



## MATHS

### BOOKS - BITSAT GUIDE

### DIFFERENTIAL COEFFICIENTS

#### Practice Exercise

1. If  $y=f(x)$  is an odd differentiable function defined on  $(-\infty, \infty)$  such that  $f'(3) = -2$  then  $f'(-3)$  equals -

A. 0

B. 1

C. 2

D. 4

**Answer: C**



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**2.**

If

$$x^2 + y^2 = t - \frac{1}{t} \text{ and } x^4 + y^4 = t^2 + \frac{1}{t^2}, \text{ then } x^3 y \frac{dy}{dx} =$$

0 (b) 1 (c) – 1 (d) none of these

A. 1

B. 2

C. 3

D. 4

**Answer: A**



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3. If  $f(x) = |\cos x|$ , then  $f'\left(\frac{3\pi}{4}\right)$  is equal to

A.  $\frac{1}{\sqrt{2}}$

B.  $\sqrt{2}$

C.  $\frac{1}{2}$

D.  $2\sqrt{2}$

**Answer: A**



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4. If  $f(x) = |\cos x - \sin x|$ , then  $f' \frac{\pi}{2}$  is equal to

- A. 1
- B. -1
- C. 0
- D. None

**Answer: A**



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5. If  $f'(x) = \varphi(x)$  and  $\varphi'(x) = f(x)$  for all  $x$ . Also,  $f(3) = 5$  and  $f'(3) = 4$ . Then the value of

$[f(3)]^2 - [\varphi(3)]^2$  is

- A. 0
- B. 9
- C. 41
- D. None of these

**Answer: B**



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6. If  $f(x) = x^n$ ,  $n \in N$ , then the value of  $f(1) - \frac{f'(1)}{1!} + \frac{f(1)}{2!} - (f''')\frac{1}{3!} + \dots + (-1)^n \frac{f^n(1)}{n!}$  is

A.  $2^n$

B. 0

C.  $2^{n-1}$

D. None of these

**Answer: B**



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7. Let  $f(x) = x^2 + xg'(1) + g''(2)$  and  
 $g(x) = x^2 + xf'(2) + f''(3)$ , then

A.  $f'(1) = 4 - f'(2)$

B.  $g'(2) = 8 - g'(1)$

C.  $g''(2) + f'''(3) = 4$

D. None of these

**Answer: C**



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8. If  $2^x + 2^y = 2^{x+y}$  then  $\frac{dy}{dx}$  is equal to

A.  $\frac{2^x + 2^y}{2^x - 2^y}$

B.  $\frac{2^x + 2^y}{1 + 2^{x+y}}$

C.  $2^{x-y} \frac{2^y - 1}{1 - 2^x}$

D.  $\frac{2^{x-y} - 2^x}{2^y}$

**Answer: C**



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9. The solution set of  $f'(x) > g'(x)$ , where

$f(x) = \frac{1}{2}(5)^{2x+1}$  and  $g(x) = 5^x + 4x \log_e 5$ , is

A.  $(1, \infty)$

B.  $(0, 1)$

C.  $(\infty, 0)$

D.  $(0, \infty)$

**Answer: D**



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10. If  $y = \sec^{-1} \frac{\sqrt{x} + 1}{\sqrt{x} - 1} + \sin^{-1} \frac{\sqrt{x} - 1}{\sqrt{x} + 1}$ , then  $\frac{dy}{dx}$  is equal to

A. 0

B.  $\frac{1}{\sqrt{x} + 1}$

C. 1

D. 3

**Answer: A**



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11. If  $Y = \tan^{-1} \frac{4x}{1 + 5x^2} + \tan^{-1} \frac{2 + 3x}{3 - 2x}$ , then  $\frac{dy}{dx} =$

A.  $\frac{1}{1+x^2}$

B.  $\frac{5}{1+25x^2}$

C. 1

D. 2

**Answer: B**



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12. Let  $g(x)$  be the inverse of the function  $f(x)$ , and

