



MATHS

BOOKS - ARIHANT MATHS (ENGLISH)

DIFFERENTIAL EQUATION

Example

1. Find the order and degree (if defined) of the following differential

equations $\left(\frac{d^3y}{dx^3}\right)^{2/3} = \frac{dy}{dx} + 2$



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2. Write order and degree (if defined) of each of the following differential

equations.

$$\frac{d^3y}{dx^3} + 2\frac{d^2y}{dx^2} + \frac{dy}{dx} = 0$$



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3. Form the differential equation, if $y^2 = 4a(x + a)$, where a is arbitrary constant.



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4. Find the differential equation of $xy = ae^x + be^{-x}$.



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5. Find the differential equation whose solution represents the family :

$$c(y + c)^2 = x^3$$



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6. Find the differential equation whose solution represents the family

$$y = ae^{3x} + be^x.$$

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7. Find the order of the family of curves $y = (c_1 + c_2)e^x + c_3e^{x+c_4}$

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8. The differential equation of all non-horizontal lines in a plane is given

by (i) $\frac{d^2y}{dx^2} = 0$ (ii) $\frac{d^2y}{dy^2} = 0$ (iii) $\frac{d^2y}{dx^2} = 0$ and $\frac{d^2y}{dy^2} = 0$ (iv) All of these

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9. The differential equation of all non-rectical lines in a plane is given by

(i) $\frac{d^2y}{dx^2} = 0$
(ii) $\frac{d^2x}{dy^2} = 0$

(iii) $\frac{d^2x}{dy^2} = 0$ and $\frac{d^2y}{dx^2} = 0$

(iv) All of these



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10. The differential equation of all straight lines which are at a constant distance p from the origin, is

(a) $(y + xy_1)^2 = p^2(1 + y_1^2)$

(b) $(y - xy_1^2) = p^2(1 + y_1)^2$

(c) $(y - xy_1)^2 = p^2(1 + y_1^2)$

(d) None of these



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11. The differential equation of all circles of radius r , is given by

(a) $\{1 + (y_1)^2\}^2 = r^2 y_2^3$

(b) $\{1 + (y_1)^2\}^3 = r^2 y_2^3$

$$(c) \left\{ 1 + (y_1)^2 \right\}^3 = r^2 y_2^2$$

(d) None of these



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12. The differential equations of all circle touching the x-axis at origin is

$$(a) (y^2 - x^2) = 2xy \left(\frac{dy}{dx} \right)$$

$$(b) (x^2 - y^2) \frac{dy}{dx} = 2xy$$

$$(c) (x^2 - y^2) = 2xy \left(\frac{dy}{dx} \right)$$

(d) None of these



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13. The differential equation of all circle in the first quadrant touch the coordinate is

$$(a) (x - y)^2 (+ y')^2 = (x + yy')^2$$

$$(b) (x - y)^2 (+ y')^2 = (x + y')^2$$

$$(c) (x - y)^2(+ y') = (x + yy')^2$$

(d) None of these

A. $(x-y)^2(1+(y')^2)=(x+yy')^2$

B. $(x-y)^2(+y')^2=(x+y')^2$

C. $(x-y)^2(1+(y')^2)=(x+yy')^2$

D. None of these

Answer:



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14. The differential equation satisfying the curve $\frac{x^2}{a^2 + \lambda} + \frac{y^2}{b^2 + \lambda} = 1$

when λ begin arbitrary unkwom, is

(a) $(x + yy_1)(xy_1 - y) = (a^2 - b^2)y_1$

(b) $(x + yy_1)(xy_1 - y) = y_1$

(c) $(x - yy_1)(xy_1 + y)(a^2 - b^2)y_1$

(d) None of these



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15. The differential equation of all conics whose centre lies at origin, is given by

(a) $(3xy_2 + x^2y_3)(y - xy_1) = 3xy_2(y - xy_1 - x^2y_2)$

(b) $(3xy_1 + x^2y_2)(y_1 - xy_3) = 3xy_1(y - xy_2 - x^2y_3)$

(c) $(3xy_2 + x^2y_3)(y_1 - xy) = 3xy_1(y - xy_1 - x^2y_2)$

(d) None of these

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16. Solve $\sec^2 x \tan y dx + \sec^2 y \tan x dy = 0$

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17. Solve the differential equation: $\frac{dy}{dx} = e^{x+y} + x^2e^y$

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18. Solve the following differential equation:

$$\sqrt{1 + x^2 + y^2 + x^2 y^2} + xy \frac{dy}{dx} = 0$$

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19. Solve $y - x \frac{dy}{dx} = a \left(y^2 + \frac{dy}{dx} \right)$

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20. Solve $e^{\frac{dy}{dx}} = x + 1$, given that when $x = 0$, $y = 3$.

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21. Solve $\frac{dy}{dx} = \sin^2(x + 3y) + 5$

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22. Solve $(x + y)^2 \frac{dy}{dx} = a^2$

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23. Solve $(2x + 3y - 1)dx + (4x + 6y - 5)dy = 0$.

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24. The solution of $\frac{xdx + ydy}{xdy - ydx} = \sqrt{\frac{a^2 - x^2 - y^2}{x^2 + y^2}}$, is given by

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25. Solve $[2\sqrt{xy} - x]dy + ydx = 0$

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26. Solve $(x^2 + y^2)dx - 2xydy = 0$.

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27. Solve the differential equation $2\frac{dy}{dx} = \frac{y}{x} + \frac{y^2}{x^2}$

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28. Solve $(1 + 2e^{x/y})dx + 2e^{x/y}(1 - x/y)dy = 0$.

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29. Solve that any equation of the form $yf'(xy)dx + xf'(xy)dy = 0$

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30. Solve the differential equation $\frac{dy}{dx} = \frac{2y - 6x - 4}{y - 3x + 3}$.



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31. Solve the differential equation $\frac{dy}{dx} = \frac{x + 2y - 1}{x + 2y + 1}$.



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32. The solution of the differential equation $\frac{dy}{dx} = \frac{\sin y + x}{\sin 2y - x \cos y}$ is

(a) $\sin^2 y = x \sin y + \frac{x^2}{2} + C$

(b) $\sin^2 y = x \sin y - \frac{x^2}{2} + C$

(c) $\sin^2 y = x + \sin y + \frac{x^2}{2} + C$

(d) $\sin^2 y = x - \sin y + \frac{x^2}{2} + C$



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33. solve the differential equation given by

$$\frac{dy}{dx} = \frac{-3x - 2y + 5}{2x + 3y + 5}$$



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34. Solve $\frac{dy}{dx} + 2y = \cos x$.

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35. Solve $\frac{dy}{dx} + \frac{y}{x} = \log x$.

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36. Solve $\frac{dy}{dx} = \frac{y}{2y \ln y + y - x}$.

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37. Solution of the equation $\cos^2 x \frac{dy}{dx} - (\tan 2x)y = \cos^4 x$, where $|x| < \frac{\pi}{4}$ and $y\left(\frac{\pi}{6}\right) = \frac{3\sqrt{3}}{8}$ is

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38. Solve $\frac{dy}{dx} + y\phi'(x) = \phi(x) \cdot \phi'(x)$, where $\phi(x)$ is a given function.

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39. Solve $(y \log x - 1)y \, dx = x \, dy$.

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40. Solve $\frac{dy}{dx} + xy = xy^2$

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41. Solve $\frac{dy}{dx} = \frac{y\phi'(x) - y^2}{\phi(x)}$, where $\phi(x)$ is a given function.

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42. $\sec^2 y \frac{dy}{dx} + 2x \tan y = x^3$



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43. Solve $\frac{dy}{dx} + x(x + y) = x^3(x + y)^3 - 1$.



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44. Solve $\sin y \cdot \frac{dy}{dx} = \cos y(1 - x \cos y)$.



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45. Find the orthogonal trajectories of $xy = c$.



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46. The orthogonal trajectories of the family of curves $y = Cx^2$, (C is an arbitrary constant), is



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47. The differential equation representing all possible curves that cut each member of the family of circles $x^2 + y^2 - 2Cx = 0$ (C is a parameter) at right angle, is

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48. The orthogonal trajectories of the circle $x^2 + y^2 - ay = 0$, (where a is a parameter), is

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49. Solve $(x^2 - ay)dx + (y^2 - ax)dy = 0$.

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50. Solve $(2x \log y)dx + \left(\frac{x^2}{y} + 3y^2\right)dy = 0$.

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51. Solve $(x^2 - ay)dx + (y^2 - ax)dy = 0$.

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52. Solve $x dx + y dy = x dy - y dx$.

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53. Solve $\frac{y + \sin x \cos^2(xy)}{\cos^2(xy)} dx + \left(\frac{x}{\cos^2(xy)} + \sin y \right) dy = 0$

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54. Solve $\frac{x + y \frac{dy}{dx}}{y - x \frac{dy}{dx}} = x^2 + 2y^2 + \frac{y^4}{x^2}$

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55. The solution of

$$e^{x\frac{(y^2-1)}{y}} \{xy^2dy + y^3dx\} + \{ydx - xdy\} = 0, \text{ is}$$

A. $e^{xy} + e^{x/y} + c = 0$

B. $e^{xy} - e^{x/y} + c = 0$

C. $e^{xy} + e^{y/x} + c = 0$

D. $e^{xy} - e^{y/x} + c = 0$

Answer:



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56. The solution of $x^2dy - y^2dx + xy^2(x - y)dy = 0$, is

A. $\log \left| \frac{x - y}{xy} \right| = \frac{y^2}{2} + c$

B. $\log \left| \frac{xy}{x - y} \right| = \frac{x^2}{2} + c$

C. $\log \left| \frac{x - y}{xy} \right| = \frac{x^2}{2} + c$

$$D. \log \left| \frac{x-y}{xy} \right| = x + c$$

Answer:



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57. The solution of the differential equation $ydx - xdy + xy^2dx = 0$, is

A. $\frac{x}{y} + x^2 = \lambda$

B. $\frac{x}{y} - \frac{x^2}{2} = \lambda$

C. $\frac{x}{2y^2} + \frac{x^2}{4} = \lambda$

D. None of these

Answer: 4



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58. The solution of differential equation

$$x dy (y^2 e^{xy} + e^{x/y}) = y dx (e^{x/y} - y^2 e^{xy}), \text{ is}$$

A. $xy = \log(e^x + \lambda)$

B. $x^2/y = \log(e^{x/y} + \lambda)$

C. $xy = \log(e^{x/y} + \lambda)$

D. $xy^2 = \log(e^{x/y} + \lambda)$

Answer:



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59. Solution of the differential equation

$$(y + x\sqrt{xy}(x + y)) dx + (y\sqrt{xy}(x + y) - x dy) = 0 \text{ is (a) [Math}$$

Processing

Error]

(ff)

(gg)

$$(hh)(ii)(jj) \frac{(kk)(ll)x^{(mn)2(nn)}(oo) + (pp)y^{(qq)2(rr)}(ss)}{tt} 2(uu)(\vee) + 2(v$$

(lll) (mmm)

$$(nnn)(\infty o)(ppp) \frac{(qqq)(rrr)x^{(sss)2(ttt)}(uuu) + (vvv)y^{(www)2(xxx)}(yyy)2(c}{zzz}$$

$$+ 2(cccc)(dddd) \cot^{(eeee)}(ffff)^{-1}(gggg)(hhhh) \sqrt{(iii)(jjj)(kkk) \frac{x}{lll}y(c}$$

(rrrr) (d) None of these

A. $\frac{x^2 + y^2}{2} + 2 \tan^{-1} \sqrt{\frac{x}{2y}} = C$

B. $\frac{x^2 + y^2}{2} + 2 \tan^{-1} \sqrt{\frac{x}{y}} = C$

C. $\frac{x^2 + y^2}{\sqrt{2}} + 2 \tan^{-1} \sqrt{\frac{x}{y}} = C$

D. None of these

Answer: B

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60. Solve $(p - x)(p - e^x)(p - 1/y) = 0$,

where $P = \frac{dy}{dx}$.

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61. Solve $x^2p^2 + xpy - 6y^2 = 0$.



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62. Solve $xy^2(p^2 + 2) = 2py^3 + x^3$.



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63. Solve $xp^2 - 2yp + ax = 0$.



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64. Solve $y = 2px - p^2$ where $p = \frac{dy}{dx}$



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65. Solve $y + 2px + y^2p^3$.



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66. Form the differential equation of $y = px + \frac{p}{\sqrt{1+p^2}}$.



