

## MATHS

### BOOKS - VK JAISWAL ENGLISH

### VECTOR & 3D DIMENSIONAL GEOMETRY

#### Exercise 1 Single Choice Problems

1. If  $ax + by + cz = p$ , then minimum value of  $x^2 + y^2 + z^2$  is

(a)  $\left(\frac{p}{a+b+c}\right)^2$  (b)  $\frac{p^2}{a^2+b^2+c^2}$  (c)  $\frac{a^2+b^2+c^2}{p^2}$  (d)  $\left(\frac{a+b+c}{p}\right)^2$

A.  $\left(\frac{p}{a+b+c}\right)^2$

B.  $\frac{p^2}{a^2+b^2+c^2}$

C.  $\frac{a^2+b^2+c^2}{p^2}$

D. 0

**Answer: B**



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2. If the angle between the vectors  $\vec{a}$  and  $\vec{b}$  is  $\frac{\pi}{3}$  and the area of the triangle with adjacent sides parallel to  $\vec{a}$  and  $\vec{b}$  is 3, then  $a \cdot b$  is

A.  $\sqrt{3}$

B.  $2\sqrt{3}$

C.  $4\sqrt{3}$

D.  $\frac{\sqrt{3}}{2}$

**Answer: B**



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3. A straight line L cuts the sides AB, AC, AD of a parallelogram ABCD at

$B_1, C_1, D_1$  respectively. If  $\vec{AB_1} = \lambda_1 \vec{AB}$ ,

$\vec{AD}_1 = \lambda_2 \vec{AD}$  and  $\vec{AC}_1 = \lambda_3 \vec{AC}$ ,

A.  $\lambda_1, \lambda_3$  and  $\lambda_2$  are in AP

B.  $\lambda_1, \lambda_3$  and  $\lambda_2$  are in GP

C.  $\lambda_1, \lambda_3$  and  $\lambda_2$  are in HP

D.  $\lambda_1 + \lambda_2 + \lambda_3 = 0$

**Answer: C**

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4. Let  $\vec{a} = 2\hat{i} + \hat{j} + \hat{k}$ , and  $\vec{b} = \hat{i} + \hat{j}$  if  $c$  is a vector such that

$\vec{a} \cdot \vec{c} = |\vec{c}|$ ,  $|\vec{c} - \vec{a}| = 2\sqrt{2}$  and the angle between

$\vec{a} \times \vec{b}$  and  $\vec{c}$  is  $30^\circ$ , then  $\left| \left( \vec{a} \times \vec{b} \right) \times \vec{c} \right|$  is equal to

A.  $\frac{2}{3}$

B.  $\frac{3}{2}$

C. 2

D. 3

**Answer: B**



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5. If acute angle between the line  $\vec{r} = \hat{i} + 2\hat{j} + \lambda(4\hat{i} - 3\hat{k})$  and  $xy$ -plane is  $\theta_1$  and acute angle between planes  $x + 2y = 0$  and  $2x + y = 0$  is  $\theta_2$ , then  $(\cos^2 \theta_1 + \sin^2 \theta_2)$  equals to :

A. 1

B.  $\frac{1}{4}$

C.  $\frac{2}{3}$

D.  $\frac{3}{4}$

**Answer: A**



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6. If  $a, b, c, x, y, z$  are real and  $a^2 + b^2 + c^2 = 25, x^2 + y^2 + z^2 = 36$  and  $ax + by + cz = 30$ , then  $\frac{a + b + c}{x + y + z}$  is equal to :
- A. 1
- B.  $\frac{6}{5}$
- C.  $\frac{5}{6}$
- D.  $\frac{3}{4}$

Answer: C

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7. If  $\vec{a}$  and  $\vec{b}$  are non-zero, non-collinear vectors such that  $|\vec{a}| = 2, \vec{a} \cdot \vec{b} = 1$  and angle between  $\vec{a}$  and  $\vec{b}$  is  $\frac{\pi}{3}$ . If  $\vec{r}$  is any vector such that  $\vec{r} \cdot \vec{a} = 2, \vec{r} \cdot \vec{b} = 8, \left( \vec{r} + 2\vec{a} - 10\vec{b} \right) \cdot \left( \vec{a} \times \vec{b} \right) = 4\sqrt{3}$  and

satisfy to  $\vec{r} + 2\vec{a} - 10\vec{b} = \lambda(\vec{a} \times \vec{b})$ , then  $\lambda$  is equal to : (a)  $\frac{1}{2}$  (b)

2 (c)  $\frac{1}{4}$  (d) none of these

A.  $\frac{1}{2}$

B. 2

C.  $\frac{1}{4}$

D. None of these

**Answer: D**



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8. Given  $\vec{a} = 3\hat{i} + 2\hat{j} + 4\hat{k}$ ,  $\vec{b} = 2(\hat{i} + \hat{k})$  and  $\vec{c} = 4\hat{i} + 2\hat{j} + 3\hat{k}$ .

Find for what number of distinct values of  $\alpha$  the equation

$x\vec{a} + y\vec{b} + z\vec{c} = \alpha(x\hat{i} + y\hat{j} + z\hat{k})$  has non-trivial solution (x, y, z).

A. -1

B. 4

C. 7

D. 8

**Answer: C**



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9. If  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} - \hat{j} + \hat{k}$ ,  $\vec{c} = \hat{i} + 2\hat{j} - \hat{k}$ , then the value of

$$\begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c} \\ \vec{c} \cdot \vec{a} & \vec{c} \cdot \vec{b} & \vec{c} \cdot \vec{c} \end{vmatrix} \text{ is equal to :}$$

A. 2

B. 4

C. 16

D. 64

**Answer: C**



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10.  $\vec{a}$  and  $\vec{b}$  are two vectors such that  $|\vec{a}| = 1$ ,  $|\vec{b}| = 4$  and  $\vec{a} \cdot \vec{b} = 2$ . If  $\vec{c} = (2\vec{a} \times \vec{b}) - 3\vec{b}$  then find angle between  $\vec{b}$  and  $\vec{c}$ .

