



## MATHS

# BOOKS - IPUCET PREVIOUS YEAR PAPERS MATHS (HINGLISH)

## GGSIU MATHEMATICS 2012

### Mcqs

1. If the lines  $x - y - 1 = 0$ ,  $4x + 3y = k$  and  $2x - 3y + 1 = 0$  are concurrent, then  $k$  is

A. 1

B.  $-1$

C. 25

D. 5

**Answer:**



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2. Circles  $x^2 + y^2 = 4$  and  $x^2 + y^2 - 2x - 4y + 3 = 0$

A. 1

B. 2

C. 3

D. 4

**Answer:**



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3. The centroid of a triangle formed by the points  $(0, 0)$ ,  $(\cos \theta, \sin \theta)$  and  $(\sin \theta, -\cos \theta)$  lie on the line  $y = 2x$ , then  $\theta$  is

A.  $\tan^{-1} 2$

B.  $\tan^{-1} \left( \frac{1}{3} \right)$

C.  $\tan^{-1} \left( \frac{1}{2} \right)$

D.  $\tan^{-1} - 3$

**Answer:**

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4. The orthocentre of the triangle formed by  $(8, 0)$  and  $(4, 6)$  with the origin, is

A.  $\left( 4, \frac{8}{3} \right)$

B. 3 , -4

C. 4 , 3

D. 3 , 4

**Answer:**



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5. If the angle between the two lines represented by  $2x^2 + 5xy + 3y^2 + 6x + 7y + 4 = 0$  is  $\tan^{-1}(m)$ , then  $m$  is equal to

A.  $\frac{1}{5}$

B. 1

C.  $\frac{7}{5}$

D. 7

**Answer:**



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6. If  $xy - 4x + 3y - \lambda = 0$  represents the asymptotes of  $xy - 4x + 3y = 0$ , then  $\lambda$  is

A. 3

B. -6

C. 8

D. 12

**Answer:**



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7. Equation of the chord of the parabola  $y^2 = 8x$  which is bisected at the point  $(2, -3)$  is

A.  $4x+3y+1 = 0$

B.  $3x+4y -1 = 0$

C.  $4x -3y-1 = 0$

D.  $3x -4y+1 = 0$

**Answer:**



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8. If  $x+y+1 = 0$  touches the parabola  $y^2 = \lambda x$ , then  $\lambda$  is equal to

A. 2

B. 4

C. 6

D. 8

**Answer:**



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9. The equation  $x = \frac{e^t + e^{-t}}{2}, y = \frac{e^t - e^{-t}}{2}, t \in \mathbb{R}$ , represents

A. an ellipse

B. a parabola

C. a hyperbola

D. a circle

**Answer:**



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10. If  $e_1$  and  $e_2$  are the eccentricities of two conics with  $e_1^2 + e_2^2 = 3$ , then the conics are

- A. ellipses
- B. parabolas
- C. circles
- D. hyperbolas

**Answer:**

11. The sum of the distances of any point on the ellipse  $3x^2 + 4y^2 = 24$  from its foci, is



A.  $8\sqrt{2}$

B. 8

C.  $16\sqrt{2}$

D.  $4\sqrt{2}$

**Answer:**



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12. In  $\triangle ABC$ , if  $a$  tends to  $2c$  and  $b$  tends to  $3c$ , then  $\cos B$  tends to

A.  $-1$

B.  $\frac{1}{2}$

C.  $\frac{1}{3}$

D.  $\frac{2}{3}$

**Answer:**

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13. If  $\sin(\pi\cos\theta) = \cos(\pi\sin\theta)$ , then which one of the following is correct?

