



## MATHS

### BOOKS - KVPY PREVIOUS YEAR

### MOCK TEST 3

#### Exercise

1. Find the values of  $\alpha$  for which the point  $(\alpha - 1, \alpha + 1)$  lies in the larger segment of the circle  $x^2 + y^2 - x - y - 6 = 0$  made by the chord whose equation is  $x + y - 2 = 0$

A. 0

B. 1

C. 2

D. None of these

**Answer:**



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2. Let  $1 \leq m < n \leq p$ . The number of subsets of the set  $A = \{1, 2, 3, \dots, p\}$  having  $m, n$  as the least and the greatest elements respectively, is

A.  $2^{n-m-1} - 1$

B.  $2^{n-m-1}$

C.  $2^{n-m}$

D. None of these

**Answer:**



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3. Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be a continuous function which satisfies

$f(x) = \int_0^x f(t) dt$ . Then the value of  $f(1)$  is \_\_\_\_\_

A. -2

B. 3

C. -1

D. 0

**Answer:**



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4. Two numbers  $a$  and  $b$  are chosen at random from the set  $\{1, 2, 3, \dots, 3n\}$ . The probability that  $a^2 + b^2$  is divisible by 3, is

A.  $\frac{1}{3}$

B.  $\frac{2}{3}$

C.  $\frac{3}{n}$

D.  $\frac{n-1}{3n}$

**Answer:**

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5. The line  $2px + y\sqrt{1-p^2} = 1$  ( $|p| < 1$ ) for different values of  $p$ , touches a fixed ellipse whose axes are the coordinate axes. Q. The locus of the point of intersection of perpendicular tangents of the ellipse is

A. An ellipse of eccentricity  $\frac{2}{\sqrt{3}}$

B. An ellipse of eccentricity  $\frac{\sqrt{3}}{2}$

C. Hyperbola of eccentricity 2

D. a hyperbola eccentricity  $\sqrt{2}$

**Answer:**



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6. If  $f: R \rightarrow R, g, R \rightarrow R$  be two functions, and  $h(x) = 2\min\{f(x) - g(x), 0\}$  then  $h(x) =$

A.  $f(x)+g(x)-|g(x)-f(x)|$

B.  $f(x)+g(x)+|g(x)-f(x)|$

C.  $f(x)-g(x)+|g(x)-f(x)|$

$$D. f(x)-g(x)-|g(x)-f(x)|$$

**Answer:**



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7. The area bounded by the curves

$$y = |x| - 1 \text{ and } y = -|x| + 1 \text{ is } 1 \text{ b. } 2 \text{ c. } 2\sqrt{2} \text{ d. } 4$$

A. 1

B. 2

C.  $2\sqrt{2}$

D. 4

**Answer:**



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**8.** A function  $\phi(x)$  satisfies the functional equation  $x^2\phi(x) + \phi(1 - x) = 2x - x^4$  for all real  $x$ . Then  $\phi(x)$  is given by

A.  $x^2$

B.  $1 - x^2$

C.  $1 + x^2$

D.  $x^2 + x + 1$



**Answer:**



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**9.** If  $n$  is a natural number, then

A.  $1^2 + 2^2 + \dots + n^2 < \frac{n^3}{3}$

B.  $1^2 + 2^2 + \dots + n^2 = \frac{n^3}{3}$

C.  $1^2 + 2^2 + \dots + n^2 > n^3$

D.  $1^2 + 2^2 + \dots + n^2 > \frac{n^3}{3}$

**Answer:**



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10.