A.  $\frac{\pi}{6}$

B.  $\frac{\pi}{3}$

C.  $\frac{2\pi}{3}$

D.  $\frac{5\pi}{3}$

**Answer: D**



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11. If  $\vec{a}, \vec{b}, \vec{c}$  are unit vectors, then the value of  $|\vec{a} - 2\vec{b}|^2 + |\vec{b} - 2\vec{c}|^2 + |\vec{c} - 2\vec{a}|^2$  does not exceed to : (a) 9 (b) 12 (c) 18 (d) 21



A. 9

B. 12

C. 18

D. 21

**Answer: D**



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12. The adjacent side vectors  $\vec{OA}$  and  $\vec{OB}$  of a rectangle OACB are  $\vec{a}$  and  $\vec{b}$  respectively, where O is the origin. If  $16|\vec{a} \times \vec{b}| = 3\left(|\vec{a}| + |\vec{b}|\right)^2$  and  $\theta$  be the acute angle between the diagonals OC and AB then the value of  $\cos\left(\frac{\theta}{2}\right)$  is : (a)  $\frac{1}{\sqrt{2}}$  (b)  $\frac{1}{2}$  (c)  $\frac{1}{\sqrt{3}}$  (d)  $\frac{1}{3}$

A.  $\frac{1}{\sqrt{2}}$

B.  $\frac{1}{2}$

C.  $\frac{1}{\sqrt{3}}$

D.  $\frac{1}{3}$

**Answer: D**



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13. If vectors  $\overrightarrow{AB} = -3\hat{i} + 4\hat{k}$  and  $\overrightarrow{AC} = 5\hat{i} - 2\hat{j} + 4\hat{k}$  are the sides of a  $\triangle ABC$ , then the length of the median through A is

A.  $\sqrt{288}$

B.  $\sqrt{72}$

C.  $\sqrt{33}$

D.  $\sqrt{18}$

**Answer: C**



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14. If  $\vec{a} = 2\hat{i} + \lambda\hat{j} + 3\hat{k}$ ,  $\vec{b} = 3\hat{i} + 3\hat{j} + 5\hat{k}$ ,  $\vec{c} = \lambda\hat{i} + 2\hat{j} + 2\hat{k}$  are linearly dependent vectors, then the number of possible values of  $\lambda$  is :

- A. 0
- B. 1
- C. 2
- D. More than 2

**Answer: C**



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15. The scalar triple product

$\left[ \vec{a} + \vec{b} - \vec{c} \quad \vec{b} + \vec{c} - \vec{a} \quad \vec{c} + \vec{a} - \vec{b} \right]$  is equal to :

- A. 0
- B.  $\left[ \vec{a} \vec{b} \vec{c} \right]$
- C.  $2 \left[ \vec{a} \vec{b} \vec{c} \right]$

D. 4  $\left[ \vec{a} \vec{b} \vec{c} \right]$

**Answer: D**



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16. If  $\hat{a}$  and  $\hat{b}$  are unit vectors then the vector defined as  $\vec{V} = (\hat{a} \times \hat{b}) \times (\hat{a} + \hat{b})$  is collinear to the vector :

A.  $\hat{a} + \hat{b}$

B.  $\hat{b} - \hat{a}$

C.  $2\hat{a} - \hat{b}$

D.  $\hat{a} + 2\hat{b}$

**Answer: B**



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17. The sine of angle formed by the lateral face ADC and plane of the base ABC of the tetrahedron ABCD, where  $A = (3, -2, 1)$ ,  $B = (3, 1, 5)$ ,  $C = (4, 0, 3)$  and  $D = (1, 0, 0)$ , is :

A.  $\frac{2}{\sqrt{29}}$

B.  $\frac{5}{\sqrt{29}}$

C.  $\frac{3\sqrt{3}}{\sqrt{29}}$

D.  $\frac{-2}{\sqrt{29}}$

**Answer: B**



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18. Let  $\vec{a}_r = x_r \hat{i} + y_r \hat{j} + z_r \hat{k}$ ,  $r = 1, 2, 3$  three mutually perpendicular

unit vectors then the value of  $\begin{vmatrix} x_1 & x_2 & x_3 \\ y_1 & y_2 & y_3 \\ z_1 & z_2 & z_3 \end{vmatrix}$  is equal to

A. 0

B.  $\pm 1$

C.  $\pm 2$

D.  $\pm 4$

**Answer: B**



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19. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three non-coplanar vectors and  $\vec{r}$  be any arbitrary vector. Then

$(\vec{a} \times \vec{b}) \times (\vec{r} \times \vec{c}) + (\vec{b} \times \vec{c}) \times (\vec{r} \times \vec{a}) + (\vec{c} \times \vec{a}) \times (\vec{r} \times \vec{b})$  is always equal to  $\left[ \vec{a} \ \vec{b} \ \vec{c} \right] \vec{r}$  b.  $2 \left[ \vec{a} \ \vec{b} \ \vec{c} \right] \vec{r}$  c.  $3 \left[ \vec{a} \ \vec{b} \ \vec{c} \right] \vec{r}$  d. none of these

A.  $\left[ \vec{a} \ \vec{b} \ \vec{c} \right] \vec{r}$

B.  $2 \left[ \vec{a} \ \vec{b} \ \vec{c} \right] \vec{r}$

C.  $4 \left[ \vec{a} \ \vec{b} \ \vec{c} \right] \vec{r}$

D.  $\vec{0}$

**Answer: B**



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20. E and F are the interior points on the sides BC and CD of a parallelogram ABCD. Let  $\overrightarrow{BE} = 4\overrightarrow{EC}$  and  $\overrightarrow{CF} = 4\overrightarrow{FD}$ . If the line EF meets the diagonal AC in G, then  $\overrightarrow{AG} = \lambda\overrightarrow{AC}$ , where  $\lambda$  is equal to :

