

MATHS

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CO-ORDINATE GEOMETRY OF THREE DIMENSIONS

Question Bank

1. Name the octant wherein the given points

lies: (1,2,3)



2. Name the octant wherein the given points lies: (-2,-1,4)



3. Name the octant wherein the given points lies: (2,-5,1)



4. Name the octant wherein the given points

lies: (-1,-3,-2)



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5. Find the distance between the points (2,-4,1) and (1,3,-1)



6. Find the value of x if the distance between the points (7,1,x) and (4,5,9) is 13.



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7. Find the co-ordinates of the point which divides the line joining the points (2,-4,3) and (-4,5,-6) in the ratio 2:1



8. Find the ratio in which the line segment joining the points (3,5,7) and (-2,4,6) is divided by YZ plane



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9. Find the direction ratios of the line joining the points (1,1,-3) and (-2,-3,2)



10. Find the direction cosines of the line joining the points (1,1,-3) and (-2,-3,2)



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11. Find the projections (feet of the perpendiculars) of the point(1,-2,4) on the Coordinate planes



12. Find the projections (feet of the perpendiculars) of the point(1,-2,4) on the Coordinate axes



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13. Find the projection of the line segment joining the points (3,3,5) and (5,4,3) on the line joining the points (2,-1,4) and (0,1,5)



14. If the co-ordinates of the point p are (1,2,2), what are the direction cosines of OP. (Here O is origin).



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15. A line makes 45° and 60° with y and z axes respectively. What angle does it make with the x axis?



16. Can the direction cosines of a line be

$$\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}?$$



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17. If OP=3 and the direction ratios of OP be 4,2 and 4 then find the co-ordinates of p.



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18. If $\cos \alpha, \cos \beta, \cos \gamma$ be the direction cosines of a line, prove that $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma = 2.$



19. Find the direction cosines of a line which makes equal angles with the coordinate axes.



20. For what value 'a' will the number $\sqrt{\frac{1}{2}}$, a, $\sqrt{\frac{1}{3}}$ be the direction cosines of a line?

21. The angle between the planes 2x-y+3z=6 and x+y+2z=7 is

A. 0°

B. 30°

C. 45°

D. 60°

Answer: D



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22. A line joining the points (1,1,1) and (2,2,2)

intersect the plane x+y+z=9 at the point

A. (3,4,2)

B. (2,3,4)

C. (3,2,4)

D. (3,3,3)

Answer: D



23. Find the image of point (3,-2,1) in the plane

$$3x-y+4z=2$$
.

- A. (0,1,3)
- B. (0,-1,-3)
- C.(0,-1,3)
- D. (0,1,-3)

Answer: B



24. Let L be the line of intersection of the planes 2x + 3y + z = 1 and x + 3y + 2z = 2

. If L makes an angles lpha with the positive x-axis, then $\cos \alpha$ equals $\frac{1}{\sqrt{3}} \frac{1}{2} 1 \frac{1}{\sqrt{2}}$

$$B. \frac{1}{\sqrt{2}}$$

C.
$$\frac{1}{\sqrt{3}}$$
 D. $\frac{1}{2}$

D.
$$\frac{1}{2}$$

Answer: C



25. The ratio in which the line joining (2,4,5) and (3,5,-4) is divided by the yz-plane is

A. 2:3

B. 3:2

C. -2:3

D. 4:(-3)

Answer: C



26. The distance of the point (2,1,-1) from the

plane
$$x-2y+4z=9$$
 is (A) $\dfrac{\sqrt{13}}{21}$ (B) $\dfrac{13}{21}$ (C)

