



MATHS

BOOKS - MAXIMUM PUBLICATION

THREE DIMENSIONAL GEOMETRY

Example

1. Consider the lines

$$\bar{r} = (\hat{i} + 2\hat{j} + 3\hat{k}) + \lambda(2\hat{i} - 3\hat{j} - 4\hat{k}),$$

$$\bar{r} = (\hat{i} + \hat{j} + \hat{k}) + \mu(\hat{i} + 3\hat{j} + 2\hat{k})$$

Write the Cartesian equation.



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2. Consider the lines

$$\bar{r} = (\hat{i} + 2\hat{j} + 3\hat{k}) + \lambda(2\hat{i} - 3\hat{j} - 4\hat{k}),$$

$$\bar{r} = (\hat{i} + \hat{j} + \hat{k}) + \mu(\hat{i} + 3\hat{j} + 2\hat{k})$$

Find the angle between the lines.



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3. Find the vector equation of the plane passing through the intersection of the planes

$$\bar{r} \cdot (\hat{i} + \hat{j} + \hat{k}) = 6 \quad \text{and}$$

$$\bar{r} \cdot (2\hat{i} + 3\hat{j} + 4\hat{k}) = -5 \text{ at the point } (1,1,1).$$



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4. Find the equation of the plane passing through the intersection of the planes

$$x + y + 4z + 5 = 0 \quad \text{and}$$

$2x - y + 3z + 6 = 0$ and contains the point $(1,0,0)$.



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5. Consider the point $(-1,-2,-3)$. In which octant ,the above point lies.



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6. Find the direction cosines of the line joining $(-1,-2,-3)$ and $(3,4,5)$.



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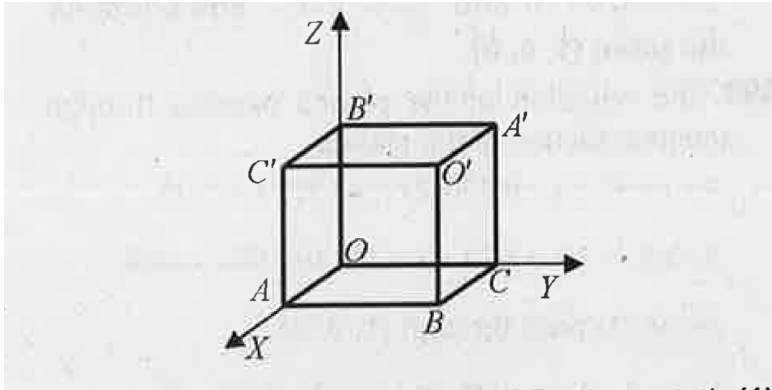
7. If P is any point such that $OP = \sqrt{50}$ and direction cosines of OP are $\frac{3}{\sqrt{50}}$, $\frac{4}{\sqrt{50}}$ and $\frac{5}{\sqrt{50}}$, then find the co-ordinate of P.



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8. Consider a cube of side 'a' unit has one vertex at the origin O.

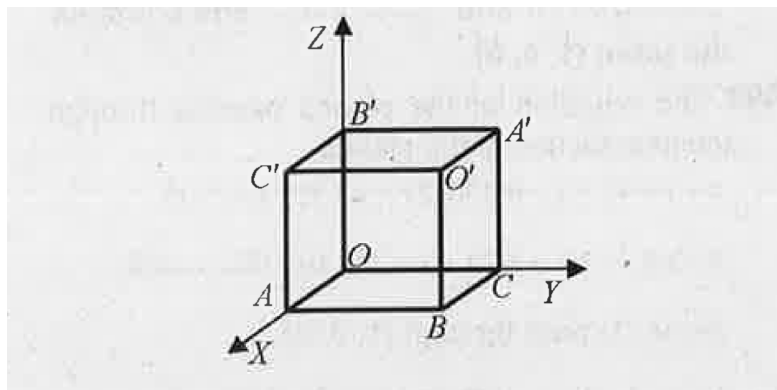
Write down the co-ordinate O , O' , A and A'



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9. Consider a cube of side ' a ' unit has one vertex at the origin O .

Find the direction ratios of OO' and AA' .

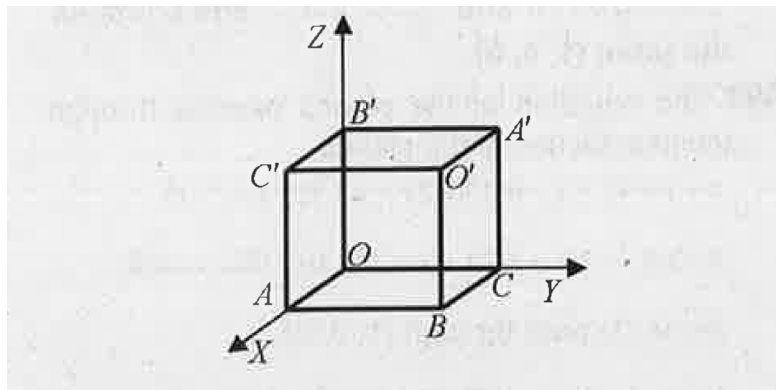


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10. Consider a cube of side 'a' unit has one vertex at the origin O.