A.  $\frac{1}{3}$

B.  $\frac{21}{25}$

C.  $\frac{7}{13}$

D.  $\frac{21}{5}$

**Answer: B**



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21. If  $\hat{a}, \hat{b}$  are unit vectors and  $\vec{c}$  is such that  $\vec{c} = \vec{a} \times \vec{c} + \vec{b}$ , then the maximum value of  $\left[ \vec{a} \vec{b} \vec{c} \right]$  is :

A. 1

B.  $\frac{1}{2}$

C. 2

D.  $\frac{3}{2}$

**Answer: B**



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22. Consider the matrices  $A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 1 & 2 \\ 1 & -1 & 1 \end{bmatrix}$   $B = \begin{bmatrix} 2 & 1 & 3 \\ 4 & 1 & -1 \\ 2 & 2 & 3 \end{bmatrix}$   
 $C = \begin{bmatrix} 14 \\ 12 \\ 2 \end{bmatrix}$   $D = \begin{bmatrix} 13 \\ 11 \\ 14 \end{bmatrix}$ . Now  $x = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$  is such that solutions of equation  $AX = C$  and  $BX = D$  represent two points L and M



respectively in 3 dimensional space. If  $L'$  and  $M'$  are hre reflections of L and M in the plane  $x+y+z=9$  then find coordinates of L,M,L',M'

A. (3, 4, 2)

B. (5, 3, 4)

C. (7, 2, 3)

D. (1, 5, 6)

**Answer: A**



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23. The value of  $\alpha$  for which point  $M(\alpha\hat{i} + 2\hat{j} + \hat{k})$ , lie in the plane containing three points  $A(\hat{i} + \hat{j} + \hat{k})$  and  $C(3\hat{i} - \hat{k})$  is :

A. 1

B. 2

C.  $\frac{1}{2}$

D.  $-\frac{1}{2}$

**Answer: B**

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24. Q is the image of point P(1, -2, 3) with respect to the plane  $x - y + z = 7$ . The distance of Q from the origin is :

A.  $\sqrt{\frac{70}{3}}$

B.  $\frac{1}{2}\sqrt{\frac{70}{3}}$

C.  $\sqrt{\frac{35}{3}}$

D.  $\sqrt{\frac{15}{2}}$

**Answer: A**

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25.  $\hat{a}$ ,  $\hat{b}$  and  $\hat{a} - \hat{b}$  are unit vectors. The volume of the parallelepiped, formed with  $\hat{a}$ ,  $\hat{b}$  and  $\hat{a} \times \hat{b}$  as coterminous edges is :

A. 1

B.  $\frac{1}{4}$

C.  $\frac{2}{3}$

D.  $\frac{3}{4}$

**Answer: D**



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26. A line passing through P(3, 7, 1) and R(2, 5, 7) meet the plane  $3x + 2y + 11z - 9 = 0$  at Q. Then PQ is equal to :

A.  $\frac{5\sqrt{41}}{59}$

B.  $\frac{\sqrt{41}}{59}$

C.  $\frac{50\sqrt{41}}{59}$

D.  $\frac{25\sqrt{41}}{59}$

**Answer: D**



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27. Let  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  be three non-zero non coplanar vectors and  $\vec{p}$ ,  $\vec{q}$  and  $\vec{r}$  be three vectors given by  $\vec{p} = \vec{a} + \vec{b} - 2\vec{c}$ ,  $\vec{q} = 3\vec{a} - 2\vec{b} + \vec{c}$  and  $\vec{r} = \vec{a} - 4\vec{b} + 2\vec{c}$

If the volume of the parallelepiped determined by  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  is  $V_1$  and that of the parallelepiped determined by  $\vec{p}$ ,  $\vec{q}$  and  $\vec{r}$  is  $V_2$ , then

$V_2 : V_1 =$

A. 10

B. 15

C. 20

D. None of these

**Answer: B**



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28. The two lines  $x = ay + b, z = cy + d$  and  $x = a'y + b', z = c'y + d'$  are perpendicular to each other if

- A. 1
- B. 2
- C. 3
- D. 4

Answer: A



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29. The perpendicular distance between the line  $\vec{r} = 2\hat{i} - 2\hat{j} + 3\hat{k} + \lambda(\hat{i} - \hat{j} + 4\hat{k})$  and the plane  $\vec{r} \cdot (\hat{i} + 5\hat{j} + \hat{k}) = 5$  is :

A.  $\frac{10}{9}$

B.  $\frac{10}{3\sqrt{3}}$

C.  $\frac{3}{10}$

D.  $\frac{10}{3}$

**Answer: B**



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30. If  $(\vec{a} \times \vec{b}) \times \vec{c} = \vec{a} \times (\vec{b} \times \vec{c})$ , where  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are any three vectors such that  $\vec{a} \cdot \vec{b} \neq 0$ ,  $\vec{b} \cdot \vec{c} \neq 0$ , then  $\vec{a}$  and  $\vec{c}$  are :

A. Inclined at an angle of  $\frac{\pi}{3}$

B. Inclined at an angle of  $\frac{\pi}{6}$

C. Perpendicular

D. Parallel

**Answer: D**



A.  $64 \vec{a}$

B.  $64 \vec{b}$

C.  $-64 \vec{a}$

D.  $-64 \vec{b}$

**Answer: D**

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**33.** If O (origin) is a point inside the triangle PQR such that

$\vec{OP} + k_1 \vec{OQ} + k_2 \vec{OR} = 0$ , where  $k_1, k_2$  are constants such that

$\frac{\text{Area}(\Delta PQR)}{\text{Area}(\Delta OQR)} = 4$ , then the value of  $k_1 + k_2$  is :

A. 2

B. 3

C. 4

D. 5



**Answer: B**



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**34.** Let PQ and QR be diagonals of adjacent faces of a rectangular box, with its centre at O. If  $\angle QOR$ ,  $\angle ROP$  and  $\angle POQ$  are  $\theta$ ,  $\phi$  and  $\Psi$  respectively then the value of ' $\cos \theta + \cos \phi + \cos \Psi$ ' is :

A. -2

B.  $-\sqrt{3}$

C. -1

D. 0

**Answer: C**



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35.