$f'(x) \frac{1}{1+x^3}$  then  $g(x)$  equals

A.  $\frac{1}{1+[g(x)]^3}$

B.  $\frac{1}{1+[f(x)]^3}$

C.  $1 + [g(x)]^3$

D.  $1 + [f(x)]^3$

**Answer: C**



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13. If  $f(x) = e^x g(x)$ ,  $g(0) = 2$ ,  $g'(0) = 1$ , then  $f'(0)$  is

A. 1

B. 3

C. 2

D. 0

**Answer: B**



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14. if  $y = \log x \cdot e^{(\tan x + x^2)}$ , then  $\frac{dy}{dx}$  is equal to

A.  $e^{(\tan x + x^2)} \frac{1}{x} + (\sec^2 x + x) \log x$

B.  $e^{(\tan x + x^2)} \frac{1}{x} + (\sec^2 x - x) \log x$

C.  $e^{(\tan x + x^2)} \frac{1}{x} + (\sec^2 x + 2x) \log x$

D.  $e^{(\tan x + x^2)} \frac{1}{x} + (\sec^2 x - 2x) \log x$

**Answer: C**



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15.

If

$$f(x) = \cos x \cos 2x \cos 4x \cos 8x \cos 16x, \quad \text{then } f'\left(\frac{\pi}{4}\right)$$

is

A.  $\sqrt{2}$

B.  $\frac{1}{\sqrt{2}}$

C. 1

D.  $\frac{\sqrt{3}}{2}$

**Answer: A**



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**16.** The derivative of  $y = (1 - x)(2 - x)(n - x)$  at  $x = 1$  is  
(b)  $(-1)(n - 1)! n! - 1$  (d)  $(-1)^{n-1}(n - 1)!$

A. 0

B.  $(-1)(n - 1)!$

C.  $n! - n!$

D.  $(-1)^{n-1}(n - 1)!$

**Answer:** B



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**17.**  $f$  and  $g$  are two differentiable functions which satisfy the condition  $g'(a) = 2$ ,  $g(a) = b$  and  $(f \circ g) = I$

identity function , then  $f'(b)$  is equal to

- A.  $\frac{1}{2}$
- B. 2
- C.  $\frac{2}{3}$
- D. None

**Answer: A**



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**18.** If  $f(x) = \sqrt{1 + \cos^2(x^2)}$ , then  $f'\left(\frac{\sqrt{\pi}}{2}\right)$  is

- A.  $\sqrt{\pi}/6$
- B.  $-\sqrt{\pi/6}$

C.  $1/\sqrt{6}$

D.  $\pi/\sqrt{6}$

**Answer: B**



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**19.** If  $y = (1 - x)(1 + x^2)(1 + x^4) \dots \dots (1 + x^{2n})$ , then

$\frac{dy}{dx}$  at  $x=0$  is equal to

A.  $-1$

B.  $\frac{1}{(1+x)^2}$

C.  $\frac{x}{(1+x)^2}$

D.  $\frac{x}{(1-x)^2}$

**Answer: A**



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20. If  $f(x) = \frac{x^2 - x}{x^2 + 2x}$ , where  $x \neq 0, -2$ , then  $\frac{d}{dx}[f^{-1}(x)]$  (wherever it is defined) is equal to

A.  $\frac{-1}{(1-x)^2}$

B.  $\frac{3}{(1-x)^2}$

C.  $\frac{1}{(1-x)^2}$

D.  $\frac{3}{(1-x)^2}$

**Answer: B**



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21. If  $y = \sin[\cos(x^2)]$  then  $\frac{dy}{dx}$  is equal to

A.  $-2x\sin x^2 \cdot \cos(\cos x^2)$

B.  $-2x\sin x^2 \cdot \cos x^2$

C.  $2x^2\sin x^2 \cdot \cos x^2$

D. None of these

**Answer: A**



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22. If  $F(x) = f(x) \cdot g(x)$  and  $f'(x) \cdot g'(x) = c$ , then

