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## MATHS

## BOOKS - HIMALAYA MATHS (KANNADA ENGLISH)

## COMMON ENTRANCE TEST -2016

## Question Bank

1. If $3 \tan ^{-1} x+\cot ^{-1} x \equiv \pi$ then x equal to
A. $\min u s 1$
B. 0
C. 44228
D. 1

## Answer: D

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2. Find the co-ordinates of the foot of the perpendicular drawn from the origin to the plane $5 y+8=0$
A. $(8 / 25,0,0)$
B. $(0,-8 / 2,2)$
C. $(0,-8 / 5,0)$
D. $(0,8 / 5,0)$

Answer: C

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3. 

If
the
straight
lines
$2 x+3 y-3=0$ and $x+k y+7=0 \quad$ are perpendicular, then the value of $k$ is
A. minus $2 / 3$
B. 44257
C. minus $3 / 2$
D. 44230

Answer: A

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4. Let * be a binaray operation deifned on $R$
by $a * b=\frac{a+b}{4} \forall$ a, b $\varepsilon R$ then the operation $*$ is
A. Associative but not commutative
B. Commutative and Associative
C. Neither Associative nor Commutative
D. Commutative but not Associative

## Answer: D

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5. $\lim _{x \rightarrow 0} \frac{x e^{x}-\sin x}{x}$ is equal to
A. 0
B. 3
C. 2
D. 1

## Answer: A

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6. The value of $\int \frac{e^{6 \log x}-e^{5 \log x}}{e^{4 \log x}-e^{3 \log x}} d x$ is equal to
A. $\frac{x^{3}}{3}$
B. $\frac{3}{x^{3}}$
C. 0
D. $1 / \mathrm{x}$

Answer: A

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7. Integrating factor of $x \frac{d y}{d x}-y=x^{4}-3 x$ is

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8. The length of latus rectum of parabola $4 y^{2}+3 x+3 y+1=0$ is

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9. Two dice are thrown simultaneously, the probability of obtaining a total score of 5 is
10. Area lying between the curves $y^{2}-2 x$ and $y=x$ is

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11. If $A$ is any aquare matrix of order $3 \times 3$ then
$|3 A|$ is equal to

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12. The solution for the differential equation $\frac{d y}{y}+\frac{d x}{x}=0$ is

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13. IF $x$ yz are not equal to $\neq 0, \neq 1$ the value of $\left|\begin{array}{lll}\log x & \log y & \log z \\ \log 2 x & \log 2 y & \log 2 z \\ \log 3 x & \log 3 y & \log 3 z\end{array}\right|$ is equal to
14. If $\vec{a}$ and $\vec{b}$ are unit vectors, then what is the angle between $\vec{a}$ and $\vec{b}$ for $\sqrt{3}$ veva $-\vec{b}$ to be a unit vectors ?

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15. The set A has 4 element and the set B has 5
elements then the number of injective mappings that can be deifned from $A$ to $B$ is

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$x^{3}-3 x y^{2}+2=0$ and $3 x^{2} y-y^{3}=2$

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17. Evaluate $\int \frac{e^{x}(1+x)}{\cos ^{2}\left(x e^{x}\right)} d x$

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> 18. The simplified form of
> $i^{n}+i^{n+1}+i^{n+2}+i^{n+3}$ is

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19. The value of $\int_{2}^{8} \frac{\sqrt{10-x}}{\sqrt{x}+\sqrt{10-x}} d x$ is

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20. The maximum value of $\left(\frac{1}{x}\right)^{x}$ is

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21. The coefficient of variation of two distribution are 60 and 70. The standard deviations are 21 and 16 respectively, then their mean is

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22. If $x, y, z$ are all different and not equal to
zero and

$$
\begin{aligned}
& \left|\begin{array}{lll}
1+x & 1 & 1 \\
1 & 1+y & 1 \\
1 & 1 & 1+z
\end{array}\right|=0 \text { then the value } \\
& \text { of } x^{-1}+y^{-1}+z^{-1} \text { is equal to }
\end{aligned}
$$

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23. If $x=2+3 \cos \theta$ and $y=1-3 \sin \theta$ represent a circle then the centre and radius is

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24. If $\sin ^{-1} x+\sin ^{-1} y=\frac{\pi}{2}$, then $x^{2}$ is equal to

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25. If $\tan ^{-1}\left(x^{2}+y^{2}\right)=\alpha$ then $\frac{d y}{d x}$ is equal to

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26. The vector equation of the plane which is
at a distance of $3 / \sqrt{14}$ from the origin and
the normal from the origin is $2 \hat{i}-3 \hat{j}+\hat{k}$ is

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27. The equation of the normal to the curve $y\left(1+x^{2}\right)=2-x \quad$ where the tangent crosses x - axis is

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28. Find the value of $\tan \frac{\pi}{8}$.

