



## MATHS

### BOOKS - MODERN PUBLICATION

### SAMPLE PAPER 2018

#### Exercise

1. Sets  $A$  and  $B$  have respectively  $m$  and  $n$  elements. The total number of relations from  $A$  to  $B$  is 64. If  $m < n$  and  $m \neq 1$ , write the values of  $m$  and  $n$  respectively.



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2. Write the principal value of

$$\sin^{-1}\left(-\frac{1}{2}\right) + \cos^{-1}\cos\left(-\frac{\pi}{2}\right)$$



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3. If every element of a third order determinant of value 8 is multiplied by 2, then write the value of the new determinant.



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4. Write the interval in which the function  $f(x) = \sin^{-1}(2 - x)$  is differentiable.



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5. A balloon is pumped at the rate of  $2 \text{ cm}^3 /$  minute. Write the rate of increase of the surface area, when the radius is 0.5 cm.



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6. If  $p$  and  $q$  are respectively degree and order of the differential equation  $y = e^{dy/dx}$ , then write the relation between  $p$  and  $q$ .



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7. If  $\left(\vec{a} \times \vec{b}\right)^2 + \left(\vec{a} \cdot \vec{b}\right)^2 = 144$ , write the value of  $ab$ .



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8. Write the equations of the line  $2x + z - 4 = 0 = 2y + z$  in the symmetrical form.



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9. Let  $\sim$  be defined by  $(m,n) \sim (p,q)$  if  $mq=np$  where  $m, n, p, q \in \mathbb{Z} - \{0\}$ . Show that it is an equivalence relation.



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10. Let  $f(x) = \sqrt{x}$  and  $g(x) = 1 - x^2$ . Compute  $f \circ g$  and  $g \circ f$  and find their natural domains.



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11. Show that  $\sin^{-1} \frac{4}{5} + 2 \tan^{-1} \frac{1}{3} = \frac{\pi}{2}$ .



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12. Show that

$$\sin^{-1} \sqrt{\frac{x-q}{p-q}} = \cos^{-1} \sqrt{\frac{p-x}{p-q}} = \cot^{-1} \sqrt{\frac{p-x}{x-q}}$$



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**13.** Solve the following LPP graphically

$$\text{Minimize } Z = 4x + 3y$$

subject to  $2x + 5y \geq 10$  and  $x, y \geq 0$ .

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**14.** A bag  $A$  contains 2 white and 3 red balls and another bag  $B$  contains 4 white and 5 red balls. One ball is drawn at random from a bag chosen at random and it is found to be red. Find the probability that it was drawn from bag  $B$ .



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**15.** If  $P(A) = 0.6$ ,  $P\left(\frac{B}{A}\right) = 0.5$ , find  $P(A \cup B)$  when  $A$  and  $B$  are independent.



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**16.** Differentiate  $y = \tan^{-1} \cdot \frac{\sqrt{1+x^2} + \sqrt{1-x^2}}{\sqrt{1+x^2} - \sqrt{1-x^2}}$



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**17.** Differentiate  $y = (\sin y)^{\sin 2x}$





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**18.** Show that  $2\sin x + \tan x \geq 3x$  for all  $x \in \left(0, \frac{\pi}{2}\right)$ .



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**19.** Evaluate  $\int \frac{dx}{(x+1)\sqrt{1-x^2}}$



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**20.** Show that

$$\int_0^1 \frac{\ln x}{\sqrt{1-x^2}} dx = \frac{\pi}{2} \ln \frac{1}{2}$$



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**21.** Find the area enclosed by the two parabolas

$$y^2 = 4ax \text{ and } x^2 = 4ay.$$



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**22.** From the differential equation whose general

$$\text{solution is } y = a \sin t + be^t.$$



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**23.** Solve the following differential equations

$$(1 + y^2)dx + \left(x - e^{-\tan^{-1}y}\right)dy = 0$$



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**24.** Find the area of the triangle ABC with vertices

A(1,2,4), B(3,1,-2) and C(4,3,1) by vector method.



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25. Prove that for any three vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$ , 
$$\left[ \vec{a} + \vec{b} \vec{b} + \vec{c} \vec{c} + \vec{a} \right] = 2 \left[ \vec{a} \vec{b} \vec{c} \right]$$



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26. If the sum of two unit vectors is a unit vector, show that the magnitude of their difference is  $\sqrt{3}$ .



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27. Prove that the measure of the angle between two main diagonals of a cube is  $\cos^{-1} \frac{1}{3}$ .



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28. Two vectors  $\vec{A}$  and  $\vec{B}$  are inclined to each other at an angle  $\theta$ . Find the unit vector perpendicular to both  $\vec{A}$  and  $\vec{B}$ .



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29. Let  $f: X \rightarrow Y$  and  $g: Y \rightarrow Z$ . Prove that  $g \circ f$  is bijective if both  $f$  and  $g$  are bijective. Also prove that  $(g \circ f)^{-1} = f^{-1} \circ g^{-1}$ .



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**30.** In a triangle  $ABC$  if  $\angle A = 90^\circ$ ,

prove that  $\tan^{-1} \frac{b}{a+b} + \frac{\tan^{-1} c}{a+b} = \frac{\pi}{4}$ .

where  $a, b, c$ , are sides of the triangle.



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**31.** Solve the following LPP graphically :

Maximize  $Z = 3x_1 + 2x_2$

subject to

$$-2x_1 + x_2 \leq 1$$

$$x_1 \leq 2$$

$$x_1 + x_2 \leq 3$$

$$x_1, x_2 \geq 0$$



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**32.** Solve the following system of equations by the matrix inversion method.

$$x + y + z = 4$$

$$2x - y + 3z = 1$$

and  $3x + 2y - z = 1$



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**33.** Two cards are drawn successively with replacement from a well-shuffled deck of 52 cards. Find the probability distribution of the number of aces.



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**34.** If  $x = \frac{1 - \cos^2 \theta}{\cos \theta}$ ,  $y = \frac{1 - \cos^{2n} \theta}{\cos^n \theta}$  then show that  $\left(\frac{dy}{dx}\right)^2 = n^2 \left(\frac{y^2 + 4}{x^2 + 4}\right)$



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**35.** Find the coordinates of the point on the curve

$$x^2y - x + y = 0$$

where the slope of the tangent is maximum.



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**36.** Evaluate:  $\int \left( \frac{2 \cos x + 7}{4 - \sin x} \right) dx$



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**37.** Find the solution of the following differential equations:

$$(4x+6y+5)dx-(2x+3y+4)dy=0$$



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**38.** Find the area enclosed by  $y = 4x - 1$  and  $y^2 = 2x$ .



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**39.** Find the shortest distance between the lines

$$\frac{x-3}{3} = \frac{y-8}{-1} = \frac{z-3}{1} \quad \text{and}$$

$$\frac{x+3}{-3} = \frac{y-7}{2} = \frac{z-6}{4}$$

Find also the equation of the line of shortest distance.



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