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67. Solve $\sqrt{1+p^2} = \tan(px - y)$. when $p = \frac{dy}{dx}$



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68. Solve $y^2 \log y = pxy + p^2$. where $p = \frac{dy}{dx}$



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69. The population of a certain is known to increase at a rate proportional to the number of people presently living in the country. If after two years

the population has doubled, and after three years the population is 20,000 estimates the number of people initially living in the country.

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70. A certain radioactive material is known to decay at a rate proportional to the amount present. Initially there is 50 kg of the material present and after 2h it is observed that the material has lost 10 percent of its original mass. Based on these data answer the following questions.

The time at which the material has decayed to one half of its initial mass is

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71. Five mice in a stable population of 500 are intentionally infected with a contagious disease to test a theory of epidemic spread that postulates the rate of change in the infected population is proportional to the product of the number of mice who have the disease with the number

that are disease free. Assuming the theory is correct, how long will it take half the population to contract the disease?

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72. Find the curve for which area of triangle formed by x-axis, tangent drawn at any point on the curve and radius vector of point of tangency is constant, equal to a^2

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73. Find the curve for which the intercept cut off by any tangent on y-axis is proportional to the square of the ordinate of the point of tangency.

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74. If $\frac{d^2x}{dy^2} \left(\frac{dy}{dx} \right)^3 + \frac{d^2y}{dx^2} = k$, then k is equal to

A. $\frac{dy}{dx}$

B. $y^2 \frac{dy}{dx}$

C. $y \frac{dy}{dx} + \left(\frac{d^2x}{dy^2} \right)^2$

D. None of these

Answer:

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75. The solution of $y^2 = 2y \frac{dy}{dx} - \left(\frac{dy}{dx} \right)^2$, is

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76. The solution of $\left(\frac{dy}{dx} \right)^2 + (2x + y) \frac{dy}{dx} + 2xy = 0$, is

A. $(y + x^2 - c_1)(x + \log y + y^2 + c_2) = 0$

B. $(y + x^2 - c_1)(x - \log y - c_2) = 0$

C. $(y + x^2 - c_1)(x + \log y - c_2) = 0$

D. None of these

Answer:



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77. A curve $y = f(x)$ passes through the origin. Through any point (x, y) on the curve, lines are drawn parallel to the co-ordinate axes. If the curve divides the area formed by these lines and co-ordinates axes in the ratio $m : n$, find the curve.

A. $y = cx^{m/n}$

B. $my^2 = cx^{m/n}$

C. $y^3 = cx^{m/n}$

D. None of these

Answer:



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78. Solve the differential equation, $\frac{a^2}{xy} \cdot \frac{dx}{dy} = \frac{x}{y} + \frac{y}{x} - 2$, is

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79. Find the family of curves, the subtangent at any point of which is the arithmetic mean of the co-ordinate point of tangency.

A. $(x - y)^2 = cy$

B. $(y - x)^2 = cy$

C. $(x - y)^2 = cxy$

D. None of these

Answer:

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80. The order of the differential equation of family of curves $y = C_1 \sin^{-1} x + C_2 \cos^{-1} x + C_3 \tan^{-1} x + C_4 \cot^{-1} x$ (where C_1, C_2, C_3 and C_4 are arbitrary constants) is

- A. 2
- B. 3
- C. 4
- D. None of these

Answer:



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81. The solution of the differential equation $\frac{dy}{dx} = \frac{1}{xy[x^2 \sin y^2 + 1]}$ is

- (a)
- (b) $(c)(d)x^{(e)2(f)}(g)\left(\cos(h)y^{(i)2(j)}(k) - \sin(l)y^{(m)2(n)}(o) - 2C(p)e^q(r)\right)$
- (z) (aa) *[Math Processing Error]* (zz) (aaa)

$$(bbb)(c)(ddd)x^{(eee)2}(fff)(ggg)\left(\cos(hhh)y^{(iii)2}(jjj)(kkk) - \sin(lll)y^{(mmm)}\right)$$

(zzz) (aaaa) None of these

A. $x^2(\cos y^2 - \sin y^2 - 2ce^{-1}) = 2$

B. $y^2(\sin x^2 - \cos y^2 - 2ce^{-1}) = 2$

C. $y^2(\cos y^2 - \sin y^2 - e^{-y^2}) = 4c$

D. None of the above

Answer:

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82. The curve satisfying the equation $\frac{dy}{dx} = \frac{y(x + y^3)}{x(y^3 - x)}$ and passing through the point $(4, -2)$ is (a) $(b)(c)(d)y^{(e)2}(f)(g) = -2x(h)$ (i) $(b)(j)(k)y = -2x(l)$ (m) $(c)(d)(e)(f)y^{(g)3}(h)(i) = -2x(j)$ (k) (d)

None of these

A. $y^2 = -2x$

B. $y = -2x$

C. $y^3 = -2x$

D. None of these

Answer:



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83. Spherical rain drop evaporates at a rate proportional to its surface area. The differential equation corresponding to the rate of change of the radius of the rain drop if the constant of proportionality is $K > 0$ is

A. $\frac{dr}{dt} + k = 0$

B. $\frac{dr}{dt} - k = 0$

C. $\frac{dr}{dt} - kr$

D. None of these

Answer:



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84. A function $y = f(x)$ satisfies the differential equation

$f(x)\sin 2x - \cos x + (1 + \sin^2 x)f'(x) = 0$ with $f(0) = 0$. The value of $f\left(\frac{\pi}{6}\right)$ equals to :

A. $1/5$

B. $3/5$

C. $4/5$

D. $2/5$

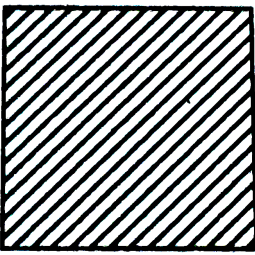
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85. The general solution of the differential equation $\frac{dy}{dx} = \frac{1-x}{y}$ is a family of curves which look like which of the following :

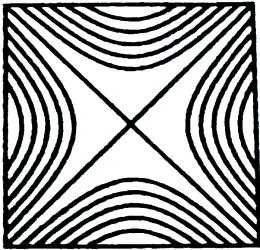
A.



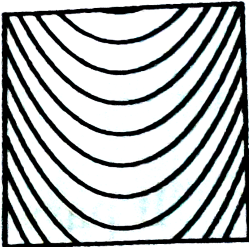
B.



C.



D.



Answer:



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86. Water is drained from a vertical cylindrical tank by opening a valve at the base of the tank. It is known that the rate at which the water level drops is proportional to the square root of water depth y , where the constant of proportionality $k > 0$ depends on the acceleration due to gravity and the geometry of the hole. If t is measured in minutes and $k = \frac{1}{15}$, then the time to drain the tank if the water is 4 m deep to start with is (a) 30 min (b) 45 min (c) 60 min (d) 80 min

A. 30 min

B. 45 min

C. 60 min

D. 80 min

Answer:



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87. Number of straight lines which satisfy the differential equation

$$\frac{dy}{dx} + x \left(\frac{dy}{dx} \right)^2 - y = 0 \text{ is}$$

A. 1

B. 2

C. 3

D. 4

Answer:



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88. Consider the two statements Statement-1: $y = \sin kt$ satisfies the differential equation $y'' + 9y = 0$. Statement 2 : $y = e^{kt}$ satisfy the differential equation $y'' + y' - 6y = 0$. The value of k for which both the statements are correct is (A) -3 (B) 0 (C) 2 (D) 3

A. -3

B. 0

C. 2

D. 3

Answer:



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89. If $y = \frac{x}{\log|cx|}$ (where c is an arbitrary constant) is the general solution of the differential equation $\frac{dy}{dx} = \frac{y}{x} + \varphi\left(\frac{x}{y}\right)$, then the

function $\varphi\left(\frac{x}{y}\right)$ is (a)

(b)(c)(d) $\frac{(e)(f)x^{(g)2(h)}(i)}{j} \left((k)(l)y^{(m)2(n)}(o) \right) (p)(q)(r)$ (s) (b)

(t)(u) $-(v) \frac{(w)(x)x^{(y)2(z)}(aa)}{bb} \left((cc)(dd)y^{(ee)2(ff)}(gg) \right) (hh)(ii)(jj)$

(kk) (c) (d)(e)(f) $\frac{(g)(h)y^{(i)2(j)}(k)}{l} \left((m)(n)x^{(o)2(p)}(q) \right) (r)(s)(t)$ (u)

(d)

(v)(w) $-(x) \frac{(y)(z)y^{(aa)2(bb)}(cc)}{dd} \left((ee)(ff)x^{(gg)2(hh)}(ii) \right) (jj)(kk)(ll)$

(mm)

A. $\frac{x^2}{y^2}$

B. $-\frac{x^2}{y^2}$

C. $\frac{y^2}{x^2}$

D. $-\frac{y^2}{x^2}$

Answer:



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90. If $\int_a^x ty(t) dt = x^2 + y(x)$, then find $y(x)$

A. $y = 2 - (2 + a^2)e^{\frac{x^2 - a^2}{2}}$

B. $y = 1 - (2 + a^2)e^{\frac{x^2 - a^2}{2}}$

C. $y = 2 - (1 + a^2)e^{\frac{x^2 - a^2}{2}}$

D. None of these

Answer:



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91. about to only mathematics

A. is homogeneous

B. can be converted into linear differential equation with some suitable substitution

C. is the family of circles touching the x-axis at the origin

D. the family the circles touching the y-axis at the origin

Answer:



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92. The differential equation $\frac{dy}{dx} = \frac{\sqrt{1-y^2}}{y}$ determines a family of circle with (a) variable radii and a fixed centre at (0, 1) (b) variable radii and a fixed centre at (c)(d)((e)(f)0, -1(g))(h) (i) (j) Fixed radius 1 and

variable centres along the x-axis. (k) Fixed radius 1 and variable centres along the y-axis.

- A. variable radii and a fixed centre at (0,1)
- B. variable radii and fixed centre at (0,-1)
- C. fixed radius 1 and variable centres along the x-axis
- D. fixed radius 1 and variable centres along the y-axis

Answer:

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93. A differentiable function satisfies

$$f(x) = \int_0^x (f(t) \cot t - \cos(t - x)) dt.$$

Which of the following hold(s) good?

- A. $f(x)$ has a minimum value $1 - e$
- B. $f(x)$ has a maximum value $1 - e^{-1}$

C. $f''\left(\frac{\pi}{2}\right) = e$

D. $f'(0) = 1$

Answer:



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94. Let $\frac{dy}{dx} + y = f(x)$ where y is a continuous function of x with $y(0) = 1$

and $f(x) = \begin{cases} e^{-x} & \text{if } 0 \leq x \leq 2 \\ e^{-2} & \text{if } x > 2 \end{cases}$ Which of the following hold(s)

good ?

A. $y(1) = 2e^{-1}$

B. $y'(1) = -e^{-1}$

C. $y(3) = -2e^{-3}$

D. $y'(3) = -2e^{-3}$

Answer:



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95. A curve $y = f(x)$ passes through $(1, 1)$ and tangent at $P(x, y)$ cuts the x-axis and y-axis at A and B , respectively, such that $BP: AP = 3$, then (a) equation of curve is $xy' - 3y = 0$ (b) normal at $(1, 1)$ is $x + 3y = 4$ (c) curve passes through $2, \frac{1}{8}$ (d) equation of curve is $xy' + 3y = 0$

A. equation of curve is $xy'-3y=0$

B. normal at $(1,1)$ is $x+3y=4$

C. curve passes through $\left(2, \frac{1}{8}\right)$

D. equation of curve is $xy'+3y=0$

Answer:



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96. Let a solution $y = y(x)$ of the differential equation $x\sqrt{x^2 - 1}dy - y\sqrt{y^2 - 1}dx = 0$, satisfy $y(2) = \frac{2}{\sqrt{3}}$

- A. Statement I is true, Statement II is also true, Statement
- B. Statement I is true, Statement II is also true, Statement II is not the correct explanation of Statement I.
- C. Statement I is true, Statement II is false.
- D. Statement I is false, Statement II is true.

Answer:



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97. A curve $y=f(x)$ satisfy the differential equation $(1 + x^2) \frac{dy}{dx} + 2yx = 4x^2$ and passes through the origin.

The function $y=f(x)$

- A. is strictly increasing , $\forall x \in R$
- B. is such that it has a minima but no maxima
- C. is such that it has a maxima but no minima

D. has no inflection point

Answer:



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98. A curve $y=f(x)$ satisfy the differential equation $(1 + x^2) \frac{dy}{dx} + 2yx = 4x^2$ and passes through the origin.

