



MATHS

BOOKS - ARIHANT MATHS (ENGLISH)

SEQUENCES AND SERIES

Examples

1. If
$$f\!:\!N o R,\,\,$$
 where $f(n)=a_n=rac{n}{\left(2n+1
ight)^2}$ write the sequence in

ordered pair from.





3. If the sum of n terms of a series is $2n^2 + 5n$ for all values of n, find its

7th term.

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4. (i) Write
$$\sum_{r=1}^{n} (r^2 + 2)$$
 in expanded form.
(ii) Write the series $\frac{1}{3} + \frac{2}{4} + \frac{3}{5} + \frac{4}{6} + \ldots + \frac{n}{n+2}$ in sigma form.
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5. Which of the following are A.P. (i) 1,3,5,7,...

(ii)
$$\pi, \pi + e^{\pi}, \pi + 2e^{\pi},$$

(iii) $a, a-b, a-2b, a-3b, \ldots$

6. Show that the sequence t_n defined by $t_n = 5n + 4$ is AP, also find its

common difference.



10. If $|x-1|, 3 ext{ and } |x-3|$ are first three terms of an increasing AP, then

find the 6th term of on AP.



11. In the sequence 1,2,2,3,3,4,4,4,4, , where n consecutive terms

have the value n, the 150th term, is

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12. If a_1, a_2, a_3, a_4 and a_5 are in AP with common difference $\neq 0$, find

the value of $\sum_{i=1}^5 a_i$ when $a_3=2.$

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13. The ratio of the sum of mandn terms of an A.P. is $m^2 : n^2$. Show that

the ratio of the mth and nth terms is (2m-1) : (2n-1).

A.
$$(2m + 1): (2n - 1),$$

 $\mathsf{B}.\,m\!:\!n$

C.
$$(2m-1):(2n-1)$$

D. None of these

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14. The sums of n terms of two arithmetic progresssions are in the ratio (7n + 1): (4n + 17). Find the ratio of their nth terms and also common differences.

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15. The sums of n terms of two AP's are in the ratio (3n-13):(5n+21). Find the ratio of their 24th terms.

16. How many terms of the A.P. 20, $19\frac{1}{3}$, $18\frac{2}{3}$, must be taken so that their sum is 300?



occupying the odd places is equal to $\frac{25}{2}$

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18. If the set of natural numbers is partitioned into subsets $S_1=\{1\}, S_2=\{2,3\}, S_3=\{4,5,6\}$ and so on then find the sum of the terms in S_{50} .



19. Find the sum of first 24 terms of on AP $t_1, t_2, t_3, ...,$ if it is known that $t_1 + t_5 + t_{10} + t_{15} + t_{20} + t_{24} = 225.$

20. If (1+3+5++p) + (1+3+5++q) = (1+3+5++r)where each set of parentheses contains the sum of consecutive odd integers as shown, the smallest possible value of p + q + r(where p > 6)is 12 b. 21 c. 45 d. 54

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21. If S_1, S_2, S_3, S_m are the sums of n terms of m A.P. 's whose first terms are 1, 2, 3, ..., m and common differences are 1, 3, 5, ..., (2m - 1) respectively. Show that $S_1 + S_2.... + S_m = \frac{mn}{2}(mn + 1)$

22. Let α and β be roots of the equation $X^2 - 2x + A = 0$ and let γ and δ be the roots of the equation $X^2 - 18x + B = 0$. If $\alpha < \beta < \gamma < \delta$ are in arithmetic progression then find the valus of A and B.



23. The digits of a positive integer, having three digits, are in A.P. and their sum is 15. The number obtained by reversing the digits is 594 less than the original number. Find the number.



24. If three positive real numbers a,b,c are in A.P. such that abc=4, then the

minimum value of b is



25. If a,b,c,d are distinct integers in an A.P. such that $d = a^2 + b^2 + c^2$,

then find the value of a+b+c+d.





33. Show that the sequence t_n defined by $t_n = rac{2^{2n-1}}{3}$ for all values of

 $n \in N$ is a GP. Also, find its common ratio.



34. Show that the sequence t_n defined by $t_n = 2 \cdot 3^n + 1$ is not a GP.



35. If first term of a GP is a, third term is b and (n+1)th term is c. The

$$(2n+1)th$$
 term of a GP is

A.
$$c\sqrt{\frac{b}{a}}$$

B. $\frac{bc}{a}$
C. abc
D. $\frac{c^2}{a}$

36. In a GP if the (m+n)th term is p and (m-n)th term is q then mth

term is

A. $p{\left(rac{q}{p}
ight)}^{rac{m}{2n}}$ B. \sqrt{pq}

C.
$$\sqrt{\frac{p}{q}}$$

D. None of these

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37. If $\sin heta,\sqrt{2}(\sin heta+1),6\sin heta+6$ are in GP, than the fifth term is

A. 81

B. $81\sqrt{2}$

C. 162

D. $162\sqrt{2}$

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38. The 1025th term in the sequence are $1, 22, 4444, 88888888, \ldots$ is

A. 2⁹ B. 2¹⁰ C. 2¹¹

 $\mathsf{D.}\,2^{12}$



39. If a, b, c are real numbers such that $3(a^2+b^2+c^2+1)=2(a+b+c+ab+bc+ca)$, than a, b, care in A. AP only

B. GP only

C. GP and AP

D. None of these

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40. Find the value of 0.3258.

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41. Find the sum upto n terms of the series $a + aa + aaa + aaaa +, \forall a \in N$ and $1 \leq a \leq 9$.



42. Find the sum of the series upto n terms $0. b + 0. bb + 0. bbb + 0. bbbb +, \forall b \in N \text{ and } 1 \leq b \leq 9.$

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43. If N, the set of natural numbers is partitioned into groups $S_1 = \{1\}, S_2 = \{2, 3\}, S_3 = \{4, 5, 6, 7\}, S_4 = \{8, 9, 10, 11, 12, 13, 14, 15\},$ find the sum of the numbers in S_{50} .

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44. If
$$S_n = 1 + rac{1}{2} + rac{1}{2^2} + \ldots + rac{1}{2^{n-1}}$$
 and $2 - S_n < rac{1}{100},$ then the

least value of n must be :

$$X = 1 + a + a^2 + a^3 + ... + \infty$$
 and $y = 1 + b + b^2 + b^3 + ... + \infty$

$$1 + ab + a^2b^2 + a^3b^3 + ... + \infty = rac{xy}{x+y-1}, ext{where} \ \ 0 < a < 1 \ \ ext{and} \ \ 0 < a < 1$$

46. If
$$1 + ab + a^2b^2 + a^3b^3 + ... + \infty = \frac{xy}{x+y-1}$$
 are the sum of infinire geometric series whose first terms are $1, 2, 3, ..., p$ and whose common ratios are $S_1, S_2, S_3, ..., S_p \frac{1}{2}, \frac{1}{3}, \frac{1}{4}, ... \frac{1}{p+1}$ respectively, prove that $S_1 + S_2 + S_3 + ... + S_p = \frac{p(p+3)}{2}$.

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47. If x_1, x_2 be the roots of the equation $x^2 - 3x + A = 0$ and x_3, x_4 be those of the equation $x^2 - 12x + B = 0$ and x_1, x_2, x_3, x_4 be an increasing GP. find find A and B.



that

48. Suppose a, b, c are in AP and a^2, b^2, c^2 are in GP, If a > b > c and $a + b + c = \frac{3}{2}$, than find the values of a and c.

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49. If the continued product of three numbers in GP is 216 and the sum of

their products in pairs is 156, then find the sum of three numbers.



50. Find a three digit numberwhose consecutive digits form a GP. If we subtract 792 from this number, we get a number consisting of the same digits written in the reverse order. Now, if we increase the second digit of the required number by 2, then the resulting digits will form an AP.

51. A square is drawn by joining mid pint of the sides of a square. Another square is drawn inside the second square in the same way and the process is continued in definitely. If the side of the first square is 16 cm, then what is the sum of the areas of all the squares ?

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52. One side of an equilateral triangle is 24 cm. The midpoints of its sides are joined to form another triangle whose midpoints are in turn joined to form still another triangle this process continues indefinitely. The sum of the perimeters of all the triangles is

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53. Let S_1, S_2 , be squares such that for each $n \ge 1$, the length of a side of S_n equals the length of a diagonal of S_{n+1} . If the length of a side of $S_1is10cm$, then for which of the following value of n is the area of S_n less than 1 sq. cm? a. 5 b. 7 c. 9 d. 10

54. about to only mathematics



55. Dipesh writes letters to four of his friends. He asks each of them to copy the letter and mail to four different persons with the request that they continue the chain similarly. Assuming that the chain is not broken and that it costs 25 paise to mail one letter, find the total money spent on postage till the 8th set of letters is mailed.

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56. An insect starts from a point and travels in a straight path 1 mm in the first second and half of the distance covered in the previous second in the succeeding second. In how much time would it reach a point 3 mm away from its starting point.

57. The pollution in a normal atmosphere is less than 0.01 %. Due to leakage of a gas from a factory, the pollution is increased to 20%. If every day 80% of pollution is neutralised, in how many days the atmosphere will be normal?

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58. If a, b, c are in HP, then
$$\frac{a-b}{b-c}$$
 is equal to

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59. Find the first term of a HP whpse secpmd ter, os $\frac{5}{4}$ and the third term is $\frac{1}{2}$.

60. If
$$\frac{1}{a} + \frac{1}{a-b} + \frac{1}{c} + \frac{1}{c-b} = 0$$
 and $a + c - b \neq 0$, then prove that
 a, b, c are in H.P.
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61. If $a_1, a_2, a_3, \dots, a_n$ are in HP, than prove that
 $a_1a_2 + a_2a_3 + a_3a_4 + \dots + a_{n-1}a_n = (n-1)a_1a_n$

62. The sum of three numbers in HP is 37 and the sum of their reciprocals is $\frac{1}{4}$. Find the numbers.

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63. If pth, qth and rth terms of a HP be respectivelya, b and c, has prove that (q - r)bc + (r - p)ca + (p - q)ab = 0. **64.** If a, b, c, are in AP, a^2, b^2, c^2 are in HP, then prove that either a = b = c or $a, b, -\frac{c}{2}$ from a GP (2003, 4M)



65. If a, b, c are in HP,b,c,d are in GP and c, d, e are in AP, than show that

$$e=rac{ab^2}{\left(2a-b
ight)^2}.$$

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66. Given a,b,c are in A.P.,b,c,d are in G.P and c,d,e are in H.P. If a=2 and e=18

, then the sum of all possible values of c is _____.

67. If three positive numbers a, b and c are in AP, GP and HP as well, than

find their values.

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68. If *a*, *b*, *c* are in AP and p is the AM between a and b and q is the AM between b and c, then show that b is the AM between p and q.

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69. Find the value of n so that $rac{a^{n+1}+b^{n+1}}{a^n+b^n}$ may be the geometric mean

between a and b.

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70. There are n AM's between 3 and 54. Such that the 8th mean and

$$(n-2)$$
th mean is 3 ratio 5. Find n.

71. If 11 AM's are inserted between 28 and 10, than find the three middle terms in the series.





numbers, prove that

$$G^2=(2p-q)(2q-p)$$





76. Insert five geimetrec means between $\frac{1}{3}$ and 9 and verify that their product is the fifth power of the geometric mean between $\frac{1}{3}$ and 9.

77. AM between two numbers whose sum is 100 is ti the GM as 5:4`, find

the numbers.



78. If $a_1, a_2, a_3, \dots, a_n$ are positive real numbers whose product is a fixed number c, then the minimum value of $a_1 + a_2 + \dots + a_{n-1} + 3a_n$ is

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79. If H be the harmonic mean between x and y, then show that $\frac{H+x}{H-x} + \frac{H+y}{H-y} = 2$

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80. IF $a_1, a_2, a_3, ..., a_{10}$ be in AP and $h_1, h_2, h_3, ..., h_{10}$ be in HP. If $a_1 = h_1 = 2$ and $a_{10} = h_{10} = 3$, then find value of a_4h_7 .



81. Find n, so that
$$rac{a^{n+1}+b^{n+1}}{a^n+b^n}(a
eq b)$$
 be HM beween a and b.



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83. If $A^x = G^y = H^z$, where A, G, H are AM,GM and HM between two

given quantities, then prove that x, y, z are in HP.



84. The harmonic mean of two numbers is 4. Their arithmetic mean A and the geometric mean G satisfy the relation $2A + G^2 = 27$. Find two

numbers.