$$\frac{13}{\sqrt{21}}$$
 (D) $\sqrt{\frac{13}{21}}$

A.
$$\frac{\sqrt{13}}{21}$$

B.
$$\frac{13}{12}$$

$$\mathsf{C.} \; \frac{13}{\sqrt{21}}$$

D.
$$\sqrt{\frac{13}{21}}$$

Answer: C



27. The line
$$\frac{x+1}{1} = \frac{y-1}{2} = \frac{z-1}{0}$$

A. is perpendicular to z-axis

B. is parallel to z-axis

C. lies in xy-plane

D. None of these

Answer: A



28. Equation of the line passing through (1,1,1)

and perpendicular to the plane 2x+3y-z-5=0 is

A.
$$\frac{x-1}{2} = \frac{y-1}{3} = \frac{z-1}{1}$$

B.
$$\frac{x-1}{2} = \frac{y-1}{3} = \frac{z-1}{-1}$$

c.
$$\frac{x-1}{2} = \frac{y-1}{-1} = \frac{z-1}{1}$$

D. None of the above

Answer: B



29. Find the distance of the following points from the origin (0,-4,4)



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30. Find the distance of the following points from the origin (2,4,-3)



31. Find the distance of the following points from the origin (4,-5,3)



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32. What is the distance of the y-axis from the point(3,-4,0)?



33. Find the distances between the following pair of points. (4,3,-6) and (-2,1,-3)



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34. Find the distances between the following pair of points. (-4,-2,3) and (3,3,5)



35. If the distance between the points (x,2,0) and (1,3,1) be $\sqrt{6}$, find the value of x.



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36. Show that the points (1,-2,-3),(2,-3,-1) and (3,-1,-2) are the vertices of an equilateral triangle



37. Show that the triangle with vertices (6,10,10),(1,0,-5) and (6,-10,0) is a right angled triangle



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38. Find the locus of the point which is equidistant from the points (1,-2,3) and (-3,4,2).



39. The distance of a point from the x-axis is twice its distance from the point (1,2,-1). Find the locus of the point.



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40. A point moves in such a way that its distance from the X-axis is twice its distance from the Y-axis. Find the locus of the point.



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41. Find the co-ordinates of the point which divides the join of (5,8,-3) and (1,0,-3) in the radio 3:1.



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42. In what ratio does the origin divides the line segment joining the points P(-1,-2,-3) and Q(4,8,12).



43. Find the co-ordinates of the centroid of the triangle whose vertices are (3,1,4),(-2,5,3) and (4,-5,3)



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44. Find the point of intersection of the medians of the triangle whose vertices are (-1,-3,-4).(4,-2,-7) and (2,3,-8).



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45. Find the lengths of the medians of the triangle whose vertices are A(2,-3,1),B(-6,5,3) and C(8,7,-7).



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46. Can there be any line which makes angles 30° , 45° and 60° with the co-ordinate axes?



47. If a line makes angles 60° and 135° respectively with x and y axes find the value of $\cos \gamma$, where γ is the angle made the line with the z axis.



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48. If a line makes angles α,β and γ with the co-ordinate axes, find $\cos\beta$, if $\cos\alpha=\frac{14}{15}$ and $\cos\gamma=-\frac{1}{3}$.



49. Find the direction cosines of the line whose direction ratio are 2,-4,6



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50. Find the direction cosines of the line whose direction ratio are $\sqrt{3},\,0,\,-1$



51. Find the direction cosines of the line whose direction ratio are a-b,b-c,c-a



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52. If a line make angle 30° and 60° with the x and y axes, what angles does it make with the z axes?



53. Find the direction ratios and direction cosines of the lines joining the following points.(1,2,3) and (4,5,6)



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54. Find the direction ratios and direction cosines of the lines joining the following points. (5,3,-2) and (3,-1,4)



55. Find the angle between the following pair of lines whose direction ratios are given 1,2,3 and 2,-4,4



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56. Find the angle between the following pair of lines whose direction ratios are given -1,2,1and 2,3,-1



57. Show that the line joining the points (1,2,3) and (4,5,7) is parallel to the line joining the points (-4,3,-6) and (2,9,2).



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58. For what value of x will the line joining the points (x,6,-3),(5,3,2) will be perpendicular to the joining the points (2,5,1),(-6,2,6)?



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59. A (6,3,2),B(4,1,4),C(3,-4,7) and D(0,2,5) are four given points. Find the projection of AB on CD and projection of CD on AB.



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60. For that value of a will be the numbers

$$\frac{1}{\sqrt{2}}$$
, a , $\frac{1}{\sqrt{3}}$ be the direction cosines of a line?

