x \rightarrow 1^-} \frac{e^{\{x\}} - \{x\} - 1}{\{x\}^2}$  equal, where  $\{ \cdot \}$  is fractional part function

and  $I$  is an integer, to :

A.  $\frac{I}{2}$

B.  $e - 2$



C.  $I$

D. does not exist

**Answer: B**



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13.  $\lim_{x \rightarrow \infty} (e^{11x} - 7x)^{\frac{1}{3x}}$  is equal to :

A.  $\frac{11}{3}$

B.  $\frac{3}{11}$

C.  $e^{\frac{3}{11}}$

D.  $e^{\frac{11}{3}}$

**Answer: D**



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14. For a certain value of 'c'  $\lim_{x \rightarrow \infty} \left[ (x^5 + 7x^4 + 2)^c - x \right]$  is finite and non-zero. Then the value of limit is :

A.  $\frac{7}{5}$

B. 1

C.  $\frac{2}{5}$

D. None of these

**Answer: A**



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15. The integer  $n$  for which  $(\lim)_{x \rightarrow 0} \left( (\cos x - 1) \frac{\cos x - e^{\widehat{x}}}{x^n} \right)$  is finite nonzero number is \_\_\_\_\_

A. 1

B. 2

C. 3

D. 4

**Answer: C**



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16. The value of  $\lim_{x \rightarrow 0} \left( \frac{\sin x}{x} \right)^{\frac{1}{1 - \cos x}}$  :

A.  $e^{-1/3}$

B.  $e^{1/3}$

C.  $e^{-1/6}$

D.  $e^{1/6}$

**Answer: A**



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17. If  $\lim_{x \rightarrow \infty} (\sqrt{x^2 - x + 1} - ax - b) = 0$ , then for  $k \geq 2, (k \in N) \lim_{x \rightarrow \infty} \sec^{2n}(k! \pi b) =$

A. a

B.  $-a$

C.  $2a$

D. b

**Answer: A**



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18. If  $f$  is a positive function such that  $f(x + T) = f(x)(T > 0), \forall x \in R$ , then

$$\lim_{n \rightarrow \infty} n \left( \frac{f(x + T) + 2f(x + 2T) + \dots + nf(x + nT)}{f(x + T) + 4f(x + 4T) + \dots + n^2 f(x + n^2 T)} \right) =$$

A. 2

B.  $\frac{2}{3}$

C.  $\frac{3}{2}$

D. none of these

**Answer: C**



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19. Let  $f(x) = 3x^{10} - 7x^8 + 5x^6 - 21x^3 + 3x^2 - 7$ , then the value of

$$\lim_{h \rightarrow 0} \frac{f(1-h) - f(1)}{h^3 + 3h}$$

A.  $\frac{50}{3}$

B.  $\frac{22}{3}$

C. 3

D.  $\frac{53}{3}$

**Answer: C**



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20.  $\lim_{x \rightarrow 0} \left( \frac{\cos x - \sec x}{x^2(x+1)} \right) =$

A. 0

B.  $-\frac{1}{2}$

C. -1

D. -2

Answer: C



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21. Let  $f(x)$  be a continuous and differentiable function satisfying

$f(x+y) = f(x)f(y) \forall x, y \in R$  if  $f(x)$  can be expressed as

$f(x) = 1 + xP(x) + x^2Q(x)$  where

$\lim_{x \rightarrow 0} P(x) = a$  and  $\lim_{x \rightarrow 0} Q(x) = b$ , then  $f'(x)$  is equal to :

A.  $af(x)$

B.  $bf(x)$

C.  $(a + b)f(x)$

D.  $(a + 2b)f(x)$

**Answer: A**



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22. The value of  $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\left\{1 - \tan\left(\frac{x}{2}\right)\right\} \{1 - \sin x\}}{\left\{1 + \tan\left(\frac{x}{2}\right)\right\} (\pi - 2x)^3}$  equals

A. not exist

B.  $\frac{1}{8}$

C.  $\frac{1}{16}$

D.  $\frac{1}{32}$

**Answer: D**



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23.  $\lim_{x \rightarrow \infty} \left( \frac{x-3}{x+2} \right)^x$  is equal to

A.  $e$

B.  $e^{-1}$

C.  $e^{-5}$

D.  $e^5$

**Answer: C**



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24.  $\lim_{x \rightarrow \frac{\pi}{2}} (\cos x)^{\cos x}$  is :