The area enclosed by $y = f^{-1}(x)$, the x-axis and the ordinate at $x = 2/3$ is

A. $2\ln 2$

B. $\frac{4}{3}\ln 2$

C. $\frac{2}{3}\ln 2$

D. $\frac{1}{3}\ln 2$

Answer:



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99. A curve $y=f(x)$ satisfy the differential equation

$$(1 + x^2) \frac{dy}{dx} + 2yx = 4x^2 \text{ and passes through the origin.}$$

The function $y=f(x)$

- A. $f(x)$ is a rational function
- B. $f(x)$ has the same domain and same range
- C. $f(x)$ is a transcendental function
- D. $y=f(x)$ is a bijective mapping

Answer:



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100. Let $y=f(x)$ be a curve passing through $(4,3)$ such that slope of normal at any point lying in the first quadrant is negative and the normal and tangent at any point P cuts the Y -axis at A and B respectively such that the mid-point of AB is origin, then the number of solutions of $y=f(x)$ and

$$f = |5 - |x||, \text{ is}$$



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101. If a function satisfies the relation

$$f(x)f''(x) - f(x)f'(x) = (f'(x))^2 \forall x \in R \text{ and } f(0) = f'(0) = 1,$$

then

The value of $\lim_{x \rightarrow -\infty} f(x)$ is



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102. For certain curve $y = f(x)$ satisfying $\frac{d^2y}{dx^2} = 6x - 4$, $f(x)$ has local minimum value 5 when $x = 1$

Global maximum value of $y = f(x)$ for $x \in [0, 2]$ is



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103. If $\phi(x)$ is a differential real-valued function satisfying $\phi'(x) + 2\phi(x) \leq 1$. prove that $\phi(x) - \frac{1}{2}$ is a non-increasing function

of x .



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104. The curve for which the ratio of the length of the segment intercepted by any tangent on the Y-axis to the length of the radius vector is constant (k), is



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105. Let $u(x)$ and $v(x)$ be two continuous functions satisfying the differential equations $(du)(dx) + p(x)u = f(x)$ and $\frac{dv}{dx} + p(x)v = g(x)$, respectively. If $u(x_1) > v(x_1)$ for some x_1 and $f(x) > g(x)$ for all $x > x_1$, prove that any point (x, y) , where $x > x_1$, does not satisfy the equations $y = u(x)$ and $y = v(x)$ simultaneously.



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106. A normal is drawn at a point $P(x, y)$ of a curve. It meets the x-axis at Q . If PQ has constant length k , then show that the differential equation describing such curves is $y \frac{dy}{dx} = \pm \sqrt{k^2 - y^2}$. Find the equation of such a curve passing through $(0, k)$.



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107. Find the equation of a curve passing through the point $(1, 1)$ if the perpendicular distance of the origin from the normal at any point $P(x, y)$ of the curve is equal to the distance of P from the x-axis.



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108. A country has a food deficit of 10%. Its population grows continuously at the rate of 3% per year. Its annual food production every year is 4% more than that of the last year. Assuming that the average food requirement per person remains constant, prove that the country

will become self-sufficient in food after n years, where n is the smallest integer bigger than or equal to $\frac{\log_e 10 - \log_e 9}{(\log_e 1.04) - 0.03}$

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109. A right circular cone with radius R and height H contains a liquid which evaporates at a rate proportional to its surface area in contact with air (proportionality constant $= k > 0$). Find the time after which the cone will be empty.

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110. For $x \in R, x \neq 0$, if $y(x)$ differential function such that $x \int_1^x y(t) dt = (x + 1) \int_1^x ty(t) dt$, then $y(x)$ equals: (where C is a constant.)

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111. Find a pair of curves such that (a) the tangents drawn at points with equal abscissas intersect on the y-axis. (b) the normal drawn at points with equal abscissas intersect on the x-axis. (c) one curve passes through (1,1) and other passes through (2, 3).

A. the tangents drawn at points with equal avscissae intersect on the y-axis.

B. the normal drawn at points with equal absicssae intersect on x-axis.

C. one curve passes through (1,1) and other passes through (2,3).

D.

Answer:



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112. Given two curves: $y = f(x)$ passing through the point $(0, 1)$ and

$g(x) = \int_{-\infty}^x f(t)dt$ passing through the point $\left(0, \frac{1}{n}\right)$. The tangents

drawn to both the curves at the points with equal abscissas intersect on the x-axis. Find the curve $y = f(x)$.

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113. A normal is drawn at a point $P(x, y)$ of a curve. It meets the x-axis and the y-axis in point A AND B , respectively, such that $\frac{1}{OA} + \frac{1}{OB} = 1$, where O is the origin. Find the equation of such a curve passing through (5, 4)

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114. A line is drawn from a point $P(x, y)$ on the curve $y = f(x)$, making an angle with the x-axis which is supplementary to the one made by the tangent to the curve at $P(x, y)$. The line meets the x-axis at A. Another line perpendicular to it drawn from $P(x, y)$ meeting the y-axis at B. If $OA = OB$, where O is the origin, the equation of all curves which pass through (1, 1) is

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115. A tangent and a normal to a curve at any point P meet the x and y axes at A, B and C, D respectively. Find the equation of the curve passing through $(1, 0)$ if the centre of circle through O, C, P and B lies on the line $y = x$ (where O is the origin).



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116. Let $f(x)$ be positive continuous and differentiable on the interval (a, b) and $\lim_{x \rightarrow a} f(x) = 1$, $\lim_{x \rightarrow b} f(x) = 3^{1/4}$. If $f'(x) \geq f^3(x) + \frac{1}{f(x)}$ then the greatest value of $b - a$ is

A. $b - a \geq \pi/4$

B. $b - a \leq \pi/4$

C. $b - a \leq \pi/24$

D. None of these

Answer:



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Solved Examples

1. If the area bounded by $y=f(x)$, $x = \frac{1}{2}$, $x = \frac{\sqrt{3}}{2}$ and the X-axis is A sq units where $f(x) = x + \frac{2}{3}x^3 + \frac{2}{3} \cdot \frac{4}{5}x^5 + \frac{2}{3} \cdot \frac{4}{5} \cdot \frac{6}{7}x^7 + \dots\infty$, $|x| < 1$,

Then the value of $[4A]$ is (where $[.]$ is G.I.F)



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Subjective Type Question

1. If (y_1, y_2) are two solutions of the differential $\frac{dy}{dx} + p(x) \cdot y = Q(x)$

Then prove that $y = y_1 + C(y_1 - y_2)$ is the genral solution of the equation where C is any constant. For what relation between the constant α, β will the linear combination $\alpha y_1 + \beta y_2$ also be a Solution.



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Exercise For Session 1

1. The differential equation of all parabolas whose axis of symmetry is along X-axis is of order.

A. 2

B. 3

C. 1

D. None of these

Answer: A



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2. The order and degree of the differential equation of all tangent lines to the parabola $x^2 = 4y$ is

A. 1,2

B. 2,2

C. 3,1

D. 4,1

Answer: A



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3. The degree of the differential equation

$$\frac{d^2y}{dx^2} + 3\left(\frac{dy}{dx}\right)^2 = x^2 \log\left(\frac{d^2y}{dx^2}\right), \text{ is}$$

A. 1

B. 2

C. 3

D. Not defined

Answer: D



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4. Find the differential equation satisfying the relation

$$\sqrt{1+x^2} + \sqrt{1+y^2} = \lambda x \sqrt{1+y^2} - y \sqrt{1+x^2}.$$

A. 1

B. 2

C. 3

D. 4

Answer: A



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5. The degree of the differential equation

$$\left(\frac{d^2y}{dx^2}\right) + \left(\frac{dy}{dx}\right)^2 = x \sin\left(\frac{d^2y}{dx^2}\right) \text{ is}$$

A. 1

B. 2

C. 3

D. Not defined

Answer: D



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6. Find the differential equation of all circles touching the x-axis at the origin y-axis is the origin

A. $y^2 - x^2 = 2xy \frac{dy}{dx}$

B. $y^2 - x^2 = 2xy \frac{dx}{dy}$

C. $y^2 - x^2 = 2xy \frac{dy}{dx}$

D. $y^2 - x^2 = 2xy \frac{dx}{dy}$

Answer: A



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7. Show that the differential equation that represents the family of all parabolas having their axis of symmetry coincident with the axis of $xy_2 + y_1^2 = 0$.

A. $yy_2 + y_1^2 - y + y_1$

B. $yy_2 + y_1^2 = 0$

C. $yy_2 + y_1^2 = y_1$

D. None of these

Answer: B



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8. The differential equation of all conics whose axes coincide with the coordinate axes, is

A. (a) $xyy_2 + xy_1^2 - yy_1 = 0$

B. (b) $yy_2 + y_1^2 - yy_1 = 0$

C. (c) $xyy_2 + (x - y)y_1 = 0$

D. (d) None of these

Answer: A



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9. The differential equation having $y = (\sin^{-1} x)^2 + A(\cos^{-1} x) + B$, where A and B are arbitrary constant, is

A. $(1 - x^2)y_2 - xy_1 = 2$

B. $(1 - x^2)y_2 + yy_1 = 0$

C. $(1 - x^2)y_2 + xy_1 = 0$

D. None of these

Answer: A



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10. The differential equation of circles passing through the points of intersection of unit circle with centre at the origin and the line bisecting the first quadrant, is

A. $y_1(x^2 + y^2 - 1) + (x + yy_1) = 0$

B. $(y_1 - 1)(x^2 + y^2 - 1) + (x + yy_1)2(x - y) = 0$

C. $y_1(x^2 + y^2 - 1) + yy_2 = 0$

D. None of these

Answer: B



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Exercise For Session 2

1. Solve $\frac{dy}{dx} = \frac{(x + y)^2}{(x + 2)(y - 2)}$

A. $(x + 2)^4 \left(1 + 2 \frac{(y - 2)}{x + 2} \right) = k^{\frac{2(y-2)}{x+2}}$

B. $(x + 2)^4 \left(1 + \frac{(y - 2)}{x + 2} \right) = k^{\frac{2(y-2)}{x+2}}$

C. $(x + 2)^3 \left(1 + 2 \frac{(y - 2)}{x + 2} \right) = k^{\frac{2(y-2)}{x+2}}$

D. None of these

Answer: B



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2. If $(y^3 - 2x^2y)dx + (2xy^2 - x^3)dy = 0$, then the value of $xy\sqrt{y^2 - x^2}$, is

A. $y^2 + x$

B. xy^2

C. any constant

D. None of these

Answer: C

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3. The solution of $\frac{dy}{dx} = \cos(x + y) + \sin(x + y)$, is given by

A. $\log \left| 1 + \tan \left(\frac{x + y}{2} \right) \right| = x + c$

B. $\log | 1 + \tan((x + y) | = x + c$

C. $\log | 1 - \tan((x + y) | = x + c$

D. None of these

Answer: A

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4. The solution of $\frac{dy}{dx} = (x + y - 1) + \frac{x + y}{\log(x + y)}$, is given by

A. $\{1 + \log(x + y)\} - \log\{1 + \log(x + y)\} = x + c$

B. $\{1 - \log(x + y)\} - \log\{1 - \log(x + y)\} = x + c$

C. $\{1 - \log(x + y)\}^2 - \log\{1 + \log(x + y)\} = x + c$

D. None of these

Answer: A



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5. $(2x^2 + 3y^2 - 7)xdx - (3x^2 + 2y^2 - 8)ydy = 0$

A. $(x^2 + y^2 - 1) = (x^2 + y^2 - 3)^5 C$

B. $(x^2 + y^2 - 1)^2 = (x^2 + y^2 - 3)^5 C$

C. $(x^2 + y^2 - 3)^2 = (x^2 + y^2 - 1)^5 C$

D. None of these

Answer: C



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6. The solution of $\frac{dy}{dx} = \frac{(x-1)^2 + (y-2)^2 \tan^{-1}\left(\frac{y-2}{x-1}\right)}{(xy - 2x - y + 2) \tan^{-1}\left(\frac{y-2}{x-1}\right)}$ is equal to

A.

$$\left\{ (x-1)^2 + (y-1)^2 \right\} \tan^{-1} \left(\frac{y-2}{x-1} \right) - 2(x-1)(y-2) = 2(x-1)(y-2)$$

B.

$$\left\{ (x-1)^2 + (y-1)^2 \right\} - 2(x-1)(y-2) \tan^{-1} \left(\frac{y-1}{x-1} \right) = 2(x-1)(y-2)$$

C.

$$\left\{ (x-1)^2 + (y-1)^2 \right\} \tan^{-1} \left(\frac{y-2}{x-1} \right) - 2(x-1)(y-2) = \log C(x-1)$$

D. None of these

Answer: A



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7. The solution of $\frac{dy}{dx} = \left(\frac{x+2y-3}{2x+y+3} \right)^2$, is

A. $(x+3)^2 - (y-3)^3 = C(x-y+6)^4$

B. $(x+3)^3 - (y-3)^3 = C$

C. $(x+3)^4 + (y-3)^4 = C$

D.