85. If the geometric mea is $\frac{1}{n}$ times the harmonic mean between two numbers, then show that the ratio of the two numbers is $1 + \sqrt{1 - n^2} : 1 - \sqrt{1 - n^2}.$

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86. Statement -1: If a,b,c are distinct real numbers in H.P, then $a^n+c^n>2b^n$ for all $n\in N.$

Statement -2: AM > GM > HM

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87. If a, b, c, d be four distinct positive quantities in AP, then

(a) bc>ad

(b)
$$c^{-1}d^{-1} + a^{-1}b^{-1} > 2 ig(b^{-1}d^{-1} + a^{-1}c^{-1} - a^{-1}d^{-1} ig)$$



88. If a, b, c, d be four distinct positive quantities in GP, then

(a)
$$a+d>b+c$$

(b) $c^{-1}d^{-1}+a^{-1}b^{-1}>2ig(b^{-1}d^{-1}+a^{-1}c^{-1}-a^{-1}d^{-1}ig)$

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89. If a, b, c, d be four disinct positive quantities in HP, then

(a)
$$a+d>b+c$$

(b)ad > bc



90. Find the sum of n terms of the series $1 + \frac{4}{5} + \frac{7}{5^2} + 10 + 5^3 + .$

91. The sum to infinity of the series

$$1 + rac{4}{5} + rac{7}{5^2} + rac{10}{5^3} + \dots, ext{ is }$$

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92. If the sum to infinity of the series $1 + 4x + 7x^2 + 10x^3 + \dots$

is
$$\frac{35}{16}$$
 then $x = (A) \frac{1}{5} (B) \frac{2}{5} (C) \frac{3}{7} (D) \frac{1}{7}$

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94. Find the sum of the series $1^2+3^2+5^2+
ightarrow n$ terms.





98. Find the sum of the series $rac{1^3}{1} + rac{1^3+2^3}{1+3} + rac{1^3+2^3+3^3}{1+3+5} + ext{ up to } n$

terms.

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99. Show that
$$S_n=rac{nig(2n^2+9n+13ig)}{24}$$

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100. Find the sum of n terms of the series $1.\ 2.\ 3+2.\ 3.\ 4+3.\ 4.\ 5+$

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101. Find sum to n terms of the series 1 + (2 + 3) + (4 + 5 + 6) +



103. Find the nth term and sum to n tems of the following series: 1+5+12+22+.....

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104. Sum to n terms the series $1 + 3 + 7 + 15 + 31 + \dots$

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105. Find the nth term of the series = 1 + 4 + 10 + 20 + 35 + ...







114. If
$$\sum_{r=1}^n T_r = rac{n(n+1)(n+2)(n+3)}{12}$$
 where T_r denotes the rth term of the series. Find $\lim_{n o\infty} \sum_{r=1}^n rac{1}{T_r}$.

115. If yz + zx + xy = 12, where x,y,z` are positive values find the greatest value of xyz.

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116. Find the greatest value of x^3y^4 if 2x+3y=7 and $x\geq 0, y\geq 0$.
117. Find the least value of 3x + 4y for positive values of x and y, dubject

to the condition $x^2y^3 = 6$.

118. The minimum value of P = bcx + cay + abz, when xyz = abc, is

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119. If a, b, c are positive real numbers such that a + b + c = 1, then prove that $\frac{a}{b+c} + \frac{b}{c+a} + \frac{c}{a+b} \ge \frac{3}{2}$ Watch Video Solution

120. If a + b - 1, a > 0,b > 0, prove that
$$\left(a + \frac{1}{a}\right)^2 + \left(b + \frac{1}{b}\right)^2 \ge \frac{25}{2}$$

121. If $b-c, 2b-\lambda, b-a$ are in HP, then $a-\frac{\lambda}{2}, b-\frac{\lambda}{2}, c-\frac{\lambda}{2}$ are is

A. AP

B. GP

C. HP

D. None of these

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Answer: B



$$\sum_{i=1}^{101} a_i = 125 \;\; ext{than the value of}\;\; \sum_{i=1}^{101} \left(rac{1}{a_i}
ight)$$
 equals.

A. 5

 $\mathsf{B}.\,\frac{1}{5}$

C.
$$\frac{1}{25}$$

D. $\frac{1}{125}$

Answer: B

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123.

$$x = 111....(20 digits), y = 333....(10 digits) \text{ and } z = 222.....2(10 digits), the second secon$$

lf

equals.

A. $\frac{1}{2}$

B. 1

C. 2

D. 4

Answer: B

124. Consider the sequence $1, 2, 2, 3, 3, 3, \ldots$, where n occurs n times

that occuts as 201th rerms is

A. 61

B. 62

C. 63

D. 64

Answer: C



125. Let $S = \sum_{r=1}^{117} \frac{1}{2[\sqrt{r}] + 1}$, when $[\cdot]$ denites the greatest integer function and if $S = \frac{p}{q}$, when p and q are co-primes, the value of p + q is

A. 20

B. 76

C. 19

D. 69

Answer: B



126. If a,b,c are non-zero real numbers, then the minimum value of the

expression
$$rac{\left(a^{8}+4a^{4}+1
ight)\left(b^{4}+3b^{2}+1
ight)\left(c^{2}+2c+2
ight)}{a^{4}b^{2}}$$
 equals

A. 12

B. 24

C. 30

D. 60

Answer: C

127. If the sum of m consecutive odd integers is m^4 , then the first integer

is

A. $m^3 + m + 1$ B. $m^3 + m - 1$ C. $m^3 - m - 1$ D. $m^3 - m + 1$

Answer: D

128.
$$\sum_{r=1}^{\infty} \frac{(4r+5)5^{-r}}{r(5r+5)}$$
A. $\frac{1}{5}$
B. $\frac{2}{5}$
C. $\frac{1}{25}$
D. $\frac{2}{25}$

Answer: A



129. Let λ be the greatest integer for which $5p^2 - 16$, $2p\lambda$, λ^2 are jdistinct consecutive terms of an AP, where $p \in R$. If the common difference of the Ap is $\left(\frac{m}{n}\right)$, $n \in N$ and m ,n are relative prime, the value of m + n is A. 133 B. 138 C. 143 D. 148

Answer: C

130. If 2λ , λ and $[\lambda^2 - 14]$, $\lambda \in R - \{0\}$ and $[\cdot]$ denotes the gratest integer function are the first three terms of a GP in order, then the 51th term of the sequence, $1, 3\lambda, 6\lambda, 10\lambda, \ldots$, is

A. 5104

B. 5304

C. 5504

D. 5704

Answer: B

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131. The first three terms of a sequence are 3, -1, -1. The next terms

are

 $\mathsf{A.}\,2$

 $\mathsf{B.}-3$

$$C. - \frac{5}{27}$$

 $D. - \frac{5}{9}$

Answer: B

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132. There are two numbers a and b whose product is 192 and the quotient of AM by HM of their greatest common divisor and least common multiple is (169)/(48). The smaller of a and b is

A. 2

B.4

C. 6

D. 12

Answer: B::D

133. Consider a series $\frac{1}{2} + \frac{1}{2^2} + \frac{2}{2^3} + \frac{3}{2^4} + \frac{5}{2^5} + \dots + \frac{\lambda n}{2^n}$. If S_n denotes its sum to n tems, then S_n cannot be A. 2 B. 3 C. 4

D. 5

Answer: A::B::C::D

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134. If
$$S_r=\sqrt{r+\sqrt{r+\sqrt{r+\sqrt{r+\ldots.\infty}}}}, r>0,\,\,$$
then which of the

following is/are correct.

A. $S_r, S_6, S_{12}, S_{20}, ext{ are in AP}$

B. S_4, S_9, S_{16} are irrational

C.
$$\left(2S_4-1
ight)^2, \left(2S_5-1
ight)^2, \left(2S_6-1
ight)^2$$
 are in AP

D. $S_2,\,S_{12},\,S_{56}$ are in GP

Answer: A::B::C::D



135. If
$$\frac{1}{a}$$
, $\frac{1}{b}$, $\frac{1}{c}$ are in A.P and a,b -2c, are in G.P where a,b,c are non-zero

then

A.
$$a^3+b^3+c^3=3abc$$

- B. -2a, b, -2c are in AP
- C. -2a, b, -2c are inGP
- D. $a^2, b^2, 4c^2$ are in GP

Answer: A::B::D

136. The nature of the $S_n=3n^2+5n$ series is

A. AP

B. GP

C. HP

D. AGP

Answer: A

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137. For the $S_n=3n^2+5n$ sequence, the number 5456 is the

A. 153th term

B. 932th term

C. 707th term

D. 909th term

Answer: D



138. Consider a sequence whose sum to n terms is given by the quadratic function $Sn = 3(n^2) + 5n$. Then sum of the squares of the first 3 terms of the given series is

A. 1100

B. 660

C. 799

D. 1000

Answer: B

139. Find the number of terms common to the two A.P. s: 3, 7, 11, 407*and*2, 9, 16, , 709.

A. 14

B. 21

C. 28

D. 35

Answer: A

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140. The 10th common terms between the series 3+7+11+ And

 $1+6+11+\ldots$ is

(i) 191

(ii) 193

(iii) 211

(iv) None of these

A. 189

B. 191

C. 211

D. 213

Answer: B

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141. The largest term common to the sequence 1,11,21,31,....to 100 terms and 31,36,41,46,..... to 100 terms is

A. 281

B. 381

C. 471

D. 521

Answer: D

142. If x > 0, y > 0, z > 0 and x + y + z = 1 then the minimum value

of
$$rac{x}{2-x}+rac{y}{2-y}+rac{z}{2-z}$$
 is:

A. (a) 0.2

B. (b) 0.4

C. (c) 0.6

D. (d) 0.8

Answer: C

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143. If $\sum_{i=1}^{n} a_i^2 = \lambda, \ \forall a_i \ge 0$ and if greatest and least values of $\left(\sum_{i=1}^{n} a_i\right)^2$ are λ_1 and λ_2 respectively, then $(\lambda_1 - \lambda_2)$ is

A. $n\lambda$

B. $(n-1)\lambda$ C. $(n+2)\lambda$ D. $(n+1)\lambda$

Answer: B

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144. If sum of the mth powers of first n odd numbers is $\lambda, Aam > 1$, then

(A)
$$\lambda < n^m$$
 (B) $\lambda > n^m$ (C) $\lambda < n^{m+1}$ (D) $\lambda > n^{m+1}$

A. $\lambda < n^m$

 $\mathsf{B}.\,\lambda>n^m$

 $\mathsf{C}.\,\lambda < n^{m+1}$

D. $\lambda > n^{m+1}$

Answer: D

145. A squence of positive terms $A_1, A_2, A_3, ..., A_n$ satisfirs the relation

 $A_{n+1}=rac{3(1+A_n)}{(3+A_n)}.$ Least integeral value of A_1 for which the sequence

is decreasing can be

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146. When the ninth term of an AP is divided by its second term we get 5

as the quotient, when the thirteenth term ia devided ny sixth term the

quotient is 2 and the remainderis 5, then the seonnd term is

147. Match the following Column I to Column II

	Calum U		
(A)	If $a_1, a_2, a_3,$ are in AP and $a_1 + a_6 + a_{10} + a_{21}$ + $a_{25} + a_{30} = 120$, then $\sum_{i=1}^{30} a_i$ is	(p)	400
(B)	If $a_1, a_2, a_3,$ are in AP and $a_1 + a_5 + a_9$ + $a_{13} + a_{17} + a_{21} + a_{25} = 112$, then $\sum_{i=1}^{25} a_i$ is	(q)	600
(C)	If $a_1, a_2, a_3,$ are in AP and $a_1 + a_4 + a_7 + a_{10} + a_{13}$ $+ a_{16} = 375$, then $\sum_{i=1}^{16} a_i$ is	(r)	800
		(s)	1000

148. Match the following Column I to Column II

	Column I	C	Column II		
(A	If $a > 0$, $b > 0$, $c > 0$ and the minimum value of $a (b^2 + c^2) + b (c^2 + a^2) + c (a^2 + b^2)$ is λabc , then λ is	(p)	2		
(B) If a, b, c are positive, $a + b + c = 1$ and the minimum value of $\left(\frac{1}{a} - 1\right) \left(\frac{1}{b} - 1\right) \left(\frac{1}{c} - 1\right)$ is λ , then λ is		4		
(C)	If $a > 0$, $b > 0$, $c > 0$, $s = a + b + c$ and the minimum value of $\frac{2s}{s-a} + \frac{2s}{s-b} + \frac{2s}{s-c}$ is $(\lambda - 1)$, then λ is	(r)	6		
(D)	If $a > 0$, $b > 0$, $c > 0$, a , b , c are in GP and the the minimum value of $\left(\frac{a}{b}\right)^{\lambda} + \left(\frac{c}{b}\right)^{\lambda}$ is 2, then λ is	(s)	8		
		(t)	10		

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149. Statement 1 The sum of first n terms of the series $1^2 - 2^2 + 3^2 - 4^2 - 5^2 - \ldots$ can be $= \pm \frac{n(n+1)}{2}$. Statement 2 Sum of first n narural numbers is $\frac{n(n+1)}{2}$

A. Statement 1 is true, Statement 2 is true, Statement 2 is a corrct

explanation for Statement 1.

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct

explanation for Statement 1.

C. Statement 1 is true, Statement 2 is false.

D. Statement 1 is false, Statement 2 is true.

Answer: A

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150. Statement 1 If a,b,c are three positive numbers in GP, then $\left(\frac{a+b+c}{3}\right)\left(\frac{3abc}{ab+bc+ca}\right) = (abc)^{\frac{2}{3}}.$ Statement 2 $(AM)(HM) = (GM)^2$ is true for positive numbers.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a corrct

explanation for Statement 1.