A. 1

B. 0

C.  $\frac{1}{e}$

D.  $\frac{2}{e}$



**Answer: A**



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25. If  $\lim_{x \rightarrow c^-} \{\ln x\}$  and  $\lim_{x \rightarrow c^+} \{\ln x\}$  exist finitely but they are not equal (where  $\{.\}$  denotes fractional part function), then:

- A.  $c'$  can take only rational values
- B.  $c'$  can take only irrational values
- C.  $c'$  can take infinite values in which only one is irrational
- D.  $c'$  can take infinite values in which only one is rational

**Answer: D**



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26.  $\lim_{x \rightarrow 0} \left( 1 + \frac{a \sin bx}{\cos x} \right)^{\frac{1}{x}}$ , where  $a, b$  are non zero constants is equal to :

A.  $e^{a/b}$

B.  $ab$

C.  $e^{ab}$

D.  $e^{b/e}$

**Answer: C**

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27. the value of  $\lim_{x \rightarrow 0} \left\{ (\cos x)^{\frac{1}{\sin^2 x}} + \frac{\sin 2x + 2 \tan^{-1} x + 3x^2}{\ln(1 + 3x + \sin^2 x) + xe^x} \right\}$

A.  $\sqrt{e} + \frac{3}{2}$

B.  $\frac{1}{\sqrt{e}} + \frac{3}{2}$

C.  $\sqrt{e} + 2$

D.  $\frac{1}{\sqrt{e}} + 2$

**Answer: D**

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$$28. \text{ Let } a = \lim_{x \rightarrow 1} \left( \frac{x}{\ln x} - \frac{1}{x \ln x} \right), b = \lim_{x \rightarrow 0} \left( \frac{x^3 - 16x}{4x + x^2} \right),$$

$$c = \lim_{x \rightarrow 1} \left( \frac{\ln(1 + \sin x)}{x} \right) \&$$

$$d = \lim_{x \rightarrow -1} \frac{(x + 1)^3}{[\sin(x + 1) - (x + 1)]}$$

Then  $\begin{bmatrix} a & b \\ c & d \end{bmatrix}$  is

A. Idempotent

B. Involutary

C. Non-singular

D. Nipotent

**Answer: D**



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29. The integral value of  $n$  so that  $\lim_{x \rightarrow 0} f(x)$  where

$$f(x) = \frac{(\sin x - x) \left( 2 \sin x - \ln \left( \frac{1+x}{1-x} \right) \right)}{x^n}$$
 is a finite non-zero number

A. 2

B. 4

C. 6

D. 8

Answer: C



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30.  $\lim_{x \rightarrow \frac{1}{\sqrt{2}^+}} \frac{\cos^{-1}(2x\sqrt{1-x^2})}{\left(x - \frac{1}{\sqrt{2}}\right)} - \lim_{x \rightarrow \frac{1}{\sqrt{2}^-} } \frac{\cos^{-1}(2x\sqrt{1-x^2})}{\left(x - \frac{1}{\sqrt{2}}\right)}$

A.  $\sqrt{2}$

B.  $2\sqrt{2}$

C.  $4\sqrt{2}$

D. 0

**Answer: C**



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**31.**

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( (\sin) \frac{\pi}{2k} - (\cos) \frac{\pi}{2k} - (\sin) \left( \frac{\pi}{2(k+2)} + (\cos) \frac{\pi}{2(k+2)} \right) \right) =$$

A. 0

B. 1

C. 2

D. 3

**Answer: D**



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32.  $\lim_{x \rightarrow 0} [1 + [x]]^{\frac{2}{x}}$ , where  $[:]$  is greatest integer function, is equal to

A. 0

B. 1

C.  $e^2$

D. Does not exist

**Answer: B**



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33. If  $m$  and  $n$  are positive integers, then  $\lim_{x \rightarrow 0} \frac{(\cos x)^{\frac{1}{m}} - (\cos x)^{\frac{1}{n}}}{x^2}$  equal to :

A.  $m - n$

B.  $\frac{1}{n} - \frac{1}{m}$

C.  $\frac{n - m}{2mn}$

D. none of these

**Answer: C**



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**34.** Find the values of  $a$  and  $b$  in order that

$$\lim_{x \rightarrow 0} \frac{x(1 + a \cos x) - b \sin x}{x^3} = 1.$$

A.  $\left(-\frac{5}{2}, -\frac{3}{2}\right)$

B.  $\left(\frac{5}{2}, \frac{3}{2}\right)$

C.  $\left(-\frac{5}{2}, \frac{3}{2}\right)$

D.  $\left(\frac{5}{2}, -\frac{3}{2}\right)$

**Answer: A**



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35. What is the value of  $a + b$ , if  $\lim_{x \rightarrow 0} \frac{\sin(ax) - \ln(e^x \cos x)}{x \sin(bx)} = \frac{1}{2}$  ?

