



MATHS

BOOKS - SHARAM PUBLICATION

QUESTION PAPER 2014

Exercise

1. What do you mean by integration ? Write your answer in one sentence.



Watch Video Solution

2. Write the differential equation of the family of straight lines parallel to the y-axis.



[Watch Video Solution](#)

3. Is $\vec{0}$ unique



[Watch Video Solution](#)

4. Under which conditions the straight line $\frac{x - a}{l} = \frac{y - b}{m} = \frac{z - c}{n}$ intersects the plane $Ax + By + Cz = 0$ at a point other than (a,b,c) ?



[Watch Video Solution](#)

5. How many straight lines in space through the origin are equally inclined to the coordinate axes?



[Watch Video Solution](#)

6. If a_{ij} is an element in i th row and j th column of a 3rd order determinant and c_{ij} be the cofactor of a_{ij} , then what is the value of $a_{12}c_{12} - a_{21}c_{21} + a_{13}c_{13} - a_{31}c_{31}$?



[Watch Video Solution](#)

7. What is the value of :

$$C_3^{20} + C_4^{20} + C_5^{20} + \dots + C_{17}^{20} ?$$



[Watch Video Solution](#)

8. If an event A is independent of it self, then what is $P(A)$?



Watch Video Solution

9. If $y = \cos ec^{-1}x$, then find $\frac{dy}{dx}$ and determine its value at $x = -2$.



Watch Video Solution

10. Examine the differentiability of $\ln x^2$ for all real values of x .



[Watch Video Solution](#)

11. Interpret Lagrange's mean value theorem geometrically.



[Watch Video Solution](#)

12. Evaluate: $\lim_{x \rightarrow 0} \left(\frac{\sin x}{x} \right)^{\frac{1}{x}}$



Watch Video Solution

13. Evaluate the following integrals :

$$\int \frac{dx}{x^{\frac{1}{2}} + x^{\frac{1}{3}}}$$



Watch Video Solution

14. $\int \frac{x e^x}{1 + x^2} dx$



Watch Video Solution

15. Evaluate: $\int_0^{\frac{3}{2}} [x^2] dx.$



[Watch Video Solution](#)

16. Find the area of the region bounded by the curve $y = \sin x$ and the straight lines $x = -\frac{\pi}{4}$, $x = \frac{\pi}{4}$ and $y = 0$.



[Watch Video Solution](#)

17. Solve the following differential equations

$$(1 + y^2)dx + (x - e^{-\tan^{-1}y})dy = 0$$



Watch Video Solution

18. Solve : $(x + y)dy + (x - y)dx = 0$.



Watch Video Solution

19. Find the differential equation whose general solution is $ax^2 + by = 1$, where a and

b are arbitrary constants.



[Watch Video Solution](#)

20. If the sum of two unit vectors is a unit vector find the magnitude of their difference.



[Watch Video Solution](#)

21. Find the value of λ such that the following vectors are coplanar:

$$-\hat{i} + \lambda\hat{j} - \lambda\hat{k}, 2\hat{i} + 4\hat{j} + 5\hat{k}, -2\hat{i} + 4\hat{j} - 4\hat{k}$$



[Watch Video Solution](#)

22. Find the co-ordinates of the foot of the perpendicular from the point $(1, 1, 1)$ on the line joining $(1, 4, 6)$ and $(54, 4)$.



[Watch Video Solution](#)

23. Find the equation of the plane Parallel to the plane $2x - y + 3z + 1 = 0$ and at a distance 3 units away from it.



[Watch Video Solution](#)

24. Using the method of elimination find the symmetrical form of equation of the line

$$6x + 8y + 3z = 10 \text{ and } x + 2y + z = 3.$$



[Watch Video Solution](#)

25. Solve the following LPP graphically

$$\text{Maximize, } Z = 20x + 30y$$

$$\text{Subject to } 3x + 5y \leq 15$$

$$x, y \geq 0.$$



Watch Video Solution

26. If A and B are square matrices of same order, then show by means of an example that $AB \neq BA$ in general.



Watch Video Solution

27. If $A = \begin{bmatrix} 0 & -\tan\left(\frac{\alpha}{2}\right) \\ \tan\left(\frac{\alpha}{2}\right) & 0 \end{bmatrix}$ show that
 $(I + A) = (I - A) \begin{bmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{bmatrix}$ where

$$I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$



[Watch Video Solution](#)

28. Five cities A,B,C,D,E are connected to each other by straight roads. What is the total number of such roads?



[Watch Video Solution](#)

29. Two balls are drawn from a bag containing 6 red and 4 yellow balls. Find the probability

that at least one of the ball is yellow?



[Watch Video Solution](#)

30. A person draws three cards at random one after another from a pack of 52 cards. Find the probability that all these cards are spades.



[Watch Video Solution](#)

31. Evaluate: $\int_0^{\pi} \frac{x}{1 + \sin x} dx$





Watch Video Solution

32. Solve the following differential equations

$$(x + \tan y)dy = \sin 2y dx$$



Watch Video Solution

33. Prove that by vector method, in any

$$\Delta ABC, \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}.$$



Watch Video Solution

34. Find the equation of the sphere inscribed in a tetrahedron whose faces are $x = 0$, $y = 0$, $z = 0$ and $2x + 2y + z = 1$.



Watch Video Solution

35. Solve the following LPP

$$\text{Maximise } Z = 20x + 10y$$

$$\text{Subject to } x + 2y \leq 40,$$

$$3x + y \geq 30,$$

$$4x + 3y \geq 60,$$

$$x, y \geq 0.$$



Watch Video Solution

36. Solve the following system of equations by the matrix inversion method.

$$x + y + z = 4$$

$$2x - y + 3z = 1$$

and $3x + 2y - z = 1$



Watch Video Solution

37. prove that :-

$$C_1 - \frac{1}{2}C_2 + \frac{1}{3}C_3 + \dots + (-1)^{n+1} \frac{1}{n}C_n =$$

$$1 + \frac{1}{2} + \dots + \frac{1}{n}$$



Watch Video Solution

38. The probability of a shooter hitting a target is $\frac{3}{4}$. Find the minimum number of times he must fire, so that the probability of hitting the target at least once is greater than 0.999.



Watch Video Solution