Show that the angle between the main

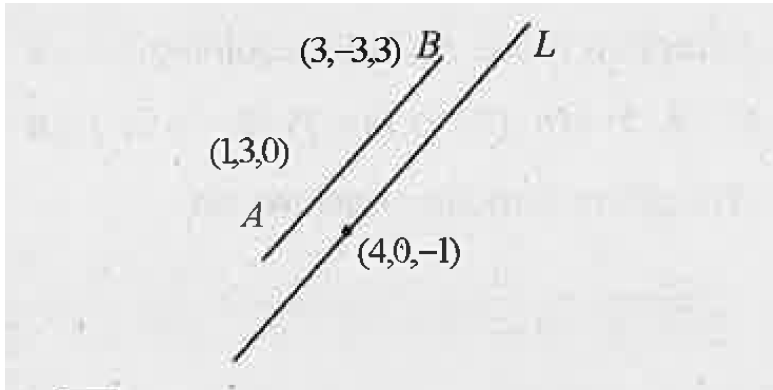
diagonals of the above cube is $\cos^{-1}\left(\frac{1}{3}\right)$



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11. Consider two points A and B and a line L as shown in figure.

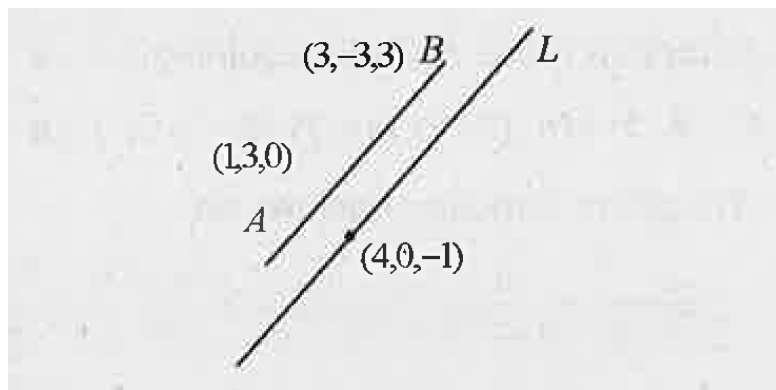
Find \overline{AB}



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12. Consider two points A and B and a line L as shown in figure.

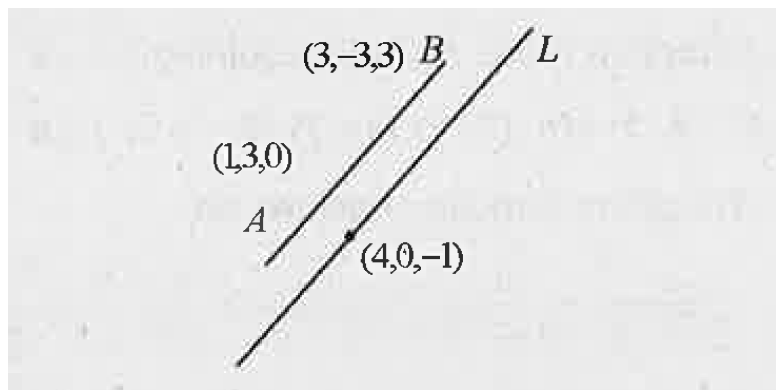
Find the Cartesian equation of the line L.



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13. Consider two points A and B on L1 and a line L2 as shown in figure. Find the foot of the perpendicular drawn from (2,3,4) on L1 to the

line L2.



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14. Cartesian equation of two lines are

$$\frac{x+2}{2} = \frac{y+2}{4} = \frac{z+2}{1},$$
$$\frac{x-1}{2} = \frac{y-1}{-3} = \frac{z-1}{-4}.$$

Write the vector

equation of the lines.



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15. Cartesian equation of two lines are

$$\frac{x+2}{2} = \frac{y+2}{4} = \frac{z+2}{1},$$
$$\frac{x-1}{2} = \frac{y-1}{-3} = \frac{z-1}{-4}.$$

find the shortest distance between the lines.



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16. Consider the points $P(1,3,4)$ & $Q(-3,5,2)$. Find the equation of the line passing through P and Q .



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17. Consider the points $(1,3,4)$ & $(-3,5,2)$. At which point that the above line cuts the plane $2x + y + z + 3 = 0$.



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18. Let the equation of a plane be $\vec{r} \cdot (2\hat{i} - 3\hat{j} + 5\hat{k}) = 7$, then find the Cartesian equation of the plane.



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19. Let the equation of a plane be $\bar{r} \cdot (2\hat{i} - 3\hat{j} + 5\hat{k}) = 7$, then find the equation of a plane passing through the point $(3,4,-1)$ and parallel to the given plane .



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20. Let the equation of a plane be $\bar{r} \cdot (2\hat{i} - 3\hat{j} + 5\hat{k}) = 7$, then find the

equation of a plane passing through the point $(3,4,-1)$ and parallel to the given plane .



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21. State the condition of the line $\bar{r} = \bar{a} + \lambda\bar{b}$ is parallel to the plane $\bar{r} \cdot \bar{n} = d$.



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22. Show that the line $\bar{r} = i + j + \lambda(2i + j + 4k)$ is parallel to the

plane $\bar{r} \cdot (-2i + k) = 5$.



