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## MATHS

## BOOKS - V PUBLICATION

## APPLICATION OF INTEGRALS

## Question Bank

1. Find the area enclosed by the circle
$x^{2}+y^{2}=a^{2}$
2. Find the area enclosed by the ellipse $\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}=1$
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3. Find the area of the region bounded by the
curve $y=x^{2}$ and the line $y=4$

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4. Find the area of the region bounded by the circle $x^{2}+y^{2}=32$, line $\mathrm{y}=\mathrm{x}$, x -axis, in first quadrant

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5. Find the area of the region bounded by the ellipse $\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}=1$, the ordinates $\mathrm{x}=0$ and x= ae where

$$
b^{2}=a^{2}\left(1-e^{2}\right), e<1
$$

6. Find the area of the region bounded by the
curve
$y^{2}=x$
$x$-axis and the lines $x=1$ and $x=4$

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7. Find the area of the region bounded by
$y^{2}=9 x, x=2, x=4$ and the $x$-axis is the
first quadrant.
8. Find the area of the region bounded by
$x^{2}=4 y, y=2, y=4$
and the $y$-axis in the first quadrant?

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9. Find the area of the region bounded by the
ellipse $\frac{x^{2}}{16}+\frac{y^{2}}{9}=1$.
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10. Find the area of the region bounded by the ellipse $\frac{x^{2}}{4}+\frac{y^{2}}{9}=1$.

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11. Find the area of the smaller part of the circle $x^{2}+y^{2}=a^{2}$ cut off by the line $x=\frac{a}{\sqrt{2}}$
12. The area between $x=y^{2}$ and $\mathrm{x}=4$ is divided into two equal parts by the line $x=a$, find the value of $a$.

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13. Find the area of the region bounded by the
curve
$y=x^{2}$ and $y=|x|$
14. Find the area enclosed between the curve
$x^{2}=4 y$
and the line $x=4 y-2$

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15. Choose the correct answer. Area of the region bounded by the curve $y^{2}=4 x$, $y$-axis and the line $y=3$ is :
16. Choose the correct answer. Area lying in the first quadrant and bounded by the circle $x^{2}+y^{2}=4$ and the lines $\mathrm{x}=0$ and $\mathrm{x}=2$ is
A. pi/'
B. $\mathrm{pi} / 2^{\prime}$
C. 'pi/3'
D. 'pi/4'.

Answer: A

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17. Choose the correct answer. Area of the region bounded by the curve $y^{2}=4 x$, $y$-axis and the line $y=3$ is :
A. 2
B. 9/4'
C. $9 / 3^{\prime}$
D. 9/2'

Answer: B
18. Consider the parabolas $y=x^{2}$ and $y^{2}=x$.

Find the area of the region bounded by the two parabolas.

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19. Using integration, find the area of the region bounded by the triangle whose vertices are $\{1,0\},\{2,2\}$ and $\{3,1\}$
20. Choose the correct answer. Smaller area enclosed by the circle $x^{2}+y^{2}=4$ and the line $x+y=2$ is:
A. $2(\mathrm{pi}-2)^{\prime}$
B. pi-2'
C. $2(\mathrm{pi}-1)^{\prime}$
D. $2(\mathrm{pi}+2)^{\prime}$

Answer: B

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21. Choose the correct answer. Area lying between the curves $y^{2}=4 x$ and $\mathrm{y}=2 \mathrm{x}$ is :
A. $2 / 3$
B. $1 / 3$
C. 1/4
D. 3/4

Answer: B
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22. Find the area of the parabola $y^{2}=4 a x$ bounded by its latus rectum.

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23. Find the area of the region bounded by the
line $y=3 x+2$, the $x$-axis and the ordinates
$x=-1$ and $x=1$.
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24. Find the area bounded by the curve $y=\cos x$ between $x=0$ and $x=2 \pi$

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25. Find the area under the given curves a given line :
$y=x^{2}, x=1, x=2$ and x -axis

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26. Find the area between the curves $y=x$ and $y=x^{2}$.

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27. Find the area of the region lying in the first quadrant and bounded by
$y=4 x^{2} x=0, y=1$ and $\mathrm{y}=4$.

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28. Sketch the graph of $y=|x+3|$ and
evaluate $\int_{-6}^{0}|x+3| \mathrm{dx}$.

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29. Find the area bounded by the curve $y=\sin x$ with x -axis, between $\mathrm{x}=0$ and $x=2 \pi$
30. Find the area enclosed between the parabola $y^{2}=4 a x$ and the line $\mathrm{y}=\mathrm{mx}$.


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31. Find the area of the smaller region bounded by the ellipse $\frac{x^{2}}{9}+\frac{y^{2}}{4}=1$ and the line $\frac{x}{3}+\frac{y}{2}=1$.

32. Find the area of the smaller region
bounded by the ellipse $\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}=1$ and the line $\frac{x}{a}+\frac{y}{b}=1$.

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33. Using the method of integration find area bounded by the curve $|x|+|y|=1$

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34. Find the area of the region bounded by the

## curve

$y=x^{2}$ and $y=|x|$

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35. Area bounded by the curve $y=x^{3}$, the $x$ axis and the ordinates $x=-2$ and $x=1$ is
a) -9 b) $-\frac{15}{4}$ c) $\frac{15}{4}$ d) $\frac{17}{4}$ A. -9'.
B. $-(15) / 4$
C. (15)/4'.
D. (17)/4'

## Answer: D

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36. The area bounded by the curve $y=x|x|, x$
-axis and the ordinates $x=-1$ and $x=1$ is given by:
A. 0
B. $1 / 3$
C. $23^{\prime}$
D. 43'.

## Answer: C

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37. Find the area of the circle,
$x^{2}+y^{2}=16$
which Is exterior to parabola
$y^{2}=6 x$
A. $4 / 3(4 \mathrm{pi} /-\mathrm{sqr} 3)^{\prime}$
B. $4 / 3(4 \mathrm{pi} /+\mathrm{sqrt} 3)^{\prime}$
C. 4/3(8 pi/-sqrt3)'
D. 4/3(8 pi/+sqrt3)'

Answer: C

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38. The area bounded by the $y$-axis, $y=\cos x$ and
$y=\sin x$ when
$0 \leq x \leq \frac{\pi}{2}$
A. 2(sqrt2-1)'
B. sqrt2-1'
C. sqrt2+4'
D. sqrt2'

Answer: B

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39. The area bounded by the curve $y=f(x), x$-axis and the line $\mathrm{x}=\mathrm{a}$ and $\mathrm{x}=\mathrm{b}$ is ?
40. Find the area of the region bounded by $y^{2}=4 x, x=1, x=4$ and $x$-axis in the first quadrant.

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41. Find the area bounded by the curve $y=\sin x$ with x -axis, between $\mathrm{x}=0$ and $x=2 \pi$
42. Find the area of the smaller part of the circle $x^{2}+y^{2}=a^{2}$ cut off by the line $x=\frac{a}{\sqrt{2}}$

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43. Find the area of the region bounded by the
curve
$y=x^{2}$ and $y=|x|$
44. Find the area included between the curves
$x^{2}=4 y$ and $y^{2}=4 x$

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45. Find the area of the region bounded by $y=2 x+1, y=3, y=5$ and the $y$ axis.

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