If

$$\vec{r} = a(\vec{m} \times \vec{n}) + b(\vec{n} \times \vec{l}) + c(\vec{l} \times \vec{m}) \text{ and } [\vec{l} \vec{m} \vec{n}] = 4, \text{ find}$$

:

A.  $\frac{1}{4}$

B.  $\frac{1}{2}$

C. 1

D. 2

**Answer: A**



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36. The volume of tetrahedron, for which three co-terminous edges are

$$\vec{a} - \vec{b}, \vec{b} + 2\vec{c} \text{ and } 3\vec{a} - \vec{c} \text{ is : (a) } 6k \text{ (b) } 7k \text{ (c) } 30k \text{ (d) } 42k$$

A. 6k

B. 7k

C. 30k

D. 42k

**Answer: D**



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**37.** The equation of a plane passing through the line of intersection of the planes :

$x + 2y + z - 10 = 0$  and  $3x + y - z = 5$  and passing through the origin is :

A.  $5x + 3z = 0$

B.  $5x - 3z = 0$

C.  $5x + 4y + 3z = 0$

D.  $5x - 4y + 3z = 0$

**Answer: B**

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**38.** Find the locus of a point whose distance from  $x$ -axis is twice the distance from the point  $(1, -1, 2)$

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### Exercise 2 One Or More Than One Answer Is Are Correct

**1.** If equation of three lines are :

$$\frac{x}{1} = \frac{y}{2} = \frac{z}{3}, \frac{x}{2} = \frac{y}{1} = \frac{z}{3} \text{ and } \frac{x-1}{1} = \frac{2-y}{1} = \frac{z-3}{0}, \text{ then}$$

which of the following statement(s) is/are correct ?

- A. Triangle formed by the line is equilateral
- B. Triangle formed by the lines is isosceles
- C. Equation of the plane containing the lines is  $x + y = z$

D. Area of the triangle formed by the lines is  $\frac{3\sqrt{3}}{2}$

Answer: B::C::D



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2.

If

$\vec{a} = \hat{i} + 6\hat{j} + 3\hat{k}$ ,  $\vec{b} = 3\hat{i} + 2\hat{j} + \hat{k}$  and  $\vec{c} = (\alpha + 1)\hat{i} + (\beta - 1)\hat{j} + \hat{k}$

are linearly dependent vectors and  $|\vec{c}| = \sqrt{6}$ , then the possible value(s)

of  $(\alpha + \beta)$  can be : (a) 1 (b) 2 (c) 3 (d) 4

A. 1

B. 2

C. 3

D. 4

Answer: A::C



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3. Consider the lines :

$$L_1: \frac{x-2}{1} = \frac{y-1}{7} = \frac{z+2}{-5}$$

$$L_2: x-4 = y+3 = -z$$

Then which of the following is/are correct ?

A. Point of intersection of  $L_1$  and  $L_2$  is  $(1, -6, 3)$

B. Equation of plane containing  $L_1$  and  $L_2$  is  $x + 2y + 3z + 2 = 0$

C. Acute angle between  $L_1$  and  $L_2$  is  $\cot^{-1}\left(\frac{13}{15}\right)$

D. Equation of plane containing  $L_1$  and  $L_2$  is  $x + 2y + 2z + 3 = 0$

Answer: A::B::C



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4. Let  $\hat{a}$ ,  $\hat{b}$  and  $\hat{c}$  be three unit vectors such that  $\hat{a} = \hat{b} + (\hat{b} \times \hat{c})$ , then the possible value(s) of  $|\hat{a} + \hat{b} + \hat{c}|^2$  can be :

A. 1

B. 4

C. 16

D. 9

**Answer: A::D**



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5. The value(s) of  $\mu$  for which the straight lines

$$\vec{r} = 3\hat{i} - 2\hat{j} - 4\hat{k} + \lambda_1(\hat{i} - \hat{j} + \mu\hat{k}) \quad \text{and}$$

$$\vec{r} = 5\hat{i} - 2\hat{j} + \hat{k} + \lambda_2(\hat{i} + \mu\hat{j} + 2\hat{k}) \text{ are coplanar is/are :}$$

A.  $\frac{5 + \sqrt{33}}{4}$

B.  $\frac{-5 + \sqrt{33}}{4}$

C.  $\frac{5 - \sqrt{33}}{4}$

D.  $\frac{-5 - \sqrt{33}}{4}$

**Answer: A::C**

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6.

