

**MATHS****BOOKS - VK JAISWAL ENGLISH****LIMIT****Exercise Single Choice Problems**

1. Evaluate  $\lim_{x \rightarrow 0} \frac{1 - \cos(1 - \cos x)}{x^4}$ .

A.  $\frac{1}{6}$

B.  $-\frac{1}{3}$

C.  $-\frac{1}{6}$

D.  $\frac{1}{3}$

**Answer: B**



2. The value of  $\lim_{x \rightarrow 0} \frac{(\sin x - \tan x)^2 - (1 - \cos 2x)^4 + x^5}{7(\tan^{-1} x)^7 + (\sin^{-1} x)^6 + 3 \sin^5 x}$  equal to:

A. 0

B. 1

C. 2

D.  $\frac{1}{3}$

Answer: D



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3. Let  $a = \lim_{x \rightarrow 0} \frac{\ln(\cos 2x)}{3x^2}$ ,  $b = \lim_{x \rightarrow 0} \frac{\sin^2 2x}{x(1 - e^x)}$ ,  $c = \lim_{x \rightarrow 1} \frac{\sqrt{x} - x}{\ln x}$ .

Then a,b,c satisfy :

A.  $a < b < c$

B.  $b < c < a$

C.  $a < c < b$

D.  $b < a < c$

**Answer: D**

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4. If  $f(x) = \cot^{-1}\left(\frac{3x - x^3}{1 - 3x^2}\right)$  and  $g(x) = \cos^{-1}\left(\frac{1 - x^2}{1 + x^2}\right)$  then  $\lim_{x \rightarrow a} \frac{f(x) - f(a)}{g(x) - g(a)}$ ,  $0 < a < \frac{1}{2}$  is :

A. 1)  $\frac{3}{2(1 + a^2)}$

B. 2)  $\frac{3}{2}$

C. 3)  $\frac{-3}{2(1 + a^2)}$

D. 4)  $-\frac{3}{2}$

**Answer: D**

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5.  $\lim_{x \rightarrow 0} \left( \frac{(1+x)^{\frac{2}{x}}}{e^2} \right)^{\frac{4}{\sin x}}$  is :

A. 1)  $e^4$

B. 2)  $e^{-4}$

C. 3)  $e^8$

D. 4)  $e^{-8}$

**Answer: B**



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6.  $\lim_{x \rightarrow \infty} \frac{3}{x} \left[ \frac{x}{4} \right] = \frac{p}{q}$  where  $[.]$  denotes greatest integer function), then  $p + q$  (where  $p, q$  are relative prime) is:

A. 2

B. 7

C. 5

**Answer: B****Watch Video Solution**

7.  $f(x) = \lim_{n \rightarrow \infty} \frac{x^n + \left(\frac{\pi}{3}\right)^\pi}{x^{n-1} + \left(\frac{\pi}{3}\right)^{n-1}}$ , (  $n$  is an even integer), then which

of the following is incorrect ?

- A. If  $f, \left[\frac{\pi}{3}, \infty\right) \rightarrow \left[\frac{\pi}{3}, \infty\right)$ , then function is invertible
- B.  $f(x) = f(-x)$  has infinite number of solutions
- C.  $f(x) = |f(x)|$  has infinite number of solutions
- D.  $f(x)$  is one-one function for all  $x \in \mathbb{R}$

**Answer: D****Watch Video Solution**

8.  $\lim_{x \rightarrow 0} \frac{\sin(\pi \cos^2(\tan(\sin x)))}{x^2}$  is equal to

A.  $\pi$

B.  $\frac{\pi}{4}$

C.  $\frac{\pi}{2}$

D. none of these

**Answer: A**



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9. if  $f(x) = \frac{(e^{(x+3) \ln 27})^{\frac{x}{27}} - 9}{3^x - 27}, x < 3$  and

$f(x) = \lambda \frac{1 - \cos(x - 3)}{(x - 3)\tan(x - 3)}, x > 3$  if  $\lim_{x \rightarrow 3} f(x)$  exist then *lmbda* is

A.  $\frac{9}{2}$

B.  $\frac{2}{9}$

C.  $\frac{2}{3}$

D. none of these

**Answer: C**



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10.  $\lim_{x \rightarrow \frac{\pi}{3}} \frac{\sin\left(\frac{\pi}{3} - x\right)}{2 \cos x - 1}$  is equal to:

A.  $\frac{2}{\sqrt{3}}$

B.  $\frac{1}{\sqrt{3}}$

C.  $\sqrt{3}$

D.  $\frac{1}{2}$

**Answer: B**



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11.  $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\sin x}{\cos^{-1}\left[\frac{1}{4}(3 \sin x - \sin 3x)\right]}$ , (where  $[.]$  denotes greatest integer function) is :

A.  $\frac{2}{\pi}$

B. 1

C.  $\frac{4}{\pi}$

D. does not exist

**Answer: A**



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12. Let  $f$  be a continuous function on  $\mathbb{R}$ . If

$$f(1/4^n) = (\sin e^n)e^{-n^2} + \frac{n^2}{n^2 + 1}, \text{ then } f(0) \text{ is}$$

A. 1

B. 0

C.  $-1$

D.  $\frac{1}{6}$

**Answer: A**





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13.  $\lim_{x \rightarrow 1^-} \frac{e^{\{x\}} - \{x\} - 1}{\{x\}^2}$  equal, where  $\{ \}$  is fractional part function

and  $I$  is an integer, to :

A.  $\frac{I}{2}$

B.  $e - 2$

C.  $I$

D. does not exist

Answer: B



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14.  $\lim_{x \rightarrow \infty} (e^{11x} - 7x)^{\frac{1}{3x}}$

A.  $\frac{11}{3}$

B.  $\frac{3}{11}$

C.  $e^{\frac{3}{11}}$

D.  $e^{\frac{11}{3}}$

**Answer: D**



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15. For a certain value of  $c$ ,  $\lim_{x \rightarrow -\infty} \left[ (x^5 + 7x^2 + 2)^c - \right] = \lambda$  is finite

and non-zero. The value of  $3xc + \lambda$  is .....

A.  $\frac{7}{5}$

B. 1

C.  $\frac{2}{5}$

D. None of these

**Answer: A**



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16. Find the integral value of  $n$  for which

$(\lim)_{x \rightarrow 0} \frac{\cos^2 x - \cos x - e^x \cos x + e^x - \frac{x^3}{2}}{x^n}$  is a finite nonzero number

A. 1

B. 2

C. 3

D. 4

**Answer: C**



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17. The value of  $\lim_{x \rightarrow 0} \left( \frac{\sin x}{x} \right)^{\frac{1}{1 - \cos x}}$  :

A.  $e^{-1/3}$

B.  $e^{1/3}$

C.  $e^{-1/6}$

D.  $e^{1/6}$

**Answer: A**



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18. If  $\lim_{x \rightarrow \infty} (\sqrt{x^2 - x + 1} - ax - b) = 0$ , then for  $k \geq 2, (k \in \mathbb{N}) \lim_{x \rightarrow \infty} \sec^{2n}(kix\pi b) =$

A. a

B.  $-a$

C.  $2a$

D. b

**Answer: A**



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19. If  $f$  is a positive function such that

$f(x + T) = f(x)(T > 0), \forall x \in R,$  then

$$\lim_{x \rightarrow \infty} n \left( \frac{f(x + T) + 2f(x + 2T) + \dots + nf(x + nT)}{f(x + T) + 4f(x + 4T) + \dots + n^2 f(x + n^2 T)} \right) =$$

A. 2

B.  $\frac{2}{3}$

C.  $\frac{3}{2}$

D. none of these

Answer: C



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20. Let  $f(x) = 3x^{10} - 7x^8 + 5x^6 - 21x^3 + 3x^2 - 7$

$$265 \left( \lim_{h \rightarrow 0} \frac{h^4 + 3h^2}{(f(1-h) - f(1)) \sin 5h} \right) =$$

A. 1

B. 2

C. 3

D.  $-3$

**Answer: C**



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21.  $\lim_{x \rightarrow 0} \left( \frac{\cos x - \sec x}{x^2(x + 1)} \right) =$

A. 0

B.  $-\frac{1}{2}$

C.  $-1$

D.  $-2$

**Answer: C**



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22. Let  $f(x)$  be a continuous and differentiable function satisfying

$f(x + y) = f(x)f(y) \forall x, y \in R$  if  $f(x)$  can be expressed as

$f(x) = 1 + xP(x) + x^2Q(x)$  where

$\lim_{x \rightarrow 0} \lim P(x) = a$  and  $\lim_{x \rightarrow 0} \lim Q(x) = b$ , then  $f'(x)$  is equal to :