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23. Find the distance between the line

$$\bar{r} = i + j + \lambda(2i + j + 4k) \text{ and the plane}$$

$$\bar{r} \cdot (-2i + k) = 5.$$



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24. If a line in the space makes angle α , β and

γ with the coordinates axes, then

$\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma$ is equal to a)1 b)2 c)0

d)3

A. 1

B. 2

C. 0

D. 3

Answer:



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25. The direction ratios of the line

$$\frac{x - 6}{1} = \frac{2 - y}{2} = \frac{z - 2}{2}$$

are a) 6,-2,-2 b) 1,2,2

c) 6,1,-2 d) 0,0,0

A. 6,-2,-2

B. 1,2,2

C. 6,1,-2

D. 0,0,0

Answer:



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26. If the vector equation of a line is

$$\bar{r} = i + j + k + \mu(2i - 3j - 4k) , \text{ then the}$$

Cartesian equation of the line is

A. $\frac{x + 2}{2} = \frac{y + 2}{4} = \frac{z + 2}{1}$

B. $\frac{x - 1}{2} = \frac{y - 1}{-3} = \frac{z - 1}{-4}$

C. $\frac{x + 2}{1} = \frac{y + 2}{4} = \frac{z + 2}{1}$

D. $\frac{x-1}{2} = \frac{y-1}{1} = \frac{z-1}{-4}$

Answer:



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27. If the Cartesian equation of a plane is $x + y + z = 12$, then the vector equation of the plane is.... a) $\bar{r} \cdot (2i + j + k) = 12$ b) $\bar{r} \cdot (i + j + k) = 12$ c) $\bar{r} \cdot (i + j + 2k) = 12$ d) $\bar{r} \cdot (i + 3j + k) = 12$

A. $\bar{r} \cdot (2i + j + k) = 12$

B. $\bar{r} \cdot (i + j + k) = 12$

C. $\bar{r} \cdot (i + j + 2k) = 12$

D. $\bar{r} \cdot (i + 3j + k) = 12$

Answer:



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28. Consider the lines

$$\bar{r} = (i + 2j - 2k) + \lambda(i + 2j)$$

$$\text{and } \bar{r} = (i + 2j - 2k) + \mu(2j - k)$$

Find the angles between the lines.



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29. Consider the lines

$$\bar{r} = (i + 2j - 2k) + \lambda(i + 2j)$$

$$\text{and } \bar{r} = (i + 2j - 2k) + \mu(2j - k)$$

Find a vector perpendicular to both the lines.



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30. Consider the lines

$$\bar{r} = (i + 2j - 2k) + \lambda(i + 2j)$$

$$\text{and } \bar{r} = (i + 2j - 2k) + \mu(2j - k)$$

Find the equation of the line passing through the point of intersection of lines and perpendicular to both the lines.



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31. Consider the line

$$\bar{r} = (2i - j + k) + \lambda(i + 2j + 3k).$$

Find the Cartesian equation of the line.



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32. Consider the line

$$\bar{r} = (2i - j + k) + \lambda(i + 2j + 3k)$$

Find the vector equation of the line passing through A (1,0,2) and parallel to the line.



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33. Consider the line

$$\bar{r} = (2i - j + k) + \lambda(i + 2j + 3k)$$

Write two points on the line obtained from vector equation of the line passing through A (1,0,2) and parallel to the line which are equidistant from A.



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34. Find the equation of the plane through the point $(1,2,3)$ and perpendicular to the plane

$$x - y + z = 2 \text{ and } 2x + y - 3z = 5$$



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35. Find the distance between the planes

$$x - 2y + 2z - 8 = 0 \text{ and } 6y - 3x - 6z = 57$$



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36. Consider the Cartesian equation of line

$$\frac{x - 3}{2} = \frac{y + 1}{3} = \frac{z - 5}{-2}$$
 Find the vector

equation of the line.



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37. Consider the Cartesian equation of line

$$\frac{x - 3}{2} = \frac{y + 1}{3} = \frac{z - 5}{-2}$$

Find its intersecting point with the plane

$$5x + 2y - 6z - 7 = 0$$



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38. Consider the Cartesian equation of line

$$\frac{x - 3}{2} = \frac{y + 1}{3} = \frac{z - 5}{-2}$$

Find the angle made by the line with the plane

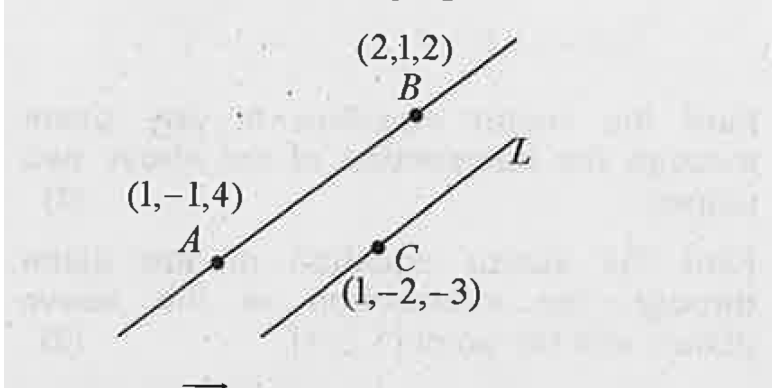
$$5x + 2y - 6z - 7 = 0$$



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39. From the following figure