If

$$\hat{i} \times [(\vec{a} - \hat{j}) \times \hat{i}] + \hat{j} \times [(\vec{a} - \hat{k}) \times \hat{j}] + \hat{k} \times [(\vec{a} - \hat{i}) \times \hat{k}] = 0 \text{ and}$$

, then :

A.  $x + y = 1$

B.  $y + z = \frac{1}{2}$

C.  $x + z = 1$

D. None of these

**Answer: A:C**[Watch Video Solution](#)7.  $\left[ \vec{a} \times \vec{b} \quad \vec{c} \times \vec{d} \quad \vec{e} \times \vec{f} \right]$  is equal to

(a)  $\begin{bmatrix} \vec{a} & \vec{b} & \vec{d} \\ \vec{c} & \vec{e} & \vec{f} \end{bmatrix} - \begin{bmatrix} \vec{a} & \vec{b} & \vec{c} \\ \vec{d} & \vec{e} & \vec{f} \end{bmatrix}$

(b)  $\begin{bmatrix} \vec{a} & \vec{b} & \vec{e} \\ \vec{f} & \vec{c} & \vec{d} \end{bmatrix} - \begin{bmatrix} \vec{a} & \vec{b} & \vec{f} \\ \vec{e} & \vec{c} & \vec{d} \end{bmatrix}$



$$(c) \begin{bmatrix} \vec{c} & \vec{d} & \vec{a} \end{bmatrix} \begin{bmatrix} \vec{b} & \vec{e} & \vec{f} \end{bmatrix} - \begin{bmatrix} \vec{a} & \vec{d} & \vec{b} \end{bmatrix} \begin{bmatrix} \vec{a} & \vec{e} & \vec{f} \end{bmatrix}$$

$$(d) \begin{bmatrix} \vec{a} & \vec{c} & \vec{e} \end{bmatrix} \begin{bmatrix} \vec{b} & \vec{d} & \vec{f} \end{bmatrix}$$

$$A. \begin{bmatrix} \vec{a} & \vec{b} & \vec{d} \end{bmatrix} \begin{bmatrix} \vec{c} & \vec{e} & \vec{f} \end{bmatrix} - \begin{bmatrix} \vec{a} & \vec{b} & \vec{c} \end{bmatrix} \begin{bmatrix} \vec{d} & \vec{e} & \vec{f} \end{bmatrix}$$

$$B. \begin{bmatrix} \vec{a} & \vec{b} & \vec{e} \end{bmatrix} \begin{bmatrix} \vec{f} & \vec{c} & \vec{d} \end{bmatrix} - \begin{bmatrix} \vec{a} & \vec{b} & \vec{f} \end{bmatrix} \begin{bmatrix} \vec{e} & \vec{c} & \vec{d} \end{bmatrix}$$

$$C. \begin{bmatrix} \vec{c} & \vec{d} & \vec{a} \end{bmatrix} \begin{bmatrix} \vec{b} & \vec{e} & \vec{f} \end{bmatrix} - \begin{bmatrix} \vec{c} & \vec{d} & \vec{b} \end{bmatrix} \begin{bmatrix} \vec{a} & \vec{e} & \vec{f} \end{bmatrix}$$

$$D. \begin{bmatrix} \vec{b} & \vec{c} & \vec{d} \end{bmatrix} \begin{bmatrix} \vec{a} & \vec{e} & \vec{f} \end{bmatrix} - \begin{bmatrix} \vec{b} & \vec{c} & \vec{f} \end{bmatrix} \begin{bmatrix} \vec{a} & \vec{e} & \vec{d} \end{bmatrix}$$

**Answer: A::B::C**



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8. If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  &  $\vec{d}$  are position vector of point A, B, C and D respectively in 3-D space no three of A, B, C, D are colinear and satisfy the relation  $3\vec{a} - 2\vec{b} + \vec{c} - 2\vec{d} = 0$  then (a) A, B, C and D are coplanar (b) The line joining the points B and D divides the line joining the point A and C in the ratio of 2: 1 (c) The line joining the points A and C divides the line joining the points B and D in the ratio of 1:1 (d) The four vectors  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$  are linearly dependent .

A. A, B, C and D are coplanar

B. The line joining the points B and D divides the line joining the point A and C in the ratio of 2: 1

C. The line joining the points A and C divides the line joining the points B and D in the ratio of 1: 1

D. The four vectors  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  and  $\vec{d}$  are linearly dependent .

**Answer: A::C::D**



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9.  $\vec{a}$  and  $\vec{c}$  are unit vectors and  $|\vec{b}| = 4$  the angle between  $\vec{a}$  and  $\vec{b}$  is  $\cos^{-1}(1/4)$  and  $\vec{b} - 2\vec{c} = \lambda\vec{a}$  the value of  $\lambda$  is

A. 2

B. -3

C. 3

D. -4

Answer: C::D

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10. Consider the lines  $x = y = z$  and line  $2x + y + z - 1 = 0 = 3x + y + 2z - 2$ , then

A. The shortest distance between the two lines is  $\frac{1}{\sqrt{2}}$

B. The shortest distance between the two lines is  $\sqrt{2}$

C. Plane containing the line  $L_2$  and parallel to line  $L_1$  is

$$z - x + 1 = 0$$

D. Perpendicular distance of origin from plane containing line  $L_2$  and

parallel to line  $L_1$  is  $\frac{1}{\sqrt{2}}$

Answer: A::D

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11. If  $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) = h\vec{a} + k\vec{b} = r\vec{c} + s\vec{d}$ , where  $\vec{a}, \vec{b}$  are non-collinear and  $\vec{c}, \vec{d}$  are also non-collinear then :

A.  $\pi^2$

B.  $\frac{5\pi^2}{4}$

C.  $\frac{35\pi^2}{4}$

D.  $\frac{37\pi^2}{4}$

Answer: B::D



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12. If  $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) = h\vec{a} + k\vec{b} = r\vec{c} + s\vec{d}$ , where  $\vec{a}, \vec{b}$  are non-collinear and  $\vec{c}, \vec{d}$  are also non-collinear then :