A. 1

B. 2

C. 3

D.  $-\frac{1}{2}$

**Answer: B**



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36. Let  $\alpha = \lim_{n \rightarrow \infty} \frac{(1^3 - 1^2) + (2^3 - 2^2) + \dots + (n^3 - n^2)}{n^4}$ , then  $\alpha$

is equal to :

A.  $\frac{1}{3}$

B.  $\frac{1}{4}$

C.  $\frac{1}{2}$



D. None existent

**Answer: B**



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37.  $\lim_{x \rightarrow 0} \frac{\cos(\tan x) - \cos x}{x^4}$  is equal to

A.  $\frac{1}{5}$

B.  $\frac{1}{6}$

C.  $\frac{1}{4}$

D.  $\frac{1}{12}$

**Answer: D**



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38. Find the values of  $a$  and  $b$  in order that

$$\lim_{x \rightarrow 0} \frac{x(1 + a \cos x) - b \sin x}{x^3} = 1.$$

A.  $\left(-\frac{5}{2}, -\frac{3}{2}\right)$

B.  $\left(\frac{5}{2}, \frac{3}{2}\right)$

C.  $\left(-\frac{5}{2}, \frac{3}{2}\right)$

D.  $\left(\frac{5}{2}, \frac{3}{2}\right)$

Answer: A



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39. Consider the sequence  $u_n = \sum_{r=1}^n \frac{r}{2^r}$ ,  $n \geq 1$  then the  $\lim_{n \rightarrow \infty} u_n$

A. 1

B. e

C.  $\frac{1}{2}$

D. 2

Answer: D

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40. The value of  $\lim_{x \rightarrow 0} \left( (\cos x)^{\frac{1}{\sin^2 x}} + \frac{\sin 2x + 2 \tan^{-1} 3x + 2x^2}{\ln(1 + 3x + \sin^2 x) + xe^x} \right)$  is:

A.  $\sqrt{e} + \frac{3}{2}$

B.  $\frac{1}{\sqrt{e}} + \frac{3}{2}$

C.  $\sqrt{e} + 2$

D.  $\frac{1}{\sqrt{e}} + 2$

Answer: D

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41. For  $n \in \mathbb{N}$  let

$f_n(x) = \tan \frac{x}{2} (1 + \sec x)(1 + \sec 2x)(1 + \sec 4x) \dots (1 + \sec 2^{n-1} x)$ . Then  $\lim_{x \rightarrow 0} \frac{f_n(x)}{2x}$  is

- A. 0
- B.  $2^n$
- C.  $2^{n-1}$
- D.  $2^{n+1}$

**Answer: C**



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42. The value of  $\lim_{x \rightarrow \frac{\pi}{4}} (1 + [x])^{1/\ln(\tan x)}$  (where  $[.]$  denote the greatest integer function) is equal to

- A. 0
- B. 1

C.  $e$

D.  $\frac{1}{e}$

**Answer: B**



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43. If  $(\lim_{x \rightarrow 0} \frac{\{(a - n)nx - \tan x\} \sin nx}{x^2} - 0)$ , where  $n$  is nonzero real number, the  $a$  is 0 (b)  $\frac{n + 1}{n}$  (c)  $n$  (d)  $n + \frac{1}{n}$

A. 0

B.  $1 + \frac{1}{n}$

C.  $\pi$

D.  $n + \frac{1}{n}$

**Answer: D**



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44. The value of  $\lim_{x \rightarrow \infty} \left( \frac{n!}{n^n} \right)^{\frac{3n^3+4}{4n^4-1}}$ ,  $n \in \mathbb{N}$  is equal to:

A.  $\left( \frac{1}{e} \right)^{3/4}$

B.  $e^{3/4}$

C.  $e^{-1}$

D. 0

**Answer: A**



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45. The value of  $\lim_{x \rightarrow \infty} \frac{ax^2 + bx + c}{dx + e}$  ( $a, b, c, d, e \in \mathbb{R} - \{0\}$ ) depends on the sign of:

A. a only

B. d only

C. a and d only

D. a,b and d only

Answer: C

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46.

