



MATHS

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DETERMINANTS

Exercise

1. If $A^2 - A + I = 0, A^{-1} = ?$



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2. Consider $\Delta = \begin{vmatrix} \alpha & \beta & \gamma \\ \alpha^2 & \beta^2 & \gamma^2 \\ \beta + \gamma & \gamma + \alpha & \alpha + \beta \end{vmatrix}$ Apply

$$R_3 \rightarrow R_1 + R_3$$



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3. Consider $\Delta = \begin{vmatrix} \alpha & \beta & \gamma \\ \alpha^2 & \beta^2 & \gamma^2 \\ \beta + \gamma & \gamma + \alpha & \alpha + \beta \end{vmatrix}$ Show

that $\Delta = (\alpha - \beta)(\beta - \gamma)(\gamma - \alpha)(\alpha + \beta + \gamma)$.



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4. If $\begin{vmatrix} 3 & x \\ x & x \end{vmatrix} = \begin{vmatrix} -2 & 2 \\ 4 & 1 \end{vmatrix}$, find the value of x.



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5. $A = \begin{bmatrix} 1 & -3 & 1 \\ 2 & 0 & 4 \\ 1 & 2 & -2 \end{bmatrix}$

Calculate $|A|$



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6. $A = \begin{bmatrix} 1 & -3 & 1 \\ 2 & 0 & 4 \\ 1 & 2 & -2 \end{bmatrix}$ Find $|\text{adj } A|$

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$$7. A = \begin{bmatrix} 1 & -3 & 1 \\ 2 & 0 & 4 \\ 1 & 2 & -2 \end{bmatrix}$$

Find $|3A|$

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$$8. \text{ If } A = \begin{bmatrix} 1 & 2 \\ 4 & 2 \end{bmatrix} \text{ then show that } |2A| = 4|A|$$

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9. If $\begin{vmatrix} x & 2 \\ 18 & x \end{vmatrix} = \begin{vmatrix} 6 & 2 \\ 18 & 6 \end{vmatrix}$, then $x =$



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10. Without expanding the determinant prove the following.

$$\begin{vmatrix} a - b & b - c & c - a \\ b - c & c - a & a - b \\ c - a & a - b & b - c \end{vmatrix} = 0$$



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11. If a, b, c are in A.P, find value of

$$\begin{vmatrix} 2y + 4 & 5y + 7 & 8y + a \\ 3y + 5 & 6y + 8 & 9y + b \\ 4y + 6 & 7y + 9 & 10y + c \end{vmatrix}$$



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12. Find the value of k if the area of a triangle with vertices $(k, 4), (2, -6)$ and $(5, 4)$ is 35 square unit.



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13. If $\begin{bmatrix} 2 & 5 \\ -3 & 7 \end{bmatrix} \times A = \begin{bmatrix} 17 & -1 \\ 47 & -13 \end{bmatrix}$ then

Find the 2x2 matrix A.



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14. If $\begin{bmatrix} 2 & 5 \\ -3 & 7 \end{bmatrix} \times A = \begin{bmatrix} 17 & -1 \\ 47 & -13 \end{bmatrix}$ then

Find A^2 .



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15. Using properties of determinants show

that

$$\begin{vmatrix} 1+a & 1 & 1 \\ 1 & 1+b & 1 \\ 1 & 1 & 1+c \end{vmatrix} = abc \left(1 + \frac{1}{a} + \frac{1}{b} + \frac{1}{c} \right)$$



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16. Consider the point

$$A(-2, -3), B(3, 2), C(-1, -8)$$

Find the area of ΔABC



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17. Consider the point `A(-2,-3),B(3,2),C(-1,-8)

Find third vertex of any other triangle with same area and base AB



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18. If $A = \begin{bmatrix} 2 & -3 \\ 4 & 6 \end{bmatrix}$. Find adj A.



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19. If $A = \begin{bmatrix} 2 & -3 \\ 4 & 6 \end{bmatrix}$. Find A^{-1} .



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20. Given $\Delta = \begin{vmatrix} y+z & x & y \\ z+x & z & x \\ x+y & y & z \end{vmatrix}$ Apply

$$R_1 \rightarrow R_1 + R_2 + R_3.$$



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21. Given $\Delta = \begin{vmatrix} y+z & x & y \\ z+x & z & x \\ x+y & y & z \end{vmatrix}$ Take $(x+y+z)$

common from R_1 .



