



MATHS

BOOKS - SHARAM PUBLICATION

MODEL QUESTION PAPER 13

Exercise

1. If $f: \mathbb{R} \rightarrow \mathbb{R}$ is defined by $f(x) = 3x + 2$ define $f(f(x))$



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2. If $\sin^{-1}\left(\frac{\pi}{5}\right) + \cos ec^{-1}\left(\frac{5}{4}\right) = \frac{5}{2}$.



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3. Evaluate $\begin{vmatrix} \sin^2 x & \cos^2 x & 1 \\ \cos^2 x & \sin^2 x & 1 \\ -10 & 12 & 2 \end{vmatrix} ?$

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4. If I_n is an identity matrix of order n , then k being a natural number, write the matrix I_n^k .

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5. If a function $f(x)$ is defined by $f(x) = \begin{cases} (1 + 7x)^{\frac{1}{x}} & \text{when } x \neq 0 \\ k & \text{when } x = 0 \end{cases}$ is

continuous at $x = 0$, then what is the value of k ?

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6. What is the maximum value of the function $f(x) = \sin x (1 + \cos x)$?

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7. Write the value of $\int_0^{\frac{\pi}{2}} \frac{\sin x}{\sin x + \cos x} dx - \int_0^{\frac{\pi}{2}} \frac{\cos x}{\sin x + \cos x} dx$

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8. If p and q are the order and degree of the differential equation

$$y \left(\frac{dy}{dx} \right)^2 + x^2 \frac{d^2y}{dx^2} + xy = \sin x, \text{ then choose the correct statement}$$

out of

$$p < q$$

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9. Write the value of the cosine of the angle which the vector

$$\vec{a} = \hat{i} + \hat{j} + \hat{k} \text{ makes with y-axis}$$

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10. Write the intercepts cutoff by the plane $2x+y-z =5$ on three axes.

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11. Show that the relation S in set $A = \{x \in \mathbb{Z} : 0 \leq x \leq 12\}$ given by $S = \{(a, b) : a, b \in A, |a - b| \text{ is divisible by } 4\}$ is an equivalence relation. Find the set of all elements related to 1.

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12. Prove that $\tan^{-1} \sqrt{x} = \frac{1}{2} \cos^{-1} \left(\frac{1-x}{1+x} \right), x \in (0, 1)$.

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13. Solve: $\sin^{-1} \left(\frac{2a}{1+a^2} \right) + \sin^{-1} \left(\frac{2b}{1+b^2} \right) = 2 \tan^{-1} x$.

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14. Solve the following LPP graphically

$$\text{Maximize, } Z = 20x + 30y$$

$$\text{Subject to } 3x + 5y \leq 15$$

$$x, y \geq 0.$$



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15. Find the inverse of the matrix

$$\begin{bmatrix} 0 & 0 & 2 \\ 0 & 2 & 0 \\ 2 & 0 & 0 \end{bmatrix}.$$



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16. If $A = \begin{bmatrix} 3 & -4 \\ 1 & -1 \end{bmatrix}$ then show that $A^k = \begin{bmatrix} 1 + 2k & -4k \\ k & 1 - 2k \end{bmatrix}, k \in \mathbb{N}$



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17. Prove without expanding that
$$\begin{vmatrix} bc & a & a^2 \\ ca & b & b^2 \\ ab & c & c^2 \end{vmatrix} = \begin{vmatrix} 1 & a^2 & a^3 \\ 1 & b^2 & b^3 \\ 1 & c^2 & c^3 \end{vmatrix}$$

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18. Solve:
$$\begin{vmatrix} x - a & 0 & 0 \\ a & x - b & 0 \\ a & b & x - c \end{vmatrix} = 0$$

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19. Prove that:
$$\begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^2 & b^2 & c^2 \end{vmatrix} = (a - b)(b - c)(c - a)$$

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20. Find the value of k , so that the function defined by

$$f(x) = \begin{cases} kx + 1, & \text{if } x \leq \pi \\ \cos x, & \text{if } x > \pi \end{cases} \text{ is continuous at } x = \pi.$$

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21. If $x^y = e^{x-y}$ then prove that $\frac{dy}{dx} = \frac{\log x}{(1 + \log x)^2}$.

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22. If $x = a \sec \theta$, $y = b \tan \theta$, then prove that $\frac{d^2y}{dx^2} = -\frac{b^4}{a^2y^3}$

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23. Find the points on the curve $x^2 + y^2 - 2x - 3 = 0$ at which the tangents are parallel to X-axis.

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24. For which value of x , the function $f(x) = 4 - x - x^2$ is maximum or minimum.



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25. Evaluate $\int (x + 3)^2 dx$



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26. Evaluate $\int_0^{\pi} \left(\frac{2}{4}\right) \sin \sqrt{x} dx$



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27. Evaluate $\int \sin^{-1} x dx$



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28. Find the area bounded by the line $y = 2x$, x - axis and the ordinate $x = 3$.



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29. Solve $\frac{dy}{dt} = e^{3t+5y}$

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30. If the position vectors of the points A, B, C are $2\hat{i} + \hat{j} - \hat{k}$, $3\hat{i} - 2\hat{j} + \hat{k}$ and $\hat{i} + 4\hat{j} - 3\hat{k}$ respectively, then prove that A, B, C are collinear.

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31. If $\vec{a} = (2,-2,1)$, $\vec{b} = (2,3,6)$ and $\vec{c} = (-1,0,2)$, Find the magnitude and direction of $\vec{a} - \vec{b} + 2\vec{c}$.

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32. Find the perpendicular distance of the point $(-1, 3, 9)$ from the

line $\frac{x - 13}{5} = \frac{y + 8}{-8} = \frac{z - 31}{1}$

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33. Find the equation of the plane passing through $(3, -6, -9)$ and parallel to xz plane

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34. If $f: R \rightarrow R$, $g: R \rightarrow R$ and $h: R \rightarrow R$ such that $f(x) = x^2$, $g(x) = \tan x$

and $h(x) = \log x$ then find $[h \circ (g \circ f)](x)$ at $x = \frac{\sqrt{\pi}}{2}$

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35. If

$\cos^{-1}\left(\frac{x}{a}\right) = \cos^{-1}\left(\frac{y}{b}\right) = \theta$, prove that $\frac{x^2}{a^2} - \frac{2xy}{ab}\cos\theta + \frac{y^2}{b^2} = \sin^2\theta$.



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36. Prove the following:

$$\begin{bmatrix} a + b + c & -c & -b \\ -c & a + b + c & -a \\ -b & -a & a + b + c \end{bmatrix}$$

$$= 2(b+c)(c+a)(a+b)$$



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37. Evaluate $\int_0^{\pi/2} \frac{\cos x}{(2 + \sin x)(3 + \sin x)} dx$



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38. Find the area of the region between the curves

$$y = \cos x \text{ and } y = \sin x, x \in \left[0, \frac{\pi}{4}\right].$$



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39. Solve $(x-y+1)dx-(x+y+5)dy=0$



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40. Show that the following vector are co-planar.

$$\hat{i} - 2\hat{j} + 2\hat{k}, 3\hat{i} + 4\hat{j} + 5\hat{k}, -2\hat{i} + 4\hat{j} - 4\hat{k}.$$



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41. Find the equation of the plane through the points $(2, 2, 1)$ and $(9, 3, 6)$ and perpendicular to the plane $2x + 6y + 6z - 1 = 0$.



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