A.  $F' = c \frac{f}{f'} + \frac{g}{g'}$

- B.  $F' = c \frac{f}{f'} - \frac{g}{g'}$
- C.  $\frac{F''}{F} = \frac{f''}{f} + \frac{g''}{g} + \frac{2c}{fg}$

D. None of these

**Answer: A**



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**23.** If  $y \cos x + x \cos y = \pi$ , then  $\frac{dy}{dx}$  is equal to

A.  $\frac{y \sin x - \cos y}{\cos x - x \sin y}$

B.  $\frac{\cos y - y \sin x}{x \sin y + \cos x}$

C.  $\frac{y \sin x + \cos y}{\cos x - x \sin y}$

D.  $\frac{y \sin x + \cos y}{\cos x + x \sin y}$

**Answer: A**



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**24.** Let  $f : (-1,1) \rightarrow \mathbb{R}$  be a differentiable function with  $f(0) = -1$  and  $f'(0) = 1$ . Let

$$g(x) = [f(2f(x) + 2)]^2, \text{ then } g'(0) =$$

A. 4

B. -4

C. 0

D. -2

**Answer: B**



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25. If  $y = \frac{a^{\cos^{-1} x}}{1 + a^{\cos^{-1} x}}$  and  $z = a^{\cos^{-1} x}$ , then  $\frac{dy}{dz}$  is equal to

- A.  $-\frac{1}{1 + a^{\cos^{-1} x}}$
- B.  $\frac{1}{1 + a^{\cos^{-1} x}}$
- C.  $\frac{1}{(1 + a^{\cos^{-1} x})^2}$
- D. None of these

**Answer: C**



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26. If  $\sqrt{1 - x^2} + \sqrt{1 - y^2} = a(x - y)$ , then  $\frac{dy}{dx}$  equals

A.  $\sqrt{\frac{1 - x^2}{1 - y^2}}$

B.  $\sqrt{\frac{1 - y^2}{1 - x^2}}$

C.  $\sqrt{\frac{x^2 - 1}{1 - y^2}}$

D.  $\sqrt{\frac{y^2 - 1}{1 - x^2}}$

**Answer: B**



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27. If  $y = \sin^{-1} \left( x\sqrt{1-x} + \sqrt{x}\sqrt{1-x^2} \right)$ , then  $\frac{dy}{dx} =$

A.  $\frac{-2x}{\sqrt{1-x^2}} + \frac{1}{2\sqrt{x-x^2}}$

B.  $\frac{-1}{\sqrt{1-x^2}} - \frac{1}{2\sqrt{x-x^2}}$

C.  $\frac{1}{\sqrt{1-x^2}} + \frac{1}{2\sqrt{x-x^2}}$

D. None of these

**Answer: C**



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**28.** If  $y = \sec(\tan^{-1} x)$  then  $\frac{dy}{dx}$  at  $x = 1$  is equal to

A.  $\frac{1}{\sqrt{2}}$

B.  $\frac{1}{2}$

C. 1

D.  $\sqrt{2}$

**Answer: A**



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**29.** If  $y = \sin^{-1} x \sin^{-1} \sqrt{1 + x^2}$ ,  $-1 \leq x \leq 1$ , then

$$\frac{dy}{dx}$$
 is

A. 0

B.  $\frac{\pi}{2}$

C. 1

D. 4

**Answer: A**



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30. If  $x = \frac{2t}{1+t^2}$  and  $y = \frac{1-t^2}{1+t^2}$ , then  $\frac{dy}{dx}$  is equal to

A.  $\frac{2t}{t^2+1}$

B.  $\frac{2t}{t^2-1}$

C.  $\frac{2t}{1-t^2}$

D. None

**Answer: B**



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31. If  $x = a \cos t \sqrt{\cos 2t}$  and  $y = a \sin t \sqrt{\cos 2t}$  (where,

$a > 0$ ), then  $\left| \frac{1 + \frac{dy^2}{dx^2}}{\frac{d^2y}{dx^2}} \right|$  at  $\frac{\pi}{6}$  is given by

A.  $\frac{a}{3}$

B.  $a\sqrt{2}$

C.  $\frac{\sqrt{2}}{3a}$

D.  $\frac{\sqrt{2a}}{3}$

**Answer: D**



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**32.** If  $x = a(\theta + \sin \theta)$  and  $y = a(1 - \cos \theta)$ , find  $dy/dx$ .