Let

$$f(x) = \lim_{n \rightarrow \infty} \tan^{-1} \left( 4n^2 \left( 1 - \cos \frac{\pi}{n} \right) \right) \text{ and } g(x) = \lim_{n \rightarrow \infty} \frac{n^2}{2} \ln \cos \left( \frac{2x}{n} \right)$$

then  $\lim_{x \rightarrow 0} \frac{e^{-2g(x)} - e^{f(x)}}{x^6}$  equals.

A.  $\frac{8}{3}$

B.  $\frac{7}{3}$

C.  $\frac{5}{3}$

D.  $\frac{2}{3}$

Answer: A

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47. If  $f(x)$  be a cubic polynomial and  $\lim_{x \rightarrow 0} \frac{\sin^2 x}{f(x)} = \frac{1}{3}$  then  $f(1)$  can not be equal to :

A. 0

B. -5

C. 3

D. -2

**Answer: C**



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48.  $\lim_{x \rightarrow 0} \frac{2e^{\sin x} - e^{-\sin x} - 1}{x^2 + 2x}$

A.  $\frac{3}{2}$

B.  $e^{3/2}$

C. 2

D.  $e^2$



**Answer: A**



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**49.** If  $x_1, x_2, x_3, \dots, x_n$  are the roots of the equation  $x^n + ax + b = 0$ , the value of

$(x_1 - x_2)(x_1 - x_3)(x_1 - x_4)\dots\dots(x_1 - x_n)$  is

A.  $nx_1 + b$

B.  $nx_1^{n-1} + a$

C.  $nx_1^{n-1}$

D.  $nx_1^{n-1}$

**Answer: B**



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**50.**  $\lim_{x \rightarrow 0} \frac{{}^3\sqrt{1 + \sin^2 x} - {}^4\sqrt{1 - 2 \tan x}}{\sin x + \tan^2 x}$  is equal to:

A.  $-1$

B.  $1$

C.  $\frac{1}{2}$

D.  $-\frac{1}{2}$

**Answer: C**



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51. if  $f(x) = \begin{vmatrix} x \cos x & 2x \sin x & x \tan x \\ 1 & x & 1 \\ 1 & 2x & 1 \end{vmatrix}$  find  $\lim_{x \rightarrow 0} \frac{f(x)}{x^2}$

A.  $0$

B.  $1$

C.  $-1$

D. Does not exist

**Answer: C**

**Exercise One Or More Than One Answer Is Are Correct**

1. if  $\lim_{x \rightarrow 0} (p \tan qx^2 - 3 \cos^2 x + 4)^{\frac{1}{3x^2}} = e^{\frac{5}{3}}$

A.  $p = \sqrt{2}, q = \frac{1}{2\sqrt{2}}$

B.  $p = \frac{1}{\sqrt{2}}, q = 2\sqrt{2}$

C.  $p = 1, q = 2$

D.  $p = 2, q = 4$

**Answer: B::C**

2.  $\lim_{x \rightarrow \infty} 2\left(\sqrt{25x^2 + x} - 5x\right)$  is:

A.  $\lim_{x \rightarrow 0} \frac{2x - \log_e (1 + x)^2}{5x^2}$

B.  $\lim_{x \rightarrow 0} \frac{e^{-x} - 1 + x}{x^2}$

C.  $\lim_{x \rightarrow 0} \frac{2(1 - \cos x^2)}{5x^4}$

D.  $\lim_{(x \rightarrow 0)} \frac{\sin \frac{\pi}{5}}{x}$

**Answer: A::C::D**

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3. Let  $\lim_{x \rightarrow \infty} (2^x + a^x + e^x)^{1/x} = L$  which of the following statement (s) is (are) correct ?

