

### **MATHS**

# BOOKS - IPUCET PREVIOUS YEAR PAPERS MATHS (HINGLISH)

## **GGSIPU MATHEMATICS 2006**



**1.** if the regression coefficient of Y on X is 4/3, then the regression coefficient of X and Y

:

A. is  $\frac{3}{4}$ 

B. is less than  $\frac{3}{4}$ 

C. is less than 1

D. can take any value

### **Answer:**



- 2. Which of the following is the inverse of the proposition 'If a number is a prime then it is odd'?
  - A. If a number is not a prime then it is odd
  - B. If a number is not a prime then it is not

odd

C. If a number is not odd then it is not a

prime

D. If a number Is odd then it is a prime



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3. What must be the matrix X if

$$2X + \left[egin{array}{cc} 1 & 2 \ 3 & 4 \end{array}
ight] = \left[egin{array}{cc} 3 & 8 \ 7 & 2 \end{array}
ight]?$$

A. 
$$\begin{bmatrix} 1 & 3 \\ 2 & -1 \end{bmatrix}$$

B. 
$$\begin{bmatrix} 1 & -3 \\ 2 & -1 \end{bmatrix}$$

$$\mathsf{C.} \left[ \begin{matrix} 2 & 6 \\ 4 & -2 \end{matrix} \right]$$

D. 
$$\begin{bmatrix} 2 & -6 \\ 4 & -2 \end{bmatrix}$$



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**4.** The value of 
$$\begin{vmatrix} 1 & 1 & 1 \ bc & ca & ab \ b+c & c+a & a+b \ \end{vmatrix}$$
 is :

**A.** 1

B. 0

$$\mathsf{C.}\,(a-b)(b-c)(c-a)$$

D. 
$$(a + b)(b + c)(c + a)$$

### **Answer: C**



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5. The value of 
$$\begin{vmatrix} 441 & 442 & 443 \\ 445 & 446 & 447 \\ 449 & 450 & 451 \end{vmatrix}$$
 is :

A. 
$$441 imes 446 imes 4510$$

B. 0

C. -1

D. 1

### **Answer: B**



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**6.** 
$$\left(\overrightarrow{a}\,\hat{i}\right)\hat{i}+\left(\overrightarrow{a}\,\hat{j}\right)\hat{j}+\left(\overrightarrow{a}\,\hat{k}\right)\hat{k}$$
 is value of :

- A.  $|\hat{i}|$
- $\mathsf{B.}\,2\Big|\overrightarrow{a}\Big|$
- $\mathsf{C.}\,3|\overrightarrow{a}|$
- D.  $\left| \overrightarrow{a} \right|$

#### **Answer:**

**7.** Inverse of the matrix  $\begin{bmatrix} \cos 2\theta & -\sin 2\theta \\ \sin 2\theta & \cos 2\theta \end{bmatrix}$  is

A. 
$$\begin{bmatrix} \cos 2\theta & -\sin 2\theta \\ \sin 2\theta & \cos 2\theta \end{bmatrix}$$

B. 
$$\begin{bmatrix} \cos 2\theta & \sin 2\theta \\ \sin 2\theta & -\cos 2\theta \end{bmatrix}$$

C. 
$$\begin{bmatrix} \cos 2\theta & \sin 2\theta \\ \sin 2\theta & \cos \theta \end{bmatrix}$$

D. 
$$\begin{bmatrix} \cos 2\theta & \sin 2\theta \\ -\sin 2\theta & \cos 2\theta \end{bmatrix}$$

### **Answer:**



**8.** If  $\left|\overrightarrow{a}\right|=3,\left|\overrightarrow{b}\right|=4$  , then a value of  $\lambda$  for which  $\overrightarrow{a}+\lambda\overrightarrow{b}$  is perpendicular to  $\overrightarrow{a}-\lambda\overrightarrow{b}$  is :