Answer: A



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$$8. \frac{dy}{dx} = - \frac{\cos x(3 \cos y - 7 \sin x - 3)}{\sin y(3 \sin x - 7 \cos y + 7)}$$

A. $(\cos y - \sin x - 1)^2(\sin x + \cos y - 1)^5 = C$

B. $(\cos y - \sin x - 1)^2(\sin x + \cos y - 1)^3 = C$

C. $(\cos y - \sin x - 1)^2(\sin x + \cos y - 1)^7 = C$

D. None of these

Answer: A



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9. A curve C has the property that if the tangent drawn at any point P on C meets the co-ordinate axis at A and B , then P is the mid-point of AB . The curve passes through the point $(1,1)$. Determine the equation of the curve.

A. $xy=1$

B. $\frac{x}{y} = 1$

C. $2x=xy-1$

D. None of these

Answer: A



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10. The family of curves whose tangent form an angle $\frac{\pi}{4}$ with the hyperbola $xy=1$, is

A. $y = x - 2 \tan^{-1}(x) + k$

B. $y = x + 2 \tan^{-1}(x) + k$

C. $y = 2x - \tan^{-1}(x) + k$

D. $y = 2x + \tan^{-1}(x) + k$

Answer: A



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11. A and B are two separate reservoirs of water. Capacity of reservoir A is double the capacity of reservoir B . Both the reservoirs are filled completely with water, their inlets are closed and then the water is released simultaneously from both the reservoirs. The rate of flow of water out of each reservoir at any instant of time is proportional to the quantity of water in the reservoir at the time. One hour after the water is released, the quantity of water in reservoir A is $1\frac{1}{2}$ times the quantity of water in reservoir B . After how many hours do both the reservoirs have the same quantity of water?

A. $\log_{3/4}(2)$

B. $\log_{3/4}(2)$

C. $\log_{1/2}\left(\frac{1}{2}\right)$

D. None of these

Answer: B



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12. A curve passes through $(2, 1)$ and is such that the square of the ordinate is twice the rectangle contained by the abscissa and the intercept of the normal. Then the equation of curve is

A. a. $x^2 + y^2 = 9x$

B. b. $4x^2 + y^2 = 9x$

C. c. $4x^2 + 2y^2 = 9x$

D. d. All of these

Answer: C

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13. A normal at $P(x, y)$ on a curve meets the x-axis at Q and N is the foot of the ordinate at P . If $NQ = \frac{x(1 + y^2)}{1 + x^2}$, then the equation of curve

given that it passes through the point $(3, 1)$ is (a)

(b) $(c)(d)x^{(e)2(f)}(g) - (h)y^{(i)2(j)}(k) = 8(l)$ (m) (b)

(n)(o)(p) $x^{(q)2(r)}(s) + 2(t)y^{(u)2(v)}(w) = 11(x)$ (y) (c)

(d)(e)(f) $x^{(g)2(h)}(i) - 5(j)y^{(k)2(l)}(m) = 4(n)$ (o) (d) None of these

A. $5(1 + y^2) = (1 + x^2)$

B. $(1 + y^2) = 5(1 + x^2)$

C. $(1 + x^2) = (1 + y^2)$

D. None of these

Answer: A

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14. Determine all curve for which the ratios of the lighth of the sagment intercepted by tangent on the y-axis to the length of the radius vector is a constant.

A. $\left(y + \sqrt{x^2 - y^2}\right)x^{k-1} = c$

B. $\left(y + \sqrt{x^2 + y^2}\right)x^{k-1} = c$

C. $\left(y - \sqrt{x^2 - y^2}\right)x^{k-1} = c$

D. $\left(y - \sqrt{x^2 + y^2}\right)x^{k-1} = c$

Answer: B



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15. A point $P(x, y)$ nores on the curve $x^{\frac{2}{3}} + y^{\frac{2}{3}} = a^{\frac{2}{3}}$, $a > 0$ for each position (x, y) of p, perpendiculars are drawn from origin upon the tangent and normal at P, the length (absolute valve) of them being $p_1(x)$ and $P_2(x)$ brespectively, then

A. $\frac{dp_1}{dx} \cdot \frac{dp_2}{dx} < 0$

B. $\frac{dp_1}{dx} \cdot \frac{dp_2}{dx} \leq 0$

C. $\frac{dp_1}{dx} \cdot \frac{dp_2}{dx} \geq 0$

D. $\frac{dp_1}{dx} \cdot \frac{dp_2}{dx} \geq 0$

Answer: B



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Exercise For Session 3

1. $(1 + x^2) \frac{dy}{dx} + y = e^{\tan^{-1} x}$

A. $2ye^{\tan^{-1} x} = e^{2 \tan^{-1} x} + C$

B. $ye^{\tan^{-1} x} = e^{2 \tan^{-1} x} + C$

C. $2ye^{\tan^{-1} x} = e^{2 \tan^{-1} x} + C$

D. None of these

Answer: A



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2. Solution of differential equation $\frac{dy}{dx} + \frac{x}{1-x^2}y = x\sqrt{y}$ is

A. a) $3\sqrt{y} + (1-x^2) = c(1-x^2)^{1/4}$

B. b) $\frac{3}{2}\sqrt{y} + (1-x^2) = c(1-x^2)^{3/2}$

C. c) $3\sqrt{y} - (1-x^2) = c(1-x^2)^{1/4}$

D. d) None of these

Answer: A



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3. Solve $\frac{dy}{dx} + x \sin 2y = x^3 \cos^2 y$

A. $e^{x^2} = (x^2 - 1)e^{x^2} \tan y + c$

B. $e^{x^2} \tan y = \frac{1}{2}(x^2 - 1)e^{x^2} + c$

C. $e^{x^2} \tan y = (x^2 - 1)\tan y + c$

D. None of these

Answer: B



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4. The solution of $3x(1 - x^2)y^2 \frac{dy}{dx} + (2x^2 - 1)y^3 = ax^3$ is

A. $y^2 = ax + c\sqrt{1 - x^2}$

B. $y^3 = ax + cx\sqrt{1 - x^3}$

C. $y^2 = ax + c\sqrt{1 - x^2}$

D. None of these

Answer: B



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5. The solution of $\frac{dy}{dx} + \frac{y}{x} \log y = \frac{y}{x^2} (\log y)^2$, is

A. a) $x = \frac{1}{2x} \log y + C$

B. b) $x^2 + \log y = C$

C. c) $\frac{1}{x \log y} = \frac{1}{2x^2} + C$

D. d) None of these

Answer: C



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6. The solution of $\frac{dy}{dx} + yf'(x) - f(x) \cdot f'(x) = 0, y \neq f(x)$ is

A. $y = f(x) + 1 + ce^{-f(x)}$

B. $y - ce^{-f(x)}$

C. $y = f(x) - 1 + ce^{-f(x)}$

D. None of these

Answer: C



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7. The solution of $(x^2 - 1) \frac{dy}{dx} \cdot \sin y - 2x \cdot \cos y = 2x - 2x^3$ is

A. $(x^2 - 1) \cos y = \frac{x^4}{2} - x^2 + C$

B. $(x^2 - 1) \sin y = \frac{x^4}{2} - x^2 + C$

C. $(x^2 - 1) \cos y = \frac{x^4}{2} - \frac{x^2}{2} + C$

D. $(x^2 - 1) \sin y = \frac{x^4}{2} - \frac{x^2}{2} + C$

Answer: A



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8. The Curve possessing the property that the intercept made by the tangent at any point of the curve on they-axis is equal to square of the abscissa of the point of tangency, is given by

A. $y^2 = x + c$

B. $y = 2x^2 + cx$

C. $Y = -x^2 + cx$

D. None of these

Answer: C



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9. The tangent at a point P of a curve meets the y-axis at A, and the line parallel to y-axis at A, and the line parallel to y-axis through P meets the x-axis at B. If area of ΔOAB is constant (O being the origin), Then the curve is

A. $cx^2 - xy + k = 0$

B. $y^2 + 2x^2 = cx$

C. $3x^2 + 4y^2 = k$

D. $xy - x^2y^2 + kx = 0$

Answer: A



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10. The value of k such that the family of parabolas $y = cx^2 + k$ is the orthogonal trajectory of the family of ellipse $x^2 + 2y^2 - y = c$, is

A. 1

B. $\frac{1}{2}$

C. $\frac{1}{3}$

D. $\frac{1}{4}$

Answer: D



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Exercise For Session 4

1. The solution of $xdy + ydx + 2x^3dx = 0$ is

A. $xy + x^4 = c$

B. $xy + \frac{1}{2}x^4 = c$

C. $\frac{x^2}{y} + \frac{x^4}{4} = c$

D. None of these

Answer: B



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2. The solution of $ydx - xdy + (1 + x^2)dx + x^2 \sin ydy = 0$, is given

by

A. $2x - y^2 + \cos y + c = 0$

B. $y + 1 - x^2 + x \cos y + c = 0$

C. $\frac{x}{y} + \frac{1}{y} - y + \cos y + c = 0$

D. $\frac{y}{x} + \frac{1}{x} - x + \cos y + c = 0$

Answer: D

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3. The solution of the differential equation

$\left\{ 1 + x\sqrt{x^2 + y^2} \right\} dx + \left\{ (x^2 + y^2) - 1 \right\} y dy = 0$ is equal to

A. $\left(1 + x\sqrt{x^2 + y^2} \right) dx + \left(-1 + \sqrt{x^2 + y^2} \right) y dy = 0,$

B. $2x - y + \frac{2}{3}(x^2 + y^2)^{3/2} = c$

C. $2y - x^2 + \frac{2}{3}(x^2 + y^2)^{3/2} = c$

D. None of these

Answer: A

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4. Solution of the differential equation $\frac{xdy}{x^2 + y^2} = \left(\frac{y}{x^2 + y^2} - 1 \right) dx,$ is

A. $\tan^{-1}\left(\frac{x}{y}\right) + x = c$

B. $\tan^{-1}\left(\frac{y}{x}\right) + x = c$

C.

D. $\tan^{-1}\left(\frac{y}{x}\right) + x^2 = c$

Answer: B



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5. The solution of the differential equation

$$ye^{x/y}dx = (xe^{x/y} + y^2 \sin y)dy \text{ is}$$

A. $e^{x/y} = -\cos y + c$

B. $e^{x/y} = +2\cos y = c$

C. $e^{x/y} = x \cos y + c$

D. $e^{x/y} = 2\cos y + c$

Answer: A

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6. The solution of $x \sin\left(\frac{y}{x}\right) dy = \left\{y \sin\left(\frac{y}{x}\right) - x\right\} dx$, is given by

A. $\log x + \cos\left(\frac{y}{x}\right) = \log C$

B. $\log x - \cos\left(\frac{y}{x}\right) = \log C$

C. $\log\left(\frac{x}{y}\right) - \cos\left(\frac{y}{x}\right) = \log C$

D. None of these

Answer: B

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7. The solution of $\frac{x dx + y dy}{x dy - y dx} = \sqrt{\frac{a^2 - x^2 - y^2}{x^2 + y^2}}$, is given by

A. $\sin^{-1}\left(\sqrt{x^2 + y^2}\right) = a \tan^{-1} + c$

B. $\sin^{-1}\left(\sqrt{x^2 + y^2}\right) = \frac{1}{a} \tan^{-1}\left(\frac{y}{x}\right) + c$

C. $\sin^{-1}\left(\sqrt{x^2 + y^2}\right) = \tan^{-1}\left(\frac{y}{x}\right) + c$

D. None of these

Answer: D



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8. Solve the following differential equation:

$$\left(1 + e^{x/y}\right)dx + e^{x/y}\left(1 - \frac{x}{y}\right)dy = 0$$

A. $x - ye^{x/y} = c$

B. $x + ye^{x/y} = c$

C. $y - \frac{x}{y}e^{x/y} = c$

D. None of these

Answer: B



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9. Solution of the differential equation $\frac{x + y \frac{dy}{dx}}{y - x \frac{dy}{dx}} = \frac{x \sin^2(x^2 + y^2)}{y^3}$.