A.  $\cos\theta = \frac{3}{2\sqrt{2}}$

B.  $\cos\left(\theta - \frac{\pi}{2}\right) = \frac{1}{2\sqrt{2}}$

C.  $\cos\left(\theta - \frac{\pi}{4}\right) = \frac{1}{2\sqrt{2}}$

D.  $\cos\left(\theta + \frac{\pi}{4}\right) = -\frac{1}{2\sqrt{2}}$

**Answer:**

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14.  $\sin 12^\circ \sin 48^\circ \sin 54^\circ$  is equal to

A.  $\frac{2}{3}$

B.  $\frac{1}{2}$

C.  $\frac{1}{8}$

D.  $\frac{1}{3}$

Answer:



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15.

if:

$$3 \sin^{-1} \left( \frac{2x}{1+x^2} \right) - 4 \cos^{-1} \left( \frac{1-x^2}{1+x^2} \right) + 2 \tan^{-1} \left( \frac{2x}{1-x^2} \right) = \frac{\pi}{3}$$

, where  $|x| < 1$ , then:  $x =$

A.  $\frac{1}{\sqrt{3}}$

B.  $-\frac{1}{\sqrt{3}}$

C.  $\sqrt{3}$

D.  $-\frac{\sqrt{3}}{2}$

**Answer:**



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**16.** The angle of elevation of the sun when the length of the shadow of a pole is  $\sqrt{3}$  times the height of the pole is

A.  $40^\circ$

B.  $\frac{45^\circ}{2}$

C.  $60^\circ$

D.  $30^\circ$

**Answer:**



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17. The point of contact of the line  $x - y + 2 = 0$  with the parabola  $y^2 - 8x = 0$  is

A. 2, 4

B. -2, 4

C. 2, -4

D. 2, 2

**Answer:**



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18. The sides of a triangle are  $x^2 + x + 1$ ,  $2x + 1$ , and  $x^2 - 1$ .

Prove that the greatest angle is  $120^\circ$ .

A.  $90^\circ$

B.  $135^\circ$

C.  $115^\circ$

D.  $120^\circ$

**Answer:**

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19.  $\cos 1^\circ \cdot \cos 2^\circ \cdot \cos 3^\circ \dots \cos 179^\circ =$

A.  $\frac{1}{\sqrt{2}}$

B. 0

C. 1

D.  $-1$

**Answer:**



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**20.** If  $\cot(\alpha + \beta) = 0$ , then  $\sin(\alpha + 2\beta) =$

A.  $\sin \alpha$

B.  $\cos \alpha$

C.  $\sin \beta$

D.  $\cos 2\beta$

**Answer:**



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21. The value of  $4 \sin A \cos^3 A - 4 \cos A \sin^3 A$  is equal to

A.  $\cos 2A$

B.  $\sin 3A$

C.  $\sin 2A$

D.  $\sin 4A$

**Answer:**



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22. If the solutions for  $\theta$  of  $\cos p\theta + \cos q\theta = 0$ ,  $p > q > 0$  are in

A.P, then numerically smallest common difference of A.P is

A.  $\frac{\pi}{p+q}$



B.  $\frac{2\pi}{p+q}$

C.  $\frac{\pi}{2(p+q)}$

D.  $\frac{1}{p+q}$

**Answer: B**



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**23.** The value of  $k$ , for which

$(\cos x + \sin x)^2 + k \sin x \cos x - 1 = 0$  is an identity, is

A.  $-1$

B.  $-2$

C.  $0$

D.  $1$

**Answer:**

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24. If  $4 \cos^{-1} x + \sin^{-1} x = \pi$ , then the value of  $x$  is

A.  $\frac{1}{2}$

B.  $\frac{1}{\sqrt{2}}$

C.  $\frac{\sqrt{3}}{2}$

D.  $\frac{2}{\sqrt{3}}$

**Answer:**

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25. A problem in mathematics is given to 3 students whose chances of solving it are  $\frac{1}{2}$ ;  $\frac{1}{3}$ ;  $\frac{1}{4}$ . What is the probability that the problem is solved?