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22. Given $\Delta = \begin{vmatrix} y + z & x & y \\ z + x & z & x \\ x + y & y & z \end{vmatrix}$ Perform

$$C_1 \rightarrow C_1 - 2C_3, C_2 \rightarrow C_2 - C_3$$



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23. Given $\Delta = \begin{vmatrix} y + z & x & y \\ z + x & z & x \\ x + y & y & z \end{vmatrix}$ Prove that

$$\Delta = (x + y + z)(x - z)^2.$$



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24. Let $A = \begin{bmatrix} -1 & 2 & 4 \\ 1 & 1 & 3 \\ 3 & 2 & 3 \end{bmatrix}$ Find $|A|$.

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25. Let $A = \begin{bmatrix} -1 & 2 & 4 \\ 1 & 1 & 3 \\ 3 & 2 & 3 \end{bmatrix}$ Find $\text{Adj } A$.

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26. Let $A = \begin{bmatrix} -1 & 2 & 4 \\ 1 & 1 & 3 \\ 3 & 2 & 3 \end{bmatrix}$ Verify that $A \cdot \text{Adj } A = |A| \cdot I$

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27. Consider $A = \begin{bmatrix} 4 & 1 \\ 5 & 3 \end{bmatrix}$. Find A^{-1} and A^T



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28. Consider $A = \begin{bmatrix} 4 & 1 \\ 5 & 3 \end{bmatrix}$. Verify
 $(A^T)^{-1} = (A^{-1})^T$.



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29. Let $A = \begin{bmatrix} 1 & 4 & 0 \\ -1 & 2 & 2 \\ 0 & 0 & 2 \end{bmatrix}$ Is A singular?

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30. Let $A = \begin{bmatrix} 1 & 4 & 0 \\ -1 & 2 & 2 \\ 0 & 0 & 2 \end{bmatrix}$ Find Adj A.

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31. Let $A = \begin{bmatrix} 1 & 4 & 0 \\ -1 & 2 & 2 \\ 0 & 0 & 2 \end{bmatrix}$ Find A^{-1}

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32. Evaluate $\begin{vmatrix} x & y & x + y \\ y & x + y & x \\ x + y & x & y \end{vmatrix}$



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33. Let $A = \begin{bmatrix} 1 & \sin \theta & 1 \\ -\sin \theta & 1 & \sin \theta \\ -1 & -\sin \theta & 1 \end{bmatrix}$, where

$$0 \leq \theta \leq 2\pi$$

Then



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34. Consider the system of equations $x - y + z = 3, 2x + y - z = 2, -x - 2y + 2z = 1$. Convert this system of equations in the standard form $AX=B$.



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35. Consider the system of equations $x - y + z = 3, 2x + y - z = 2, -x - 2y + 2z = 1$. Is A invertible?



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36. Given $\Delta = \begin{vmatrix} x & x^2 & 1 + px^3 \\ y & y^2 & 1 + py^3 \\ z & z^2 & 1 + pz^3 \end{vmatrix}$ Express this as sum of two determinants.

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37. Given $\Delta = \begin{vmatrix} x & x^2 & 1 + px^3 \\ y & y^2 & 1 + py^3 \\ z & z^2 & 1 + pz^3 \end{vmatrix}$ Prove that $\Delta = (1 + pxyz)(x - y)(y - z)(z - x)$.

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38. Ashok purchased 3 pencils, 2 instrument boxes and 1 pen and paid Rs 41. From the same shop, Babu purchased 2 pencils, 1 instrument box and 2 pens and paid Rs 29 while Rajesh purchased 2 pencil, 2 instrument boxes and 2 pens and paid Rs.44. Formulate the problem into a system of linear equations.



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39. Ashok purchased 3 pencils, 2 instrument boxes and 1 pen and paid Rs 41. From the same

shop, Babu purchased 2 pencils, 1 instrument box and 2 pens and paid Rs 29 while Rajesh purchased 2 pencil, 2 instrument boxes and 2 pens and paid Rs.44. Find the cost of 1 pencil, 1 instrument box and 1 pen.



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40. If $A = \begin{bmatrix} 1 & 2 & -3 \\ 2 & 3 & 2 \\ 3 & -3 & -4 \end{bmatrix}$ Is A non-singular?

