# びdoubtnut 

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## MATHS

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## FUNCTION

## Question Bank

1. Write the following sets in roster set builder form $A=$ collection of months of a year beginning with the letter J.

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2. Write the following sets in roster set builder form $B=$ collection all the natural numbers less than 10 .
3. Write the following sets in roster set builder form $\mathrm{C}=$ collection of all even integers

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4. Write the following sets in roster form $D=$ collection of all the letters of the word TRIGONOMETRY.

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5. Write the following sets in set builder form $E=$ collection of all positive rational numbers.

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6. Let $\mathrm{A}=\{1,2,3\}, \mathrm{B}=\{3,4\}, \mathrm{C}=\{4,5,6\}$, find $A \times(B \cap C)$
7. If $\mathrm{A}=\{1,2,3\}, B=\{3,4\}$ and $C=\{4,5,6\}$, then find each of the following :
(i) $A \times(B \cap C)$
$(i i)(A \times B) \cap(A \times C)$
$(i i i) A \times(B \cup C) \quad(i v)(A \times B) \cup(A \times C)$

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8. Let $\mathrm{A}=\{1,2,3\}, \mathrm{B}=\{3,4\}, \mathrm{C}=\{4,5,6\}$, find $A \times(B \cup C)$

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9. Let $A=\{1,2,3,4, \ldots ., 14\}$ Define a relation $R$ from a set $A$ to $A$ by $R=\{(x, y): 2 x-y=0, x, y \in A\}$ Write down its domain and range.

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10. Which of the following relations are functions from $A$ to $B$ write their domain and range if it is not a function give reason ? $f: A \rightarrow B$ is defined by $f=\{(1,-2),(3,7),(5,6),(9,0)\}, A=\{1,3,5,9\}, B=\{-2,7,-6,0$,

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11. Which of the following relations are functions from $A$ to $B$ write their domain and range if it is not a function give reason ? $f=\{(1,0),(1,-1),(2,3),(4,10)\}, A=\{1,2,4\}, B=\{0,-1,3,10\}$

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12. Which of the following relations are functions from $A$ to $B$ write their domain and range if it is not a function give reason ?
$f=\{(a, b),(b, c),(c, b),(d, c)\}, A=\{a, b, c, d, e\}, B=\{b, c\}$
13. Which of the following relations are functions from $A$ to $B$ write their domain and range if it is not a function give reason ? $f=\{(a, b),(a, 2),(b, 3),(b, 4)\}, A=\{a, b\}, B=\{b, 2,3,4\}$

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14. Show that the function $f: N \rightarrow N$ given by $f(x)=3 x$ is one one but not onto

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15. Show that the function $f: R \rightarrow R$ defined by $f(x)=x^{2}$ is neither one-one nor onto.

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16. the function $f: R \rightarrow R$ defined as $f(x)=x^{3}$ is
17. Show that the function $f: R \rightarrow R$ defined by $f(x)=|x|$ is neither one one nor onto

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18. In each of the following case check whether the functions are one-one onto or bijective. Justify your answer $f: R \rightarrow R$ defined by $f(x)=3-4 x$

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19. in each of the following case check whether the functions are one one or onto or bijective justify your answer $f: R-\{3\} \rightarrow\{1\}$ defined by $f(x)=\frac{x-2}{x-3}$

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20. find the period of the following functions: $f(x)=3 \sin 2 x$

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21. find the period of the following functions: $f(x)=\cos \left(\frac{x}{2}\right)$

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22. find the period of the following functions: $f(x)=\tan \left(\frac{x}{4}\right)$

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23. find $g 0 f$ and $f 0 g$ if $f: R \rightarrow R$ and $g: R \rightarrow R$ are given by $f(x)=\cos x$ and $g(x)=3 x^{2}$ also show that $g 0 f$ is not equal to $f 0 g$

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24. Which of the following relations are functions? Give reasons. If it is a function, determine its domain and range.
(i) $\{(2,1),(5,1),(8,1),(11,1),(14,1),(17,1)\}$
(ii) $\{(2,1),(4,2),(6,3),(8,4),(10,5),(12,6),(14,7)\}$
(iii) $\{(1,3),(1,5),(2,5)\}$

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25. which of the following relation are functions and give reason if it is a function determine its domain and range $\{(2,1),(4,2),(6,3),(8,4),(10,5),(12,6),(14,7)\}$

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26. Which of the following relations are functions? Give reasons. If it is a function, determine its domain and range.
(i) $\{(2,1),(5,1),(8,1),(11,1),(14,1),(17,1)\}$
(ii) $\{(2,1),(4,2),(6,3),(8,4),(10,5),(12,6),(14,7)\}$
(iii) $\{(1,3),(1,5),(2,5)\}$

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27. if $f(x)=\frac{x-1}{|x-1|}$ find the value of $\mathrm{f}(-1)$ and $\mathrm{f}(2)$

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28. Find the domain and range of the following function $f(x)=\sqrt{x-1}$

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29. Find the domain and range of the following function $f(x)=|x-1|$