A. 
$$\frac{9}{16}$$

$$\mathsf{B.}\;\frac{3}{4}$$

c. 
$$\frac{3}{2}$$

D. 
$$\frac{4}{2}$$

### **Answer: B**



**9.** A line passes through the point (6, -7, -1) and (2, -3, 1). The direction cosines of the line so directed that the angle made by it with the positive direction of x-axis is acute, are

A. 
$$\frac{2}{3}$$
,  $-\frac{2}{3}$ ,  $-\frac{1}{3}$ 

B. 
$$-\frac{2}{3}, \frac{2}{3}, \frac{1}{3}$$

c. 
$$\frac{2}{3}$$
,  $-\frac{2}{3}$ ,  $\frac{1}{3}$ 

D. 
$$\frac{2}{3}$$
,  $\frac{2}{3}$ ,  $\frac{1}{3}$ 



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10. The maximum of the function  $3\cos x-4\sin x$ 

is:

A. 2

B. 3

C. 4

D. 5

### **Answer: D**



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11. If the distance s metre traversed by a particle in t seconds is given by  $s=t^3-3t^2$ , then the velocity of the particle when the acceleration is zero, in metre/second is

**A.** 3

B.-2

 $\mathsf{C.}-3$ 

D. 2

### **Answer:**



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**12.** For the curve  $y^n=a^{n-1}x$  if the subnormal at any point is a constant, then n is equal to

**A.** 1

B. 2

 $\mathsf{C}.-2$ 

$$D. -1$$



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**13.** If 
$$a=A\cos 4t+B\sin 4t$$
, then  $\dfrac{d^2x}{dt^2}$  is equal to

A. -16x

B.16x

 $\mathsf{C}.\,x$ 

$$D.-x$$



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**14.** If tangent to the curve  $x=at^2,\,y=2at$  is perpendicular to X-axis, then its pointt of contact is

A. a,a

B. 0,a

C. 0,0

D. a,0

### **Answer:**



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**15.** The general solution of the differential equation  $\frac{dy}{dx} + \frac{1+\cos 2y}{1-\cos 2x} = 0$  is given by

A. tany cotx = c

B. tany - cotx = c

C. 
$$tanx - coty = c$$

D. 
$$tanx + coty = c$$



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**16.** The area enclosed between the curves

$$y=x^3$$
 and  $y=\sqrt{x}$  is

$$\mathsf{A.}\;\frac{5}{3}$$

$$\mathsf{B.}\;\frac{5}{4}$$

D. 
$$\frac{12}{5}$$

c.  $\frac{5}{12}$ 



17. 
$$\int_0^{\pi/8} \cos^3 4 heta d heta =$$

A. 
$$\frac{5}{3}$$
B.  $\frac{5}{4}$ 

c. 
$$\frac{1}{3}$$

D. 
$$\frac{1}{6}$$



**18.** 
$$\int_0^{\pi/2} \frac{\cos x - \sin x}{1 + \cos x \sin x} dx$$
 is equal to

B. 
$$\frac{\pi}{2}$$

$$\frac{\tau}{\pi}$$

D. 
$$\frac{\pi}{6}$$



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**19.** If  $ax^2-y^2+4x-y=0$  represents a pair of lines , then a is equal to

A. - 16

B. 16

C. 4

D.-4



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**20.** What is the equation of the locus of a point which moves such that 4 times its distance from the x-axis is the square of its distance from the origin

A. 
$$x^2 + y^2 - 4y = 0$$

B. 
$$x^2 + y^2 - 4 = 0$$

C. 
$$x^2 + y^2 - 4x = 0$$

D. 
$$x^2 + y^2 - 4x = 0$$



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21. If the area of the triangle with vertices x,0,1,1 and 0,2 1, 4 sq units,then the value of x is :

A.-2

B.-4

$$\mathsf{C.}-6$$

D. 8

### **Answer:**



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**22.** 
$$\lim_{\theta \to \frac{\pi}{2}} \frac{\frac{\pi}{2} - \theta}{\cot \theta}$$
 is equal to

**A.** 0

B. - 1

**C**. 1

 $D. \infty$ 

### **Answer:**



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23. The probability that A can solve a problem is  $\frac{4}{5}$  and B can solve it is  $\frac{2}{3}$ . If both attempt the problem what is the probability that exactly one of the problem gets solved?



