

### **MATHS**

## **BOOKS - MAHAVEER PUBLICATION**

#### **FUNCTION**

# **Question Bank**

**1.** Write the following sets in roster set builder form A=collection of months of a year beginning with the letter J.



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**2.** Write the following sets in roster set builder form B=collection all the natural numbers less than 10.



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**3.** Write the following sets in roster set builder form C= collection of all even integers



**4.** Write the following sets in roster form D= collection of all the letters of the word TRIGONOMETRY.



**5.** Write the following sets in set builder form E= collection of all positive rational numbers.



**6.** Let A={1,2,3},B={3,4},C={4,5,6}, find  $A imes (B \cap C)$ 



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**7.** If  $A = \{1, 2, 3\}, B = \{3, 4\} \text{ and } C = \{4, 5, 6\}, \text{ then find each of the following:}$ 

$$(i)A imes (B\cap C) \qquad (ii)(A imes B)\cap (A imes C)$$

$$(iii)A imes (B \cup C) \qquad (iv)(A imes B) \cup (A imes C)$$



- **8.** Let A={1,2,3},B={3,4},C={4,5,6}, find  $A imes (B \cup C)$ 
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- **9.** Let A={1,2,3,4,....,14} Define a relation R from a set A to A by  $R=\{(x,y): 2x-y=0, x,y\in A\}$  Write down its domain and range.
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10. Which of the following relations are functions from A to B write their

domain and range if it is not a function give reason 
$$?f \colon A o B$$
 is defined by

 $f = \{(1, -2), (3, 7), (5, 6), (9, 0)\}, A = \{1, 3, 5, 9\}, B = \{-2, 7, -6, 0, -$ 



11. Which of the following relations are functions from A to B write their domain and range if it is not a function give reason  $f = \{(1,0), (1,-1), (2,3), (4,10)\}, A = \{1,2,4\}, B = \{0,-1,3,10\}$ 



12. Which of the following relations are functions from A to B write their domain and range if it is not a function give reason  $f = \{(a, b), (b, c), (c, b), (d, c)\}, A = \{a, b, c, d, e\}, B = \{b, c\}$ 



**13.** Which of the following relations are functions from A to B write their domain and range if it is not a function give reason ?  $f = \{(a, b), (a, 2), (b, 3), (b, 4)\}, A = \{a, b\}, B = \{b, 2, 3, 4\}$ 



**14.** Show that the function  $f\colon N o N$  given by f(x)=3x is one one but not onto



**15.** Show that the function  $f\!:\!R o R$  defined by  $f(x)=x^2$  is neither one-one nor onto.



**16.** the function  $f\!:\!R o R$  defined as  $f(x)=x^3$  is

**17.** Show that the function  $f\!:\!R o R$  defined by f(x)=|x| is neither one one nor onto



**18.** In each of the following case check whether the functions are one-one onto or bijective. Justify your answer  $f\!:\!R o R$  defined by f(x)=3-4x



**19.** in each of the following case check whether the functions are one one or onto or bijective justify your answer  $f\colon R-\{3\} o\{1\}$  defined by  $f(x)=rac{x-2}{x-3}$ 



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**20.** find the period of the following functions:  $f(x) = 3\sin 2x$ 



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**21.** find the period of the following functions:  $f(x) = \cos\left(\frac{x}{2}\right)$ 



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**22.** find the period of the following functions:  $f(x) = an \left( rac{x}{4} 
ight)$ 



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**23.** find g0f and f0g if  $f\!:\!R \to R$  and  $g\!:\!R \to R$  are given by  $f(x)=\cos x \, ext{ and } \, g(x)=3x^2$  also show that g0f is not equal to f0g



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24. Which of the following relations are functions? Give reasons. If it is a function, determine its domain and range.

- (i)  $\{(2,1),(5,1),(8,1),(11,1),(14,1),(17,1)\}$
- (ii)  $\{(2,1),(4,2),(6,3),(8,4),(10,5),(12,6),(14,7)\}$
- (iii) {(1,3),(1,5),(2,5)}



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25. which of the following relation are functions and give reason if it is a function determine domain its and range  $\{(2,1), (4,2), (6,3), (8,4), (10,5), (12,6), (14,7)\}$ 



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26. Which of the following relations are functions? Give reasons. If it is a function, determine its domain and range.

