



## MATHS

### BOOKS - MBD MATHS (ODIA ENGLISH)

### THREE DIMENSIONAL GEOMETRY

#### Question Bank

1. The number of lines making equal angles with coordinate axes is\_\_\_\_\_.

A. 1

B. 2

C. 4

D. 8

**Answer:**



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2. Fill in the blanks in the length of the projection of the line segment joining  $(1,3,-1)$  and  $(3,2,4)$  on z-axis is \_\_\_\_\_.

[1, 3, 4, 5]

A. 1

B. 3

C. 4

D. 5

**Answer:**



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3. If a line is perpendicular to z-axis and makes an angle measuring  $60^{\circ}$  with x-axis, then the angle it makes with y-axis measures\_\_\_\_\_.

A.  $30^{\circ}$

B.  $60^{\circ}$

C.  $90^{\circ}$

D.  $120^0$

**Answer: C**



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4. If the distance between the points  $(-1, -1, z)$  and  $(1, -1, 1)$  is  $2\sqrt{2}$  then  $z =$  \_\_\_\_\_.

A. 1

B.  $\sqrt{2}$

C. 2

D. 0

**Answer: A**



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5. The line through  $(1, -1, 2)$  and  $(-2, -1, 2)$  is always perpendicular to z-axis.



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6. The line passing through  $(0, 0, 0)$  and  $(1, 2, 3)$  has direction cosines  $(-1, -2, -3)$



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7. If  $l, m, n$  be three real numbers proportional to the direction cosines of  $L$ , then  $l^2 + m^2 + n^2 = 1$ .

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8. If  $\alpha, \beta, \gamma$  be any three arbitrary angles then  $\cos \alpha, \cos \beta, \cos \gamma$  can always be considered as the direction cosines of a line.

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9. If two lines are perpendicular to a third line, then the direction ratios of the two lines are proportional.

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10. Show that the points  $(3,-2,4)$ ,  $(1,1,1)$  and  $(-1,4,-1)$  are collinear.



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11. Show that points  $(0,1,2)$ ,  $(2,5,8)$ ,  $(5,6,6)$  and  $(3,2,0)$  form a parallelogram.



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**12.** Find the co-ordinates of the foot of the perpendicular from the point  $(1, 1, 1)$  on the line joining  $(1, 4, 6)$  and  $(54, 4)$ .

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**13.** Find the co-ordinates of the point where the perpendicular from the origin meets the line joining the points  $(-9, 4, 5)$  and  $(11, 0, -1)$ .

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14. Prove that the points  $P(3,2,-4)$ ,  $Q(5,4,-6)$  and  $R(9,8,-10)$  are collinear. Find the ratio in which the point  $Q$  divides the line segment  $PR$ .

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15. If  $P(1, y, z)$  lies on the line through  $(3, 2, -1)$  and  $(-4, 6, 3)$  find  $y$  &  $z$ .

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16. If  $A, B, C, D$  are the points  $(6, 3, 2)$ ,  $(3, 5, 7)$ ,  $(2, 3, -1)$  and  $(3, 5, -3)$

respectively, then find the projection of  $\overline{AB}$  on  $\overleftrightarrow{CD}$



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17. The projection of a line segment  $\overline{OP}$ , through origin O, on the co-ordinate axes are 6, 2, 3. Find the length of the line segment OP and its direction cosines.



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18. The projection of a line segment of x, y and z-axis respectively are 12, 4, 3. Find the length and the direction cosines of the line segment.



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19. If A, B, C are the points  $(1, 4, 2)$ ,  $(-2, 1, 2)$  and  $(2, -3, 4)$  respectively then find the angles of the triangle ABC.



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20. Find the acute angle between the lines passing through  $(-3, -1, 0)$ ,  $(2, -3, 1)$  and  $(1, 2, 3)$ ,  $(-1, 4, -2)$  respectively.



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21. Prove the following by vector method. Measure of the angle between two diagonals of a cube is

$$\cos^{-1}\left(\frac{1}{3}\right)$$



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22. Prove the angle between the diagonal of one of the faces of the cube and the diagonal of the cube intersecting the diagonal of the face of the cube is

$$\cos^{-1}\sqrt{\frac{2}{3}}$$



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23. Find the angle which a double ordinate of length  $2a$  subtends at its vertex and focus.

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24. Find the angle between the lines whose dcs.  $l, m, n$  are connected by the relation,  
 $3l + m + 5n = 0$  and  $6mn - 2nl + 5lm = 0$

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25. If  $l_1, m_1, n_1$  and  $l_2, m_2, n_2$  are the direction cosines of two mutually perpendicular lines show that

the d.c.s. Of the line perpendicular to both of them are

$$m_1n_2 - n_1m_2, n_1l_2 - l_1n_2, l_1m_2 - m_1l_2$$



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**26.** State True or False .Through any four points one and only one plane can pass.



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**27.** State True or False . The equation of xy-plane is  $x + y = 0$ .



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**28.** The plane  $ax + by + c = 0$  is perpendicular to z-axis.



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**29.** The equation of the plane parallel to xz-plane and passing through  $(2, -4, 0)$  is  $y + 4 = 0$ .



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**30.** State True or False .The planes  $2x - y + z - 1 = 0$  and  $6x - 3y + 3z = 1$  are coincident.

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**31.** State true or False .The planes  $2x + 4y - z + 1 = 0$  and  $x - 2y - 6z + 3 = 0$  are perpendicular to each other.

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**32.** The distance of a point from a plane is same as the distance of the point from any line lying in that plane.

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33. The equation of a plane passing through  $(1, 1, 2)$  and parallel to  $x + y + z - 1 = 0$  is \_\_\_\_\_

A.  $x + y + z = 0$

B.  $x + y + 2z - 1 = 0$

C.  $x + y + z = 0$

D.  $x + y + z = 4$

**Answer: D**



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34. The equation of plane perpendicular to z-axis and passing through  $(1, -2, 4)$  is \_\_\_\_\_

A.  $x = 1$

B.  $y + 2 = 0$

C.  $z - 4 = 0$

D.  $x + y + z - 3 = 0$

**Answer: D**



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35. The distance between the parallel planes

$$2x - 3y + 6z + 1 = 0 \quad \text{and} \quad 4x - 6y + 12z - 5 = 0$$

is \_\_\_\_\_

A.  $\frac{1}{2}$

B.  $\frac{1}{7}$

C.  $\frac{4}{7}$

D.  $\frac{6}{7}$

**Answer: A::B::C**



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36. The plane  $y - z + 1 = 0$  is \_\_\_\_\_

- A. parallel to x-axis
- B. perpendicular to x-axis
- C. parallel xy-plane
- D. perpendicular to yz-plane

**Answer: A::B::C::D**



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37. A plane whose normal has direction ratios  $\langle 3, -2, k \rangle$  is parallel to the line joining  $(-1, 1, -4)$

and  $(5,6,-2)$ . Then the value of  $k = \dots\dots\dots [6,-4,-1,0]$

A. 6

B. -4

C. -1

D. 0

**Answer: D**



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**38.** Find the equation of planes passing through the points  $(6, -1, 1)$ ,  $(5,1,2)$  and  $(1,-5,-4)$



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**39.** Find the equation of planes passing through the points  $(2, 1, 3)$ ,  $(3, 2, 1)$  and  $(1, 0, -1)$

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**40.** Find the equation of planes passing through the points  $(-1, 0, 1)$ ,  $(-1, 4, 2)$  and  $(2, 4, 1)$

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**41.** Find the equation of planes passing through the points  $(-1, 5, 4)$ ,  $(2, 3, 4)$  and  $(2, 3, -1)$

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**42.** Find the equation of planes passing through the points  $(1, 2, 3)$ ,  $(1, -4, 3)$  and  $(-1, 3, 2)$

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**43.** Find the equation of the plane .Passing through the point  $(2, 3 - 1)$  and parallel to the plane  $3x - 4y + 7z = 0$ .

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**44.** Passing through the point  $(2, -3, 1)$  and  $(-1, 1 - 7)$  and perpendicular to the plane  $x - 2y + 5z + 1 = 0$ .



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**45.** Find the equation of the plane passing through the foot of the perpendiculars drawn from  $P(a,b,c)$  on the co-ordinate planes.



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**46.** passing through the point  $(-1, 3, 2)$   
perpendicular to the planes  $x + 2y + 2z = 5$  and  
 $3x + 3y + 2z = 8$ .

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**47.** Bisecting the line segment joining  $(-1, 4, 3)$  and  
 $(5, -2, -1)$  at right angles.

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**48.** Find the equation of the plane Parallel to the plane  
 $2x - y + 3z + 1 = 0$  and at a distance 3 units away

from it.



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**49.** Write the equation of the plane  $3x - 4y + 6z - 12 = 0$  in intercept form and hence obtain the co-ordinates of the point where it meets the co-ordinate axes.



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**50.** Write the equation of the plane  $2x - 3y + 5z + 1 = 0$  in normal form and find its

distance from the origin. Find also the distance between from the point (3,1,2).

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51. Find the distance between the parallel planes  $2x - 2y + z + 1 = 0$  and  $4x - 4y + 2z + 3 = 0$ .

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52. In each of the following case, verift whether the four given points are coplanar or not.  
(1, 2, 3), ( - 1, 1, 10), (2, 1, 3), (1, 1, 2)

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**53.** In each of the following case, verify whether the four given points are coplanar or not.

$(1, 1, 1), (3, 1, 2), (1, 4, 0), (-1, 1, 0)$



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**54.** In each of the following case, verify whether the four given points are coplanar or not.

$(0, -1, -1), (4, 5, 1), (3, 9, 4), (-4, 4, 4)$



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55. In each of the following case, verify whether the four given points are coplanar or not.

$(-6, 3, 2), (3, -2, 4), (5, 7, 3)$  and

$(-13, 17, -1)$ .