Let

$$S_n = \sum_{k=1}^n \frac{n}{n^2 + nk + k^2} \quad \text{and} \quad T_n = \sum_{k=0}^{n-1} \frac{n}{n^2 + nk + k^2}$$

for  $n = 1, 1, 2, 3, \dots$ , they

A.  $S_n < \frac{\pi}{3\sqrt{3}}$

B.  $S_n > \frac{\pi}{3\sqrt{3}}$

C.  $T_n < \frac{\pi}{3\sqrt{3}}$

D.  $T_n \geq \frac{\pi}{3\sqrt{3}}$

**Answer:**



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11. Two friends visit a restaurant randomly during 5 pm to 6 pm . Among the two, whoever comes first waits for 15 min and then leaves. The probability that they meet is :

A.  $\frac{1}{4}$

B.  $\frac{1}{16}$

C.  $\frac{7}{16}$

D.  $\frac{9}{16}$

**Answer:**



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12. For any  $n \in \mathbb{N}$ , the value of the expression

$$\sqrt{2 + \sqrt{2 + \sqrt{2 + \dots n \times}}}$$

A.  $2 \cos\left(\frac{\pi}{2^{n+1}}\right)$

B.  $2 \sin\left(\frac{\pi}{2^{n+1}}\right)$

C.  $\sqrt{2} \cos(2^{n+1}\pi)$

D. None of these

**Answer:**



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13. If  $a$ ,  $b$  and  $c$  are distinct positive numbers, then

the

expression

$(a + b - c)(b + c - a)(c + a - b) - abc$  is:

A. positive

B. negative

C. non-positive

D. non-negative

**Answer:**



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**14.** The general value of  $\theta$  satisfying the equation

$$2 \sin^2 \theta - 3 \sin \theta - 2 = 0 \text{ is}$$

A.  $n\pi + (-1)^n \pi / 6$

B.  $n\pi + (-1)^n \pi / 2$

C.  $n\pi + (-1)^n (5\pi) / 6$

D.  $n\pi + (-1)^n (7\pi) / 6$

**Answer:**



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**15.** For  $3 \times 3$  matrices  $M$  and  $N$ , which of the following statement(s) is/are not correct?

A.  $N^T MN$  is symmetric or skew

symmetric, according as M is symmetric or skew

symmetric

B.  $MN - NM$  is skew symmetric for all symmetric

matrices M and N

C.  $MN$  is symmetric for all symmetric matrices M

and N

D. None of these

**Answer:**



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16. If the inequality

$$(mx^2 + 3x + 4 + 2x) / (x^2 + 2x + 2) < 5 \quad \text{is}$$

satisfied for all  $x \in R$ , then find the value of  $m$ .

A.  $1 < m < 5$

B.  $-1 < m < 1$

C.  $-5 < m < \frac{11}{24}$

D.  $m < \frac{71}{24}$

**Answer:**



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17. If  $f(x) = g(x^3) + xh(x^3)$  is divisible by  $x^2 + x + 1$ , then

- A. both  $g(x)$  and  $h(x)$  are divisible by  $(x-1)$
- B.  $h(x)$  is divisible but  $g(x)$  is not divisible  $x-1$
- C.  $g(x)$  is divisible but  $h(x)$  is not divisible  $x-1$
- D. None of these

**Answer:**



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18. The area of the trapezium whose vertices lie on the parabola  $y^2 = 4x$  and its diagonals pass through  $(1,0)$  and having length  $\frac{25}{4}$  units each is

A.  $\frac{75}{4}$

B.  $\frac{73}{4}$

C.  $\frac{75}{2}$

D.  $\frac{70}{3}$

**Answer:**



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19. A person goes to office either by car, scooter, bus or train probability of which being  $\frac{1}{7}$ ,  $\frac{3}{7}$ ,  $\frac{2}{7}$  and  $\frac{1}{7}$  respectively. Probability that he reaches office late, if he takes car, scooter, bus or train is  $\frac{2}{9}$ ,  $\frac{1}{9}$ ,  $\frac{4}{9}$  and  $\frac{1}{9}$  respectively. Given that he reached office in time, then what is the probability that he travelled by a car?

