



## MATHS

### BOOKS - MAHAVEER PUBLICATION

### METHODS OF INTEGRATION

Question Bank

1. Evaluate  $\int(x + 1)(2x - 1)^{\frac{5}{2}} dx$



Watch Video Solution

2. Evaluate  $\int \frac{x + 2}{(x^2 + 4x + 5)^2} dx$



**Watch Video Solution**

3. Evaluate:  $\int \frac{\sin x + \cos x}{\sin x - \cos x} dx$



**Watch Video Solution**

4.  $\int \frac{\cos x}{1 + \sin^2 x} dx$



**Watch Video Solution**

5. Evaluate  $\int \frac{x^3}{1 + x^8} dx$



**Watch Video Solution**

6. Evaluate:  $\int x \sqrt{x^2 + 1} dx.$



**Watch Video Solution**

7. Evaluate  $\int \frac{dx}{\sqrt{2x + 1}}$



**Watch Video Solution**

8. Evaluate  $\int \frac{\sin(\log x)}{x} dx$



**Watch Video Solution**

9.  $\int \frac{\sin^{-1} x}{\sqrt{1 - x^2}} dx.$



**Watch Video Solution**

10. Evaluate:  $\int \frac{e^{2x}}{1 + e^x} dx$



**Watch Video Solution**

11. Evaluate  $\int \frac{dx}{e^{-x} + 1}$



Watch Video Solution

12.  $\int \frac{dx}{e^x + e^{-x}}$



Watch Video Solution

13. Evaluate:  $\int \frac{e^x - e^{-x}}{e^x + e^{-x}} dx$



Watch Video Solution

14. Evaluate  $\int \frac{dx}{x \left\{ 1 + (\log x)^2 \right\}}$



Watch Video Solution

15. Evaluate  $\int \log x dx$



Watch Video Solution

16. Evaluate  $\int x e^x dx$



Watch Video Solution

17. Evaluate  $\int x \cos x dx$ .



**Watch Video Solution**

18. Evaluate  $\int x \sec^2 x dx$



**Watch Video Solution**

19. Evaluate:  $\int x^2 \sin x dx$



**Watch Video Solution**

$$20. \text{ Evaluate } \int x \tan^{-1} x dx$$



**Watch Video Solution**

$$21. \int \frac{x^2 \tan^{-1} x}{1 + x^2} dx$$



**Watch Video Solution**

$$22. \int \frac{x + \sin x}{1 + \cos x} dx$$



**Watch Video Solution**

23.  $\int \frac{\log x}{(1+x)^2} dx$



Watch Video Solution

24. Evaluate  $\int \left( \frac{e^{\tan^{-1} x}}{1+x^2} + x^2 e^x \right) dx$



Watch Video Solution

25.  $\int e^x (\cos x + \sin x) dx$



Watch Video Solution

**26.** Evaluate  $\int e^x \left( \frac{1}{\log x} - \frac{1}{x(\log x)^2} \right) dx$



**Watch Video Solution**

**27.** Evaluate  $\int e^x \left( \frac{1}{x+1} - \frac{1}{(x+1)^2} \right) dx$



**Watch Video Solution**

**28.**  $\int \frac{dx}{x^2 - 9}$



**Watch Video Solution**

**29.** Find the integral of the following integral

$$\int \frac{dx}{\sqrt{9x^2 + 1}}$$



**Watch Video Solution**

**30.** Find the integral of the following integral

$$\int \frac{3x dx}{2x^4 + 1}$$



**Watch Video Solution**

31. Evaluate  $\int \frac{\cos x}{\sqrt{25 - \sin^2 x}} dx$



Watch Video Solution

32.  $\int \frac{dx}{\sqrt{1 - x - x^2}}$



Watch Video Solution

33. Evaluate:  $\int \frac{dx}{\sqrt{x^2 + 2x + 2}}$



Watch Video Solution

**34. Integrate the Following Integral**

$$\int \frac{2x - 3}{\sqrt{2x^2 - 6x + 1}} dx$$



**Watch Video Solution**

**35. Integrate the Following Integral**

$$\int \frac{2x + 3}{\sqrt{x^2 + 2x + 10}} dx$$



**Watch Video Solution**

**36. Evaluate  $\int \sqrt{x^2 + 16} dx$**



Watch Video Solution

