# ©゙ doubtnut 

## MATHS

## BOOKS - ARIHANT MATHS (ENGLISH)

## SEQUENCES AND SERIES

## Examples

1. If $f: N \rightarrow R$, where $f(n)=a_{n}=\frac{n}{(2 n+1)^{2}}$ write the sequence in ordered pair from.

## - Watch Video Solution

2. The Fibonacci sequence is defined by
$1=a_{1}=a_{2}(\text { and } a)_{n}=a_{n-1}+a_{n-2}, n>2$. Find $\frac{a_{n+1}}{a_{n}}$, for $\mathrm{n}=1,2,3$,
4, 5.
3. If the sum of $n$ terms of a series is $2 n^{2}+5 n$ for all values of $n$, find its 7th term.

## - Watch Video Solution

4. (i) Write $\sum_{r=1}^{n}\left(r^{2}+2\right)$ in expanded form.
(ii) Write the series $\frac{1}{3}+\frac{2}{4}+\frac{3}{5}+\frac{4}{6}+\ldots+\frac{n}{n+2}$ in sigma form.

## Watch Video Solution

5. Which of the following are A.P. (i) $1,3,5,7, \ldots$
(ii) $\pi, \pi+e^{\pi}, \pi+2 e^{\pi}, \ldots$.
(iii) $a, a-b, a-2 b, a-3 b, \ldots$

## Watch Video Solution

6. Show that the sequence $t_{n}$ defined by $t_{n}=5 n+4$ is AP, also find its common difference.

## - Watch Video Solution

7. Show that the the sequence defined by $T_{n}=3 n^{2}+2$ is not an AP.

## - Watch Video Solution

8. Which term of the sequence $20,19 \frac{1}{4}, 18 \frac{1}{2}, 17 \frac{3}{4}$, is the first negative term?

## - Watch Video Solution

9. If $m$ th term of an AP is $1 / n$ and its $n$th term is $1 / m$, then show that its (mn)th term is 1

## - Watch Video Solution

10. If $|x-1|, 3$ and $|x-3|$ are first three terms of an increasing AP, then find the 6th term of on AP .

## - Watch Video Solution

11. In the sequence $1,2,2,3,3,4,4,4,4, \ldots \ldots$. . . where $n$ consecutive terms have the value $n$, the 150th term, is

## - Watch Video Solution

12. If $a_{1}, a_{2}, a_{3}, a_{4}$ and $a_{5}$ are in AP with common difference $\neq 0$, find the value of $\sum_{i=1}^{5} a_{i}$ when $a_{3}=2$.

## - Watch Video Solution

13. The ratio of the sum of $\operatorname{mandn}$ terms of an A.P. is $m^{2}: n^{2}$. Show that the ratio of the $m$ th and $n$th terms is $(2 m-1):(2 n-1)$.
A. $(2 m+1):(2 n-1)$,
B. $m: n$
C. $(2 m-1):(2 n-1)$
D. None of these

## Watch Video Solution

14. The sums of $n$ terms of two arithmetic progresssions are in the ratio $(7 n+1):(4 n+17)$. Find the ratio of their $n$th terms and also common differences.

## - Watch Video Solution

15. The sums of $n$ terms of two AP's are in the ratio $(3 n-13):(5 n+21)$. Find the ratio of their 24th terms.
16. How many terms of the A.P. $20,19 \frac{1}{3}, 18 \frac{2}{3}, \ldots . . . . . .$. must be taken so that their sum is 300 ?

## - Watch Video Solution

17. Find the arithmetic progression consisting of 10 terms, if sum of the terms occupying the even places is equal to 15 and the sum of those occupying the odd places is equal to $\frac{25}{2}$

## - Watch Video Solution

18. If the set of natural numbers is partitioned into subsets $S_{1}=\{1\}, S_{2}=\{2,3\}, S_{3}=\{4,5,6\}$ and so on then find the sum of the terms in $S_{50}$.

## - Watch Video Solution

19. Find the sum of first 24 terms of on $\mathrm{AP} t_{1}, t_{2}, t_{3}, \ldots$., if it is known that $t_{1}+t_{5}+t_{10}+t_{15}+t_{20}+t_{24}=225$.

## D Watch Video Solution

20. If $(1+3+5++p)+(1+3+5++q)=(1+3+5++r)$ where each set of parentheses contains the sum of consecutive odd integers as shown, the smallest possible value of $p+q+r(w h e r e p>6)$ is 12 b. 21 c. 45 d. 54

## - Watch Video Solution

21. If $S_{1}, S_{2}, S_{3}, S_{m}$ are the sums of $n$ terms of $m$ A.P. ' $s$ whose first terms are $1,2,3, \ldots m$ and common differences are $1,3,5, \ldots(2 m-1)$ respectively. Show that $S_{1}+S_{2} \ldots .+S_{m}=\frac{m n}{2}(m n+1)$

## - Watch Video Solution

22. Let $\alpha$ and $\beta$ be roots of the equation $X^{2}-2 x+A=0$ and let $\gamma$ and $\delta$ be the roots of the equation $X^{2}-18 x+B=0$. If $\alpha<\beta<\gamma<\delta$ are in arithmetic progression then find the valus of $A$ and $B$.

## - Watch Video Solution

23. The digits of a positive integer, having three digits, are in A.P. and their sum is 15 . The number obtained by reversing the digits is 594 less than the original number. Find the number.

## - Watch Video Solution

24. If three positive real numbers $a, b, c$ are in A.P. such that $a b c=4$, then the minimum value of $b$ is

## - Watch Video Solution

25. If a,b,c,d are distinct integers in an A.P. such that $d=a^{2}+b^{2}+c^{2}$, then find the value of $a+b+c+d$.

## - Watch Video Solution

26.1, $2,4,8,16, \ldots$.

## - View Text Solution

27. $9,3,1, \frac{1}{3}, \frac{1}{9}, \ldots$.

## - View Text Solution

28. Find the 5 th and nth term of sequence $-2,-6,-18, \ldots \ldots . . .{ }^{\prime \prime}$

## - Watch Video Solution

29. What is the sum of this series upto infinite terms $-8,-4,-2,-1,-\frac{1}{2}, \ldots$

## Watch Video Solution

30. Find the nth and 5 th term of sequence $5,-10,20, \ldots$

## - Watch Video Solution

31. Find the sum of series to $n$ terms $5,5,5,5, \ldots$..

## - Watch Video Solution

32.1, $1+I, 2 i,-2+2 i, \ldots . i=\sqrt{-1}$

## - Watch Video Solution

33. Show that the sequence $t_{n}$ defined by $t_{n}=\frac{2^{2 n-1}}{3}$ for all values of $n \in N$ is a GP. Also, find its common ratio.

## - Watch Video Solution

34. Show that the sequence $t_{n}$ defined by $t_{n}=2 \cdot 3^{n}+1$ is not a GP.

## Watch Video Solution

35. If first term of a GP is a , third term is b and $(n+1)$ th term is c . The
$(2 n+1) t h$ term of a GP is
A. $c \sqrt{\frac{b}{a}}$
B. $\frac{b c}{a}$
C. $a b c$
D. $\frac{c^{2}}{a}$
36. In a $G P$ if the $(m+n) t h$ term is $p$ and $(m-n) t h$ term is $q$ then $m t h$ term is
A. $p\left(\frac{q}{p}\right)^{\frac{m}{2 n}}$
B. $\sqrt{p q}$
C. $\sqrt{\frac{p}{q}}$
D. None of these

## - Watch Video Solution

37. If $\sin \theta, \sqrt{2}(\sin \theta+1), 6 \sin \theta+6$ are in GP , than the fifth term is
A. 81
B. $81 \sqrt{2}$
C. 162
D. $162 \sqrt{2}$

## - Watch Video Solution

38. The 1025th term in the sequence are $1,22,4444,88888888, \ldots$ is
A. $2^{9}$
B. $2^{10}$
C. $2^{11}$
D. $2^{12}$
39. If $a, b, c$ are real numbers such that $3\left(a^{2}+b^{2}+c^{2}+1\right)=2(a+b+c+a b+b c+c a)$, than $a, b, c$ are in
A. AP only
B. GP only
C. GP and AP
D. None of these

## - Watch Video Solution

40. Find the value of 0.3258 .

## - Watch Video Solution

41. Find the sum upto $n$ terms of the series
$a+a a+a a a+a a a a+\ldots \ldots, \forall a \in N$ and $1 \leq a \leq 9$.
42. Find the sum of the series upto $n$ terms $0 . b+0 . b b+0 . b b b+0 . b b b b+\ldots \ldots ., \forall \mathrm{b} \in N$ and $1 \leq b \leq 9$.

## - Watch Video Solution

43. If N , the set of natural numbers is partitioned into groups
$S_{1}=\{1\}, S_{2}=\{2,3\}, S_{3}=\{4,5,6,7\}, S_{4}=\{8,9,10,11,12,13,14,15\},$.
find the sum of the numbers in $S_{50}$.

## - Watch Video Solution

44. If $S_{n}=1+\frac{1}{2}+\frac{1}{2^{2}}+\ldots+\frac{1}{2^{n-1}}$ and $2-S_{n}<\frac{1}{100}$, then the least value of $n$ must be :

## - Watch Video Solution

45. 

$X=1+a+a^{2}+a^{3}+\ldots+\infty$ and $y=1+b+b^{2}+b^{3}+\ldots+\infty$ show that $1+a b+a^{2} b^{2}+a^{3} b^{3}+\ldots+\infty=\frac{x y}{x+y-1}$, where $0<a<1$ and 0

## - Watch Video Solution

46. If $1+a b+a^{2} b^{2}+a^{3} b^{3}+\ldots+\infty=\frac{x y}{x+y-1}$ are the sum of infinire geometric series whose first terms are $1,2,3, \ldots, p$ and whose common ratios are $S_{1}, S_{2}, S_{3}, \ldots, S_{p} \frac{1}{2}, \frac{1}{3}, \frac{1}{4}, \ldots \frac{1}{p+1}$ respectively, prove that $S_{1}+S_{2}+S_{3}+\ldots+S_{p}=\frac{p(p+3)}{2}$.

## D Watch Video Solution

47. If $x_{1}, x_{2}$ be the roots of the equation $x^{2}-3 x+A=0$ and $x_{3}, x_{4}$ be those of the equation $x^{2}-12 x+B=0$ and $x_{1}, x_{2}, x_{3}, x_{4}$ be an increasing GP. find find $A$ and $B$.
48. Suppose $a, b, c$ are in AP and $a^{2}, b^{2}, c^{2}$ are in GP, If $a>b>c$ and $a+b+c=\frac{3}{2}$, than find the values of $a$ and $c$.

## - Watch Video Solution

49. If the continued product of three numbers in GP is 216 and the sum of their products in pairs is 156 , then find the sum of three numbers.

## - Watch Video Solution

50. Find a three digit numberwhose consecutive digits form a GP. If we subtract 792 from this number, we get a number consisting of the same digits written in the reverse order. Now, if we increase the second digit of the required number by 2 , then the resulting digits will form an AP.

## - Watch Video Solution

51. A square is drawn by joining mid pint of the sides of a square. Another square is drawn inside the second square in the same way and the process is continued in definitely. If the side of the first square is 16 cm , then what is the sum of the areas of all the squares ?

## - Watch Video Solution

52. One side of an equilateral triangle is 24 cm . The midpoints of its sides are joined to form another triangle whose midpoints are in turn joined to form still another triangle this process continues indefinitely. The sum of the perimeters of all the triangles is

## - Watch Video Solution

53. Let $S_{1}, S_{2}$, be squares such that for each $n \geq 1$, the length of a side of $S_{n}$ equals the length of a diagonal of $S_{n+1}$. If the length of a side of $S_{1} i s 10 \mathrm{~cm}$, then for which of the following value of $n$ is the area of $S_{n}$ less than 1 sq. cm? a. 5 b. 7 c. 9 d. 10

## - Watch Video Solution

54. about to only mathematics

## - Watch Video Solution

55. Dipesh writes letters to four of his friends. He asks each of them to copy the letter and mail to four different persons with the request that they continue the chain similarly. Assuming that the chain is not broken and that it costs 25 paise to mail one letter, find the total money spent on postage till the 8th set of letters is mailed.

## - Watch Video Solution

56. An insect starts from a point and travels in a straight path 1 mm in the first second and half of the distance covered in the previous second in the succeeding second. In how much time would it reach a point 3 mm away from its starting point.
57. The pollution in a normal atmosphere is less than $0.01 \%$. Due to leakage of a gas from a factory, the pollution is increased to $20 \%$. If every day $80 \%$ of pollution is neutralised, in how many days the atmosphere will be normal?

## Watch Video Solution

58. If $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are in HP , then $\frac{a-b}{b-c}$ is equal to

## - Watch Video Solution

59. Find the first term of a HP whpse secpmd ter, os $\frac{5}{4}$ and the third term is $\frac{1}{2}$.

## - Watch Video Solution

60. If $\frac{1}{a}+\frac{1}{a-b}+\frac{1}{c}+\frac{1}{c-b}=0$ and $a+c-b \neq 0$, then prove that $a, b, c$ are in H.P.

## - Watch Video Solution

61. If $a_{1}, a_{2}, a_{3}, \ldots ., a_{n}$ are in HP, than prove that $a_{1} a_{2}+a_{2} a_{3}+a_{3} a_{4}+\ldots . .+a_{n-1} a_{n}=(n-1) a_{1} a_{n}$

## - Watch Video Solution

62. The sum of three numbers in HP is 37 and the sum of their reciprocals is $\frac{1}{4}$. Find the numbers.

## - Watch Video Solution

63. If pth, qth and rth terms of a HP be respectivelya, $b$ and $c$, has prove that $(q-r) b c+(r-p) c a+(p-q) a b=0$.
64. If $a, b, c$, are in $A P, a^{2}, b^{2}, c^{2}$ are in HP, then prove that either $a=b=c$ or $a, b,-\frac{c}{2}$ from a GP $(2003,4 \mathrm{M})$

## - Watch Video Solution

65. If $a, b, c$ are in $\mathrm{HP}, \mathrm{b}, \mathrm{c}, \mathrm{d}$ are in GP and $c, d, e$ are in AP, than show that $e=\frac{a b^{2}}{(2 a-b)^{2}}$.

## - Watch Video Solution

66. Given $a, b, c$ are in A.P.,b,c,d are in G.P and $c, d, e$ are in H.P .If $a=2$ and $e=18$ , then the sum of all possible values of c is $\qquad$ .

## - Watch Video Solution

67. If three positive numbers $a, b$ and c are in AP, GP and HP as well, than find their values.

## - Watch Video Solution

68. If $a, b, c$ are in AP and p is the AM between a and b and q is the AM between $b$ and $c$, then show that $b$ is the $A M$ between $p$ and $q$.

## - Watch Video Solution

69. Find the value of $n$ so that $\frac{a^{n+1}+b^{n+1}}{a^{n}+b^{n}}$ may be the geometric mean between $a$ and $b$.

## - Watch Video Solution

70. There are n AM's between 3 and 54.Such that the 8th mean and $(n-2)$ th mean is 3 ratio 5 . Find n .
71. If 11 AM's are inserted between 28 and 10 , than find the three middle terms in the series.

## - Watch Video Solution

72. If $a, b, c$ are in AP, than show that $a^{2}(b+c)+b^{2}(c+a)+c^{2}(a+b)=\frac{2}{9}(a+b+c)^{3}$.

## - Watch Video Solution

73. If a is the A.M. of b and c and the two geometric means are $G_{1}$ and $G_{2}$, then prove that $G_{1}^{3}+G_{2}^{3}$

## - Watch Video Solution

74. If one G.M., $G$ and two A.M's $p$ and $q$ be inserted between two given numbers, prove that
$G^{2}=(2 p-q)(2 q-p)$

## - Watch Video Solution

75. Find the value of $n$ so that $\frac{a^{n+1}+b^{n+1}}{a^{n}+b^{n}}$ may be the geometric mean between $a$ and $b$.

## - Watch Video Solution

76. Insert five geimetrec means between $\frac{1}{3}$ and 9 and verify that their product is the fifth power of the geometric mean between $\frac{1}{3}$ and 9 .