A.  $h = \begin{bmatrix} \vec{a} & \vec{c} & \vec{d} \\ \vec{b} & \vec{c} & \vec{d} \end{bmatrix}$

B.  $k = \begin{bmatrix} \vec{a} & \vec{c} & \vec{d} \\ \vec{a} & \vec{c} & \vec{d} \end{bmatrix}$

$$C. r = \begin{bmatrix} \vec{a} & \vec{b} & \vec{d} \end{bmatrix}$$

$$D. s = - \begin{bmatrix} \vec{a} & \vec{b} & \vec{c} \end{bmatrix}$$

**Answer: B::C::D**



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13. Let  $a$  be a real number and  $\vec{\alpha} = \hat{i} + 2\hat{j}$ ,  $\vec{\beta} = 2\hat{i} + a\hat{j} + 10\hat{k}$ ,  $\vec{\gamma} = 12\hat{i} + 20\hat{j} + a\hat{k}$  be three vectors, then  $\vec{\alpha}$ ,  $\vec{\beta}$  and  $\vec{\gamma}$  are linearly independent for :

A.  $a > 0$

B.  $a < 0$

C.  $a = 0$

D. No value of  $a$

**Answer: A::B::C**



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14. The volume of a right triangular prism  $ABCA_1B_1C_1$  is equal to 3 cubic unit. Then the co-ordinates of the vertex  $A_1$ , if the co-ordinates of the base vertices of the prism are  $A(1,0,1)$ ,  $B(2,0,0)$  and  $C(0,1,0)$ , are

A.  $(2, 2, 2)$

B.  $(0, 2, 0)$

C.  $(0, -2, 2)$

D.  $(0, -2, 0)$

**Answer: A:D**

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15. If  $\vec{a} = x\hat{i} + y\hat{j} + z\hat{k}$ ,  $\vec{b} = y\hat{i} + z\hat{j} + x\hat{k}$  and  $\vec{c} = z\hat{i} + x\hat{j} + y\hat{k}$ , then  $\vec{a} \times (\vec{b} \times \vec{c})$  is

(a) parallel to  $(y - z)\hat{i} + (z - x)\hat{j} + (x - y)\hat{k}$  (b) orthogonal to

- $\hat{i} + \hat{j} + \hat{k}$  (c)orthogonal to  $(y + z)\hat{i} + (z + x)\hat{j} + (x + y)\hat{k}$
- (d)orthogonal to  $x\hat{i} + y\hat{j} + z\hat{k}$
- A. Parallel to  $(y - z)\hat{i} + (z - x)\hat{j} + (x - y)\hat{k}$
- B. Orthogonal to  $\hat{i} + \hat{j} + \hat{k}$
- C. Orthogonal to  $(y + z)\hat{i} + (z + x)\hat{j} + (x + y)\hat{k}$ ,
- D. Orthogonal to  $x\hat{i} + y\hat{j} + z\hat{k}$

**Answer: A::B::C::D**



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**16.** If a line has a vector equation,  $\vec{r} = 2\hat{i} + 6\hat{j} + \lambda(\hat{i} - 3\hat{j})$  then which of the following statements holds good ?

- A. the line is parallel to  $2\hat{i} + 6\hat{j}$
- B. the line passes through the point  $3\hat{i} + 3\hat{j}$
- C. the line passes through the point  $\hat{i} + 9\hat{j}$

D. the line is parallel to  $xy$  plane

**Answer: B::C::D**



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17. Let  $M, N, P$  and  $Q$  be the mid points of the edges  $AB, CD, AC$  and  $BD$  respectively of the tetrahedron  $ABCD$ . Further,  $MN$  is perpendicular to both  $AB$  and  $CD$  and  $PQ$  is perpendicular to both  $AC$  and  $BD$ . Then which of the following is/are correct:

A.  $AB = CD$

B.  $BC = DA$

C.  $AC = BD$

D.  $AN = BN$

**Answer: A::B::C::D**



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18. The solution vectors  $\vec{r}$  of the equation  $\vec{r} \times \hat{i} = \hat{j} + \hat{k}$  and  $\vec{r} \times \hat{j} = \hat{k} + \hat{j}$  represent two straight lines which are :

- A. Intersecting
- B. Non coplanar
- C. Coplanar
- D. Non intersecting

**Answer: B::D**



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19. The lines with vector equations are,  $\vec{r}_1 = 3\hat{i} + 6\hat{j} + \lambda(-4\hat{i} + 3\hat{j} + 2\hat{k})$  and  $\vec{r}_2 = -2\hat{i} + 7\hat{j} + \mu(-4\hat{i} + \dots)$  are such that :

- A. they are coplanar

B. they do not intersect

C. they are skew

D. the angle between them is  $\tan^{-1}(3/7)$

**Answer: B::C::D**



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### Exercise 3 Comprehension Type Problems

1. The vertices of  $\Delta ABC$  are  $(2, 0, 0)$ ,  $B(0, 1, 0)$ ,  $C(0, 0, 2)$ . Its orthocentre is H and circumcentre is S. P is a point equidistant from A, B, C and the origin O.

Q. The z-coordinate of H is :

A. 1

B.  $1/2$

C.  $1/6$

D.  $1/3$

**Answer: D**



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2. The vertices of  $\triangle ABC$  are  $(2, 0, 0)$ ,  $B(0, 1, 0)$ ,  $C(0, 0, 2)$ . Its orthocentre is H and circumcentre is S. P is a point equidistant from A, B, C and the origin O.

Q. The y-coordinate of S is :

A.  $5/6$

B.  $1/3$

C.  $1/6$

D.  $1/2$

**Answer: C**



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3. The vertices of  $\Delta ABC$  are  $(2, 0, 0)$ ,  $B(0, 1, 0)$ ,  $C(0, 0, 2)$ . Its orthocentre is H and circumcentre is S. P is a point equidistant from A, B, C and the origin O.

Q. PA is equal to :

A. 1

B.  $\sqrt{2}$

C.  $\sqrt{\frac{3}{2}}$

D.  $\frac{3}{2}$

**Answer: D**



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4. Consider a plane  $\pi: \vec{r} \cdot \vec{n} = d$  (where  $\vec{n}$  is not a unit vector). There are two points  $A(\vec{a})$  and  $B(\vec{b})$  lying on the same side of the plane.

