



## MATHS

### BOOKS - MODERN PUBLICATION

### CONTINUITY AND DIFFERENTIABILITY

#### Example

1. Prove that :

every constant function is continuous in  $\mathbb{R}$



[Watch Video Solution](#)

2. Prove that :

the identity function is continuous in  $\mathbb{R}$ .



[Watch Video Solution](#)

3. Discuss the continuity of the function  $f$  given by  $f(x) = |x|$  at  $x = 0$



[Watch Video Solution](#)

4. Show that the function 'f' given by:

$$f(x) = \begin{cases} x & \text{if } x \geq 1 \\ x^2 & \text{if } x < 1 \end{cases} \text{ is continuous every where on } \mathbb{R}.$$



[Watch Video Solution](#)

5. Prove that the greatest integer function  $[x]$  is continuous at all points except at integral points.



[Watch Video Solution](#)

6. Show that  $f(x) = 2x - |x|$  is continuous at  $x = 0$

 [Watch Video Solution](#)

7. Test the continuity of the function  $f(x)$  at the origin:

$$f(x) = \begin{cases} (|x|/x, x \text{ not equals to } 0) \\ (0, x=0) \end{cases}$$

 [Watch Video Solution](#)

8. Find all the points of discontinuity of the function  $f$  defined by

$$f(x) = \begin{cases} x + 2 & \text{if } x < 1 \\ 0 & \text{if } x = 1 \\ x - 2 & \text{if } x > 1 \end{cases}$$

 [Watch Video Solution](#)

9. Show that the function  $f(x) = \begin{cases} |x| & x \leq 2 \\ [x] & x > 2 \end{cases}$  is continuous on  $[0, 2]$

 [Watch Video Solution](#)

10. Find  $a$  for which the function  $f$  defined as

$$f(x) = \left\{ \left[ \left( a \sin \left( \frac{\pi}{2} \right) (x + 1) \right) \text{ if } x \leq 0 \right], \left[ \left( \frac{\tan x - \sin x}{x^3} \right) \text{ if } x > 0 \right] \right\}$$

is continuous at  $(x = 0)$ .

 [Watch Video Solution](#)

11. For what value of  $k$ , function  $f(x)$  is continuous at  $x = 0$  where

$$f(x) = \begin{cases} \frac{1 - \cos 4x}{8x^2}, & (x \neq 0) \\ k, & (x = 0) \end{cases}$$



 [Watch Video Solution](#)

12. For what value of 'a' and 'b', the function 'f' defined as:

$$f(x) = \begin{cases} 3ax + b & \text{if } x < 1 \\ 11 & \text{if } x = 1 \\ 5ax - 2b & \text{if } x > 1 \end{cases} \text{ is continuous at } x=1$$

 [Watch Video Solution](#)

13. Find the value of 'k', for which:

$$f(x) = \begin{cases} \frac{\sqrt{1+kx} - \sqrt{1-kx}}{x}, & \text{if } -1 \leq x < 0 \\ \left( \frac{2x+1}{x-1}, & \text{if } 0 \leq x < 1 \end{cases}$$

is continuous at  $x=0$

 [Watch Video Solution](#)

14.

If

$$f(x) = \begin{cases} \left( \left( \frac{\sin(a+1)x + 2\sin x}{x} \right)^2, & x < 0 \right) \\ 2, & x = 0 \\ \left( \frac{\sqrt{1+bx} - 1}{x}, & x > 0 \right) \end{cases}$$

is continuous at  $x = 0$ , then find the values of  $a$  and  $b$ .

 [Watch Video Solution](#)

15. Show that the following function is continuous at  $x = 0$ :

$$f(x) = x \sin \frac{1}{x}, \text{ when } x \neq 0 \quad f(0) = 0.$$

 [Watch Video Solution](#)

16. Show that the function  $f$  defined by  $f(x) = |1 - x + |x||$  where  $x$  is any real number, is a continuous function.