(i)  $\{(2,1),(5,1),(8,1),(11,1),(14,1),(17,1)\}$ 

- (iii) {(1,3),(1,5),(2,5)}
  - 0
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  - 27. if  $f(x)=rac{x-1}{|x-1|}$  find the value of f(-1) and f(2)

**28.** Find the domain and range of the following function  $f(x) = \sqrt{x-1}$ 

**29.** Find the domain and range of the following function f(x) = |x-1|

(ii)  $\{(2,1),(4,2),(6,3),(8,4),(10,5),(12,6),(14,7)\}$ 

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**30.** Find the domain and range of the following function

$$f(x)=2-3x, x\in R, x>0$$



**31.** Find the domain and range of the following function  $f(x)=x^2+2$ 



**32.** Find the domain and range of the following function  $f(x) = \frac{1}{x}$ 



**33.** Find the domain and range of the following function f(x) = -|x|



**34.** Find the domain and range of the following function  $f(x) = \sqrt{16-x^2}$ 



**35.** Find the domain and range of the following functions:

$$\overline{1+x^2}$$

 $x^2$ 



Z defined by f(x)=ax+b for some integer a and b. Determine a and b

**36.** let  $f = \{(1, 1), (2, 3), (0, -1), (-1, -3)\}$  be a function from Z to



**37.** Find the domain of the function  $f(x) = rac{x^2 + 3x + 5}{x^2 - 5x + 4}$ 



**38.** Find the domain of the function  $f(x) = \frac{x^2 + 2x + 1}{x^2 - 8x + 12}$ 



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**39.** Find the domain of the function  $f(x)=rac{x^2-x+x}{x^2+x+1}$ 



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**40.** Find the domain of the function  $f(x) = \frac{x-2}{3-x}$ 



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**41.** Find the domain of the function f(x) = 1 - |x-2|



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**42.** Find the domain of the function 
$$f(x) = \frac{1}{\sqrt{x-5}}$$



**43.** Find the domain of the function 
$$f(x) = rac{|x-4|}{r} - 4$$

**44.** Find the domain of the function  $f(x) = \frac{1}{x^3}$ 

**45.** Find the domain of the function  $f(x) = \frac{x^2 - 4}{x^4}$ 





**47.** Find the domain of the function 
$$y = \cos x$$

**48.** Find the domain of the function  $y = \tan x$ 

**49.** Find the domain of the function  $y = \sin x + \cos x$ 

**50.** If  $f(x)=rac{1}{2x+1},\;x
eq-rac{1}{2},\;$  then show that  $f(f(x))=rac{2x+1}{2x+3}$  ,











provided that  $x \neq -\frac{3}{2}$ .

**51.** If  $f\!:\!R o R$  is defined by  $f(x)=rac{x}{r^2+1}$  find f(f(2))



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**52.** If  $f(x) = \frac{1}{1-x}$  show that f(f(f(x)))=x



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**53.** If  $f(x) = \frac{x-1}{x+1}$  then show that  $f\left(\frac{1}{x}\right) = -f(x)$  and  $f\bigg(-\frac{1}{x}\bigg) = \frac{-1}{f(x)}$ 



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**54.** If  $f(x)=x^2-3x+1$  find  $x\in R$  such that f(2x)=f(x).



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**55.** If  $f(x) = x^2 - 3x + 1$  find  $x \in R$  such that f(2x) = 2f(x)



**56.** Determine whether the functions are even or odd f(x) = |-x|



**57.** Determine whether the functions are even or odd f(x) = |x-2|



**58.** Determine whether the functions are even or odd if  $f(x)=x^2+kx+1$  for all x and f is an even function then find k



**59.** Let  $f\!:\!N o N\!:\!f(x)=2x,g\!:\!N o N\!:\!g(y)=3y+4$ 

and  $h\!:\!N o N\!:\!h(z)=\,$  sin z

Show that  $h \circ (g \circ f) = (h \circ g) \circ f$ .



