



MATHS

BOOKS - SHARAM PUBLICATION

CONTINUITY AND DIFFERENTIABILITY

Example

1. If a function $f(x) = \frac{x^2 - 4}{x - 2}$ is continuous at $x = 2$, then what is the value of $f(2)$?

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2. If $f(x) = \frac{x^3 + x^2 - 16x + 20}{(x - 2)^2}$ if $x \neq 2 = k$ if $x = 2$ is continuous at for all x , then what is the value of k .

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3. If $f(x) = (1 + 2x)^{\frac{1}{x}}$, $x \neq 0$ is continuous at $x=0$, then what is the value of $f(0)$?

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4. The function $f(x) = \begin{cases} 6.5 & f \text{ or } x \leq 0 \\ 2a + x & f \text{ or } x > 0 \end{cases}$ continuous at $x = 0$. Then what is value of a ?

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5. The function $f(x) = \begin{cases} \left[\frac{x^3 - 3x + 2}{x^2 - 10^2}, [K, \text{ if } x = 1] \right. \end{cases}$ is continuous for all x then what is value of k .

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6. If the function $f(x) = \frac{\sin 10x}{x}$ is continuous at $x = 0$ then what is $f(0)$?



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7. If $f(x) = \left\{ \left(\frac{x^3 - 8}{x - 2} \right), \text{ when } x \neq 2 \right\}, (k, \text{ when } x = 2) : \}$ is continuous at $x = 2$, then what is the value of k .



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8. Discuss the continuity of $f(x) = \left\{ \left(\frac{x^2 - 25}{x - 5} \right), \text{ when } x \neq 5 \right\}, (9, \text{ when } x = 5) : \}$



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9. Discuss the continuity of the function

$$f(x) = \left\{ \frac{\sin 3x}{2x}, \text{ when } x \neq 0 \right\}, \left(\frac{3}{2}, \text{ when } x = 0 \right) : \} \text{ at } x=0$$



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10. Show that the function $f(x) = \begin{cases} \frac{e^{1/x} - 1}{e^{1/x} + 1}, & \text{when } x \neq 0 \\ 0, & \text{when } x = 0 \end{cases}$ is discontinuous at $x = 0$.

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11. Examine the continuity of the function $f(x) = \begin{cases} \frac{1}{x + [x]} & \text{if } x < 0 \\ -1 & \text{if } x \geq 0 \end{cases}$ at $x=0$.

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12. Discuss the continuity of the function

$$f(x) = \begin{cases} \frac{|x|}{x}, & \text{if } x \neq 0 \\ 0, & \text{if } x = 0 \end{cases} \quad \text{at } x = 0.$$

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13. If a function is continuous at $x=a$, then find

$$\lim_{h \rightarrow 0} + \frac{1}{2} \{f(a+h) + f(a-h)\}$$

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14. Examine the continuity of $f(x) = \frac{\sin(\pi(x))}{2}$ at $x = 0$.

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15. Find the value of a such that the function f defined by

$$f(x) = \begin{cases} \frac{\sin ax}{\sin x} & \text{if } x \neq 0 \\ \frac{1}{a} & \text{if } x = 0 \end{cases}$$

is continuous at $x=0$.

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16. If $f(x) = \begin{cases} ax^2 + b & \text{if } x < 1 \\ 1 & \text{if } x = 1 \\ 2ax - b & \text{if } x > 1 \end{cases}$

is continuous at $x=1$, then find a and b .



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17. Show that $\sin x$ is continuous for every real x .



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18. For what value of k is the function defined by

$$\begin{cases} k(x^2 + 2) & \text{when } x \leq 0 \\ 3x + 1 & \text{when } x > 0 \end{cases} \text{Continuous at } x = 0. \text{ Also write whether the}$$

function is continuous at $x = 1$.



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19. Find the value of k if the function $f(x)$ defined by

$$f(x) = \begin{cases} 2x - 1 & \text{when } x < 2 \\ k & \text{when } x = 2 \\ x + 1 & \text{when } x > 2 \end{cases} \text{ is continuous at } x=2.$$



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20. For what value of λ is the function

$$f(x) = \begin{cases} \lambda(x^2 - 2x), & \text{if } x \leq 0 \\ 4x + 1, & \text{if } x > 0 \end{cases} \text{ continuous at } x=0?$$

What about continuity at $x=1$?



