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## MATHS

## BOOKS - MAXIMUM PUBLICATION

## APPLICATION OF INTEGRALS

Example

1. Consider the following figure
find the point of intersection ( $P$ ) of the
parabola and the line.


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2. using the given figure
find the area of the enclosed region


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3. Consider the following figure
find the point of intersection ( $P$ ) of the
parabola and the line.


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4. using the given figure
find the area of the enclosed region


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## 5. Consider the following figure

find the point of intersection $P$ of the circle
$x^{2}+y^{2}=32$
and the line $y=x$


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6. using the given figure
find the area of the enclosed region


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# 7. Shade the area enclosed by $x^{2}=4 y, y=2, y=4$ and the $y$-axis in the 

first quadrant?

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8. Find the area of the region bounded by
$x^{2}=4 y, y=2, y=4$
and the $y$-axis in the first quadrant?

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9. Draw a rough sketch of the graph of the
function
$y^{2}=4 x$

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10. Draw the graph of
$y^{2}=4 x$
and $\mathrm{y}=\mathrm{x}$ ?

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11. Find the points of intersection of $y^{2}=4 x$ and $\mathrm{y}=\mathrm{x}$ ?

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12. Draw the graph of the function $y=x^{2}$ and $x=y^{2}$ in a coordinate axis.

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13. Using the figure
find the area of the shaded region as the sum
of the area of two triangles

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## 14. Identify the function from the above graph



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## 15. Using the figure

verify the area of the shaded region using
integration


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16. The figure given below contains a straight
line $L$ with a slope
$\sqrt{8}$
and a circle

Find the point of intersection $P$.


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17. The figure given below contains a straight line $L$ with a slope
$\sqrt{8}$
and a circle
Find the point of intersection $P$.


## - Watch Video Solution

18. The figure given below contains a straight
line $L$ with a slope
$\sqrt{8}$
and a circle

Find the point of intersection $P$.


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## 19. Using the given figure

Define the equation of the circle and ellipse in
the figure .


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20. Using the given figure
find the area of the ellipse using integration


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21. Using the given figure
find the area of the shaded region (using
formula to find the area of the circle)

22. Find the area bounded by the curve $y=\sin x$ with x -axis, between $\mathrm{x}=0$ and $x=2 \pi$

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23. Find the area of the region bounded by the
curve
$y=x^{2}$ and $y=|x|$

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24. Consider the functions $f(x)=\sin x$ and $g(x)=\cos x$ in the interval
$[0,2 \pi]$
draw the rough sketch of the above function ?

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25. Consider the functions $f(x)=\sin x$ and
$g(x)=\cos x$ in the interval
$[0,2 \pi]$
find the area enclosed by these curves in the given interval ?

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26. Evaluate
$\int_{o}^{r} \sqrt{r^{2}-x^{2}} d x$
,where $r$ is a fixed positive number .Hence prove the area of the circle of radius $r$ is $\pi r^{2}$

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27. Find the area of the circle,
$x^{2}+y^{2}=16$
which Is exterior to parabola
$y^{2}=6 x$

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28. Using the figure
define the equation of ellipse and circle in the

## given figure



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29. Using the figure
find the area of ellipse using integration


## 30. Using the figure

find the area of the shaded region(Area of the
circle can be found by direct formula)


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31. The area bounded by the curve $y=f(x), x$-axis and the line $x=a$ and $x=b$ is ?

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32. Find the area enclosed between parabola
$y=x^{2}$
and the straight line $2 x-y+3=0$

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33. Find the area enclosed between the curve $x^{2}=4 y$
and the line $x=4 y-2$

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34. Area of the shaded portion in the figure is
equal to

A. $\int_{d}^{c} f(x) d x$
B. $\int_{c}^{d} f(x) d x$
C. $\int_{d}^{c} f(y) d x$
D. $\int_{c}^{d} f(y) d x$

## Answer: D

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35. Consider the curves
$y=x^{3}, \mathrm{x}=0, \mathrm{y}=1, \mathrm{y}=4$

Draw a rough sketch and shade the region bounded by these curves, Find area of the shaded region

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## 36. Consider the following figure

find the point of intersection $P$ of the circle
$x^{2}+y^{2}=32$
and the line $y=x$

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37. using the given figure
find the area of the enclosed region


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38. The area bounded by the curve above the
$x$-axis, between $x=a$ and $x=b$ is
A. $\int_{f(a)}^{b} y d y$
B. $\int_{a}^{f(b)} y d y$
C. $\int_{a}^{b} x d y$
D. $\int_{a}^{b} y d x$

## Answer: D

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39. Find the area of the circle
$x^{2}+y^{2}=4$
using integration
40. The area bounded by $y=2 \cos x$, the $x$ axis from $\mathrm{x}=0$ to $\left.\left.\left.x=\frac{\pi}{2} . \mathrm{a}\right) 0 \mathrm{~b}\right) 1 \mathrm{c}\right) 2 \mathrm{~d}$ )-1
A. 0
B. 1
C. 2
D. -1

Answer: C
41. Find the area of the region bounded by the $y^{2}=4 a x$ and $x^{2}=4 a y, \mathrm{a}>0$

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42. Consider the circle
$x^{2}+y^{2}=16$
and the straight line
$y=\sqrt{3} x$
as shown in the figure

Find the points $A$ and $B$ as shown in the figure

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43. Consider the circle
$x^{2}+y^{2}=16$
and the straight line
$y=\sqrt{3} x$
as shown in the figure
find the area of the shaded region in the figure using definite integrals

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44. Draw the rough sketch of
$\frac{x^{2}}{4}+\frac{y^{2}}{9}=1$

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45. Find the area enclosed between the curve
$y^{2}=x$
, $x=1, x=4$ and $x$-axis

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46. Using integration, find the area of the region bounded by the triangle whose vertices are $\{1,0\},\{2,2\}$ and $\{3,1\}$

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47. Using the given figure

Find the equation of $A B$


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48. Using the given figure

Find the equation of $A B$


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49. Find area of the shaded region using
integration.


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50. Consider the ellipse
$\frac{x^{2}}{9}+\frac{y^{2}}{4}=1$
and the line
$\frac{x}{3}+\frac{y}{2}=1$

Find the points where the line intersects the ellipse?

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51. Consider the ellipse
$\frac{x^{2}}{9}+\frac{y^{2}}{4}=1$
and the line
$\frac{x}{3}+\frac{y}{2}=1$
shade the smaller region bounded by the ellipse and the line?

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52. Consider the ellipse
$\frac{x^{2}}{9}+\frac{y^{2}}{4}=1$
and the line
$\frac{x}{3}+\frac{y}{2}=1$
find the area of the shaded region?

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53. Consider the function
$f(x)=|x|-1, g(x)=1-|x|$
sketch the graph and shade the enclosed

## region between them

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54. Consider the function
$f(x)=|x|-1, g(x)=1-|x|$
Find the area of the shaded region

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55. using the given figure
define the equation of the given curve


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56. using the given figure
find the area of the enclosed region


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57. using the given figure
find the area when $a=10$ and $b=5$
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