A.  $\tan \frac{\theta}{2}$

B.  $\cot \frac{\theta}{2}$

C.  $\tan \theta$

D.  $\cot \theta$

**Answer: A**



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**33.** If  $x = e^{-t^2}$ ,  $y = \tan^{-1}(2t + 1)$ , then  $\frac{dy}{dx} =$

A.  $\frac{e^{t^2}}{2t(t^2 + 2t + 1)}$

B.  $\frac{-e^{t^2}}{2t(2t^2 + 2t + 1)}$

C.  $\frac{-e^{t^2}}{2t(t^2 + 2t + 1)}$

D. None of these

**Answer: B**



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34. If  $\sqrt{(x^2 + y^2)} = ae^{\tan^{-1}(y/x)}$ ,  $a > 0$ , then  $y''(0)$  equals

A.  $\frac{a}{2}e^{\pi/2}$

B.  $ae^{\pi/2}$

C.  $\frac{-2}{a}e^{-\pi/2}$

D.  $\frac{a}{2}e^{-\pi/2}$

**Answer: C**



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35. The expression of  $\frac{dy}{dx}$  of the function  $y = a^{x^{a^{x^{...^{\infty}}}}}$ , is

- A.  $\frac{y^2}{x(1 - y \log x)}$
- B.  $\frac{y^2 \log y}{x(1 - y \log x)}$
- C.  $\frac{y^2 \log y}{x(1 - y \log x \log y)}$
- D.  $\frac{y^2 \log y}{x(1 + y \log x \log y)}$

**Answer: C**



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**36.** Derivative of  $(\sin x)^x + \sin^{-1} \sqrt{x}$  with respect to x is

- A.  $(x \cot x + \log \sin x) + \frac{1}{2\sqrt{x - x^2}}$
- B.  $(x \cot x + \log \sin x) + \frac{1}{\sqrt{x - x^2}}$
- C.  $(\sin x)(x \cot x + \log) + \frac{1}{\sqrt{x - x^2}}$

$$\text{D. } (\sin x)^x(x \cot x + \log \sin x) + \frac{1}{2\sqrt{x-x^2}}$$

**Answer: D**



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37. If  $x^m \cdot y^n = (x + y)^{m+n}$ , then:  $\frac{dy}{dx}$  is independent of

A.  $\frac{x+y}{xy}$

B.  $xy$

C.  $\frac{x}{y}$

D.  $\frac{y}{x}$

**Answer: D**



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38. Let  $y = \sqrt{x + \sqrt{x + \sqrt{x + \dots \infty}}}$ , then  $\frac{dy}{dx}$  is equal to

A.  $\frac{1}{2y - 1}$

B.  $\frac{y}{2x + y}$

C.  $\frac{1}{\sqrt{1 + 4x}}$

D. All

**Answer: D**



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**39.** Let  $y$  be an implicit function of  $x$  defined by

$x^{2x} - 2x^x \cot y - 1 = 0$ . Then  $y'(1)$  equals:

a.  $-1$   
b.  $\log 2$   
c.  $-\log 2$   
d.  $-1$

A.  $-1$

B.  $1$

C.  $\log 2$

D.  $-\log 2$

**Answer: A**



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40. The derivative of  $\tan^{-1}\left(\frac{\sqrt{1+x^2}-1}{x}\right)$  with respect to  $\tan^{-1}\left(\frac{2x\sqrt{1-x^2}}{1-2x^2}\right)$  at  $x = 0$  is (a)  $\frac{1}{8}$  (b)  $\frac{1}{4}$  (c)  $\frac{1}{2}$  (d) 1