## - Watch Video Solution

77. AM between two numbers whose sum is 100 is ti the GM as $5: 4^{2}$, find the numbers.

## - Watch Video Solution

78. If $a_{1}, a_{2}, a_{3}, \ldots . a_{n}$ are positive real numbers whose product is a fixed number c , then the minimum value of $a_{1}+a_{2}+\ldots .+a_{n-1}+3 a_{n}$ is

## - Watch Video Solution

79. If H be the harmonic mean between x and y , then show that $\frac{H+x}{H-x}+\frac{H+y}{H-y}=2$

## ( Watch Video Solution

80. IF $a_{1}, a_{2}, a_{3}, \ldots . a_{10}$ be in AP and $h_{1}, h_{2}, h_{3}, \ldots . h_{10}$ be in HP. If $a_{1}=h_{1}=2$ and $a_{10}=h_{10}=3$, then find value of $a_{4} h_{7}$.
81. Find n , so that $\frac{a^{n+1}+b^{n+1}}{a^{n}+b^{n}}(a \neq b)$ be HM beween a and b .

## - Watch Video Solution

82. Insert 6 harmonic means between 3 and $\frac{6}{23}$

## - Watch Video Solution

83. If $A^{x}=G^{y}=H^{z}$, where $A, G, H$ are AM,GM and HM between two given quantities, then prove that $x, y, z$ are in HP.

## - Watch Video Solution

84. The harmonic mean of two numbers is 4. Their arithmetic mean $A$ and the geometric mean $G$ satisfy the relation $2 A+G^{2}=27$. Find two

## numbers.

## - Watch Video Solution

85. If the geometric mea is $\frac{1}{n}$ times the harmonic mean between two numbers, then show that the ratio of the two numbers is $1+\sqrt{1-n^{2}}: 1-\sqrt{1-n^{2}}$.

## - Watch Video Solution

86. Statement -1: If $a, b, c$ are distinct real numbers in H.P, then $a^{n}+c^{n}>2 b^{n}$ for all $n \in N$.

Statement -2: $A M>G M>H M$

## - Watch Video Solution

87. If $a, b, c, d$ be four distinct positive quantities in AP , then
(a) $b c>a d$
(b) $c^{-1} d^{-1}+a^{-1} b^{-1}>2\left(b^{-1} d^{-1}+a^{-1} c^{-1}-a^{-1} d^{-1}\right)$

## - Watch Video Solution

88. If $a, b, c, d$ be four distinct positive quantities in GP,then
(a) $a+d>b+c$
(b) $c^{-1} d^{-1}+a^{-1} b^{-1}>2\left(b^{-1} d^{-1}+a^{-1} c^{-1}-a^{-1} d^{-1}\right)$

## - Watch Video Solution

89. If $a, b, c, d$ be four disinct positive quantities in HP , then
(a) $a+d>b+c$
(b) $a d>b c$

## - Watch Video Solution

90. Find the sum of $n$ terms of the series $1+\frac{4}{5}+\frac{7}{5^{2}}+10+5^{3}+$.
91. The sum to infinity of the series
$1+\frac{4}{5}+\frac{7}{5^{2}}+\frac{10}{5^{3}}+\ldots$, is

## ( Watch Video Solution

92. If the sum to infinity of the series $1+4 x+7 x^{2}+10 x^{3}+\ldots \ldots \ldots \ldots$. is $\frac{35}{16}$ then $x=$ (A) $\frac{1}{5}$ (B) $\frac{2}{5}$ (C) $\frac{3}{7}$ (D) $\frac{1}{7}$

## - Watch Video Solution

93. Find the sum of the series
$1+2^{2} x+3^{2} x^{2}+4^{2} x^{3}+\ldots$ upto $\infty|x|<1$.

## - Watch Video Solution

94. Find the sum of the series $1^{2}+3^{2}+5^{2}+\rightarrow n$ terms.
95. Find the sum of $n$ terms of the series $1.2^{2}=2.3^{2}+3.4^{2}+$

## - Watch Video Solution

96. Find the sum of n terms of the series whose $n$th terms is
(i) $n(n-1)(n+1)$.

## - Watch Video Solution

97. Find the sum of n terms of the series whose $n$th terms is
(ii) $n^{2}+3^{n}$.

## - Watch Video Solution

98. Find the sum of the series $\frac{1^{3}}{1}+\frac{1^{3}+2^{3}}{1+3}+\frac{1^{3}+2^{3}+3^{3}}{1+3+5}+$ up to $n$ terms.

## - Watch Video Solution

99. Show that $S_{n}=\frac{n\left(2 n^{2}+9 n+13\right)}{24}$.

## - Watch Video Solution

100. Find the sum of $n$ terms of the series $1.2 .3+2.3 .4+3.4 .5+$

## - Watch Video Solution

101. Find sum to $n$ terms of the series $1+(2+3)+(4+5+6)+\ldots$.

## - Watch Video Solution

102. Find the sum of the series
$1 \cdot n+2 \cdot(n-1)+3 \cdot(n-2)+4 \cdot(n-3)+\ldots+(n-1) \cdot 2+, \cdot 1$ also, find the coefficient of $x^{n-1}$ in th cxpansion of $\left(1+2 x+3 x^{2}+\ldots . n x^{n-1}\right)^{2}$.

## - Watch Video Solution

103. Find the nth term and sum to n tems of the following series: 1+5+12+22+.

## - Watch Video Solution

104. Sum to n terms the series $1+3+7+15+31+\ldots$

## - Watch Video Solution

105. Find the nth term of the series $=1+4+10+20+35+\ldots$
106. Find the nth term of the series $1+5+18+58+179+\ldots$.

## - Watch Video Solution

107. Sum of the following series to $n$ term: $2+4+7+11+16+$

## - Watch Video Solution

108. Find the sum of the following series to $n$ terms $5+7+13+31+85+$

## - Watch Video Solution

109. Find the nth term of the series $1+2+5+12+25+46+\ldots .$.
110. Find the $n$th term of the series $2+5+12+31+86+\ldots$.

## - Watch Video Solution

111. Find the $n$th term and sum to $n$ terms of the series $12+40+90+168+280+432+\ldots .$.

## - Watch Video Solution

112. Find the sum upto $n$ terms of the series $1+4+7+10+13+16+\ldots$.

## - Watch Video Solution

113. Find the sum to $n$ terms of the series $\frac{1}{1 \cdot 3 \cdot 5 \cdot 7 \cdot 9}+\frac{1}{3 \cdot 5 \cdot 7 \cdot 9 \cdot 11}+\frac{1}{5 \cdot 7 \cdot 9 \cdot 11 \cdot 13}+\ldots \ldots$. Also, find the sum to infinty terms.

## Watch Video Solution

114. If $\sum_{r=1}^{n} T_{r}=\frac{n(n+1)(n+2)(n+3)}{12}$ where $T_{r}$ denotes the rth term of the series. Find $\lim _{n \rightarrow \infty} \sum_{r=1}^{n} \frac{1}{T_{r}}$.

## D Watch Video Solution

115. If $y z+z x+x y=12$, where $\mathrm{x}, \mathrm{y}, \mathrm{z}^{\prime}$ are positive values find the greatest value of $x y z$.

## - Watch Video Solution

116. Find the greatest value of $x^{3} y^{4}$ if $2 x+3 y=7$ and $x \geq 0, y \geq 0$.

## - Watch Video Solution

117. Find the least value of $3 x+4 y$ for positive values of x and y , dubject to the condition $x^{2} y^{3}=6$.

## - Watch Video Solution

118. The minimum value of $P=b c x+c a y+a b z$, when $x y z=a b c$, is

## - Watch Video Solution

119. If $a, b, c$ are positive real numbers such that $a+b+c=1$, then prove that $\frac{a}{b+c}+\frac{b}{c+a}+\frac{c}{a+b} \geq \frac{3}{2}$

## - Watch Video Solution

120. If $\mathrm{a}+\mathrm{b}-1, \mathrm{a}>0, \mathrm{~b}>0$, prove that $\left(a+\frac{1}{a}\right)^{2}+\left(b+\frac{1}{b}\right)^{2} \geq \frac{25}{2}$
121. If $b-c, 2 b-\lambda, b-a$ are in HP, then $a-\frac{\lambda}{2}, b-\frac{\lambda}{2}, c-\frac{\lambda}{2}$ are is
A. AP
B. GP
C. HP
D. None of these

## Answer: B

## - Watch Video Solution

122. Let $a_{1}, a_{2}, a_{3}, \ldots \ldots a_{10}$ are in GP with $a_{51}=25$ and $\sum_{i=1}^{101} a_{i}=125$ than the value of $\sum_{i=1}^{101}\left(\frac{1}{a_{i}}\right)$ equals.
A. 5
B. $\frac{1}{5}$
C. $\frac{1}{25}$
D. $\frac{1}{125}$

## Answer: B

## - Watch Video Solution

123. 

$x=111 \ldots . .(20$ digits $), y=333 \ldots .(10$ digits $)$ and $z=222 \ldots . .2(10$ digits $), t$
equals.
A. $\frac{1}{2}$
B. 1
C. 2
D. 4

## Answer: B

124. Consider the sequence $1,2,2,3,3,3, \ldots \ldots$, where n occurs n times that occuts as 201th rerms is
A. 61
B. 62
C. 63
D. 64

## Answer: C

## - Watch Video Solution

125. Let $S=\sum_{r=1}^{117} \frac{1}{2[\sqrt{r}]+1}$, when $[\cdot]$ denites the greatest integer function and if $S=\frac{p}{q}$, when p and q are co-primes, the value of $p+q$ is
A. 20
B. 76
C. 19
D. 69

## Answer: B

## - Watch Video Solution

126. If $a, b, c$ are non-zero real numbers, then the minimum value of the expression $\frac{\left(a^{8}+4 a^{4}+1\right)\left(b^{4}+3 b^{2}+1\right)\left(c^{2}+2 c+2\right)}{a^{4} b^{2}}$ equals
A. 12
B. 24
C. 30
D. 60

## Answer: C

127. If the sum of $m$ consecutive odd integers is $m^{4}$, then the first integer is
A. $m^{3}+m+1$
B. $m^{3}+m-1$
C. $m^{3}-m-1$
D. $m^{3}-m+1$

## Answer: D

## - Watch Video Solution

128. $\sum_{r=1}^{\infty} \frac{(4 r+5) 5^{-r}}{r(5 r+5)}$
A. $\frac{1}{5}$
B. $\frac{2}{5}$
C. $\frac{1}{25}$
D. $\frac{2}{25}$

## D Watch Video Solution

129. Let $\lambda$ be the greatest integer for which $5 p^{2}-16,2 p \lambda, \lambda^{2}$ are jdistinct consecutive terms of an AP, where $p \in R$. If the common difference of the Ap is $\left(\frac{m}{n}\right), n \in N$ and $\mathrm{m}, \mathrm{n}$ are relative prime, the value of $m+n$ is
A. 133
B. 138
C. 143
D. 148

## Answer: C

130. If $2 \lambda, \lambda$ and $\left[\lambda^{2}-14\right], \lambda \in R-\{0\}$ and [ $\cdot$ ] denotes the gratest integer function are the first three terms of a GP in order, then the 51th term of the sequence, $1,3 \lambda, 6 \lambda, 10 \lambda, \ldots$, is
A. 5104
B. 5304
C. 5504
D. 5704

## Answer: B

## - Watch Video Solution

131. The first three terms of a sequence are $3,-1,-1$. The next terms are
A. 2
B. -3
C. $-\frac{5}{27}$
D. $-\frac{5}{9}$

## Answer: B

## - Watch Video Solution

132. There are two numbers $a$ and $b$ whose product is 192 and the quotient of $A M$ by $H M$ of their greatest common divisor and least common multiple is ${ }^{`}(169) /(48)$. The smaller of $a$ and $b$ is
A. 2
B. 4
C. 6
D. 12

## Answer: B::D

133. Consider a series $\frac{1}{2}+\frac{1}{2^{2}}+\frac{2}{2^{3}}+\frac{3}{2^{4}}+\frac{5}{2^{5}}+\ldots \ldots \ldots \ldots .+\frac{\lambda n}{2^{n}}$. If $S_{n}$ denotes its sum to $n$ tems, then $S_{n}$ cannot be
A. 2
B. 3
C. 4
D. 5

## Answer: A::B::C::D

## - Watch Video Solution

134. If $S_{r}=\sqrt{r+\sqrt{r+\sqrt{r+\sqrt{r+\ldots . \infty}}}}, r>0$, then which of the following is/are correct.
A. $S_{r}, S_{6}, S_{12}, S_{20}$, are in AP
B. $S_{4}, S_{9}, S_{16}$ are irrational
C. $\left(2 S_{4}-1\right)^{2},\left(2 S_{5}-1\right)^{2},\left(2 S_{6}-1\right)^{2}$ are in AP
D. $S_{2}, S_{12}, S_{56}$ are in GP

## Answer: A::B::C::D

## - Watch Video Solution

135. If $\frac{1}{a}, \frac{1}{b}, \frac{1}{c}$ are in A.P and $\mathrm{a}, \mathrm{b}-2 \mathrm{c}$, are in G.P where $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are non-zero then
A. $a^{3}+b^{3}+c^{3}=3 a b c$
B. $-2 a, b,-2 c$ are in AP
C. $-2 a, b,-2 c$ are inGP
D. $a^{2}, b^{2}, 4 c^{2}$ are in GP

## Answer: A::B::D

136. The nature of the $S_{n}=3 n^{2}+5 n$ series is
A. AP
B. GP
C. HP
D. AGP

## Answer: A

137. For the $S_{n}=3 n^{2}+5 n$ sequence, the number 5456 is the
A. 153th term
B. 932th term
C. 707th term
D. 909th term

## Answer: D

## D Watch Video Solution

138. Consider a sequence whose sum to $n$ terms is given by the quadratic function $\mathrm{Sn}=3\left(\mathrm{n}^{\wedge} 2\right)+5 \mathrm{n}$. Then sum of the squares of the first 3 terms of the given series is
A. 1100
B. 660
C. 799
D. 1000

## Answer: B

139. Find the number of terms common to the two A.P. $s$ : 3, 7, 11, 407and2, 9, 16, , 709 .
A. 14
B. 21
C. 28
D. 35

## Answer: A

## - Watch Video Solution

140. The 10th common terms between the series $3+7+11+\ldots .$. And $1+6+11+\ldots .$. is
(i) 191
(ii) 193
(iii) 211
(iv) None of these
A. 189
B. 191
C. 211
D. 213

## Answer: B

## - Watch Video Solution

141. The largest term common to the sequence $1,11,21,31, \ldots$. .to 100 terms and $31,36,41,46$,...... to 100 tetms is
A. 281
B. 381
C. 471
D. 521

## Answer: D

142. If $x>0, y>0, z>0$ and $x+y+z=1$ then the minimum value of $\frac{x}{2-x}+\frac{y}{2-y}+\frac{z}{2-z}$ is:
A. (a) 0.2
B. (b) 0.4
C. (c) 0.6
D. (d) 0.8

## Answer: C

## - Watch Video Solution

143. If $\sum_{i=1}^{n} a_{i}^{2}=\lambda, \forall a_{i} \geq 0$ and if greatest and least values of
$\left(\sum_{i=1}^{n} a_{i}\right)^{2}$ are $\lambda_{1}$ and $\lambda_{2}$ respectively, then $\left(\lambda_{1}-\lambda_{2}\right)$ is
A. $n \lambda$
B. $(n-1) \lambda$
C. $(n+2) \lambda$
D. $(n+1) \lambda$

## Answer: B

## - Watch Video Solution

144. If sum of the mth powers of first n odd numbers is $\lambda, A a m>1$, then
(A) $\lambda<n^{m}$
(B) $\lambda>n^{m}$ (C) $\lambda<n^{m+1}$
(D) $\lambda>n^{m+1}$
A. $\lambda<n^{m}$
B. $\lambda>n^{m}$
C. $\lambda<n^{m+1}$
D. $\lambda>n^{m+1}$