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30. Find the domain and range of the following function $f(x)=2-3 x, x \in R, x>0$

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31. Find the domain and range of the following function $f(x)=x^{2}+2$

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32. Find the domain and range of the following function $f(x)=\frac{1}{x}$

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33. Find the domain and range of the following function $f(x)=-|x|$

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34. Find the domain and range of the following function $f(x)=\sqrt{16-x^{2}}$

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35. Find the domain and range of the following functions:
$\frac{x^{2}}{1+x^{2}}$

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36. let $f=\{(1,1),(2,3),(0,-1),(-1,-3)\}$ be a function from Z to
$Z$ defined $b y f(x)=a x+b$ for some integer $a$ and $b$. Determine $a$ and $b$

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37. Find the domain of the function $f(x)=\frac{x^{2}+3 x+5}{x^{2}-5 x+4}$
38. Find the domain of the function $f(x)=\frac{x^{2}+2 x+1}{x^{2}-8 x+12}$

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39. Find the domain of the function $f(x)=\frac{x^{2}-x+x}{x^{2}+x+1}$

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40. Find the domain of the function $f(x)=\frac{x-2}{3-x}$

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41. Find the domain of the function $f(x)=1-|x-2|$

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42. Find the domain of the function $f(x)=\frac{1}{\sqrt{x-5}}$

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43. Find the domain of the function $f(x)=\frac{|x-4|}{x}-4$

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44. Find the domain of the function $f(x)=\frac{1}{x^{3}}$

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45. Find the domain of the function $f(x)=\frac{x^{2}-4}{x-4}$

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46. Find the domain of the function $y=\sin x$
47. Find the domain of the function $y=\cos x$

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48. Find the domain of the function $y=\tan x$

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49. Find the domain of the function $y=\sin x+\cos x$

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50. If $f(x)=\frac{1}{2 x+1}, x \neq-\frac{1}{2}$, then show that $f(f(x))=\frac{2 x+1}{2 x+3}$, provided that $x \neq-\frac{3}{2}$.
51. If $f: R \rightarrow R$ is defined by $f(x)=\frac{x}{x^{2}+1}$ find $f(f(2))$

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52. If $f(x)=\frac{1}{1-x}$ show that $\mathrm{f}(\mathrm{f}(\mathrm{f}(\mathrm{x})))=\mathrm{x}$

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53. If $f(x)=\frac{x-1}{x+1}$ then show that $f\left(\frac{1}{x}\right)=-f(x)$ and $f\left(-\frac{1}{x}\right)=\frac{-1}{f(x)}$

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54. If $f(x)=x^{2}-3 x+1$ find $x \in R$ such that $f(2 x)=f(x)$.
55. If $f(x)=x^{2}-3 x+1$ find $x \in R$ such that $f(2 x)=2 f(x)$

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56. Determine whether the functions are even or odd $f(x)=|-x|$

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57. Determine whether the functions are even or odd $f(x)=|x-2|$

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58. Determine whether the functions are even or odd if $f(x)=x^{2}+k x+1$ for all x and f is an even function then find k

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59. Let $f: N \rightarrow N: f(x)=2 x, g: N \rightarrow N: g(y)=3 y+4$ and $h: N \rightarrow N: h(z)=\sin z$

Show that $h \circ(g \circ f)=(h \circ g) \circ f$.

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60. Find $g o f$ and $f o g$ if $f(x)=|x|$ and $g(x)=|3-2 x|$

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61. Find $g o f$ and $f o g$ if $f(x)=8 x^{3}$ and $g(x)=x^{\frac{1}{3}}$

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62. What is the maximum number of points in which a vertical line can meet the graph of real valued function?

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63. Fid the domain for which the functions
$f(x)=2 x^{2}-1 \operatorname{andg}(x)=1-3 x$ are equal.

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64. Write the range of the function $f(x)=-x^{2}, x \in R$

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65. Write the domain and range of the signum function,
66. Is the function $f(x)=x^{3 n}, n \in N$ even?

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67. Write the range of the function $f(x)=x^{2}+1, x \in R$

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68. Write the domain and range of the function $f(x)=[x]$

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69. If $f(x)=4 x-x^{2}$ then find $\mathrm{f}(\mathrm{a}+1)-\mathrm{f}(\mathrm{a}-1)$

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70. If A and B are finite sets with $\mathrm{n}(\mathrm{A})=3$ and $\mathrm{N}(\mathrm{B})=6$ then find $n(A \times B)$

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71. Is the function $f: R \rightarrow R$ be defined by $\mathrm{f}(\mathrm{x})=2 \mathrm{x}+3$ a one on one function?

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72. Find the range of the function $f(x)=\frac{|x-a|}{x-a}, x$ is not equal to a

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73. Find the domain of the function $f(x)=\frac{x}{x^{2}+5 x+6}$

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74. Find the range of the function $f(x)=-x^{2}-100$

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75. Is the function $f(x)=|x|$ one on one?

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76. Show that the function $f: R \rightarrow R$ defined by $f(x)=x^{2}$ is neither one-one nor onto.