A.  $1/8$

B.  $1/4$

C.  $1/2$

D. 1

**Answer: B**



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41. If  $f(x) = \begin{vmatrix} \sec \theta & \tan^2 \theta & 1 \\ \theta \sec x & \tan x & x \\ 1 & \tan x - \tan \theta & 0 \end{vmatrix}$ , then  $f'(\theta)$  is

A. zero

B. -1

C. independent of  $\theta$

D. None of these

**Answer: B**



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42. Let  $f(x) = \begin{vmatrix} x^3 & \sin x & \cos x \\ 6 & -1 & 0 \\ p & p^2 & p^3 \end{vmatrix}$  where  $p$  is a constant.

Then  $\frac{d^3}{dx^3}\{f(x)\}$  at  $x=0$  is

A. P

B.  $P + P^2$

C.  $P + P^3$

D. independent of P

**Answer: D**



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**43.** If  $y = Ae^{-kt} \cos(pt + c)$ , then prove that

$$\frac{d^2y}{dt^2} + 2k\frac{dy}{dx} + n^2y = 0, \text{ where } n^2 = p^2 + k^2$$

A.  $p^2 - k^2$

B.  $p^2$

C.  $k^2$

D.  $p^2 + k^2$

**Answer: D**



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44. if  $\sqrt{x+y} + \sqrt{y-x} = c$  then  $\frac{d^2y}{dx^2}$  equals

A.  $2/c$

B.  $-2/c^2$

C.  $2/c^2$

D. None

**Answer: C**



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1. If  $x$  is in degrees, then:  $\frac{d}{dx}(\cos x) =$

A.  $-\sin x$

B.  $-\frac{180}{\pi} \sin x$

C.  $-\frac{\pi}{180} \sin x$

D.  $\sin x$

**Answer: C**



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2.  $\frac{d}{dx}[\log(\sec x - \tan x)]$  is equal to

A.  $-\sec x$

B.  $\sec x + \tan x$

C.  $\sec x$

D.  $\sec x - \tan x$

**Answer: A**



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3. If  $x = \cos^3 \theta$  and  $y = \sin^3 \theta$ , then  $1 + \frac{d^2y}{dx^2}$  is equal to

A.  $\tan^2 \theta$

B.  $\cot^2 \theta$

C.  $\sec^2 \theta$

D.  $\cos ec^2\theta$

**Answer: C**



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4. If  $x = at^2$ ,  $y = 2at$ , then  $\frac{d^2y}{dx^2}$  is equal to

A.  $-\frac{1}{t^2}$

B.  $-\frac{1}{2at^3}$

C.  $\frac{1}{t^2}$

D.  $-\frac{a}{2t^3}$

**Answer: B**



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5. If  $\Delta_1 = \begin{vmatrix} x & a & b \\ b & x & a \\ a & b & x \end{vmatrix}$  and  $\Delta_2 = \begin{vmatrix} x & b \\ a & x \end{vmatrix}$  are the given determinants then

- A.  $\Delta_1 = 3(\Delta_2)^2$
- B.  $\frac{d}{dx}(\Delta_1) = 3\Delta_2$
- C.  $\frac{d}{dx}(\Delta_1) = 3(\Delta_2)^2$
- D.  $\Delta_1 = 3(\Delta_2)^{3/2}$

**Answer: B**



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6.  $\frac{d}{dx}(x^x)$  is equal to

A.  $x^x \log(e/x)$

B.  $x^x \log ex$

C.  $\log ex$

D.  $x^x \log x$

**Answer: B**



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7. If  $y^2 = P(x)$  is a polynomial of degree 3, then

$2\left(\frac{d}{dx}\right) \left(y^2 \frac{d^2y}{dx^2}\right)$  is equal to (a)  $P^x + P'(x)$  (b)  $P^x \dot{P}^x$   
 $P(x) \dot{P}^x$  (c) a constant