A.  $\frac{1}{4}$

B.  $\frac{1}{24}$

C.  $\frac{23}{24}$

D.  $\frac{3}{4}$

**Answer:**



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26. In a non leap year the probability of getting 53 Sundays or 53 Tuesdays or 53 Thursdays

A.  $\frac{1}{7}$

B.  $\frac{2}{7}$

C.  $\frac{3}{7}$

D.  $\frac{4}{7}$

**Answer:**



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27. The probability for arandomly chosen month to have its 10<sup>th</sup> day as Sunday , is

A.  $\frac{1}{84}$

B.  $\frac{10}{12}$

C.  $\frac{10}{84}$

D.  $\frac{1}{7}$

**Answer:**



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**28.** If the mean of the numbers  $27 + x$ ,  $31 + x$ ,  $89 + x$ ,  $107 + x$ ,  $156 + x$  is 82, then the mean of  $130 + x$ ,  $126 + x$ ,  $68 + x$ ,  $50 + x$ ,  $1 + x$  is

A. 79

B. 157

C. 82

D. 75

**Answer:**



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29. If  $\bar{X}$  is the mean of a distribution of  $X$ , then under usual notation sum  $\sum_{i=1}^n f_i(x_2 - \bar{x})$  is

A. MD

B. SD

C. 0

D. relative frequency

**Answer:**



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30. Two cards are drawn successively with replacement from a well-shuffled pack of 52 cards. The probability of drawing two aces is

A.  $\frac{1}{13}$

B.  $\frac{1}{13} \times \frac{1}{17}$

C.  $\frac{1}{52} \times \frac{1}{51}$

D.  $\frac{1}{13} \times \frac{1}{13}$

**Answer:**



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31. If  $\sec\left(\frac{x+y}{x-y}\right) = a$ , prove that  $\frac{dy}{dx} = \frac{y}{x}$ .

A.  $\frac{x}{y}$

B.  $\frac{y}{x}$

C.  $y$

D.  $x$

**Answer:**



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32. If  $x^y = e^{x-y}$ , then  $\frac{dy}{dx}$  is equal to

A.  $\frac{\log x}{1 + \log x}$

B.  $\frac{\log x}{1 - \log x}$

C.  $\frac{\log x}{1 + \log x^2}$

D.  $\frac{y \log x}{x(1 + \log x)}$

**Answer:**



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33. For  $y = \cos(m \sin^{-1} x)$ , which of the following is true?



A.  $1 - x^2y + xy_1 - m^2y = 0$

B.  $1 - x^2y_2 - xy_1 + m^2y = 0$

C.  $1 + x^2y_2 + xy_1 - m^2y = 0$

D.  $(-x^2)y_2 + xy_1 + m^2y = 0$

**Answer:**

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34. If  $f(x) = \begin{cases} x + 1 & x \leq 1 \\ 3 - ax^2 & x > 1 \end{cases}$  is continuous at  $x = 1$ , then the value of  $a$  is

A.  $-1$

B.  $2$

C.  $-3$

D.  $1$

**Answer:**



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35.  $\lim_{x \rightarrow \frac{\pi}{2}} \frac{a^{\cot x} - a^{\cos x}}{\cot x - \cos x}$  is equal to

A.  $\log a$

B.  $\log 2$

C.  $a$

D.  $\log x$

**Answer:**



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36. If  $f''(0) = k, k \neq 0$ , then the value of

$$\lim_{x \rightarrow 0} \frac{2f(x) - 3f(2x) + f(4x)}{x^2} \text{ is}$$

- A.  $k$
- B.  $2k$
- C.  $3k$
- D.  $4k$

**Answer:**



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37. If  $g$  is the inverse function of  $f$  and  $f'(x) = \frac{1}{1+x^n}$  then  $g'(x)$  is equal to

- A.  $1 + gx^n$

B.  $1 - gx$

C.  $1 + gx$

D.  $1 - gx^n$

**Answer:**



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**38.** The curves  $4x^2 + 9y^2 = 72$  and  $x^2 - y^2 = 5$  touch each other (b) cut orthogonally intersect at  $45^\circ$  (d) intersect at  $60^\circ$