Why?



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41. If $A = \begin{bmatrix} 1 & 2 & -3 \\ 2 & 3 & 2 \\ 3 & -3 & -4 \end{bmatrix}$ find A^{-1} .



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42. If $A = \begin{bmatrix} 1 & 2 & -3 \\ 2 & 3 & 2 \\ 3 & -3 & -4 \end{bmatrix}$ Solve the system of

linear equations $x+2y-3z=-4$, $2x+3y+2z=2$, $3x-3y-4z=11$



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43. If $A^{-1} = \begin{bmatrix} 3 & -1 & 1 \\ -15 & 6 & -5 \\ 5 & -2 & 2 \end{bmatrix}$ and

$B = \begin{bmatrix} 1 & 2 & -2 \\ -1 & 3 & 0 \\ 0 & -2 & 1 \end{bmatrix}$ find $(AB)^{-1}$



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44. If $\begin{vmatrix} 1 & -3 & 2 \\ 4 & -1 & 2 \\ 3 & 5 & 2 \end{vmatrix} = 40$, then $\begin{vmatrix} 1 & 4 & 3 \\ -3 & -1 & 5 \\ 2 & 2 & 2 \end{vmatrix} =$

A. 0

B. -40

C. 40

D. 2

Answer:



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45.

Show

that

$$\Delta = \begin{vmatrix} -a^2 & ab & ac \\ ba & -b^2 & bc \\ ac & bc & -c^2 \end{vmatrix} = 4a^2b^2c^2$$



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46. Let the value of a determinant is Δ .

Then the value of a determinant obtained by interchanging two rows is

A. Δ

B. $-\Delta$

C. 0

D. 1

Answer:



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47.

Show

that

$$\begin{vmatrix} a+b & b+c & c+a \\ b+c & c+a & a+b \\ c+a & a+b & b+c \end{vmatrix} = 2 \begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$$


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48. The value of the determinant

$$\begin{vmatrix} \sin 10 & -\cos 10 \\ \sin 50 & \cos 50 \end{vmatrix} \text{ is a) } -1 \text{ b) } \frac{\sqrt{3}}{2} \text{ c) } \frac{1}{2} \text{ d) } -2$$

A. -1

B. $\frac{\sqrt{3}}{2}$ C. $\frac{1}{2}$

D. -2

Answer:



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49. Using properties of determinants,

show that

$$\begin{vmatrix} a & a^2 & b + c \\ b & b^2 & c + a \\ c & c^2 & a + b \end{vmatrix} = (b - c)(c - a)(a - b)(a + b + c)$$



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50. Choose the correct answer from the

bracket. The value of the determinant

$$\begin{vmatrix} 0 & p - q & p - r \\ q - p & 0 & q - r \\ r - p & r - q & 0 \end{vmatrix} \text{ is}$$

A. $p+q+r$

B. 1

C. 0

D. $3pqr$

Answer:



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51. Consider
$$\begin{vmatrix} a & a + b & a + b + c \\ 2a & 3a + 2b & 4a + 3b + 2c \\ 3a & 6a + 3b & 10a + 6b + 3c \end{vmatrix}$$



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52. Choose the correct answer from the

bracket. Consider a square matrix of

order 3. Let C_{11}, C_{12}, C_{13} are cofactors

of the elements a_{11}, a_{12}, a_{13}

respectively, then

$$a_{11}C_{11} + a_{12}C_{12} + a_{13}C_{13} \text{ is}$$

A. 0

B. $|A|$

C. 1

D. none of these

Answer:



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53. Verify $A(\text{adj}A) = (\text{adj}A)A = |A|I$ for the

matrix $A = \begin{bmatrix} 5 & -2 \\ 3 & -2 \end{bmatrix}$ that, where $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$



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54. Choose the correct answer from the bracket.