## Answer: D

145. A squence of positive terms $A_{1}, A_{2}, A_{3}, \ldots ., A_{n}$ satisfirs the relation $A_{n+1}=\frac{3\left(1+A_{n}\right)}{\left(3+A_{n}\right)}$. Least integeral value of $A_{1}$ for which the sequence is decreasing can be

## - Watch Video Solution

146. When the ninth term of an AP is divided by its second term we get 5 as the quotient, when the thirteenth term ia devided ny sixth term the quotient is 2 and the remainderis 5 , then the seonnd term is

## - Watch Video Solution

147. Match the following Column I to Column II

## Column I

| (A) | If $a_{1}, a_{2}, a_{3}, \ldots$ are in AP and $a_{1}+a_{6}+a_{10}+a_{21}$ <br> $+a_{25}+a_{30}=120$, then $\sum_{i=1}^{30} a_{i}$ is | Column II |
| :--- | :--- | :---: | :---: |
| (B) | If $a_{1}, a_{2}, a_{3}, \ldots$ are in AP and $a_{1}+a_{5}+a_{9}$ <br> $+a_{13}+a_{17}+a_{21}+a_{25}=112$, then $\sum_{i=1}^{25} a_{i}$ is | 400 |
| (C) | If $a_{1}, a_{2}, a_{3}, \ldots$ are in AP and <br> $a_{1}+a_{4}+a_{7}+a_{10}+a_{13}$ <br> $+a_{16}=375$, then $\sum_{i=1}^{16} a_{i}$ is | 600 |

## D Watch Video Solution

148. Match the following Column I to Column II

| Column I |  | Column II |  |
| :---: | :---: | :---: | :---: |
| (A) | If $a>0, b>0, c>0$ and the minimum value of $a\left(b^{2}+c^{2}\right)+b\left(c^{2}+a^{2}\right)+c\left(a^{2}+b^{2}\right)$ is $\lambda a b c$, then $\lambda$ is | (p) | 2 |
| (B) | If $a, b, c$ are positive, $a+b+c=1$ and the minimum value of $\left(\frac{1}{a}-1\right)\left(\frac{1}{b}-1\right)\left(\frac{1}{c}-1\right)$ is $\lambda$, then $\lambda$ is | (q) | 4 |
| (C) | If $a>0, b>0, c>0, s=a+b+c$ and the minimum value of $\frac{2 s}{s-a}+\frac{2 s}{s-b}+\frac{2 s}{s-c}$ is $(\lambda-1)$, then $\lambda$ is | (r) | 6 |
| (D) | If $a>0, b>0, c>0, a, b, c$ are in GP and the the minimum value of $\left(\frac{a}{b}\right)^{\lambda}+\left(\frac{c}{b}\right)^{\lambda}$ is 2 , hen $\lambda$ is | (s) | 8 |
|  |  | (t) | 10 |

## - Watch Video Solution

149. Statement 1 The sum of first $n$ terms of the series $1^{2}-2^{2}+3^{2}-4^{2}-5^{2}-\ldots .$. can be $= \pm \frac{n(n+1)}{2}$. Statement 2 Sum of first n narural numbers is $\frac{n(n+1)}{2}$
A. Statement 1 is true, Statement 2 is true, Statement 2 is a corrct explanation for Statement 1.
B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1.
C. Statement 1 is true, Statement 2 is false.
D. Statement 1 is false, Statement 2 is true.

## Answer: A

## - Watch Video Solution

150. Statement 1 If $a, b, c$ are three positive numbers in GP, then $\left(\frac{a+b+c}{3}\right)\left(\frac{3 a b c}{a b+b c+c a}\right)=(a b c)^{\frac{2}{3}}$.
Statement $2(A M)(H M)=(G M)^{2}$ is true for positive numbers.
A. Statement 1 is true, Statement 2 is true, Statement 2 is a corrct explanation for Statement 1.
B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1.
C. Statement 1 is true, Statement 2 is false.
D. Statement 1 is false, Statement 2 is true.

## Answer: C

## - Watch Video Solution

151. Consider an AP with a as the first term and $d$ is the common difference such that $S_{n}$ denotes the sum to n terms and $a_{n}$ denotes the nth term of the AP. Given that for some $\mathrm{m}, n \in N, \frac{S_{m}}{S_{n}}=\frac{m^{2}}{n^{2}}(\neq n)$.
Statement $1 d=2 a$ because
Statement $2 \frac{a_{m}}{a_{n}}=\frac{2 m+1}{2 n+1}$.
A. Statement 1 is true, Statement 2 is true, Statement 2 is a corrct explanation for Statement 1.
B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1.
C. Statement 1 is true, Statement 2 is false.
D. Statement 1 is false, Statement 2 is true.

## Answer: C

## - Watch Video Solution

152. Statement $11,2,4,8, \ldots$ is a $G P, 4,8,16,32, \ldots$ is a GP and $1+4,2+8,4+16,8+32, \ldots$ is also a GP. Statement 2 Let general term of a GP with common ratio $r$ be $T_{k+1}$ and general term of another GP with common ratio r be $T^{\prime}{ }_{k+1}$, then the series whode general term $T^{\prime \prime}{ }_{k+1}=T_{k+1}+T^{\prime}{ }_{k+1}$ is also a GP woth common ratio r .
A. Statement 1 is true, Statement 2 is true, Statement 2 is a corrct explanation for Statement 1.
B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1.
C. Statement 1 is true, Statement 2 is false.
D. Statement 1 is false, Statement 2 is true.

## Answer: A

## D Watch Video Solution

153. In a set of four numbers, the first three are in G.P. and the last three are in A.P. with difference 6. If the first number is the same as the fourth, find the four numbers.

## D Watch Video Solution

154. Find the natural number $a$ for which $\sum_{k=1}^{n} f(a+k)=16\left(2^{n}-1\right)$, where the function $f$ satisfies the relation $f(x+y)=f(x) f(y)$ for all natural number $x$, yand, further,$f(1)=2$.

## (D) Watch Video Solution

155. If n is a root of $x^{2}(1-a c)-x\left(a^{2}+c^{2}\right)-(1+a c)=0$ and if n harmonic means are inserted between $a$ and $c$, find the difference between the first and the last means.

## - Watch Video Solution

156. A number consists of three digits which are in GP the sum of the right hand and left hand digits exceeds twice the middle digits by 1 and the sum of the left hand and middle digits is two thirds of the sum of the middle and right hand digits. Find the number.

## - Watch Video Solution

157. $S=\sum_{i=1}^{n} \sum_{j=1}^{i} \sum_{k=1}^{j} 1$
158. Three numbers are in G.P. whose sum is 70 . If the extremes be each multiplied by 4 and the means by 5 , they will be in A.P. Find the numbers.

## D Watch Video Solution

159. If the sum of $m$ terms of an A.P. is equal to the sum of either the next $n$ terms or the next $p$ terms, then prove that $(m+n)\left(\frac{1}{m}-\frac{1}{p}\right)=(m+p)\left(\frac{1}{m}-\frac{1}{n}\right)$.

## ( Watch Video Solution

160. Find the sum of all possible products of the first $n$ natural numbers taken two by two.

## - Watch Video Solution

161. $l_{n}=\int_{0}^{\frac{\pi}{4}} \tan ^{n} x d x \quad$ show that
$l_{6}, \frac{1}{l_{5}+l_{7}}, \ldots$ from an AP. Find its common difference.

## - Watch Video Solution

162. If the sum of the terms of an infinitely decreasing GP is equal to the greatest value of the fuction $f(x)=x^{3}+3 x-9$ on the iterval $[-5,3]$ and the difference between the first and second terms is $f^{\prime}(0)$, then show that the common ratio of the progression is $\frac{2}{3}$.

## - Watch Video Solution

163. Find the relation between $x$ and $y$ : $\log _{10} x+\frac{1}{2} \log _{10} x+\frac{1}{4} \log _{10} x+\ldots=y$
164. If $0<x<\frac{\pi}{2} \exp \left[\left(\sin ^{2} x+\sin ^{4} x+\sin ^{6} x+{ }^{\prime} \ldots .+\infty\right) \log _{e} 2\right]$ satisfies the quadratic equation $x^{2}-9 x+8=0$, find the value of $\frac{\sin x-\cos x}{\sin x+\cos x}$.

## - Watch Video Solution

165. The natural numbers arearranged innthe form given below


The rth group containing $2^{r-1}$ numbers. Prove that sum of the numbers in the $n$th group is $2^{n-2}\left[2^{n}+2^{n-1}-1\right]$.

## - Watch Video Solution

166. If $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are in HP , then prove that $\frac{a+b}{2 a-b}+\frac{c+b}{2 c-b}>4$.
167. Find the sum to $n$ terms of the series
$\frac{1}{1+1^{2}+1^{4}}+\frac{2}{1+2^{2}+2^{4}}+\frac{3}{1+3^{2}+3^{4}}+\ldots$.

## - Watch Video Solution

168. The value of $x y z$ is 55 or $\frac{343}{55}$ according as the series $a, x, y, z, b$ is an AP or HP. Find the values of $a$ and $b$ given that they are positive integers.

## - Watch Video Solution

169. Find the sum of first $n$ terms of the series $1^{3}+3 \times 2^{2}+3^{3}+3 \times 4^{2}+5^{3}+3 \times 6^{2}+$ when $n$ is even $n$ is odd

## D Watch Video Solution

170. Find out the largest term of the sequence $\frac{1}{503}, \frac{4}{524}, \frac{9}{581}, \frac{16}{692}, \ldots$.

## - Watch Video Solution

171. IF $f(r)=1+\frac{1}{2}+\frac{1}{3}+\ldots .+\frac{1}{r} \quad$ and $\quad f(0)=0$, find $\sum_{r=1}^{n}(2 r+1) f(r)$.

## - Watch Video Solution

172. If the equation $x^{4}-4 x^{3}+a x^{2}+b x+1=0$ has four positive roots, find the values of $a$ and $b$.

## - Watch Video Solution

173. Evaluate $\sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \frac{m^{2} n}{3^{m}\left(n \cdot 3^{m}+m \cdot 3^{n}\right)}$.

## - Watch Video Solution

174. The value of $\sum_{i=0}^{\infty} \sum_{j=0}^{\infty} \sum_{k=0}^{\infty} \frac{1}{3^{i} 3^{j} 3^{k}}$ is

## - Watch Video Solution

175. Let $S_{n}, n=1,2,3, \ldots$ be the sum of infinite geometric series, whose first term is n and the common ratio is $\frac{1}{n+1}$. Evaluate $\lim _{n \rightarrow \infty} \frac{S_{1} S_{n}+S_{2} S_{n-1}+S_{3} S_{n-2}+\ldots+S_{n} S_{1}}{S_{1}^{2}+S_{2}^{2}+\ldots \ldots+S_{n}^{2}}$.

## - Watch Video Solution

176. The $n$th term of a series is given by $t_{n}=\frac{n^{5}+n^{3}}{n^{4}+n^{2}+1}$ and if sum of
its n terms can be expressed as $S_{n}=a_{n}^{2}+a+\frac{1}{b_{n}^{2}+b}$ where $a_{n}$ and $b_{n}$ are the nth terms of some arithmetic progressions and a, b are some constants, prove that $\frac{b_{n}}{a_{n}}$ is a costant.

## - Watch Video Solution

1. First term of a sequence is 1 and the $(n+1)$ th term is obtained by adding $(n+1)$ to the nth term for all natural numbers n , the 6th term of the sequence is
A. 7
B. 13
C. 21
D. 27

## Answer: C

## - Watch Video Solution

2. The first three terms of a sequence are $3,3,6$ and each term after the sum of two terms preceding it, then the 8 th term of the sequence
A. 15
B. 24
C. 39
D. 63

## Answer: D

## - Watch Video Solution

3. If $a_{n}=\sin \left(\frac{n \pi}{6}\right)$ then the value of $\sum a_{n}^{2}$
A. 2
B. 3
C. 4
D. 7

## Answer: B

4. If for a sequence $\left\{a_{n}\right\}, S_{n}=2 n^{2}+9 n$, where $S_{n}$ is the sum of n terms, the value of $a_{20}$ is
A. 65
B. 75
C. 87
D. 97

## Answer: C

## - Watch Video Solution

5. If $a_{1}=2$ and $a_{n}=2 a_{n-1}+5$ for $n>1$, the value of $\sum_{r=2}^{5} a_{r}$ is
A. 130
B. 160
C. 190

## Answer: C

## - Watch Video Solution

## Exercise For Session 2

1. If $n$th term of the series $25+29+33+37 \ldots .$. and $3+4+6+9+13+\ldots \ldots .$. are equal, then $n$ equal
A. 11
B. 12
C. 13
D. 14

## Answer: B

2. The 15 th term of the series $2 \frac{1}{2}+1 \frac{7}{13}+1 \frac{1}{9}+\frac{20}{23}+\ldots$ is
A. $\frac{20}{5 r+3}$
B. $\frac{20}{5 r-3}$
C. $20(5 r+3)$
D. $\frac{20}{5 r^{2}+3}$

## Answer: A

## - Watch Video Solution

3. In a certain A.P., 5 times the 5 th term is equal to 8 times the 8 th terms then find its 13th term.
A. 0
B. -1
C. -12
D. -13

## Watch Video Solution

4. If the 9th term of an AP is zero, then prove that its 29th term is twice its 19th term.
A. 1: 2
B. 2:1
C. 1:3
D. 3:1

## Answer: B

## - Watch Video Solution

5. about to only mathematics
A. 1
B. -1
C. 0
D. $\frac{1}{2}$

## Answer: C

## - Watch Video Solution

6. The 6 th term of an $A P$ is equal to 2 , the value of the common difference of the $A P$ which makes the product $a_{1} a_{4} a_{5}$ least is given by
A. $\frac{8}{5}$
B. $\frac{5}{4}$
C. $\frac{2}{3}$
D. $\frac{1}{3}$

## Answer: C

7. The sum of first $2 n$ terms of an $A P$ is $\alpha$. and the sum of next $n$ terms is $\beta$, its common difference is
A. $\frac{\alpha-2 \beta}{3 n^{2}}$
B. $\frac{2 \beta-\alpha}{3 n^{2}}$
C. $\frac{\alpha-2 \beta}{3 n}$
D. $\frac{2 \beta-\alpha}{3 n}$

## Answer: B

## - Watch Video Solution

8. The sum of three numbers in AP is -3 and their product is 8 , then sum of squares of the numbers is
B. 10
C. 12
D. 21
9. Let $S_{n}$ denote the sum of first n terms of an AP and $3 S_{n}=S_{2 n}$ What is $S_{3 n}: S_{n}$ equal to?
A. (a) 9
B. (b) 6
C. (c) 16
D. (d) 12
10. Find the sum of the products of the ten numbers $\pm 1, \pm 2, \pm 3, \pm 4$, and $\pm 5$ taking two at a time.
A. -65
B. 165
C. -55
D. 95

## - Watch Video Solution

11. If $a_{1}, a_{2}, a_{3}, \ldots, a_{n}$ are in AP, where $a_{i}>0$ for all I, the value of
$\frac{1}{\sqrt{a}_{1}+\sqrt{a}_{2}}+\frac{1}{\sqrt{a_{2}}+\sqrt{a}_{3}}+\ldots \ldots+\frac{1}{\sqrt{a}_{n-1}+\sqrt{a}_{n}}$ is
A. $\frac{1}{\sqrt{a}_{1}+\sqrt{a}_{n}}$
B. $\frac{1}{\sqrt{a}_{1}-\sqrt{a_{n}}}$
C. $\frac{n}{\sqrt{a}_{1}-\sqrt{a}_{n}}$
D. $\frac{n-1}{\sqrt{a}_{1}+\sqrt{a_{n}}}$

## - Watch Video Solution

## Exercise For Session 3

1. The fourth, seventh, and the last term of a G.P. are 10,80 , and 2560 , respectively. Find the first term and the number of terms in G.P.
A. $\frac{4}{5}, 12$
B. $\frac{4}{5}, 10$
C. $\frac{5}{4}, 12$
D. $\frac{5}{4}, 10$