A.  $af(x)$

B.  $bf(x)$

C.  $(a + b)f(x)$

D.  $(a + 2b)f(x)$

**Answer: A**



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23. The value of  $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\left\{1 - \tan\left(\frac{x}{2}\right)\right\} \{1 - \sin x\}}{\left\{1 + \tan\left(\frac{x}{2}\right)\right\} (\pi - 2x)^3}$  equals

A. does not exist

B.  $\frac{1}{8}$

C.  $\frac{1}{16}$

D.  $\frac{1}{32}$

**Answer: D**



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24.  $\lim_{x \rightarrow \infty} \left( \frac{x-3}{x+2} \right)$  is equal to :

A.  $e$

B.  $e^{-1}$

C.  $e^{-5}$

D.  $e^5$

**Answer: C**



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25.  $\lim_{x \rightarrow \frac{\pi}{2}} (\cos x)^{\cos x}$  is :

A. 1

B. 0

C.  $\frac{1}{e}$

D.  $\frac{2}{e}$

**Answer: A**



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26. If  $\lim_{e \rightarrow e^-} \{\ln x\}$  and  $\lim_{x \rightarrow x^+} \{\ln x\}$  exist finitely but they are not equal

(where  $\{.\}$  denotes fractional part function), then:

A.  $c'$  can take only rational values

B.  $c'$  can take only irrational values

C.  $c'$  can take infinite values in which only one is irrational

D. 'c' can take infinite values I which only one is rational

**Answer: D**



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27.  $\lim_{x \rightarrow 0} \left( 1 + \frac{a \sin bx}{\cos x} \right)^{\frac{1}{x}}$ , where a,b are non-zero constants is equal to

:

A.  $e^{a/b}$

B.  $ab$

C.  $e^{ab}$

D.  $e^{b/e}$

**Answer: C**



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28. The value of  $\lim_{x \rightarrow 0} \left( (\cos x)^{\frac{1}{\sin^2 x}} + \frac{\sin 2x + 2 \tan^{-1} 3x + 2x^2}{\ln(1 + 3x + \sin^2 x) + xe^x} \right)$  is:

A.  $\sqrt{e} + \frac{3}{2}$

B.  $\frac{1}{\sqrt{e}} + \frac{3}{2}$

C.  $\sqrt{e} + 2$

D.  $\frac{1}{\sqrt{e}} + 2$

**Answer: D**



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29. Let  $a = \lim_{x \rightarrow 1} \left( \frac{x}{\ln x} - \frac{1}{x \ln x} \right)$ ,  $b = \lim_{x \rightarrow 0} \left( \frac{x^3 - 16x}{4x + x^2} \right)$ ,

$$c = \lim_{x \rightarrow 1} \left( \frac{\ln(1 + \sin x)}{x} \right) \&$$

$$d = \lim_{x \rightarrow -1} \frac{(x + 1)^3}{[\sin(x + 1) - (x + 1)]}$$

Then  $\begin{bmatrix} a & b \\ c & d \end{bmatrix}$  is

A. Idempotent

B. Involutary

C. Non-singular

D. Nipotent

**Answer: D**



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30. The integral value of  $n$  so that  $\lim_{x \rightarrow 0} f(x)$  where

$$f(x) = \frac{(\sin x - x) \left( 2 \sin x - \ln \left( \frac{1+x}{1-x} \right) \right)}{x^n}$$

is a finite non-zero number, is:

A. 2

B. 4

C. 6

D. 8

**Answer: C**



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31.

$$\lim_{x \rightarrow \left(\frac{1}{\sqrt{2}}\right)^+} \frac{\cos^{-1}\left(2x\sqrt{1-x^2}\right)}{\left(x - \frac{1}{\sqrt{2}}\right)} - \lim_{x \rightarrow \left(\frac{1}{\sqrt{2}}\right)^-} \frac{\cos^{-1}\left(2x\sqrt{1-x^2}\right)}{\left(x - \frac{1}{\sqrt{2}}\right)} =$$

A.  $\sqrt{2}$

B.  $2\sqrt{2}$

C.  $4\sqrt{2}$

D. 0

Answer: C



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$$32. \lim_{x \rightarrow \infty} \sum_{k=1}^n \left( \sin \frac{\pi}{2k} - \cos \frac{\pi}{2k} - \sin \left( \frac{\pi}{2(k+2)} \right) + \frac{\cos(\pi)}{2(k+2)} \right) =$$

A. 0

B. 1

C. 2

D. 3

**Answer: D**



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33.  $\lim_{x \rightarrow 0^+} [1 + [x]]^{2/x}$ , where  $[.]$  is greatest integer function, is equal to