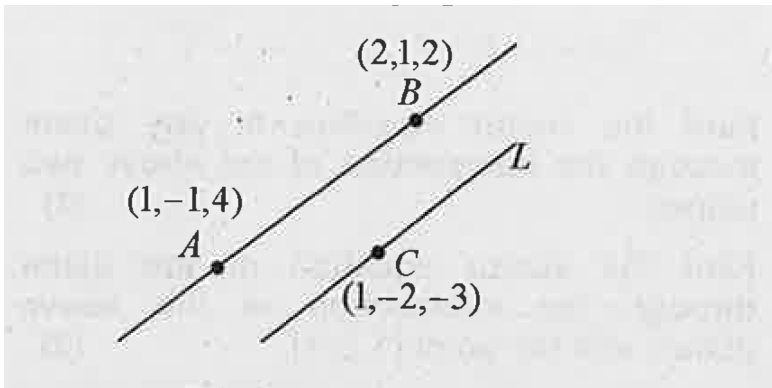
Find \overrightarrow{AB}



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40. From the following figure

Find the vector equation of line L .

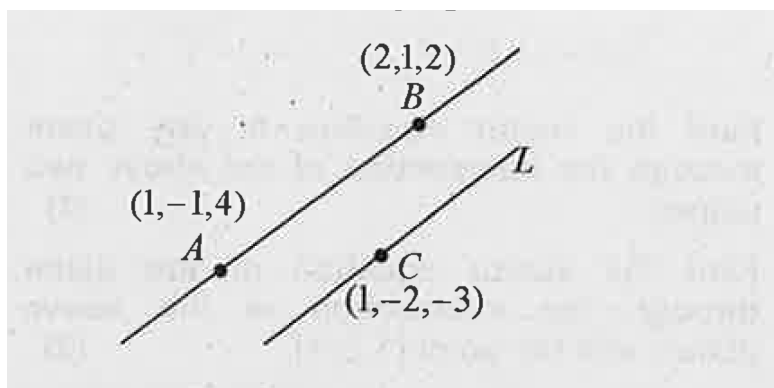




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41. From the following figure

Find a point on line L other than C .



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42. Find the vector equation of the plane which is at a distance of $\frac{6}{\sqrt{29}}$ from the origin with perpendicular vector $2i - 3j + 4k$. Convert into Cartesian form. Also find the foot of the perpendicular drawn from the origin to the plane.



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43. Consider the Plane $\bar{r} \cdot (-6i - 3j - 2k) + 1 = 0$. find the

direction cosines perpendicular to the plane and perpendicular distance from the origin.



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44. Consider three points $(6,-1,1)$, $(5,1,2)$ and $(1,-5,-4)$ on space. Find the Cartesian equation of the plane passing through these points .



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45. Consider three points $(6,-1,1)$, $(5,1,2)$ and $(1,-5,-4)$ on space. Find directions ratios normal to the Planes



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46. Consider three points $(6,-1,1)$, $(5,1,2)$ and $(1,-5,-4)$ on space. Find a unit vector normal to the plane.



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47. Consider a straight line through a fixed point with position vectors $2i-2j+3k$ and parallel to $i-j+4k$.

Write down the vector equation of the straight line.



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48. Consider a straight line through a fixed point with position vectors $2i-2j+3k$ and parallel to $i-j+4k$.

Show that the straight line is parallel to the plane $\bar{r} \cdot (i + 5j + k) = 5$



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49. Consider a straight line through a fixed point with position vectors $2i-2j+3k$ and parallel to $i-j+4k$.

Find the distance between the line and plane $\bar{r} \cdot (i + 5j + k) = 5$



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50. Consider the vector equation of two planes

$$\bar{r} \cdot (2i + j + k) = 3, \bar{r} \cdot (i - j - k) = 4$$

Find vector equation of any plane through the intersection of the above two planes.



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51. Consider the vector equation of two planes

$$\bar{r} \cdot (2i + j + k) = 3, \bar{r} \cdot (i - j - k) = 4$$

Find vector equation of the plane through the intersection of the above planes and the point

(1,2,-1).



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52. Distance of the point(0,0,1) from the plane

$$x + y + z = 3 \quad \text{a) } \frac{1}{\sqrt{3}} \text{ units} \quad \text{b) } \frac{2}{\sqrt{3}} \text{ units} \quad \text{c) } \sqrt{3}$$

$$\text{units d) } \frac{\sqrt{3}}{2} \text{ units}$$

A. $\frac{1}{\sqrt{3}}$ units

B. $\frac{2}{\sqrt{3}}$ units

C. $\sqrt{3}$ units

D. $\frac{\sqrt{3}}{2}$ units

Answer:



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53. Find the equation of the plane through the line of intersection of the planes $x+y+z=1$ and $2x+3y+4z=5$ which is perpendicular to $x-y+z=0$



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54. Consider a plane

$$\bar{r} \cdot (6i - 3j - 2k) + 1 = 0$$

Find dc's perpendicular to the plane.