## Answer: B

## - Watch Video Solution

2. If the first and the $n^{\text {th }}$ term of a GP are a and b , respectively, and if P is the product of n terms, prove that $P^{2}=(a b)^{n}$.
A. $a b$
B. $(a b)^{\frac{n}{2}}$
C. $(a b)^{n}$
D. None of these

## Answer: C

## - Watch Video Solution

3. If $a_{1}, a_{2}, a_{3}\left(a_{1}>0\right)$ are three successive terms of a GP with common ratio $r$, the value of $r$ for which $a_{3}>4 a_{2}-3 a_{1}$ holds is given by
A. $1<r<3$
B. $-3<r<-1$
C. $r<1$ or $r>3$
D. None of these

## Answer: B

## - Watch Video Solution

4. If $x, 2 x+2$ and $3 x+3$ are the first three terms of a G.P., then the fourth term is a. 27 b. -27 c. 13.5 d. -13.5
A. 27
B. -27
C. 13.5
D. -13.5

## Answer: C

5. In a sequence of 21 terms the first 11 terms are in A.P. with common difference 2. and the last 11 terms are in G.P. with common ratio 2 . If the middle tem of the A.P. is equal to the middle term of the G.P., then the middle term of the entire sequence is
A. $-\frac{10}{31}$
B. $\frac{10}{31}$
C. $-\frac{32}{31}$
D. $\frac{32}{31}$

## Answer: D

## - Watch Video Solution

6. Three distinct numbers $x, y, z$ form a GP in that order and the numbers
$7 x+5 y, 7 y+5 z, 7 z+5 x$ form an AP in that order. The common ratio of GP is
A. -4
B. -2
C. 10
D. 18
7. Prove that the sum to $n$ terms of the series $11+103+1005+\ldots$. Is (10/9) $\left(10^{n}-1\right)+n^{2}$.
A. $\frac{1}{9}\left(10^{n}-1\right)+n^{2}$
B. $\frac{1}{9}\left(10^{n}-1\right)+2 n$
C. $\frac{10}{9}\left(10^{n}-1\right)+n^{2}$
D. $\frac{10}{9}\left(10^{n}-1\right)+2 n$
8. In a G.P the sum of the first and last terms is 66 , the product of the second and the last but one is 128 , and the sum of the terms is 126 If the decresing G.P is considered, then the sum of infinite terms is
A. 6
B. 8
C. 10
D. 12

## - Watch Video Solution

9. If $S_{1}, S_{2}, S_{3}$ be respectively the sum of $\mathrm{n}, 2 \mathrm{n}$ and 3 n terms of a GP, then $\frac{S_{1}\left(S_{3}-S_{2}\right)}{\left(S_{2}-S_{1}\right)^{2}}$ is equal to
A. (a) 1
B. (b) 2
C. (c) 3
D. (d) 4

## - Watch Video Solution

10. If $|a|<1|b|<1$ and $|x|<1$ then the solution of $\sin ^{-1}\left(\frac{2 a}{1+a^{2}}\right)-\cos ^{-1}\left(\frac{1-b^{2}}{1+b^{2}}\right)=\tan ^{-1}\left(\frac{2 x}{1-x^{2}}\right)$ is
A. $\frac{a-b}{1-a b}$
B. $\frac{a-b}{1+a b}$
C. $\frac{a b-1}{1+a b}$
D. none of these
11. If the sides of a triangle are in GP and its largest angle is twice tha smallset then the common ratio $r$ satisfies the inequality
A. $0<r<\sqrt{2}$
B. $1<r<\sqrt{2}$
C. $1<r<2$
D. $r>\sqrt{2}$

## - Watch Video Solution

12. If $a x^{3}+b x^{2}+c x+d$ is divisible by $a x^{2}+c$, thena, $b, c, d$ are in a.
A.P. b. G.P. c. H.P. d. none of these
A. AP
B. GP
C. HP
D. None of these

## D Watch Video Solution

13. If $(r)_{n}$, denotes the number $r r r \ldots$ (ndigits), where $r=1,2,3, \ldots, 9$ and $a=(6)_{n}, b=(8)_{n}, c=(4)_{2 n}$, then
A. $a^{2}+b+c=0$
B. $a^{2}+b-c=0$
C. $a^{2}+b 2 c=0$
D. $a^{2}+b-9 c=0$

## - Watch Video Solution

14. $0.4 \overline{27}$ represents the rational number
A. $\frac{47}{99}$
B. $\frac{47}{110}$
C. $\frac{47}{999}$
D. $\frac{49}{99}$
15. If the product of three numbers in GP be 216 and their sum is 19 , then the numbers are
A. $4,6,9$
B. $4,7,8$
C. $3,7,9$
D. None of these

## Exercise For Session 4

1. If $a, b, c$ are in AP and $b, c, d$ be in HP, then
A. $a b=c d$
B. $a d=b c$
C. $a c=b d$
D. $a b c d=1$

## Answer: C

## - Watch Video Solution

2. If a,b,c are in AP, then $\frac{a}{b c}, \frac{1}{c}, \frac{1}{b}$ are in
A. AP
B. GP
C. HP
D. None of these

## Answer: C

## - Watch Video Solution

3. about to only mathematics
A. AP
B. GP
C. HP
D. None of these

## Answer: C

4. If $x, 1, z$ are in AP and $x, 2, z$ are in GP, then $x, 4, z$ will be in
A. AP
B. GP
C. HP
D. None of these

## Answer: D

## - Watch Video Solution

5. If $a, b, c$ are in G.P. and $a-b, c-a, a n d b-c$ are in H.P., then prove that $a+4 b+c$ is equal to 0 .
A. 0
B. 1
C. -1
D. None of these

## D Watch Video Solution

6. If the $(m+1) t h,(n+1) t h$, $a n d(r+1)$ th terms of an A.P., are in G.P. and $m, n, r$ are in H.P., then find the value of the ratio of the common difference to the first term of the A.P.
A. $-\frac{2}{n}$
B. $\frac{2}{n}$
C. $-\frac{n}{2}$
D. $\frac{n}{2}$

## Answer: A

7. If $a, b, c$ are in AP and $a^{2}, b^{2}, c^{2}$ are in HP, then
A. $a=b=c$
B. $2 b=3 a+c$
C. $b^{2}=\sqrt{\frac{a c}{8}}$
D. None of these
8. If $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are in HP., then $\frac{a}{b+c}, \frac{b}{c+a}, \frac{c}{a+b}$ are in
A. AP
B. GP
C. HP
D. None of these
9. If $\frac{x+y}{2}, y, \frac{y+z}{2}$ are in HP, then $\mathrm{x}, \mathrm{y}, \mathrm{z}$ are in
A. AP
B. GP
C. HP
D. None of these

## - Watch Video Solution

10. if $\frac{a+b}{1-a b}, b, \frac{b+c}{1-b c}$ are in $A P$ then $a, \frac{1}{b}, c$ are in
A. AP
B. GP
C. HP
D. None of these

## Exercise For Session 5

1. If the arithmetic means of two positive number a and $\mathrm{b}(a>b)$ is twice their geometric mean, then find the ratio $a: b$
A. $2+\sqrt{3}: 2-\sqrt{3}$
B. $7+4 \sqrt{3}: 7-4 \sqrt{3}$
C. $2: 7+4 \sqrt{3}$
D. $2: \sqrt{3}$

## Answer: C

## - Watch Video Solution

2. Let $\alpha$ and $\beta$ be two positive real numbers. Suppose $A_{1}, A_{2}$ are two arithmetic means; $G_{1}, G_{2}$ are tow geometrie means and $H_{1} H_{2}$ are two
harmonic means between $\alpha$ and $\beta$, then
A. $A_{1} H_{2}$
B. $A_{2} H_{1}$
C. $G_{1} G_{2}$
D. None of these

## Answer: A

## - Watch Video Solution

3. The geometric mean between -9 and -16 is $12 \mathrm{~b} .-12 \mathrm{c}$. -13 d . none of these
A. 12
B. -12
C. -13
D. None of these

## - Watch Video Solution

4. Let $n \in N, n>25$. Let $A, G, H$ deonote te arithmetic mean, geometric man, and harmonic mean of 25 and $n$. The least value of $n$ for which $A, G, H \in\{25,26, n\}$ is a. 49 b. 81 c. 169 d .225
A. 49
B. 81
C. 169
D. 225

## Answer: C

5. If nine arithmetic means and nine harmonic means are inserted between 2 and 3 alternatively, then prove that $A+6 / H=5$ (where $A$ is any of the A.M.'s and $H$ the corresponding H.M.).
A. 8
B. 9
C. 10
D. None of these

## Answer: B

## - Watch Video Solution

6. If $H_{1}$. , $H_{2}, \ldots, H_{20}$ are 20 harmonic means between 2 and 3 , then $\frac{H_{1}+2}{H_{1}-2}+\frac{H_{20}+3}{H_{20}-3}=$
A. $n$
B. $n+1$
C. 2 n
D. $2 n-2$

## Answer: B

## - Watch Video Solution

7. The A.M. of two given positive numbers is 2 . If the larger number is increased by 1, the G.M. of the numbers becomes equal to the A.M. of the given numbers. Then find the H.M.
A. $\frac{3}{2}$
B. $\frac{2}{3}$
C. $\frac{1}{2}$
D. 2

## Answer: B

8. If $a, a_{1}, a_{2}, a_{3}, a_{2 n}, b$ are in A.P. and $a, g_{1}, g_{2}, g_{3},, g_{2 n}, b$. are in G.P. and $h \quad \mathrm{~s}$ the H.M. of aandb, then prove that $\frac{a_{1}+a_{2 n}}{g_{1} g_{2 n}}+\frac{a_{2}+a_{2 n-1}}{g_{1} g_{2 n-1}}++\frac{a_{n}+a_{n+1}}{g_{n} g_{n+1}}=\frac{2 n}{h}$
A. $\frac{2 n}{h}$
B. 2 nh
C. nh
D. $\frac{n}{h}$

## Answer: B

## - Watch Video Solution

## Exercise For Session 6

1. Sum of the first $n$ terms of the series $\frac{1}{2}+\frac{3}{4}+\frac{7}{8}+\frac{15}{16}+$ is equals to (a). $2^{n}-n-1$ (b). $1-2^{-n}$ (c). $n+2^{-n}-1$ (d). $2^{n}+1$
A. $2^{n}-n-1$
B. $1-2^{-n}$
C. $n+26(-n)-1$
D. $26(n)-1$

## Answer: B

## D Watch Video Solution

2. about to only mathematics
A. 1
B. $\frac{3}{2}$
C. 2
D. $\frac{5}{2}$

## Answer: D

3. Sum to n terms the series $1+3+7+15+31+\ldots$
A. $2^{n+1}-n$
B. $2^{n+1}-n-2$
C. $2^{n}-n-2$
D. None of these

## Answer: B

## - Watch Video Solution

4. $99^{\text {th }}$ term of the series $2+7+14+23 \ldots$
A. 9998
B. 9999
C. 10000
D. 100000

## Answer: C

## - Watch Video Solution

5. Find the sum of $n$ terms of the series $1.2 .3+2.3 .4+3.4 .5+$
A. $n(n+1)(n+2)$
B. $(n+1)(n+2)(n+3)$
C. $\frac{1}{4} n(n+1)(n+2)(n+3)$
D. $\frac{1}{4}(n+1)(n+2)(n+3)$

Answer: A

- Watch Video Solution

6. Find the sum of $n$ terms of the series:

$$
\frac{1}{1.2}+\frac{1}{2.3}+\frac{1}{3.4}++\frac{1}{n n+1}
$$

A. $\frac{1}{n(n+1)}$
B. $\frac{n}{n+1}$
C. $\frac{2 n}{n+1}$
D. $\frac{2}{n(n+1)}$

## Answer: B

7. Sum of the $n$ terms of the series

$$
\frac{3}{1^{2}}+\frac{5}{1^{2}+2^{2}}+\frac{7}{1^{2}+2^{2}+3^{3}}+\ldots \ldots . \text { is }
$$

A. $\frac{2 n}{n+1}$
B. $\frac{4 n}{n+1}$
C. $\frac{6 n}{n+1}$
D. $\frac{9 n}{n+1}$

## Answer: A

## - Watch Video Solution

8. If $t_{n}=\frac{1}{4}(n+2)(n+3) f$ or $n=1,2,3,, \quad$ then
$\frac{1}{t_{1}}+\frac{1}{t_{2}}+\frac{1}{t_{3}}++\frac{1}{t_{2003}}=\frac{4006}{3006}$ b. $\frac{3006}{3007}$ c. $\frac{4006}{3008}$ d. $\frac{4006}{3009}$
A. $\frac{4006}{3006}$
B. $\frac{4003}{3007}$
C. $\frac{4006}{3008}$
D. $\frac{4006}{3009}$

Answer: C

## - Watch Video Solution

9. 

value

$$
\frac{1}{(1+a)(2+a)}+\frac{1}{(2+a)(3+a)}+\frac{1}{(3+a)(4+a)} \ldots \ldots . . \text { upto } \infty \text { is }
$$

(where, a is constant)
A. A. $\frac{1}{1+a}$
B. B. $\frac{2}{1+a}$
C. C. $\infty$
D. D. None of these

## Answer: B

## Watch Video Solution

10. If $f$ is a function satisfying $f(x+y)=f(x) \times f(y)$ for all $x, y \in N$ such that $f(1)=3$ and $\sum_{x=1}^{n} f(x)=120$, find the value of $n$.
A. 4
B. 5
C. 6
D. None of these

## Answer: C

## - Watch Video Solution

## Exercise For Session 7

1. The minimum value of $4^{x}+4^{2-x}, x \in R$ is
A. 0
B. 2
C. 4
D. 8

Answer: A
2. If $0<\theta<\pi$, then the minmum value of $\sin ^{3} \theta+\cos e c^{3} \theta+2$ is
A. 0
B. 2
C. 4
D. 8

## Answer: C

## - Watch Video Solution

3. If $a, b, c$ and $d$ are four real numbers of the same sign, then the value of $\frac{a}{b}+\frac{b}{c}+\frac{c}{d}+\frac{d}{a}$ lies in the interval
A. $[2, \infty)$
B. $[3, \infty)$
C. $(4, \infty)$
D. $[4, \infty)$

## Answer: B

## - Watch Video Solution

4. If $0<x<\frac{\pi}{2}$, then the minimum value of $2(\sin x+\cos x+\operatorname{cosec} 2 x)^{3}$ is
A. (a) 27
B. (b) 13.5
C. (c) 6.75
D. (d) 0

Answer: D

## - Watch Video Solution

5. If $a+b+c=3$ and $a>0, b>0, c>0$ then the greatest value of $a^{2} b^{3} c^{2}$ is
A. $\frac{3^{4} \cdot 2^{10}}{7^{7}}$
B. $\frac{3^{10} \cdot 2^{4}}{7^{7}}$
C. $\frac{3^{2} \cdot 2^{12}}{7^{7}}$
D. $\frac{3^{12} \cdot 2^{2}}{7^{7}}$

## Answer: C

## ( Watch Video Solution

6. If $x+y+z=a$ and the minimum value of $\frac{a}{x}+\frac{a}{y}+\frac{a}{z}$ is $81^{\lambda}$, then the value of.$\lambda$ is
A. $\frac{1}{2}$
B. 1
C. $\frac{1}{4}$

## D. 2

## Answer: C

## - Watch Video Solution

7. If $x, y, z$ be three positive numbers such that $x y z^{2}$ has the greatest value $\frac{1}{64}$, then the value of $\frac{1}{x}+\frac{1}{y}+\frac{1}{z}$ is
A. $a=b=\frac{1}{2}, c=\frac{1}{4}$
B. $a=b=c=\frac{1}{3}$
C. $a=b=\frac{1}{4}, c=\frac{1}{2}$
D. $a=b=c=\frac{1}{4}$