**24.** If the foci of the ellipse  $\frac{x^2}{16}+\frac{y^2}{b^2}=1$  and the hyperbola  $\frac{x^2}{144}-\frac{y^2}{81}=\frac{1}{25}$  coincide write the value of  $b^2$ .

- **A.** 1
- B. 7
- C. 5
- D. 9

### **Answer:**



**25.** The differential coefficient of  $f(\sin x)$  with respect to x, where  $f(x)=\log x$ , is

- A. tan x
- $\mathsf{B.}\cot x$
- $\mathsf{C}.\,f(\cos x)$
- D.  $\frac{1}{x}$

### **Answer:**



**26.** If 
$$f(x) = \left\{ egin{array}{ll} rac{1-\cos x}{x}, & x 
eq 0 \ k, & x = 0 \end{array} 
ight.$$
 is continuous

at x = 0, then the value of k is

B. 
$$\frac{1}{2}$$

c. 
$$\frac{1}{4}$$

$$\mathsf{D.}-\frac{1}{2}$$

### **Answer:**



**27.** If  $y = \tan^{-1}(\sec x - \tan x)$ , then  $\frac{dy}{dx}$  is equal to

$$B.-2$$

$$\mathsf{C.}\ \frac{1}{2}$$

$$\mathsf{D.}-\frac{1}{2}$$

### **Answer:**



**28.** If  $x+rac{1}{x}=2\cos heta$ , then  $x^n+rac{1}{x^n}$  is equal to

A. 
$$2^n \cos \propto$$

B. 
$$2^n \cos n \propto$$

C. 
$$2i\cos n \propto$$

D. 
$$2\cos n \propto$$

### **Answer:**



**29.** The value of 
$$\displaystyle \int_{-1}^{1} |1-x| dx$$
 is equal to -

$$A.-2$$



**30.** If a sphere of constant radius k passes through the origin and meets the axis in A,B,C then the centroid of the triangle ABC lies on :

A. 
$$x^2 + y^2 + z^2 = k^2$$

B. 
$$x^2 + y^2 + z^2 = 4k^2$$

$$\mathsf{C.}\, 9x^2 + y^2 + z^2 = 4k^2$$

D. 
$$9x^2 + y^2 + z^2 = k^2$$

### **Answer:**



31. 
$$\int \frac{dx}{x^2+2x+2}$$
 is equal to

A. 
$$\sin^{-1} x + 1 + c$$

$$\mathsf{B.} \sin h^{-1}x + 1 + c$$

C. 
$$\tanh^{-1} x + 1 + c$$

D. 
$$\tan^{-1} x + 1 + c$$

### **Answer: D**



**32.** If the tangent to the curve  $y=6x-x^2$  is parallel to line 4x-2y-1=0, then the point of tangency on the curve is

- A. 2,8
- B. 8,2
- C. 6,1
- D. 4,2

### **Answer:**



**33.** A four figure number is formed of the figures 1, 2, 3, 4, 5 with no repetitions. The probability that the number is divisible by 5 is 3/4 b. 1/4 c. 1/8 d. none of these

A. 
$$\frac{3}{4}$$

$$\mathsf{B.}\;\frac{1}{4}$$

c. 
$$\frac{1}{8}$$

D. none of these

### **Answer:**



34. The number of solutions for the equation

$$|x^2 - 5|x| + 6 = 0$$
 is :

A. 4

B. 3

C. 2

D. 1

### **Answer:**



**35.** How many numbers of 6 digits can be formed from the digits of number 1; 1; 2; 2; 3; 3?

A. 30

B. 60

C. 90

D. 120

### **Answer:**



## **36.** The last digit of $7^{2003}$ is

**A.** 7

B. 9

C. 1

D. 3

## **Answer:**



37. If 
$$\frac{\log x}{a-b}=\frac{\log y}{b-c}=\frac{\log z}{c-a}$$
 , then xyz is equal to :

$$\mathsf{C.}-1$$

# **Answer: B**



## **38.** What is the smallest positive integer n for

which 
$$(1+i)^{2n} = (1-i)^{2n}$$
?