:

A. 0

B. 1

C.  $e^2$

D. Does not exist

**Answer: B**



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34. If  $m$  and  $n$  are positive integers, then  $\lim_{x \rightarrow 0} \frac{(\cos x)^{1/m} - (\cos x)^{1/n}}{x^2}$  equals to:

A.  $m - n$

B.  $\frac{1}{n} - \frac{1}{m}$

C.  $\frac{n - m}{2mn}$

D. none of these

**Answer: C**



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35. The value of ordered pair  $(a, b)$  such that

$$\lim_{x \rightarrow 0} \frac{x(1 + a \cos x) - b \sin x}{x^3} = 1, \text{ is:}$$

A.  $\left(-\frac{5}{2}, -\frac{3}{2}\right)$

B.  $\left(\frac{5}{2}, \frac{3}{2}\right)$

C.  $\left(-\frac{5}{2}, \frac{3}{2}\right)$

D.  $\left(\frac{5}{2}, -\frac{3}{2}\right)$

**Answer: A**



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36. What is the value of  $a + b$ , if  $\lim_{x \rightarrow 0} \frac{\sin(ax) - \ln(e^x \cos x)}{x \sin(bx)} = \frac{1}{2}$ ?

A. 1

B. 2

C. 3

D.  $-\frac{1}{2}$

**Answer: B**



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37. Let  $\alpha = \lim_{x \rightarrow \infty} \frac{(1^3 - 1^2) + (2^3 - 2^2) + \dots + (n^3 - n^2)}{n^4}$ , then  $\alpha$  is equal to:

A.  $\frac{1}{3}$

B.  $\frac{1}{4}$

C.  $\frac{1}{2}$

D. None existent

**Answer: B**



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38. The value of  $\lim_{x \rightarrow 0} \frac{\cos(\sin x) - \cos x}{x^4}$  is equal to :

A.  $\frac{1}{5}$

B.  $\frac{1}{6}$

C.  $\frac{1}{4}$

D.  $\frac{1}{12}$

**Answer: D**



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**39.** The value of ordered pair  $(a,b)$  such that

$$\lim_{x \rightarrow 0} \frac{x(1 + a \cos x) - b \sin x}{x^3} = 1, \text{ is:}$$

A.  $\left(-\frac{5}{2}, -\frac{3}{2}\right)$

B.  $\left(\frac{5}{2}, \frac{3}{2}\right)$

C.  $\left(-\frac{5}{2}, \frac{3}{2}\right)$

D.  $\left(\frac{5}{2}, \frac{3}{2}\right)$

**Answer: A**



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40. Consider the sequence :  $u_n = \sum_{r=1}^n \frac{r}{2^r}, n \geq 1$  Then the limit of  $u_n$  as  $n \rightarrow \infty$  is:

A. 1

B. e

C.  $\frac{1}{2}$

D. 2

**Answer: D**



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41. The value of  $\lim_{x \rightarrow 0} \left( (\cos x)^{\frac{1}{\sin^2 x}} + \frac{\sin 2x + 2 \tan^{-1} 3x + 2x^2}{\ln(1 + 3x + \sin^2 x) + xe^x} \right)$  is:

A.  $\sqrt{e} + \frac{3}{2}$

B.  $\frac{1}{\sqrt{e}} + \frac{3}{2}$

C.  $\sqrt{e} + 2$

D.  $\frac{1}{\sqrt{e}} + 2$

**Answer: D**



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42. For  $n \in \mathbb{N}$  let  $f_n(x) = \tan \frac{x}{2} (1 + \sec x)(1 + \sec 2x)(1 + \sec 4x) \dots (1 + \sec 2^n x)$ . Then  $\lim_{x \rightarrow 0} \frac{f_n(x)}{2x}$  is

A. 0

B.  $2^n$

C.  $2^{n-1}$

D.  $2^{n+1}$

**Answer: C**



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43. The value of  $\lim_{x \rightarrow \frac{\pi}{4}} (1 + [x])^{\frac{1}{\ln(\tan x)}}$  is:

when  $[.]$  denotes greatest integer function).