A. if  $L = a(a > 0)$ , then the range of a is  $[e, \infty)$

B. if  $L = 2e(a > 0)$ , then the range of a is  $\{2e\}$

C. if  $L = e(a > 0)$ , then the range of a is  $(0, e]$

D. if  $L = 2a(a > 1)$ , then the range of a is  $\left(\frac{e}{2}, \infty\right)$

**Answer: A::B::C**

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4. Let  $x \tan \alpha + y \sin \alpha = \alpha$  and  $x \alpha \operatorname{cosec} \alpha + y \cos \alpha = 1$  be two variable straight lines,  $\alpha$  being the parameter. Let  $P$  be the point of intersection of the lines. In the limiting position when  $\alpha \rightarrow 0$ , the point  $P$  lies on the line :

A.  $x = 2$

B.  $x = -1$

C.  $y + 1 = 0$

D.  $y = 2$

**Answer: A::C::D**



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5. Let  $f: \mathbb{R} \rightarrow [-1, 1]$  be defined as  $f(x) = \cos(\sin x)$ , then which of the following is(are) correct ?

A.  $f$  is periodic with fundamental period  $2\pi$

B. Range of  $f = [\cos 1, 1]$

C.  $\lim_{x \rightarrow \frac{\pi}{2}} \left( f\left(\frac{\pi}{2} - x\right) + f\left(\frac{\pi}{2} + x\right) \right) = 2$

D.  $f$  is neither even nor odd function

**Answer: B::C**

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6. Let  $f(x) = x + \sqrt{x^2 + 2x}$  and  $g(x) = \sqrt{x^2 + 2x} - x$ , then:

A.  $\lim_{x \rightarrow \infty} g(x) = 1$

B.  $\lim_{x \rightarrow \infty} f(x) = 1$

C.  $\lim_{x \rightarrow -\infty} f(x) = -1$

D.  $\lim_{x \rightarrow \infty} g(x) = -1$

**Answer: A::C::D**

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7. Which of the following limits does not exist ?(a)

$$\lim_{x \rightarrow \infty} \cos e c^{-1}\left(\frac{x}{x+7}\right) \text{ (B)} \quad \lim_{x \rightarrow 1} \sec^{-1}(\sin^{-1} x) \text{ (C)} \quad \lim_{x \rightarrow 0^+} x^{\frac{1}{x}} \text{ (D)}$$

$$\lim_{x \rightarrow 0} \left(\tan\left(\frac{\pi}{8} + x\right)\right)^{\cot x}$$

A.  $\lim_{x \rightarrow \infty} \cos e c^{-1}\left(\frac{x}{x+7}\right)$

B.  $\lim_{x \rightarrow 1} \sec^{-1}(\sin^{-1} x)$

C.  $\lim_{x \rightarrow 0^+} x^{\frac{1}{x}}$

D.  $\lim_{x \rightarrow 0} \left(\tan\left(\frac{\pi}{8} + x\right)\right)^{\cot x}$

**Answer: A::D**



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8. If  $f(x) = \left(\lim\limits_{n \rightarrow \infty} \left(\frac{3}{2} + [\cos x] \left(\sqrt{n^2 + 1} - \sqrt{n^2 - 3n + 1}\right)\right)\right)$

where  $[y]$  denotes largest integer  $\leq$ , then identify the correct

statement(s).  $(\lim)_{n \rightarrow \infty} f(x) = 0$   $(\lim)_{n \rightarrow \frac{\pi}{2}} f(x) = \frac{3\pi}{4}$

$f(x) = \frac{3x}{2} \forall x \in \left[0, \frac{\pi}{2}\right]$   $f(x) = 0 \forall x \in \left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$

A.  $\lim_{x \rightarrow 0} f(x) = 0$

B.  $\lim_{x \rightarrow \frac{\pi}{2}} f(x) = \frac{3\pi}{4}$

C.  $f(x) = \frac{3\pi}{2} \forall x \in \left[0, \frac{\pi}{2}\right]$

D.  $f(x) = 0 \forall x \in \left(\frac{\pi}{2}, \frac{3\pi}{2}\right)$

**Answer: A::C::D**



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**9.**

Let

$$f: R \rightarrow R; f(x) = \begin{cases} (-1)^n & \text{if } x = \frac{1}{2^{2^n}}, n = 1, 2, 3, \dots \text{ and } 0 \\ 0 & \text{otherwise} \end{cases}$$

otherwisw then identity the correct statement (s).