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55. Consider a plane

$$\bar{r} \cdot (6i - 3j - 2k) + 1 = 0$$

Find a vector of magnitude 14 units perpendicular to given plane.



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56. Consider a plane

$\vec{r} \cdot (6i - 3j - 2k) + 1 = 0$. Find the equation of a line parallel to the above vector and passing through the point (1,2,1).



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57. Consider the pair of lines whose equations

are $\frac{x - 2}{2} = \frac{y - 1}{5} = \frac{z + 3}{-3}$ and

$$\frac{x + 1}{-1} = \frac{y - 4}{8} = \frac{z - 5}{4}$$

Write the direction ratios of the lines.





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58. Consider the pair of lines whose equations

are $\frac{x - 2}{2} = \frac{y - 1}{5} = \frac{z + 3}{-3}$ and

$$\frac{x + 1}{-1} = \frac{y - 4}{8} = \frac{z - 5}{4}$$

Find the shortest distance between the above skew lines.



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59. Consider the pair of lines whose equations

are $\frac{x - 2}{2} = \frac{y - 1}{5} = \frac{z + 3}{-3}$ and

$$\frac{x + 1}{-1} = \frac{y - 4}{8} = \frac{z - 5}{4}$$

Find the angle between these two lines.



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60. Consider the pair of lines

$$\bar{r} = 3i + 4j - 2k + \lambda(-i + 2j + k) \dots L_1,$$

$$\bar{r} = i - 7j - 2k + \mu(i + 3j + 2k) \dots L_2$$

Find one point each on lines L_1 and L_2 .



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61. Consider the pair of lines

$$\bar{r} = 3i + 4j - 2k + \lambda(-i + 2j + k) \dots L_1,$$

$$\bar{r} = i - 7j - 2k + \mu(i + 3j + 2k) \dots L_2$$

Find one point each on lines L_1 and L_2 .

Find the distance between those points.



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62. Consider the pair of lines

$$\bar{r} = 3i + 4j - 2k + \lambda(-i + 2j + k) \dots L_1,$$

$$\bar{r} = i - 7j - 2k + \mu(i + 3j + 2k) \dots L_2$$

Find the shortest distance between L_1 and L_2



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63. Consider the points $A(2,2,-1)$, $B(3,4,2)$ and $C(7,0,6)$ Are A,B and C collinear? Explain.



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64. Consider the points $A(2,2,-1)$, $B(3,4,2)$ and $C(7,0,6)$. Find the vector and Cartesian equation

of the plane passing these three points.



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65. Consider the points $A(2,2,-1)$, $B(3,4,2)$ and $C(7,0,6)$.

Find the vector and Cartesian equation of the plane passing these three points.

Find the angle between the above plane and the line $\bar{r} = (i + 2j - k) + \lambda(i - j + k)$



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66. Consider three points on space $(2,1,0)$, $(3,-2,-2)$ and $(3,1,7)$. Find the Cartesian equation of the plane passing through the above points.



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67. Consider three points on space $(2,1,0)$, $(3,-2,-2)$ and $(3,1,7)$. Find the Cartesian equation of the plane passing through the above points. Convert the equation into vector form.



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68. Consider three points on space $(2,1,0)$, $(3,-2,-2)$ and $(3,1,7)$

Find the Cartesian equation of the plane passing through the above points.

find a unit vector perpendicular to the plane and also find the perpendicular distance of the plane from the origin..



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$$69. \overline{OA} = i + 2j + 3k$$

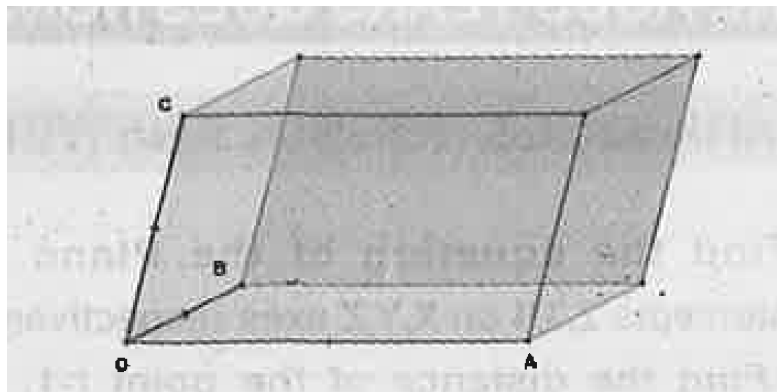
$$\overline{OB} = i - 2j + 4k$$

$$\overline{OC} = 2i + 3j + k$$

are adjacent sides of the parallelepiped.

Find the base area of the parallelepiped.