A. 0

B. 1

C. e

D.  $\frac{1}{e}$

**Answer: B**



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44. If  $\lim_{x \rightarrow 0} \frac{\{(a - n)nx - \tan x\} \sin nx}{x^2} = 0$ , where  $n$  is non zero real number then  $a$  is equal to

A. 0

B.  $1 + \frac{1}{n}$

C.  $\pi$

D.  $n + \frac{1}{n}$

**Answer: D**

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45. The value of  $\lim_{x \rightarrow \infty} \left( \frac{n!}{n^n} \right)^{\frac{3n^3+4}{4n^4-1}}$ ,  $n \in \mathbb{N}$  is equal to:

A.  $\left( \frac{1}{e} \right)^{3/4}$

B.  $e^{3/4}$

C.  $e^{-1}$

D. 0

**Answer: A**

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46. The value of  $\lim_{x \rightarrow \infty} \frac{ax^2 + bx + c}{dx + e}$  ( $a, b, c, d, e \in \mathbb{R} - \{0\}$ )

depends on the sign of :

A. a only

B. d only

C. a and d only

D. a,b and d only

**Answer: C**



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47. If  $f(x) = \lim_{n \rightarrow \infty} \tan^{-1} \left( 4n^2 \left( 1 - \cos \left( \frac{x}{n} \right) \right) \right)$  and  $g(x) =$

$\lim_{n \rightarrow \infty} \frac{n^2}{2} \ln \cos \left( 2 \frac{x}{n} \right)$  then  $\lim_{x \rightarrow 0} \frac{e^{-2g(x)} - e^{f(x)}}{x^6}$  equals

A.  $\frac{8}{3}$

B.  $\frac{7}{3}$

C.  $\frac{5}{3}$

D.  $\frac{2}{3}$

**Answer: A**



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48. If  $f(x)$  be a cubic polynomial and  $\lim_{x \rightarrow 0} \frac{\sin^2 x}{f(x)} = \frac{1}{3}$  then  $f(1)$  can not be equal to :

A. 0

B.  $-5$

C. 3

D.  $-2$

**Answer: C**



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49.  $\lim_{x \rightarrow 0} \frac{2e^{\sin x} - e^{-\sin x} - 1}{x^2 + 2x}$  equals to :

A.  $\frac{3}{2}$

B.  $e^{3/2}$

C. 2

D.  $e^2$

**Answer: A**



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50. If  $x_1, x_2, x_3, \dots, x_n$  are the roots of  $x^n + ax + b = 0$ , then the value of  $(x_1 - x_2)(x_1 - x_3)(x_1 - x_4) \dots (x_1 - x_n)$  is equal to

A.  $nx_1 + b$

B.  $nx_1^{n-1} + a$

C.  $nx_1^{n-1}$

D.  $nx_1^{n-1}$

**Answer: B**



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51.  $\lim_{x \rightarrow 0} \frac{\sqrt[3]{1 + \sin^2 x} - \sqrt[4]{1 - 2 \tan x}}{\sin x + \tan^2 x}$  is equal to:

A.  $-1$

B.  $1$

C.  $\frac{1}{2}$

D.  $-\frac{1}{2}$

**Answer: C**



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52. If  $f(x) = \begin{vmatrix} x \cos x & 2x \sin x & x \tan x \\ 1 & x & 1 \\ 1 & 2x & 1 \end{vmatrix}$ , find  $\lim_{x \rightarrow 0} \frac{f(x)}{x^2}$ .

A. 0

B. 1

C. -1

D. Does not exist

**Answer: C**



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**Exercise One Or More Than One Answer Is Are Correct**

1. If  $\lim_{x \rightarrow 0} (p \tan qx^2 - 3 \cos^2 x + 4)^{1/(3x^2)} = e^{5/3} = e^{5/3}, p, q \in R$  then:

A.  $p = \sqrt{2}, q = \frac{1}{2\sqrt{2}}$

B.  $p = \frac{1}{\sqrt{2}}, q = 2\sqrt{2}$

C.  $p = 1, q = 2$

D.  $p = 2, q = 4$

**Answer: B::C**



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2.  $\lim_{x \rightarrow \infty} 2\left(\sqrt{25x^2 + x} - 5x\right)$  is equal to:

A.  $\lim_{x \rightarrow 0} \frac{2x - \log_e (1 + x)^2}{5x^2}$

B.  $\lim_{x \rightarrow 0} \frac{e^{-x} - 1 + x}{x^2}$

C.  $\lim_{x \rightarrow 0} \frac{2(1 - \cos x^2)}{5x^4}$

D.  $\lim_{(x \rightarrow 0)} \frac{\sin \frac{\pi}{5}}{x}$

**Answer: A::C::D**



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3. Let  $\lim_{x \rightarrow \infty} (2^x + a^x + e^x)^{1/x} = L$

which of the following statement (s) is (are) correct ?