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56. Find the equation of the plane Passing through the intersection of planes

$2x + 3y - 4z + 1 = 0$  and  $2x - y + z + 2 = 0$  and

passing through the point  $(3,2,1)$ .



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**57.** Find the equation of the plane Which contains the line of intersection of the planes  $x + 2y + 3z - 4 = 0$  and  $2x + y - z + 5 = 0$  and perpendicular of the plane  $5x + 3y + 6z + 8 = 0$ .



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**58.** Find the equation of the plane Passing through the intersection of  $ax + by + cz + d = 0$  and  $a_1x + b_1y + c_1z + d_1 = 0$  perpendicular to xy-plane.



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**59.** Find the equation of the plane Passing through the intersection of the planes  $x + 3y - z + 1 = 0$  and  $3x - y + 5z + 3 = 0$  and is at a distance  $2/3$  units from origin.



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**60.** Find the angle between the following pairs of planes.  $x + 3y - 5z + 1 = 0$  and  $2x + y - z + 3 = 0$



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**61.** Find the angle between the following pairs of planes.

$$x + 2y + 2z - 3 = 0$$

and

$$3x + 4y + 5z + 1 = 0$$



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**62.** Find the angle between the following pairs of planes.  $x + 2y + 2z - 7 = 0$  and  $2x - y + z = 6$



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**63.** Find the equation of the bisector of the angles between the following pairs of planes and specify the



ones which bisects the acute angles ,

$$3x - 6y + 2z + 5 = 0 \text{ and } 4x - 12y + 3z - 3 = 0$$

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**64.** Find the equation of the bisector of the angles between the following pairs of planes and specify the

ones which bisects the acute angles ,

$$2x + y - 2z - 1 = 0 \text{ and } 4x - 12y + 3z + 3 = 0$$

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**65.** Show that the origin lies in the interior of the acute angle between planes.  $x + 2y + 2z + 9$  and

$4x - 3y + 12z + 13 = 0$ , Find the equation of bisector of the acute angle.

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**66.** Prove that the line joining  $(1, 2, 3)$ ,  $(2, 1, -1)$  intersects the line joining  $(-1, 3, 1)$  and  $(3, 1, 5)$ .

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**67.** Show that the point  $\left(-\frac{1}{2}, 2, 0\right)$  is the circumcentre of the triangle formed by the points  $(1, 1, 0)$ ,  $(1, 2, 1)$  and  $(-2, 2, -1)$ .

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**68.** Show that plane  $ax + by + cz + d = 0$  divides the line segment joining  $(x_1, y_1, z_1)$  and  $(x_2, y_2, z_2)$  in a ratio  $-\frac{ax_1 + by_1 + cz_1 + d}{ax_2 + by_2 + cz_2 + d}$



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**69.** A variable plane is at a constant distance  $p$  from the origin and meets the axes at A,B,C. Through A,B,C plane are drawn parallel to the co-ordinate planes.

Show that the locus of their points of intersection is

$$\frac{1}{x^2} + \frac{1}{y^2} + \frac{1}{z^2} = \frac{1}{p^2}.$$



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**70.** A variable plane passes through a fixed point  $(a,b,c)$  and meets the co-ordinate axes at  $A,B,C$ . Show that the locus of the point common to the planes drawn through  $A,B$  and  $C$  parallel to the co-ordinate planes is

$$\frac{a}{x} + \frac{b}{y} + \frac{c}{z} = 1$$



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**71.** The plane  $4x + 7y + 4z + 81 = 0$  is rotated through a right angle about its line of intersection with the plane  $5x + 3y + 10z - 25 = 0$ . Find the equation of the plane in new position.



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72. The plane  $lx + my = 0$  is rotated about its line of intersection with the plane  $z=0$  through angle measure  $\alpha$ . Prove that the equation of the plane in new position is  $lx + my \pm z\sqrt{l^2 + m^2} \tan \alpha = 0$



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73. State which of the following statements are true (T) or false(F)

The line  $\frac{x - 1}{2} = \frac{y - 1}{2} = \frac{z - 1}{2}$  pass though the origin.



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**74.** State which of the following statements are true (T) or false(F)

The line  $\frac{x+2}{-1} = \frac{y-3}{2} = \frac{z+4}{k}$  and  $\frac{x-4}{-4} = \frac{y-3}{k} = \frac{z+1}{2}$  are perpendicular at value of  $k=-1$ .



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**75.** State which of the following statements are true (T) or false(F)

The line  $\frac{x+5}{-2} = \frac{y-3}{1} = \frac{z-2}{3}$  lies on the plane  $x-y+z+1=0$ .



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76. State which of the following statements are true

(T) or false(F)

The line  $\frac{x - 2}{3} = \frac{1 - y}{4} = \frac{5 - z}{1}$  is parallel to the plane  $2x - y - 2z = 0$ .



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77. State which of the following statements are true

(T) or false(F)

The line  $\frac{x + 3}{-1} = \frac{y - 2}{3} = \frac{z - 1}{4}$  is perpendicular to the plane  $3x - 3y + 3z - 1 = 0$

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78. The line  $\frac{x + 2}{-4} + \frac{y - 1}{5} = \frac{z - 1}{3}$  and  $\frac{1 - x}{-4} = \frac{y - 0}{5} = \frac{2 - z}{3}$  are \_\_\_\_\_

- A. parallel
- B. perpendicular
- C. coincident
- D.

**Answer: A::C::D**

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79. The line passing through  $(-1,0,1)$  and perpendicular to the plane  $x+2y+1=0$  is \_\_\_\_\_

A.  $\frac{x + 1}{1} = \frac{y - 0}{2} = \frac{z - 1}{2}$

B.  $\frac{x + 1}{1} = \frac{y}{2} = \frac{z - 1}{0}$

C.  $\frac{x - 1}{1} = \frac{y - 0}{2} = \frac{z - 1}{0}$

D.

Answer: A::B



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80. The line  $\frac{x + 1}{2} = \frac{y - 6}{1} = \frac{z - 4}{0}$  is \_\_\_\_\_

- A. parallel to x-axis
- B. perpendicular to y-axis
- C. perpendicular to z-axis
- D.

**Answer: perpendicular to z-axis**



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81. If the line  $\frac{x - 3}{2} = \frac{y + k}{-1} = \frac{z + 1}{-5}$  lies on the plane  $2x - y + z - 7 = 0$ ,

then  $k = -(2, -1, -2)$



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**82.** If  $l, m, n$  be d.c.s, of a line ,then the line is perpendicular to the plane  $x - 3y + 2z + 1 = 0$  if \_\_\_\_\_.

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**83.** Find the equation of lines joining the points.  $(4, -6, 1)$  and  $(0, 3, -1)$

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**84.** Find the equation of lines joining the points.  $(a,a,a)$   
and  $(a,0,a)$



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**85.** Find the equation of lines joining the points.  $(2,1,3)$   
and  $(4,-2,5)$ .



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**86.** Write the symmetric form of equation of the  
following lines : x-axis



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87. Write the symmetric form of equation of the following lines :  $y = b, z = c$

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88. Write the symmetric form of equation of the following lines :  $ax + by + d = 0, 5z = 0$

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89. Write the symmetric form of equation of the following lines :  $x - 2y = 3, 2x + y - 5z = 0,$



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90. Write the symmetric form of equation of the following lines :

$$4x + 4y - 5z - 12 = 0 = 8x + 12y - 13z - 32,$$



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91. Write the symmetric form of equation of the following lines :  $3x - 2y + z = 1$ ,  $5x - 4y - 6z = 2$ .



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**92.** Obtain the equation of the line through the point

$(1, 2, 3)$  and parallel to the line

$$x - y + 2z - 5 = 0, 3x + y + z = -6$$



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**93.** Find the equation of the line through the point

$(3, -1, 2)$  and parallel to the planes

$$x + y + 2z - 4 = 0 \text{ and } 2x - 3y + z + 3 = 0$$



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**94.** Obtain the equation of the line through the point

$(1, 2, -3)$  and perpendicular to each of the lines

$$x + 4y - 3z = 0 = 2x - 5y + 7 \quad \text{and}$$

$$y + 3z - 2 = 0 = x + 2z + 5$$



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**95.** Show that the line passing through the points

$(a_1, b_1, c_1)$  and  $(a_2, b_2, c_2)$  passes through the origin ,

if  $a_1a_2 + b_1b_2 + c_1c_2 = p_1p_2$ . where  $p_1$  and  $p_2$  are

distances of the points from origin.



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**96.** Prove that the lines  $x = az + b, y = cz + d$  and  $x = a_1z + b_1, y = c_1z + d_1$  are perpendicular if  $aa_1 + cc_1 + 1 = 0$ .



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**97.** Find the points of intersection of the line  $\frac{x - 1}{1} = \frac{y + 2}{3} = \frac{z - 1}{-1}$  and the plane  $2x + y + z = 9$ .



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**98.** Find the co-ordinates of the point where the line joining  $(3, 4, -5)$  and  $(2, -3, 1)$  meets the plane  $2x + y + z - 7 = 0$ .

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**99.** Find the distance of the point  $(-1, -5, -10)$  from the point of intersection of the line  $\frac{x-2}{2} = \frac{y+1}{4} = \frac{z-2}{12}$  and the plane  $x - y + z = 5$ .

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**100.** Find the image of the point  $(2, -1, 3)$  in the plane  $3x - 2y + z - 9 = 0$



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**101.** Prove that the lines  $\frac{x + 4}{3} = \frac{y + 6}{5} = \frac{z - 1}{-2}$  and  $3x - 2y + z + 5 = 0 = 2x + 3y + 4z - 4$  are coplanar.



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**102.** Show that the line joining the points  $(0, 2, -4)$  and  $(-1, 1, -2)$  and the lines joining the points

$(-2, 3, 3)$  and  $(-3, -2, 1)$  are co-planar. Find their point of intersection.