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct

explanation for Statement 1.

C. Statement 1 is true, Statement 2 is false.

D. Statement 1 is false, Statement 2 is true.

Answer: C

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151. Consider an AP with a as the first term and d is the common difference such that S_n denotes the sum to n terms and a_n denotes the nth term of the AP. Given that for some m, $n \in N$, $\frac{S_m}{S_n} = \frac{m^2}{n^2} (\neq n)$.

Statement 1 d = 2a because

Statement 2 $rac{a_m}{a_n}=rac{2m+1}{2n+1}.$

A. Statement 1 is true, Statement 2 is true, Statement 2 is a corrct

explanation for Statement 1.

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct

explanation for Statement 1.

C. Statement 1 is true, Statement 2 is false.

D. Statement 1 is false, Statement 2 is true.

Answer: C

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152. Statement 1 1, 2, 4, 8, is a GP,4, 8, 16, 32, is a GP and 1 + 4, 2 + 8, 4 + 16, 8 + 32, is also a GP. Statement 2 Let general term of a GP with common ratio r be T_{k+1} and general term of another GP with common ratio r be T'_{k+1} , then the series whode general term $T''_{k+1} = T_{k+1} + T'_{k+1}$ is also a GP woth common ratio r.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a corrct explanation for Statement 1.

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct

explanation for Statement 1.

C. Statement 1 is true, Statement 2 is false.

D. Statement 1 is false, Statement 2 is true.

Answer: A

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153. In a set of four numbers, the first three are in G.P. and the last three are in A.P. with difference 6. If the first number is the same as the fourth, find the four numbers.

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154. Find the natural number a for which $\sum_{k=1}^{n} f(a+k) = 16(2^{n}-1)$, where the function f satisfies the relation f(x+y) = f(x)f(y) for all natural number x, yand, further, f(1) = 2.

155. If n is a root of $x^2(1 - ac) - x(a^2 + c^2) - (1 + ac) = 0$ and if n harmonic means are inserted between a and c, find the difference between the first and the last means.

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156. A number consists of three digits which are in GP the sum of the right hand and left hand digits exceeds twice the middle digits by 1 and the sum of the left hand and middle digits is two thirds of the sum of the middle and right hand digits. Find the number.



157.
$$S = \sum_{i=1}^n \sum_{j=1}^i \sum_{k=1}^j 1$$

158. Three numbers are in G.P. whose sum is 70. If the extremes be each multiplied by 4 and the means by 5, they will be in A.P. Find the numbers.

159. If the sum of m terms of an A.P. is equal to the sum of either the next

$$n$$
 terms or the next p terms, then prove that
 $(m+n)\left(rac{1}{m}-rac{1}{p}
ight)=(m+p)\left(rac{1}{m}-rac{1}{n}
ight).$

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160. Find the sum of all possible products of the first n natural numbers

taken two by two.



161. If $l_n = \int_0^{\frac{\pi}{4}} \tan^n x \, dx$ show that $\frac{1}{l_2 + l_4}, \frac{1}{l_3 + l_5}, \frac{1}{l_4 + l_6}, \frac{1}{l_5 + l_7}, \dots$ from an AP. Find its common difference.



162. If the sum of the terms of an infinitely decreasing GP is equal to the greatest value of the fuction $f(x) = x^3 + 3x - 9$ on the iterval [-5, 3] and the difference between the first and second terms is f'(0), then show that the common ratio of the progression is $\frac{2}{3}$.

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163. Find the relation between x and y:
$$\log_{10} x + \frac{1}{2} \log_{10} x + \frac{1}{4} \log_{10} x + ... = y$$

164. If $0 < x < \frac{\pi}{2} \exp \left[\left(\sin^2 x + \sin^4 x + \sin^6 x + '.... + \infty \right) \log_e 2 \right]$ satisfies the quadratic equation $x^2 - 9x + 8 = 0$, find the value of $\frac{\sin x - \cos x}{\sin x + \cos x}$.







The rth group containing 2^{r-1} numbers. Prove that sum of the numbers in the nth group is $2^{n-2}[2^n+2^{n-1}-1].$

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166. If a,b,c are in HP, then prove that $\displaystyle rac{a+b}{2a-b} + \displaystyle rac{c+b}{2c-b} > 4.$



171. IF
$$f(r) = 1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{r}$$
 and $f(0) = 0$, find $\sum_{r=1}^{n} (2r+1)f(r).$

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172. If the equation $x^4 - 4x^3 + ax^2 + bx + 1 = 0$ has four positive roots, find the values of a and b.

173. Evaluate
$$\sum_{m=1}^{\infty}\sum_{n=1}^{\infty}rac{m^2n}{3^m(n\cdot 3^m+m\cdot 3^n)}.$$

174. The value of $\sum_{i=0}^{\infty} \sum_{j=0}^{\infty} \sum_{k=0}^{\infty} rac{1}{3^i 3^j 3^k}$ is

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175. Let $S_n, n = 1, 2, 3, \ldots$ be the sum of infinite geometric series, whose

first term is n and the common ratio is $rac{1}{n+1}$. Evaluate $\lim_{n o\infty} rac{S_1S_n+S_2S_{n-1}+S_3S_{n-2}+...+S_nS_1}{S_1^2+S_2^2+....+S_n^2}.$

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176. The nth term of a series is given by $t_n = \frac{n^5 + n^3}{n^4 + n^2 + 1}$ and if sum of its n terms can be expressed as $S_n = a_n^2 + a + \frac{1}{b_n^2 + b}$ where a_n and b_n are the nth terms of some arithmetic progressions and a, b are some constants, prove that $\frac{b_n}{a_n}$ is a costant.

1. First term of a sequence is 1 and the (n + 1)th term is obtained by adding (n + 1) to the nth term for all natural numbers n, the 6th term of the sequence is

A. 7 B. 13 C. 21 D. 27

Answer: C



2. The first three terms of a sequence are 3, 3, 6 and each term after the sum of two terms preceding it, then the 8th term of the sequence

B. 24

C. 39

D. 63

Answer: D

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3. If
$$a_n = \sin \Bigl(rac{n \pi}{6} \Bigr)$$
then the value of $\sum a_n^2$

A. 2

B. 3

C. 4

D. 7

Answer: B

4. If for a sequence $\{a_n\}, S_n=2n^2+9n$, where S_n is the sum of n terms,

the value of a_{20} is

A. 65

B.75

C. 87

D. 97

Answer: C

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5. If
$$a_1=2$$
 and $a_n=2a_{n-1}+5$ for $n>1$, the value of $\displaystyle\sum_{r=2}^5 a_r$ is

A. 130

B. 160

C. 190

D. 220

Answer: C



Exercise For Session 2

1.	lf	nth	term	of	the	series	25 + 29 + 33 + 37	and
3 +	- 4 +	6 + 9	+ 13 +	•••••	are	equal, th	en n equal	
	A. 11							
	B. 12							
	C. 13							
	D. 14							

Answer: B

2. The 15th term of the series $2rac{1}{2}+1rac{7}{13}+1rac{1}{9}+rac{20}{23}+\ldots$ is

A.
$$\frac{20}{5r+3}$$

B. $\frac{20}{5r-3}$
C. $20(5r+3)$
D. $\frac{20}{5r^2+3}$

Answer: A

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3. In a certain A.P., 5 times the 5th term is equal to 8 times the 8th terms then find its 13th term.

A. 0

 $\mathsf{B.}-1$

 $\mathsf{C}.-12$

 $\mathsf{D.}-13$
Answer: A

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4. If the 9th term of an AP is zero, then prove that its 29th term is twice its 19th term.

A. 1:2 B. 2:1 C. 1:3

D. 3:1

Answer: B

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5. about to only mathematics

A. 1

 $\mathsf{B.}-1$

D.
$$\frac{1}{2}$$

Answer: C



6. The 6th term of an AP is equal to 2, the value of the common difference of the AP which makes the product $a_1a_4a_5$ least is given by

A.
$$\frac{8}{5}$$

B. $\frac{5}{4}$
C. $\frac{2}{3}$
D. $\frac{1}{3}$

Answer: C

7. The sum of first 2n terms of an AP is α . and the sum of next n terms is

 β , its common difference is

A.
$$rac{lpha-2eta}{3n^2}$$

B. $rac{2eta-lpha}{3n^2}$
C. $rac{lpha-2eta}{3n}$
D. $rac{2eta-lpha}{3n}$

Answer: B

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8. The sum of three numbers in AP is -3 and their product is 8, then sum

of squares of the numbers is

B. 10

C. 12

D. 21

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9. Let S_n denote the sum of first n terms of an AP and $3S_n=S_{2n}$ What is

 S_{3n} : S_n equal to?

A. (a) 9

B. (b) 6

C. (c) 16

D. (d) 12



10. Find the sum of the products of the ten numbers $\pm 1, \pm 2, \pm 3, \pm 4, \text{ and } \pm 5$ taking two at a time.

A. - 65

B. 165

C. - 55

D. 95

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11. If $a_1, a_2, a_3, \ldots, a_n$ are in AP, where $a_i > 0$ for all I, the value of

$$\frac{1}{\sqrt{a_1} + \sqrt{a_2}} + \frac{1}{\sqrt{a_2} + \sqrt{a_3}} + \dots + \frac{1}{\sqrt{a_{n-1}} + \sqrt{a_n}} \text{ is }$$
A. $\frac{1}{\sqrt{a_1} + \sqrt{a_n}}$
B. $\frac{1}{\sqrt{a_1} - \sqrt{a_n}}$
C. $\frac{n}{\sqrt{a_1} - \sqrt{a_n}}$
D. $\frac{n-1}{\sqrt{a_1} + \sqrt{a_n}}$

Exercise For Session 3

1. The fourth, seventh, and the last term of a G.P. are 10, 80, and 2560, respectively. Find the first term and the number of terms in G.P.

A.
$$\frac{4}{5}$$
, 12
B. $\frac{4}{5}$, 10
C. $\frac{5}{4}$, 12
D. $\frac{5}{4}$, 10

Answer: B

2. If the first and the n^{th} term of a GP are a and b, respectively, and if P is the product of n terms, prove that $P^2 = (ab)^n$.

A. ab

 $\mathsf{B.}\,(ab)^{\frac{n}{2}}$

 $\mathsf{C}.(ab)^n$

D. None of these

Answer: C

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3. If $a_1, a_2, a_3(a_1 > 0)$ are three successive terms of a GP with common ratio r, the value of r for which $a_3 > 4a_2 - 3a_1$ holds is given by

A. 1 < r < 3

B. -3 < r < -1

C. r < 1 or r > 3

D. None of these

Answer: B



4. If x, 2x + 2 and 3x + 3 are the first three terms of a G.P., then the fourth term is a. 27 b. -27 c. 13.5 d. -13.5

A. 27

B. - 27

C. 13.5

 $\mathsf{D.}-13.5$

Answer: C

5. In a sequence of 21 terms the first 11 terms are in A.P. with common difference 2. and the last 11 terms are in G.P. with common ratio 2. If the middle term of the A.P. is equal to the middle term of the G.P., then the middle term of the entire sequence is

A.
$$-\frac{10}{31}$$

B. $\frac{10}{31}$
C. $-\frac{32}{31}$
D. $\frac{32}{31}$

Answer: D

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6. Three distinct numbers x,y,z form a GP in that order and the numbers 7x + 5y, 7y + 5z, 7z + 5x form an AP in that order. The common ratio of GP is

$$\mathsf{A.}-4$$

 $\mathsf{B.}-2$

C. 10

D. 18

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7. Prove that the sum to n terms of the series $11 + 103 + 1005 + \dots$ Is (10/9)

$$(10^n - 1) + n^2.$$

A.
$$rac{1}{9}(10^n-1)+n^2$$

B. $rac{1}{9}(10^n-1)+2n$
C. $rac{10}{9}(10^n-1)+n^2$
D. $rac{10}{9}(10^n-1)+2n$

8. In a G.P the sum of the first and last terms is 66, the product of the second and the last but one is 128, and the sum of the terms is 126 If the decresing G.P is considered , then the sum of infinite terms is

A. 6

B. 8

C. 10

D. 12

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9. If S_1, S_2, S_3 be respectively the sum of n, 2n and 3n terms of a GP, then ${S_1(S_3-S_2)\over (S_2-S_1)^2}$ is equal to

A. (a) 1

B. (b) 2

C. (c) 3

D. (d) 4

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10. If
$$|a| < 1|b| < 1$$
 and $|x| < 1$ then the solution of $\sin^{-1}\left(\frac{2a}{1+a^2}\right) - \cos^{-1}\left(\frac{1-b^2}{1+b^2}\right) = \tan^{-1}\left(\frac{2x}{1-x^2}\right)$ is
A. $\frac{a-b}{1-ab}$
B. $\frac{a-b}{1+ab}$
C. $\frac{ab-1}{1+ab}$

D. none of these

11. If the sides of a triangle are in GP and its largest angle is twice tha smallset then the common ratio r satisfies the inequality

A.
$$0 < r < \sqrt{2}$$

B. $1 < r < \sqrt{2}$
C. $1 < r < 2$
D. $r > \sqrt{2}$

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12. If $ax^3 + bx^2 + cx + d$ is divisible by $ax^2 + c$, thena, b, c, d are in a.