## Answer: A

## - Watch Video Solution

1. If the number $\mathrm{x}, \mathrm{y}, \mathrm{z}$ are in H.P. , then $\frac{\sqrt{y z}}{\sqrt{y}+\sqrt{z}}, \frac{\sqrt{x z}}{\sqrt{x}+\sqrt{z}}, \frac{\sqrt{x y}}{\sqrt{x}+\sqrt{y}}$ are in
A. AP
B. GP
C. HP
D. None of these

## Answer: A

## D Watch Video Solution

2. If $a_{1}, a_{2}, \ldots .$, are in HP and $f_{k}=\sum_{r=1}^{n} a_{r}-a_{k}$, then $2^{\alpha_{1}}, 2^{\alpha_{2}}, 2^{\alpha_{3}} 2^{\alpha_{4}}, \ldots$. are in $\left\{\right.$ where $\left.\alpha_{1}=\frac{a_{1}}{f_{1}}, \alpha_{2}=\frac{a_{2}}{f_{2}}, \alpha_{3}=\frac{a_{3}}{f_{3}}, \ldots.\right\}$.
B. GP
C. HP
D. None of these

## Answer: D

## - Watch Video Solution

3. ABC is a right-angled triangle in which $\angle B=90^{\circ}$ and $B C=a$. If n points $L_{1}, L_{2}, \ldots, L_{n}$ on AB is divided in $\mathrm{n}+1$ equal parts and $L_{1} M_{1}, L_{2} M_{2}, \ldots, L_{n} M_{n}$ are line segments parallel to BC and $M_{1}, M_{2}, \ldots, M_{n}$ are on AC, then the sum of the lengths of $L_{1} M_{1}, L_{2} M_{2}, \ldots, L_{n} M_{n}$ is
A. $\frac{n(n+1)}{(2)}$
B. $\frac{a(n-1)}{2}$
C. $\frac{a n}{2}$
D. Impossible to find from the given data

## - Watch Video Solution

4. Let $S_{n}$ denotes the sum of the terms of n series $(1 \leq n \leq 9)$
$1+22+333+\ldots . .999999999$, is
A. $S_{n}-S_{n-1}=\frac{1}{9}\left(10^{n}-n^{2}+n\right)$
B. $S_{n}=\frac{1}{9}\left(10^{n}-n^{2}+2 n-2\right)$
C. $9\left(S_{n}-S_{n-1}\right)=n\left(10^{n}-1\right)$
D. None of these

## Answer: C

## - Watch Video Solution

5. If $a, b, c$ are in GP, show that the equations $a x^{2}+2 b x+c=0$ and $d x^{2}+2 e x+f=0$ have a common root if $\frac{a}{d}, \frac{b}{e}, \frac{c}{f}$ are in HP
A. AP
B. GP
C. HP
D. None of these

## Answer: A

## - Watch Video Solution

6. Sum of the first $n$ terms of the series $\frac{1}{2}+\frac{3}{4}+\frac{7}{8}+\frac{15}{16}+$
equals to (a). $2^{n}-n-1$ (b). $1-2^{-n}$ (c). $n+2^{-n}-1$ (d). $2^{n}+1$
A. $2^{n}-n-1$
B. $1-2^{-n}$
C. $n+2^{-n}-1$
D. $2^{n}-1$

## Answer: C

7. If in a triangle $P Q R ; \sin P, \sin Q, \sin R$ are in A.P; then (A)the altitudes are in AP (B)the altitudes are in HP (C)the altitudes are in GP (D)the medians are in AP
A. the altitudes are in AP
B. the altitudes are in HP
C. the medians are in GP
D. the medians are in AP

## Answer: B

## - Watch Video Solution

8. Let $a_{1}, a_{2}, a_{10}$ be in A.P. and $h_{1}, h_{2}, h_{10}$ be in H.P. If $a_{1}=h_{1}=2 a n d a_{10}=h_{10}=3$, thena $_{4} h_{7}$ is 2 b. 3 c. 5 d. 6
A. 2
B. 3
C. 5
D. 6

## Answer: D

## - Watch Video Solution

9. If $I_{n}=\int_{0}^{\pi} \frac{1-\sin 2 n x}{1-\cos 2 x} d x$ then $I_{1}, I_{2}, I_{3}, \ldots$. are in
A. AP
B. GP
C. HP
D. None of these

## Answer: A

10. Show that If $a(b-c) x^{2}+b(c-a) x y+c(a-b) y^{2}=0$ is a perfect square, then the quantities $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are in harmonic progresiion
A. AP
B. GP
C. HP
D. None of these

## Answer: C

## - Watch Video Solution

11. The sum to infinity of the series
$1+2\left(1-\frac{1}{n}\right)+3\left(1-\frac{1}{n}\right)^{2}+\ldots \ldots$, is (A) $n^{2} \quad$ (B) $n(n+1)$
$n\left(1+\frac{1}{n}\right)^{2}$ (D) None of these
A. $n^{2}$
B. $n(n+1)$
C. $n\left(1+\frac{1}{n}\right)^{2}$
D. None of these

## Answer: A

## D Watch Video Solution

12. If $\log _{3} 2, \log _{3}\left(2^{x}-5\right)$ and $\log _{3}\left(2^{x}-\frac{7}{2}\right)$ are in A.P., then x is equal to
A. 2
B. 3
C. 4
D. 2,3

## Answer: B

13. If $x, y, z$ be three positive prime numbers. The progression in which $\sqrt{x}, \sqrt{y}, \sqrt{z}$ can be three terms (not necessarily consecutive) is
A. AP
B. GP
C. HP
D. None of these

## Answer: D

## - Watch Video Solution

14. If n is an odd integer greater than or equal to 1 , then the value of $n^{3}-(n-1)^{3}+(n-1)^{3}-(n-1)^{3}+\ldots .+(-1)^{n-1} 1^{3}$
A. $\frac{(n+1)^{2}(2 n-1)}{4}$
B. $\frac{(n-1)^{2}(2 n-1)}{4}$
C. $\frac{(n+1)^{2}(2 n+1)}{4}$
D. None of these

## Answer: A

## - Watch Video Solution

15. If the sides of a right angled triangle are in A.P then the sines of the acute angles are
A. $\frac{3}{5}, \frac{4}{5}$
B. $\sqrt{3}, \frac{1}{3}$
C. $\sqrt{\frac{\sqrt{5}-1}{2}}, \sqrt{\frac{\sqrt{5}+1}{2}}$
D. $\frac{\sqrt{3}}{2}, \frac{1}{2}$

## Answer: A

16. The 6 th term of an $A P$ is equal to 2 , the value of the common difference of the $A P$ which makes the product $a_{1} a_{4} a_{5}$ least is given by
A. $\frac{8}{5}$
B. $\frac{5}{4}$
C. $\frac{2}{3}$
D. None of these

## Answer: C

## - Watch Video Solution

17. If the arithmetic progression whose common difference is nonzero the sum of first $3 n$ terms is equal to the sum of next $n$ terms. Then, find the ratio of the sum of the $2 n$ terms to the sum of next $2 n$ terms.
A. $\frac{1}{5}$
B. $\frac{2}{3}$
C. $\frac{3}{4}$
D. None of these

## Answer: A

## - Watch Video Solution

18. The coefficient of $x^{n}$ in the expansion of $(1+x)(1-x)^{n}$ is
A. $\frac{n\left(n^{2}+2\right)(3 n+1)}{24}$
B. $\frac{n\left(n^{2}-1\right)(3 n+2)}{24}$
C. $\frac{n\left(n^{2}+1\right)(3 n+4)}{24}$
D. None of these

## Answer: B

## - Watch Video Solution

19. Consider the pattern shown below:
Row 11

Row | 2 | 3 | 5 |
| :--- | :--- | :--- | :--- |

$\begin{array}{lllllll}\text { Row } & 3 & 7 & 9 & 11 & e t c .\end{array}$
$\begin{array}{llllll}\text { Row } & 4 & 13 & 15 & 17 & 19\end{array}$
The number at the end of row 60 is
A. 3659
B. 3519
C. 3681
D. 3731

## Answer: A

Watch Video Solution
20. Let $a_{n}$ be the nth term of an AP, if $\sum_{r=1}^{100} a_{2 r}=\alpha$ and $\sum_{r=1}^{100} a_{2 r-1}=\beta$,
then the common difference of the AP is

$$
\text { A. (a) } \alpha-\beta
$$

B. (b) $\beta-\alpha$
C. (c) $\frac{\alpha-\beta}{2}$
D. (d) None of these

## Answer: D

## - Watch Video Solution

21. If $a_{1}, a_{2}, a_{3}, a_{4}, a_{5}$ are in HP, then $a_{1} a_{2}+a_{2} a_{3}+a_{3} a_{4}+a_{4} a_{5}$ is equal to
A. $2 a_{1} a_{5}$
B. $3 a_{1} a_{5}$
C. $4 a_{1} a_{5}$
D. $6 a_{1} a_{5}$

## Answer: C

22. If $a, b, c$ and $d$ are four positive real numbers such that $a b c d=1$, what is the minimum value of $(1+a)(1+b)(1+c)(1+d)$.
A. 1
B. 4
C. 16
D. 64

## Answer: C

## - Watch Video Solution

23. If $a, b, c$ are in AP and $(a+2 b-c)(2 b+c-a)(c+a-b)=\lambda a b c$, then $\lambda$ is
A. 1
B. 2
C. 4
D. None of these

## Answer: C

## - Watch Video Solution

24. If $a_{1}, a_{2}, a_{3} \ldots$. are in GP with first term a and common ratio r , then
$\frac{a_{1} a_{2}}{a_{1}^{2}-a_{2}^{2}}+\frac{a_{2} a_{3}}{a_{2}^{2}-a_{3}^{2}}+\frac{a_{3} a_{4}}{a_{3}^{2}-a_{4}^{2}}+\ldots .+\frac{a_{n-1} a_{n}}{a_{n-1}^{2}-a_{n}^{2}}$ is equal to
A. $\frac{n r}{1-r^{2}}$
B. $\frac{(n-1) r}{1-r^{2}}$
C. $\frac{n r}{1-r}$
D. $\frac{(n-1) r}{1-r}$

## Answer: B

25. If the sum of first 10 terms of an A.P. is 4 times the sum of its first 5 terms, then find the ratio of first term and common difference.
A. $\frac{1}{2}$
B. 2
C. $\frac{1}{4}$
D. 4

## Answer: A

## - Watch Video Solution

26. If $\cos (x-y), \cos x$ and $\cos (x+y)$ are in H.P., then $\cos x \sec \left(\frac{y}{2}\right)$ is
A. $\pm \sqrt{2}$
B. $\frac{1}{\sqrt{2}}$
C. $-\frac{1}{\sqrt{2}}$
D. None of these

## - Watch Video Solution

27. If eleven A.M. s are inserted between 28 and 10 , then find the number of integral A.M. s.
A. 5
B. 6
C. 7
D. 8

## Answer: A

## - Watch Video Solution

28. If $x>1, y>1$, andz>1 are in G.P., then $\frac{1}{1+\ln x}, \frac{1}{1+\ln y}$ and $\frac{1}{1+\ln z}$ are in a. $A \dot{P}$. b. $H \dot{P} \cdot$ c. $G \dot{P}$. d. none of
these
A. AP
B. GP
C. HP
D. None of these

## Answer: C

## - Watch Video Solution

29. The minimum value of $\frac{\left(a^{2}+3 a+1\right)\left(b^{2}+3 b+1\right)\left(c^{2}+3 c+1\right)}{a b c}$ The minimum value of, where $a, b, c \in R^{+}$is
A. $\frac{11^{3}}{2^{3}}$
B. 125
C. 25
D. 27

## Answer: B

## - Watch Video Solution

30. Let $a_{1}, a_{2}, \ldots$ be in AP and $q_{1}, q_{2}, \ldots$ be in GP. If $a_{1}=q_{1}=2$ and $a_{10}=q_{10}=3$, then
A. $a_{7} q_{19}$ is not an integer
B. $a_{19} q_{7}$ is an integer
C. $a_{7} q_{19}=a_{19} q_{10}$
D. None of these

## Answer: C

## D Watch Video Solution

Exercise (More Than One Correct Option Type Questions)

1. For a positive integer $n$ let

$$
\begin{aligned}
& a(n)=1+\frac{1}{2}+\frac{1}{3}+\frac{1}{4}+\ldots .+\frac{1}{\left(2^{n}\right)-1} . \text { Then } a(100) \leq 100 \mathrm{~b} . \\
& a(100)>100 \text { c. } a(200) \leq 100 \text { d. } a(200) \leq 100
\end{aligned}
$$

A. $a(100)<100$
B. $a(100)>100$
C. $a(200)>100$
D. $a(200)<100$

## Answer: A:C

## - Watch Video Solution

2. The corresponding first and the (2n-1)th terms of an A.P a G.P and a H.P are equal ,If their nth terms are $a, b$ and $c$, respectively, then
A. $a=b=c$
B. $a \geq b \geq c$
C. $a+c=b$
D. $a c-b^{2}=0$

## Answer: B::D

## - Watch Video Solution

3. If $0<\theta<\frac{\pi}{2}, x=\sum_{n=0}^{\infty} \cos ^{2 n} \theta, y=\sum_{n=0}^{\infty} \sin ^{2 n} \theta \quad$ and
$z=\sum_{n=0}^{\infty} \cos ^{2 n} \theta \cdot \sin ^{2 n} \theta$, then show $x y z=x y+z$.
A. $x y z=x z+y$
B. $x y z=x y+z$
C. $x y z=x+y+z$
D. $x y z=y z+x$

## Answer: B::C

4. If $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are in A.P. and $a^{2}, b^{2}, c^{2}$ are in H.P. then which of the following could and true (A) $-\frac{a}{2}, b$, care $\in G . P$. (B) $a=b=c$ (C) $a^{3}, b^{3}, c^{3}$ are in G.P. (D) none of these
A. $-\frac{a}{2}, b, c$ are in GP
B. $a=b=c$
C. $a^{2}, b^{2}, c^{2}$ are in GP
D. None of these

## Answer: A::B

## - Watch Video Solution

5. The next term of the G.P. $x, x^{2}+2, a n d x^{3}+10$ is $\frac{729}{16}$ b. 6 c. 0 d. 54
A. 0
B. 6
C. $\frac{729}{16}$
D. 54

## Answer: C::D

## - Watch Video Solution

6. Consecutive odd integers whose sum is $25^{2}-11^{2}$ are
A. $n=14$
B. $n=16$
C. first odd number is 23
D. last odd number is 49

## Answer: A::C::D

## - Watch Video Solution

7. The geometric mean $G$ of two positive numbers is 6 . Their arithmetic mean $A$ and harmonic mean $H$ satisfy the equation $90 A+5 H=918$, then $A$ may be equal to:
A. (A) $\frac{5}{2}$
B. (B) 10
C. (C) 5
D. (D) $\frac{1}{5}$

## Answer: A: D

## - Watch Video Solution

8. If the sum to $n$ terms of the series $\frac{1}{1 \cdot 3 \cdot 5 \cdot 7}+\frac{1}{3 \cdot 5 \cdot 7 \cdot 9}+\frac{1}{5 \cdot 7 \cdot 9 \cdot 11}+\ldots \ldots$. is $\frac{1}{90}-\frac{\lambda}{f(n)}$, then find $f(0), f(1)$ and $f(\lambda)$

$$
\text { A. } f(0)=15
$$

B. $f(1)=105$
C. $f(\lambda)=\frac{640}{27}$
D. $\lambda=\frac{1}{3}$

## Answer: A::B::C

## - Watch Video Solution


A. 7 th term is 16
B. 7 th term is 18
C. sum of first 10 terms is $\frac{505}{4}$
D. sum of first 10 terms is $\frac{405}{4}$

## - Watch Video Solution

10. Let $E=\frac{1}{1^{2}}+\frac{1}{2^{2}}+\frac{1}{3^{2}}+$ Then, $E<3$ b. $E>3 / 2$ c. $E>2$ d. $E<2$
A. $E<3$
B. $E>\frac{3}{2}$
C. $E<2$
D. $E>2$

## Answer: B::C

## - Watch Video Solution

11. Let $S_{n}(n \leq 1)$ be a sequence of sets defined by
$S_{1}\{0\}, S_{2}=\left\{\frac{3}{2}, \frac{5}{2}\right\}, S_{3}=\left\{\frac{15}{4}, \frac{19}{4}, \frac{23}{4}, \frac{27}{4}\right\}, \ldots \ldots$. then
A. (a)third element in $S_{20}$ is $\frac{439}{20}$
B. (b)third element in $S_{20}$ is $\frac{431}{20}$
C. (c)sum of the element in $S_{20}$ is 589
D. (d)sum of the element in $S_{20}$ is 609

## Answer: A:C

## - Watch Video Solution

12. Which of the following sequences are unbounded?
A. $\left(1+\frac{1}{n}\right)^{n}$
B. $\left(\frac{2 n+1}{n+2}\right)$
C. $\left(1+\frac{1}{n}\right)^{n^{2}}$
D. $\tan n$

## Answer: C::D

13. Let a sequence $\left\{a_{n}\right\}$ be defined by
$a_{n}=\frac{1}{n+1}+\frac{1}{n+2}+\frac{1}{n+3}+\ldots .+\frac{1}{3 n}$. Then:
A. (a) $a_{2}=\frac{11}{12}$
B. (b) $a_{2}=\frac{19}{20}$
C. (c) $a_{n+1}-a_{n}=\frac{(9 n+5)}{(3 n+1)(3 n+2)(3 n+3)}$
D. (d) $a_{n+1}-a_{n}=\frac{-2}{3(n+1)}$

## Answer: B::C

Watch Video Solution
14. Find $\frac{d y}{d x}$ if $y+\sin y=\cos x$

## - Watch Video Solution

15. All the terms of an AP are natural numbers and the sum of the first 20 terms is greater than 1072 and Iss than 1162. If the sixth term is 32 , then
A. first term is 7
B. first term is 12
C. common difference is 4
D. common difference is 5

## Answer: A: D

## - Watch Video Solution

## Exercise (Passage Based Questions)

1. $S_{n}$ be the sum of n terms of the series $\frac{8}{5}+\frac{16}{65}+\frac{24}{325}+\ldots \ldots$.