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29. The real part of $(1-\cos \theta+I \sin \theta)^{-1}$ is

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30. If $x^{m} y^{n}=(x+y)^{m+n}$ then $\frac{d y}{d x}$ is equal to

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31. The differential coefficient of $\log _{10} x$ with respect to $\log _{x} 10$ is

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32. $\int_{0}^{\pi / 2} \frac{\sin ^{1000} x d x}{\sin ^{1000} x+\cos ^{1000} x}$ is equal to

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33. The value of
$f e^{x} \frac{x^{2} \tan ^{-1} x+\tan ^{-1} x+1}{x^{2}+1} d x$ is equal to

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34. The $11^{\text {th }}$ term in the expansion of
$\left(x+\frac{1}{\sqrt{x}}\right)^{14}$ is
35. The general solution of $\cot \theta+\tan \theta=2$ is

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36. If $A=\left[\begin{array}{ll}\cos 2 \text { thet } & -\sin 2 \theta \\ \sin 2 \theta & \cos 2 \theta\end{array}\right]$ and
$A+A^{T}=1$, where I is the unit matrix of
$2 \times 2 \& A^{T}$ is the transpose of A . then the value of $\theta$ is equla to

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37. If A is matrix of order $m \times n$ and B is a matrix such that $A B^{\prime}$ and $B^{\prime} A$ are both defined, the order of the matrix $B$ is

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38. The value of $1 \sin ^{-1}\left(\frac{\cos (53 \pi)}{5}\right)$ is

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39. If $2 \vec{a} \cdot \vec{b}=|\vec{a}| \cdot|\vec{b}|$ then the between $\vec{a}$ and $\vec{b}$ is
A. $90^{\circ}$
B. $30^{\circ}$
C. $60^{\circ}$
D. $45^{\circ}$

Answer: C
40. If $1+\sin \theta+\sin ^{2} \theta+\ldots$ upto $\infty 2 \sqrt{3}+4$
, then $\theta=$

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41. The function $f(x)=[x]$ where $[x]$ is the greatest integer function is continous at
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42. Let $f: R \rightarrow R$ be defined by $f(x)=2 x+6$ which is bijective mapping then $f^{-1}(x)$ is given by

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43. If $\cos \alpha, \cos \beta, \cos \gamma$ are the direction cosines fo a vector $\vec{a}$, then $\cos 2 \alpha+\cos 2 \beta+\cos 2 \gamma$ is equal to
44. Write the converse and contrapositive of the statement " If $x$ is a prime number then $x$ is odd "
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45. The value of $\int_{-\pi / 4}^{\pi / 4} \sin ^{103} x \cdot \cos ^{101} x d x$ is
46. If $\mathrm{a}=3, \mathrm{~b}=4, \mathrm{c}=5$ each one of $\vec{a}, \vec{b}$ and
$\vec{c}$ is perpendicular to the sum of the remaining then $|\vec{a}+\vec{b}+\vec{c}|$ is equal to
A. $5 \sqrt{2}$
B. $\sqrt{2}$
C. $\frac{5}{\sqrt{2}}$
D. $\sqrt{5}$

Answer: A

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$\vec{a}+\vec{b}+\vec{c}=0,|\vec{a}|=3,|\vec{b}|=5,|\vec{c}|=7$
, then the angle between $\vec{a}$ and $\vec{b}$ is
A. $\frac{\pi}{3}$
B. $\frac{\pi}{2}$
C. $\pi$
D. $\frac{\pi}{4}$

Answer: A

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48. If $x^{y}=e^{x-y}$ then $\frac{d y}{d x}$ is equal to

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49. If $P(A \cap B)=7 / 10$ and $P(B)=17 / 20$, where P stands for probability then $P(A \mid B)$
is equal to

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50. Find a value of "x"for which $x(\hat{i}+\hat{j}+\hat{k})$
is a unit vector .

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51. If $y=e^{\sin ^{-1}\left(t^{2}-1\right)} \quad \& \quad x=e^{\sec -1\left(\frac{1}{t^{2-1}}\right)}$
then $\frac{d y}{d x}$ is equal to
52. If $A=\frac{1}{\pi}\left[\begin{array}{ll}\sin ^{-1}(x \pi) & \tan ^{-1}\left(\frac{x}{\pi}\right) \\ \sin ^{-1}\left(\frac{x}{\pi}\right) & \cot ^{-1}(\pi x)\end{array}\right]$
$B=\frac{1}{\pi}\left[\begin{array}{cc}-\cos ^{-1}(x \pi) & \tan ^{-1}\left(\frac{x}{\pi}\right) \\ \sin ^{-1}\left(\frac{x}{\pi}\right) & -\tan ^{-1}(\pi x)\end{array}\right]$
then $A-B$ is equal to :

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53. The slope of the tangent to the curve
$x=t^{2}+3 t-8, y=2 t^{2}-2 t-5 \quad$ at $\quad$ the
point $(2,-1)$ is

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54. The rate of change of area of a circle with respect to its radius at $r=2 \mathrm{cms}$ is

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55. IF $A=\left[\begin{array}{ll}3 & 1 \\ -1 & 2\end{array}\right]$ then $A^{2}-5 A$ is equal to
56. The value of the
$\sin 1^{\circ}+\sin 2^{\circ}+\ldots+\sin 359^{\circ}$ is equal to

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57. The order and degree of the differential equation

$$
\left[1+\left(\frac{d y}{d x}\right)^{2}+\sin \left(\frac{d y}{d x}\right)\right]^{3 / 4}=\frac{d^{2} y}{d x^{2}}
$$

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58. $\tan ^{-1}\left(\frac{x}{y}\right)-\tan ^{-1}\left(\frac{x-y}{x+y}\right)$ is

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59. The sum of $1^{\text {st }} \mathrm{n}$ terms of the series
$\frac{1^{2}}{1}+\frac{1^{2}+2^{2}}{1+2}+\frac{1^{2}+2^{2}+3^{2}}{1+2+3}+$.

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60. Two cards are drawn at randrom from a
pack of 52 cards. The probability of these two

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