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21. Find the value of k , so that the function defined by

$$f(x) = \begin{cases} kx + 1, & \text{if } x \leq \pi \\ \cos x, & \text{if } x > \pi \end{cases} \text{ is continuous at } x = \pi.$$



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22. Examine the continuity of the following functions at the indicated

$$\text{points } f(x) = \begin{cases} 2x + 1 & \text{if } x \leq 0 \\ x & \text{if } 0 < x < 1 \text{ at } x = 0, 1. \\ 2x - 1 & \text{if } x \geq 1 \end{cases}$$

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23. Examine the continuity of the function f defined by $f(x) =$

$$\begin{cases} 2x + 1 & \text{if } x < 1 \\ 0 & \text{if } x = 1 \\ x^2 - 1 & \text{if } x > 1 \end{cases} .$$

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24. If $f(x) = \begin{cases} ax^2 + b & \text{if } x < 1 \\ 1 & \text{if } x = 1 \\ 2ax - b & \text{if } x > 1 \end{cases}$

is continuous at $x=1$, then find a and b .

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25. Find the relationship between a and b so that the function defined by

$$f(x) = \begin{cases} ax + b & \text{if } x \leq 3 \\ bx + 3 & \text{if } x > 3 \end{cases} \text{ is continuous at } x = 3.$$

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26. Find the value of a and b if the function given below is continuous.

$$f(x) = \begin{cases} 5 & \text{if } x \leq 2 \\ ax + b & \text{if } 2 < x < 10 \\ 21 & \text{if } x \geq 10 \end{cases}$$

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27. For what value of k the following function is continuous at $x = 0$?

$$f(x) = \begin{cases} \frac{1 - \cos 4x}{8x^2}, & x \neq 0 \\ k, & x = 0 \end{cases}$$

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28. If $f(x) = \begin{cases} ax^2 + b & \text{if } x < 1 \\ 1 & \text{if } x = 1 \\ 2ax - b & \text{if } x > 1 \end{cases}$

is continuous at $x=1$, then find a and b .

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29. Show that : $\sin^2 x$ is continuous for every real value of x .

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30. $f(x) = \begin{cases} x^2 \sin\left(\frac{1}{x}\right) & x \neq 0 \\ 0 & x = 0 \end{cases}$

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31. If 'f(x) = $\left\{ \left(\frac{1 - \cos 4x}{x^2} \right), \text{when } x < 0, (k, \text{when } x = 0), \left(\frac{\sqrt{x}}{\sqrt{16 + \sqrt{x}}} - 4 \right), \text{when } x > 0 \right\}$, and f is continuous at $x=0$, then find the value of k .

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32. Find the value of k so that the function f defined by

$$f(x) = \left\{ \left(\frac{k \cos x}{\pi - 2x} \right), \text{ when } x \neq \frac{\pi}{2}, \left(0, \text{ at } x = \frac{\pi}{2} \right) : \right\} \text{ is continuous at } x = \frac{\pi}{2}.$$

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33. If the function $f(x) = \begin{cases} 3ax + b, & \text{if } x > 1 \\ 11, & \text{if } x = 1 \\ 5ax - 2b, & \text{if } x < 1 \end{cases}$ is continuous at $x = 1$,

then find the values of a and b

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34. Find all points of discontinuity of f , where f is defined by

$$f(x) = \begin{cases} |x| + 3, & \text{if } x \leq -3 \\ -2x, & \text{if } -3 < x < 3 \\ 6x + 2, & \text{if } x \geq 3 \end{cases}$$

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35. Find the derivative of $\tan^{-1}\left(\frac{\cos x + \sin x}{\cos x - \sin x}\right)$ w.r.t. x .

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36. What is the derivative of $e^{3 \log x}$ w.r.t. x ?

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37. If $u = t^2$ and $v = \sin t^2$ then $dv/du =$ _____.

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38. If $y = \frac{\sec^{-1}(\sqrt{x} + 1)}{\sqrt{x}} + \sin^{-1} \frac{\sqrt{x}}{\sqrt{x} + 1}$ then $\frac{dy}{dx} =$ _____

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39. Write the derivative of $\sin x$ with respect to $\cos x$.



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40. If $y = \sin^{-1} \left[x\sqrt{1-x} - \sqrt{x}\sqrt{1-x^2} \right]$ then find $\frac{dy}{dx}$



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41. If $e^x + e^y = e^{x+y}$ then show that $\frac{dy}{dx} + e^{y-x} = 0$.



