



MATHS

BOOKS - PATHFINDER MATHS

(BENGALI ENGLISH)

CONTINUITY & DIFFERENTIABILITY

Question Bank

1. If $f(x) = |x-2|+1$, evaluate $\lim_{x \rightarrow 2^+} \frac{f(x) - f(2)}{x - 2}$
and $\lim_{x \rightarrow 2^-} \frac{f(x) - f(2)}{x - 2}$. What can you say

about the existence of $f'(x)$ at $x=2$?



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2. Is the function defined by

$f(x) = x^2 - \sin x + 5$ continuous at $x=\pi$?



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3. Discuss the continuity of the function $[1-x]+$

$[x-1]$ at the point $x=1$.



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$$4. \text{ If } f(x) = \begin{cases} \frac{x-5}{|x-5|} + a & \text{if } x < 5 \\ a & \text{if } x = 5 \\ \frac{x-5}{|x-5|} + b & \text{if } x > 5 \end{cases}$$



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5. Show that the following function is continuous

$$|1 - x + |x||.$$



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6. Find the inverse function of the function $f(x)$

$$= 2^{x(x-1)} \quad (x > 0).$$



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7. Examine the continuity of the following

$$\text{function } f(x) = \begin{cases} |x| & \text{if } x \leq 2 \\ [x] & \text{if } x > 2 \end{cases} \text{ on } [0, 2]$$



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8. Given, $f(x) = \frac{x - 1}{2x^2 - 7x + 5}$ when $x \neq 1$

Find the derivative of $f(x)$ at $x=1$



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9. Let $f(x) = \frac{1}{x} \sin(x^2)$ when $x \neq 0$

$f(x) = 0$ when $x=0$

Discuss the continuity and differentiability of

$f(x)$ at $x=0$.



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10. The function $f(x) = \frac{x^3 - 8}{x^2 - 4}$ is undefined at $x=2$.

Redefine the function so as to make it continuous at $x=2$



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11. The function $f(x) = \frac{\log(1 + ax) - \log(1 - bx)}{x}$ is not defined at $x=0$. Find the value of $f(0)$, so that $f(x)$ is continuous at $x=0$.



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12. Determine the values of a so that the function is continuous at $x=1$.

$$f(x) = x^2 + 4 \text{ when } x \leq 2.$$

$$= x^2 + a^2, \text{ when } x < 1.$$



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13. $f(x) = \frac{x^2 - 1}{x^3 - 1}$ is undefined at $x=1$. What should be the value of $f(x)$ at $x=1$ such that $f(x)$ may be continuous at $x=1$?



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