A. if  $L = a$  ( $a > 0$ ), then the range of  $a$  is  $[e, \infty)$

B. if  $L = 2e$  ( $a > 0$ ), then the range of  $a$  is  $\{2e\}$

C. if  $L = e$  ( $a > 0$ ), then the range of  $a$  is  $(0, e]$

D. if  $L = 2a$  ( $a > 1$ ), then the range of  $a$  is  $(\frac{e}{2}, \infty)$

**Answer: A::B::C**



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4. Let  $x \tan \alpha + y \sin \alpha = a$  and  $x \alpha \cos e c \alpha + y \cos \alpha = 1$  be two variable straight lines,  $\alpha$  being the parameter. Let  $P$  be the point of intersection of the lines. In the limiting position when  $a \rightarrow 0$ , the point  $P$  lies on the line :

A.  $x = 2$

B.  $x = -1$

C.  $y + 1 = 0$

D.  $y = 2$

**Answer: A::C::D**



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5. Let  $f: \mathbb{R} \rightarrow [-1, 1]$  be defined as  $f(x) = \cos(\sin x)$ , then which of the following is (are) correct ?

A.  $f$  is periodic with fundamental period  $2\pi$

B. Range of  $f = [\cos 1, 1]$

C.  $\lim_{x \rightarrow \frac{\pi}{2}} \left( f\left(\frac{\pi}{2} - x\right) + f\left(\frac{\pi}{2} + x\right) \right) = 2$

D.  $f$  is neither even nor odd function

**Answer: B::C**



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6. Let  $f(x) = x + \sqrt{x^2 + 2x}$  and  $g(x) = \sqrt{x^2 + 2x} - x$ , then:

A.  $\lim_{x \rightarrow \infty} g(x) = 1$

B.  $\lim_{x \rightarrow \infty} f(x) = 1$

C.  $\lim_{x \rightarrow -\infty} f(x) = -1$

D.  $\lim_{x \rightarrow \infty} g(x) = -1$

**Answer: A::C::D**



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7. Which of the following limits does not exist ?

A.  $\lim_{x \rightarrow \infty} \cos e c^{-1} \left( \frac{x}{x+7} \right)$

B.  $\lim_{x \rightarrow 1} \sec^{-1}(\sin^{-1} x)$

C.  $\lim_{x \rightarrow 0^+} x^{\frac{1}{x}}$

D.  $\lim_{x \rightarrow 0} \left( \tan \left( \frac{\pi}{8} + x \right) \right)^{\cot x}$

**Answer: A::D**



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8. If  $f(x) = \lim_{x \rightarrow \infty} x \left( \frac{3}{2} + [\cos x] \left( \sqrt{n^2 + 1} - \sqrt{n^2 - 3n + 1} \right) \right)$

where  $[y]$  denotes largest integer  $\leq y$ , then identify the correct statement (s).

A.  $\lim_{x \rightarrow 0} f(x) = 0$

B.  $\lim_{x \rightarrow \frac{\pi}{2}} f(x) = \frac{3\pi}{4}$

C.  $f(x) = \frac{3\pi}{2} \forall x \in \left[ 0, \frac{\pi}{2} \right]$

D.  $f(x) = 0 \forall x \in \left( \frac{\pi}{2}, \frac{3\pi}{2} \right)$

**Answer: A::C::D**



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9. Let  $f: \mathbb{R} \rightarrow \mathbb{R}$ ,  $f(x) = \begin{cases} (-1)^n & \text{if } x = \frac{1}{2^{2^n}}, \quad n = 1, 2, 3, \dots \\ 0 & \text{otherwise} \end{cases}$  then

identify the correct statement (s).

- A.  $\lim_{x \rightarrow 0} f(x)f(2x) = 0$
- B.  $\lim_{x \rightarrow 0} f(x)$  does not exist
- C.  $\lim_{x \rightarrow 0} f(x)f(2x) = 0$
- D.  $\lim_{x \rightarrow 0} f(x)(2x)$  does not exist

**Answer: B::C**



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10. If  $\lim_{x \rightarrow a} f(x) = \lim_{x \rightarrow a} [f(x)]$  ([.] denotes the greatest integer function)

and  $f(x)$  is non-constant continuous function, then

- A.  $\lim_{x \rightarrow 0} f(x)$  is an integer
- B.  $\lim_{x \rightarrow 0} f(x)$  is non-integer

C.  $f(x)$  has local maximum at  $x = a$

D.  $f(x)$  has local minimum at  $x = a$

**Answer: A::D**



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11. Let  $f(x) = \frac{\sin^{-1}(1 - \{x\}) \times \cos^{-1}(1 - \{x\})}{\sqrt{2\{x\}} \times (1 - \{x\})}$ , where  $\{x\}$  denotes

the fractional part of  $x$ .