Q. If foot of perpendicular from A and B to the plane  $\pi$  are P and Q respectively, then length of PQ be :

A.  $\frac{\left| \left( \vec{b} - \vec{a} \right) \cdot \vec{n} \right|}{\left| \vec{n} \right|}$

B.  $\left| \left( \vec{b} - \vec{a} \right) \cdot \vec{n} \right|$

C.  $\frac{\left| \left( \vec{b} - \vec{a} \right) \times \vec{n} \right|}{\left| \vec{n} \right|}$

D.  $\left| \left( \vec{b} - \vec{a} \right) \times \vec{n} \right|$

**Answer: C**



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5. Consider a plane  $\pi: \vec{r} \cdot \vec{n} = d$  (where  $\vec{n}$  is not a unit vector). There are two points  $A(\vec{a})$  and  $B(\vec{b})$  lying on the same side of the plane.

Q. If foot of perpendicular from A and B to the plane  $\pi$  are P and Q respectively, then length of PQ be :

A.  $\vec{a} + \frac{2}{(\vec{n})^2} (d - \vec{a} \cdot \vec{n}) \vec{n}$

B.  $\vec{a} - \frac{1}{(\vec{n})^2} (d - \vec{a} \cdot \vec{n}) \vec{n}$

$$C. \vec{a} + \frac{2}{(\vec{n})^2} (d + \vec{a} \cdot \vec{n}) \vec{n}$$

$$D. \vec{a} + \frac{2}{(\vec{n})^2} \vec{n}$$

**Answer: A**

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6. Consider a plane  $\pi: \vec{r} \cdot \vec{n} = d$  (where  $\vec{n}$  is not a unit vector). There are two points  $A(\vec{a})$  and  $B(\vec{b})$  lying on the same side of the plane.

Q. If foot of perpendicular from A and B to the plane  $\pi$  are P and Q respectively, then length of PQ be :

$$A. \frac{\left| (\vec{a} - \vec{b}) \cdot \vec{n} \right|}{|\vec{n}|}$$

$$B. \left| (\vec{a} - \vec{b}) \cdot \vec{n} \right|$$

$$C. \left| (\vec{a} - \vec{b}) \times \vec{n} \right|$$

$$D. \frac{\left| (\vec{a} - \vec{b}) \times \vec{n} \right|}{|\vec{n}|}$$

**Answer: A**



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7. Consider a plane  $\Pi: \vec{r} \cdot (2\hat{i} + \hat{j} - \hat{k}) = 5$ , a line  $L_1: \vec{r} = (3\hat{i} - \hat{j} + 2\hat{k}) + \lambda(2\hat{i} - 3\hat{j} - \hat{k})$  and a point  $a(3, -4, 1)$ .  $L_2$  is a line passing through A intersecting  $L_1$  and parallel to plane  $\Pi$ .

Q. Equation of  $L_2$  is :

A.  $\vec{r} = (1 + \lambda)\hat{i} + (2 - 3\lambda)\hat{j} + (1 - \lambda)\hat{k}; \lambda \in R$

B.  $\vec{r} = (3 + \lambda)\hat{i} - (4 - 2\lambda)\hat{j} + (1 + 3\lambda)\hat{k}, \lambda \in R$

C.  $\vec{r} = (3 + \lambda)\hat{i} - (4 + 3\lambda)\hat{j} + (1 - \lambda)\hat{k}, \lambda \in R$

D. None of the above

**Answer: C**



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8. Consider a plane  $\Pi : \vec{r} \cdot (2\hat{i} + \hat{j} - \hat{k}) = 5$ , a line  $L_1 : \vec{r} = (3\hat{i} - \hat{j} + 2\hat{k}) + \lambda(2\hat{i} - 3\hat{j} - \hat{k})$  and a point  $a(3, -4, 1) \cdot L_2$  is a line passing through A intersecting  $L_1$  and parallel to plane  $\Pi$ .

Q. Plane containing  $L_1$  and  $L_2$  is :

- A. parallel to yz-plane
- B. parallel to x-axis
- C. parallel to y-axis
- D. passing through origin

**Answer: B**

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9. Consider three planes :

$$2x + py + 6z = 8, x + 2y + qz = 5 \text{ and } x + y + 3z = 4$$

Q. Three planes do not have any common point of intersection if :



A.  $p = 2, q \neq 3$

B.  $p \neq 2, q \neq 3$

C.  $p \neq 2, q = 3$

D.  $p = 2, q = 3$

**Answer: B**



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**10.** Consider three planes :

$$2x + py + 6z = 8, x + 2y + qz = 5 \text{ and } x + y + 3z = 4$$

Q. Three planes do not have any common point of intersection if :

A.  $p = 2, q \neq 3$

B.  $p \neq 2, q \neq 3$

C.  $p \neq 2, q = 3$

D.  $p = 2, q = 3$

**Answer: C**



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11. Consider a tetrahedron  $D - ABC$  with position vectors of its angular points as

$A(1, 1, 1), B(1, 2, 3), C(1, 1, 2)$

and centre of tetrahedron  $\left(\frac{3}{2}, \frac{3}{4}, 2\right)$ .

Q. Shortest distance between the skew lines AB and CD :

A.  $\frac{1}{2}$

B.  $\frac{1}{3}$

C.  $\frac{1}{4}$

D.  $\frac{1}{5}$

**Answer: B**



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12. Consider a tetrahedron  $D - ABC$  with position vectors if its angular points as

$A(1, 1, 1), B(1, 2, 3), C(1, 1, 2)$

and centre of tetrahedron  $\left(\frac{3}{2}, \frac{3}{4}, 2\right)$ .