37. Evaluate  $\int \sqrt{49 - 16x^2} dx$



Watch Video Solution

38. Evaluate  $\int \sqrt{x^2 + 2x - 3} dx$



Watch Video Solution

39. Evaluate  $\int \sqrt{8 - 2x - x^2} dx$



**Watch Video Solution**

**40.** Evaluate  $\int \frac{x^2}{(x^2 - 4)} dx$



**Watch Video Solution**

**41.** Evaluate  $\int \frac{x - 1}{(x - 2)(x - 3)} dx$



**Watch Video Solution**

**42.** Evaluate  $\int 3 \frac{x}{x^2 - x - 2} dx$



Watch Video Solution

43. Evaluate  $\int \frac{x^2}{(x + 1)(x + 2)} dx$



Watch Video Solution

44.  $\int \frac{1}{1 + 3e^x + 2e^{2x}} dx$



Watch Video Solution

**45.** Choose the correct answer of the given question

$$\int \frac{1}{1 + \tan x} dx = \underline{\quad} + c$$

A.  $\log |\sec x - \tan x|$

B.  $2 \frac{\sec^2 x}{2}$

C.  $\log|x + \sin x|$

D.  $\frac{1}{2}[x + \log|\sin x + \cos x|]$

**Answer:** D



**Watch Video Solution**

**46.** Choose the correct answer of the given question

$$\int \frac{e^x + 1}{e^x - 1} dx = \underline{\quad} + c$$

A.  $2 \log \left| e^{\frac{x}{2}} - e^{-\frac{x}{2}} \right|$

B.  $2 \log \left| e^{\frac{x}{2}} + e^{-\frac{x}{2}} \right|$

C.  $2 \log |e^x - 1| - x$

D.  $2 \log |e^x + 1|$

**Answer: C**



**Watch Video Solution**

**47.** Choose the correct answer of the given question

$$\int \frac{1}{x(\log x)^n} dx = \underline{\hspace{2cm}} + c$$

A.  $\frac{(\log x)^{1-n}}{1-n}$

B.  $\frac{(\log x)^{1+n}}{1+n}$

C.  $\frac{(\log x)^n}{n}$

D.  $\frac{\log x}{1-n}$

**Answer:** A



Watch Video Solution

48.  $\int \frac{\cos \sqrt{x}}{\sqrt{x}} dx$

A.  $2 \cos \sqrt{x} + c$

B.  $\sqrt{\frac{\cos x}{x}} + c$

C.  $\sin \sqrt{x} + c$

D.  $2 \sin \sqrt{x} + c$

**Answer:** D



Watch Video Solution

**49.** Choose the correct answer of the given question

$$\int \sqrt{\frac{1-x}{x}} dx = \underline{\quad} + c$$

A.  $\sqrt{1-x^2} + \frac{1}{2}\sin^{-1}(2x+3)^{\frac{3}{2}}$

B.  $\sqrt{x-x^2} - \frac{1}{2}\sin^{-1}(2x+3)^{\frac{3}{2}}$

C.  $\sqrt{x-x^2} + \frac{1}{2}\sin^{-1}(2x+3)^{\frac{3}{2}}$

D.  $\sqrt{x-1} + \frac{1}{2}\sin^{-1}(2x+3)^{\frac{3}{2}}$

**Answer: C**



**View Text Solution**

**50.** Choose the correct answer of the given question

$$\int 2^x dx = \underline{\quad} + c$$

A.  $2^x \log 2$

B.  $\frac{2^x}{\log 2}$

C.  $2^x \log x$

D.  $2 \log x$

**Answer:** B



**Watch Video Solution**

**51. Choose the correct answer of the given question**

$$\int e^{\sqrt{x}} dx = \underline{\quad} + c$$

A.  $2e^{\sqrt{x}}(\sqrt{x} - 1)$

B.  $e^{\sqrt{x}}(\sqrt{x} - 1)$

C.  $2e^{\sqrt{x}}(\sqrt{x} + 1)$

D.  $2e^{\sqrt{x}}(x - 1)$

**Answer: A**



**Watch Video Solution**

**52.** Choose the correct answer of the given question

$$\int \sqrt{\frac{1 - \cos x}{2}} dx$$

A.  $-2 \cos\left(\frac{x}{2}\right) + c$

B.  $e^{\sqrt{x}} \cos x + c$

C.  $2 \sin x + c$

D.  $\sqrt{2} \sin x + c$

**Answer:** D



Watch Video Solution

**53.**  $\int(x - 1)e^{-x}dx =$

A.  $e^{-x} + c$

B.  $-xe^x + c$