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103. Prove that the line  $\frac{x-1}{2} = \frac{y+2}{-3} = \frac{z-3}{1}$  lies on the plane  $7x + 5y + z = 0$

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104. Find the angle between the plane  $x + y + 4 = 0$  and the line  $\frac{x+3}{2} = \frac{y-1}{1} = \frac{z+4}{-2}$ .

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**105.** Find the angle between the plane

$$4x + 3y + 5z - 1 = 0$$

and

line

$$\frac{x + 3}{2} = \frac{y - 1}{3} = \frac{z + 4}{6}$$



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**106.** Find the equation of the plane passing through

the intersection of the planes  $2x + y + 3z - 7 = 0$

and  $2x + 5y + 3z - 9 = 0$  and the point  $(2,1,3)$ .



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**107.** A line with direction ratios  $\langle 2, 1, 2 \rangle$  meets each of the lines  $x = y + a = z$  and  $x + a = 2y = 2z$ . Find the co-ordinates of the points of intersection.



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**108.** Obtain the co-ordinates of the foot of the perpendicular drawn from the point  $(3, -1, 11)$  to the plane  $ex/2 = (y-2)/3 = (z-3)/4$ . Obtain the equation of the perpendicular also.



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**109.** Find the perpendicular distance of the point

$(-1, 3, 9)$  from the line

$$\frac{x - 13}{5} = \frac{y + 8}{-8} = \frac{z - 31}{1}$$



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**110.** Find the distance of the point  $(1, -2, 3)$  from

the plane  $x - y + z = 5$ , measured parallel to the

line  $\frac{x}{2} = \frac{y}{3} = \frac{z}{-6}$



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**111.** Find the distance of the point  $(1, -1, -10)$

from the line  $\frac{x - 4}{1} = \frac{y + 3}{-4} = \frac{z + 1}{7}$  measured

parallel to the line  $\frac{x + 2}{2} = \frac{y - 3}{-3} = \frac{z - 4}{8}$



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**112.** Find the equation of plane through the point

$(2, 0, -3)$  and containing the line

$$3x + y + z - 5 = 0 = x - 2y + 4z + 4$$



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**113.** Find the equation of the straight line perpendicular to the line  $\frac{x - 2}{3} = \frac{y + 1}{4} = \frac{z - 6}{7}$  and lying in the plane  $x - 2y + 4z - 51 = 0$ .



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**114.** Find the shortest distance between the lines  $\frac{x - 3}{3} = \frac{y - 8}{-1} = \frac{z - 3}{1}$  and  $\frac{x + 3}{-3} = \frac{y - 7}{2} = \frac{z - 6}{4}$ . Find also the equation of the line of shortest distance.



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**115.** Show that the shortest distance between the lines  $x = y + 2a = 6z - 6a$  and  $x + a = 2y = -12z$  is  $2a$ .

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**116.** Find the equation in vector and Cartesian form of the plane passing through the point  $(3, -3, 1)$  and normal to the line joining the points  $(3, 4, -1)$  and  $(2, -1, 5)$

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**117.** Find the vector equation of the plane whose Cartesian form of equation is  $3x - 4y + 2z = 5$

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**118.** Show that the normals to the planes  $\vec{r} \cdot (\hat{i} - \hat{j} + \hat{k}) = 3$  and  $\vec{r} \cdot (3\hat{i} + 2\hat{j} - \hat{k}) = 0$  are perpendicular to each other.

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**119.** Find the angle between the planes  $\vec{r} \cdot (2\hat{i} - \hat{j} + 2\hat{k}) = 6$  and  $\vec{r} \cdot (3\hat{i} + 6\hat{j} - 2\hat{k}) = 9$

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120. Find the angle between the line

$$\vec{r} = (\hat{i} + 2\hat{j} - \hat{k}) + \lambda(\hat{i} - \hat{j} + \hat{k}) \text{ and the plane}$$

$$\vec{r} \cdot (2\hat{i} - \hat{j} + \hat{k}) = 4$$

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121. Prove that the acute angle between the lines whose direction cosines are given by the relation

$$l + m + n = 0 \text{ and } l^2 + m^2 - n^2 = 0 \text{ and } \frac{\pi}{3}$$

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**122.** Prove that the three lines drawn from origin with direction cosines

$(l_1, m_1, n_1), (l_2, m_2, n_2), (l_3, m_3, n_3)$  are coplanar if

$$\begin{bmatrix} l_1 & m_1 & n_1 \\ l_2 & m_2 & n_2 \\ l_3 & m_3 & n_3 \end{bmatrix} = 0.$$



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**123.** Prove that three lines drawn from origin with direction cosines proportional to

$(1, -1, 1), (2, -3, 0), (1, 0, 3)$  lie on one plane .



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**124.** Determine  $k$  so that the lines joining the points  $P_1(k, 1 - k, 1)$  and  $P_2(2k, 0, 2)$  shall be perpendicular to the line from  $P_2$  to  $P_3(2 + 2k, k, 1)$ .

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**125.** Find the angle between the lines whose direction ratios are proportional to  $a, b, c$  and  $b-c, c-a, a-b$ .

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**126.**  $O$  is the origin and  $A$  is the point  $(a, b, c)$ . Find the equation of the plane through  $A$  at right angles to

$\vec{OA}$ .



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**127.** Find the equation of the plane through  $(6,3,1)$  and  $(8, -5, 3)$  parallel to x-axis.



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**128.** Is the function  $[x]$  differentiable at  $x=2$ ?



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**129.** Is the function  $[x]$  differentiable at  $x=2.5$ ?



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**130.** Is the function  $[x]$  differentiable at  $x=0$ ?



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**131.** Is the function  $[x]$  differentiable at  $x=2$ ?



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**132.** If  $f(x) = |x|$ , what is the value of  $f(0^-)$ ?





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**133.** If the first derivative of a function vanishes at all points and if  $f(0) = 1$ , then what is  $f(x)$ ?



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**134.** Give example of a function which is continuous but not differentiable at  $x=1$ .



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**135.** Give example of a function whose is continuous but not differentiable at  $x=2$ .



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**136.** If  $f(x+y) = f(x) f(y)$  for all  $x,y$  and if  $f(5) = 2$  and  $f(0) = 3$ , then what is the value of  $f'(5)$ ?



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**137.** A differentiable function  $f$  defined for all  $x > 0$  and satisfies  $f(x^2) = x^3$  for all  $x > 0$ . What is the value  $f'(16)$  ?

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138. If  $f(x) = [\tan^2 x]$ , what is  $f'(0)$ ?

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139. If  $f(x) = (3x + 2)^{100}$  and  $f'(x) = n(3x + 2)^{99}$  then what is the value of  $n$ ?

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140. If  $x \in \left(\frac{3\pi}{4}, \pi\right)$  what is  $\frac{dy}{dx}$  for  $y = |\cos x| + |\sin x|$ ?



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**141.** What is the derivative of  $f(\ln x)$  with respect to  $x$  where  $f(x) = \ln x$  ?



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**142.** If  $f'(x) = \sqrt{2x^2 - 1}$  and  $y = f(x^2)$  then what is  $\frac{dy}{dx}$  at  $x = 1$  ?



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**143.** Defferentiate

$$\tan^{-1} \frac{2x}{1-x^2} \text{ w. r. t. } \sin^{-1} \frac{2x}{1+x^2}$$



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**144.** What is the differential co-efficient of

$$\tan^{-1} \frac{\sqrt{1+x^2}-1}{x} \text{ with respect to } \tan^{-1} x$$



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**145.** If  $y = at^2$ ,  $x = 2at$  where  $a$  is a constant what is the

$$\text{value of } \frac{d^2y}{dx^2} \text{ at } x = \frac{1}{2}?$$



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**146.** Is the function  $f(x) = \sin^{-1} \frac{2x}{1+x^2}$  differentiable at

$$x = \pm 1?$$



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**147.** Write the value of  $\frac{d}{dx} (\sin^{-1} x + \cos^{-1} x)$  for

$$x \in (-1, 1).$$



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**148.** Write the value of  $\frac{d}{dx} \sec^{-1} \left( \frac{1}{2x^2 - 1} \right)$ , for  $x \in \left( 0, \frac{1}{\sqrt{2}} \right)$ .

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**149.** Write the interval in which the function  $f(x) = \sin^{-1}(1 - x)$  is differentiable.

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**150.** Write the value  $x$  for which  $\frac{d}{dx} \sin(\sin^{-1} x) = 1$

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151. Write the value  $x$  for which  $\frac{d}{dx}\sin^{-1}(\sin x) = 1$

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152. Write the derivative of  $\sec^{-1} x$  with respect to  $x$   
at  $x = -\frac{1}{3}$ .

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153. Find the derivative of  $\ln_x a$ .

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154. Write a logarithmic functions which is differentiable at every point in  $\mathbb{R}$ .

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155. Give example of two functions which are not derivable at  $x = 0$ , but their sum is derivable at  $x=0$

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156. Write the value of  $x$  for which

$$\frac{d}{dx} \tan^{-1} \left( \frac{2x}{1-x^2} \right) = \frac{2}{1+x^2}$$

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157. If  $y = 5^t$  and  $t = e^{3x}$ . Write the value of  $\frac{dy}{dx}$  at  $x=$

0



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158. Write the derivative of  $\sin^{-1} x$  with respect to  $\cos^{-1} x$ .



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159. Write the value of  $\frac{dy}{dx}$  if

$$y = \sin x + \sqrt{\sin x + \sqrt{\sin x + \sqrt{\sin x + \dots \infty}}}$$

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160. Write the value of  $\frac{dy}{dx}$  if  $y = x^{x^{\dots \infty}}$

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161. Write the value of  $\frac{dy}{dx}$  at  $(1,0)$  where  $x^2y + y^2 + x = 0$ .