**60.** Find gof and fog if f(x) = |x| and g(x) = |3 - 2x|



**61.** Find gof and fog if  $f(x)=8x^3$  and  $g(x)=x^{\frac{1}{3}}$ 



**62.** What is the maximum number of points in which a vertical line can meet the graph of real valued function?



**63.** Fid the domain for which the functions  $f(x) = 2x^2 - 1$ andg(x) = 1 - 3x are equal.



**64.** Write the range of the function  $f(x) = -x^2, x \in R$ 



65. Write the domain and range of the signum function,



**66.** Is the function  $f(x) = x^{3n}, n \in N$  even?



**67.** Write the range of the function  $f(x) = x^2 + 1$  , $x \in R$ 



**68.** Write the domain and range of the function  $f(x) = \left[x
ight]$ 



**69.** If  $f(x)=4x-x^2$  then find f(a+1)-f(a-1)



**70.** If A and B are finite sets with n(A) =3 and N(B)=6 then find  $n(A \times B)$ 



**71.** Is the function  $f\colon R \to R$  be defined by f(x)=2x+3 a one on one function?



**72.** Find the range of the function  $f(x)=\dfrac{|x-a|}{x-a}$  , x is not equal to a



**73.** Find the domain of the function  $f(x) = \frac{x}{x^2 + 5x + 6}$ 



**74.** Find the range of the function  $f(x) = -x^2 - 100$ 



**75.** Is the function f(x) = |x| one on one?



**76.** Show that the function  $f\!:\!R o R$  defined by  $f(x)=x^2$  is neither one-one nor onto.



**77.** If R denotes the set of all real numbers, then the function  $f\!:\!R o R$  defined by f(x)=[x] is



**78.** A horizontal line meets the graph of the function y=f(x) in two points is fone one?



**79.** If  $t(C)=rac{9C}{5}+32$  write the value of t(28)



**80.** Find the range of the function  $f(x) = [x], 1 \le x < 3$ 



**81.** Find the total number of function from a set A to B where n(A)=3 and n(B)=4



82. Find the period of the function  $f(x)=\sin 5x$ 



**83.** If (x+y,x-y)=(1,2) find x and y



**84.** Find the domain and range of the following relation  $R = \{(1,3), (1,5), (1,7), (1,9)\}$ 



**85.** Find the domain and range of the following relation  $R=\{(x,y)\colon x\in N, x<6 \ ext{and} \ y=4\}$ 



**86.** Find the domain and range of the following relation



 $R = \{(x+2, x+4) : x \in \{0, 1, 2, 3, 4, 5\}\}$ 

**87.** which of the following relations are functions from A={1,3,5,7,9} to B=

$$\{1,2,3,4,5\}$$
  $f = \{(3,2), (1,5), (5,1), (7,4), (9,5)\}$ 



88. which of the following relations are functions from A={1,3,5,7,9} to B=

$$\{1,2,3,4,5\}\ f=\{(1,3),(3,1),(5,3),(5,5),(1,4)\}$$



**89.** If  $f\!:\!R o R$  defined by  $f(x)=x^2-2x+3$ , then find f(f(x)).



**90.** Find the domain and range of the following  $f(x) = \frac{1}{2x-1}$ 



**91.** Find the domain and range of the following  $f(x)=rac{3}{2-x^2}$ 



**92.** Find the domain and range of the following  $f(x) = 1 + 3\cos 2x$ 



**93.** Find the domain and range of the following  $f(x)=\dfrac{1}{x^2-1}$ 



**94.** Find the domain and range of the following  $f(x) = \frac{1}{\sqrt{1-\cos x}}$ 



 $f(x) = x^4 + x^2$ 



96. Which of the following functions are even and which odd?  $f(x) = x^3 + x$ 

97. which of the following functions are even and which odd?

95. Which of the following functions are even and which odd?



 $f(x) = x^3 + x$ 





**98.** if  $f(x) = \frac{1}{1-x}$  then find  $f\left(\frac{x-1}{x}\right)$ 



**100.** If f and g are two functions defined by  $f(x)=\sqrt{x+1}$  and  $g(x)=rac{1}{x}$  then find the following functions: f+g



**101.** If f and g are two functions defined by  $f(x)=\sqrt{x+1}$  and  $g(x)=rac{1}{x}$  then find the following functions: f-g



**102.** If f and g are two functions defined by  $f(x)=\sqrt{x+1}$  and  $g(x)=rac{1}{x}$  then find the following functions: fg

**103.** If f and g are two functions defined by 
$$f(x)=\sqrt{x+1}$$
 and  $g(x)=rac{1}{x}$  then find the following functions:  $rac{f}{a}$ 



**104.** If f and g are two functions defined by  $f(x)=\sqrt{x+1}$  and  $g(x)=rac{1}{x}$  then find the following functions: 2f-3g



**105.** If f and g are two functions defined by  $f(x)=\sqrt{x+1}$  and  $g(x)=rac{1}{x}$  then find the following functions:  $2f^2+\sqrt{2}g$ 



**106.** Draw the graph of the following functions and hence find the range of f(x)=1-x





**107.** Draw the graph of the following functions and hence find its ranges  $f(x) = 2x^2$ 



**108.** Draw the graph of the following functions and hence find its ranges :



109. Draw the graph of the following functions and hence find its ranges:

 $f(x)=2x^3$ 

 $2x^3$ 

**110.** Check the injectivity and surjectivity of the following functions  $f\colon Z o Z$  defined by  $f(x)=x^2$ 

**111.** Check the injectivity and surjectivity of the following functions  $f\colon R o R$  defined by f(x)=3x+10



112. Check the injectivity and surjectivity of the following functions

$$f{:}R-\left\{\left(-rac{4}{3}
ight)
ightarrow R$$
 defined by  $f(x)=4rac{x}{3x+4}$ 

113. Check the injectivity and surjectivity of the following functions

$$f{:}\,R o [5,\infty)$$
 defined by  $f(x) = 9x^2 + 6x - 5$ 



**114.** If 
$$f\!:\!R-\left\{\frac{2}{3}\right\} o R$$
 defined by  $f(x)=\frac{4x+3}{6x-4}$  show that  $f(f(x))=x$ 



**115.** Show that the function  $f\!:\!R o R$  defined by  $f(x)=x^4+5$  is neither one one nor onto