C.  $-xe^{-x} + c$

D.  $1 - xe^x + c$

**Answer:** B



**Watch Video Solution**

**54.**  $\int \frac{1}{2 + \cos x} dx$

A.  $\frac{1}{3} \tan^{-1}\left(\frac{1}{\sqrt{3}} \tan\left(\frac{x}{2}\right)\right) + c$

B.  $\frac{1}{\sqrt{3}} \tan^{-1}\left(\frac{1}{\sqrt{3}} \tan\left(\frac{x}{2}\right)\right) + c$

C.  $\frac{4}{\sqrt{3}} \tan^{-1}\left(\frac{1}{\sqrt{3}} \tan\left(\frac{x}{2}\right)\right) + c$

D.  $\frac{2}{\sqrt{3}} \tan^{-1}\left(\tan\left(\frac{x}{2}\right)\right) + c$

**Answer:** B



**Watch Video Solution**

**55.** Evaluate:  $\int \frac{1}{e^x + e^{-x}} dx$

A.  $\tan^{-1}(e^{-x}) + c$

B.  $\tan^{-1}(e^x) + c$

C.  $\tan^{-1} x + c$

D.  $1 + e^x + c$

**Answer:** A



**Watch Video Solution**

**56.** Choose the correct answer of the given question

$$\int \frac{dx}{1+x^2} = - - + c$$

A.  $\tan^{-1} x$

B.  $\sin^{-1} x$

C.  $\cos^{-1} x$

D.  $\cot^{-1} x$

**Answer:** A



**Watch Video Solution**

57.  $\int \frac{\sin x}{(1 + \sin x)} dx = ?$

A.  $x + \tan x + \sec x + C$

B.  $x - \tan x + C$

C.  $x + \sec x + C$

D.  $x - \tan x + \sec x + C$

**Answer: D**



**Watch Video Solution**

**58.** Choose the correct answer of the given question

$$\int \frac{1 - x^4}{1 - x} dx = \underline{\quad} + c$$

A.  $\frac{x^2}{2} + \frac{x^3}{3}$

B.  $x + \frac{x^2}{2} + \frac{x^3}{3} + \frac{x^4}{4}$

C.  $\frac{x^2}{2} + \frac{x^3}{3} + \frac{x^4}{4}$

D.  $\frac{x^2}{2} + \frac{x^4}{4}$

**Answer: C**



**Watch Video Solution**

**59.** Evaluate  $\int \frac{dx}{x + x \log x}$

A.  $1 + \log x$

B.  $x + \log x$

C.  $\log(1 + \log x) + c$

D.  $x \log(1 + \log x) + c$

**Answer:** C



**Watch Video Solution**

$$60. \int e^x [f(x) + f'(x)] dx =$$

A.  $e^x f(x) + c$

B.  $\frac{e^x}{f(x)} + c$

C.  $e^x + f(x) + c$

D.  $e^x + c$

**Answer: A**



**Watch Video Solution**

$$61. \int \frac{e^x(1 - \sin x)}{1 - \cos x} dx$$

A.  $e^x \frac{\tan x}{2} + c$

B.  $-e^x \frac{\cot x}{2} + c$

C.  $-e^x \frac{\tan x}{2} + c$

D.  $e^x \frac{\cot x}{2} + c$

**Answer: B**



**Watch Video Solution**

**62.** Choose the correct answer of the given question

$$\int e^x \left( \frac{1}{x} - \frac{1}{x^2} \right) dx =$$

A.  $e^x \left( \frac{1}{x^2} \right) + c$

B.  $e^x + c$

C.  $e^x \left( \frac{1}{x} \right) + c$

D.  $-e^x + c$

**Answer:** C



**Watch Video Solution**

$$63. \int \frac{e^{\tan^{-1} x}}{1+x^2} dx$$

A. 0

B.  $-e^{\tan^{-1} x} + c$

C.  $\tan^{-1} x + c$

D.  $e^{\tan^{-1} x} + c$

**Answer: D**



**Watch Video Solution**

**64.** Choose the correct answer of the given question

$$\int \frac{2}{1 - \cos 2x} dx =$$

A.  $-\cot x + c$

B.  $\cot x + c$

C.  $-\tan x + c$

D.  $\tan x + c$

**Answer:** A



**Watch Video Solution**

65. Find the following integral (using Substitution method)

$$\int x^2 \sqrt{1 + x^2} dx$$



[View Text Solution](#)

66. Find the following integral (using Substitution method)

$$\int (2x + 5) \sqrt{x^2 + 5x} dx$$



[Watch Video Solution](#)