(Base determined by \overline{OA} and \overline{OB})



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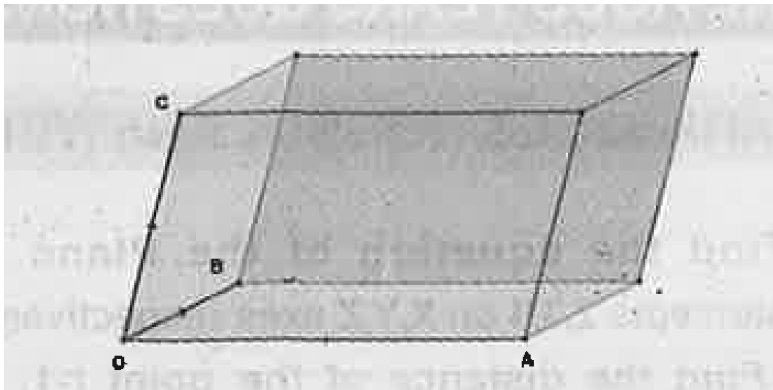
$$70. \overline{OA} = i + 2j + 3k$$

$$\overline{OB} = i - 2j + 4k$$

$$\overline{OC} = 2i + 3j + k$$

are adjacent sides of the parallelepiped.

Find the volume of the parallelepiped.



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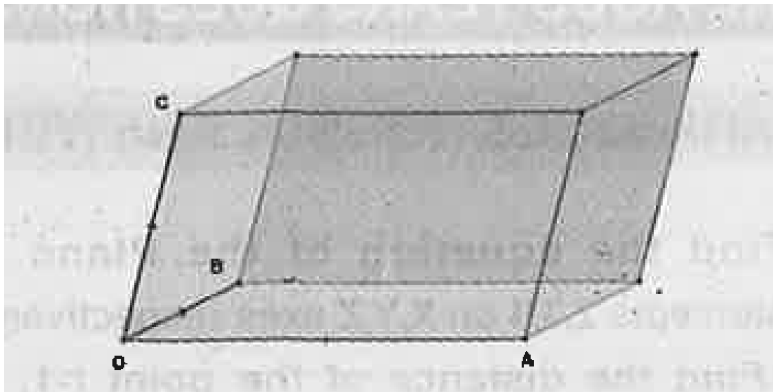
$$71. \overline{OA} = i + 2j + 3k$$

$$\overline{OB} = i - 2j + 4k$$

$$\overline{OC} = 2i + 3j + k$$

are adjacent sides of the parallelepiped.

Find the height of the parallelepiped.



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72. Find the equation of the line passing through the point $(2,1,0)$ and $(3,2,-1)$



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73. Find the equation of the line passing through the point $(2,1,0)$ and $(3,2,-1)$

Find the shortest distance of the line from the line

$$\bar{r} = (i - j + 2k) + \lambda(2i + j - 3k)$$



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74. The equation of two lines are

$$\frac{x - 1}{2} = \frac{y - 2}{2} = \frac{z - 3}{3} \quad \text{and}$$

$\frac{x}{-3} = \frac{y}{2} = \frac{z}{5}$, then Find the dr's of the given lines.



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75. The equation of two lines are

$$\frac{x - 1}{2} = \frac{y - 2}{2} = \frac{z - 3}{3} \quad \text{and}$$

$\frac{x}{-3} = \frac{y}{2} = \frac{z}{5}$, then Find the angle between the given lines.



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76. The equation of two lines are

$$\frac{x - 1}{2} = \frac{y - 2}{2} = \frac{z - 3}{3}$$

and

$$\frac{x}{-3} = \frac{y}{2} = \frac{z}{5}, \text{ then}$$

Find the equation of the line passing through (2,1,3) and perpendicular to the given lines.



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77. Find the direction cosine of the vector $2i+2j-k$.



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78. Find the distance of the point $(2,3,4)$ from the plane $\vec{r} \cdot (3i - 6j + 2k) = -11$.



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79. Find the shortest distance between the lines $\bar{r} = (2i - j - k) + \lambda(3i - 5j + 2k)$ and $\bar{r} = (i + 2j + k) + \mu(i - j + k)$



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80. Find the equation of the Plane with intercepts 2,3,4 on X,Y,Z axes respectively.



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81. Find the distance of the point $(-1,-2,3)$ from the Plane $\bar{r} \cdot (2i - 3j + 4k) = 4$



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82. Consider the points $A(2,2,-1)$, $B(3,4,2)$, $C(7,0,6)$. Find AB .



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83. Consider the points $A(2,2,-1)$, $B(3,4,2)$, $C(7,0,6)$. Find the Cartesian and vector equation of the plane passing through these points.



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84. Consider the points $A(3,-4,-5)$ and $B(2,-3,1)$. Find the vector and Cartesian equation of the line passing through the points A and B.



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85. Consider the points $A(3,-4,-5)$ and $B(2,-3,1)$

Find the point where the line crosses the XY Plane.



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86. Find the Cartesian equation of the plane passing through the point $(1,2,-3)$ perpendicular to the vector $2i-j+2k$.



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87. Find the Cartesian equation of the plane passing through the point $(1,2,-3)$ perpendicular to the vector $2i-j+2k$.

Find the angle between the Plane and the line

$$\frac{x - 1}{2} = \frac{y - 3}{3} = \frac{z}{6}$$



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88. Find the angle between the lines having direction ratios $1,1,2$ and $\sqrt{3} - 1, -\sqrt{3} - 1, 4$



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89. If lines $\frac{x - 1}{3} = \frac{y - 1}{2\lambda} = \frac{z - 3}{2}$ and $\frac{x - 1}{3\lambda} = \frac{y - 1}{1} = \frac{z - 6}{-5}$ are perpendicular, find the value of λ



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90. Find the equation of the plane passing through the points $(3,-1,2)$, $(5,2,4)$, $(-1,-1,6)$



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91. Find the equation of the plane passing through the points $(3,-1,2)$, $(5,2,4)$, $(-1,-1,6)$.Find the perpendicular distance from the point $(6,5,9)$ to this plane.



