MATHS

BOOKS - ARIHANT PUBLICATION

CHSE ODISHA EXAMINATION PAPER - 2018

Very Short Answer Type Questions Answer All The Questions

1. If p and q are respectively degree and order of the differential equation $y = e^{dy/dx}$, then write

the relation between p and q.

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2. If $\left(\vec{a} \times \vec{b}\right)^2 + \left(\vec{a} \cdot \vec{b}\right)^2 = 144$, write the value of ab.

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3. Write the equations of the line $2x + z - 4 = 0 = 2y + z$ in the symmetrical form.

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4. Sets A and B have respectively m and n elements. The total number of relations from A to B is 64. If $m < n$ and $m \neq 1$, write the values of m and n respectively.

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5. Write the principal value of $\sin^{-1}\left(-\frac{1}{2}\right) + \cos^{-1}\cos\left(-\frac{\pi}{2}\right)$

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6. If every element of a third order determinant of value 8 is multiplied by 2, then write the value of the new determinant.

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7. In a Davis Cup tie between India and South Korea, write the probability that India is ahead 2-1 after 3 matches assuming that both the teams are equally likely to win each match.

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8. Write the interval in which the function $f(x) = \sin^{-1}(2 - x)$ is differentiable.

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9. A balloon is pumped at the rate of 2 cm^3 / minute. Write the rate of increase of the surface area, when the radius is 0.5 cm.

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10. Write the definite integral which is equal to

$$\lim_{n \to \infty} \frac{1}{n} \sum_{r=1}^{n} \frac{r}{\sqrt{n^2 + r^2}}$$

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Short Answer Type Questions Answer Any Three Questions

1. Show that

$$\sin^{-1} \sqrt{\frac{x-q}{p-q}} = \cos^{-1} \sqrt{\frac{p-x}{p-q}} = \cot^{-1} \sqrt{\frac{p-x}{x-q}}$$

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2. Sole the following LPP graphically

Minimize $Z = 4x + 3y$

subject to $2x + 5y \geq 10$and $x, y \geq 0.$

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3. Let ~ be defined by (m,n)~(p,q) if mq=np where m, n, p,$q \in Z$-{0}. Show that it is an equivalence relation.

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4. Let $f(x) = \sqrt{x}, g(x) = 1 - x^2$. Compute fog and gof and find their natural domains.

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5. Show that $\sin^{-1}\frac{4}{5} + 2\tan^{-1}\frac{1}{3} = \frac{\pi}{2}$.

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6. A bag A contains 2 white and 3 red balls and another bag B contains 4 white and 5 red balls. One ball is drawn at random from a bag chosen at

random and it is found to be red. Find the probability that it was drawn from bag B.

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7. If $P(A) = 0.6$, $P\left(\frac{B}{A}\right) = 0.5$, find $P(A \cup B)$ when A and B are independent.

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8. If A,B,C are matrices of order 2×2 each and $2A + B + C = \begin{bmatrix} 1 & 2 \\ 3 & 0 \end{bmatrix}$

$A + B + C = \begin{bmatrix} 0 & 1 \\ 2 & 1 \end{bmatrix}$

$A + B - C = \begin{bmatrix} 1 & 2 \\ 1 & 0 \end{bmatrix}$ find A,B and C.

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9. Find the inverse of the following matrix $\begin{bmatrix} 1 & 1 & 2 \\ 0 & 1 & 2 \\ 1 & 2 & 1 \end{bmatrix}$.

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10. Prove that

$$\begin{vmatrix} a-b-c & 2a & 2a \\ 2b & b-c-a & 2b \\ 2c & 2c & c-a-b \end{vmatrix} = (a+b+c)^3$$

.

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11. Show that the sum of the intercepts on the coordinate axes of any tangent to the curve $\sqrt{x}+\sqrt{y}=\sqrt{a}$ is constant.

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12. Show that 2sinx+tanx $\geq$ 3x for all x $\varepsilon\left(0, \frac{\pi}{2}\right)$.