A.  $P'''(x)P'(x)$

B.  $P''(x)P''''(x)$

C.  $P(x)P''''(x)$

D. constant

**Answer: C**



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**8.** If  $f(x) = (1 - x)^n$ , then the value of

$$f(0) + f'(0) + \frac{f''(0)}{2!} + \dots + \frac{f^n(0)}{n!}, \text{ is}$$

A.  $2^n$

B. 0

C.  $2^{n-1}$

D. 1

**Answer: B**



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9. If  $f(x) = \log_x (\ln x)$  then  $f'(x)$  at  $x=e$  is

A.  $1/e$

B. e

C.  $-1/e$

D. 0

**Answer: A**



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10. Let  $f(x) = 2^{2x-1}$  and  $g(x) = -2^x + 2x \log 2$ .

Then the set of points satisfying  $f'(x) > g'(x)$ , is

A.  $0 < x < 1$

B.  $0 \leq x < 1$

C.  $x > 0$

D.  $x \neq 0$

**Answer: C**



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$$11. y = \sin^{-1} \left( \frac{5x + 12\sqrt{1 - x^2}}{13} \right)$$

- A.  $\frac{1}{\sqrt{1 - x^2}}$
- B.  $-\frac{1}{\sqrt{1 - x^2}}$
- C.  $\frac{3}{\sqrt{1 - x^2}}$
- D.  $\sqrt{1 - x^2}$

**Answer: A**



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12. If  $x = a \left\{ \cos \theta + \log \tan \frac{\theta}{2} \right\}$  and  $y = a \sin \theta$ , then  $\frac{dy}{dx}$  is equal to

A.  $\cot \theta$

B.  $\tan \theta$

C.  $\sin \theta$

D.  $\cos \theta$

**Answer: B**



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13. The derivative of  $\sin^{-1} \left( \frac{2x}{1+x^2} \right)$  with respect to  $\cos^{-1} \left( \frac{1-x^2}{1+x^2} \right)$  is

A. -1

B. 1

C. 2

D. 4

**Answer: B**



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14. If  $\cos^{-1} \frac{1-x^2}{1+x^2}$ , then  $\frac{dy}{dx}$  is equal to

A.  $\frac{x}{y}$

B.  $-\frac{x}{y}$

C.  $\frac{y}{x}$

D.  $-\frac{y}{x}$

**Answer: B**



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15.

If

$$y = \tan^{-1} \left[ \frac{\sqrt{1+x^2} - \sqrt{1-x^2}}{\sqrt{1+x^2} + \sqrt{1-x^2}} \right] \text{ find } \frac{dy}{dx}$$

A.  $\frac{x^2}{\sqrt{1-x^4}}$

B.  $\frac{x^2}{\sqrt{1-x^2}}$

C.  $\frac{x}{\sqrt{1+x^4}}$

D.  $\frac{x}{\sqrt{1-x^4}}$

**Answer: D**



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**16.** If  $x = \sin t$  and  $y = \cos pt$ , then

A.  $(1 - x^2)y_2 + xy_1 + p^2y = 0$

B.  $(1 - x^2)y_2 + xy_1 - p^2y = 0$

C.  $(1 + x^2)y_2 - xy_1 + p^2y = 0$

D.  $(1 - x)^2y_2 - xy_1 + p^2y = 0$

**Answer:** D



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**17.** If  $r = [2\varphi + \cos^2(2\varphi + \pi/4)]^{1/2}$ , then what is the value of the derivative of  $dr/d\varphi$  at  $\varphi = \pi/4$ ?

A.  $2 \frac{1^{1/2}}{\pi + 1}$

B.  $2 \frac{1^2}{\pi + 1}$

C.  $\frac{2^{1/2}}{\pi + 1}$

D.  $2 \frac{2^{1/2}}{\pi + 1}$

**Answer: D**



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