Which of the following is true?

A.  $\lim_{x \rightarrow 0^+} f(x) = \frac{\pi}{4}$

B.  $\lim_{x \rightarrow 0^+} f(x) = \sqrt{2} \lim_{x \rightarrow 0^-} f(x)$

C.  $\lim_{x \rightarrow 0^-} f(x) = \frac{\pi}{4\sqrt{2}}$

D.  $\lim_{x \rightarrow 0^-} f(x) = \frac{\pi}{2\sqrt{2}}$

**Answer: B::D**



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12.  $\lim_{x \rightarrow 0} \frac{\sin(\sin x) - \sin x}{ax^3 + bx^5 + c} = -\frac{1}{12}$  then

A.  $a = 2$

B.  $a = -2$

C.  $c = 0$

D.  $b \in \mathbb{R}$

Answer: A:C



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13. If  $f(x) = \lim_{n \rightarrow \infty} \left( n(x^{1/n} - 1) \right)$  for  $x > 0$ , then which of the following is/are true?

A.  $f\left(\frac{1}{x}\right) = 0$

B.  $f\left(\frac{1}{x}\right) = \frac{1}{f(x)}$

C.  $f\left(\frac{1}{x}\right) = -f(x)$

$$D. f(xy) = f(x) + f(y)$$

**Answer: C::D**



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14. The value of  $\lim_{n \rightarrow \infty} \cos^2\left(\pi\left(\sqrt[3]{n^3 + n^2 + 2n}\right)\right)$  (where  $n \in N$ ) :

A.  $\frac{1}{3}$

B.  $\frac{1}{2}$

C.  $\frac{1}{4}$

D.  $\frac{1}{9}$

**Answer: A::B::C**



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15. If  $\alpha, \beta \in \left(-\frac{\pi}{2}, 0\right)$  such that  $(\sin \alpha + \sin \beta) + \frac{\sin \alpha}{\sin \beta} = 0$  and  $(\sin \alpha + \sin \beta) \frac{\sin \alpha}{\sin \beta} = -1$  and  $\lambda = \lim_{x \rightarrow \infty} \frac{1 + (2 \sin \alpha)^{2n}}{(2 \sin \beta)^{2n}}$  then:

A.  $\alpha = -\frac{\pi}{6}$

B.  $\lambda = 2$

C.  $\alpha = -\frac{\pi}{3}$

D.  $\lambda = 1$

**Answer: B**

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16. Let  $f(x) = \{|x - 2| + a^2 - 6a + 9, x < 2$  and  $5 - 2x, x \geq 2$  If  $\lim_{x \rightarrow 2} [f(x)]$  exists the possible values a can take is/are (where  $[.]$  represents the gretest integer function)

A. 2

B.  $\frac{5}{2}$

C. 3

D.  $\frac{7}{2}$

**Answer: B**

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## Exercise Comprehension Type Problems

1.

Let

$$f(x) = [(x + 3, , - 2 < x < 0), (4, x = 0), (2x + 5, , 0 < x < 1),$$

then

$$\lim_{x \rightarrow 0} f\left(\left\{\frac{x}{\tan x}\right\}\right) \text{ is: } (\{.\} \text{ denotes fractional part of function})$$

A. 2

B. 4

C. 5

D. none of these

**Answer: B**



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2.

Let

$$f(x) = [(x + 3, , - 2 < x < 0), (4, x = 0), (2x + 5, , 0 < x < 1),$$

then

$$\lim_{x \rightarrow 0} f\left(\left\{\frac{x}{\tan x}\right\}\right) \text{ is: } (\{.\} \text{ denotes fractional part of function})$$

A. 4

B. 5

C. 7

D. none of these

**Answer: C**



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3. A certain function  $f(x)$  has the property that  $f(2x) = \alpha f(x)$  for all positive real values of  $x$  and  $f(x) = 1 - |x - 2|$  for  $1 \leq x \leq 3$

$\lim_{x \rightarrow 2} (f(x))^{\cos ec\left(\frac{\pi x}{2}\right)}$  is :