Q. If N be the foot of the perpendicular from point D on the plane face ABC then the position vector of N are :

A.  $(-1, 1, 2)$

B.  $(1, -1, 2)$

C.  $(1, 1, -2)$

D.  $(-1, -1, 2)$

**Answer: B**



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13. In a triangle AOB, R and Q are the points on the side OB and AB respectively such that  $3OR = 2RB$  and  $2AQ = 3QB$ . Let OQ and AR intersect

at the point P (where O is origin).

Q. If the point P divides OQ in the ratio of  $\mu : 1$ , then  $\mu$  is :

A.  $\frac{2}{19}$

B.  $\frac{2}{17}$

C.  $\frac{2}{15}$

D.  $\frac{10}{9}$

**Answer: D**



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### Exercise 5 Subjective Type Problems

1. If  $\hat{a}$ ,  $\hat{b}$  and  $\hat{c}$  are non-coplanar unit vectors such that  $[\hat{a}\hat{b}\hat{c}] = [\hat{b} \times \hat{c} \quad \hat{c} \times \hat{a} \quad \hat{a} \times \hat{b}]$ , then find the projection of  $\hat{b} + \hat{c}$  on  $\hat{a} \times \hat{b}$ .



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2. If  $M$  is the matrix  $\begin{bmatrix} 1 & -3 \\ -1 & 1 \end{bmatrix}$  then find matrix  $\sum_{r=0}^{\infty} \left(\frac{-1}{3}\right)^r M^{r+1}$

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3. A sequence of  $2 \times 2$  matrices  $\{M_n\}$  is defined as follows

$$M_n = \begin{bmatrix} \frac{1}{(2n+1)!} & \frac{1}{(2n+2)!} \\ \sum_{k=0}^n \frac{(2n+2)!}{(2k+2)!} & \sum_{k=0}^n \frac{(2n+1)!}{(2k+1)!} \end{bmatrix} \quad \text{then}$$

$$\lim_{n \rightarrow \infty} \det. (M_n) = \lambda - e^{-1}. \text{ Find } \lambda.$$

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4. Let  $|\vec{a}| = 1$ ,  $|\vec{b}| = 1$  and  $|\vec{a} + \vec{b}| = \sqrt{3}$ . If  $\vec{c}$  be a vector such that  $\vec{c} = \vec{a} + 2\vec{b} - 3(\vec{a} \times \vec{b})$  and  $p = \left| (\vec{a} \times \vec{b}) \times \vec{c} \right|$ , then find  $[p^2]$ . (where  $[ ]$  represents greatest integer function).

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5. Let  $\vec{r} = (\vec{a} \times \vec{b}) \sin x + (\vec{b} \times \vec{c}) \cos y + 2(\vec{c} \times \vec{a})$ , where  $\vec{a}, \vec{b}, \vec{c}$  are non-zero and non-coplanar vectors. If  $\vec{r}$  is orthogonal to  $\vec{a} + \vec{b} + \vec{c}$ , then find the minimum value of  $\frac{4}{\pi^2} (x^2 + y^2)$ .

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6. The plane denoted by  $P_1: 4x + 7y + 4z + 81 = 0$  is rotated through a right angle about its line of intersection with plane  $P_2: 5x + 3y + 10z = 25$ . If the plane in its new position be denoted by P, and the distance of this plane from the origin is d, then the value of  $\left[ \frac{k}{2} \right]$  (where [.] represents greatest integer less than or equal to k) is....

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7. ABCD is a regular tetrahedron, A is the origin and B lies on x-axis. ABC lies in the xy-plane  $\left| \overrightarrow{AB} \right| = 2$  Under these conditions, the number of possible tetrahedrons is :

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8. A, B, C, D are four points in the space and satisfy  $|\vec{AB}| = 3$ ,  $|\vec{BC}| = 7$ ,  $|\vec{CD}| = 11$  and  $|\vec{DA}| = 9$ . Then find the value of  $\vec{AC} \cdot \vec{BD}$ .

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9. Let OABC be a regular tetrahedron of edge length unity. Its volume be V and  $6V = \sqrt{\frac{p}{q}}$  where p and q are relatively prime. The find the value of  $(p + q)$ .

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10. If  $\vec{a}$  and  $\vec{b}$  are non zero, non collinear vectors and  $\vec{a}_1 = \lambda \vec{a} + 3 \vec{b}$ ,  $\vec{b}_1 = 2 \vec{a} + \lambda \vec{b}$ ,  $\vec{c}_1 = \vec{a} + \vec{b}$ . Find the sum of all possible real values of  $\lambda$  so that points  $A_1, B_1, C_1$  whose position vectors are  $\vec{a}_1, \vec{b}_1, \vec{c}_1$  respectively are collinear is equal to.



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11. Let P and Q are two points on curve  $y = \log_{\frac{1}{2}}\left(x - \frac{1}{2}\right) + \log_2 \sqrt{4x^2 - 4x + 1}$  and P is also on  $x^2 + y^2 = 10$ . Q lies inside the given circle such that its abscissa is integer. Find the smallest possible value of  $\vec{OP} \cdot \vec{OQ}$  where 'O' being origin.



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12. If  $a, b, c, l, m, n \in \mathbb{R} - \{0\}$  such that  $al + bm + cn = 0, bl + cm + an = 0, cl + am + bn = 0$ . If a, b, c are distinct and  $f(x) = ax^3 + bx^2 + cx + 2$ . Find  $f(1)$ .



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13. Let  $\vec{u}$  and  $\vec{v}$  be unit vectors such that  $\vec{u} \times \vec{v} + \vec{u} = \vec{w}$  and  $\vec{w} \times \vec{u} = \vec{v}$ . Find the value of  $[\vec{u} \vec{v} \vec{w}]$ .



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