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162. Write the minimum value of  $y_2$  where  $y = \sin^2 x \cos^2 x$

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163. If  $x = \log t$ ,  $y = t^2 - 1$ , then what is  $y_2$  at  $t=1$ ?

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164. What is the slope of the tangent to the curve  
 $y = 3x^2 + 2x - 1$  at  $x=2$ ?

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165. If  $y = \frac{1}{x(x+1)}$  then what is  $y_3$ ?

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166. If  $f(x) = e^{ax} \sin ax$  and  $f''(0) = 2$ , then what is  $a$  ?



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167. A balloon is pumped at the rate of 10 cubic cm/min . What is the rate of increase of its radius when its radius is 15 cm ?



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168. For what values of  $a$  the function  $e^{ax}$  is increasing ?



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**169.** What is the interval in which  $\log_5 x$  is increasing ?



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**170.** What is the interval in which

$f(x) = x^3 - 3x^2 + 3x - 10$  is strictly increasing ?



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**171.** Give example of a function which is increasing in

$(-\infty, 2)$  and  $(3, \infty)$  and decreases in  $(2, 3)$ .



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**172.** Write the least value of  $a$  for which the function  $f$  defined by  $f(x) = x^2 + ax + 1$  increases.



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**173.** For what value of  $K$ ,  $Kf$  is increasing if  $f$  is increasing ?



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174. At what point of  $x^2 = 2y$  the point (0,3) is nearest to the curve?

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175. If  $\theta + \phi = \frac{\pi}{3}$ , then for what value of a  $\sin \theta$ .  $\sin \phi$  is maximum ?

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176. Write the absolute maximum and absolute minimum of the function  $f(x) = \frac{x}{|x|}$  in  $[-2, 2]$ .

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177. Which condition of Rolle's theorem is violated by the function  $f(x) = \sin x$  in  $\left[0, \frac{3\pi}{4}\right]$

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178. Which condition of Rolle's theorem is violated by the function  $f(x) = |x|$  in  $[-1,1]$

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179. Is there any tangent to the curve  $y = |2x - 1|$  at  $\left(\frac{1}{2}, 0\right)$ ?



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180. Write the subinterval of  $(0, \pi)$  in which  $\sin\left(x + \frac{\pi}{4}\right)$  is increasing.



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181. Given  $f(2) = 6$ ,  $f'(1) = 4$  find

$$\lim_{h \rightarrow 0} \frac{f(2 + 2h + h^2) - f(2)}{f(1 + h - h^2) - f(1)}$$



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182. If  $(f(x))^n = f(nx)$ , find  $\frac{f'(nx)}{f'(x)}$ .



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183. Evaluate  $\frac{d}{dx} (a^{\sin x} + e^{-x})$  by chain rule.



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184. If  $f(x) = \sin |x| - |x|$ , find  $f'(0^+)$



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185. Find the derivative of  $\ln \sqrt{\frac{1 - \cos x}{1 + \cos x}}$ .

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186. If  $y = \cos^{-1}\left(\frac{a + b \cos x}{a + b \cos x}\right)$  find  $\frac{dy}{dx}$ .

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187. If  $y = \tan^{-1}(\cot x) + \cot^{-1}(\tan x)$ , find  $\frac{dy}{dx}$ .

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188. If  $y = \tan^{-1} \left( \frac{3x - x^3}{1 - x^2} \right)$ , find  $\frac{dy}{dx}$ .

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189. If  $x = a \left( \frac{1 + t^2}{1 - t^2} \right)$ ,  $y = \frac{2t}{1 - t^2}$  find  $\frac{dy}{dx}$  at  $t = \frac{1}{\sqrt{3}}$ .

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190. If  $x = a \cos^{30} \theta$ ,  $y = b \sin^{30} \theta$ , find  $\frac{dy}{dx}$ .

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191. If  $y = e^{x^{e^x}}$ , find  $\frac{dy}{dx}$ .



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192. If  $x^y + y^x = 1$ , find  $\frac{dy}{dx}$ .



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193. If  $e^x + e^y = e^{x+y}$ , find  $\frac{dy}{dx}$ .



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194. If  $x^y y^x = 1$ , find  $\frac{dy}{dx}$ .

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195. Find the derivative of  $\tan^{-1}\left(\frac{\sqrt{1-x^2}}{x}\right)$  with respect to  $\cos^{-1}x$ .

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196. Find  $\frac{d^2y}{dx^2}$  if  $x=a \cos \theta$ ,  $y = b \sin \theta$ .

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197. If  $y = e^{ax} \sin bx$  show that  $y_2 - 2ay_1 + (a^2 + b^2)y = 0$ .



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198. If  $x^7 y^3 = (x + y)^{10}$ , then find  $\frac{d^2 y}{dx^2}$



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199. If  $u = f\left(\frac{x^2 + y^2}{x} y\right)$  prove that

$$x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = 0.$$


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200. If  $f(x+y)=f(x).f(y)$  for all  $x,y$  and  $f(5)=2$  and  $f'(0)=3$ , then show that  $f'(5)=6$ .





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201. If  $(f \circ g)(1) = 3$ ,  $g(1) = 2$ ,  $g'(1) = 1$ , then show that  $f'(2) = 3$ .



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202. If  $f(a) = 2$ ,  $f'(a) = 1$ ,  $g(a) = -1$  and  $g'(a) = 2$ , then find

$$\lim_{x \rightarrow a} \frac{g(x)f(a) - g(a)f(x)}{x - a}.$$



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203. Find the rate of change of the area of circle w.r.t.  $r$  when  $r = 8$  cm.



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**204.** The side of a square is increasing at the rate of  $0.1$   $cm/sec$  and at the same time the area is increasing at the rate of  $30$   $sq. cm/sec$ . Find the length of side of the square.



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**205.** A particle moves along a straight line according to the law  $s = t^3 - 3t^2 + 5t$ . Find its velocity and acceleration at the end of  $1$  sec.



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**206.** Show that the function  $f(x) = \frac{1}{x}$  is decreasing in  $(0, \infty)$ .

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**207.** Find the intervals where the function  $f(x) = x^3 - 12x + 10$  is increasing.

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**208.** Find the slope of the normal to the curve  $y = xe^{-x}$  at  $x=2$ .

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**209.** Find the angle between the tangents to the curve

$$y = x^2 - 5x + 6 \text{ at the points } (2,0) \text{ and } (3,0).$$

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**210.** Find the point on the curve

$$y^2 - x^2 + 2x - 1 = 0$$

where the tangent is parallel to the x - axis.

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**211.** Find the points on the curve  $9y^2 = x^2$ , where normal to the curve makes equal intercepts with axes.

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**212.** If  $y = x^4 - 12$  and if  $x$  changes from 2 to 1.99, find the approximate error in  $y$ .

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**213.** Using differential find the value of  $\sqrt{16.2}$ .

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**214.** Show that  $f(x) = x^3 - 6x^2 + 24x + 4$  has neither a maximum nor a minimum value.

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**215.** Find the points where  $f(x) = 8x^2 - x^4 - 4$  has local maximum or minimum.

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**216.** Find the absolute maximum and absolute minimum value of the function  $f(x) = 2x^3$  in  $[-2,2]$ .

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217. Find the absolute maximum and absolute minimum value of  $f(x) = x - x^3$  in  $[0,1]$ .

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218. Using mean value theorem, prove that  $\sin x < x$ ,  $x \in (0, \pi/2)$ .

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219. Write antiderivative of  $\tan^2 x$

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220. Write the value of  $\int x a^{x^2+1} dx$

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221. Write the value of  $\int \sqrt{1 - \cos 2x} dx$

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222. If  $f'(x) = e^x + \frac{1}{1+x^2}$ , what is  $f(x)$  ?

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223. Write the value of  $\int e^{\log \cot^2 x} dx$



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224. Write the value of  $\int \frac{e^x - 1}{1 - e^{-x}} dx$



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225. Write the value of  $\int \frac{e^x - 1}{1 - e^{-x}} dx$



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226. Write the value of  $\int x^{20} \sec^2 x dx - \int x^{20} \tan^2 x dx$



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227. Write the value of  $\int \frac{\sec^2 x}{\cos ec^2 x} dx$ .



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228. Write the value of  $\int \frac{1}{\sqrt{x} e^{\sqrt{x}}} dx$



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229. Write the primitive of  $\sin^3 x$

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230. Write the primitive of  $\sin^3 x$

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231. Write the value of  $\int e^x e^{e^x} e^{e^{e^x}} dx$ .

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232. Write the value of  $\int \frac{d(x^2 + 1)}{x^2 + 5}$ .



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233. Write the value of  $\int \frac{d(x^2 + 1)}{1 + x^4} dx$

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234. Write the value of  $\int x \sec^2 x dx$ .

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235. Write the value of  $\int e^{-x} (1 - \tan x) \sec x dx$ .

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236. Write the value of  $\int \cos^{-1} \left( \frac{1 - x^2}{1 + x^2} \right) dx$ .

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237. Write the value of  $\int e^x (In \sin x + \cot x) dx$ .

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238.  $\int \sin^{-1} \sqrt{\frac{x}{a+x}} dx = \text{-----}$ .

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239.  $\int \tan^{-1} \left( \frac{x-5}{1+5x} \right) dx = \text{-----}$ .

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240.  $\int \tan^{-1} \sqrt{x} dx = \text{-----}$ .

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241.  $\int e^{\cos 2x} \sin 2x dx = \text{-----}$ .

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242.  $\int \frac{dx}{e^x + e^{-x}} = \text{-----}$ .



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243. Write the value of  $\int \frac{1}{x(\ln x)} dx$



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244. Write the value of  $\int \frac{x(5x^3 + 4x^2 + 3x)}{x^5 + x^4 + x^3 + 1} dx.$



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245. Write the value of  $\int \frac{dx}{x^{1/5}(1 + x^{4/5})^{1/2}}.$



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246. Write the value of  $\int \frac{\{f(x)\phi(x) + f(x)\phi(x)\} \{\log\phi(x) + \log f(x)\}}{f(x)\phi(x)} dx$ .