 [Watch Video Solution](#)

17. Is  $f(x) = |x-1|+|x-2|$  differentiable at  $x=2$ ?

 [Watch Video Solution](#)

18. For what values of 'a' and 'b' , the function:

$$f(x) = \begin{cases} x^2 & \text{if } x \leq 2 \\ ax + b & \text{if } x > 2 \end{cases} \text{ is derivable at } x=2?$$

 [Watch Video Solution](#)

19. If 'f' is derivable at  $x = a$ , find  $\lim_{x \rightarrow a} \frac{xf(a) - af(x)}{x - a}$

 [Watch Video Solution](#)

20. Examine the derivability of:

$$f(x) = \begin{cases} x^2 \sin\left(\frac{1}{x}\right) & x \neq 0 \\ 0 & x = 0 \end{cases} \text{ at } x=0$$

 [Watch Video Solution](#)

21. Find  $\frac{dy}{dx}$  if  $ax + by^2 = \cos y$

 [Watch Video Solution](#)

22. Use chain rule to find  $\frac{dy}{dx}$  if  $y = \left(\frac{2x-1}{2x+1}\right)^2$

 [Watch Video Solution](#)

23. Differentiate  $\cos^2(\sqrt{x})$  w.r.t  $x$ .



Watch Video Solution

24. Differentiate  $\sin(\cos(x^2))$  with respect to  $x$ .



Watch Video Solution

25. if  $y = \sqrt{\frac{1-x}{1+x}}$ , prove that :  $(1-x)^2 \left(\frac{dy}{dx}\right) + y = 0$



Watch Video Solution

26. If  $y = \left(x + \sqrt{x^2 + a^2}\right)^n$ , prove that  $\frac{dy}{dx} = \frac{ny}{\sqrt{x^2 + a^2}}$ .



Watch Video Solution

27. Find  $\frac{dy}{dx}$  in the following:  $2x + 3y = \sin x$

 [Watch Video Solution](#)

28. Find  $\frac{dy}{dx}$ , if  $y + \sin y = \cos x$

 [Watch Video Solution](#)

29. If  $x \sin (a+y) + \sin a \cos (a+y) = 0$ , then prove that :

$$\frac{dy}{dx} = \frac{\sin^2(a+y)}{\sin a}$$

 [Watch Video Solution](#)

30. If  $x^2 + y^2 = 1$ , then

 [Watch Video Solution](#)

31. Differentiate  $\sin^{-1}(\sqrt{\cos x})$  w.r.t.  $x$ , using chain rule.

 [Watch Video Solution](#)

32. If  $y = \sqrt{\cot^{-1}\sqrt{x}}$ , find  $\frac{dy}{dx}$

 [Watch Video Solution](#)

33. If  $y = \sin(2\sin^{-1}x)$ , show that:  $\frac{dy}{dx} = 2\sqrt{\frac{1-y^2}{1-x^2}}$

 [Watch Video Solution](#)

34. If  $y = \sec^{-1}\left(\frac{1}{2x^2 - 1}\right)$ , then find  $\frac{dy}{dx}$ , given  $0 < x < \frac{1}{\sqrt{2}}$

 [Watch Video Solution](#)

35. If  $y = \sin^{-1} \left[ x\sqrt{1-x} - \sqrt{x} \left( \sqrt{1-x^2} \right) \right]$  find  $\frac{dy}{dx}$

 [Watch Video Solution](#)

36. Find  $\frac{dy}{dx}$  if  $y = \sin^{-1} \left[ \frac{6x - 4\sqrt{1-4x^2}}{5} \right]$

 [Watch Video Solution](#)

37. Prove that :  $\frac{d}{dx} \left[ \frac{x}{2} \sqrt{a^2 - x^2} + \frac{a^2}{2} \sin^{-1} \left( \frac{x}{a} \right) \right] = \sqrt{a^2 - x^2}$

 [Watch Video Solution](#)



38. Prove that:  $\frac{d}{dx} \left[ \sin^{-1} \sqrt{x} \right] = \frac{1}{2\sqrt{x-x^2}}$

 [Watch Video Solution](#)

39. Is it true that  $x = e^{\log x}$  for all real  $x$ ?

 [Watch Video Solution](#)

40. Differentiate the following w.r.t.x:  $3^{x+2}$

 [Watch Video Solution](#)

41. Differentiate  $10^x \cdot x^{10}$  w.r.t.x

 [Watch Video Solution](#)