A. $-\cot(x^2 + y^2) = \left(\frac{x}{y}\right)^2 + C$

B. $\tan(x^2 + y^2) = x^2 y^2 + C$

C. $\cot(x^2 + y^2) = \frac{x}{y} + C$

D. None of these

Answer: A



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10. The solution of $\frac{dy}{dx} + \frac{y}{x} = \frac{1}{(1 + \log x + \log y)^2}$ is given by

A. $xy(1 + \log(xy)) = C$

B. $xy^2(1 + \log(xy)) = C$

C. $xy(1 + \log(xy))^2 = C$

D. $xy\left(1 + (\log xy)^2\right) - \frac{x^2}{2} = C$

Answer: D



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Exercise For Session 5

1. Show that the curve for which the normal at every point passes through a fixed point is a circle.

- A. a circle
- B. an ellipse
- C. a hyperbola
- D. None of these

Answer: A



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2. If the tangent at any point P of a curve meets the axis of ΞnT . find the curve for which $OP = PT$, O being the origin.

A. $x = cy^2$

B. $x = cy^2$ or $x = c/y^2$

C. $x = cy$ or $x = c/y$

D. None of these

Answer: C



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3. According to Newton's law, rate of cooling is proportional to the difference between the temperature of the body and the temperature of the air. If the temperature of the air is $20^\circ C$ and body cools for 20 min from $100^\circ C$ to $60^\circ C$ then the time it will take for its temperature to drop to 30° is

A. 30 min

B. 40 min

C. 60 min

D. 80 min

Answer: C



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4. Let $f(x, y)$ be a curve in the x-y plane having the property that distance from the origin of any tangent to the curve is equal to distance of point of contact from the y-axis. It $f(1, 2) = 0$, then all such possible curves are

A. $x^2 + y^2 = 5x$

B. $x^2 - y^2 = 5x$

C. $x^2y^2 = 5x$

D. All of these

Answer: A



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5. Given the curves $y=f(x)$ passing through the point $(0,1)$ and $y = \int_{-\infty}^x f(t)$ passing through the point $\left(0, \frac{1}{2}\right)$ The tangents drawn to both the curves at the points with equal abscissae intersect on the x-axis. Then the curve $y=f(x)$, is

A. $f(x) = x^2 + x + 1$

B. $f(x) = \frac{x^2}{e^2}$

C. $f(x) = e^{2x}$

D.

Answer: C



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6. A curve passing through $(1, 0)$ is such that the ratio of the square of the intercept cut by any tangent on the y -axis to the Sub-normal is equal to the ratio of the product of the Coordinates of the point of tangency to the product of square of the slope of the tangent and the subtangent at the same point, is given by

A. $x = e^{\pm 2\sqrt{y}/x}$

B. $x = e^{\pm \sqrt{y}/x}$

C. $x = e^{\pm \sqrt{y}/x} - 1$

D. $xy + e^{\pm y/x} - 1 = 0$

Answer: A



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7. Consider a curve $y = f(x)$ in xy -plane. The curve passes through $(0,0)$ and has the property that a segment of tangent drawn at any point

$P(x, f(x))$ and the line $y = 3$ gets bisected by the line $x + y = 1$ then the equation of curve, is

A. $y^2 = 9(x - y)$

B. $(y - 3)^2 = 9(1 - x - y)$

C. $(y + 3)^2 = 9(1 - x - y)$

D. $(y - 3)^2 = 9(1 + x + y)$

Answer: B



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8. Consider the curved mirror $y = f(x)$ passing through $(0, 6)$ having the property that all light rays emerging from origin, after getting reflected from the mirror becomes parallel to x-axis, then the equation of curve, is

A. $y^2 = 4(x - y)$ or $y^2 = 36(9 + x)$

B. $y^2 = 4(1 - x)$ or $y^2 = 36(9 - x)$

C. $y^2 = 4(1 + x)$ or $y^2 = 36(9 - x)$

D. None of these

Answer: D

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Exercise Single Option Correct Type Questions

1. If the differential equation of the family of curve given by

$y = Ax + Be^{2x}$, where A and B are arbitrary constants is of the form

$(1 - 2x) \frac{d}{dx} \left(\frac{dy}{dx} + ly \right) + k \left(\frac{dy}{dx} + ly \right) = 0$, then the ordered pair

(k,l) is

A. (2,-2)

B. (-2,2)

C. (2,2)

D. (-2,-2)

Answer: A



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2. about to only mathematics

A. $y = x \tan^{-1}\left(\ln \frac{e}{x}\right)$

B. $y = x \tan^{-1}(\ln 2)$

C. $y = \frac{1}{x} \tan^{-1}\left(\ln \frac{e}{x}\right)$

D. None of these

Answer: A



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3. The x-intercept of the tangent to a curve is equal to the ordinate of the point of contact. The equation of the curve through the point (1,1) is

A. $ye^{\frac{x}{y}} = e$

B. $xe^{\frac{x}{y}} = e$

C. $xe^{\frac{y}{x}} = e$

D. $ye^{\frac{y}{x}} = e$

Answer: A

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4. A function $y = f(x)$ satisfies the condition

$f'(x)\sin x + f(x)\cos x = 1$, $f(x)$ being bounded when $x \rightarrow 0$. If

$I = \int_0^{\frac{\pi}{2}} f(x)dx$ then (A) $\frac{\pi}{2} < I < \frac{\pi^2}{4}$ (B) $\frac{\pi}{4} < I < \frac{\pi^2}{2}$ (C)

$1 < I < \frac{\pi}{2}$ (D) $0 < I < 1$

A. $\frac{\pi}{2} < I < \frac{\pi^2}{4}$

B. $\frac{\pi}{4} < I < \frac{\pi^2}{2}$

C. $1 < I < \frac{\pi}{2}$

D. $0 < I < 1$

Answer: A



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5. A curve is such that the area of the region bounded by the co-ordinate axes, the curve & the coordinate of any point on it is equal to the cube of that ordinate. The curve represents

- A. a pair of straight lines
- B. a circle
- C. a parabola
- D. an ellipse

Answer: C



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6. The value of the constant 'm' and 'c' for which $y = mx + c$ is a solution of the differential equation $\left(d^2 \frac{y}{dx^2}\right) - 3 \frac{dy}{dx} - 4y = -4x$ is:

A. is $m = -1, c = 3/4$

B. is $m = 1, c = -3/4$

C. no such real m,c

D. is $m = 1, c = 3/4$

Answer: B



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7. Find the real value of m for which the substitution $y = u^m$ will transform the differential equation $2x^4 y \frac{dy}{dx} + y^4 = 4x^6$ in to a homogeneous equation.

A. $m = 0$

B. $m = 1$

C. $1m=3//2`$

D. No value of m

Answer: C



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8. The solution of the differential equation,

$$x^2 \frac{dy}{dx} \cos \frac{1}{x} - y \sin \frac{1}{x} = -1, \text{ where } y \rightarrow -1 \text{ as } x \rightarrow \infty \text{ is}$$

A. $y = \sin \frac{1}{x} - \cos \frac{1}{x}$

B. $y = \frac{x+1}{x \sin \frac{1}{x}}$

C. $y = \sin \frac{1}{x} + \cos \frac{1}{x}$

D. $y = \frac{x+1}{x \cos \frac{1}{x}}$

Answer: A



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9. A wet porous substance in the open air loses its moisture at a rate proportional to the moisture content. If a sheet hung in the wind loses half its moisture during the first hour, then the time when it would have lost 99.9 % of its moisture is (weather conditions remaining same)

- A. (a) more than 100 h
- B. (b) more than 10 h
- C. (c) approximately 10 h
- D. (d) None of these

Answer: C

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10. A curve C passes through origin and has the property that at each point (x, y) on it the normal line at that point passes through $(1, 0)$. The equation of a common tangent to the curve C and the parabola $y^2 = 4x$ is

A. $x=0$

B. $y=0$

C. $y=x+1$

D. $x+y+1=0$

Answer: A



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11. A function $y = f(x)$ satisfies $(x + 1)f'(x) - 2(x^2 + x)f(x) = \frac{e^{x^2}}{x + 1}$, $x > -1$. If $f(0) = 5$, then $f(x)$ is

A. $\left(\frac{3x + 5}{x + 1}\right) \cdot e^{x^2}$

B. $\left(\frac{6x + 5}{x + 1}\right) \cdot e^{x^2}$

C. $\left(\frac{6x + 5}{(x + 1)^2}\right) \cdot e^{x^2}$

D. $\left(\frac{5x - 6x}{x + 1}\right) \cdot e^{x^2}$

Answer: B



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12. The curve with the property that the projection of the ordinate on the normal is constant and has a length equal to a is

A. $x - a \ln \left(\sqrt{y^2 - a^2} + y \right) = C$

B. $x + a \sqrt{a^2 - y^2} = C$

C. $(y - a)^2 = Cx$

D. $ay = \tan^{-1}(x + c)$

Answer: A



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13. The differential equation corresponding to the family of curves

$y = e^x(ax + b)$ is

A. $\frac{d^2y}{dx^2} + 2\frac{dy}{dx} - y = 0$

B. $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} - y = 0$

C. $\frac{d^2y}{dx^2} + 2\frac{dy}{dx} + y = 0$

D. $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} - y = 0$

Answer: B



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14. The equation to the orthogonal trajectories of the system of parabolas $y = ax^2$ is

A. $\frac{x^2}{2} + y^2 = C$

B. $x^2 - \frac{x^2}{2} = C$

C. $\frac{x^2}{2} - y^2 = C$

D. $x^2 - \frac{y^2}{2} = C$

Answer: A

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15. A function satisfying $\int_0^1 f(tx) dt = nf(x)$, where $x > 0$ is

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16. The substitution $y = z^\alpha$ transforms the differential equation $(x^2y^2 - 1)dy + 2xy^3dx = 0$ into a homogeneous differential equation for

A. $\alpha = -1$

B. 0

C. $\alpha = 1$

D. No value of α

Answer: A

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17. A curve passing through (2, 3) and satisfying the differential equation

$$\int_0^t ty(t) dt = x^2y(x), (x > 0) \text{ is}$$

A. $x^2 + y^2 = 13$

B. $y^2 = \frac{9}{2}x$

C. $\frac{x^2}{8} + \frac{y^2}{18} = 1$

D. $xy=6$

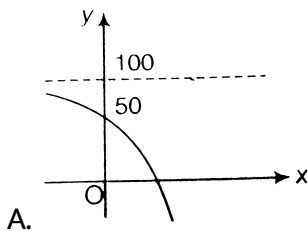
Answer: D

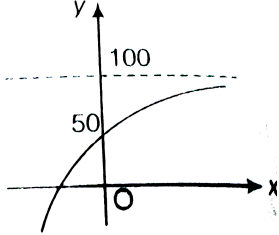


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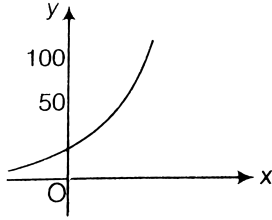
18. Which one of the following curves represents the solution of the

initial value problem $\frac{dy}{dx} = 100 - y$, where $y(0) = 50$

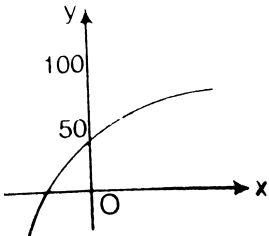




B.



C.



D.

Answer: B



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Exercise More Than One Correct Option Type Questions

1. The differential equation $x \frac{dy}{dx} + \frac{3}{\frac{dy}{dx}} = y^2$

A. is of order 1

B. is of degree 2

C. is linear

D. is non-linear

Answer: A::B::D



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2. The function $f(x)$ satisfying the equation

$$f^2(x) + 4f'(x)f(x) + (f'(x))^2 = 0$$

A. $f(x) = C. e^{(2-\sqrt{3})x}$

B. $f(x) = C. e^{(2+\sqrt{3})x}$

C. $f(x) = C. e^{(\sqrt{3}-2)x}$

D. $f(x) = C. e^{-(2+\sqrt{3})x}$

Answer: C::D

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3. Which of the following pair (s) *is / are* orthogonal ?