A.  $\lim_{x \rightarrow 0} f(x)f(2x) = 0$

B.  $\lim_{x \rightarrow 0} f(x)$  does not exist

C.  $\lim_{x \rightarrow 0} f(x)f(2x) = 0$

D.  $\lim_{x \rightarrow 0} f(x)(2x)$  does not exist



Answer: B::C



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10. If  $\lim_{x \rightarrow a} f(x) = \lim_{x \rightarrow a} [f(x)]$  ( $[.]$  denotes the greatest integer function) and  $f(x)$  is non-constant continuous function, then

- A.  $\lim_{x \rightarrow 0} f(x)$  is an integer
- B.  $\lim_{x \rightarrow 0} f(x)$  is non-integer
- C.  $f(x)$  has local maximum at  $x = a$
- D.  $f(x)$  has local minimum at  $x = a$

Answer: A:D



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11. Let  $f(x) = \frac{\sin^{-1}(1 - \{x\}) \times \cos^{-1}(1 - \{x\})}{\sqrt{2\{x\}} \times (1 - \{x\})}$ , where  $\{x\}$  denotes the fractional part of  $x$ .

Which of the following is true?

A.  $\lim_{x \rightarrow 0^+} f(x) = \frac{\pi}{4}$

B.  $\lim_{x \rightarrow 0^+} f(x) = \sqrt{2} \lim_{x \rightarrow 0^-} f(x)$

C.  $\lim_{x \rightarrow 0^-} f(x) = \frac{\pi}{4\sqrt{2}}$

D.  $\lim_{x \rightarrow 0^-} f(x) = \frac{\pi}{2\sqrt{2}}$

**Answer: B::D**



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12.  $L = \lim_{x \rightarrow 0} \frac{\sin(\sin x) - \sin x}{ax^5 + bx^3 + c} = -\frac{1}{12}$

The value/values of a is

A.  $a = 2$

B.  $a = -2$

C.  $c = 0$

D.  $b \in R$

**Answer: A::C**



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13. If  $f(x) = \lim_{n \rightarrow \infty} \left( n \left( x^{1/n} - 1 \right) \right)$  for  $x > 0$ , then which of the following is/are true?

A.  $f\left(\frac{1}{x}\right) = 0$

B.  $f\left(\frac{1}{x}\right) = \frac{1}{f(x)}$

C.  $f\left(\frac{1}{x}\right) = -f(x)$

D.  $f(xy) = f(x) + f(y)$

**Answer: C::D**



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14.  $\lim_{n \rightarrow \infty} \cos^2 \left( \pi \left( 3\sqrt{n^3 + n^2 + 2n} - n \right) \right)$  where n is an integer, equals

A.  $\frac{1}{3}$

B.  $\frac{1}{2}$

C.  $\frac{1}{4}$

D.  $\frac{1}{9}$

Answer: A::B::C



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15. If  $\alpha, \beta \in \left(-\frac{\pi}{2}, 0\right)$  such that  $(\sin \alpha + \sin \beta) + \frac{\sin \alpha}{\sin \beta} = 0$  and  $(\sin \alpha + \sin \beta) \frac{\sin \alpha}{\sin \beta} = -1$  and  $\lambda =$  li

then :

A.  $\alpha = \frac{\pi}{6}$

B.  $\lambda = 2$

C.  $\alpha = -\frac{\pi}{3}$

D.  $\lambda = 1$

**Answer: B**



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16. Let  $f(x) = \begin{cases} |x - 2| + a^2 - 6a + 9, & x < 2 \\ 5 - 2x, & x \geq 2 \end{cases}$  If  $\lim_{x \rightarrow 2} [f(x)]$  exists the possible values  $a$  can take is/are (where  $[.]$  represents the greatest integer function)

A. 2

B.  $\frac{5}{2}$

C. 3

D.  $\frac{7}{2}$

**Answer: B**



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17. If  $f(x) = \begin{cases} x + \frac{1}{2}, & x < 0 \\ 2x + \frac{3}{4}, & x \geq 0 \end{cases}$ , then

$\left[ \lim_{x \rightarrow 0} f(x) \right] =$  (where  $[.]$  denotes the greatest integer function) a.

b. c. does not exist d. none of these

A. 2

B. 4

C. 5

D. none of these

**Answer: B**



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18.