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42. Differentiate $\tan^{-1} \left(\frac{x}{\sqrt{1-x^2}} \right)$ w.r.t. $\sin^{-1} (2x\sqrt{1-x^2})$



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43. Differentiate $\tan^{-1} \left(\frac{x}{\sqrt{1-x^2}} \right)$ w.r.t. $\sin^{-1} (2x\sqrt{1-x^2})$



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44. Differentiate $\tan^{-1}\left(\frac{\sqrt{1+x^2}-1}{x}\right)$ w.r.t $\sin^{-1}\left(\frac{2x}{1+x^2}\right)$ when $x \neq 0$.

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45. Write that condition of Rolle's theorem which is violated by the function $f(x) = |x - 1|$ in $[0, 2]$.

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46. If $f(0) = 0, f'(0) = 2$ then what is the derivative of $y = f(f(f(f(x))))$ at $x=0$.

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47.

If

$$y = \tan^{-1}\left(\frac{1}{1+x+x^2}\right) + \tan^{-1}\left(\frac{1}{x^2+3x+3}\right) + \tan^{-1}\left(\frac{1}{x^2+5x+7}\right) + \dots$$

..... Up to n terms then find $y'(0)$.



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48. If $x = a\left(\cos t + \log \tan\left(\frac{t}{2}\right)\right)$, $y = a \sin t$, then what is $\frac{d^2y}{dx^2}$ at $t = \frac{\pi}{3}$.



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49. What is the first derivative of $\cos^{-1}\left(\sin\left(\frac{\sqrt{1+x}}{2}\right)\right) + x^x$ w.r.t x at $x=1$.



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50. If $f(x) = |\log x|$ then for $x \neq 1$, then what is $f'(x)$?



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51. If $y = |\cos x| + |\sin x|$ then what is $\frac{dy}{dx}$ at $x = \frac{2\pi}{3}$?



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52. If $f(x) = \log_x^2(\log x)$, then $f(e)$



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53. If $y = \tan^{-1} \left[\left(\frac{x}{\log e} x^3 \right) \right] + \tan^{-1} \left[\frac{5 + 3 \log x}{1 - 15 \log x} \right]$ then find $\frac{dy}{dx}$.



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54. If $f(x) = a|\sin x| + b.e^{|x|} + c|x|^3$ and $f(x)$ is differentiable at $x = 0$, then what are the values of a, b, c ?



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55. What is the value of the derivative of $f(x) = |x - 1| + |x - 3|$ at $x=2$?

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56. If $f(x+y) = f(x) f(y)$ for all x, y and if $f(5) = 2$ and $f(0) = 3$, then what is the value of $f'(5)$?

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57. Write the derivative of $e^{3 \log x}$ w.r.t. x^2

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58. Differentiate $a^{\ln x}$ w. r. tx^2 .

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59. If $x = \int_0^y \left(\frac{1}{\sqrt{1+4t}} \right) dt$ then what is the value of $\frac{d^2y}{dx^2}$.

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60. If x and y are variables related by the equation $x = \int_0^y \left(\frac{1}{\sqrt{1+9u^2}} \right) dx$, then what is the value of $\frac{dy}{dx}$?

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61. What is the derivative of $\sec^{-1}\left(\frac{1}{2x^2-1}\right)$, with respect to $(\sqrt{1-x^2})$?

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62. If $y = \sec^{-1}\left(\frac{x+1}{x-1}\right) + \sin^{-1}\left(\frac{x-1}{x+1}\right)$, then find $\frac{dy}{dx}$.

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63. Differentiate $\sin^{-1}(\cos x)$ w.r.t. x

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64. Differentiate $\cos^{-1}(\sin x)$ w.r.t. x .

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65. What is the derivative of $\sec^{-1} x$ w.r.t. x , if $x < -1$?

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66. What is the derivative of $\sin^{-1}(3x - 4x^3)$ w.r.t. $\sin^{-1} x$?

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67. What is the derivative of $\sin^{-1}\left(\frac{2x}{1+x^2}\right)$ w.r.t $\tan^{-1}\left(\frac{2x}{1-x^2}\right)$?

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68. Find $\frac{d}{dx} \cot^{-1} \tan\left(\frac{\pi}{2} - x\right)$.

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69. If $y = \frac{\sec^{-1}(\sqrt{x} + 1)}{\sqrt{x}} + \sin^{-1} \frac{\sqrt{x}}{\sqrt{x} + 1}$ then $\frac{dy}{dx} = \text{---}$

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70. What is the first derivative of $\cos^{-1}\left(\sin\left(\frac{\sqrt{1+x}}{2}\right)\right) + x^x$ w.r.t x at $x=1$.