A.P. b. G.P. c. H.P. d. none of these

A. AP

B. GP

C. HP

D. None of these



13. If $(r)_n$, denotes the number rrr...(ndigits), where r = 1, 2, 3, ..., 9and $a = (6)_n, b = (8)_n, c = (4)_{2n}$, then

A.
$$a^2 + b + c = 0$$

<u>م</u>

 $\mathsf{B}.\,a^2+b-c=0$

C.
$$a^2 + b2c = 0$$

D.
$$a^2 + b - 9c = 0$$

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14. $0.4\overline{27}$ represents the rational number

A.
$$\frac{47}{99}$$

B. $\frac{47}{110}$
C. $\frac{47}{999}$
D. $\frac{49}{99}$



15. If the product of three numbers in GP be 216 and their sum is 19, then the numbers are

A. 4, 6, 9

B. 4, 7, 8

C. 3, 7, 9

D. None of these



Exercise For Session 4

1. If a,b,c are in AP and b,c,d be in HP, then

A. ab = cd

B.ad = bc

 $\mathsf{C}.\,ac=bd$

D. abcd = 1

Answer: C

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2. If a,b,c are in AP, then
$$\frac{a}{bc}$$
, $\frac{1}{c}$, $\frac{1}{b}$ are in

A. AP

B. GP

C. HP

D. None of these

Answer: C

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3. about to only mathematics

A. AP

B. GP

C. HP

D. None of these

Answer: C

4. If x, 1, z are in AP and x, 2, z are in GP, then x, 4, z will be in

A. AP

B. GP

C. HP

D. None of these

Answer: D

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5. If a, b, c are in G.P. and a - b, c - a, andb - c are in H.P., then prove

that a + 4b + c is equal to 0.

A. 0

B. 1

C. -1

D. None of these

Answer: A



6. If the (m + 1)th, (n + 1)th, and(r + 1)th terms of an A.P., are in G.P. and m, n, r are in H.P., then find the value of the ratio of the common difference to the first term of the A.P.



Answer: A

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7. If a,b,c are in AP and $a^2,\,b^2,\,c^2$ are in HP, then

A. a = b = c

$$\mathsf{B.}\,2b = 3a + c$$

$$\mathsf{C.}\,b^2 = \sqrt{\frac{ac}{8}}$$

D. None of these

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8. If a, b, c are in HP., then
$$\frac{a}{b+c}$$
, $\frac{b}{c+a}$, $\frac{c}{a+b}$ are in

A. AP

B. GP

C. HP

D. None of these

9. If $\displaystyle \frac{x+y}{2}, \, y, \, \displaystyle \frac{y+z}{2}$ are in HP, then x,y, z are in

A. AP

B. GP

C. HP

D. None of these

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10. if
$$\displaystyle rac{a+b}{1-ab}, b, \displaystyle rac{b+c}{1-bc}$$
 are in AP then $a, \displaystyle rac{1}{b}, c$ are in

A. AP

B. GP

C. HP

D. None of these



Exercise For Session 5

1. If the arithmetic means of two positive number a and b (a > b) is twice their geometric mean, then find the ratio a: b

A.
$$2 + \sqrt{3}: 2 - \sqrt{3}$$

B. $7 + 4\sqrt{3}: 7 - 4\sqrt{3}$
C. $2: 7 + 4\sqrt{3}$
D. $2: \sqrt{3}$

Answer: C



2. Let α and β be two positive real numbers. Suppose A_1, A_2 are two arithmetic means; G_1, G_2 are tow geometrie means and H_1H_2 are two

harmonic means between α and β , then

A. A_1H_2

 $\mathsf{B.}\,A_2H_1$

 $\mathsf{C}.\,G_1G_2$

D. None of these

Answer: A

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3. The geometric mean between -9 and -16 is 12 b. -12 c. -13 d. none of

these

A. 12

B. -12

C. -13

D. None of these

Answer: A



4. Let $n \in N, n > 25$. Let A, G, H deonote te arithmetic mean, geometric man, and harmonic mean of 25 and n. The least value of n for which $A, G, H \in \{25, 26, n\}$ is a. 49 b. 81 c.169 d. 225

A. 49

B. 81

C. 169

D. 225

Answer: C

5. If nine arithmetic means and nine harmonic means are inserted between 2 and 3 alternatively, then prove that A + 6/H = 5 (where A is any of the A.M.'s and H the corresponding H.M.).

A. 8 B. 9 C. 10

D. None of these

Answer: B

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6. If H_1 , H_2 , ..., H_{20} are 20 harmonic means between 2 and 3, then $rac{H_1+2}{H_1-2}+rac{H_{20}+3}{H_{20}-3}=$

A. n

 $B.\,n+1$

C. 2n

 ${\sf D}.\,2n-2$

Answer: B

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7. The A.M. of two given positive numbers is 2. If the larger number is increased by 1, the G.M. of the numbers becomes equal to the A.M. of the given numbers. Then find the H.M.

A.
$$\frac{3}{2}$$

B. $\frac{2}{3}$
C. $\frac{1}{2}$
D. 2

Answer: B

8. If $a, a_1, a_2, a_3, a_{2n}, b$ are in A.P. and $a, g_1, g_2, g_3, g_{2n}, b$. are in G.P. and

the H.M. of *aandb*, then h s prove that $rac{a_1+a_{2n}}{g_1g_{2n}}+rac{a_2+a_{2n-1}}{g_1g_{2n-1}}+ \ + \ rac{a_n+a_{n+1}}{g_ng_{n+1}}=rac{2n}{h}$ A. $\frac{2n}{b}$ B. 2nh C. nh D. $\frac{n}{h}$

Answer: B

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Exercise For Session 6

1. Sum of the first n terms of the series $\frac{1}{2} + \frac{3}{4} + \frac{7}{8} + \frac{15}{16} + \dots$ is equals to (a). $2^n - n - 1$ (b). $1 - 2^{-n}$ (c). $n + 2^{-n} - 1$ (d). $2^n + 1$

A.
$$2^n - n - 1$$

B. $1 - 2^{-n}$
C. $n + 26(-n) - 1$
D. $26(n) - 1$

Answer: B

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2. about to only mathematics

A. 1

$$\mathsf{B}.\,\frac{3}{2}$$

D.
$$\frac{5}{2}$$

Answer: D

3. Sum to n terms the series $1 + 3 + 7 + 15 + 31 + \dots$

A.
$$2^{n+1} - n$$

- $\mathsf{B}.\, 2^{n+1}-n-2$
- $C. 2^n n 2$
- D. None of these

Answer: B

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4. 99^{th} term of the series 2+7+14+23...

A. 9998

B. 9999

C. 10000

D. 100000

Answer: C



5. Find the sum of n terms of the series 1. 2. 3 + 2. 3. 4 + 3. 4. 5 + 3

A.
$$n(n + 1)(n + 2)$$

B. $(n + 1)(n + 2)(n + 3)$
C. $\frac{1}{4}n(n + 1)(n + 2)(n + 3)$
D. $\frac{1}{4}(n + 1)(n + 2)(n + 3)$

Answer: A

6. Find the sum of *n* terms of the series:

$$\frac{1}{1.2} + \frac{1}{2.3} + \frac{1}{3.4} + \frac{1}{nn+1}$$

A. $\frac{1}{n(n+1)}$
B. $\frac{n}{n+1}$
C. $\frac{2n}{n+1}$
D. $\frac{2}{n(n+1)}$

Answer: B



7. Sum of the n terms of the series

$$\frac{3}{1^2} + \frac{5}{1^2 + 2^2} + \frac{7}{1^2 + 2^2 + 3^3} + \dots \text{ is}$$
A. $\frac{2n}{n+1}$
B. $\frac{4n}{n+1}$
C. $\frac{6n}{n+1}$

D.
$$rac{9n}{n+1}$$

Answer: A



8. If
$$t_n = \frac{1}{4}(n+2)(n+3)f$$
 or $n = 1, 2, 3, ,$ then
 $\frac{1}{t_1} + \frac{1}{t_2} + \frac{1}{t_3} + \frac{1}{t_{2003}} = \frac{4006}{3006}$ b. $\frac{3006}{3007}$ c. $\frac{4006}{3008}$ d. $\frac{4006}{3009}$
A. $\frac{4006}{3006}$
B. $\frac{4003}{3007}$
C. $\frac{4006}{3008}$
D. $\frac{4006}{3009}$

Answer: C

9. The value of
$$\frac{1}{(1+a)(2+a)} + \frac{1}{(2+a)(3+a)} + \frac{1}{(3+a)(4+a)}$$
..... upto ∞ is

(where, a is constant)

A. A.
$$\frac{1}{1+a}$$

B. B. $\frac{2}{1+a}$

C. C.
$$\infty$$

D. D. None of these

Answer: B

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10. If f is a function satisfying f(x+y)=f(x) imes f(y) for all $x,y\in N$ such that f(1)=3 and $\sum_{x=1}^n f(x)=120,\,$ find the value of n .

A. 4

B. 5

C. 6

D. None of these

Answer: C

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Exercise For Session 7

1. The minimum value of $4^x+4^{2-x}, x\in R$ is

A. 0

B. 2

C. 4

D. 8

Answer: A

2. If $0 < heta < \pi$, then the minmum value of $\sin^3 heta + \cos e c^3 heta + 2$ is

A. 0	
B. 2	
C. 4	
D. 8	

Answer: C

Watch Video Solution

3. If a,b,c and d are four real numbers of the same sign, then the value of

 $\frac{a}{b} + \frac{b}{c} + \frac{c}{d} + \frac{d}{a}$ lies in the interval A. $[2, \infty)$ B. $[3, \infty)$ C. $(4, \infty)$ D. $[4,\infty)$

Answer: B



4. If
$$0 < x < \frac{\pi}{2}$$
, then the minimum value of $2(\sin x + \cos x + \cos ec 2x)^3$ is
A. (a) 27
B. (b) 13.5
C. (c) 6.75
D. (d) 0
Answer: D
5. If a+b+c=3 and a>0, b>0, c>0 then the greatest value of $a^2b^3c^2$ is

A.
$$\frac{3^{4} \cdot 2^{10}}{7^{7}}$$
B.
$$\frac{3^{10} \cdot 2^{4}}{7^{7}}$$
C.
$$\frac{3^{2} \cdot 2^{12}}{7^{7}}$$
D.
$$\frac{3^{12} \cdot 2^{2}}{7^{7}}$$

Answer: C

Watch Video Solution

6. If x+y+z=a and the minimum value of $\frac{a}{x}+\frac{a}{y}+\frac{a}{z}$ is 81^{λ} , then the value of . λ is

A.
$$\frac{1}{2}$$

B. 1
C. $\frac{1}{4}$

Answer: C

Watch Video Solution

7. If x, y, z be three positive numbers such that xyz^2 has the greatest value $\frac{1}{64}$, then the value of $\frac{1}{x} + \frac{1}{y} + \frac{1}{z}$ is

A. $a = b = \frac{1}{2}, c = \frac{1}{4}$ B. $a = b = c = \frac{1}{3}$ C. $a = b = \frac{1}{4}, c = \frac{1}{2}$ D. $a = b = c = \frac{1}{4}$

Answer: A

Watch Video Solution

Exercise (Single Option Correct Type Questions)

1. If the number x,y,z are in H.P. , then $\frac{\sqrt{yz}}{\sqrt{y}+\sqrt{z}}, \frac{\sqrt{xz}}{\sqrt{x}+\sqrt{z}}, \frac{\sqrt{xy}}{\sqrt{x}+\sqrt{y}}$

are in

A. AP

B. GP

C. HP

D. None of these

Answer: A

2. If
$$a_1, a_2, \ldots$$
, are in HP and $f_k = \sum_{r=1}^n a_r - a_k$, then
 $2^{\alpha_1}, 2^{\alpha_2}, 2^{\alpha_3} 2^{\alpha_4}, \ldots$ are in
 $\left\{ \text{ where } \alpha_1 = \frac{a_1}{f_1}, \alpha_2 = \frac{a_2}{f_2}, \alpha_3 = \frac{a_3}{f_3}, \ldots \right\}.$

B. GP

C. HP

D. None of these

Answer: D

Watch Video Solution

3. ABC is a right-angled triangle in which $\angle B = 90^{\circ}$ and BC = a. If n points L_1, L_2, \ldots, L_n on AB is divided in n+1 equal parts and $L_1M_1, L_2M_2, \ldots, L_nM_n$ are line segments parallel to BC and M_1, M_2, \ldots, M_n are on AC, then the sum of the lengths of $L_1M_1, L_2M_2, \ldots, L_nM_n$ is