The value of $\lim _{n \rightarrow \infty} S_{n}$ is (a)0 (b) $\frac{1}{2}$ (c)2 (d)4
A. 0
B. $\frac{1}{2}$
C. 2
D. 4

## Answer: C

## - Watch Video Solution

2. $S_{n}$ be the sum of n terms of the series $\frac{8}{5}+\frac{16}{65}+\frac{24}{325}+\ldots \ldots$ The seveth term of the series is (a) $\frac{56}{2505}$ (b) $\frac{56}{6505}$ (c) $\frac{56}{5185}$ (d) $\frac{107}{9605}$
A. $\frac{56}{2505}$
B. $\frac{56}{6505}$
C. $\frac{56}{5185}$
D. $\frac{107}{9605}$

## Answer: D

3. $S_{n}$ be the sum of $n$ terms of the series $\frac{8}{5}+\frac{16}{65}+\frac{24}{325}+\ldots \ldots$. The value of $S_{8}$, is (a) $\frac{288}{145}$ (b) $\frac{1088}{545}$ (c) $\frac{81}{41}$ (d) $\frac{107}{245}$
A. $\frac{288}{145}$
B. $\frac{1088}{545}$
C. $\frac{81}{41}$
D. $\frac{107}{245}$

## Answer: A

## - Watch Video Solution

4. Two consecutive numbers from $1,2,3 \ldots, \mathrm{n}$ are removed .The arithmetic mean of the remaining numbers is 105/4

The sum of all numbers
A. $(41,51)$
B. $(52,62)$
C. $(63,73)$
D. $(74,84)$

## Answer: A

## - Watch Video Solution

5. Two consecutive numbers from $1,2,3$...., n are removed .The arithmetic mean of the remaining numbers is 105/4

The sum of all numbers
A. are less than 10
B. lies between 10 to 30
C. lies between 30 to 70
D. greater than 70

## Answer: A

6. Two consecutive numbers from $1,2,3 \ldots, \mathrm{n}$ are removed .The arithmetic mean of the remaining numbers is 105/4

The sum of all numbers
A. less than 1000
B. lies between 1200 to 1500
C. greater than 1500
D. None of these

## Answer: B

## - Watch Video Solution

7. There are two sets $A$ and $B$ each of which consists of three numbers in AP whose sum is 15 and where D and d are the common differences such that $D=1+d, d>0$. If $\mathrm{p}=7(\mathrm{q}-\mathrm{p})^{\prime}$, where p and q are the product of the
nymbers respectively in the two series.
The value of $p$ is
A. 105
B. 140
C. 175
D. 210

## Answer: A

## - Watch Video Solution

8. There are two sets $A$ and $B$ each of which consists of three numbers in AP whose sum is 15 and where D and d are the common differences such that $D=1+d, d>0$. If $p=7(q-p)$, where p and q are the product of the nymbers respectively in the two series.

The value of $q$ is
A. 200
B. 160
C. 120
D. 80

## Answer: C

## D Watch Video Solution

9. There are two sets $A$ and $B$ each of which consists of three numbers in AP whose sum is 15 and where $D$ and $d$ are the common differences such that $D=1+d, d>0$. If $p=7(q-p)$, where p and q are the product of the nymbers respectively in the two series.

The value of $7 D+8 d$ is
A. 37
B. 22
C. 67
D. 52

## - Watch Video Solution

10. There are two sets $A$ and $B$ each of which consists of three numbers in GP whose product is 64 and $R$ and $r$ are the common ratios such that $R=r+2$. If $\frac{p}{q}=\frac{3}{2}$, where p and q are sum of numbers taken two at a time respectively in the two sets.

The value of $p$ is
A. 66
B. 72
C. 78
D. 84

## Answer: D

11. There are two sets $A$ and $B$ each of which consists of three numbers in GP whose product is 64 and R and r are the common ratios sich that $R=r+2$. If $\frac{p}{q}=\frac{3}{2}$, where p and q are sum of numbers taken two at a time respectively in the two sets.

The value of $q$ is
A. 54
B. 56
C. 58
D. 60

## Answer: B

## - Watch Video Solution

12. There are two sets $A$ and $B$ each of which consists of three numbers in GP whose product is 64 and R and r are the common ratios sich that $R=r+2$. If $\frac{p}{q}=\frac{3}{2}$, where p and q are sum of numbers taken two at a
time respectively in the two sets.
The value of $r^{R}+R^{r}$ is
A. 5392
B. 368
C. 32
D. 4

## Answer: C

## - Watch Video Solution

13. The numbers $1,3,6,10,15,21,28 \ldots$ are called triangular numbers. Let $t_{n}$ denote the $n^{t h}$ triangular number such that $t_{n}=t_{n-1}+n, \forall n \geq 2$. The value of $t_{50}$ is:
A. (a) 1075
B. (b) 1175
C. (c) 1275
D. (d) 1375

## Answer: C

## - Watch Video Solution

14. The numbers $1,3,6,10,15,21,28 \ldots$ are called triangular numbers. Let
$t_{n}$ denote the $n^{t h}$ triangular number such that $t_{n}=t_{n-1}+n, \forall n \geq 2$. The number of positive integers lying between $t_{100}$ and $t_{101}$ are:
A. (a) 99
B. (b) 100
C. (c) 101
D. (d) 102

## Answer: B

## D Watch Video Solution

15. The numbers $1,3,6,10,15,21,28 \ldots$ are called triangular numbers. Let $t_{n}$ denote the $n^{\text {th }}$ triangular number such that $t_{n}=t_{n-1}+n, \forall n \geq 2$. If $(m+1)$ is the $n^{\text {th }}$ triangular number, then $(n-m)$ is
A. (a) $1+\sqrt{\left(m^{2}+2 m\right)}$
B. (b) $1+\sqrt{\left(m^{2}+2\right)}$
C. (c) $1+\sqrt{\left(m^{2}+m\right)}$
D. (d) None of these

## Answer: D

## - Watch Video Solution

16. Let $A_{1}, A_{2}, A_{3}, \ldots \ldots . A_{m}$ be arithmetic means between -3 and 828 and $G_{1}, G_{2}, G_{3}, \ldots \ldots . G_{n}$ be geometric means between 1 and 2187. Produmt of geometrimc means is $3^{35}$ and sum of arithmetic means is 14025.

The valjue of $n$ is
A. 45
B. 30
C. 25
D. 10

## Answer: D

## D Watch Video Solution

17. Let $A_{1}, A_{2}, A_{3}, \ldots \ldots . A_{m}$ be arithmetic means between -3 and 828 and $G_{1}, G_{2}, G_{3}, \ldots \ldots . G_{n}$ be geometric means between 1 and 2187. Produmt of geometrimc means is $3^{35}$ and sum of arithmetic means is 14025.

The value of $m$ is
A. 17
B. 34
C. 51

## D. 68

## Answer: B

## - Watch Video Solution

18. Let $A_{1}, A_{2}, A_{3}, \ldots \ldots . A_{m}$ be arithmetic means between -3 and 828 and $G_{1}, G_{2}, G_{3}, \ldots \ldots . G_{n}$ be geometric means between 1 and 2187. Produmt of geometrimc means is $3^{35}$ and sum of arithmetic means is 14025.

The value of $m$ is
A. 2044
B. 1022
C. 511
D. None of these

## Answer: D

19. Suppose $\alpha, \beta$ are roots of $a x^{2}+b x+c=0$ and $\gamma, \delta$ are roots of $A x^{2}+B x+C=0$.

If $\alpha, \beta, \gamma, \delta$ are in AP, then common difference of AP is
A. $\frac{1}{4}\left(\frac{b}{a}-\frac{B}{A}\right)$
B. $\frac{1}{3}\left(\frac{b}{a}-\frac{B}{A}\right)$
C. $\frac{1}{2}\left(\frac{c}{a}-\frac{B}{A}\right)$
D. $\frac{1}{3}\left(\frac{c}{a}-\frac{C}{A}\right)$

## Answer: A

## - Watch Video Solution

20. Suppose $\alpha, \beta$ are roots of $a x^{2}+b x+c=0$ and $\gamma, \delta$ are roots of $A x^{2}+B x+C=0$. If $a, b, c$ are in GP as well as $\alpha, \beta, \gamma, \delta$, then $A, B, C$ are in:
A. (a) AP only
B. (b) GP only
C. (c) AP and GP
D. (d) None of these

## Answer: B

## ( Watch Video Solution

21. Suppose $\alpha, \beta$ are roots of $a x^{2}+b x+c=0$ and $\gamma, \delta$ are roots of $A x^{2}+B x+C=0$.

If $\alpha, \beta, \gamma, \delta$ are in GP, then common ratio of GP is
A. $\sqrt{\left(\frac{b A}{a B}\right)}$
B. $\sqrt{\left(\frac{a B}{b A}\right)}$
C. $\sqrt{\left(\frac{b C}{c B}\right)}$
D. $\sqrt{\left(\frac{c B}{b C}\right)}$

## Answer: B

## - Watch Video Solution

22. Suppose p is the first of $n(n>1)$ arithmetic means between two positive numbers $a$ and $b$ and $q$ the first of $n$ harmonic means between the same two numbers.

The value of $p$ is
A. $\frac{n a+b}{n+1}$
B. $\frac{n b+a}{n+1}$
C. $\frac{n a-b}{n+1}$
D. $\frac{n b-a}{n+1}$

## Answer: A

## D Watch Video Solution

23. Suppose p is the first of $n(n>1)$ arithmetic means between two positive numbers a and b and q the first of n harmonic means between the same two numbers.

The value of $q$ is
A. $\frac{(n-1) a b}{n b+a}$
B. $\frac{(n+1) a b}{n b+a}$
C. $\frac{(n-1) a b}{n a+b}$
D. $\frac{(n-1) a b}{n a+b}$

## Answer: B

## - Watch Video Solution

24. about to only mathematics
A. q lies between p and $\left(\frac{n+1}{n-1}\right)^{2} p$
B. q lies between p and $\left(\frac{n+1}{n-1}\right) p$
C. q does not lie between p and $\left(\frac{n+1}{n-1}\right)^{2} p$
D. q does not lie between p and $\left(\frac{n+1}{n-1}\right) p$

## Answer: C

## - Watch Video Solution

## Exercise (Single Integer Answer Type Questions)

1. Let $a, b, c, d$ be positive real numbers with $a<b<c<d$. Given that $a, b, c, d$ are the first four terms of an AP and $a, b, d$ are in GP. The value of $\frac{a d}{b c}$ is $\frac{p}{q}$, where $p$ and $q$ are prime numbers, then the value of $q$ is

## - Watch Video Solution

2. If the coefficient of x in the expansion of $\prod_{r=1}^{110}(1+r x)$ is $\lambda(1+10)\left(1+10+10^{2}\right)$, then the value of $\lambda$ is

## - Watch Video Solution

3. A 3 digit palindrome is a 3 digit number (not starting with zero) which reads the same backwards as forwards For example, 242. The sum of all even 3 digit palindromes is $2^{n_{1}} \cdot 3^{n_{2}} \cdot 5^{n_{3}} \cdot 7^{n_{4}} \cdot 11^{n_{5}}$. value of $n_{1}+n_{2}+n_{3}+n_{4}+n_{5}$ is

## - Watch Video Solution

4. If $n$ is $a$ positive integer satisfying the equation $2+\left(6 \cdot 2^{2}-4 \cdot 2\right)+\left(6 \cdot 3^{2}-4 \cdot 3\right)+\ldots \ldots .+\left(6 \cdot n^{2}-4 \cdot n\right)=140$ then the value of $n$ is

## - Watch Video Solution

5. Let $S(x)=1+x-x^{2}-x^{3}+x^{4}+x^{5}-x^{6}-x^{7}+\ldots \ldots . .+\infty$, where $0<x<1$. If $S(x)=\frac{\sqrt{2}+1}{2}$, then the value of $(x+1)^{2}$ is
6. The sequence $a_{1}, a_{2}, a_{3}, \ldots \ldots$, is a geometric sequence with common ratio $r$. The sequence $b_{1}, b_{2}, b_{3}, \ldots \ldots$, is also a geometric sequence. If $b_{1}=1, b_{2}=\sqrt[4]{7}-\sqrt[4]{28}+1, a_{1}=\sqrt[4]{28}$ and $\sum_{n=1}^{\infty} \frac{1}{a_{n}}=\sum_{n=1}^{\infty}\left(b_{n}\right)$, then the value of $\left(1+r^{2}+r^{4}\right)$ is

## - Watch Video Solution

7. Let $\left(a_{1}, b_{1}\right)$ and $\left(a_{2}, b_{2}\right)$ are the pair of real numbers such that $10, \mathrm{a}, \mathrm{b}, \mathrm{ab}$ constitute an arithmetic progression. Then, the value of $\left(\frac{2 a_{1} a_{2}+b_{1} b_{2}}{10}\right)$ is

## D Watch Video Solution

8. If one root of $A x^{3}+B x^{2}+C x+D=0, D \neq 0$ is the arithmetic mean of the other two roots, then the relation $2 B^{3}+\lambda A B C+\mu A^{2} D=0$ holds good. Then, the value of $2 \lambda+\mu$ is
9. If $|x|>1$,then sum of the series
$\frac{1}{1+x}+\frac{2}{1+x^{2}}+\frac{2^{2}}{1+x^{4}}+\frac{2^{3}}{1+x^{8}}+\ldots \ldots$ upto terms $\infty$ is
$\frac{1}{x-\lambda}$,then the value of $\lambda$ is

## - Watch Video Solution

10. Three non-zero real numbers form a AP and the squares of these numbers taken in same order form a GP. If the possible common ratios are $(3 \pm \sqrt{k})$ where $k \in N$, then the value of $\left[\frac{k}{8}-\frac{8}{k}\right]$ is (where [] denotes the greatest integer function).