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247. Write the value of A if

$$\int \frac{dx}{(x+1)(x+2)} = A \log|x+1| - \log|x+2| + C$$

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248. Write the value of  $\int \frac{\cos x - \sin x}{\sin x + \cos x} dx$ .

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249. Write the value of  $\int \frac{1}{1 + \sin^2 x} dx$ .

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250.  $\int_{-\pi/2}^{\pi/2} (\sin|x| - \cos|x|) dx = \underline{\hspace{2cm}}$ .

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251.  $\int_{-\pi/6}^{x/3} \frac{dx}{1 + \sqrt{\tan x}} dx = \underline{\hspace{2cm}}$

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$$252. \int_0^{x/2} \frac{\sin x - \cos x}{1 + \sin x \cdot \cos x} dx = \text{-----}$$



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$$253. \int_{-1}^1 e^{|x|} dx = \text{-----}$$



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$$254. \int_0^2 |2x - 1| dx = \text{-----}$$



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$$255. \int_{-1}^1 \log \frac{4-x}{4+x} dx = \underline{\hspace{2cm}}$$

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256. If  $f(0) = 1$ ,  $f(2) = 3$ ,  $f'(2) = 5$ , then the value

$$\text{of } \int_0^1 x f''(2x) dx = \underline{\hspace{2cm}}.$$

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$$257. \int_0^{\pi/2} \log \tan x dx \underline{\hspace{2cm}}.$$



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258. If  $F(x) = \int_0^x e^{2t} \cos 5t dt$ , what is  $F'(x)$ ?

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259. write the value of  $\frac{d}{dx} \int_0^{x^2} \sin t dt$

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260. Write the value of

$$\lim_{x \rightarrow 0} \left[ \frac{d}{dx} \left( \int_0^x \sqrt{1+t^2} dt \right) \right].$$



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261. Write the value of  $\int_{-1}^1 (\sin^5 x + x) dx$ .



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262. Write the value of  $\frac{d}{dx} \int_0^{\pi/2} \frac{\sqrt{\sin x}}{\sqrt{\sin x} + \sqrt{\cos x}} dx$



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263. If  $f(3 - x) = f(x)$ , then  $\int_1^2 x f(x) dx = \underline{\hspace{2cm}}$ .



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$$264. \lim_{x \rightarrow 0} \frac{\int_0^x \sec^2 t dt}{x \sin x} =$$



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$$265. \int_0^1 x(1-x)^n dx$$



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$$266. \int_0^{\frac{3}{2}} [2x] dx$$



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267.  $\int_0^{\pi} \cos^2 x dx = \underline{\hspace{2cm}}$

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268. Area under the curve  $x + y = 1$  in the first quadrant is  $\underline{\hspace{2cm}}$

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269. The value of  $\int_1^2 [f\{g(x)\}]^{-1} f'\{g(x)\}g'(x) dx$  for  $g(1) = g(2)$  is  $\underline{\hspace{2cm}}$



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270. If  $f(x)$  is a quadratic polynomial such that

$$f(0) = 2, f'(0) = -3 \quad \text{and} \quad f''(0)=4, \quad \text{then}$$

$$\int_{-1}^1 f(x) dx = \underline{\hspace{2cm}},$$



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271. The value of  $\int_0^{\pi/2} [\cos x] dx = \underline{\hspace{2cm}},$



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272. If  $\int_0^a f(x)dx = \lambda$  and  $\int_0^a f(2a - x)dx = \mu$  then

$$\int_0^{2a} f(x)dx = \text{-----}$$

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273. Evaluate  $\int \{2x + 1\} (x^2 + x + 1)^{10} dx$

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274. Evaluate  $\int \left\{ \frac{e^{2 \log x} + e^{3 \log x}}{x + x^2} \right\} dx$ .

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275.

Evaluate

$$\int \left[ \cos^{-1} \left( \frac{1 - \tan^2 x}{1 + \tan^2 x} \right) + \sin^{-1} \left( \frac{2 \tan x}{1 + \tan^2 x} \right) \right] dx.$$



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276. Evaluate  $\int \frac{1 - \cos 2x}{1 + \cos 2x} dx.$



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277. Evaluate  $\int \frac{1}{\sin^2 x \cos^2 x} dx.$



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278. If  $f'(x) = e^x + \frac{1}{1+x^2}$  and  $f(0) = 1$ , then find  $f(x)$ .

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279. Evaluate  $\int 2^{\cos 2x} \sin 2x dx$ .

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280. Evaluate  $\int \frac{\sin x}{\cos(x-a)} dx$ .

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281. Evaluate  $\int \left( 1 + \frac{1}{\tan x} \right) dx$

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282. Evaluate  $\int \frac{\cos 4x + \cos 2x}{\sin 4x + \sin 2x} dx.$

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283. Evaluate  $\int \tan x \sec^4 x dx.$

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284. Evaluate  $\int \frac{x^9}{x^{20} + 4} dx$

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285. Evaluate  $\int \frac{3x + 4}{x^2 + 4} dx.$

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286. Evaluate  $\int \frac{\cos 3x \cdot \cos x}{1 + \cos 2x} dx.$

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287. Integrate  $\int \frac{x^5}{x^2 + 1} dx$

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288.  $\int \frac{2x + 5}{(x + 2)^{\frac{7}{2}}} dx$

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289. Integrate  $\int \tan^{-1} x dx$ .

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290.  $\int \sec \theta \tan \theta \sqrt{\tan^2 \theta - 3} d\theta$

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291. Evaluate  $\int \frac{1}{x + x^{1/3}} dx.$

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292. Evaluate  $\int (6x + 1) \sqrt{3x + 4} dx.$

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293. If  $\int \frac{x}{(x-1)(2x-1)} = \int \left[ \frac{A}{x-1} + \frac{B}{2x-1} \right] dx$

find A and B.

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294. Evaluate  $\int \frac{1}{2 \sin x + 3 \cos x} dx$ .

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295. Evaluate  $\int \cos^4 x dx$ .

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296. Evaluate  $\int \frac{\cos 2x}{\sin 7x \cos 5x} dx$ .



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297. Evaluate  $\int \frac{\sec^2 \theta}{\cos 2\theta + 2 \sin^2 \theta} d\theta$



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298. Evaluate  $\int e^x \left( \frac{1 + \sin x}{1 + \cos x} \right) dx$ .



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299. Evaluate  $\int e^{\tan^{-1} x} x \left( \frac{1 + x + x^2}{1 + x^2} \right) dx.$

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300. Evaluate  $\int \frac{\sin^{-1} x}{(1 - x^2)^{3/2}} dx.$

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301.  $\int \sin^{-1} \sqrt{\frac{x}{a+x}} dx = \text{-----}.$

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302. Evaluate  $\int \frac{\sqrt{\tan x}}{\sin x \cos x}$ .

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303. Evaluate  $\int_0^1 \frac{x^2}{x^2 + 1} dx$ .

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304. Evaluate  $\lim_{x \rightarrow 0} \frac{\int_0^{x^2} \sin \sqrt{t} dt}{x^3}$ .

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305. Evaluate  $\int_0^{\pi/2} x \sin x dx$ .

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306. Evaluate  $\int_{-1}^3 \{|x| + [x]\} dx$ .

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307. Evaluate  $\int_{-3}^3 |x + 1| dx$ .

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308.  $\int_0^{10} \sin(x - [x])\pi dx$

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309. If  $f(x) = \int_1^{x^2} \tan^{-1} \sqrt{t} dt$ ,  $t > 0$ , find  $f'(1)$ .

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310.  $f(x) = \frac{1}{x^2} \int_2^x [t^2 + f(t)] dt$ , find  $f(2)$

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311. If  $f(x) = \cos x - \int_0^x (x-1)f(t)dt$ , then find  $f''(x) + f(x)$ .

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312. Evaluate  $I = \int_0^4 [\sqrt{x}] dx$ .

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313. Evaluate  $\int_0^{\pi/2} \frac{\cos x dx}{(2 - \sin x)(3 + \sin x)}$ .

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314. Evaluate  $\int_0^5 \sqrt{25 - x^2} dx$

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315. Evaluate  $\int_3^6 \frac{\sqrt{x}}{\sqrt{9-x} + \sqrt{x}} dx.$

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316. Evaluate  $\int_3^{\pi/2} \ln \cot x dx.$

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**317.** Find the area bounded by the curve  $x = y^2$  and the straight lines  $x = 0, y = 1$ .

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**318.** Find the area bounded by the curve  $y = \sin x$  between  $x = 0$  and  $x = 2\pi$ .

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**319.** Find the area of the parabola  $y^2 = 36x$  bounded by its latus rectum.

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**320.** Find the area of the region bounded by  $y = 6x - x^2$  x-axis and between ordinates  $x = 0$  and  $x = 6$ .

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**321.** Find the area of the trapezium bounded by the sides  $y = x, x = 0, y = 3, y = 4$ .

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**322.** Write the order and degree of the differential

equations given by: 
$$\frac{d^2y}{dx^2} + 3\left(\frac{dy}{dx}\right)^4 + y = 0$$

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**323.** Write the order and degree of the differential

equations given by: 
$$\left\{ y + \left(\frac{dy}{dx}\right)^3 \right\}^{1/2} = 1 + x$$

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**324.** Write the order and degree of the differential

equation given by: 
$$\frac{d^2y}{dx^2} = \left[ 1 + \left(\frac{dy}{dx}\right)^2 \right]^{\frac{4}{3}}$$



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**325.** Write the order and degree of the differential

equation given by: 
$$\left(\frac{d^2y}{dx^2}\right)^{\frac{3}{2}} = 1 + \left(\frac{dy}{dx}\right)^5$$



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**326.** The degree of the differential equation satisfying

$$\sqrt{1-x^2} + \sqrt{1+y^2} = a(x-y) \text{ is } \underline{\hspace{2cm}}.$$



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327. Write the differential equation corresponding to

$$v = \frac{a}{r} + b \text{ is } \underline{\hspace{2cm}}.$$



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328. The differential equation of

$$y = a \cos 2x + b \sin 2x \text{ is } \underline{\hspace{2cm}}.$$



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329. The differential equation of the family of straight

lines parallel to x-axis is \_\_\_\_.