42. If  $xy = e^{x-y}$ , prove that  $\frac{dy}{dx} = \frac{y(x-1)}{x(y+1)}$

 [Watch Video Solution](#)

43. Differentiate  $\sin^{-1}\left(\frac{2^{x+1}}{1+4^x}\right)$  w.r.t  $x$

 [Watch Video Solution](#)

44. Differentiate the following with respect to  $x$ :

$$\sin^{-1}\left[\frac{2^{x+1} \cdot 3^x}{1+(36)^x}\right]$$

 [Watch Video Solution](#)

45. Find  $\frac{dy}{dx}$ , if :

$$y = \log\left((x + 2) + \sqrt{x^2 + 2}\right)$$

 [Watch Video Solution](#)

46. If  $y = \log_{\tan(\pi/4 + x/2)}$ , show that  $\frac{dy}{dx} - \sec x = 0$

 [Watch Video Solution](#)

47. If  $y = \log_{10}x + \log_x 10 + \log_x X + \log_{10} 10$ ,  $f \in d \frac{dy}{dx}$

 [Watch Video Solution](#)

48. Find  $f'(x)$ , where:  $f(x) = (1 + x^2)I_n(2x)$

 [Watch Video Solution](#)

49. Find  $f'(x)$ , where:  $f(x) = \cos(\log x)^2$  where  $x > 0$

 [Watch Video Solution](#)

50. If  $e^x + e^y = e^{x+y}$ , prove that  $\frac{dy}{dx} = \frac{e^x(e^y - 1)}{e^y(e^x - 1)}$

 [Watch Video Solution](#)

51. Find the derivative of  $\sin(\log x)$  ( $x > 0$ ) w.r.t.  $x$  by Chain Rule

 [Watch Video Solution](#)

52. Find the derivative of  $\sin(\log x)$  ( $x > 0$ ) w.r.t.  $x$



 Watch Video Solution

53. Find  $\frac{dy}{dx}$ , when:  $x = a \frac{1-t^2}{1+t^2}$ ,  $y = b \frac{2t}{1+t^2}$ .

 Watch Video Solution

54. Find  $\frac{dy}{dx}$ , when:  $x = a(1 - \cos\theta)$ ,  $y = a(\theta + \sin\theta)$

 Watch Video Solution

55. Find  $\frac{dy}{dx}$  if  $x^{\frac{2}{3}} + y^{\frac{2}{3}} = a^{\frac{2}{3}}$

 Watch Video Solution

56. Find  $\frac{dy}{dx}$ , when:  $x = e^{\theta} \left( \theta + \frac{1}{\theta} \right)$  and  $y = e^{-\theta} \left( \theta - \frac{1}{\theta} \right)$

 [Watch Video Solution](#)

57. Find the value of  $\frac{dy}{dx}$  at  $\theta = \frac{\pi}{4}$ , if:  $x = a\cos(\theta)(\sin\theta - \cos\theta)$  and  $y = ae^{\theta}(\sin\theta + \cos\theta)$

 [Watch Video Solution](#)

58. If  $x = a \sin 2t(1 + \cos 2t)$  and  $y = b \cos 2t(1 - \cos 2t)$ , find: the value of  $\frac{dy}{dx}$  at  $t = \frac{\pi}{3}$

 [Watch Video Solution](#)

59. Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = at^2, y = 2at$$

 [Watch Video Solution](#)

60. Differentiate  $\log(1 + \theta)$  w. r. t.  $\sin^{-1}\theta$ .

 [Watch Video Solution](#)

61. Differentiate  $\sin^{-1}\left(\frac{x}{\sqrt{1+x^2}}\right)$  w.r.t.  $\tan^{-1}x$ .

 [Watch Video Solution](#)

62. Differentiate  $\sin^{-1}\left(\frac{x}{\sqrt{1+x^2}}\right)$  w. r. t.  $\cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$

 [Watch Video Solution](#)

63. Differentiate the following w.r.t. as indicated:

$$x^2 \text{ w. r. t. } x^3$$



Watch Video Solution

64. Differentiate the following w.r.t. as indicated:

$$\frac{ax + b}{cx + d} \text{ w. r. t. } \frac{a'x + b'}{c'x + d'}$$



Watch Video Solution

65. Differentiate the following w.r.t. as indicated:

$$e^{2x} \text{ w. r. t. } te^x$$



Watch Video Solution



**66.** Differentiate the following w.r.t. as indicated:

$$\frac{x^2}{1+x^2} \text{ w. r. t. } tx^2$$

 [Watch Video Solution](#)