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13. Differentiate $y = \tan^{-1}. \frac{\sqrt{1+x^2}+\sqrt{1-x^2}}{\sqrt{1+x^2}-\sqrt{1-x^2}}$

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14. Differentiate $y = (\sin y)^{\sin 2x}$

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15. Test the continuity of the following function at

$x = 0$

$$f(x) = \begin{cases} \frac{1-e^{-x}}{x}, & x \neq 0 \\ 1 \quad\quad , & x = 0 \end{cases}$$

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16. From the differential equation whose general solution is $y = a \sin t + be^t$.

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17. Solve the following differential equations

$$(1+y^2)dx+\left(x-e^{-\tan^{-1}y}\right)dy=0$$

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18. Evaluate $\int \frac{dx}{(x+1)\sqrt{1-x^2}}$

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19. $\int_0^{\frac{1}{2}} \frac{1}{\sqrt{1-x^2}}dx.$

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20. Find the area enclosed bt the two paraboles $y^2 = 4$ ax and $x^2 = 4$ay.

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21. Prove that the measure of the angle between two main diagonals of a cube is $\cos^{-1}\frac{1}{3}$.

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22. The position vectors of two points A and B are $3\hat{i}+\hat{j}+2\hat{k}$ and $\hat{i}-2\hat{j}-4\hat{k}$, respectively. Find the equation of the plane passing through B and prependicular to AB.

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23. Find the area of the triangle ABC with vertices A(1,2,4), B(3,1,-2) and C(4,3,1) by vector method.

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24. Prove that $\left[\vec{a}+\vec{b} \quad \vec{b}+\vec{c} \quad \vec{c}+\vec{a}\right]=2\left[\vec{a} \quad \vec{b} \quad \vec{c}\right]$.

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25. If the sum of two unit vectors is a unit vector, show that the magnitude of their difference is $\sqrt{3}$.

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26. If $a = 2\hat{i} + \hat{k}, b = \hat{i} + \hat{j} + \hat{k}$ and $c = 4\hat{i} - 3\hat{j} + 7\hat{k}$, then find the vector $\vec{r}$ which satisfies $r \times b = c \times b$ and $r.\, a = 0$.

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27. Find the shortest distance between the lines $\frac{x-3}{3} = \frac{y-8}{-1} = \frac{z-3}{1}$ and $\frac{x+3}{-3} = \frac{y-7}{2} = \frac{z-6}{4}$ Find also the equation of the line of shortest distance.

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28. Solve the following LPP graphically :

Maximize $Z = 3x_1 + 2x_2$

subject to

$-2x_1 + x_2 \leq 1$

$x_1 \leq 2$

$x_1 + x_2 \leq 3$

$x_1, x_2 \geq 0$

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29. Let $f: X \to Y$ and $g: Y \to Z$. Prove that gof is bijective if both f and g are bijective. Also prove

that $(gof)^{-1} = f^{-1}og^{-1}$.

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30. In a ΔABC, if $m\angle A = 90^\circ$, prove that $\tan^{-1}\frac{b}{a+c} + \tan^{-1}\frac{c}{a+b} = \frac{\pi}{4}$, where a,b, c are sides of the triangle.

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31. By elementary operations, find A^{-1} for the following: $A = \begin{bmatrix} 1 & 1 & 0 \\ 1 & -1 & 1 \\ 1 & -1 & 2 \end{bmatrix}$

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32. Solve the following system of equations by the matrix inversion method.

$x + y + z = 4$

$2x - y + 3z = 1$

and $3x + 2y - z = 1$

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33. Two cards are drawn successively with replacement from a well-shuffled deck of 52 cards.

Find the probability distribution of the number of aces.

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34. Find the coordinates of the point on the curve $x^2y - x + y = 0$ where the slope of the tangent is maximum.

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35. If $x = \frac{1 - \cos^2\theta}{\cos\theta}, y = \frac{1 - \cos^{2n}\theta}{\cos^n\theta}$ then show that $\left(\frac{dy}{dx}\right)^2 = n^2\left(\frac{y^2 + 4}{x^2 + 4}\right)$

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36. Find the solution of the following differential equations:

(4x+6y+5)dx-(2x+3y+4)dy=0

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37. Evaluate: $\int\left(\frac{2\cos x+7}{4-\sin x}\right)dx$

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38. Find the area enclosed by $y = 4x - 1$ and $y^2 = 2x$.