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71. If $f(x) = |\log x|$ then for $x \neq 1$, then what is $f'(x)$?

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72. What is the derivative of $\tan^{-1}(\cos \sqrt{x})$.

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73. If $y = \cot^{-1}\left(\frac{\sqrt{1+x^2}}{x}\right)$ then $(dy)/(dx)=?$

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74. Find the derivative of $\cos^{-1}\left(\frac{\sqrt{1+x}}{2}\right)$.

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75. Differentiate $\cos^{-1}(4x^3 - 3x)$.



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76. Differentiate $\tan^{-1}\left(\frac{\sqrt{x} - x}{1 + x\sqrt{x}}\right)$.



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77. If $y = 10^x$ and $z = 100^{\frac{x}{2}}$ then find $\frac{d}{dx}\left(\frac{y^2}{z}\right)$.



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78. What is the derivative of $\cos(\sin^{-1} x)$ w.r.t $\cos^{-1} x$?



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79. What is the derivative of $\cos ec^{-1} x$ w. r. t x when $|x| > 1$.



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80. Find $\frac{dy}{dx}$ when $y = \log|x|$.

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81. Find $\frac{dy}{dx}$ at $t = \frac{1}{2}$ when $x = (at^2)$, $y=2at$.

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82. Find $\frac{d}{dx} \ln \sin^{-1} \cos \left(\frac{\pi - 2e^x}{2} \right)$.

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83. If $y = \tan^{-1} \left(\frac{a}{x} \right) + \log \sqrt{\frac{x-a}{x+a}}$, then prove that $\frac{dy}{dx} = \frac{2a^3}{x^4 - a^4}$.

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84. If $(\tan^{-1} x)^y + y^{\cot x} = 1$ then find $\frac{dy}{dx}$.



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85. If $x^y = e^{x-y}$ then prove that $\frac{dy}{dx} = \frac{\log x}{(1 + \log x)^2}$.



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86. If $y = x \log\left(\frac{x}{a+bx}\right)$ then prove that $x^3 \frac{d^2y}{dx^2} = \left(x \frac{dy}{dx} - y\right)^2$.



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87. If $y = (\sin x)^x + \sin^{-1} \sqrt{x}$, then find $\frac{dy}{dx}$.



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88. If $x = 2 \cos \theta - \cos 2\theta$ and $y = 2 \sin \theta - \sin 2\theta$, then prove that

$$\frac{dy}{dx} = \tan\left(\frac{3\theta}{2}\right)$$



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89. Differentiate the following function w.r.t. x ,

$$(\log x)^x + x^{\log x}.$$



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90. If $y = \log \left[x + \sqrt{x^2 + 1} \right]$, then prove that $(x^2 + 1) \frac{d^2y}{dx^2} + x \frac{dy}{dx} = 0$



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91. If $x = a \cos^3 \theta, y = a \sin^3 \theta$, then find $\frac{d^2y}{dx^2}$



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92. If $\sin y = x \sin (a + y)$ then show that $\frac{dy}{dx} = \frac{\sin^2(a + y)}{\sin a}$



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93. Find dy/dx if

$$x^m y^n = \left(\frac{x}{y}\right)^{m+n}$$

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94. Find $\frac{dy}{dt}$, when $y = \sin^{-1}\left(2\frac{\sqrt{t^2-1}}{t^2}\right)$

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95. If $x = a \sec \theta$, $y = b \tan \theta$, then prove that $\frac{d^2y}{dx^2} = -\frac{b^4}{a^2y^3}$

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96. IF $x^y = e^{x-y}$ then show that $\frac{dy}{dx} = \frac{\log x}{[\log(xe)]^2}$.

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97. If $\sin y = x \sin (a + y)$ then show that $\frac{dy}{dx} = \frac{\sin^2(a + y)}{\sin a}$

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98. If $x = a(\cos t + t \sin t)$ and $y = a(\sin t - t \cos t)$, then find $\frac{d^2y}{dx^2}$ at $t = \frac{\pi}{4}$.

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99. If $\cos x = \sqrt{\frac{1}{1+t^2}}$, $\sin y = \frac{2t}{1+t^2}$ then show that $\frac{dy}{dx}$ is independent of t .

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100. Find $\frac{dy}{dx}$, when $y^x = x^{\sin y}$



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101. If $y^2 \cot x = x^2 \cot y$ then find $\frac{dy}{dx}$.