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**330.** The differential equation of the family of straight lines passing through origin is\_\_\_\_\_.



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**331.** The differential equation of the family of parabolas with axis along x-axis is\_\_\_\_\_.



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**332.** Write the differential equation whose general solution is  $y = ce^{2x}$



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**333.** Write the differential equation of parabolas

$$y^2 = 8x + c$$



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**334.** Write the differential equation whose general

solution is  $y = a \cos 3x + b \sin 3x$



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**335.** Write the general solution of the differential

equations :  $\frac{dy}{dx} = \cos x - x$



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**336.** Write the general solution of the differential

equations :  $\frac{dy}{dx} = \frac{2}{s^2}$



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**337.** Write the general solution of the differential

equations :  $\frac{dy}{dx} = \cot^2 y$



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**338.** Write the general solution of the differential

equations :  $\frac{dy}{dx} = 4x^3 + 2x + \sec^2 x$

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**339.** Write the general solution of the differential

equations :  $\frac{dy}{dx} = \frac{1 + y^2}{1 + x^2}$

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**340.** Write the general solution of the differential

equations :  $\frac{d^2y}{dx^2} = 0$





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**341.** Write the general solution of the differential

equations :  $\frac{d^2y}{dx^2} = x$



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**342.** Write the solution  $\frac{d^2y}{dx^2} = 0$ ,  $y(0)$  and  $y'(0) = 1$ .



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**343.** Write the solution of  $\frac{d^2y}{dx^2} = 2x$ ,  $y = 2$  when  $x =$

1.



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344. Write the general solution of  $\frac{ydx - xdy}{y} = 0$ .



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345. Write solution  $\sqrt[3]{4 + \frac{dy}{dx}} = 2$ .



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346. Write solution  $\frac{dy}{dx} = \frac{1}{1 + x^2}$ ,  $x = 0$ ,  $y = 1$



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347. Write solution of  $\frac{dy}{dx} = 2y, y(0) = 2$



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348. Write solution of  $\frac{dy}{dx} = \frac{2}{y}, y(0) = 0$



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349. Write the solution of  $ydx - xdy = x^2ydx$ .



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350. Write integrating factor of

$$(1 + y^2)dx + xdy = \tan^{-1} ydy$$

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351. Find the solution of  $\frac{dy}{dx} = e^x \sin x$

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352. Find the solution of  $\frac{dy}{dx} = \frac{y}{x}$ .

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353. Find integrating factor of  $(x + \tan y) dy = \tan y dx$



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354. Find integrating factor of

$$(x - \ln y) \frac{dy}{dx} = -y \ln y.$$



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355. Solve  $e^{-2x} \frac{dy}{dx} = x.$



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356. Solve  $\frac{dy}{dx} = x + y$

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357. Solve  $\frac{dy}{dx} = \frac{x + y + 1}{x + y + 2}$ .

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358. Find the equation of the curve whose slope is given by  $\frac{dy}{dx} = \frac{2y}{x}$  and which passes through (1,1).

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359. If  $y + \frac{dy}{dx} = 0$  and  $y(0) = 2$ , find  $y$ .



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360. Find differential equation of the curve

$$y = ae^{3x} + be^{5x}.$$



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361. Write the projection of the point  $(1,2,3)$  on  $xy$ -plane.



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**362.** Write the projection of the point  $(2,3,1)$  on  $y$ -axis is.



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**363.** Write the image on the point  $(2,1,3)$  with respect to  $yz$ -plane.



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**364.** Write the distance of the point  $(3,1,5)$  from  $y$ -axis.



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**365.** A line is perpendicular to  $xy$ -plane Write the angle made by the line with  $z$ -axis.

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**366.** If the distance between the points  $(1,2,z)$  and  $(-1, 2, 1)$  is 3, then find  $z$ .

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**367.** If the direction angles of a line are  $\alpha = 30^\circ$  and  $\beta = 60^\circ$ , find the other direction angle  $\gamma$

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**368.** Write the direction cosine of the line whose direction ratios are  $\{1,2,3\}$ .

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**369.** Write the direction cosines of the line joining  $(1,2,3)$  and  $(1,1,2)$ .

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**370.** Write the distance of the point  $(1,1,2)$  from x-axis.

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**371.** Write the distance of the point  $(2,3,6)$  from  $zx$ -plane.



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**372.** Write the locus of a point  $p$  which moves in space such that its distance from origin is 4 units.



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**373.** Write the centroid of the triangle with vertices  $(1,2,3)$ ,  $(2,1,2)$ ,  $(3,0,1)$ .



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**374.** Write the ratio in which the line joining the points  $(2,3,4)$  and  $(-3, 5, -4)$  is divided by  $yz$ -plane.



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**375.** Write the value of  $y$  so that the points  $(1,y,2)$ ,  $(3,2,-1)$  and  $(-4, 6, 3)$  are collinear.



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**376.** Write the projection of the line segment joining the points  $(2,1,3)$  and  $(3,2,4)$  on z-axis.

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**377.** Write the projection of the line segment joining  $(2,4,3)$  and  $(3,2,4)$  on yz-plane.

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**378.** If d.c.s. of a line be  $\left(\frac{1}{2}, \frac{3}{4}, \frac{k}{4}\right)$  what is the value of k ?

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**379.** If  $\alpha, \beta, \gamma$  be direction angles of a line, what is the value of  $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma$ .

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**380.** Write the direction cosines of the normal to the plane  $x - y + 1 = 0$ .

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**381.** Write the equation of the plane passing through the point  $(1,2,3)$ , the direction ratios of the normal to

the plane being  $\langle 3, 5, 7 \rangle$



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**382.** Write the value of x-intercept of the plane

$$x + y + 2z = 1.$$



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**383.** The equation  $ax + by + c = 0$  represents a plane

parallel to \_\_\_\_ axis.



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**384.** Write the equation of the plane parallel to x-axis having intercepts 5 and 6 on y and z-axis respectively.

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**385.** The plane having equation  $2x + 5z + 1 = 0$  is parallel to \_\_\_\_ plane.

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**386.** What is the distance from origin of the plane  $3x + 4y = 1$ .

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**387.** Write the equation of the plane passing through  $(1,2,3)$  and parallel to the plane  $x + 2y + 5z = 0$ .



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**388.** Write the distance between the plane  $x - 2y + z = 6$  and  $2x - 4y + 2z = 8$



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**389.** Write the equation of the plane through origin and passing through the intersection of the planes  $3x - 2y + z - 1 = 0$  and  $x - 2y + 3z - 1 = 0$

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**390.** Write the position of the points A (2, 4, - 3) and B (2,-6,2) with respect to the plane  $4x+7y+6=0$

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**391.** Write the equation of the plane  $3x - 4y + z + 5 = 0$  in normal form.

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**392.** Write the equation of the plane

$x + 3y - 7z + 2 = 0$  in the intercept form.



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**393.** Write the equation of the plane passing through

x-axis and y-axis.



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**394.** Write the equation of the plane perpendicular to

z-axis and passing through  $(1, -2, 4)$ .



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**395.** If the plane  $2x + 4y + z + 2 = 0$  and  $x - 2y + kz + 5 = 0$  are perpendicular to each other what is the value of  $k$ ?



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**396.** Write down the equation of x-axis.



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**397.** Write the vector equation of a line through the point  $(1,2,3)$  and parallel to the vector  $3\hat{i} + 2\hat{j} - 2\hat{k}$



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**398.** Write the equation of the line passing through the points  $(3, -2, -5)$  and  $(3, -2, 6)$ .



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**399.** Write the equation of the line

$$\frac{x - 5}{3} = \frac{y + 4}{7} = \frac{z - 6}{2} \text{ in vector form.}$$



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**400.** Write the equation of the line in symmetric form through the point  $(1, -2, 3)$  having direction ratios  $(3, -4, 5)$ .



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**401.** Write the equation of the line  $x = ay + b, z = cy + d$  in symmetric form.



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**402.** Write the equation of the plane passing through the point  $(2, 3, 1)$  and perpendicular to the line.

$$\frac{x - 1}{1} = \frac{y - 2}{-1} = \frac{z + 1}{3}$$



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**403.** What is the number of independent constants that occur in the general equation of a plane.



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**404.** The angle between the planes  $x + y + z + 1 = 0$  and  $2x + y + z + 2 = 0$  is\_\_\_\_\_.



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**405.** The angle between the plane  $3x + 3z - 5 = 0$

and the line  $\frac{x - 1}{1} = \frac{y - 2}{-1} = \frac{z - 3}{0}$  is.



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**406.** If the lines  $\frac{x - 1}{k} = \frac{y - 3}{2} = \frac{2 - z}{-5}$  and

$\frac{x - 1}{3} = \frac{2 - y}{-4} = \frac{z}{k}$  are perpendicular to each

other, then what is the value of  $k$ ?



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**407.** Find the equation of the plane passing through

the intersection of the planes



$$\vec{r} = (\hat{i} + \hat{j} + \hat{k}) = 1 \quad \text{and}$$

$$\vec{r} = (2\hat{i} + 3\hat{j} + \hat{k}) + 4 = 0 \text{ and parallel to x-axis.}$$

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**408.** Find the co-ordinates of the foot of the perpendicular drawn from the point (1,3,4) to the line joining the points (3, 0, - 1) and (0, 1, - 2).