**67.** Find the following integral

$$\int \frac{x^3}{1+x^3} dx$$



**Watch Video Solution**

**68.** Find the following integral (using Substitution method)

$$\int \frac{dx}{x(\log x)^2}$$



**Watch Video Solution**

**69.** Find the following integral (using Substitution method)

$$\int \frac{x^3}{\sqrt{x^2 + 1}} dx$$



**Watch Video Solution**

$$70. \int \frac{e^x - 1}{e^x + 1} dx$$



**Watch Video Solution**

71. Find the following integral (using Substitution method)

$$\int \frac{e^x + e^{-x}}{e^x - e^{-x}} dx$$



**Watch Video Solution**

72. Find the following integral (using Substitution method)

$$\int \frac{dx}{x \log x}$$



**Watch Video Solution**

73. Find the following integral (using Substitution method)

$$\int x(3x^2 + 7)^7 dx$$



**Watch Video Solution**

74. Find the following integral (using Substitution method)

$$\int (3x^2 - 5x + 7)^m (6x - 5) dx$$



**Watch Video Solution**

**75.** Evaluate the following integrals:

$$\int x \cos 2x dx$$



**Watch Video Solution**

**76.** Integrate the following :

$$\int x \sin x dx.$$



**Watch Video Solution**

**77.**  $\int x \sin^2 x dx$



**Watch Video Solution**

$$78. \int x \sin^{-1} x \, dx$$



**Watch Video Solution**

79. Find the following integral (using  
Integration by parts method)

$$\int x \sec^{-1} x \, dx$$



**Watch Video Solution**

$$80. \int x^2 \log x dx.$$



**Watch Video Solution**

$$81. \int x^2 \tan^{-1} x dx$$



**Watch Video Solution**

$$82. \int \tan^{-1} x dx$$



**Watch Video Solution**

$$83. \int \frac{\sin^{-1} x}{x^2} dx$$



**Watch Video Solution**

84. Find the following integral (using  
Integration by parts method)

$$\int x^3 e^x dx$$



**Watch Video Solution**

**85.** Find the following integral (using partial fraction method)

$$\int \frac{2x + 1}{(x - 1)(x + 2)(x - 3)} dx$$



**Watch Video Solution**

**86.** Find the following integral (using partial fraction method)

$$\int \frac{x^2 + 1}{(x - 1)^2(x + 3)} dx$$



**Watch Video Solution**

**87.** Find the following integral (using partial fraction method)

$$\int \frac{2x + 1}{(x + 1)(x - 2)} dx$$



**Watch Video Solution**

**88.** Evaluate:  $\int \frac{x}{(x + 1)(x^2 + 1)} dx$



**Watch Video Solution**

**89.** Find the following integral (using partial fraction method)

$$\int \frac{dx}{x(x^2 + 8)}$$



**Watch Video Solution**

**90.**  $\int \frac{dx}{x^4 - 1}$



**Watch Video Solution**

**91.** Find the following integral (using partial fraction method)

$$\int \frac{3x}{(x - 1)(x - 2)} dx$$



**Watch Video Solution**

**92.** Evaluate the following Integrals :

$$\int \frac{dx}{x(x^n + 1)}$$



**Watch Video Solution**

**93.** Find the following integral (using partial fraction method)

$$\int \frac{3x - 1}{(x + 2)^3} dx$$



**Watch Video Solution**

**94.**  $\int \frac{x^3 + x + 1}{x^2 - 1} dx$



**Watch Video Solution**

**95.** Evaluate  $\int \frac{1}{x^2 + 4x + 8} dx$



Watch Video Solution

$$96. \int \frac{1}{3x^2 + 13x - 10} dx$$



Watch Video Solution

$$97. \text{ Evaluate: } \int \frac{x}{x^4 - x^2 + 1} dx$$



Watch Video Solution

$$98. \int \frac{1}{x^2 - 5x + 6} dx$$



Watch Video Solution

$$99. \int \frac{dx}{\sqrt{(x-1)(x-2)}}$$



Watch Video Solution

100. Evaluate

$$\int \frac{1}{\sqrt{9 + 8x - 4x^2}} dx$$



Watch Video Solution

$$101. \int \frac{x + 2}{\sqrt{x^2 + 5x + 6}} dx$$



**Watch Video Solution**

$$102. \text{ Evaluate: } \int \frac{5x + 3}{\sqrt{x^2 + 4x + 10}} dx$$



**Watch Video Solution**

$$103. \int \sqrt{4x^2 + 9} dx$$



**Watch Video Solution**

$$104. \int \sqrt{8 + 2x - x^2} dx$$



Watch Video Solution

105. Evaluate

$$\int \sqrt{9x^2 + 4} dx$$



Watch Video Solution

106. Evaluate

$$\int \sqrt{5 - 2x - x^2} dx$$



Watch Video Solution