Let

$$f(x) = \begin{cases} (x + 3), & -2 < x < 0 \\ 4, & x = 0 \\ (2x + 5), & 0 < x < 1 \end{cases}$$

then

$$\lim_{x \rightarrow 0} f\left(\left\{ \frac{x}{\tan x} \right\}\right) \text{ is: } (\{.\} \text{ denotes fractional part of function})$$

A. 4

B. 5

C. 7

D. none of these

**Answer: C**



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**19.** A certain function  $f(x)$  has the property that  $f(3x) = \alpha f(x)$  for all positive real values of  $x$  and  $f(x) = 1 - |x - 2|$  for  $1 \leq x \leq 3$ ,

$\lim_{x \rightarrow 2} (f(x))^{\csc\left(\frac{\pi x}{2}\right)}$  is

A.  $\frac{2}{\pi}$

B.  $-\frac{2}{\pi}$

C.  $e^{2/\pi}$

D. none of these

**Answer: D**



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20. If  $L = \lim_{x \rightarrow 0} \frac{1}{x^3} \left( \frac{1}{\sqrt{1+x}} - \frac{1+ax}{1+bx} \right)$  exists, then

A. 1

B.  $\frac{3}{4}$

C.  $\frac{1}{2}$

D.  $\frac{1}{4}$

**Answer: D**



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21. If  $L = \lim_{x \rightarrow 0} \frac{1}{x^3} \left( \frac{1}{\sqrt{1+x}} - \frac{1+ax}{1+bx} \right)$  exists, then

A.  $\frac{3}{4}$



B.  $\frac{1}{2}$

C. 1

D. 0

**Answer: C**



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22. If  $L = \lim_{x \rightarrow 0} \frac{1}{x^3} \left( \frac{1}{\sqrt{1+x}} - \frac{1+ax}{1+bx} \right)$  exists, then

A. 38

B. 16

C. 72

D. 3

**Answer: D**



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23. For the curve  $\sin x + \sin y = 1$  lying in first quadrant. If  $\lim_{x \rightarrow 0} x^\alpha \frac{d^2y}{dx^2}$  exists and non-zero than  $2\alpha =$

A.  $\frac{1}{2}$

B.  $\frac{1}{\sqrt{2}}$

C.  $\frac{3}{2}$

D. 2

Answer: C



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24. For the curve  $\sin x + \sin y = 1$  lying in first quadrant. If  $\lim_{x \rightarrow 0} x^\alpha \frac{d^2y}{dx^2}$  exists and non-zero than  $2\alpha =$

A.  $\frac{1}{2}$

B. 1

C.  $\frac{1}{2\sqrt{2}}$

D.  $\frac{1}{2\sqrt{3}}$

Answer: C



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## Exercise Subjective Type Problems

1. If  $\lim_{x \rightarrow 0} \frac{\ln \cot\left(\frac{\pi}{4} - \beta x\right)}{\tan \alpha x} = 1$ , then  $\frac{\alpha}{\beta} = \dots$ .



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2. If  $\lim_{x \rightarrow 0} \frac{f(x)}{\sin^2 x} = 8$ ,  $\lim_{x \rightarrow 0} \frac{g(x)}{2 \cos x - xe^x + x^3 + x - 2} = \lambda$  and  $\lim_{x \rightarrow 0} (1 + 2f(x))^{\frac{1}{g(x)}} = \frac{1}{e}$ , then

The value of  $\lambda$  is



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3. If  $\alpha, \beta$  are two distinct real roots of the equation  $ax^3 + x - 1 - a = 0$  ( $a \neq -1, 0$ ), none of which is equal to unity. If

the value of  $\lim_{x \rightarrow \frac{1}{\alpha}} \frac{(1+a)x^3 - x^2 - a}{(e^{1-\alpha x} - 1)(x-1)}$  is  $\frac{al(k\alpha - \beta)}{\alpha}$  the value of  $kl$

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4. The value of

$$\lim_{x \rightarrow 0} \frac{(140)^x - (35)^x - (28)^x - (20)^x + 7^x + 5^x + 4^x - 1}{x \sin^2 x} = 2 \ln 2 \ln k \ln 7$$

, then  $k =$

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5. If  $\lim_{x \rightarrow 0} \frac{a \cos x}{x^2} + \frac{b}{x^2} = \frac{1}{3}$ , then  $b - a =$

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6. Find the value of  $\lim_{x \rightarrow \infty} \left(x + \frac{1}{x}\right) e^{1/x} - x$ .

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7. Find  $\lim_{x \rightarrow \alpha^+} \left[ \frac{\min(\sin x, \{x\})}{x - 1} \right]$  where  $\alpha$  is the root of the equation  $\sin x + 1 = x$  Here  $[.]$  represents greatest integer function and  $\{.\}$  represents fractional part function



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