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92. Consider the vector equation of two planes

$$\bar{r} \cdot (2i + j + k) = 3, \bar{r}(i - j - k) = 4$$

Find vector equation of any plane through the intersection of the above two planes.





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93. Consider the vector equation of two planes $\bar{r} \cdot (2i + j + k) = 3$, $\bar{r} \cdot (i - j - k) = 4$ Find vector equation of the plane through the intersection of the above planes and the point $(1,2,-1)$.



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94. Consider the planes $2x + y - 2z = 5$ and $3x - 6y - 2z = 7$. Find their normal vectors.



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95. Consider the planes

$$2x + y - 2z = 5 \text{ and}$$

$$3x - 6y - 2z = 7$$

Find the angle between these two planes.



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96. If a_1, b_1, c_1 and a_2, b_2, c_2 are the direction ratios of two lines, then write the condition of

its perpendicularity.



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97. Find the angle between the lines

$$\frac{x + 3}{3} = \frac{y - 1}{5} = \frac{z + 3}{4} \text{ and}$$

$$\frac{x + 1}{1} = \frac{y - 4}{1} = \frac{z - 5}{2}.$$



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98. Find the shortest distance between the

lines $\bar{r} = i + j + \lambda(2i - j + k)$ and

$$\bar{r} = 2i + j - k + \mu(3i - 5j + 2k)$$



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99. The equation of the line which passes through the point (1,2,3) and parallel to the vector $3i+2j-2k$ is

A. $\bar{r} = 3i + 2j - 2k + \lambda(i + 2j + 3k)$

B. $\bar{r} = 2i - 5k + \lambda(3i + 2j - 2k)$

C. $\bar{r} = i + 2j + 3k + \lambda(-2i + 4j - 2k)$

D. $\bar{r} = i + 2j + 3k + \lambda(3i + 2j - 2k)$

Answer:



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100. Find the angle between the pair lines

$$\bar{r} = 2i - 5j + k + \lambda(3i + 2j + 6k) \text{ and}$$

$$\bar{r} = 7i - 6k + \mu(i + 2j + 2k)$$



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101. Consider the lines

$$\frac{x - 3}{2} = \frac{y - 1}{5} = \frac{z + 3}{4} \text{ and}$$

$$\frac{x + 5}{1} = \frac{y + 2}{1} = \frac{z - 3}{2}$$

Find the angle between them.



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102. Consider the lines

$$\frac{x - 3}{2} = \frac{y - 1}{5} = \frac{z + 3}{4} \text{ and}$$

$$\frac{x + 5}{1} = \frac{y + 2}{1} = \frac{z - 3}{2}$$

Find the shortest distance between them



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103. Find the vector equation of the Plane
Passing through the intersection of the planes

$$\bar{r} \cdot (i + j + k) = 6 \quad \text{and}$$

$$\bar{r} \cdot (2i + 3j + 4k) = -5 \quad \text{and through the}$$

point (1,1,1).



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104. Express the vector equation

$$\bar{r} \cdot (5i + 3j + 4k) = 0 \quad \text{of a Plane in Cartesian}$$

form and hence find its perpendicular distance from the origin.



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105. Given the plane $5x-2y+4z-9=0$

Find the foot of the perpendicular drawn from the origin to the Plane.



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106. Given the plane $5x-2y+4z-9=0$

Find the foot of the perpendicular drawn from the origin to the Plane.

write the vector and Cartesian equation of this perpendicular.



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107. The foot of the perpendicular from the origin to a plane is $P(4,-2,5)$. Write \overline{OP}



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108. The foot of the perpendicular from the origin to a plane is $P(4,-2,5)$. Write \overline{OP}

Find the equation of the plane in vector and Cartesian form.



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109. Consider the lines

$$\frac{x - 3}{3} = \frac{y - 8}{-1} = \frac{z - 3}{1} \text{ and}$$

$$\frac{x + 3}{3} = \frac{y + 7}{2} = \frac{z - 6}{4}$$

Express the equation to the lines into vector form.



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110. Consider the lines

$$\frac{x - 3}{3} = \frac{y - 8}{-1} = \frac{z - 3}{1} \text{ and}$$
$$\frac{x + 3}{3} = \frac{y + 7}{2} = \frac{z - 6}{4}$$

Find the shortest distance between the lines.



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111. Consider the Cartesian equation of a line

$$\frac{x - 3}{2} = \frac{y + 1}{3} = \frac{z - 5}{-2}$$

Find its vector equation .



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112. Consider the Cartesian equation of a line

$$\frac{x - 3}{2} = \frac{y + 1}{3} = \frac{z - 5}{-2}$$

Find the intersecting point with the plane

$$5x + 2y - 6z - 7 = 0$$



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113. The foot of the perpendicular drawn from origin to a Plane is $(4,-2,5)$.

How far is the plane from origin?