A. $16x^2 + y^2 = c$ and $y^{16} = kx$

B. $y = x + ce^{-x}$ and $x + 2 = y + ke^{-y}$

C. $y = Cx^2$ and $x^2 + 2y^2 = k$

D. $x^2 - y^2 = C$ and $xy = k$

Answer: A::B::C::D

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4. Family of curves whose tangent at a point with its intersection with the curve $xy = c^2$ form an angle of $\frac{\pi}{4}$ is

A. $y^2 - 2xy - x^2 = k$

B. $y^2 + 2xy - x^2 = k$

$$C. y = x - 2c \tan^{-1}\left(\frac{x}{c}\right) + k$$

$$D. y = c \ln \left| \frac{c+x}{c-x} \right| - x + k$$

Answer: B::C::D



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5. The general solution of the differential equation,

$$x \left(\frac{dy}{dx} \right) = y \cdot \log \left(\frac{y}{x} \right) \text{ is}$$

A. $y = x e^{1-c}$

B. $y = x e^{1+c}$

C. $y = ex \cdot e^{Cx}$

D. $y = x e^{Cx}$

Answer: C



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6. Which of the following equation (s) is/are linear?

A. $\frac{dy}{dx} + \frac{y}{x} = \ln x$

B. $y\left(\frac{dy}{dx}\right) + 4x = 0$

C. $dx + dy = 0$

D. $\frac{d^2y}{dx^2} = \cos x$

Answer: A::C::D



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7. The equation of the curve satisfying the differential equation

$y\left(\frac{dy}{dx}\right)^2 + (x - y)\frac{dy}{dx} - x = 0$ can be a (a) circle (b) Straight line (c)

Parabola (d) Ellipse

A. $x - y + 1 = 0$

B. $x^2 + y^2 = 25$

C. $x^2 + y^2 - 5x - 10 = 0$

D. $x+y-7=0$

Answer: A::B



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8. Identify the statement(s) which is/are true.

A. $f(x, y) = e^{y/x} + \frac{\tan(y)}{x}$ is homogeneous of degree zero.

B. $x \cdot \log \frac{y}{x} dx + \frac{y^2}{x} \sin^{-1} \frac{y}{x} dy = 0$ is homogeneous differential equation.

C. $f(x, y) = x^2 + \sin x \cdot \cos y$ is not homogenous.

D. $(x^2 + y^2) dx - (xy^2 - y^3) dy = 0$ is a homogeneous differential equation.

Answer: A::B::C::D



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9. The graph of the function $y = f(x)$ passing through the point (0,1) and satisfying the differential equation $\frac{dy}{dx} + y \cos x = \cos x$ is such that (a) it is a constant function. (b) it is periodic (c) it is neither an even nor an odd function. (d) it is continuous and differentiable for all (e)(f)xg(h)

- A. it is a constant function
- B. it is periodic
- C. it is neither an even nor an odd function
- D. it is continuous and differentiable for all x

Answer: A::B::D

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10. A function $y = f(x)$ satisfies the differential

$$\frac{dy}{dx} \cdot \sin x - y \cos x + \frac{\sin^2 x}{x^2} = 0 \text{ such that } y \rightarrow 0 \text{ as } x \rightarrow \infty. \text{ Then:}$$

A. (a) $\lim_{x \rightarrow 0} f(x) = 1$

B. (b) $\int_0^{\pi/2} f(x) dx$ is lesser than $\frac{\pi}{2}$

C. (c) $\int_0^{\pi/2} f(x) dx$ is greater than unity

D. (d) $f(x)$ is an odd function

Answer: A::B::C::D

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11. Identify the statement(s) which is/are true.

A. $\lim_{x \rightarrow 0} f(x) = 1$

B. $\int_0^{\pi/2} f(x) dx$ is less than $\frac{\pi}{2}$

C. $\int_0^{\pi/2} f(x) dx$ is greater than unity

D. $f(x)$ is an odd function

Answer: A::B::C::D

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12. Let $y = (A + Bx)e^{3x}$ is a Solution of the differential equation

$$\frac{d^2y}{dx^2} + m\frac{dy}{dx} + ny = 0, m, n \in I, \text{ then}$$

A. $m=-6$

B. $n=-6$

C. $m=9$

D. $n=9$

Answer: A::D



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13. A curve C has the property that its initial ordinate of any tangent drawn is less the abscissa of the point of tangency by unity.

Statement I. Differential equation satisfying the curve is linear.

Statement II. Degree of differential equation is one.

- A. Statement I is true ,and Statement II is the correct explanation for Statement I.
- B. Statement I is true, Statement II is true and Statement II is the correct explanation for Statment I
- C. Statement I is true, Statement II is false.
- D. Statement I is false, Statement II is true.

Answer: b

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Exercise Statement I And li Type Questions

1. Statement I Differential equation corresponding to all lines, $ax+by+c=0$ has the order 3.
- Statement II General solution of a differential equation of nth order contains n independent arbitaray constanis.

- A. Statement I is true ,and Statement II is the correct explanation for Statement I.
- B. Statement I is true, Statement II is true and Statement II is the correct explanation for Statment I
- C. Statement I is true, Statement II is false.
- D. Statement I is false, Statement II is true.

Answer: d



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2. Statement I Integral curves denoted by the first order linear differential equation $\frac{dy}{dx} - \frac{1}{x}y = -x$ are family of parabolas passing throught the origin.

Statement II Every differential equation geomrtrically represents a family of curve having some common property.

- A. Statement I is true ,and Statement II is the correct explanation for Statement I.
- B. Statement I is true, Statement II is true and Statement II is the correct explanation for Statment I
- C. Statement I is true, Statement II is false.
- D. Statement I is false, Statement II is true.

Answer: d



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3. Statement I The solution of $(ydx - xdy)\cos\left(\frac{x}{y}\right) = ny^2dx$ is $\sin\left(\frac{x}{y}\right) = Ce^{nx}$ Statement II Such type of differential equation can only be solved by the substitution $x=vy$.

- A. Statement I is true ,and Statement II is the correct explanation for Statement I.

B. Statement I is true, Statement II is true and Statement II is the correct explanation for Statment I

C. Statement I is true, Statement II is false.

D. Statement I is false, Statement II is true.

Answer: d

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4. Statement 1 : The order of the differential equation whose general solution is $y = c_1 \cos 2x + c_2 \sin^2 x + c_3 \cos^2 x + c_4 e^{2x} + c_5 e^{2x+c_6}$ is

3. Statement 2 : Total number of arbitrary parameters in the given general solution in the statement (1) is 3.

A. Statement I is true ,and Statement II is the correct explanation for Statement I.

B. Statement I is true, Statement II is true and Statement II is the correct explanation for Statment I

C. Statement I is true, Statement II is false.

D. Statement I is false, Statement II is true.

Answer: A



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5. Consider differential equation $(x^2 + 1) \cdot \frac{d^2y}{dx^2} = 2x \cdot \frac{dy}{dx}$

Statement I For many member of this family $y \rightarrow \infty$ as $x \rightarrow \infty$.

Statement II Any solution of this differential equation is a polynomial of odd degree with positive coefficient of maximum power.

A. Statement I is true ,and Statement II is the correct explanation for

Statement I.

B. Statement I is true, Statement II is true and Statement II is the

correct explanation for Statment I

C. Statement I is true, Statement II is false.

D. Statement I is false, Statement II is true.

Answer: a



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6. Statement I Order of differential equation of family of parabola whose axis is parallel to y-axis and latusrectum is fixed is 2. Statement II Order of first equation is same as actual number of arbitrary constant present in differential equation.

- A. Statement I is true ,and Statement II is the correct explanation for Statement I.
- B. Statement I is true, Statement II is true and Statement II is the correct explanation for Statment I
- C. Statement I is true, Statement II is false.
- D. Statement I is false, Statement II is true.

Answer: A



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7. Statement I The differential equation of all non-vertical lines in a plane is $\frac{d^2x}{dy^2} = 0$.

Statement II The general equation of all non-vertical lines in a plane is $ax+by=1$, where $b \neq 0$.

- A. Statement I is true ,and Statement II is the correct explanation for Statement I.
- B. Statement I is true, Statement II is true and Statement II is the correct explanation for Statment I
- C. Statement I is true, Statement II is false.
- D. Statement I is false, Statement II is true.

Answer: d



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8. Statement I The order of differential equation of all conics whose centre lies at origin is , 2.

Statement II The order of differential equation is same as number of arbitrary unknowns in the given curve.

A. Statement I is true ,and Statement II is the correct explanation for Statement I.

B. Statement I is true, Statement II is true and Statement II is the correct explanation for Statment I

C. Statement I is true, Statement II is false.

D. Statement I is false, Statement II is true.

Answer: d



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9. Statement I $y = a \sin x + b \cos x$ is general solution of $y'' + y = 0$.

Statement II $y = a \sin x + b \cos x$ is a trigonometric function.

- A. Statement I is true ,and Statement II is the correct explanation for Statement I.
- B. Statement I is true, Statement II is true and Statement II is not the correct explanation for Statment I
- C. Statement I is true, Statement II is false.
- D. Statement I is false, Statement II is true.

Answer: b



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Exercise Passage Based Questions

1. Let $y = f(x)$ satisfies the equation

$$f(x) = (e^{-x} + e^x) \cos x - 2x + \int_0^x (x-t)f'(t)dt$$

y satisfies the differential equation

A. $\frac{dy}{dx} + y = e^x(\cos x - \sin x) - e^{-x}(\cos x + \sin x)$

B. $\frac{dy}{dx} - y = e^x(\cos x - \sin x) - e^{-x}(\cos x + \sin x)$

C. $\frac{dy}{dx} + y = e^x(\cos x + \sin x) - e^{-x}(\cos x - \sin x)$

D. $\frac{dy}{dx} - y = e^x(\cos x - \sin x) + e^{-x}(\cos x - \sin x)$

Answer: A



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2. Let $y = f(x)$ satisfies the equation

$$f(x) = (e^{-x} + e^x) \cos x - 2x + \int_0^x (x-t)f'(t)dt$$

y satisfies the differential equation

A. -1

B. 2

C. 1

D. 0

Answer: D



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3. Let $y = f(x)$ satisfies the equation

$$f(x) = (e^{-x} + e^x) \cos x - 2x + \int_0^x (x - t) f'(t) dt$$

y satisfies the differential equation

A. $e^{-x}(\cos x - \sin x) + \frac{e^x}{5}(3 \cos + \sin x) + \frac{2}{5}e^{-x}$

B. $e^{-x}(\cos x + \sin x) + \frac{e^x}{5}(3 \cos - \sin x) - \frac{2}{5}e^{-x}$

C. $e^{-x}(\cos x - \sin x) + \frac{e^x}{5}(3 \cos - \sin x) + \frac{2}{5}e^{-x}$

D. $e^{-x}(\cos x + \sin x) + \frac{e^x}{5}(3 \cos - \sin x) - \frac{2}{5}e^{-x}$

Answer: C



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4. For certain curve $y = f(x)$ satisfying $\frac{d^2y}{dx^2} = 6x - 4$, $f(x)$ has local minimum value 5 when $x = 1$

Global maximum value of $y = f(x)$ for $x \in [0, 2]$ is

A. 0

B. 1

C. 2

D. 3

Answer: C



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5. For certain curve $y = f(x)$ satisfying $\frac{d^2y}{dx^2} = 6x - 4$, $f(x)$ has local minimum value 5 when $x = 1$

Global maximum value of $y = f(x)$ for $x \in [0, 2]$ is

A. 5

B. 7

C. 8

D. 9

Answer: A



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6. For certain curve $y = f(x)$ satisfying $\frac{d^2y}{dx^2} = 6x - 4$, $f(x)$ has local minimum value 5 when $x = 1$

Global maximum value of $y = f(x)$ for $x \in [0, 2]$ is

A. 5

B. 7

C. 8

D. 9

Answer: B



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7. If any differentisl equation in the form

$$f(f_1(x, y)d(f_1(x, y) + \phi(f_2(x, y)d(f_2(x, y)) + \dots = 0$$

then each term can be intergrated separately.

For example,

$$\int \sin xy d(xy) + \int \left(\frac{x}{y}\right) d\left(\frac{x}{y}\right) = -\cos xy + \frac{1}{2} \left(\frac{x}{y}\right)^2 + C$$

The solution of the differential equation

$$xdy - ydx = \sqrt{x^2 - y^2} dx \text{ is}$$

A. (a) $Cx = e^{\sin^{-1} \frac{y}{x}}$

B. (b) $x e^{\sin^{-1} \frac{y}{x} = c}$

C. (c) $x + e^{\sin^{-1} \frac{y}{x} = c}$

D. (d) None of these

Answer: A



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8. If any differentisl equation in the form

$$f(f_1(x, y)d(f_1(x, y) + \phi(f_2(x, y)d(f_2(x, y)) + \dots = 0$$

then each term can be intergrated separately.