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**409.** If the points (-1,-1,2), (2,m,5) and (3,11,6) are collinear, then find the value of m.

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**410.** Two vertices of a triangle are  $(1,2,3)$  and  $(3, -2, 7)$  and centroid is  $(2,1,-2)$ . Find the remaining vertex of the triangle.



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**411.** Show that the points  $(1,2,3)$ ,  $(2,3,1)$  and  $(3,1,2)$  form an equilateral triangle.



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**412.** Find the direction cosines of the line segment joining  $(1, -1, 2)$  and  $(2,1,1)$ .



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**413.** Find the projection of the line segment joining  $(1,2,3)$  and  $(2,3,4)$  on a straight line having d.r.s  $\langle 2, 1, 3 \rangle$ .



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**414.** If P,Q,R,S are points  $(1,2,5)$ ,  $(-2, 1, 3)$ ,  $(4,4,2)$  and  $(2, 1, -4)$  respectively, find the projection of PQ on

RS.



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**415.** If A,B,C are points  $(0,4,1)$ ,  $(2,3,-1)$ ,  $(4,5,0)$  find the angle that AB makes with BC.



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**416.** Find the acute angle between the lines whose d.r.s are  $(1, 1, 2)$  and  $(\sqrt{3} - 1, -\sqrt{3} - 1, 4)$  respectively.



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**417.** Find the equation of the plane passing through the points  $(2,1,3)$ ,  $(3,2,1)$  and  $(1, 0, -1)$ .



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**418.** Find the equation of the plane parallel to z-axis and with intercepts 3 and 4 on x and y axes respectively.



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**419.** Find the equation of the plane through the point  $(-1, 3, 0)$ , which is perpendicular to both the planes  $x + 2y + 2z - 5 = 0$  and  $3x + 3y + 2z - 8 = 0$ .



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**420.** Find the equation of the plane if the point  $(5, -3, 4)$  is the foot of the perpendicular drawn from origin to the plane.



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**421.** Find the equation of a plane which is at a distance 3 units from the origin and which is normal to the vector  $2\hat{i} + 3\hat{j} - 6\hat{k}$ .



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**422.** Find the components of the unit vector perpendicular to the plane

$$r \rightarrow (2\hat{i} + 3\hat{j} - 6\hat{k}) - 6 = 0$$



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**423.** Writing the equation of the plane  $3x - 2y + z + 2 = 0$  in normal form find its distance from origin.



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**424.** Find the angle between the planes

$$x + 2y + 3z + 1 = 0 \text{ and } 3x + 2y + z + 2 = 0$$



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**425.** Find the equation of the plane through the point

$(2,1,0)$  and passing through the intersection of the

planes  $3x - 2y + z - 1 = 0$  and

$$x - 2y + 3z - 1 = 0$$



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**426.** Find the position of the points  $(1, 2, -1)$  and  $(2, -1, 3)$  with respect to the plane  $x + 3y + z + 1 = 0$ .

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**427.** Find the intercepts of a plane  $3x + 4y + 7z = 84$  on co-ordinate axes.

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**428.** Find the equation of the plane through the points  $(1,1,0)$ ,  $(-2,2,1)$  and  $(1,2,1)$ .

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**429.** Find the equation of the plane passing through the points  $(1, -1, 1)$  and  $(1, 1, -1)$  and perpendicular to  $xy$ -plane.

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**430.** A plane meets the co-ordinate axes at  $A, B, C$  such that the centroid of  $\triangle ABC$  is  $(2, -2, 3)$ . Find the equation of the plane.

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**431.** Find the equation of the plane through the feet of the perpendicular drawn from  $P(2,3,5)$  on coordinate planes.



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**432.** Find equation of a plane through  $(2, -3, 1)$  and perpendicular to the line joining the points  $(3, 4, -1)$  and  $(2,-1,5)$ .



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**433.** Find the equation of a plane bisecting the line segment joining  $(-1, 4, 3)$  and  $(5, -2, -1)$  at right angle.



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**434.** Find the equation of planes parallel to the plane  $6x - 3y - 2z + 5 = 0$  and at a distance 2 units from origin.



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**435.** Find the point where the line  $\frac{x-2}{1} = \frac{y}{-1} = \frac{z-1}{2}$  meets the plane  $2x + y + z = 2$ .

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**436.** If the points  $(-1, 3, 2)$ ,  $(-4, 2, -1)$  and  $(5, 5, \lambda)$  are collinear, find  $\lambda$ .

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**437.** Find the angle between the plane  $x + y + z - 2 = 0$  and line

$$\frac{x + 3}{2} = \frac{y - 1}{1} = \frac{z + 1}{4}$$



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**438.** Find the equation of the plane passing through the point  $(2,3,1)$  and perpendicular to the line

$$\frac{x - 1}{1} = \frac{y - 2}{-1} = \frac{z + 1}{2}$$



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**439.** Find the image of the point  $(3, -2, 1)$  in the plane  $x - y + 3z = 2$ .



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**440.** Find the equation of the plane passing through the line  $\frac{x - 8}{3} = \frac{y + 19}{-16} = \frac{z - 10}{7}$  and the point  $(1, 2, -4)$ .



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**441.** Find the length of the perpendicular from  $(2,0,1)$  on the line  $x = y = z$ .



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**442.** Find the equation of the line through  $(-1, 0, 1)$  and perpendicular to the plane  $x + 2y + 1 = 0$ .

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**443.** Show that the lines  $\frac{x+3}{2} = \frac{y+5}{3} = \frac{z-7}{-3}$   
and  $\frac{x+1}{4} = \frac{y+1}{5} = \frac{z+1}{-1}$  are co-planar.

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**444.** Show that the plane  $2x - y - 2z - 4 = 0$   
touches the sphere  $x^2 + y^2 + z^2 + 2x - 6y + 1 = 0$ .

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**445.** Find the equation of the sphere concentric with the sphere  $x^2 + y^2 + z^2 + 4x - 6y + 8z - 5 = 0$  and passing through origin.

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**446.** Find equation of the sphere whose centre is  $(2, -3, 4)$  and which passes through the point  $(1, 2, -1)$ .

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**447.** Find equation of the sphere with centre  $(3, 6, -4)$  and touching the plane  $2x - 2y - z - 10 = 0$ .

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**448.** Find equation of the sphere passing through the points  $(0,0,0)$ ,  $(2,0,0)$ ,  $(0,3,0)$  and  $(0,0,4)$ .

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**449.** If one end of a diameter of a sphere  $x^2 + y^2 + z^2 - 4x - 2y + 2z - 30 = 0$  is  $(4, 5, -5)$

find the other end.



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**450.** Find the equation of the sphere on the join of  $(2,3,5)$  and  $(4, 9, -3)$  as ends of diameter.



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**451.** If the vectors  $\vec{a} = 2\hat{j} - 3\hat{k}$  and  $\vec{b} = 2\hat{j} + \alpha\hat{j} + 6\hat{k}$  are parallel, white the value of  $\alpha$ .



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**452.** If  $|\alpha \vec{a}| = 2$ , what is the value of  $\alpha$ ?



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**453.** If the position vectors of two points A and B are  $3\hat{i} + 2\hat{j} + \hat{k}$  and  $2\hat{i} - 5\hat{j} + 4\hat{k}$  respectively, what is the magnitude of  $\vec{AB}$ ?



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**454.** Given position vectors of P and Q, as  $(1, 0, -2)$  and

$(3, -2, 0)$  respectively, with the unit vector  $\hat{r}_{\text{parallel}} \leq l \rightarrow$   
overset{rarr}(PQ) ?

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**455.** Given co-ordinates of the points A and B as  $(-1, -2)$  and  $(-5, -6)$  respectively, what is the magnitude of  $\overrightarrow{AB}$  ?

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**456.** Write the unit vectors parallel to the vector  $3\hat{i} + \hat{j} - 2\hat{k}$ .

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**457.** Find the direction cosines of the vectors,  $\vec{r}_1 - \vec{r}_2$

where  $\vec{r}_1 = \hat{i} + \hat{j} + \hat{k}$  and  $\vec{r}_2 = 2\hat{i} + \hat{j} + 2\hat{k}$ .



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**458.** Are the points A (2,6,3), B (1,2,7) and (3, 10, - 1)

collinear?



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**459.** What is the angle between the vectors

$\vec{a} = \hat{i} + \hat{j} + \hat{k}$  and  $\vec{b} = 2\hat{i} - \hat{j} + \hat{k}$



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**460.** What is the scalar product of the vectors

$$\vec{a} = 2\hat{i} + \hat{j} + 2\hat{k} \text{ and } \vec{b} = \hat{i} - 2\hat{j} + \hat{k}$$



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**461.** What is the scalar projection of the vector

$$\vec{a} = \hat{i} + \hat{j} + \hat{k} \text{ on } \vec{b} = 2\hat{i} + 2\hat{j} - \hat{k}$$



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**462.** What is the vector projection (component) of the vector  $\vec{a} = 2\hat{i} + \hat{j} - \hat{k}$  on  $\vec{b} = \hat{i} + 2\hat{j} + \hat{k}$



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**463.** What is the unit vector perpendicular to each of the vectors  $\hat{i} + \hat{j}$ ,  $\hat{j} + \hat{k}$ ?



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**464.** What is the area of the parallelogram whose sides are vectors  $2\hat{i} + \hat{j}$  and  $2\hat{j} + \hat{k}$ ?



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**465.** The area of the triangle with vertices  $(2,0,0)$ ,  $(0,1,0)$  and  $(0,0,3)$  is \_\_\_\_\_.



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**466.** If the vectors  $\hat{i} + 2\hat{j} + \hat{k}$  and  $2\hat{i} + 3\hat{j} + \alpha\hat{k}$  are perpendicular, then what is  $\alpha$ ?



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**467.** If the vectors  $\alpha\hat{i} + 3\hat{j} + \hat{k}$  and  $2\hat{i} + \hat{j} + \hat{k}$  are perpendicular, what is  $\alpha$ ?