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102. Find the derivative of $x^{\sin x}$ w.r.t.x.

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103. Differentiate $\sin^{-1}\left(\frac{2X}{1+X^2}\right)$ with respect to $\cos^{-1}\left(\frac{1-X^2}{1+X^2}\right)$.

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104. Differentiate $y = \tan^{-1} \frac{\sqrt{1+x^2} + \sqrt{1-x^2}}{\sqrt{1+x^2} - \sqrt{1-x^2}}$

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105. Differentiate $y = (\sin y)^{\sin 2x}$

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106. Test the differentiability and continuity of the following function at

$$x=0: f(x) = \begin{cases} \frac{1-e^{-x}}{x} & x \neq 0 \\ 1 & x = 0 \end{cases}$$

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107. What is the derivative of $\sec^{-1}\left(\frac{1}{2x^2 - 1}\right)$, with respect to $(\sqrt{1-x^2})$?

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108. If $y = \left(x + \frac{1}{x + \frac{1}{x + \dots \infty}}\right)$ find $\frac{dy}{dx}$, the rhs being a valid expression.

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109. If $y = e^{\sin^{-1} x}$ and $u = \log x$ then what is $\frac{dy}{du}$?

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110. Find the slope of the tangent to the curve $x = 2(\theta - \sin 2\theta)$, $y = 2(1 - \cos \theta)$ at $\theta = \frac{\pi}{4}$.

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111. If $\cos y = x \cos(a+y)$ then prove that

$$\frac{dy}{dx} = \frac{\cos^2(a+y)}{\sin a}$$

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112. Differentiate $\sec^{-1}\left(\frac{x+x^{-1}}{x-x^{-1}}\right)$ w.r.t. x .

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113. Prove that $y = \tan(x + y)$, then $\frac{dy}{dx} = \frac{1 + y^2}{-y^2}$

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114. Find $\frac{dy}{dx}$, if $y = \log_{x^2} 3$.

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115. Find $\frac{dy}{dx}$ when $y = 10^{\sin x}$.

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116. If $F(x) = \int_x^{x^2} e^{-t^4} dt$ then find $F^1(x)$.

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117.

If

$f(x) = \sin x$ and $g(x) = x^3$ then find the value of $[f(x) \cdot g(x)]'$ at $x = \frac{\pi}{2}$.

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118. Find the derivative of $\sin^{-1}\left(\frac{2x^3}{1+x^6}\right)$.

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119. Find the derivative of $\tan^{-1}(\cos^2 x)$.

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120. Examine the differentiability of $\ln x^2$ for all real values of x .

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121. Find $\frac{dy}{dx}$ when $y = \tan^{-1}\left(\frac{4x}{1+5x^2}\right) + \tan^{-1}\left(\frac{2+3x}{3-2x}\right)$.

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122. Differentiate $\sin^{-1}\left(\frac{2X}{1+X^2}\right)$ with respect to $\cos^{-1}\left(\frac{1-X^2}{1+X^2}\right)$.

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123. Find $\frac{dy}{dx}$ when $y = x^y$.

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124. If $2z = x\left(2 + \frac{dz}{dx}\right)$, then prove that $\frac{d^2z}{dx^2}$ is a constant.

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125. If $\sin(x + y) = y \cos(x + y)$ then prove that

$$\frac{dy}{dx} = -\frac{1 + y^2}{y^2}$$

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126. If $e^{y/x} = \frac{x}{a + bx}$ then show that $x^3 \frac{d}{dx} \left(\frac{dy}{dx} \right) = \left(x \frac{dy}{dx} - y \right)^2$

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127. If $(\cos x)^y = (\cos y)^x$, then find $\frac{dy}{dx}$.

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128. If $x = \sqrt{a^{\sin^{-1} t}}$, $y = \sqrt{a^{\cos^{-1} t}}$, then show that $\frac{dy}{dx} = -\frac{y}{x}$.

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129. Differentiate $\tan^{-1} \left(\frac{\sqrt{1+x^2}-1}{x} \right)$ w. r. to x .

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130. If $y = (\tan^{-1} x)^2$ then show that $(x^2 + 1)^2 \frac{d^2y}{dx^2} + 2x(x^2 + 1) \left(\frac{dy}{dx} \right) = 2$.

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131. If $y = x^{\sin x - \cos x} + \frac{x^2 - 1}{x^2 + 1}$, then find $\frac{dy}{dx}$

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132. If $x = a(\cos t + t \sin t)$ and $y = a(\sin t - t \cos t)$, then find $\frac{d^2y}{dx^2}$ at $t = \frac{\pi}{4}$.