For example,

$$\int \sin xy d(xy) + \int \left(\frac{x}{y}\right) d\left(\frac{x}{y}\right) = -\cos xy + \frac{1}{2}\left(\frac{x}{y}\right)^2 + C$$

The solution of the differential equation

$$(xy^4 + y)dx - xdy = 0 \text{ is}$$

A. $\frac{x^3}{4} + \frac{1}{2}\left(\frac{x}{y}\right)^2 = C$

B. $\frac{x^4}{4} + \frac{1}{3}\left(\frac{x}{y}\right)^3 = C$

C. $\frac{x^4}{4} - \frac{1}{2}\left(\frac{x}{y}\right)^3 = C$

D. $\frac{x^4}{4} - \frac{1}{2}\left(\frac{x}{y}\right)^2 = C$

Answer: B



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9. If any differential equation in the form

$$f(f_1(x, y))d(f_1(x, y)) + \phi(f_2(x, y))d(f_2(x, y)) + \dots = 0$$

then each term can be intergrated separately.

For example,

$$\int \sin xy d(xy) + \int \left(\frac{x}{y}\right) d\left(\frac{x}{y}\right) = -\cos xy + \frac{1}{2}\left(\frac{x}{y}\right)^2 + C$$

Solution of differential equation

$$(2x \cos y + y^2 \cos x) dx + (2y \sin x - x^2 \sin y) dy = 0 \text{ is}$$

A. $x^2 \cos y + y^2 \sin x = C$

B. $x \cos y + y \sin x = C$

C. $x^2 \cos^2 y + y^2 \sin^2 x = C$

D. None of the above

Answer: A



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10. Differential equation $\frac{dy}{dx} = f(x)g(y)$ can be solved by separating variable $\frac{dy}{g(y)} = f(x)dx$.

The equation of the curve to the point (1,0) which satisfies the differential equation $(1 + y^2)dx = xydy = 0$ is

A. $x^2 + y^2 = 1$

B. $x^2 - y^2 = 1$

C. $x^2 + y^2 = 2$

D. None of these

Answer: B



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11. Differential equation $\frac{dy}{dx} = f(x)g(x)$ can be solved by separating variable $\frac{dy}{g(y)} = f(x)dx$.

Solution of the differential equation $\frac{dy}{dx} + \frac{1 + y^2}{\sqrt{1 - x^2}} = 0$ is

A. $\tan^{-1} y + \sin^{-1} x = C$

B. $\tan^{-1} x + \sin^{-1} y = C$

C. $\tan^{-1} y \cdot \sin^{-1} x = C$

D. $\tan^{-1} y - \sin^{-1} x = C$

Answer: A



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12. Differential equation $\frac{dy}{dx} = f(x)g(x)$ can be solved by separating variable $\frac{dy}{g(y)} = f(x)dx$.

If $\frac{dy}{dx} = 1 + x + y + xy$ and $y(-1) = 0$, then y is equal to

A. $e^{\frac{1-x^2}{2}}$

B. $e^{\frac{1+x^2}{2}} - 1$

C. $\ln(1+x) - 1$

D. None of these

Answer: B



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13. Let C be the set of curves having the property that the point of intersection of tangent with y -axis is equidistant from the point of tangency and origin $(0,0)$

If $C_1, C_2 \in C$ such that

C_1 : Curve is passing through $(1, 0)$

C_2 : Curve is passing through $(-1, 0)$

The number of common tangents for C_1 and C_2 is

A. 1

B. 2

C. 3

D. None of these

Answer: C



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14. Let C be the set of curves having the property that the point of intersection of tangent with y -axis is equidistant from the point of tangency and origin $(0,0)$

If $C_3 \in C$

C_3 : is passing through $(2,4)$. If $\frac{x}{a} + \frac{y}{b} = 1$. is tangent to C_3 , then

A. $25a + 10b^2 - ab^2 = 0$

B. $25a + 10b - 13ab = 0$

C. $13a + 25b - 16ab = 0$

D. $29a + b - 13ab = 0$

Answer: A

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15. Let C be the set of curves having the property that the point of intersection of tangent with y -axis is equidistant from the point of tangency and origin $(0,0)$

If common tangents of C_1 and C_2 form an equilateral triangle, where C_1, C_2 in C and C_1 : Curve passes through $f(2,0)$, then C_2 may passes through

A. $(-1/3, 1/3)$

B. $(-1/3, 1)$

C. $(-2/3, 4)$

D. $(-2/3, 2)$

Answer: A



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1. Match the following :

| Column I | Column II |
|---|---|
| (A) $\frac{xdx + ydy}{xdy - ydx} = \sqrt{\frac{a^2 - x^2 - y^2}{x^2 + y^2}}$ | (p) $y = \frac{C}{x^3} e^{-1/x}$ |
| (B) Solution of $\cos^2 x \frac{dy}{dx} - \tan 2x \cdot y = \cos^4 x$, where $ x < \frac{\pi}{4}$ and $y\left(\frac{\pi}{6}\right) = \frac{3\sqrt{3}}{8}$ | (q) $\sqrt{x^2 + y^2} = a \sin \left\{ C + \tan^{-1} \left(\frac{y}{x} \right) \right\}$ |
| (C) The equation of all possible curves that will cut each member of the family of circles $x^2 + y^2 - 2cx = 0$ at right angle | (r) $x^2 + y^2 + Cy = 0$ |
| (D) Solution of the equation $x \int_0^x y(t) dt = (x+1) \int_0^x y(t) dt, x > 0$ is | (s) $y = \frac{\sin 2x}{2(1 - \tan^2 x)}$ |



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2. Match the following :

| Column I | Column II |
|--|---------------------------|
| (A) Circular plate is expanded by heat from radius 5 cm to 5.06 cm. Approximate increase in area is | (p) 4 |
| (B) Side of cube increasing by 1%, then percentage increase in volume is | (q) 0.6π |
| (C) If the rate of decrease of $\frac{x^2}{2} - 2x + 5$ is twice the rate of decrease of x , then x is equal to | (r) 3 |
| (D) Rate of increase in area of equilateral triangle of side 15 cm, when each side is increasing at the rate of 0.1 cm/s: is | (s) $\frac{3\sqrt{3}}{4}$ |



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3. Match the following :

| Column I | Column II |
|--|-----------|
| (A) The differential equation of the family of curves $y = e^x (A \cos x + B \sin x)$, where A, B are arbitrary constants, has the degree n and order m . Then, the values of n and m are, respectively | (p) 2, 1 |
| (B) The degree and order of the differential equation of the family of all parabolas whose axis is the x -axis, are respectively | (q) 1, 1 |
| (C) The order and degree of the differential equations of the family of circles touching the x -axis at the origin, are respectively | (r) 2, 2 |
| (D) The degree and order of the differential equation of the family of ellipse having the same foci, are respectively. | (s) 1, 2 |



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Exercise Single Integer Answer Type Questions

1. Find the constant of intergration by the general solution of the differential equation $(2x^2y - 2y^4)dx + (2x^3 + 3xy^3)dy = 0$ if curve passes through (1,1).



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2. A tank initially contains 50 gallons of fresh water. Brine contains 2 pounds per gallon of salt, flows into the tank at the rate of 2 gallons per

minutes and the mixture kept uniform by stirring, runs out at the same rate. If it will take for the quantity of salt in the tank to increase from 40 to 80 pounds (in seconds) is 206λ , then find λ

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3. If $f: R - \{-1\} \rightarrow R$ and f is differentiable function satisfies $f(x + f(y) + xf(y)) = y + f(x) + y \cdot f(x) \forall x, y \in R - \{-1\}$ then find the value of $2010[1 + f(2009)]$

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4. If $\phi(x)$ is a differential real-valued function satisfying $\phi'(x) + 2\phi(x) \leq 1$, then the value of $2\phi(x)$ is always less than or equal to

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5. The degree of the differential equation satisfying by the curves

$$\sqrt{1+x} - a\sqrt{1+y} = 1, \text{ is}$$

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6. Let $f(x)$ be a differentiable bounded function satisfying

$$2f^5(x) \cdot f'(x) + 2(f'(x))^3 \cdot f^5(x) = f''(x). \text{ If } f(x) \text{ is bounded in}$$

between $y = k_1$, and $y = k_2$, then the number of intergers between

k_1 and k_2 is/are (where $f(0) = f'(0) = 0$).

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7. Let $y(x)$ be a function satisfying $\frac{d^2y}{dx^2} - \frac{dy}{dx} + e^{2x} = 0$, $y(0) =$ and

$y'(0) = 1$. If maximum value of $y(x)$ is $y(\alpha)$, then integral part of 2α

is.....

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8. Find the time required for a cylindrical tank of radius r and height H to empty through a round hole of area a at the bottom. The flow through the hole is according to the law $v(t) = k\sqrt{2gh(t)}$, where $v(t)$ and $h(t)$, are respectively, the velocity of flow through the hole and the height of the water level above the hole at time t , and g is the acceleration due to gravity.



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Exercise Subjective Type Questions

1. A hemi-spherical tank of radius 2 m is initially full of water and has an outlet of 12cm^2 cross-sectional area at the bottom. The outlet is opened at some instant. The flow through the outlet is according to the law $v(t) = 0.6\sqrt{2gh(t)}$, where $v(t)$ and $h(t)$ are, respectively, the velocity of the flow through the outlet and the height of water level above the outlet and the height of water level above the outlet at time t , and g is the acceleration due to gravity. Find the time it takes to empty the tank.



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2. Let $f: \mathbb{R}^+ \rightarrow \mathbb{R}$ satisfies the functional equation $f(xy) = e^{xy-x-y}\{e^y f(x) + e^x f(y)\}$, $\forall x, y \in \mathbb{R}^+$. If $f'(1) = e$, determine $f(x)$.

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3. Let $y=f(x)$ be curve passing through $(1, \sqrt{3})$ such that tangent at any point P on the curve lying in the first quadrant has positive slope and the tangent and the normal at the point P cut the x-axis at A and B respectively so that the mid-point of AB is origin. Find the differential equation of the curve and hence determine $f(x)$.

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4. If y_1 and y_2 are the solutions of the differential equation $\frac{dy}{dx} + Py = Q$, where P and Q are functions of x alone and $y_2 = y_1 z$,

then move that $z = 1 + ce^{-\int \left(\frac{Q}{y}\right) dx}$, where c is an arbitrary constant.

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Differential Equations Exercise 7

1. Let $y=f(x)$ be a differentiable function $\forall \xi \in R$ and satisfies:

$$f(x) = x + \int_0^1 x^2 z f(z) dz + \int_0^1 x z^2 f(z) dz.$$

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Exercise Questions Asked In Previous 13 Years Exam

1. If $f: R - \{-1\} \rightarrow R$ and f is differentiable function satisfies:

$$f((x) + f(y) + x f(y)) = y + f(x) + y f(x) \forall x,$$

$y \in R - \{-1\}$ Find $f(x)$.

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2. A solution curve of the differential equation $(x^2 + xy + 4x + 2y + 4) \left(\frac{dy}{dx} \right) - y^2 = 0$ passes through the point $(1, 3)$. Then the solution curve is

- A. intersects $y=x+2$ exactly at one point
- B. intersects $y=x+2$ exactly at two points
- C. intersects $y = (x + 2)^2$
- D. does not intersect $y = (x + 3)^2$

Answer: A:D



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3.

Let $f: (0, \infty) \rightarrow \mathbb{R}$ be a differentiable function such that $f'(x) = 2 -$

Then

A. $\lim_{x \rightarrow 0^+} \int' \left(\frac{1}{x} \right) = 1$

B. $\lim_{x \rightarrow 0^+} x \int \left(\frac{1}{x} \right) = 1$

C. $\lim_{x \rightarrow 0^+} x^2 \int \left(\frac{1}{x} \right) = 1$

D. $|f(x)| \leq 2$ for all $x \in (0, 2)$

Answer: A::D



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4. Let $y(x)$ be a solution of the differential equation $(1 + e^x)y' + ye^x = 1$. If $y(0) = 2$, then which of the following statements is (are) true?

A. $y(-4)=0$

B. $y(-2)=0$

C. $y(x)$ has a critical point in the interval $(-1,0)$

D. $y(x)$ has no critical point in the interval $(-1,0)$

Answer: A::C::D

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5. Consider the family of all circles whose centers lie on the straight line $y = x$. If the family of circles is represented by the differential equation $P y'' + Q y' + 1 = 0$, where P, Q are functions of x, y and y' (here $y' = \frac{dy}{dx}, y'' = \frac{d^2y}{dx^2}$), then which of the following statements is (are) true?