A.
$$\frac{n(n+1)}{(2)}$$

B. $\frac{a(n-1)}{2}$
C. $\frac{an}{2}$

D. Impossible to find from the given data

Answer: C



4. Let S_n denotes the sum of the terms of n series $(1 \le n \le 9)$ $1+22+333+\ldots..9999999999,$ is

A.
$$S_n - S_{n-1} = rac{1}{9} ig(10^n - n^2 + n ig)$$

B.
$$S_n = rac{1}{9} ig(10^n - n^2 + 2n - 2 ig)$$

C.
$$9(S_n-S_{n-1})=n(10^n-1)$$

D. None of these

Answer: C

5. If a, b, c are in GP, show that the equations $ax^2 + 2bx + c = 0$ and $dx^2 + 2ex + f = 0$ have a common root if $\frac{a}{d}, \frac{b}{e}, \frac{c}{f}$ are in HP

A. AP

B. GP

C. HP

D. None of these

Answer: A

Watch Video Solution

6. Sum of the first n terms of the series $\frac{1}{2} + \frac{3}{4} + \frac{7}{8} + \frac{15}{16} + \dots$ is equals to (a). $2^n - n - 1$ (b). $1 - 2^{-n}$ (c). $n + 2^{-n} - 1$ (d). $2^n + 1$

A. $2^n - n - 1$

B. $1 - 2^{-n}$

 $C. n + 2^{-n} - 1$

 $\mathsf{D.}\, 2^n-1$

Answer: C

7. If in a triangle PQR; $\sin P$, $\sin Q$, $\sin R$ are in A.P; then (A)the altitudes are in AP (B)the altitudes are in HP (C)the altitudes are in GP (D)the medians are in AP

A. the altitudes are in AP

B. the altitudes are in HP

C. the medians are in GP

D. the medians are in AP

Answer: B

Watch Video Solution

8. Let $a_1, a_2, , a_{10}$ be in A.P. and h_1, h_2, h_{10} be in H.P. If $a_1 = h_1 = 2anda_{10} = h_{10} = 3, then a_4 h_7$ is 2 b. 3 c. 5 d. 6

A. 2	
B. 3	
C. 5	
D. 6	

Answer: D

Watch Video Solution

9. If
$$I_n=\int_0^\pi rac{1-\sin 2nx}{1-\cos 2x}dx$$
 then I_1,I_2,I_3,\ldots are in

A. AP

B. GP

C. HP

D. None of these

Answer: A

10. Show that If $a(b-c)x^2 + b(c-a)xy + c(a-b)y^2 = 0$ is a perfect square, then the quantities a, b, c are in harmonic progresiion

A. AP

B. GP

C. HP

D. None of these

Answer: C

Watch Video Solution

11. The sum to infinity of the series

$$1+2\left(1-rac{1}{n}
ight)+3\left(1-rac{1}{n}
ight)^2+\ldots$$
, is (A) n^2 (B) $n(n+1)$ (C) $n\left(1+rac{1}{n}
ight)^2$ (D)None of these

A. n^2

B. n(n + 1)

$$\mathsf{C.}\,n\!\left(1+\frac{1}{n}\right)^2$$

D. None of these

Answer: A

Watch Video Solution

12. If
$$\log_3 2, \log_3(2^x-5)$$
 and $\log_3\left(2^x-rac{7}{2}
ight)$ are in A.P., then x is equal to

A. 2

B. 3

C. 4

D.2, 3

Answer: B

13. If x,y,z be three positive prime numbers. The progression in which $\sqrt{x}, \sqrt{y}, \sqrt{z}$ can be three terms (not necessarily consecutive) is

A. AP

B. GP

C. HP

D. None of these

Answer: D

Watch Video Solution

14. If n is an odd integer greater than or equal to 1, then the value of $n^{3} - (n-1)^{3} + (n-1)^{3} - (n-1)^{3} + \dots + (-1)^{n-1}1^{3}$ A. $\frac{(n+1)^{2}(2n-1)}{4}$ B. $\frac{(n-1)^{2}(2n-1)}{4}$ C. $\frac{(n+1)^{2}(2n+1)}{4}$ D. None of these

Answer: A



15. If the sides of a right angled triangle are in A.P then the sines of the acute angles are

A.
$$\frac{3}{5}, \frac{4}{5}$$

B. $\sqrt{3}, \frac{1}{3}$
C. $\sqrt{\frac{\sqrt{5}-1}{2}}, \sqrt{\frac{\sqrt{5}+1}{2}}$
D. $\frac{\sqrt{3}}{2}, \frac{1}{2}$

Answer: A

16. The 6th term of an AP is equal to 2, the value of the common difference of the AP which makes the product $a_1a_4a_5$ least is given by

A.
$$\frac{8}{5}$$

B. $\frac{5}{4}$
C. $\frac{2}{3}$

D. None of these

Answer: C



17. If the arithmetic progression whose common difference is nonzero the sum of first 3n terms is equal to the sum of next n terms. Then, find the ratio of the sum of the 2n terms to the sum of next 2n terms.

A.
$$\frac{1}{5}$$

B. $\frac{2}{3}$

$$\mathsf{C}.\,\frac{3}{4}$$

D. None of these

Answer: A

Watch Video Solution

18. The coefficient of x^n in the expansion of $(1+x)(1-x)^n$ is

A.
$$rac{nig(n^2+2ig)(3n+1)}{24}$$

B. $rac{nig(n^2-1ig)(3n+2)}{24}$
C. $rac{nig(n^2+1ig)(3n+4)}{24}$

D. None of these

Answer: B

19. Consider the pattern shown below:

Row	1	1			
Row	2	3	5		oto
Row	3	7	9	11	eic.
Row	4	13	15	17	19

The number at the end of row 60 is

A. 3659

B. 3519

C. 3681

D. 3731

Answer: A

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20. Let a_n be the nth term of an AP, if $\sum_{r=1}^{100} a_{2r} = lpha$ and $\sum_{r=1}^{100} a_{2r-1} = eta$,

then the common difference of the AP is

A. (a)
$$lpha-eta$$

B. (b) $\beta - lpha$

C. (c)
$$rac{lpha-eta}{2}$$

D. (d) None of these

Answer: D

Watch Video Solution

21. If a_1, a_2, a_3, a_4, a_5 are in HP, then $a_1a_2 + a_2a_3 + a_3a_4 + a_4a_5$ is equal

to

A. $2a_1a_5$

B. $3a_1a_5$

C. $4a_1a_5$

D. $6a_1a_5$

Answer: C

22. If a,b,c and d are four positive real numbers such that abcd=1 , what is the minimum value of (1 + a)(1 + b)(1 + c)(1 + d).

A. 1 B. 4 C. 16

D. 64

Answer: C

Watch Video Solution

23. If a,b,c are in AP and $(a+2b-c)(2b+c-a)(c+a-b)=\lambda abc$,

then λ is

A. 1

B. 2

C. 4

D. None of these

Answer: C

24. If
$$a_1, a_2, a_3, \ldots$$
 are in GP with first term a and common ratio r, then

$$\frac{a_1a_2}{a_1^2 - a_2^2} + \frac{a_2a_3}{a_2^2 - a_3^2} + \frac{a_3a_4}{a_3^2 - a_4^2} + \dots + \frac{a_{n-1}a_n}{a_{n-1}^2 - a_n^2} \text{ is equal to}$$

A.
$$\frac{nr}{1-r^2}$$

B. $\frac{(n-1)r}{1-r^2}$
C. $\frac{nr}{1-r}$
D. $\frac{(n-1)r}{1-r}$

Answer: B

25. If the sum of first 10 terms of an A.P. is 4 times the sum of its first 5 terms, then find the ratio of first term and common difference.

A. $\frac{1}{2}$ B. 2 C. $\frac{1}{4}$ D. 4

Answer: A

Watch Video Solution

26. If $\cos(x - y)$, $\cos x$ and $\cos(x + y)$ are in H.P., then $\cos x \sec\left(\frac{y}{2}\right) is$

A.
$$\pm \sqrt{2}$$

B. $\frac{1}{\sqrt{2}}$
C. $-\frac{1}{\sqrt{2}}$

D. None of these

Answer: A Watch Video Solution 27. If eleven A.M. s are inserted between 28 and 10, then find the number of integral A.M. s.

A. 5 B. 6 C. 7 D. 8

Answer: A



 $\begin{array}{cccc} \textbf{28.} & \text{If} & x>1, y>1, and z>1 & \text{are} & \text{in} & \text{G.P.,} & \text{then} \\ \\ \hline \frac{1}{1+\ln x}, \frac{1}{1+lny} and \frac{1}{1+lnz} & \text{are} & \text{in} & \text{a.} & A\dot{P} \cdot \text{b.} & H\dot{P} \cdot \text{c.} & G\dot{P} \cdot \text{d.} & \text{none of} \end{array}$

these

A. AP

B. GP

C. HP

D. None of these

Answer: C

Watch Video Solution

29. The minimum value of
$$rac{\left(a^2+3a+1
ight)\left(b^2+3b+1
ight)\left(c^2+3c+1
ight)}{abc}$$
 The

minimum value of , where $a,b,c\in R^+$ is

A.
$$\frac{11^3}{2^3}$$

B. 125

C. 25

D. 27

Answer: B



30. Let a_1, a_2, \ldots be in AP and q_1, q_2, \ldots be in GP. If

 $a_1 = q_1 = 2 \;\; {
m and} \;\; a_{10} = q_{10} = 3$, then

A. a_7q_{19} is not an integer

B. $a_{19}q_7$ is an integer

 $\mathsf{C}.\,a_7q_{19}=a_{19}q_{10}$

D. None of these

Answer: C

Watch Video Solution

Exercise (More Than One Correct Option Type Questions)

1. For a positive integer n let $a(n) = 1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots + \frac{1}{(2^n) - 1}$. Then $a(100) \le 100$ b. a(100) > 100 c. $a(200) \le 100$ d. $a(200) \le 100$

A. a(100) < 100

B.a(100) > 100

C.a(200) > 100

D.a(200) < 100

Answer: A::C

Watch Video Solution

2. The corresponding first and the (2n-1)th terms of an A.P a G.P and a H.P are equal ,If their nth terms are a, b and c , respectively , then

A.
$$a = b = c$$

 $\mathsf{B.}\, a \geq b \geq c$

 $\mathsf{C}. a + c = b$

D.
$$ac - b^2 = 0$$

Answer: B::D



Answer: B::C

4. If a,b,c are in A.P. and a^2, b^2, c^2 are in H.P. then which of the following could and true (A) $-\frac{a}{2}$, b, $care \in G$. P. (B) a = b = c (C) a^3, b^3, c^3 are in G.P. (D) none of these

A.
$$-rac{a}{2}, b, c$$
 are in GP

 $\mathsf{B.}\, a=b=c$

C.
$$a^2, b^2, c^2$$
 are in GP

D. None of these

Answer: A::B



5. The next term of the G.P.
$$x, x^2 + 2, andx^3 + 10$$
 is $\frac{729}{16}$ b. 6 c. 0 d. 54

B. 6

C. $\frac{729}{16}$

D. 54

Answer: C::D



- **6.** Consecutive odd integers whose sum is 25^2-11^2 are
 - A. n = 14
 - $\mathsf{B.}\,n=16$
 - C. first odd number is 23
 - D. last odd number is 49

Answer: A::C::D



7. The geometric mean G of two positive numbers is 6. Their arithmetic mean A and harmonic mean H satisfy the equation 90A + 5H = 918, then A may be equal to:

A. (A)
$$\frac{5}{2}$$

B. (B) 10
C. (C) 5
D. (D) $\frac{1}{5}$

Answer: A::D

Watch Video Solution

8. If the sum to n terms of the series

$$\frac{1}{1\cdot 3\cdot 5\cdot 7} + \frac{1}{3\cdot 5\cdot 7\cdot 9} + \frac{1}{5\cdot 7\cdot 9\cdot 11} + \dots \text{ is } \frac{1}{90} - \frac{\lambda}{f(n)}, \text{ then}$$
find $f(0), f(1)$ and $f(\lambda)$

A. f(0) = 15

B.
$$f(1)=105$$

C. $f(\lambda)=rac{640}{27}$
D. $\lambda=rac{1}{3}$

Answer: A::B::C



9. For the series,

$$S = 1 + \frac{1}{(1+3)}(1+2)^2 + \frac{1}{(1+3+5)}(1+2+3)^2 + \frac{1}{(1+3+5+7)}(1+3+5+7)(1+3+5+7)(1+3+5+7)(1+3+5+7)(1+3+5+7))(1+3+5+7)(1+3+5+7)(1+3+5+7)(1+3+5+7))(1+3+5+7)(1+3+5+7)(1+3+5+7))(1+3+5+7)(1+3+5+7)(1+3+5+7))(1+3+5+7)(1+3+5+7))(1+3+5+7)(1+3+5+7))(1+3+5+7)(1+3+5+7))(1+3+5+7)(1+3+5+7))(1+3+5+7)(1+3+5+7))(1+3+5+7))(1+3+5+7))(1+3+5+7)(1+3+5+7))(1+3+7))(1+3+5+7))(1+3+7))(1+3+5+7))(1+3+7))$$

A. 7th term is 16

B. 7th term is 18

C. sum of first 10 terms is $\frac{505}{4}$ D. sum of first 10 terms is $\frac{405}{4}$

Answer: A::C



10. Let
$$E = \frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} +$$
 Then, $E < 3$ b. $E > 3/2$ c. $E > 2$ d.
 $E < 2$
A. $E < 3$
B. $E > \frac{3}{2}$
C. $E < 2$
D. $E > 2$