A. touch each other

B. cut orthogonally

C. intersect at  $45^\circ$

D. intersect at  $60^\circ$

**Answer:**



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**39.** The velocity in m/s of a particle is proportional to the cube of the time. If the velocity after 2 s is 4m/s, then  $v$  is equal to

A.  $t^3$

B.  $\frac{t^3}{2}$

C.  $\frac{t^3}{3}$

D.  $\frac{t^3}{4}$

**Answer:**



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40. The minimum value of  $x (\log)_e x$  is equal to  $e$  (b)  $1/e$  (c)  $-1/e$  (d)  $2e$  (e)  $e$

A.  $e$

B.  $\frac{1}{e}$

C.  $-\frac{1}{e}$

D.  $\frac{2}{e}$

**Answer:**



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41. A particle moves along the x-axis so that its position is given  $x = 2t^3 - 3t^2$  at a time  $t$  second. What is the time interval during which particle will be on the negative half of the axis?

A.  $0 < t < \frac{2}{3}$

B.  $0 < 1$

C.  $0 < t < \frac{3}{2}$

D.  $\frac{1}{2} < t < 1$

**Answer:**



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**42.** A stone thrown vertically upwards satisfies the equations  $s = 80t - 16t^2$ . The time required to reach the maximum height is

A. 2 s

B. 4s

C. 3 s

D. 2.5 s

**Answer:**

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**43.** If  $f(x+y) = f(x) \cdot f(y)$ ,  $f(3) = 3$ ,  $f'(0) = 11$ . Then  $f'(3)$  is equal to

A.  $11 \cdot e^{33}$

B. 33

C. 11

D.  $g^{33}$

**Answer:**

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**44.** If  $y = x \tan y$ , then  $\frac{dy}{dx}$  is equal to



A.  $\frac{x \tan y}{x + x^2 - y^2}$

B.  $\frac{y}{x - x^2 - y^2}$

C.  $\frac{\tan y}{y - x}$

D.  $\frac{\tan x}{x - y^2}$

**Answer:**

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**45.** The product of the lengths of subtangent and subnormal at any point  $x, y$  of a curve is

A.  $x^2$

B.  $y^2$

C. a constant

D.  $x$

**Answer:**

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46. The equation to the tangent to  $\left(\frac{x}{a}\right)^n + \left(\frac{y}{b}\right)^n = 2$  at  $(a, b)$

A.  $\frac{x}{a} + \frac{y}{b} = 2$

B.  $\frac{x}{a} + \frac{y}{b} = 1$

C.  $\frac{x}{b} + \frac{y}{a} = 2$

D.  $ax + by = 2$

**Answer:**

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47. The value of  $\int_0^{\infty} \frac{dx}{(x^2 + 4)(x^2 + 9)}$  is

A.  $\frac{\pi}{60}$

B.  $\frac{\pi}{20}$

C.  $\frac{\pi}{40}$

D.  $\frac{\pi}{80}$

**Answer:**

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48.  $\int e^{a \log x} + e^{x \log a} dx$  is equal to

A.  $\frac{x^{a+1}}{a+1} + C$

B.  $\frac{x^{a+1}}{a+1} + \frac{a^x}{\log a} + C$

C.  $x^{a+1} + a^x + c$

D.  $\frac{x^{a+1}}{a-1} + \frac{\log a}{a^x} + C$

**Answer:**



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49.  $\int_0^a \frac{dx}{x + \sqrt{a^2 - x^2}}$

A.  $\frac{a^2}{4}$

B.  $\frac{\pi}{2}$

C.  $\frac{\pi}{4}$

D.  $\pi$

**Answer:**



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50. If  $\int_{-1}^4 f(x) dx = 4$  and  $\int_2^4 (3 - f(x)) dx = 7$ , then  $\int_{-1}^2 f(x) dx =$

A.  $-2$

B.  $3$

C.  $5$

D.  $8$

**Answer:**



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