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114. The foot of the perpendicular drawn from origin to a Plane is $(4,-2,5)$.

Find a unit vector perpendicular to that Plane.



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115. The foot of the perpendicular drawn from origin to a Plane is $(4,-2,5)$.

Obtain the equation of the Plane in general form



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116. Equation of the plane with intercepts $2,3,4$ on the x,y,z axis respectively is

A. $2x+3y+4z=1$

B. $2x+3y+4z=12$

C. $6x+4y+3z=1$

D. $6x+4y+3z=12$

Answer:



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117. Find the Cartesian equation of the plane passing through the point $A(2,5,-3)$, $B(-2,-3,5)$ and $C(5,3,-3)$.



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118. The distance of the plane $x+y+z = 1$ from the point $(1,1,1)$ is

a) 4 units b) $\frac{1}{\sqrt{3}}$ units c) $\frac{4}{\sqrt{3}}$ units d) $\frac{1}{4\sqrt{3}}$ units

A. 4 units

B. $\frac{1}{\sqrt{3}}$ units

C. $\frac{4}{\sqrt{3}}$ units

D. $\frac{1}{4\sqrt{3}}$ units

Answer:



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119. Find the equation of the plane passing through $(1,0,-2)$ and perpendicular to each of the planes $2x+y-z=2$ and $x-y-z=3$



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120. The lines $x-1=y=z$ is perpendicular to the

line....a) $\frac{x-2}{1} = \frac{y-1}{2} = \frac{z}{-3}$ b)

$$x - 2 = y - 2 = z \quad \text{c) } \frac{x - 2}{1} = \frac{y - 1}{2} = \frac{z}{3}$$

$$\text{d) } x=y=z/2$$

$$\text{A. } \frac{x - 2}{1} = \frac{y - 1}{2} = \frac{z}{-3}$$

$$\text{B. } x - 2 = y - 2 = z$$

$$\text{C. } \frac{x - 2}{1} = \frac{y - 1}{2} = \frac{z}{3}$$

$$\text{D. } x=y=z/2$$

Answer:



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121. Find the shortest distance between the lines $\bar{r} = i + 2j + 3k + \lambda(i + j + k)$ and

$$\bar{r} = i + j + k + \mu(i + j + k)$$



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122. Find the shortest distance between the

lines $\frac{x + 1}{7} = \frac{y + 1}{-6} = \frac{z + 1}{1}$ and

$$\frac{x - 3}{1} = \frac{y - 5}{-2} = \frac{z - 7}{1}$$



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123. Find the equation of the Plane passing through one point $(-1,3,2)$ and \perp r to the planes $x + 2y + 3z = 5$ and $3x + 3y + z = 0$



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124. A line makes equal angles with the coordinate axis . Find the direction cosines.



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125. Find the equation of the plane passing through $(1,1,-1)$, $(2,3,5)$ and $(-1,4,-5)$.



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126. Find p and q , if the plane $x+py+qz=0$ is perpendicular to the plane $3x+2y+z=0$ and the line $\frac{x-3}{2} = \frac{y-2}{3} = \frac{z-1}{1}$



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127. Given the straight lines

$$\bar{r} = 3i + 2j - 4k + \lambda(i + 2j + 2k) \quad \text{and}$$

$$\bar{r} = 5i - 2k + \mu(3i + 2j + 6k)$$

Find the angle between the lines.



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128. Given the straight lines

$$\bar{r} = 3i + 2j - 4k + \lambda(i + 2j + 2k) \quad \text{and}$$

$$\bar{r} = 5i - 2k + \mu(3i + 2j + 6k)$$

Obtain the unit vector perpendicular to both the lines.



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129. Given the straight lines

$$\bar{r} = 3i + 2j - 4k + \lambda(i + 2j + 2k) \quad \text{and}$$

$$\bar{r} = 5i - 2k + \mu(3i + 2j + 6k)$$

Form the equation of the line perpendicular to the given lines and passing through the point(1,1,1)



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130. Write the Cartesian equation of the straight line through the point $(1,2,3)$ and along the vector $3i+j+2k$



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131. Write the Cartesian equation of the straight line through the point $(1, 2, 3)$ and along the vector $3i + j + 2k$. Write a general point on this straight line.



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132. Write the Cartesian equation of the straight line through the point $(1,2,3)$ and along the vector $3i + j + 2k$. Find the point of intersection of this straight line with the plane $2x + 3y - z + 2 = 0$



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133. Find the distance from $(1,2,3)$ to the plane $2x+3y-z+2=0$



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134. Consider a plane passing through the point $(5,2,-4)$ and perpendicular to the line

$$\bar{r} = (i + j) + \lambda(2i + 3j - k)$$

Write the equation in Cartesian form.



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135. Consider a plane passing through the point $(5,2,-4)$ and perpendicular to the line

$$\bar{r} = (i + j) + \lambda(2i + 3j - k)$$

Find its distance from the point (1,2,-1).



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136. Consider a plane passing through the point (5,2,-4) and perpendicular to the line

$$\bar{r} = (i + j) + \lambda(2i + 3j - k)$$

Find the angle made by it with line

$$\frac{x - 1}{2} = \frac{y - 2}{1} = \frac{z - 3}{-2}.$$



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