Answer: B::C

11. Let $S_n(n \le 1)$ be a sequence of sets defined by $S_1\{0\}, S_2 = \left\{\frac{3}{2}, \frac{5}{2}\right\}, S_3 = \left\{\frac{15}{4}, \frac{19}{4}, \frac{23}{4}, \frac{27}{4}\right\}, \dots$ then

A. (a)third element in S_{20} is $rac{439}{20}$

B. (b)third element in S_{20} is $\frac{431}{20}$

C. (c)sum of the element in S_{20} is 589

D. (d)sum of the element in S_{20} is 609

Answer: A::C

D Watch Video Solution

12. Which of the following sequences are unbounded?

A.
$$\left(1+rac{1}{n}
ight)^n$$

B. $\left(rac{2n+1}{n+2}
ight)$
C. $\left(1+rac{1}{n}
ight)^{n^2}$

 $D. \tan n$

Answer: C::D

13. Let a sequence
$$\{a_n\}$$
 be defined by
 $a_n = \frac{1}{n+1} + \frac{1}{n+2} + \frac{1}{n+3} + \dots + \frac{1}{3n}$. Then:
A (a) $a_2 = \frac{11}{12}$
B. (b) $a_2 = \frac{19}{20}$
C. (c) $a_{n+1} - a_n = \frac{(9n+5)}{(3n+1)(3n+2)(3n+3)}$
D. (d) $a_{n+1} - a_n = \frac{-2}{3(n+1)}$

Answer: B::C

D Watch Video Solution

14. Find
$$rac{dy}{dx}$$
 if $y+\sin y=\cos x$

15. All the terms of an AP are natural numbers and the sum of the first 20 terms is greater than 1072 and lss than 1162.If the sixth term is 32, then

A. first term is 7

B. first term is 12

C. common difference is 4

D. common difference is 5

Answer: A::D

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Exercise (Passage Based Questions)

1.
$$S_n$$
 be the sum of n terms of the series $rac{8}{5}+rac{16}{65}+rac{24}{325}+...$
The value of $\lim_{n o\infty}~S_n$ is (a)0 (b) $rac{1}{2}$ (c)2 (d)4

B.
$$\frac{1}{2}$$

C. 2

D. 4

Answer: C

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2. S_n be the sum of n terms of the series $\frac{8}{5} + \frac{16}{65} + \frac{24}{325} + \dots$ The seveth term of the series is (a) $\frac{56}{2505}$ (b) $\frac{56}{6505}$ (c) $\frac{56}{5185}$ (d) $\frac{107}{9605}$

A.
$$\frac{56}{2505}$$

B. $\frac{56}{6505}$
C. $\frac{56}{5105}$

D. $\frac{107}{9605}$

Answer: D

3. S_n be the sum of n terms of the series $\frac{8}{5} + \frac{16}{65} + \frac{24}{325} + \dots$ The value of S_8 , is (a) $\frac{288}{145}$ (b) $\frac{1088}{545}$ (c) $\frac{81}{41}$ (d) $\frac{107}{245}$

A.
$$\frac{288}{145}$$

B. $\frac{1088}{545}$
C. $\frac{81}{41}$
D. $\frac{107}{245}$

Answer: A

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4. Two consecutive numbers from 1,2,3, n are removed .The arithmetic

mean of the remaining numbers is 105/4

The sum of all numbers

A.(41, 51)

B. (52, 62)

C. (63, 73)

D. (74, 84)

Answer: A

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5. Two consecutive numbers from 1,2,3, n are removed .The arithmetic

mean of the remaining numbers is 105/4

The sum of all numbers

A. are less than 10

B. lies between 10 to 30

C. lies between 30 to 70

D. greater than 70

Answer: A



6. Two consecutive numbers from 1,2,3, n are removed .The arithmetic

mean of the remaining numbers is 105/4

The sum of all numbers

A. less than 1000

B. lies between 1200 to 1500

C. greater than 1500

D. None of these

Answer: B

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7. There are two sets A and B each of which consists of three numbers in AP whose sum is 15 and where D and d are the common differences such that D = 1 + d, d > 0. If p=7(q-p), where p and q are the product of the
nymbers respectively in the two series.

The value of p is

A. 105

B. 140

C. 175

D. 210

Answer: A

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8. There are two sets A and B each of which consists of three numbers in AP whose sum is 15 and where D and d are the common differences such that D = 1 + d, d > 0. If p = 7(q - p), where p and q are the product of the nymbers respectively in the two series.

The value of q is

B. 160

C. 120

D. 80

Answer: C

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9. There are two sets A and B each of which consists of three numbers in AP whose sum is 15 and where D and d are the common differences such that D = 1 + d, d > 0. If p = 7(q - p), where p and q are the product of the nymbers respectively in the two series.

The value of 7D + 8d is

A. 37

B. 22

C. 67

D. 52

Answer: B



10. There are two sets A and B each of which consists of three numbers in GP whose product is 64 and R and r are the common ratios such that R = r + 2. If $\frac{p}{q} = \frac{3}{2}$, where p and q are sum of numbers taken two at a time respectively in the two sets.

The value of p is

A. 66

B.72

C. 78

D. 84

Answer: D

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11. There are two sets A and B each of which consists of three numbers in GP whose product is 64 and R and r are the common ratios sich that R = r + 2. If $\frac{p}{q} = \frac{3}{2}$, where p and q are sum of numbers taken two at a time respectively in the two sets.

The value of q is

A. 54

B. 56

C. 58

D. 60

Answer: B

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12. There are two sets A and B each of which consists of three numbers in GP whose product is 64 and R and r are the common ratios sich that R = r + 2. If $\frac{p}{q} = \frac{3}{2}$, where p and q are sum of numbers taken two at a

time respectively in the two sets.

The value of $r^R + R^r$ is

A. 5392

B. 368

C. 32

D. 4

Answer: C

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13. The numbers 1, 3, 6, 10, 15, 21, 28... are called triangular numbers. Let t_n denote the n^{th} triangular number such that $t_n = t_{n-1} + n, \ \forall n \ge 2$. The value of t_{50} is:

A. (a) 1075

B. (b) 1175

C. (c) 1275

D. (d) 1375

Answer: C

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14. The numbers 1, 3, 6, 10, 15, 21, 28... are called triangular numbers. Let t_n denote the n^{th} triangular number such that $t_n = t_{n-1} + n, \ \forall n \ge 2$. The number of positive integers lying between t_{100} and t_{101} are:

A. (a) 99

B. (b) 100

C. (c) 101

D. (d) 102

Answer: B

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15. The numbers 1, 3, 6, 10, 15, 21, 28... are called triangular numbers. Let t_n denote the n^{th} triangular number such that $t_n = t_{n-1} + n, \ \forall n \ge 2$. If (m+1) is the n^{th} triangular number, then (n-m) is

A. (a)
$$1 + \sqrt{\left(m^2 + 2m
ight)}$$

B. (b) $1 + \sqrt{\left(m^2 + 2
ight)}$
C. (c) $1 + \sqrt{\left(m^2 + m
ight)}$

D. (d) None of these

Answer: D



16. Let $A_1, A_2, A_3, \dots, A_m$ be arithmetic means between -3 and 828 and $G_1, G_2, G_3, \dots, G_n$ be geometric means between 1 and 2187. Produmt of geometrimc means is 3^{35} and sum of arithmetic means is 14025.

The valjue of n is

A. 45	
B. 30	
C. 25	
D. 10	

Answer: D

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17. Let $A_1, A_2, A_3, \dots, A_m$ be arithmetic means between -3 and 828 and $G_1, G_2, G_3, \dots, G_n$ be geometric means between 1 and 2187. Produmt of geometrimc means is 3^{35} and sum of arithmetic means is 14025.

The value of m is

A. 17

B. 34

C. 51

Answer: B

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18. Let $A_1, A_2, A_3, \dots, A_m$ be arithmetic means between -3 and 828 and $G_1, G_2, G_3, \dots, G_n$ be geometric means between 1 and 2187. Produmt of geometrimc means is 3^{35} and sum of arithmetic means is 14025.

The value of m is

A. 2044

B. 1022

C. 511

D. None of these

Answer: D

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19. Suppose lpha, eta are roots of $ax^2+bx+c=0$ and γ, δ are roots of $Ax^2+Bx+C=0.$

If $lpha, eta, \gamma, \delta$ are in AP, then common difference of AP is

A.
$$\frac{1}{4}\left(\frac{b}{a} - \frac{B}{A}\right)$$

B. $\frac{1}{3}\left(\frac{b}{a} - \frac{B}{A}\right)$
C. $\frac{1}{2}\left(\frac{c}{a} - \frac{B}{A}\right)$
D. $\frac{1}{3}\left(\frac{c}{a} - \frac{C}{A}\right)$

Answer: A

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20. Suppose α , β are roots of $ax^2 + bx + c = 0$ and γ , δ are roots of $Ax^2 + Bx + C = 0$. If a, b, c are in GP as well as $\alpha, \beta, \gamma, \delta$, then A, B, C

are in:

A. (a) AP only

B. (b) GP only

C. (c) AP and GP

D. (d) None of these

Answer: B

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21. Suppose lpha, eta are roots of $ax^2 + bx + c = 0$ and γ, δ are roots of $Ax^2 + Bx + C = 0.$

If $lpha,\,eta,\,\gamma,\,\delta$ are in GP, then common ratio of GP is

A.
$$\sqrt{\left(\frac{bA}{aB}\right)}$$

B. $\sqrt{\left(\frac{aB}{bA}\right)}$
C. $\sqrt{\left(\frac{bC}{cB}\right)}$
D. $\sqrt{\left(\frac{cB}{bC}\right)}$

Answer: B



22. Suppose p is the first of n(n > 1) arithmetic means between two positive numbers a and b and q the first of n harmonic means between the same two numbers.

The value of p is

A.
$$\frac{na+b}{n+1}$$

B.
$$\frac{nb+a}{n+1}$$

C.
$$\frac{na-b}{n+1}$$

D.
$$\frac{nb-a}{n+1}$$

Answer: A

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23. Suppose p is the first of n(n > 1) arithmetic means between two positive numbers a and b and q the first of n harmonic means between the same two numbers.

The value of q is

A.
$$\displaystyle \frac{(n-1)ab}{nb+a}$$

B. $\displaystyle \frac{(n+1)ab}{nb+a}$
C. $\displaystyle \frac{(n-1)ab}{na+b}$
D. $\displaystyle \frac{(n-1)ab}{na+b}$

Answer: B

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A. q lies between p and
$$\left(\frac{n+1}{n-1}\right)^2 p$$

B. q lies between p and $\left(\frac{n+1}{n-1}\right)p$

C. q does not lie between p and $\left(\frac{n+1}{n-1}\right)^2 p$ D. q does not lie between p and $\left(\frac{n+1}{n-1}\right)p$

Answer: C

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Exercise (Single Integer Answer Type Questions)

1. Let a, b, c, d be positive real numbers with a < b < c < d. Given that a, b, c, d are the first four terms of an AP and a, b, d are in GP. The value of $\frac{ad}{bc}$ is $\frac{p}{q}$, where p and q are prime numbers, then the value of q is _____

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2. If the coefficient of x in the expansion of $\prod_{r=1}^{110} (1+rx)$ is

$\lambda(1+10)ig(1+10+10^2ig)$, then the value of λ is

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3. A 3 digit palindrome is a 3 digit number (not starting with zero) which reads the same backwards as forwards For example, 242. The sum of all even 3 digit palindromes is $2^{n_1} \cdot 3^{n_2} \cdot 5^{n_3} \cdot 7^{n_4} \cdot 11^{n_5} \cdot$ value of $n_1 + n_2 + n_3 + n_4 + n_5$ is

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4. If n is a positive integer satisfying the equation $2 + \left(6 \cdot 2^2 - 4 \cdot 2\right) + \left(6 \cdot 3^2 - 4 \cdot 3\right) + \dots + \left(6 \cdot n^2 - 4 \cdot n\right) = 140$

then the value of n is

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5. Let $S(x) = 1 + x - x^2 - x^3 + x^4 + x^5 - x^6 - x^7 + + \infty$, where 0 < x < 1. If $S(x) = \frac{\sqrt{2} + 1}{2}$, then the value of $(x + 1)^2$ is

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6. The sequence a_1, a_2, a_3, \ldots , is a geometric sequence with common ratio r. The sequence b_1, b_2, b_3, \ldots , is also a geometric sequence. If $b_1 = 1, b_2 = \sqrt[4]{7} - \sqrt[4]{28} + 1, a_1 = \sqrt[4]{28}$ and $\sum_{n=1}^{\infty} \frac{1}{a_n} = \sum_{n=1}^{\infty} (b_n)$, then the value of $(1 + r^2 + r^4)$ is

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7. Let (a_1, b_1) and (a_2, b_2) are the pair of real numbers such that 10,a,b,ab

constitute an arithmetic progression. Then, the value of $\left(rac{2a_1a_2+b_1b_2}{10}
ight)$

is

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8. If one root of $Ax^3 + Bx^2 + Cx + D = 0, D \neq 0$ is the arithmetic mean of the other two roots, then the relation $2B^3 + \lambda ABC + \mu A^2D = 0$ holds good. Then, the value of $2\lambda + \mu$ is



10. Three non-zero real numbers form a AP and the squares of these numbers taken in same order form a GP. If the possible common ratios are $(3 \pm \sqrt{k})$ where $k \in N$, then the value of $\left[\frac{k}{8} - \frac{8}{k}\right]$ is (where [] denotes the greatest integer function).