- **A.** 1
- B. 2
- C. 3
- D. 4

#### **Answer:**



**39.** If  $\cos^{-1} p + \cos^{-1} q + \cos^{-1} r = 3\pi$ , then  $p^2+q^2+r^2+2pqr$  is equal to

A. 3

B. 1

C. 2

D. -1

## **Answer:**



**40.** If 
$$\sin^{-1}\Bigl(\frac{x}{5}\Bigr) + \cos ec^{-1}\biggl(\frac{5}{4}\biggr) = \frac{\pi}{2}$$
, then

the value of x is

- **A.** 1
- B. 4
- C. 3
- D. 5

#### **Answer:**



**41.** if  $0 \leq x \leq \pi$  and  $81^{\sin^2 x} + 81^{\cos^2 x} = 30$ 

then x =

A. 
$$\frac{\pi}{6}$$

$$\mathsf{B.}\;\frac{\pi}{2}$$

C. 
$$\frac{\pi}{4}$$

D. 
$$\frac{3\pi}{4}$$

## **Answer:**



42. The equation of the director circle of the

hyperbola 
$$\frac{x^2}{16} - \frac{y^2}{4} = 1$$
 is given by :

A. 
$$x^2 + y^2 = 16$$

B. 
$$x^2 + y^2 = 4$$

C. 
$$x^2 + y^2 = 20$$

D. 
$$x^2 + y^2 = 12$$

## Answer:



**43.** Let Q be the set of all rational numbers and \* be the binary operation , defined by  $a^*$  b=a+ab for all  $a,b\in Q.$  then ,

**A.** 1

B. 0

C. -1

D. 2

#### **Answer:**



**44.** Thecircle  $x^2 + y^2 - 8x + 4y + 4 = 0$ 

touches

- A. x axis
- B. y-axis
- C. both axis
- D. neither x axis nor y-axis

#### **Answer:**



**45.** If f(x)=log 
$$(1+x)-\frac{2x}{2+x}$$
 is increasing ,

then.....

A. 
$$0, \infty$$

$$B.-\infty, 0$$

$$\mathsf{C}.-\infty,\infty$$

D. none of these

#### **Answer:**



**46.** The minimum value

of

$$igg(1+rac{1}{\sin^nlpha}igg)igg(1+rac{1}{\cos^nlpha}igg)$$
 is

A. 1

B. 2

C. 1+2

D. none of these

## **Answer:**



**47.** 
$$\lim_{x o \infty} \ \left(1 - \frac{4}{x-1}\right)^{3x-1}$$
 is equal to

A.  $e^{12}$ 

B.  $e^{-12}$ 

 $\mathsf{C.}\,e^4$ 

D.  $e^3$ 

#### **Answer:**



**48.** If 
$$A + B + C = 180^{\circ}$$
, then

 $\Sigma \tan \frac{A}{2} \tan \frac{B}{2}$  is

A. 0

B. 1

C. 2

D. 3

## **Answer:**



**49.** In a triangle ABC if  $b=2, B=30^{\circ}$  then the area of the circumcircle of triangle ABC in square units is :

A.  $\pi$ 

B.  $2\pi$ 

C.  $4\pi$ 

D.  $6\pi$ 

## **Answer: C**



 $\cos^{12}x + 3\cos^{10}x + 3\cos^8x + \cos^6x =$ 

- **A.** 1
- B. 2
- C. 3
- D. 0

**Answer:** 



51. If R denotes the set of all real number, then

the function  $f\!:\!R o R$  defined f(x) =  $|\mathsf{x}|$  is :

A. one-one only

B. onto only

C. both one - one and onto

D. neither one-one nor onto

#### **Answer:**