A.  $\frac{2}{\pi}$

B.  $-\frac{2}{\pi}$

C.  $e^{2/\pi}$

D. none of these

**Answer: D**



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4. If  $L = \lim_{x \rightarrow 0} \frac{1}{x^3} \left( \frac{1}{\sqrt{1+x}} - \frac{1+ax}{1+bx} \right)$  exists, then

A. 1

B.  $\frac{3}{4}$



C.  $\frac{1}{2}$

D.  $\frac{1}{4}$

**Answer: D**



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5. If  $L = \lim_{x \rightarrow 0} \frac{1}{x^3} \left( \frac{1}{\sqrt{1+x}} - \frac{1+ax}{1+bx} \right)$  exists, then

A.  $\frac{3}{4}$

B.  $\frac{1}{2}$

C. 1

D. 0

**Answer: C**



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6. If  $L = \lim_{x \rightarrow 0} \frac{1}{x^3} \left( \frac{1}{\sqrt{1+x}} - \frac{1+ax}{1+bx} \right)$  exists, then

A. 38

B. 16

C. 72

D. 24

**Answer: D**



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7. For the curve  $\sin x + \sin y = 1$  lying in first quadrant. If  $\lim_{x \rightarrow 0} x^\alpha \frac{d^2y}{dx^2}$  exists and non-zero then  $2\alpha =$

A.  $\frac{1}{2}$

B.  $\frac{1}{\sqrt{2}}$

C.  $\frac{3}{2}$

D. 2

Answer: C



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8. For the curve  $\sin x + \sin y = 1$  lying in first quadrant. If  $\lim_{x \rightarrow 0} x^\alpha \frac{d^2y}{dx^2}$  exists and non-zero then  $2\alpha =$

A.  $\frac{1}{2}$

B. 1

C.  $\frac{1}{2\sqrt{2}}$

D.  $\frac{1}{2\sqrt{3}}$

Answer: C



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Column-I	Column-II
(A) $\lim_{n \rightarrow \infty} \left( \frac{1 + \sqrt[n]{4}}{2} \right)^n =$	(P) 2
(B) Let $f(x) = \lim_{n \rightarrow \infty} \frac{2x}{\pi} \tan^{-1}(nx)$ , then $\lim_{x \rightarrow 0^+} f(x) =$	(Q) 0
(C) $\lim_{x \rightarrow \frac{\pi}{2}^-} \frac{\cos(\tan^{-1}(\tan x))}{x - \frac{\pi}{2}} =$	(R) 1
(D) If $\lim_{x \rightarrow 0^+} (x)^{\frac{1}{\ln \sin x}} = e^L$ , then $L + 2 =$	(S) 3
	(T) Non-existent

1.



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## Exercise Subjective Type Problems

1. If  $\lim_{x \rightarrow 0} \frac{\ln \cot\left(\frac{\pi}{4} - \beta x\right)}{\tan \alpha x} = 1$ , then  $\frac{\alpha}{\beta} = \dots$



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2.

If

$$\lim_{x \rightarrow 0} \frac{f(x)}{\sin^2 x} = 8, \quad \lim_{x \rightarrow 0} \frac{g(x)}{2 \cos x - ye^x + x^3 + x - 2} = \lambda \quad \text{and} \quad \lim_{x \rightarrow 0} (1 + f(x))^{g(x)}$$

then  $\lambda =$



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3. If  $\alpha, \beta$  are the roots of the equation  $x^2 + x + 1 = 0$ , find the value of  $\alpha^3 - \beta^3$ .



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4. The value of

$$\lim_{x \rightarrow 0} \frac{(140)^x - (35)^x - (28)^x - (20)^x + 7^x + 5^x + 4^x - 1}{x \sin^2 x} = 2 \ln 2 \ln k \ln 7$$

, then  $k =$



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5. If  $\lim_{x \rightarrow 0} \frac{a \cos x}{x^2} + \frac{b}{x^2} = \frac{1}{3}$ , then  $b - a =$



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6. Find the value of  $\lim_{x \rightarrow \infty} \left(x + \frac{1}{x}\right) e^{1/x} - x$ .



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7. Find  $\lim_{x \rightarrow a^+} \left[ \frac{\min(\sin x, \{x\})}{x-1} \right]$  where  $\alpha$  is root of equation  $\sin x + 1 = x$  (here  $[.]$  represent greatest integer and  $\{.\}$  represent fractional part function)



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