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77. If R denotes the set of all real numbers, then the function $f: R \rightarrow R$ defined by $f(x)=[x]$ is

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78. A horizontal line meets the graph of the function $\mathrm{y}=\mathrm{f}(\mathrm{x})$ in two points is fone one?
79. If $t(C)=\frac{9 C}{5}+32$ write the value of $\mathrm{t}(28)$

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80. Find the range of the function $f(x)=[x], 1 \leq x<3$

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81. Find the total number of function from a set $A$ to $B$ where $n(A)=3$ and $\mathrm{n}(\mathrm{B})=4$

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82. Find the period of the function $f(x)=\sin 5 x$
83. If $(x+y, x-y)=(1,2)$ find $x$ and $y$

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84. Find the domain and range of the following relation $R=\{(1,3),(1,5),(1,7),(1,9)\}$

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85. Find the domain and range of the following relation $R=\{(x, y): x \in N, x<6$ and $y=4\}$

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86. Find the domain and range of the following relation $R=\{(x+2, x+4): x \in\{0,1,2,3,4,5\}\}$
87. which of the following relations are functions from $A=\{1,3,5,7,9\}$ to $B=$ $\{1,2,3,4,5\} f=\{(3,2),(1,5),(5,1),(7,4),(9,5)\}$

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88. which of the following relations are functions from $A=\{1,3,5,7,9\}$ to $B=$ $\{1,2,3,4,5\} f=\{(1,3),(3,1),(5,3),(5,5),(1,4)\}$

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89. If $f: R \rightarrow R$ defined by $f(x)=x^{2}-2 x+3$, then find $f(f(x))$.

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90. Find the domain and range of the following $f(x)=\frac{1}{2 x-1}$
91. Find the domain and range of the following $f(x)=\frac{3}{2-x^{2}}$

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92. Find the domain and range of the following $f(x)=1+3 \cos 2 x$

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93. Find the domain and range of the following $f(x)=\frac{1}{x^{2}-1}$

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94. Find the domain and range of the following $f(x)=\frac{1}{\sqrt{1-\cos x}}$

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95. Which of the following functions are even and which odd? $f(x)=x^{4}+x^{2}$

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96. Which of the following functions are even and which odd?
$f(x)=x^{3}+x$

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97. which of the following functions are even and which odd?
$f(x)=x^{3}+x$

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98. if $f(x)=\frac{1}{1-x}$ then find $f\left(\frac{x-1}{x}\right)$
99. If $f: R \div R$ be defined by $f(x)=\left(3-x^{3}\right)^{1 / 3}$, then find $f o f(x)$

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100. If f and g are two functions defined by $f(x)=\sqrt{x+1}$ and $g(x)=\frac{1}{x}$ then find the following functions: $\mathrm{f}+\mathrm{g}$

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101. If f and g are two functions defined by $f(x)=\sqrt{x+1}$ and $g(x)=\frac{1}{x}$ then find the following functions: $\mathrm{f}-\mathrm{g}$

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102. If f and g are two functions defined by $f(x)=\sqrt{x+1}$ and $g(x)=\frac{1}{x}$ then find the following functions: fg
103. If f and g are two functions defined by $f(x)=\sqrt{x+1}$ and $g(x)=\frac{1}{x}$ then find the following functions: $\frac{f}{g}$

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104. If f and g are two functions defined by $f(x)=\sqrt{x+1}$ and $g(x)=\frac{1}{x}$ then find the following functions: $2 f-3 \mathrm{~g}$

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105. If f and g are two functions defined by $f(x)=\sqrt{x+1}$ and $g(x)=\frac{1}{x}$ then find the following functions: $2 f^{2}+\sqrt{2} g$

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106. Draw the graph of the following functions and hence find the range of $f(x)=1-x$

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107. Draw the graph of the following functions and hence find its ranges
$f(x)=2 x^{2}$

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108. Draw the graph of the following functions and hence find its ranges :
$f(x)=1-x$

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109. Draw the graph of the following functions and hence find its ranges:
$\mathrm{f}(\mathrm{x})=2 x^{3}$
110. Check the injectivity and surjectivity of the following functions $f: Z \rightarrow Z$ defined by $f(x)=x^{2}$

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111. Check the injectivity and surjectivity of the following functions $f: R \rightarrow R$ defined by $\mathrm{f}(\mathrm{x})=3 \mathrm{x}+10$

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112. Check the injectivity and surjectivity of the following functions
$f: R-\left\{\left(-\frac{4}{3}\right) \rightarrow R\right.$ defined by $f(x)=4 \frac{x}{3 x+4}$

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113. Check the injectivity and surjectivity of the following functions $f: R \rightarrow[5, \infty)$ defined by $f(x)=9 x^{2}+6 x-5$

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114. If $f: R-\left\{\frac{2}{3}\right\} \rightarrow R$ defined by $f(x)=\frac{4 x+3}{6 x-4}$ show that $f(f(x))=x$

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115. Show that the function $f: R \rightarrow R$ defined by $f(x)=x^{4}+5$ is neither one one nor onto

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