A. $P=y+x$

B. $P=y-x$

C. $P+Q=1-x+y+y'+(y')^2$

D. $P-Q=x+y-y'-(y')^2$

Answer: B::C::D

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6. The function $y = f(x)$ is the solution of the differential equation

$$\frac{dy}{dx} + \frac{xy}{x^2 - 1} = \frac{x^4 + 2x}{\sqrt{1 - x^2}} \text{ in } (-1, 1) \text{ satisfying } f(0) = 0. \text{ Then}$$

$$\int_{\frac{\sqrt{3}}{2}}^{\frac{\sqrt{3}}{2}} f(x) dx \text{ is (a) (b)(c)(d) } \frac{\pi}{e} 3(f)(g) - (h) \frac{(i)\sqrt{(j)3(k)(l)}}{m} 2(n)(o)(p)$$

$$(q) (b) (r)(s)(t) \frac{\pi}{u} 3(v)(w) - (x) \frac{(y)\sqrt{(z)3(aa)(bb)}}{cc} 4(dd)(ee)(ff) (gg)$$

$$(c) (d)(e)(f) \frac{\pi}{g} 6(h)(i) - (j) \frac{(k)\sqrt{(l)3(m)(n)}}{o} 4(p)(q)(r) \quad (s) \quad (d)$$

$$(t)(u)(v) \frac{\pi}{w} 6(x)(y) - (z) \frac{(aa)\sqrt{(bb)3(cc)(dd)}}{ee} 2(ff)(gg)(hh) \text{ (ii)}$$

A. $\frac{\pi}{3} - \frac{\sqrt{3}}{2}$

B. $\frac{\pi}{3} - \frac{\sqrt{3}}{4}$

C. $\frac{\pi}{6} - \frac{\sqrt{3}}{4}$

D. $\frac{\pi}{6} - \frac{\sqrt{3}}{2}$

Answer: B



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7. Let $f: \left[\frac{1}{2}, 1\right] \rightarrow \mathbb{R}$ (the set of all real numbers) be a positive, non-constant, and differentiable function such that $f'(x) < 2f(x)$ and $f\left(\frac{1}{2}\right) = 1$. Then the value of $\int_{\frac{1}{2}}^1 f(x) dx$ lies in the interval (a) $(2e - 1, 2e)$ (b) $(3 - 1, 2e - 1)$ $\left(\frac{e - 1}{2}, e - 1\right)$ (d) $\left(0, \frac{e - 1}{2}\right)$

A. $(2e-1, 2e)$

B. $(e-1, 2e-1)$

C. $\left(\frac{e - 1}{2}, e - 1\right)$

D. $\left(0, \frac{e - 1}{2}\right)$

Answer: D



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8. A curve passes through the point $\left(1, \frac{\pi}{6}\right)$. Let the slope of the curve at each point (x, y) be $\frac{y}{x} + \sec\left(\frac{y}{x}\right)$, $x > 0$. Then, the equation of the curve

is

A. $\sin\left(\frac{y}{x}\right) = \log x + \frac{1}{2}$

B. $\operatorname{cosec}\frac{y}{x} = \log x + 2$

C. $\sec\left(\frac{2y}{x}\right) = \log x + 2$

D. $\cos\left(\frac{2y}{x}\right) = \log x + \frac{1}{2}$

Answer: A



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9. Let $f: [0, 1] \rightarrow \mathbb{R}$ (the set of all real numbers) be a function. Suppose the function f is twice differentiable, $f(0) = f(1) = 0$ and satisfies $f'(x) - 2f''(x) + f(x) \geq e^x, x \in [0, 1]$ If the function $e^{-x}f(x)$ assumes its minimum in the interval $[0, 1]$ at $x = \frac{1}{4}$, which of the following is true?

(A) $f'(x) < f(x), \frac{1}{4} < x < \frac{3}{4}$

(B) $f'(x) > f(x), 0 < x < \frac{1}{4}$

(C) $f'(x) < f(x), 0 < x < \frac{1}{4}$

(D) $f'(x) < f(x), \frac{3}{4} < x < 1$

A. $f'(x) < f(x), \frac{1}{4} < x < \frac{3}{4}$

B. $f'(x) > f(x), 0 < x < \frac{1}{4}$

C. $f'(x) < f(x), 0 < x < \frac{1}{4}$

D. $f'(x) < f(x), \frac{3}{4} < x < 1$

Answer: C



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10. Let $f: [0, 1] \rightarrow \mathbb{R}$ be a function. Suppose the function f is twice differentiable, $f(0) = f(1) = 0$ and satisfies $f''(x) - 2f'(x) + f(x) \geq e^x, x \in [0, 1]$ Which of the following is true for $0 < x < 1$?

A. (a) $0 < f(x) < \infty$

B. (b) $-\frac{1}{2} < f(x) < \frac{1}{2}$

C. (c) $-\frac{1}{4} < f(x) < 1$

D. (d) $-\infty < f(x) < 0$

Answer: D



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11. Let $f: [0, 1] \rightarrow \mathbb{R}$ (the set of all real numbers) be a function. Suppose the function f is twice differentiable, $f(0) = f(1) = 0$ and satisfies $f''(x) - 2f'(x) + f(x) \geq e^x, x \in [0, 1]$ Which of the following is true for $0 < x < 1$? (A) $0 < f(x) < \infty$ (B) $-\frac{1}{2} < f(x) < \frac{1}{2}$ (C) $-\frac{1}{4} < f(x) < 1$ (D) $-\infty < f(x) < 0$

A. g is increasing on $(1, \infty)$

B. g is decreasing on $(0, 1)$

C. g is increasing on $(1,2)$ and decreasing on $(2, \infty)$

D. g is decreasing on $(1,2)$ and increasing on $(2, \infty)$

Answer: B



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12. Let $f: [0, 1] \rightarrow \mathbb{R}$ (the set of all real numbers) be a function. Suppose the function f is twice differentiable, $f(0)=f(1)=0$ and satisfies

$$f''(x) - 2f'(x) + f(x) \geq e^x, x \in [0, 1]$$
 Consider the statements.

I. There exists some $x \in \mathbb{R}$ such that, $f(x) + 2x = 2(1 + x^2)$

(II) There exists some $x \in \mathbb{R}$ such that, $2f(x)+1=2x(1+x)$

A. Both I and II are true

B. I is true and II is false

C. I is false and II is true

D. Both I and II are false

Answer: C



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13. If $y(x)$ satisfies the differential equation $y' - y \tan x = 2x \sec x$ and $y(0) = 0$, then

(a) $y\left(\frac{\pi}{4}\right) = \frac{\pi}{g} 4(h)(i)(j) = (k) \frac{(l)(m)\pi^{(n)2(o)}(p)}{q} \left((r) 8\sqrt{(s)2(t)} \right)$

(b) *[Math Processing Error]* (xx) (c)

(d) $y\left(\frac{\pi}{i} 3(j)(k)(l)\right) = (m) \frac{(n)(o)\pi^{(p)2(q)}(r)}{s} 9(t)(u)(v)$

(w) (d) *[Math Processing Error]* (ddd)

A. $y\left(\frac{\pi}{4}\right) = \frac{\pi^2}{8\sqrt{2}}$

B. $y\left(\frac{\pi}{4}\right) = \frac{\pi^2}{18}$

C. $y\left(\frac{\pi}{3}\right) = \frac{\pi^2}{9}$

D. $y\left(\frac{\pi}{3}\right) = \frac{4\pi}{3} + \frac{2\pi^2}{3\sqrt{3}}$

Answer: D

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14. Let $y'(x) + y(x)g'(x) = g(x)g'(x)$, $y(0) = 0$, $x \in R$, where $f'(x)$ denotes $\frac{dy(x)}{dx}$, and $g(x)$ is a given non-constant differentiable function

on R with $g(0) = g(2) = 0$. Then the value of $y(2)$ is _____



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15. Let $f: R \rightarrow R$ be a continuous function which satisfies $f(x) = \int_0^x f(t) dt$. Then the value of $f(1n5)$ is _____



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16. Let a solution $y=y(x)$ of the differential equation

$$x\sqrt{x^2-1}dy - y\sqrt{y^2-1}dx = 0 \text{ satisfy } y(2) = \frac{2}{\sqrt{3}}$$

Statement I $y(x) = \sec\left(\sec^{-1}x - \frac{\pi}{6}\right)$

Statement II $y(x)$ is given by $\frac{1}{y} = \frac{2\sqrt{3}}{x} - \sqrt{1 - \frac{1}{x^2}}$

A. Statement I is true, Statement II is also true, Statement II is the correct explanation of Statement I.

B. Statement I is true, Statement II is also true, Statement II is not the correct explanation of Statement I.

C. Statement I is true, Statement II is false.

D. Statement I is false, Statement II is true.

Answer: C



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17. If a curve $y = f(x)$ passes through the point $(1, -1)$ and satisfies the differential equation $y(1 + xy)dx = xdy$, then $f\left(-\frac{1}{2}\right)$ is equal to:

A. $-\frac{2}{5}$

B. $-\frac{4}{5}$

C. $\frac{2}{5}$

D. $\frac{4}{5}$

Answer: D



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18. Let $y(x)$ be the solution of the differential equation $(x \log x) \frac{dy}{dx} + y = 2x \log x$, ($x \geq 1$), Then $y(e)$ is equal to

A. e

B. 0

C. 2

D. 2e

Answer: C



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19. Let the population of rabbits surviving at a time t be governed by the differential equation $\frac{dp(t)}{dt} = \frac{1}{2}p(t) - 200$. If $p(0) = 100$, then $p(t)$ equals (1) $400 - 300e^{t/2}$ (2) $300 - 200e^{-t/2}$ (3) $600 - 500e^{t/2}$ (4) $40 - 300e^{-t/2}$

A. $400 - 300e^{\frac{t}{2}}$

B. $300 - 200e^{\frac{t}{2}}$

C. $600 - 500e^{\frac{t}{2}}$

D. $400 - 300e^{\frac{t}{2}}$

Answer: A



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20. At present, a firm is manufacturing 2000 items. It is estimated that the rate of change of production P w.r.t. additional number of workers x is given by $\frac{dP}{dx} = 100 - 12\sqrt{x}$. If the firm employs 25 more workers, then the new level of production of items is (1) 3000 (2) 3500 (3) 4500 (4) 2500

A. 2500

B. 3000

C. 3500

D. 4500

Answer: C



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21. The population $p(t)$ at time t of a certain mouse species satisfies the differential equation $d\frac{p(t)}{dt} = 0.5p(t) - 450$ If $p(0) = 850$, then the time at which the population becomes zero is

(1) $2 \ln 18$ (2) $\ln 9$ (3) $\frac{1}{2} \ln 18$ (4) $\ln 18$

A. $2\log 18$

B. $\log 9$

C. $\frac{1}{2}\log 18$

D. $\log 18$

Answer: A



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22. If $\frac{dy}{dx} = y + 3$ and $y(0)=2$, then $y(\log 2)$ is equal to

A. 5

B. 13

C. -2

D. 7

Answer: D



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23. Let I be the purchase value of an equipment and $V(t)$ be the value after it has been used for t years. The value $V(t)$ depreciates at a rate

given by differential equation $\frac{dV(t)}{dt} = -k(T-t)$, where $k > 0$ is a constant

and T is the total life in years of the equipment. Then the scrap value $V(T)$

of the equipment is : (1) $T^2 - \frac{1}{k}$ (2) $I - \frac{kT^2}{2}$ (3) $I - \frac{k(T-t)^2}{2}$ (4)

e^{-kT}

A. $I - \frac{kT^2}{2}$

B. $I - \frac{k(T - t^2)}{2}$

C. e^{-kT}

D. $T^2 - \frac{1}{k}$

Answer: A



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24. Solution of the differential equation

$\cos x dy = y(\sin x - y)dx, 0 < x < \frac{\pi}{2}$ is

A. $\sec x = (\tan x + C)y$

B. $y \sec x = \tan x + C$

C. $y \tan x = \sec x + C$

D. $\tan x = (\sec x + C)y$

Answer: A



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25. The differential equation which represents the family of curves $y = c_1 e^{c_2 x}$ where c_1 and c_2 are arbitrary constants is

A. $y' = y^2$

B. $y'' = y'y$

C. $yy'' = y'$

D. $yy'' = (y')^2$

Answer: D



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26. The differential equation of the family of circles with fixed radius 5 units and centre on the line $y=2$ is

A. $(x - 2)y'^2 = 25 - (y - 2)^2$

B. (b) $(y - 2)y'^2 = 25 - (y - 2)^2$

C. (c) $(y - 2)y'^2 = 25 - (y - 2)^2$

D. (d) $(x - 2)y'^2 = 25 - (y - 2)^2$

Answer: C



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