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Exercise (Matching Type Questions)

1. Match the following Column I to Column II

	Column I		Column II
(A)	a, b, c, d are in AP, then	(p)	a+d > b+c
(B)	a, b, c, d are in GP, then	(q)	ad > bc
(C)	a, b, c, d are in HP, then	(r)	$\frac{1}{a} + \frac{1}{d} > \frac{1}{b} + \frac{1}{c}$
		(s)	ad < bc

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	Column I		Column II
(A)	For an AP $a_1, a_2, a_3,, a_n,;$ $a_1 = \frac{5}{2}; a_{10} = 16.$ If $a_1 + a_2$ $+ + a_n = 110$, then 'n' equals	(p)	9
(B)	The interior angles of a convex non-equiangular polygon of 9 sides are in AP. The least positive integer that limits the upper value of the common difference between the measures of the angles in degrees is	(q)	10
(C)	For an increasing GP, $a_1, a_2, a_3,, a_n,;$ $a_6 = 4 \ a_4; a_9 - a_7 = 192,$ if $a_4 + a_5 + a_6 + + a_n = 1016$, then <i>n</i> equals	(r)	11
		(s)	12

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2.

3. Match the following Column I to Column II

The second second second second	Column I		Column II
(B)	If $a_1, a_2, a_3,$ are in AP and $a_1 + a_5 + a_{10} + a_{15} + a_{20} + a_{24}$ = 195, $\alpha = a_2 + a_7 + a_{18} + a_{23}$ and $\beta = 2 (a_3 + a_{22}) - (a_8 + a_{17})$, then	(q)	$\alpha + 2\beta = 260$
(C)	If a_1, a_2, a_3, \dots are in AP and $a_1 + a_7 + a_{10} + a_{21} + a_{24} + a_{30} = 225$, $\alpha = a_2 + a_7 + a_{24} + a_{29}$ and $\beta = 2 (a_{10} + a_{21}) - (a_3 + a_{28})$, then	(r)	$\alpha + 2\beta = 220$
		(s)	$\alpha - \beta = 5\lambda, \lambda \in I$
		(t)	$\alpha + \beta = 15\mu, \mu \in I$
		`´	-

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Matching Type Questions

Column I			Column II		
(A)	If $a_1, a_2, a_3,$ are in AP and $a_1 + a_4 + a_7 + a_{14} + a_{17} + a_{20} = 165$, $\alpha = a_2 + a_6 + a_{15} + a_{19}$ and $\beta = 2 (a_9 + a_{12}) - (a_3 + a_{18})$, then	(p)	$\alpha = 2\beta$		

1.

	Column I		Column II
(A)	If $4a^2 + 9b^2 + 16c^2$ = 2 (3ab + 6bc + 4ca), where a, b, c are non-zero numbers, then a, b, c are in	(p)	AP
(B)	If $17a^2 + 13b^2 + 5c^2$ = $(3ab + 15bc + 5ca)$, where a, b, c are non-zero numbers, then a, b, c are in	(q)	GP
(C)	If $a^2 + 9b^2 + 25c^2$ = $abc\left(\frac{15}{a} + \frac{5}{b} + \frac{3}{c}\right)$, where a, b, c are non-zero numbers, then a, b, c are in	(r)	HP
(D)	If $(a^2 + b^2 + c^2)p^2 - 2p(ab + bc + ca)$ + $(a^2 + b^2 + c^2) \le 0$, where a, b, c, p are non-zero numbers, then a, b, c are in		

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Exercise (Statement I And Ii Type Questions)

1. Statement 1 4, 8, 16, are in GP and 12,16,24 are in HP.

Statement 2 If middle term is added in three consecutive terms of a GP, resultant will be in HP.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct

explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct

explanation for Statement 1

C. Statement 1 is true, Statement 2 is false

D. Statement 1 is false, Statement 2 is true

Answer: A

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2. Satement 1 If the nth terms of a series is $2n^3 + 3n^2 - 4$, then the

second order differences must be an AP.

Statement 2 If nth term of a series is a polynomial of degree m, then mth order differences of series are constant.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct

explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct

explanation for Statement 1

C. Statement 1 is true, Statement 2 is false

D. Statement 1 is false, Statement 2 is true

Answer: A

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3. Statement 1 The sum of the products of numbers $\pm a_1, \pm a_2, \pm a_3, \dots, \pm a_n$ taken two at a time is $-\sum_{i=1}^n a_i^2$. Statement 2 The sum of products of numbers $a_1, a_2, a_3, \dots, a_n$ taken two at a time is denoted by $\sum_{1 \le i \le n} \sum a_i a_j$. A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct

explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct

explanation for Statement 1

C. Statement 1 is true, Statement 2 is false

D. Statement 1 is false, Statement 2 is true

Answer: B

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4. Statement 1 a + b + c = 18(a, b, c > 0), then the maximum value of

abc is 216.

Statement 2 Maximum value occurs when a = b = c.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct

explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct

explanation for Statement 1

C. Statement 1 is true, Statement 2 is false

D. Statement 1 is false, Statement 2 is true

Answer: A

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5. If $4a^2 + 9b^2 + 16c^2 = 2(3ab + 6bc + 4ca)$, where a,b,c are non-zero real numbers, then a,b,c are in GP. Statement 2 If $(a_1 - a_2)^2 + (a_2 - a_3)^2 + (a_3 - a_1)^2 = 0$, then

 $a_1 = a_2 = a_3, \, orall a_1, a_2, a_3 \in R.$

A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct

explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct

explanation for Statement 1

C. Statement 1 is true, Statement 2 is false

D. Statement 1 is false, Statement 2 is true

Answer: D

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6. Statement 1 If a and b be two positive numbers, where a > b and $4 \times GM = 5 \times HM$ for the numbers. Then, a = 4b.

Statement 2 $(AM)(HM) = (GM)^2$ is true for positive numbers.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct

explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct

explanation for Statement 1

- C. Statement 1 is true, Statement 2 is false
- D. Statement 1 is false, Statement 2 is true

Answer: C

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7. Statement 1 The difference between the sum of the first 100 even natural numbers and the sum of the first 100 odd natural numbers is 100. Statement 2 The difference between the sum opf the first n even natural numbers and sum of the first n odd natural numbers is n.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct

explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct

explanation for Statement 1

- C. Statement 1 is true, Statement 2 is false
- D. Statement 1 is false, Statement 2 is true

Answer: A

Exercise (Subjective Type Questions)

1. The pth, (2p)th and (4p)th terms of an AP, are in GP, then find the common ratio of GP.

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2. Find the sum of n terms of the series $(a+b) + (a^2 + ab + b^2) + (a^3 + a^2b + ab^2 + b^3) + \dots$ where $a \neq 1, b \neq 1$ and $a \neq b$.

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3. The sequence of odd natural numbers is divided into groups $1, 3, 5, 7, 9, 11, \ldots$ and so on. Show that the sum of the numbers in nth group is n^3 .



4. Let a,b,c are respectively the sums of the first n terms, the next n terms and the next n terms of a GP. Show that a,b,c are in GP.



5. If the first four terms of an arithmetic sequence are a, 2a, b and (a - 6 - b) for some numbers a and b, find the sum of the first 100 terms of the sequence.



7. If the arithmetic mean of $a_1, a_2, a_3, \dots, a_n$ is a and $b_1, b_2, b_3, \dots, b_n$ have the arithmetic mean b and $a_i + b_i = 1$ for $i = 1, 2, 3, \dots, n$, prove that $\sum_{i=1}^n (a_i - a)^2 + \sum_{i=1}^n a_i b_i = nab$. Watch Video Solution

8. If a_1, a_2, a_3, \ldots is an arithmetic progression with common difference 1 and $a_1 + a_2 + a_3 + \ldots + a_{98} = 137$, then find the value of $a_2 + a_4 + a_6 + \ldots + a_{98}$.

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9. If
$$t_1 = 1, t_r - t_{r-1} = 2^{r-1}, r \geq 2$$
, find $\sum_{r=1}^n t_r$.

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10. Prove that $I_1, I_2, I_3...$ form an AP, if

$$I_n = \int_0^\pi rac{\sin 2nx}{\sin x} dx \ .$$

11. Consider the sequence $S=7+13+21+31+....+T_n$, find the value of $T_{70}.$

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12. Find value of
$$\left(x+rac{1}{x}
ight)^3+\left(x^2+rac{1}{x^2}
ight)^3+....+\left(x^n+rac{1}{x^n}
ight)^3.$$

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13. If the sequence $a_1, a_2, a_3, \ldots, a_n$, \cdot forms an A.P., then prove that

$$a_1^2-a_2^2+a_3^2-a_4^2+.....+a_{2n-1}^2-a_{2n}^2=rac{n}{2n-1}ig(a_1^2-a_{2n}^2ig)$$

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14. If three unequel numbers are in HP and their squares are in AP, show





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16. Balls are arranged in rows to form an equilateral triangle. The first row consists of one ball, the second row of two balls and so on. If 669 more balls are added, then all the balls can be arranged in the shape of a square and each of the sides, then contains 8 balls less than each side of the triangle. Determine the initial number of balls.

17. If $heta_1, heta_2, heta_2, heta_3, \dots, \Theta_n$ are in AP whose common difference is d,

show that sec
$$heta_1 \sec heta_2 + \sec_3 + \ldots + \sec heta_{n-1} \sec heta_n = \frac{\tan heta_n - \tan heta_1}{\sin d}$$
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18. Show that,
$$(1+5^{-1})(1+5^{-2})(1+5^{-4})(1+5^{-8})....(1+5^{-2n}) = rac{5}{4}(1-5^{-2(n+1)})$$
.

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19. Evaluate
$$S=\sum_{n=0}^n rac{2^n}{\left(a^{2^n}+1
ight)}$$
 (where $a>1$).

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20. Find the sum of the series :

$$\tan^{-1}\left(\frac{1}{3}\right) + \tan^{-1}\left(\frac{2}{9}\right) + \dots + \tan^{-1}\left(\frac{2^{n-1}}{1+2^{2n-1}}\right) + \dots \infty$$

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21. Find the sum to n terms, whose nth term is $\tan[\alpha + (n-1)\beta]\tan(\alpha + n\beta).$

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22. If
$$\sum_{r=1}^n t_r = rac{n}{8}(n+1)(n+2)(n+3), ext{ then find } \sum_{r=1}^n rac{1}{t_r}.$$



23. If s_1, s_2, s_3 denote the sum of n terms of 3 arithmetic series whose first terms are unity and their common difference are in H.P., Prove that $n = \frac{2s_3s_1 - s_1s_2 - s_2s_3}{s_1 - 2s_2 + s_3}$ **24.** Three friends whose ages form a G.P. divide a certain sum of money in proportion to their ages. If they do that three years later, when the youngest is half the age of the oldest, then he will receive 105 rupees more that the he gets now and the middle friends will get 15 rupees more that he gets now, then ages of the friends are

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Exercise (Questions Asked In Previous 13 Years Exam)

1. Let a,b,c be in A.P. and
$$|a|<1,\,|b|<1|c|<1.$$
 if $x=1+a+a^2+\ldots$ to $\infty,\,y=1+b+b^2$, then x,y,z are in

A. AP

B. GP

C. HP

D. None of these

Answer: C

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3. If
$$a_1, a_2, a_3$$
, be terms of an A.P. and
 $\frac{a_1 + a_2 + \dots + a_p}{a_1 + a_2 + \dots + a_q} = \frac{p^2}{q^2}, p \neq q, then \frac{a_6}{a_{21}}$ equals to (a).41/11 (b). 7/2
(c). 2/7 (d). 11/41

A.
$$\frac{41}{11}$$

B. $\frac{7}{2}$
C. $\frac{2}{7}$
D.
$$\frac{11}{41}$$

Answer: D



4. If
$$a_1, a_2, a_3, \dots, a_n$$
 are in H.P. and
 $a_1a_2 + a_2a_3 + a_3a_4 + \dots + a_{n-1}a_n = ka_1a_n$, then k is equal to
A. $n(a_1 - a_n)$
B. $(n - 1)(a_1 - a_n)$
C. na_1a_n
D. $(n - 1)a_1a_n$

Answer: D

5. Let V_r denotes the sum of the first r terms of an arithmetic progression whose first term is r and the common difference is (2r - 1). Let $T_r = V_{r+1} - V_r - 2$ and $Q_r = T_{r+1} - T_r$ for r = 1, 2, ... T_r is always