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468. If  $\vec{a} = \hat{i} - 2\hat{j}$ ,  $\vec{b} = \hat{j} + \hat{k}$ , what is the component of  $\vec{a}$  perpendicular to  $\vec{b}$



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469. If  $|\vec{a}| = 10$ ,  $|\vec{b}| = 1$  and  $\vec{a} \cdot \vec{b} = 0$ , then  $|\vec{a} \times \vec{b}| = \underline{\hspace{2cm}}$ .



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470. If  $\vec{a} \cdot \vec{b} = 0$  and  $\vec{a} \times (\vec{b} \times \vec{c}) = \vec{0}$  then  $\vec{a} \cdot \vec{c} = ?$

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471. If two vectors  $\vec{a}$  and  $\vec{b}$  are such that  $|\vec{a} + \vec{b}| = |\vec{a} - \vec{b}|$ , then what is the angle between  $\vec{a}$  and  $\vec{b}$ ?

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472. If  $[\vec{a} \ \vec{b} \ \vec{c}] = 10$ , what is the value of  $[\vec{a} + \vec{b}, \vec{b} + \vec{c}, \vec{c} + \vec{a}]$ ?



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473. If  $\vec{a} = 4\hat{i} + n\hat{j} + 3\hat{k}$  and  $|\vec{a}| = 13$ , what is the value of  $n$ ?



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474. If  $\left[ \vec{a} \vec{b} \vec{c} \right] = 5$ , then what is  $\left[ \vec{a} \times \vec{b} \vec{b} \times \vec{c} \vec{c} \times \vec{a} \right]$ ?



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475. What is the value of  $x$  of the vectors  $3\hat{i} - 7\hat{j} - 4\hat{k}$ ,  $3\hat{i} - 2\hat{j} + \hat{k}$  and  $\hat{i} + \hat{j} + x\hat{k}$

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476. If  $(\vec{a} + \vec{b})(\vec{a} - \vec{b}) = 12$  and  $|\vec{a}| = 2|\vec{b}|$  then what is  $|\vec{a}|$

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477. If  $\vec{a}, \vec{b}, \vec{c}$  are unit vectors such that  $\vec{a} + \vec{b} + \vec{c} = 0$ , then what is the value of  $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}$ ?



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478. If  $\theta$  is angle between  $\vec{a}$  and  $\vec{b}$  and  $|\vec{a} \times \vec{b}| = |\vec{a} \vec{b}|$  Then  $\theta$  equal to?



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479. If  $\vec{a} = 2\vec{j}$  and  $\vec{c} = -3\vec{j}$  what is the angle between  $\vec{a}$  and  $\vec{c}$ ?



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**480.** Show that the points A,B,C with position vectors  $\vec{i} + 2\vec{j} + 3\vec{k}$ ,  $2\vec{i} + 11\vec{j} - 4\vec{k}$  and  $-7\vec{j} + 10\vec{k}$  are co-planer.

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**481.** Find a vector in the direction of the vector  $\vec{a} = 5\hat{i} - \hat{j} + 2\hat{k}$  which has magnitude 8 units.

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**482.** Write the values of m and n for which the vectors  $(m - 1)\hat{i} + (n + 2)\hat{j} + 4\hat{k}$  and

$(m + 1)\hat{i} + (n - 2)\hat{j} + 8\hat{k}$  are parallel



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**483.** Find the magnitude of  $\vec{a} + \vec{b} - 2\vec{c}$  where

$$\vec{a} = (2, 3, 4) \quad \vec{b} = (1, -1, 2) \quad \text{and} \quad \vec{c} = (1, 0, 3)$$



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**484.** Show that the vectors  $\hat{i} + \hat{j} - 2\hat{k}$ ,  $\hat{i} - 2\hat{j} + \hat{k}$  and  $2\hat{i} - \hat{j} - \hat{k}$  are the sides of an equilateral triangle.



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485.

If

$$\vec{a} = (2, 3, 6), \vec{b} = (2, -2, 1), \vec{c} = (-1, 0, 2)$$

find the direction cosines of  $\vec{b} - \vec{a} + 2\vec{c}$ .



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486. If the sum of two unit vectors is a unit vector  
find the magnitude of their difference.



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487. Show that the vectors  $3\hat{i} - 4\hat{j} - 4\hat{k}$ ,  $2\hat{i} - \hat{j} + \hat{k}$   
and  $\hat{i} - 3\hat{j} - 5\hat{k}$  form a right angled triangle.



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**488.** Find the value of  $k$  for which  $A(1,0,3)$ ,  $B(-1,2,4)$ ,  $C(1,2,1)$  and  $D(k,2,5)$  are coplaner.



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**489.** Find the scalar components of the unit vector which is perpendicular to the vectors  $\hat{i} + 2\hat{j} - \hat{k}$  and  $3\hat{i} - \hat{j} + 2\hat{k}$ .



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**490.** Find a unit vector perpendicular to each of the vectors  $(\vec{a} + \vec{b})(\vec{a} - \vec{b})$  where  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$  and  $\vec{b} = 2\hat{i} + 3\hat{k}$



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**491.** Find the vector of magnitude 5 units and parallel to the resultant of the vectors  $\vec{a} = 2\hat{i} + 3\hat{j} - \hat{k}$  and  $\vec{b} = \hat{i} - 2\hat{j} + \hat{k}$  then find the angle between  $\vec{a} + \vec{b}$  and  $\vec{a} - \vec{b}$ .



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**492.** If  $\vec{a} = \hat{i} + 2\hat{j} - 3\hat{k}$  and  $\vec{b} = 3\hat{i} - \hat{j} + 2\hat{k}$  then find the angle between

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**493.** State True or False. The region given by  $2x + 5y \geq 1$  is a bounded region.

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**494.** State True or False .The region  $x + 2y \leq 8, 2x + y \leq 8$  and  $x \geq 0, y \geq 0$  is unbounded.

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**495.** The feasible region  $x + y \geq 0$ ,  $2x + y \leq 0$  is a bounded set.

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**496.**  $(1,5)$  is a point in the region  $2x - y \geq 4$ ,  $2x + 5y \leq 2$

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**497.** The minimum value of  $2x + 5$  subject to  $3x - 1 \geq 1$  is \_\_\_\_\_.

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**498.** Shade the feasible region for the inequations  $2x + 3y \leq 6$ ,  $x \geq 0$ ,  $y \geq 0$  in a rough figure.

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**499.** Find the feasible region satisfying the inequation  $2x + y \leq 4$ ,  $x \geq 0$ ,  $y \geq 0$ .

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**500.** For the LPP:

$$\text{Maximize } z = 5x_1 + 7x_2$$

$$\text{subject to } x_1 + x_2 < 4$$

$$3x_1 + 8x_2 \leq 24.$$

$$10x_1 + 7x_2 \leq 35.$$

$$x \geq 0, y \geq 0.$$

Examine whether  $\left(\frac{10}{3}, \frac{11}{5}\right)$  is a feasible solution or not.



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**501.** Find the feasible solution for the system

$$x + y \geq 1, 2x + y \leq 4, x \geq 0, y \geq 0.$$



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**502.** Is the number set  $\{0.2, -0.5, 0.9, 0.4\}$

determining a probability distribution ?



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**503.** Does the number set  $\{0.6, 0.5, 0.9, 0.1\}$  give a

probability distribution ?



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**504.** If a die is rolled twice and  $X$  is the sum of scores obtained is greater than 10, then find  $P(X < 10)$ .



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**505.** If  $X$  be a random variable which takes the values  $0, 1, 2, \dots$  with probabilities  $P(X = i) = cp^i, 0 < p < 1$ , then find  $c$  if  $X$  is a probability distribution.



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**506.** If  $\{0.1, 0.2, c, 0.5\}$  determines a probability distribution, find  $c$ .



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**507.** An unbiased die is thrown twice. What is the probability distribution of the number of sixes ?



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**508.** A fair coin is tossed repeatedly. If tails appear on first four tosses, what is the probability of head appearing on the fifth toss ?

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**509.** If two cards are drawn at random from a desk of cards, and  $X$  be the number of aces obtained, what is  $E(X)$  ?

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**510.** What is the variance of  $X$ , given as follows : For the given data :



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511. A die is thrown 5 times. If getting an even number is a success, what is the probability of 3 successes ?

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512. The standard deviation of a binomial distribution  $(p + q)^{16}$  is 2. Find its mean.

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513. The maximum value of variance in binomial distribution with parameters  $n$  and  $p$  is \_\_\_\_.

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**514.** A binomial distribution has mean 5 and variance 4. Find the number of trials.

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**515.** A die is thrown 15 times. Getting a number greater than 5 is a success. Find the mean and variance of the number of successes ?

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**516.** The probability of an event happening in one trial of an experiment is 0.6. Three independent trials are made. Find the probability that the event happens at least once.



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**517.** Two dice are tossed 6 times. Find the probability that 7 will show an exactly four of the tosses.



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**518.** If  $X$ -following a Binomial distribution with parameter  $n=6$  and  $p$ , and if  $4 P(X=4)=P(X=2)$  find  $p$ .



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**519.** A cartoon contains 20 bulbs, 5 of which are defective. Find the probability that if a sample of 3 bulbs is chosen at random from the cartoon 2 will be defective.



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**520.** An unbiased coin is tossed  $n$  times. Let  $X$  denote the number of times head occurs. If  $p(X=4)$ ,  $p(X=5)$  and  $p(X=6)$  are in A.P. then find the value of  $n$ .



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**521.** An experiment succeeds twice as often as it fails. Find the probability that in the next six trials there are at least 4 success.



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**522.** Find the expectation of the number of tails in 15 tosses of a coin.



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**523.** If the sum of the mean and the variance of a binomial distribution for 5 trials is 1,8, find the distribution.



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