If $A = \begin{bmatrix} \cos x & \sin x \\ -\sin x & \cos x \end{bmatrix}$ and

$A(\text{adj}A) = k \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$, then the value of k is a)0

b)3 c)1 d)2

A. 0

B. 3

C. 1

D. 2

Answer:



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55. Find the inverse of the following

$$A = \begin{bmatrix} 1 & -1 & 2 \\ 0 & 2 & -3 \\ 3 & -2 & 4 \end{bmatrix}$$



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56. If $A = \begin{bmatrix} 2 & 3 \\ 1 & -2 \end{bmatrix}$ and $A^{-1} = kA$, then

the value of 'k' is

A. 7

B. -7

C. $\frac{1}{7}$

D. $-\frac{1}{7}$

Answer:



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57. If $A = \begin{bmatrix} 1 & -1 & 1 \\ 2 & -1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$,

Find A^2



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58. If $A = \begin{bmatrix} 1 & -1 & 1 \\ 2 & -1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$,

Show that $A^2 = A^{-1}$



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59. Choose the correct answer. If each element of a third order square matrix 'A' is multiplied by 3, then the determinant of the newly formed matrix is

a) $9|A|$ b) $3|A|$ c) $27|A|$ d) $(|A|)^3$

A. $9|A|$

B. $3|A|$

C. $27|A|$

D. $(|A|)^3$

Answer:



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60. Consider the matrix $A = \begin{bmatrix} -8 & 5 \\ 2 & 4 \end{bmatrix}$ Show that 'A' satisfies the equation $x^2 + 4x - 42 = 0$



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61. Consider the matrix $A = \begin{bmatrix} -8 & 5 \\ 2 & 4 \end{bmatrix}$ Hence find A^{-1} .



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62. If A and B are matrices of order 3 such that $|A| = -1, |B| = 3$, then $|3AB|$ is

- A. -9
- B. -27
- C. -81
- D. 9

Answer:



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63. If $A = \begin{bmatrix} 1 & \tan x \\ -\tan x & 1 \end{bmatrix}$, Show that,

$$A^T A^{-1} = \begin{bmatrix} \cos 2x & -\sin 2x \\ \sin 2x & \cos 2x \end{bmatrix}.$$



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64. If $A = \begin{bmatrix} 1 & 1 & 5 \\ 0 & 1 & 3 \\ 0 & -1 & -2 \end{bmatrix}$

what is the value of $|3A|$?





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65. Find the equation of the line joining the points (1,2) and (-3,-2) using determinants.



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66. Find the values of x in which

$$\begin{vmatrix} 3 & x \\ x & 1 \end{vmatrix} = \begin{vmatrix} 3 & 2 \\ 4 & 1 \end{vmatrix}$$



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67. Using the property of determinants, show

that the points

$A(a, b + c), B(b, c + a), C(c, a + b)$ are

collinear.



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68. Examine the consistency of system of

following equations:

$$5x - 6y + 4z = 15$$

$$7x + y - 3z = 19$$

$$2x + y + 6z = 46$$



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69. If $A = \begin{bmatrix} 3 & -2 & 3 \\ 2 & 1 & -1 \\ 4 & -3 & 2 \end{bmatrix}$

Find $|A|$



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70. If $A = \begin{bmatrix} 3 & -2 & 3 \\ 2 & 1 & -1 \\ 4 & -3 & 2 \end{bmatrix}$

Find A^{-1}



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71. If $A = \begin{bmatrix} 3 & -2 & 3 \\ 2 & 1 & -1 \\ 4 & -3 & 2 \end{bmatrix}$

Solve the linear equations

$$3x - 2y + 3z = 8$$

$$2x + y - z = 1$$

$$4x - 3y + 2z = 4$$



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72. Arjun' purchased 3 pens,2 purses and 1 instrument box and pays Rs. 410. From the same shop 'Deeraj' purchases 2 pens,1 purse and 2

instrument boxes and pays Rs.290, while 'Sindhu' purchases 2pens,2 purses,2 instrument boxes and pays Rs. 440. Translate the equation into system of linear equations.



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73. Arjun' purchased 3 pens,2 purses and 1 instrument box and pays Rs. 410.From the same shop 'Deeraj' purchases 2 pens,1 purse and 2 instrument boxes and pays Rs.290,while 'Sindhu' purchases 2pens,2 purses,2 instrument boxes and pays Rs.

440.

The cost of one pen, one purse and one instrument box using matrix method.



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74. Write the value of $x + y + z$, if

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \\ 0 \end{bmatrix}$$



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75. Using properties of determinants prove the following.

$$\begin{vmatrix} b+c & a & a \\ b & c+a & b \\ c & c & a+b \end{vmatrix} = 4abc$$



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76. Consider the points $(b,c+a)$, $(c,a+b)$ and $(a,b+c)$. Find the area of the triangle formed by these points.