A.
$$rac{1}{12}n(n+1)ig(3n^2-n+1ig)$$

B. $rac{1}{12}n(n+1)ig(3n^2+n+2ig)$
C. $rac{1}{2}nig(2n^2-n+1ig)$
D. $rac{1}{3}ig(2n^3-2n+3ig)$

Answer: B

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6. Let V_r denote the sum of the first r terms of an arithmetic progression (AP) whose first term is r and the common difference is (2r - 1). Let T_r=V_(r+1)-V_r-2 and Q_r =T_(r+1)-T_r for r=1,2T_r` is always (A) an odd number (B) an even number (C) a prime number (D) a composite num,ber A. an odd number

B. an even number

C. a prime number

D. a composite number

Answer: D

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7. Let V(r) denote the sum of the first r terms of an arithmetic progression (AP) whose first term is r and the common difference is (2r-1). LetT(r)=V(r+1)-V(r)-2 and Q(r) =T(r+1)-T(r) for r=1,2 $Whicho \neq of the follow \in gisac \text{ or } rectstatement? (A)Q_1, Q_2,$ Q_3, $are \in A. P. with commond \Leftrightarrow erence5(B)Q_1, Q_2,$ Q_3, $are \in A. P. with commond \Leftrightarrow erence6(C)Q_1, Q_2,$ Q_3 ..., $are \in A. P. with commond \Leftrightarrow erence11(D)Q_1=Q_2=Q_3'$

A. Q_1, Q_2, Q_3, \ldots are in AP with common difference 5

B. Q_1, Q_2, Q_3, \ldots are in AP with common difference 6

C. Q_1, Q_2, Q_3, \ldots are in AP with common difference 11

D. $Q_1 = Q_2 = Q_3 = \dots$

Answer: B

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8. Let A_1 , G_1 , H_1 denote the arithmetic, geometric and harmonic means respectively, of two distinct positive numbers. For $n \ge 2$, let A_{n-1} , G_{n-1} and H_{n-1} has arithmetic, geometric and harmonic means as A_n , G_n , H_n respectively.

Which of the following statement is correct?

A. $G_1 > G_2 > G_3 >$

B. $G_1 < G_2 < G_3 < \dots$

 $C. G_1 = G_2 = G_3 = \dots$

D. $G_1 < G_3 < G_5 < ...$ and $G_(2)gtG_(4)gtG_(6)gt...$

Answer: C

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9. Let A_1, G_1, H_1 denote the arithmetic, geometric and harmonic means respectively, of two distinct positive numbers. For n > 2, let A_{n-1}, G_{n-1} and H_{n-1} has arithmetic, geometric and harmonic means as A_n, G_N, H_N , respectively.

- A. $A_1 > A_2 > A_3 > \dots$
- B. $A_1 < A_2 < A_3 < \dots$
- ${\sf C}.\, A_1 > A_3 > A_5 >$ and $A_2 < A_4 < A_6 < ...$
- $ext{D.} A_1 < A_3 < A_5 < ext{ and } A_2 > A_4 > A_6 > ext{}$

Answer: A

10. Let A_1 , G_1 , H_1 denote the arithmetic, geometric and harmonic means respectively, of two distinct positive numbers. For $n \ge 2$, let A_{n-1} , G_{n-1} and H_{n-1} has arithmetic, geometric and harmonic means as A_n , G_n , H_n respectively.

Which of the following statement is correct?

A. $H_1 > H_2 > H_3 >$

 ${\sf B}.\, H_1 < H_2 < H_3 < \ldots \ldots$

 ${\sf C}.\, H_1 > H_3 > H_5 > \dots \, \, \, {
m and} \, \, \, H_2 < H_4 < H_6 < \dots \, \, \, \,$

D. $H_1 < H_3 < H_5 < \dots$ and $H_2 > H_4 > H_6 > \dots$

Answer: B



11. In a G.P of positive terms if any term is equal to the sum of the next two terms, then the common ratio of the G.P is

A.
$$\frac{1}{2}(1-\sqrt{5})$$

B. $\frac{1}{2}\sqrt{5}$
C. $\sqrt{5}$
D. $\frac{1}{2}(\sqrt{5}-1)$

Answer: D

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12. Suppose four distinct positive numbers a_1 , a_2 , a_3 , a_4 are in G.P. Let $b_1 = a_1 + , a_b = b_1 + a_2, b_3 = b_2 + a_3$ and $b_4 = b_3 + a_4$. Statement -1 : The numbers b_1 , b_2 , b_3 , b_4 are neither in A.P. nor in G.P. Statement -2: The numbers b_1 , b_2 , b_3 , b_4 are in H.P.

A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct

explanation for Statement 1

B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct

explanation for Statement 1

C. Statement 1 is true, Statement 2 is false

D. Statement 1 is false, Statement 2 is true

Answer: C

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13. The first two terms of a geometric progression add up to 12. The sum of the third and the fourth terms is 48. If the terms of the geometric progression are alternately positive and negative, then the first term is

A. - 12

B. 12

C. 4

 $\mathsf{D.}-4$

Answer: A

14. If the sum of first n terms of an A.P. is cn^2 then the sum of squares of

these n terms is

A.
$$rac{n(4n^2-1)c^2}{6}$$

B. $rac{n(4n^2+1)c^2}{3}$
C. $rac{n(4n^2-1)c^2}{3}$
D. $rac{n(4n^2+1)c^2}{6}$

Answer: C



15. The sum to infinity of the series $1+rac{2}{3}+rac{6}{3^2}+rac{14}{3^4}+...is$

A. 6

B. 2

C. 3

Answer: C

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16. Let S_k , k = 1, 2, ..., 100 denote the sum of the infinite geometric series whose first term is $\frac{k-1}{K!}$ and the common ration is $\frac{1}{k}$ then the value of $\frac{(100)^2}{100!} + \sum_{k=1}^{100} |(k^2-3k+1)S_k|$ is _____`

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17. Let
$$a_1, a_2, a_3, a_{11}$$
 be real numbers satisfying
 $a_1 = 15, 27 - 2a_2 > 0$ and $a_k = 2a_{k-1} - a_{k-2}$ for $k = 3, 4, 11$. If
 $\frac{a12 + a22 + ... + a112}{11} = 90$, then the value of $\frac{a1 + a2 + a11}{11}$ is
equals to _____.

18. A person is to count 4500 currency notes. Let a_n denote the number of notes he counts is the n^{th} minute .If $a_1 = a_2 = \dots = a_{10}$ = 150 and $a_{10}, a_{11}...$, are in A.P with common difference -2, then the time to count all notes

A. 34 min

B. 125 min

C. 135 min

D. 24 min

Answer: A

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19. The minimum value of the sum of real numbers a^{-5} , a^{-4} , $3a^{-3}$, 1, a^8

and a^{10} with a>0 is _____.

20. A man saves ₹ 200 in each of the first three months of his servies. In each of the subsequent monts his saving increases by ₹ 40 more than the saving of immediately previous month. His total saving from the start of service will be ₹ 11040 after .

A. 19 months

B. 20 months

C. 21 months

D. 18 months

Answer: C

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21. Let
$$a_n$$
 be the nth term of an AP, if $\sum_{r=1}^{100} a_{2r} = lpha$ and $\sum_{r=1}^{100} a_{2r-1} = eta$,

then the common difference of the AP is

A.
$$rac{lpha-eta}{200}$$

B.
$$\alpha - \beta$$

C. $\frac{\alpha - \beta}{100}$
D. $\beta - \alpha$

Answer: C



22. Let, a_1 , a_2 _ a, a_3 , be in harmonic progression with $a_1 = 5$ and $a_{20} = 25$ The least positive integer n for which $a_n < 0$ A. 22 B. 23 C. 24 D. 25

Answer: D

23. Statement 1: The sum of the series $1 + (1 + 2 + 4) + (4 + 6 + 9) + (9 + 12 + 16) + \dots$ + (361 + 380 + 400)is8000. Statement 2: $\sum_{k=1}^{n} (k^3 - (k - 1)^3) = n^3$ for any natural number n. (1) Statement 1 is false, statement 2 is true (2) Statement 1 is true, statement 2 is true; statement 2 is a correct explanation for statement 1 (3) Statement 1 is true, statement 2 is true; statement 2 is not a correct explanation for statement 1 (4) Statement 1 is true, statement 2 is false

- A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1
- B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct

explanation for Statement 1

C. Statement 1 is true, Statement 2 is false

D. Statement 1 is false, Statement 2 is true

Answer: A

24. If 100 times the 100 th term of an A.P with non- zero common difference equals the 50 times its 50th term,then the 150th term of this A.P is

A.P IS

A. 150 times its 50th term

B. 150

C. zero

D. -150

Answer: C

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25. If x,y,z are in AP and $\tan^{-1} x$, $\tan^{-1} y$, $\tan^{-1} z$ are also in AP, then

A. 2x = 3y = 6z

B. 6x = 3y = 2z

C. 6x = 4y = 3z

 $\mathsf{D}.\, x=y=z$

Answer: D

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26. The sum of first 20 terms of the sequence 0.7, 0.77, 0.777, is

A.
$$rac{7}{9} (99 - 10^{-20})$$

B. $rac{7}{81} (179 + 10^{-20})$
C. $rac{7}{9} (99 + 10^{-20})$
D. $rac{7}{81} (179 - 10^{-20})$

Answer: B

27. $LetS_n=\sum\limits_{k=1}^{4n}(-1)^{rac{k(k+1)}{2}}k^2.$ Then S_n can take value (s)

A. 1056

B. 1088

C. 1120

D. 1332

Answer: A::D

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28. A pack contains n cards numbered from 1 to n. Two consecutive numbered cards are removed from the pack and the sum of the numbers on the remaining cards is 1224. If the smaller of het numbers on the removed cards is k, then k - 20 = _____.

29. If $(10)^9 + 2(11)^2(10)^7 + \ldots + 10(11)^9 = k(10)^9$

A. 100

B. 110



Answer: A

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30. Three positive numbers form an increasing GP. If the middle terms in this GP is doubled, the new numbers are in AP. Then, the common ratio of the GP is

A. $2-\sqrt{3}$

 $\mathsf{B.}\,2+\sqrt{3}$

C. $\sqrt{2} + \sqrt{3}$

D. $3 + \sqrt{2}$

Answer: B



31. about to only mathematics

32. The sum of first 9 terms of the series

$$\frac{1^{3}}{1} + \frac{1^{3} + 2^{3}}{1 + 3} + \frac{1^{3} + 2^{3} + 3^{3}}{1 + 3 + 5} + \dots \text{ is}$$
A. 192
B. 71
C. 96
D. 142

Answer: C



33. If m is the A.M. of two distinct real numbers l and n(l, n > 1) and G1, G2 and G3 are three geometric means between l and n, then G14 + 2G24 + G34 equals, (1) $4l^2$ mn (2) $4l^m \hat{\ } 2$ mn (3) $4lmn^2$ (4) $4l^2m^2n^2$

A. $4l^2m^2n^2$

 $\mathsf{B.}\,4l^2mn$

 $\mathsf{C.}\,4lm^2n$

D. $4lmn^2$

Answer: C

34. Soppose that all the terms of an arithmetic progression (AP) are natural numbers. If the ratio of the sum of the first seven terms to the sum of the first eleven terms is 6:11 and the seventh term lies between 130 and 140, then the common difference of this AP is

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35. If the 2nd , 5th and 9th terms of a non-constant A.P are in G.P then the common ratio of this G.P is

A. 1

B.
$$\frac{7}{4}$$

C. $\frac{8}{5}$
D. $\frac{4}{3}$

Answer: D

36. If the sum of the first ten terms of the series $\left(1\frac{3}{5}\right)^2 + \left(2\frac{2}{5}\right)^2 + \left(3\frac{1}{5}\right)^2 + 4^2 + \left(4\frac{4}{5}\right)^2 + \dots$, is $\frac{16}{5}$ m, then

m is equal to: (1) 102 (2) 101 (3) 100 (4) 99

A. 100

B. 99

C. 102

D. 101

Answer: D

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37. Let $b_i > 1$ for i = 1, 2,, 101. Suppose $\log_e b_1, \log_e b_2, \log_e b_3, ..., \log_e b_{101}$ are in Arithmetic Progression (AP) with the common difference $\log_e 2$. Suppose $a_1, a_2, a_3, ..., a_{101}$ are in AP. Such that, $a_1 = b_1$ and $a_{51} = b_{51}$. If $t = b_1 + b_2 + ..., + b_{51}$ and $s = a_1 + a_2 + ..., + a_{51}$, then

- A. (a) $s > t \; \; ext{and} \; \; a_{101} > b_{101}$
- B. (b)s > t and $a_{101} < b_{101}$
- C. (c) $s < t \; \; ext{and} \; \; a_{101} > b_{101}$
- D. (d)s < t and $a_{101} < b_{101}$

Answer: B

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38. For any three positive real numbers a,b and $c,9ig(25a^2+b^2ig)+25ig(c^2-3acig)=15b(3a+c)$. Then :

A. a,b and c are in GP

B. b,c and a are in GP

C. b,c and a are in AP

D. a,b and c are in AP

Answer: C