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133. If $x = \cos t + \log \tan t/2$ and $y = \sin t$, then find the value of

$$\frac{d^2y}{dt^2} \text{ and } \frac{d^2y}{dx^2} = \frac{\pi}{4}.$$



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134. If $x\sqrt{1+y} + y\sqrt{1+x} = 0$ for $-1 < x, y < 1$ then prove that

$$\frac{dy}{dx} = \frac{-1}{(x+1)^2}$$



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135. If $x = \tan(1/a \log y)$, show that $(1+x^2)d^2y/dx^2 + (2x-a)dy/dx = 0$.



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136. Differentiate the following function w.r.t.x

$$\tan^{-1} \left(\frac{\sqrt{1+x} - \sqrt{1-x}}{\sqrt{1+x} + \sqrt{1-x}} \right).$$



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137. If $y = \sin^{-1} \left[\left(\frac{5x + 12(\sqrt{1-x^2})}{13} \right) \right]$ then find $\frac{dy}{dx}$.

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138. If $y = \tan(x + y)$, then find $\frac{dy}{dx}$.

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139. If $y = x^{\cot x} + (\sin x)^x$ then find $\frac{dy}{dx}$.

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140. If $y = \frac{\sin^{-1} x}{\sqrt{1-x^2}}$, then prove that $(1-x^2) \frac{d^2y}{dx^2} - 3x \frac{dy}{dx} - y = 0$.

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141. If $x = \frac{1 - \cos^2 \theta}{\cos \theta}$, $y = \frac{1 - \cos^{2n} \theta}{\cos^n \theta}$ then show that

$$\left(\frac{dy}{dx}\right)^2 = n^2 \left(\frac{y^2 + 4}{x^2 + 4}\right)$$

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142. If $y = (\log x)^{\cos x} + \frac{x^2 + 1}{x^2 - 1}$ find $\frac{dy}{dx}$.

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143. If $y = \cos^{-1} \left[\frac{3x + 4\sqrt{1 - x^2}}{5} \right]$ then find $\frac{dy}{dx}$.

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144. Prove that

$$\cot^{-1} \left(\frac{\sqrt{1 + \sin x} + \sqrt{1 - \sin x}}{\sqrt{1 + \sin x} - \sqrt{1 - \sin x}} \right) = \frac{x}{2}, 0 < x < \frac{\pi}{2}, \text{ or } x \in \left(0, \frac{\pi}{4}\right)$$



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145. Differentiate $\sin^{-1}\left(2ax\sqrt{1-a^2x^2}\right)$ with respect to $\sqrt{1-a^2x^2}$.



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146. If $\sin(x+y) = y \cos(x+y)$ then prove that

$$\frac{dy}{dx} = -\frac{1+y^2}{y^2}$$



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147. Find $\frac{dy}{dx}$ when $y = \cot^{-1}(\cos ecx) + \frac{x \sin^{-1} x}{\sqrt{1-x^2}}$.



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148. Find the derivative of $\left(\frac{x-1}{x^2+5}\right)^{-4} \cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$



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149. Find $\frac{dy}{dx}$ when $y = \tan^{-1} \sqrt{\frac{1 + \sin x}{\sin x}}$.

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150. Find $\frac{dy}{dx}$ when $(x+y)^{p+q} = x^p y^q$.

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151. If $x e^{xy} + y = \sin^2 x$, then find $\frac{dy}{dx}$ at $x=0$.

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152. If $\sin y = x \sin (a + y)$ then show that $\frac{dy}{dx} = \frac{\sin^2(a + y)}{\sin a}$

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153. If $x=a \cos^3 \theta, y=a \sin^3 \theta$, then find $\frac{d^2y}{dx^2}$

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154. Differentiate $\tan^{-1} \left(\frac{1 + \sin x}{1 - \sin x} \right)^{\frac{1}{2}}$ with respect to $\left(\frac{1 + \cos x}{1 - \cos x} \right)$.

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155. Find $\frac{dy}{dx}$ when $x = e^{\tan^{-1} \left(\frac{y-x^2}{x^2} \right)}$.

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156. If $y = x^{\sin^{-1}x} + x^3 \left(\frac{\sqrt{x^2 + 4}}{\sqrt{x^3 + 3}} \right)$ then find $\frac{dy}{dx}$.

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