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77. Consider the points $(b, c+a)$, $(c, a+b)$ and $(a, b+c)$.

Are the given points collinear? Why?



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78. If $\Delta = \begin{bmatrix} a - b - c & 2a & 2a \\ 2b & b - c - a & 2b \\ 2c & 2c & c - a - b \end{bmatrix}$

Perform $R_1 \rightarrow R_1 + R_2 + R_3$ on Δ



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79. If $\Delta = \begin{bmatrix} a - b - c & 2a & 2a \\ 2b & b - c - a & 2b \\ 2c & 2c & c - a - b \end{bmatrix}$

Perform $R_1 \rightarrow R_1 + R_2 + R_3$ on Δ . Take $(a+b+c)$ common from R_1 & rewrite Δ .



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80. Using properties of determinants prove the following.

$$\begin{vmatrix} a - b - c & 2a & 2a \\ 2b & b - c - a & 2b \\ 2c & 2c & c - a - b \end{vmatrix} = (a + b + c)^3$$



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81. Given $\Delta = \begin{bmatrix} a + b & b + c & c + a \\ b + c & c + a & a + b \\ c + a & a + b & b + c \end{bmatrix}$ Express

given determinant as the sum of 8 determinants.



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82.

Show

that

$$\begin{vmatrix} a + b & b + c & c + a \\ b + c & c + a & a + b \\ c + a & a + b & b + c \end{vmatrix} = 2 \begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$$



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83. Find the equation of line joining (1,2) and (3,6) using determinants.



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84. Prove that $\begin{vmatrix} x & \sin \theta & \cos \theta \\ -\sin \theta & -x & 1 \\ \cos \theta & 1 & x \end{vmatrix}$ is

independent of θ



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85. Prove that $\begin{vmatrix} x & \sin \theta & \cos \theta \\ -\sin \theta & -x & 1 \\ \cos \theta & 1 & x \end{vmatrix}$ is

independent of θ



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86. using properties of determinants, prove that

$$\begin{vmatrix} 1 & a & a^2 \\ 1 & b & b^2 \\ 1 & c & c^2 \end{vmatrix} = (a - b)(b - c)(c - a).$$



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87. If $A = \begin{bmatrix} 2 & -3 & 5 \\ 3 & 2 & -4 \\ 1 & 1 & -2 \end{bmatrix}$

Find A^{-1}



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88. If $A = \begin{bmatrix} 2 & -3 & 5 \\ 3 & 2 & -4 \\ 1 & 1 & -2 \end{bmatrix}$

Using it solve the system of equations

$$2x - 3y + 5z = 16$$

$$3x + 2y - 4z = -4$$

$$x + y - 2z = -3$$



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89. prove that
$$\begin{vmatrix} a & b & c \\ a + 2x & b + 2y & c + 2z \\ x & y & z \end{vmatrix} = 0$$



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90. if $A = \begin{bmatrix} 1 & -1 & 2 \\ 0 & 2 & -3 \\ 3 & -2 & 4 \end{bmatrix}$ $B = \begin{bmatrix} -2 & 0 & 1 \\ 9 & 2 & -3 \\ 6 & 1 & -2 \end{bmatrix}$

Prove that $B = A^{-1}$



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91. if

$$A = \begin{bmatrix} 1 & -1 & 2 \\ 0 & 2 & -3 \\ 3 & -2 & 4 \end{bmatrix} \quad B = \begin{bmatrix} -2 & 0 & 1 \\ 9 & 2 & -3 \\ 6 & 1 & -2 \end{bmatrix}$$

Using

A^{-1} solve the system of linear equation given

below: $x-y+2z=1$, $2y-3z=1$, $3x-2y+4z=2$



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92. If $A = \begin{bmatrix} a & 1 \\ 1 & 0 \end{bmatrix}$ is such that $A^2 = I$ then a

equals

A. 1

B. -1

C. 0

D. 2

Answer:



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93. Solve the system of equations

$$x - y + z = 4, 2x + y - 3z = 0, x + y + z = 2$$

Using matrix method



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94. The value of $\begin{vmatrix} x & x - 1 \\ x + 1 & x \end{vmatrix}$ is a) 1 b) x c) x^2 d) 0

A. 1

B. x

C. x^2

D. 0

Answer:



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95. Using properties of determinants prove the following.

$$\begin{vmatrix} 1 & x & x^2 \\ x^2 & 1 & x \\ x & x^2 & 1 \end{vmatrix} = (1 - x^3)^2$$



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96. Prove that

$$\begin{vmatrix} 1 & x & x^3 \\ 1 & y & y^3 \\ 1 & z & z^3 \end{vmatrix} = (x + y + z)(x - y)(y - z)(z - y)$$



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97. Prove that $\begin{vmatrix} 1! & 2! & 3! \\ 2! & 3! & 4! \\ 3! & 4! & 5! \end{vmatrix} = 4!$

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98. Solve the system of Linear equations

$$x + 2y + z = 8, 2x + y - z = 1, x - y + z = 2$$

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99. Inverse of the matrix $\begin{bmatrix} 0 & 1 & 2 \\ 0 & 1 & 1 \\ 1 & 0 & 2 \end{bmatrix}$





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100. Find the values of x in which

$$\begin{vmatrix} 3 & x \\ x & 1 \end{vmatrix} = \begin{vmatrix} 3 & 2 \\ 4 & 1 \end{vmatrix}$$



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101. Using the property of determinants, show

that the points

$A(a, b + c)$, $B(b, c + a)$, $C(c, a + b)$ are

collinear.



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102. Examine the consistency of system of following equations:

$$5x - 6y + 4z = 15$$

$$7x + y - 3z = 19$$

$$2x + y + 6z = 46$$



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103. Let B is a square matrix of order 5, then

$|kB|$ is equal to....

A. $|B|$

B. $K|B|$

C. $K^5|B|$

D. $5|B|$

Answer:



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104.

Prove

that

$$\begin{vmatrix} 1 & x & x^2 \\ 1 & y & y^2 \\ 1 & z & z^2 \end{vmatrix} = (x - y)(y - z)(z - x)$$



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105. Check the consistency of the following equations,

$$2x + 3y + z = 6, x + 2y - z = 2,$$

$$7x + y + 2z = 10$$



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106. If $\begin{vmatrix} x & 3 \\ 5 & 2 \end{vmatrix} = 5$, then $x = \dots$



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107. By using properties of determinants, prove that

$$\begin{vmatrix} y+k & y & y \\ y & y+k & y \\ y & y & y+k \end{vmatrix} = k^2(3y+k)$$



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108. Solve the following system of linear

Equations, using matrix method,

$$5x + 2y = 3, 3x + 2y = 5$$



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109. Find values of x if i) $\begin{vmatrix} 2 & 4 \\ 5 & 1 \end{vmatrix} = \begin{vmatrix} 2x & 4 \\ 6 & x \end{vmatrix}$ ii)

$$\begin{vmatrix} 2 & 3 \\ 4 & 5 \end{vmatrix} = \begin{vmatrix} x & 3 \\ 2x & 5 \end{vmatrix}$$



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110. Find the values of x , if $\begin{vmatrix} 2 & 3 \\ 4 & 5 \end{vmatrix} = \begin{vmatrix} x & 3 \\ 2x & 5 \end{vmatrix}$



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111. Using properties of determinants prove the following.

$$\begin{vmatrix} 1 & x & x^2 \\ x^2 & 1 & x \\ x & x^2 & 1 \end{vmatrix} = (1 - x^3)^2$$



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112. Find the adjoint of $B = \begin{bmatrix} 1 & -1 & 2 \\ 2 & 3 & 5 \\ -2 & 0 & 1 \end{bmatrix}$



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113. By using properties of determinants, prove that

$$\begin{vmatrix} x + 4 & 2x & 2x \\ 2x & x + 4 & 2x \\ 2x & 2x & x + 4 \end{vmatrix} = (5x + 4)(4 - x)^2$$



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114. Prove that

$$\begin{vmatrix} y + k & y & y \\ y & y + k & y \\ y & y & y + k \end{vmatrix} = k^2(3y + k)$$



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115. If $A = \begin{bmatrix} 1 & 2 \\ 4 & 2 \end{bmatrix}$ then show that $|2A| = 4|A|$



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116. Prove that

$$\begin{vmatrix} a - b - c & 2a & 2a \\ 2b & b - c - a & 2b \\ 2c & 2c & c - a - b \end{vmatrix} = (a + b + c)^3$$



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