## - Watch Video Solution

Exercise (Matching Type Questions)

1. Match the following Column I to Column II

| Column I |  | Column II |  |
| :--- | :--- | :--- | :--- |
| (A) | $a, b, c, d$ are in AP, then | (p) | $a+d>b+c$ |
| (B) | $a, b, c, d$ are in GP, then | (q) | $a d>b c$ |
| (C) | $a, b, c, d$ are in HP, then | (r) | $\frac{1}{a}+\frac{1}{d}>\frac{1}{b}+\frac{1}{c}$ |
|  |  | $(\mathrm{~s})$ | $a d<b c$ |

Column I

| (A) | For an AP $a_{1}, a_{2}, a_{3}, \ldots, a_{n}, \ldots ;$ <br> $a_{1}=\frac{5}{2} ; a_{10}=16$. If $a_{1}+a_{2}$ <br> $+\ldots+a_{n}=110$, then ' $n$ ' equals | (p) | 9 |
| :---: | :--- | :---: | :---: |
| (B) | The interior angles of a convex <br> non-equiangular polygon of 9 sides <br> are in AP. The least positive integer <br> that limits the upper value of the <br> common difference between the <br> measures of the angles in degrees is | (q) | 10 |
| (C) | For an increasing GP, <br> $a_{1}, a_{2}, a_{3}, \ldots, a_{n}, \ldots ;$ <br> $a_{6}=4 a_{4} ; a_{9}-a_{7}=192$, <br> if $a_{4}+a_{5}+a_{6}+\ldots+a_{n}=1016$, then <br> $n$ equals | (r) | 11 |
|  | (s) | 12 |  |

## D View Text Solution

3. Match the following Column I to Column II

## Column I

| (B) | If $a_{1}, a_{2}, a_{3}, \ldots$ are in AP and <br> $a_{1}+a_{5}+a_{10}+a_{15}+a_{20}+a_{24}$ <br> $=195$, <br> $\alpha=a_{2}+a_{7}+a_{18}+a_{23}$ and <br> $\beta=2\left(a_{3}+a_{22}\right)-\left(a_{8}+a_{17}\right)$, <br> then |  |  |
| :--- | :--- | :--- | :--- |
| (C) | If $a_{1}, a_{2}, a_{3}, \ldots$ are in AP and <br> $a_{1}+a_{7}+a_{10}+a_{21}+$ <br> $a_{24}+a_{30}=225$, <br> $\alpha=a_{2}+a_{7}+a_{24}+a_{29}$ and <br> $\beta=2\left(a_{10}+a_{21}\right)-\left(a_{3}+a_{28}\right)$, <br> then | (r) | $\alpha+2 \beta=260$ |
|  |  | (s) | $\alpha-\beta \beta=220$ |
|  | (t) | $\alpha+\beta=15 \mu, \mu \in I$ |  |

## ( Watch Video Solution

## Matching Type Questions

| Column I |  | Column II |  |
| :--- | :--- | :--- | :---: |
| (A) | If $a_{1}, a_{2}, a_{3}, \ldots$ are in AP and <br> $a_{1}+a_{4}+a_{7}+a_{14}+a_{17}+$ <br> $a_{20}=165$, <br> $\alpha=a_{2}+a_{6}+a_{15}+a_{19}$ and <br> $\beta=2\left(a_{9}+a_{12}\right)-\left(a_{3}+a_{18}\right)$, <br> then | (p) | $\alpha=2 \beta$ |

1. 

| Column I |  | Column II |  |
| :--- | :--- | :---: | :---: |
| (A) | If $4 a^{2}+9 b^{2}+16 c^{2}$ <br> $=2(3 a b+6 b c+4 c a)$, where $a, b, c$ <br> are non-zero numbers, then $a, b, c$ are <br> in | (p) | AP |
| (B) | If $17 a^{2}+13 b^{2}+5 c^{2}$ <br> $=(3 a b+15 b c+5 c a)$, where <br> $a, b, c$ are non-zero numbers, then <br> $a, b, c$ are in | (q) | GP |
| (C) | If $a^{2}+9 b^{2}+25 c^{2}$ <br> $=a b c\left(\frac{15}{a}+\frac{5}{b}+\frac{3}{c}\right)$, where $a, b, c$ are <br> non-zero numbers, then $a, b, c$ are in | (r) | HP |
| (D) | If $\left(a^{2}+b^{2}+c^{2}\right) p^{2}-2 p(a b+b c+c a)$ <br> $+\left(a^{2}+b^{2}+c^{2}\right) \leq 0$, where $a, b, c, p$ <br> are non-zero numbers, then $a, b, c$ are <br> in |  |  |

## - View Text Solution

1. Statement $14,8,16$, are in GP and $12,16,24$ are in HP.

Statement 2 If middle term is added in three consecutive terms of a GP, resultant will be in HP.
A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1
B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1
C. Statement 1 is true, Statement 2 is false
D. Statement 1 is false, Statement 2 is true

## Answer: A

## D Watch Video Solution

2. Satement 1 If the $n$th termn of a series is $2 n^{3}+3 n^{2}-4$, then the second order differences must be an AP.

Statement 2 If $n$th term of a series is a polynomial of degree $m$, then $m$ th order differences of series are constant.
A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1
B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1
C. Statement 1 is true, Statement 2 is false
D. Statement 1 is false, Statement 2 is true

## Answer: A

## - Watch Video Solution

3. Statement 1 The sum of the products of numbers $\pm a_{1}, \pm a_{2}, \pm a_{3}, \ldots . \pm a_{n}$ taken two at a time is $-\sum_{i=1}^{n} a_{i}^{2}$.

Statement 2 The sum of products of numbers $a_{1}, a_{2}, a_{3}, \ldots . . a_{n}$ taken two at a time is denoted by $\sum_{1 \leq i<j \leq n} \sum a_{i} a_{j}$.
A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1
B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1
C. Statement 1 is true, Statement 2 is false
D. Statement 1 is false, Statement 2 is true

## Answer: B

## D View Text Solution

4. Statement $1 a+b+c=18(a, b, c>0)$, then the maximum value of abc is 216 .

Statement 2 Maximum value occurs when $a=b=c$.
A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1
B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1
C. Statement 1 is true, Statement 2 is false
D. Statement 1 is false, Statement 2 is true

## Answer: A

## - Watch Video Solution

5. If $4 a^{2}+9 b^{2}+16 c^{2}=2(3 a b+6 b c+4 c a)$, where $a, b, c$ are non-zero real numbers, then $a, b, c$ are in GP.

Statement 2 If $\left(a_{1}-a_{2}\right)^{2}+\left(a_{2}-a_{3}\right)^{2}+\left(a_{3}-a_{1}\right)^{2}=0, \quad$ then $a_{1}=a_{2}=a_{3}, \forall a_{1}, a_{2}, a_{3} \in R$.
A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1
B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct
C. Statement 1 is true, Statement 2 is false
D. Statement 1 is false, Statement 2 is true

## Answer: D

## - Watch Video Solution

6. Statement 1 If a and b be two positive numbers, where $a>b$ and $4 \times G M=5 \times H M$ for the numbers. Then, $a=4 b$.

Statement $2(A M)(H M)=(G M)^{2}$ is true for positive numbers.
A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1
B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct
explanation for Statement 1
C. Statement 1 is true, Statement 2 is false
D. Statement 1 is false, Statement 2 is true

## Answer: C

## - Watch Video Solution

7. Statement 1 The difference between the sum of the first 100 even natural numbers and the sum of the first 100 odd natural numbers is 100 .

Statement 2 The difference between the sum opf the first n even natural numbers and sum of the first $n$ odd natural numbers is $n$.
A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1
B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1
C. Statement 1 is true, Statement 2 is false
D. Statement 1 is false, Statement 2 is true

## Answer: A

## Exercise (Subjective Type Questions)

1. The pth, $(2 p) t h$ and $(4 p) t h$ terms of an AP, are in GP, then find the common ratio of GP.

## - Watch Video Solution

2. Find the sum of $n$ terms of the series
$(a+b)+\left(a^{2}+a b+b^{2}\right)+\left(a^{3}+a^{2} b+a b^{2}+b^{3}\right)+\ldots \ldots . . \quad$ where $a \neq 1, b \neq 1$ and $a \neq b$.

## - Watch Video Solution

3. The sequence of odd natural numbers is divided into groups $1,3,5,7,9,11, \ldots$ and so on. Show that the sum of the numbers in $n t h$ group is $n^{3}$.
4. Let $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are respectively the sums of the first n terms, the next n terms and the next n terms of a GP. Show that $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are in GP.

## - Watch Video Solution

5. If the first four terms of an arithmetic sequence are $a, 2 a, b$ and $(a-6-b)$ for some numbers a and b , find the sum of the first 100 terms of the sequence.

## - Watch Video Solution

6. If $\frac{1}{1^{2}}+\frac{1}{2^{2}}+\frac{1}{3^{2}}+\ldots \infty=\frac{\pi^{2}}{6} \quad$ then value of
$1-\frac{1}{2^{2}}+\frac{1}{3^{2}}-\frac{1}{4^{2}}+\ldots \infty=$

## - Watch Video Solution

7. If the arithmetic mean of $a_{1}, a_{2}, a_{3}, \ldots \ldots . . a_{n}$ is a and $b_{1}, b_{2}, b_{3}, \ldots \ldots . b_{n}$ have the arithmetic mean b and $a_{i}+b_{i}=1$ for $i=1,2,3, \ldots \ldots n$, prove that $\sum_{i=1}^{n}\left(a_{i}-a\right)^{2}+\sum_{i=1}^{n} a_{i} b_{i}=n a b$.

## - Watch Video Solution

8. If $a_{1}, a_{2}, a_{3}, \ldots \ldots .$. is an arithmetic progression with common difference 1 and $a_{1}+a_{2}+a_{3}+\ldots+a_{98}=137$, then find the value of $a_{2}+a_{4}+a_{6}+\ldots+a_{98}$.

## - Watch Video Solution

9. If $t_{1}=1, t_{r}-t_{r-1}=2^{r-1}, r \geq 2$, find $\sum_{r=1}^{n} t_{r}$.

## - Watch Video Solution

10. Prove that $I_{1}, I_{2}, I_{3} \ldots$ form an AP, if

$$
I_{n}=\int_{0}^{\pi} \frac{\sin 2 n x}{\sin x} d x .
$$

## - Watch Video Solution

11. Consider the sequence $S=7+13+21+31+\ldots \ldots+T_{n}$, find the value of $T_{70}$.

## - Watch Video Solution

12. Find value of $\left(x+\frac{1}{x}\right)^{3}+\left(x^{2}+\frac{1}{x^{2}}\right)^{3}+\ldots \ldots . .+\left(x^{n}+\frac{1}{x^{n}}\right)^{3}$.

## - Watch Video Solution

13. If the sequence $a_{1}, a_{2}, a_{3}, \ldots \ldots a_{n}$, forms an A.P., then prove that $a_{1}^{2}-a_{2}^{2}+a_{3}^{2}-a_{4}^{2}+\ldots \ldots .+a_{2 n-1}^{2}-a_{2 n}^{2}=\frac{n}{2 n-1}\left(a_{1}^{2}-a_{2 n}^{2}\right)$

## - Watch Video Solution

14. If three unequel numbers are in HP and their squares are in AP, show that they are in the ratio $1+\sqrt{3}:-2: 1-\sqrt{3}$ or $1-\sqrt{3}:-2: 1+\sqrt{3}$.

## - Watch Video Solution

15. If $a_{1}, a_{2}, a_{3}, \ldots \ldots ., a_{n}$ are in AP with $a_{1}=0$, prove that $\frac{a_{3}}{a_{2}}+\frac{a_{4}}{a_{3}}+\ldots \ldots+\frac{a_{n}}{a_{n-1}}-a_{2}\left(\frac{1}{a_{2}}+\frac{1}{a_{3}}+\ldots \ldots . .+\frac{1}{a_{n-2}}\right)=\frac{a_{n-1}}{a_{2}}+\frac{}{a}$

## - Watch Video Solution

16. Balls are arranged in rows to form an equilateral triangle. The first row consists of one ball, the second row of two balls and so on. If 669 more balls are added,then all the balls can be arranged in the shape of a square and each of the sides, then contains 8 balls less than each side of the triangle. Determine the initial number of balls.
17. If $\theta_{1}, \theta_{2}, \theta_{2}, \theta_{3}, \ldots \ldots \ldots . \Theta_{n}$ are in AP whose common difference is d , show that
$\theta_{1} \sec \theta_{2}+\sec _{3}+\ldots+\sec \theta_{n-1} \sec \theta_{n}=\frac{\tan \theta_{n}-\tan \theta_{1}}{\sin d}$

## - Watch Video Solution

18. 

Show
that,
$\left(1+5^{-1}\right)\left(1+5^{-2}\right)\left(1+5^{-4}\right)\left(1+5^{-8}\right) \ldots . .\left(1+5^{-2 n}\right)=\frac{5}{4}\left(1-5^{-2(n+}\right.$

## - Watch Video Solution

19. Evaluate $S=\sum_{n=0}^{n} \frac{2^{n}}{\left(a^{2^{n}}+1\right)}($ where $a>1)$.

## - Watch Video Solution

20. Find the sum of the series : $\tan ^{-1}\left(\frac{1}{3}\right)+\tan ^{-1}\left(\frac{2}{9}\right)+\ldots .+\tan ^{-1}\left(\frac{2^{n-1}}{1+2^{2 n-1}}\right)+\ldots \ldots \infty$

## - Watch Video Solution

21. Find the sum to $n$ terms, whose $n t h$ term is $\tan [\alpha+(n-1) \beta] \tan (\alpha+n \beta)$.

## - Watch Video Solution

22. If $\sum_{r=1}^{n} t_{r}=\frac{n}{8}(n+1)(n+2)(n+3)$, then find $\sum_{r=1}^{n} \frac{1}{t_{r}}$.

## - Watch Video Solution

23. If $s_{1}, s_{2}, s_{3}$ denote the sum of n terms of 3 arithmetic series whose first terms are unity and their common difference are in H.P., Prove that $n=\frac{2 s_{3} s_{1}-s_{1} s_{2}-s_{2} s_{3}}{s_{1}-2 s_{2}+s_{3}}$

## (D) Watch Video Solution

24. Three friends whose ages form a G.P. divide a certain sum of money in proportion to their ages. If they do that three years later, when the youngest is half the age of the oldest, then he will receive 105 rupees more that the he gets now and the middle friends will get 15 rupees more that he gets now, then ages of the friends are

## - Watch Video Solution

## Exercise (Questions Asked In Previous 13 Years Exam)

1. 