A.  $\frac{1}{7}$

B.  $\frac{2}{7}$

C.  $\frac{6}{7}$

D.  $\frac{5}{7}$

**Answer:**



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**20.** The line  $x + y = 1$  meets X-axis at A and Y-axis at B, P is the mid-point of AB,  $P_1$  is the foot of perpendicular from P to OA,  $M_1$ , is that of  $P_1$ , from OP;  $P_2$ , is that of  $M_1$  from OA,  $M_2$ , is that of  $P_2$ , from OP;  $P_3$  is that of  $M_2$ , from OA and so on. If  $P_n$  denotes the nth foot of the perpendicular on OA, then find  $OP_n$ .

A.  $\left(\frac{1}{2}\right)^{n-1}$

B.  $\left(\frac{1}{2}\right)^n$

C.  $\left(\frac{1}{2}\right)^{n+1}$

D. None of these

**Answer:**



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**21.** If  $x, y$  and  $z$  are three real numbers such that  $x + y + z = 4$  and  $x^2 + y^2 + z^2 = 6$ , then show that each of  $x, y$  and  $z$  lie in the closed interval  $\left[\frac{2}{3}, 2\right]$

A.  $[2/3, 2]$

B.  $[0, 2/3]$

C.  $[0,2]$

D.  $[-1/3,2/3]$

**Answer:**



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**22.** A variable point  $P$  on the ellipse of eccentricity  $e$  is joined to the foci  $S$  and  $S'$ . The eccentricity of the

locus of incentre of the triangle  $PSS'$  is (A)  $\sqrt{\frac{2e}{1+e}}$

(B)  $\sqrt{\frac{e}{1+e}}$  (C)  $\sqrt{\frac{1-e}{1+e}}$  (D)  $\frac{e}{2(1+e)}$

A. 5

B. 2

C. 1

D. -1

**Answer:**



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**23.** Let  $z, z_0$  be two complex numbers  $z_0$  being the conjugate of  $z_0$ . The numbers  $z, z_0, z\bar{z}_0, 1$  and  $0$  are represented in argand diagram by  $P, P_0, Q, A$  and origin respectively. If  $|z| = 1$ , then (A)  $\triangle POP_0$  and  $\triangle AOQ$  are congruent (B)  $|z - z_0| = |z\bar{z}_0 - 1|$  (C)  $|z - z_0| = \frac{1}{2}|z\bar{z}_0 - 1|$  (D) none of these

- A. Only I is true
- B. Only II is true
- C. Both I & II are true
- D. Both I & II are false

**Answer:**



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**24.** A person throws dice, one the common cube and the other reglowest terahedron, the number on the lowest face being taken in the case of a tetrahedron.



The chance that the sum of numbers throws is not less than 5 is

A.  $\frac{1}{4}$

B.  $\frac{3}{4}$

C.  $\frac{4}{5}$

D.  $\frac{5}{6}$

**Answer:**



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**25.** The integers  $x, y$  and  $z$  each are perfect squares and  $x > y > z > 0$ . If  $x, y, z$  form an A.P. and  $x + y + z = 75$ , then

the smallest possible value of  $x$  is

A. 39

B. 31

C. 41

D. 49

**Answer:**



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**26.** let  $A_1, A_2, A_3, \dots, A_n$  are the vertices of a regular  $n$  sided polygon inscribed in a circle of radius  $R$ . If

$(A_1A_2)^2 + (A_1A_3)^2 + \dots + (A_1A_n)^2 = 14R^2$  then find the number of sides in the polygon.

A. 3

B. 4

C. 5

D. None of these

**Answer:**



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27. If  $p, q, r, s$  are in A.P. and

$$f(x) = \begin{vmatrix} p + \sin x & q + \sin x & p - r + \sin x \\ q + \sin x & r + \sin x & -1 + \sin x \\ r + \sin x & s + \sin x & s - q + \sin x \end{vmatrix} \quad \text{such}$$

that  $\int_0^2 f(x) dx = -4$  then the common difference

of the A.P. can be : (A) 1 (B)  $\frac{3}{2}$  (C) -1 (D) 3

A.  $\pm 1$

B.  $\frac{1}{2}$

C.  $\pm 2$

D. None of these

**Answer:**



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