Let
a,b,c
be
in
A.P.
and
$|a|<1,|b|<1|c|<1$. if $x=1+a+a^{2}+\ldots$ to $\infty, y=1+b+b^{2}$
, then $x, y, z$ are in
A. AP
B. GP
C. HP
D. None of these

## Answer: C

## - Watch Video Solution

2. about to only mathematics

## - Watch Video Solution

3. If $a_{1}, a_{2}, a_{3}$, be terms of an A.P. and $\frac{a_{1}+a_{2}+\ldots .+a_{p}}{a_{1}+a_{2}+\ldots .+a_{q}}=\frac{p^{2}}{q^{2}}, p \neq q$, then $\frac{a_{6}}{a_{21}}$ equals to (a).41/11 (b). $7 / 2$
(c). 2/7 (d). 11/41
A. $\frac{41}{11}$
B. $\frac{7}{2}$
C. $\frac{2}{7}$
D. $\frac{11}{41}$

## Answer: D

## - Watch Video Solution

4. If $a_{1}, a_{2}, a_{3}, \ldots . a_{n}$ are in H.P. and $a_{1} a_{2}+a_{2} a_{3}+a_{3} a_{4}+\ldots \ldots . . a_{n-1} a_{n}=k a_{1} a_{n}$, then $k$ is equal to
A. $n\left(a_{1}-a_{n}\right)$
B. $(n-1)\left(a_{1}-a_{n}\right)$
C. $n a_{1} a_{n}$
D. $(n-1) a_{1} a_{n}$

Answer: D
5. Let $V_{r}$ denotes the sum of the first r terms of an arithmetic progression whose first term is $r$ and the common difference is $(2 r-1)$. Let $T_{r}=V_{r+1}-V_{r}-2$ and $Q_{r}=T_{r+1}-T_{r}$ for $r=1,2, \ldots$. $T_{r}$ is always
A. $\frac{1}{12} n(n+1)\left(3 n^{2}-n+1\right)$
B. $\frac{1}{12} n(n+1)\left(3 n^{2}+n+2\right)$
C. $\frac{1}{2} n\left(2 n^{2}-n+1\right)$
D. $\frac{1}{3}\left(2 n^{3}-2 n+3\right)$

## Answer: B

## - Watch Video Solution

6. Let $V_{r}$ denote the sum of the first $r$ terms of an arithmetic progression (AP) whose first term is $r$ and the common difference is $(2 r-1)$. Let $T_{-} r=V_{-}(r+1)-V_{-} r-2$ and $Q_{-} r=T_{-}(r+1)-T_{-} r$ for $r=1,2 T_{-} r^{\prime}$ is always (A) an odd number (B) an even number (C) a prime number (D) a composite num,ber
A. an odd number
B. an even number
C. a prime number
D. a composite number

## Answer: D

## D Watch Video Solution

7. Let $V(r)$ denote the sum of the first $r$ terms of an arithmetic progression (AP) whose first term is $r$ and the common difference is $(2 r-1) \cdot \operatorname{Let} \mathrm{T}(\mathrm{r})=\mathrm{V}(\mathrm{r}+1)-\mathrm{V}(\mathrm{r})-2 \quad$ and $\quad \mathrm{Q}(\mathrm{r}) \quad=\mathrm{T}(\mathrm{r}+1)-\mathrm{T}(\mathrm{r}) \quad$ for $\quad \mathrm{r}=1,2$ Whicho $\neq$ ofthe follow $\in$ gisac or rectstatement $?(A) Q_{-} 1, \quad$ Q_2, Q_3.............,are $\in A . P$. withcommond $\Leftrightarrow$ erence5 $(B)$ Q_1, $\quad$ Q_2,

Q_3............., are $\in A . P$. withcommond $\Leftrightarrow$ erence6( $C$ Q_1, Q_2, Q_3............., are $\in A . P$. withcommond $\Leftrightarrow$ erence $11(D)$ Q_1=Q_2=Q_3`

$$
\text { A. } Q_{1}, Q_{2}, Q_{3}, \ldots . . \text { are in AP with common difference } 5
$$

B. $Q_{1}, Q_{2}, Q_{3}, \ldots$. are in AP with common differemce 6
C. $Q_{1}, Q_{2}, Q_{3}, \ldots$. are in AP with common difference 11
D. $Q_{1}=Q_{2}=Q_{3}=\ldots .$.

## Answer: B

## - Watch Video Solution

8. Let $A_{1}, G_{1}, H_{1}$ denote the arithmetic, geometric and harmonic means respectively, of two distinct positive numbers. For $n \geq 2$, let $A_{n-1}, G_{n-1}$ and $H_{n-1}$ has arithmetic,geometric and harmonic means as $A_{n}, G_{n}, H_{n}$ respectively.

Which of the following statement is correct?
A. $G_{1}>G_{2}>G_{3}>\ldots \ldots$.
B. $G_{1}<G_{2}<G_{3}<\ldots . .$.
C. $G_{1}=G_{2}=G_{3}=\ldots \ldots$.
D. $G_{1}<G_{3}<G_{5}<\ldots \ldots$. and $\mathrm{G}_{-}(2)$ gtG_(4)gtG_(6)gt.......

## D Watch Video Solution

9. Let $A_{1}, G_{1}, H_{1}$ denote the arithmetic, geometric and harmonic means respectively, of two distinct positive numbers. For $n>2$, let $A_{n-1}, G_{n-1}$ and $H_{n-1}$ has arithmetic, geometric and harmonic means as $A_{n}, G_{N}, H_{N}$, respectively.
A. $A_{1}>A_{2}>A_{3}>\ldots \ldots$.
B. $A_{1}<A_{2}<A_{3}<\ldots \ldots$.
C. $A_{1}>A_{3}>A_{5}>\ldots \ldots . \quad$ and $A_{2}<A_{4}<A_{6}<\ldots \ldots$.
D. $A_{1}<A_{3}<A_{5}<\ldots \ldots$. and $A_{2}>A_{4}>A_{6}>\ldots \ldots$.

## Answer: A

## - Watch Video Solution

10. Let $A_{1}, G_{1}, H_{1}$ denote the arithmetic, geometric and harmonic means respectively, of two distinct positive numbers. For $n \geq 2$, let $A_{n-1}, G_{n-1}$ and $H_{n-1}$ has arithmetic,geometric and harmonic means as $A_{n}, G_{n}, H_{n}$ respectively.

Which of the following statement is correct?
A. $H_{1}>H_{2}>H_{3}>\ldots \ldots$.
B. $H_{1}<H_{2}<H_{3}<\ldots \ldots$.
C. $H_{1}>H_{3}>H_{5}>\ldots \ldots$. and $H_{2}<H_{4}<H_{6}<\ldots \ldots$
D. $H_{1}<H_{3}<H_{5}<\ldots \ldots$ and $H_{2}>H_{4}>H_{6}>\ldots \ldots$

## Answer: B

## - Watch Video Solution

11. In a G.P of positive terms if any term is equal to the sum of the next two terms, then the common ratio of the G.P is
A. $\frac{1}{2}(1-\sqrt{5})$
B. $\frac{1}{2} \sqrt{5}$
C. $\sqrt{5}$
D. $\frac{1}{2}(\sqrt{5}-1)$

## Answer: D

## - Watch Video Solution

12. Suppose four distinct positive numbers $a_{1}, a_{2}, a_{3}, a_{4}$ are in G.P. Let $b_{1}=a_{1}+, a_{b}=b_{1}+a_{2}, b_{3}=b_{2}+a_{3}$ and $b_{4}=b_{3}+a_{4}$.

Statement -1: The numbers $b_{1}, b_{2}, b_{3}, b_{4}$ are neither in A.P. nor in G.P.
Statement -2: The numbers $b_{1}, b_{2}, b_{3}, b_{4}$ are in H.P.
A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1
B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct
C. Statement 1 is true, Statement 2 is false
D. Statement 1 is false, Statement 2 is true

## Answer: C

## - Watch Video Solution

13. The first two terms of a geometric progression add up to 12 . The sum of the third and the fourth terms is 48 . If the terms of the geometric progression are alternately positive and negative, then the first term is
A. -12
B. 12
C. 4
D. -4

## Answer: A

14. If the sum of first n terms of an A.P. is $\mathrm{cn}^{2}$ then the sum of squares of these n terms is
A. $\frac{n\left(4 n^{2}-1\right) c^{2}}{6}$
B. $\frac{n\left(4 n^{2}+1\right) c^{2}}{3}$
C. $\frac{n\left(4 n^{2}-1\right) c^{2}}{3}$
D. $\frac{n\left(4 n^{2}+1\right) c^{2}}{6}$

## Answer: C

## - Watch Video Solution

15. The sum to infinity of the series $1+\frac{2}{3}+\frac{6}{3^{2}}+\frac{14}{3^{4}}+\ldots i s$
A. 6
B. 2
C. 3

## D. 4

## Answer: C

## - Watch Video Solution

16. Let $S_{k}, k=1,2, \ldots .100$ denote the sum of the infinite geometric series whose first term is $\frac{k-1}{K!}$ and the common
ration is $\frac{1}{k}$ then the value of $\frac{(100)^{2}}{100!}+\sum_{k=1}^{100}\left|\left(k^{\wedge} 2-3 k+1\right) S_{-} k\right|$ is

## - Watch Video Solution

17. Let $a_{1}, a_{2}, a_{3}, a_{11}$ be real numbers satisfying
$a_{1}=15,27-2 a_{2}>0$ anda $a_{k}=2 a_{k-1}-a_{k-2} \quad$ for $\quad k=3,4,, 11$. If
$\frac{a 12+a 22+\ldots+a 112}{11}=90$, then the value of $\frac{a 1+a 2++a 11}{11}$ is equals to $\qquad$ .

## - Watch Video Solution

18. A person is to count 4500 currency notes. Let $a_{n}$ denote the number of notes he counts is the $n^{\text {th }}$ minute .If $a_{1}=a_{2}=\ldots . . . .=a_{10}=150$ and $a_{10}, a_{11} \ldots$, are in A.P with common difference -2 , then the time to count all notes
A. 34 min
B. 125 min
C. 135 min
D. 24 min

## Answer: A

## - Watch Video Solution

19. The minimum value of the sum of real numbers $a^{-5}, a^{-4}, 3 a^{-3}, 1, a^{8}$ and $a^{10}$ with $a>0$ is $\qquad$ .
20. A man saves ₹ 200 in each of the first three months of his servies.In each of the subsequent monts his saving increases by ₹ 40 more than the saving of immediately previous month.His total saving from the start of service will be ₹ 11040 after .
A. 19 months
B. 20 months
C. 21 months
D. 18 months

## Answer: C

## - Watch Video Solution

21. Let $a_{n}$ be the nth term of an AP, if $\sum_{r=1}^{100} a_{2 r}=\alpha$ and $\sum_{r=1}^{100} a_{2 r-1}=\beta$, then the common difference of the AP is
A. $\frac{\alpha-\beta}{200}$
B. $\alpha-\beta$
C. $\frac{\alpha-\beta}{100}$
D. $\beta-\alpha$

## Answer: C

## - Watch Video Solution

22. Let, $a_{1}, a_{2}-a, a_{3}, \ldots$ be in harmonic progression with $a_{1}=5$ and $a_{20}=25$ The least positive integer n for which $a_{n}<0$
A. 22
B. 23
C. 24
D. 25

## Answer: D

23. Statement 1: The sum of the series $1+(1+2+4)+(4+6+9)+(9+12+16)+\ldots \ldots$ $+(361+380+400) i s 8000$. Statement 2: $\sum_{k=1}^{n}\left(k^{3}-(k-1)^{3}\right)=n^{3}$ for any natural number n . (1) Statement 1 is false, statement 2 is true (2) Statement 1 is true, statement 2 is true; statement 2 is a correct explanation for statement 1 (3) Statement 1 is true, statement 2 is true; statement 2 is not a correct explanation for statement 1 (4) Statement 1 is true, statement 2 is false
A. Statement 1 is true, Statement 2 is true, Statement 2 is a correct explanation for Statement 1
B. Statement 1 is true, Statement 2 is true, Statement 2 is not a correct explanation for Statement 1
C. Statement 1 is true, Statement 2 is false
D. Statement 1 is false, Statement 2 is true
24. If 100 times the 100 th term of an A.P with non- zero common difference equals the 50 times its 50th term,then the 150th term of this A.P is
A. 150 times its 50th term
B. 150
C. zero
D. -150

## Answer: C

## - Watch Video Solution

25. If $\mathrm{x}, \mathrm{y}, \mathrm{z}$ are in AP and $\tan ^{-1} x, \tan ^{-1} y, \tan ^{-1} z$ are also in AP, then
A. $2 x=3 y=6 z$
B. $6 x=3 y=2 z$
C. $6 x=4 y=3 z$
D. $x=y=z$

## Answer: D

## - Watch Video Solution

26. The sum of first 20 terms of the sequence $0.7,0.77,0.777 \ldots$,..., is
A. $\frac{7}{9}\left(99-10^{-20}\right)$
B. $\frac{7}{81}\left(179+10^{-20}\right)$
C. $\frac{7}{9}\left(99+10^{-20}\right)$
D. $\frac{7}{81}\left(179-10^{-20}\right)$

## Answer: B

27. $L e t S_{n}=\sum_{k=1}^{4 n}(-1)^{\frac{k(k+1)}{2}} k^{2}$. Then $S_{n}$ can take value (s)
A. 1056
B. 1088
C. 1120
D. 1332

## Answer: A: D

## - Watch Video Solution

28. A pack contains $n$ cards numbered from 1 to $n$. Two consecutive numbered cards are removed from the pack and the sum of the numbers on the remaining cards is 1224 . If the smaller of het numbers on the removed cards is $k$, then $k-20=$ $\qquad$ .
29. If $(10)^{9}+2(11)^{2}(10)^{7}+\ldots .+10(11)^{9}=k(10)^{9}$
A. 100
B. 110
C. $\frac{121}{10}$
D. $\frac{441}{100}$

## Answer: A

## - Watch Video Solution

30. Three positive numbers form an increasing GP. If the middle terms in this GP is doubled, the new numbers are in AP. Then, the common ratio of the GP is
A. $2-\sqrt{3}$
B. $2+\sqrt{3}$
C. $\sqrt{2}+\sqrt{3}$
D. $3+\sqrt{2}$

## Answer: B

## - Watch Video Solution

31. about to only mathematics

## - Watch Video Solution

32. The sum of first 9 terms of the series $\frac{1^{3}}{1}+\frac{1^{3}+2^{3}}{1+3}+\frac{1^{3}+2^{3}+3^{3}}{1+3+5}+\ldots \ldots$. is
A. 192
B. 71
C. 96
D. 142

## Answer: C

## - Watch Video Solution

33. If $m$ is the A.M. of two distinct real numbers $l$ and $n(l, n>1)$ and G1, G2 and G3 are three geometric means between $l$ and $n$, then $G 14+2 G 24+G 34$ equals, (1) $4 l^{2} \mathrm{mn}$ (2) $4 l^{m} \wedge 2 \mathrm{mn}$ (3) $4 l m n^{2}$ $4 l^{2} m^{2} n^{2}$
A. $4 l^{2} m^{2} n^{2}$
B. $4 l^{2} m n$
C. $4 l m^{2} n$
D. $4 l m n^{2}$

## Answer: C

## D Watch Video Solution

34. Soppose that all the terms of an arithmetic progression (AP) are natural numbers. If the ratio of the sum of the first seven terms to the sum of the first eleven terms is $6: 11$ and the seventh term lies between 130 and 140 , then the common difference of this AP is

## - Watch Video Solution

35. If the 2nd , 5th and 9th terms of a non-constant A.P are in G.P then the common ratio of this G.P is
A. 1
B. $\frac{7}{4}$
C. $\frac{8}{5}$
D. $\frac{4}{3}$

## Answer: D

36. If the sum of the first ten terms of the series $\left(1 \frac{3}{5}\right)^{2}+\left(2 \frac{2}{5}\right)^{2}+\left(3 \frac{1}{5}\right)^{2}+4^{2}+\left(4 \frac{4}{5}\right)^{2}+\ldots$. , is $\frac{16}{5} \mathrm{~m}$, then m is equal to: (1) 102 (2) 101 (3) 100 (4) 99
A. 100
B. 99
C. 102
D. 101

## Answer: D

## - Watch Video Solution

37. Let
$b_{i}>1$ for $i=1,2$,
38. 

Suppose $\log _{e} b_{1}, \log _{e} b_{2}, \log _{e} b_{3}, \ldots \ldots . . \log _{e} b_{101}$ are in Arithmetic Progression (AP) with the common difference $\log _{e} 2$. Suppose $a_{1}, a_{2}, a_{3}, \ldots \ldots . . a_{101}$ are in AP. Such that, $a_{1}=b_{1}$ and $a_{51}=b_{51}$. If $t=b_{1}+b_{2}+\ldots \ldots \ldots+b_{51}$ and $s=a_{1}+a_{2}+\ldots \ldots \ldots+a_{51}$, then
A. (a) $s>t$ and $a_{101}>b_{101}$
B. (b) $s>t$ and $a_{101}<b_{101}$
C. (c) $s<t$ and $a_{101}>b_{101}$
D. (d) $s<t$ and $a_{101}<b_{101}$

## Answer: B

## - Watch Video Solution

38. For any three positive real numbers $a, b$ and $c, 9\left(25 a^{2}+b^{2}\right)+25\left(c^{2}-3 a c\right)=15 b(3 a+c)$. Then :
A. a,b and c are in GP
B. b,c and a are in GP
C. b,c and a are in AP
D. $a, b$ and $c$ are in AP

## Answer: C