**67.** Differentiate the following w.r.t. as indicated:

$$(x^{-1})^{4/5} \text{ w. r. t. } |x|.$$

 [Watch Video Solution](#)

**68.** Differentiate the following w.r.t. as indicated:

$$\cos^{-1}\theta, \text{ w. r. t. } \log(1 + \theta)$$

 [Watch Video Solution](#)

**69.** Differentiate the following w.r.t. as indicated:

$\sin^{-1}\theta$ , w. r. t.  $\log(1 + \theta)$

 [Watch Video Solution](#)

**70.** Differentiate the following w.r.t. as indicated:

$\tan x$ , w. r. t.  $\cos x$

 [Watch Video Solution](#)

**71.** Differentiate the following w.r.t. as indicated:

$\sec x$  w. r. t.  $\operatorname{cosec} x$

 [Watch Video Solution](#)

72. Differentiate the following w.r.t. as indicated:

$$\sin^2 x \text{ w.r.t. } e^{\cos x}$$

 [Watch Video Solution](#)

73. Differentiate  $\cos^{-1}\left(\frac{1}{\sqrt{1+x^2}}\right)$  w.r.t.  $\tan^{-1}x$ .

 [Watch Video Solution](#)

74. Differentiate the following w.r.t. as indicated:

$$\sin^{-1}\left(2\frac{x}{1+x^2}\right) \text{ w.r.t. } \tan^{-1}x$$

 [Watch Video Solution](#)

75. Differentiate the following w.r.t. as indicated:

$$\sin^{-1}\left(2\frac{x}{1+x^2}\right) \text{ w. r. t. } \tan^{-1}\left(2\frac{x}{1-x^2}\right)$$

 [Watch Video Solution](#)

76. Differentiate the following w.r.t. as indicated:

$$\frac{\tan^{-1}(3x - x^3)}{1 - 3x^2} \text{ w. r. t. } \tan^{-1}\left(2\frac{x}{1+x^2}\right)$$

 [Watch Video Solution](#)

77. Differentiate  $\cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$  w.r.t.  $\tan^{-1}\left(\frac{3x-x^3}{1-3x^2}\right)$

 [Watch Video Solution](#)

78. Differentiate the following w.r.t. as indicated:

$$\tan^{-1}\left(\frac{3x - x^3}{1 - 3x^2}\right) \text{ w. r. t. } \tan^{-1}\left(\frac{x}{\sqrt{1 - x^2}}\right)$$

 [Watch Video Solution](#)

79. Differentiate the following w.r.t. as indicated:

$$\tan^{-1}\left(\frac{\sqrt{1 + x^2} - 1}{x}\right) \text{ w. r. t. } \tan^{-1}x$$

 [Watch Video Solution](#)

80. Differentiate the following w.r.t. as indicated:

$$\tan^{-1}\left(\frac{\sqrt{1 + a^2x^2} - 1}{ax}\right) \text{ w. r. t. } \tan^{-1}ax$$

 [Watch Video Solution](#)

81. Differentiate the following w.r.t. as indicated:

$$\tan^{-1}\left(\frac{\sqrt{1+x^2}-1}{x}\right) \text{ w. r. t. } \sin^{-1}\left(\frac{2x}{1+x^2}\right)$$

 [Watch Video Solution](#)

82. Differentiate the following w.r.t. as indicated:

$$\tan^{-1}\left(\frac{x}{\sqrt{1-x^2}}\right) \text{ r. t. } \sin^{-1}\left(2x\sqrt{1-x^2}\right)$$

 [Watch Video Solution](#)

83. Differentiate the following w.r.t. as indicated:

$$\tan^{-1}\left(\frac{x}{1+\sqrt{1-x^2}}\right) \text{ w. r. t. } \sin\left(2\cot^{-1}\sqrt{\frac{1+x}{1-x}}\right)$$

 [Watch Video Solution](#)

**84.** Differentiate the following w.r.t. as indicated:

$$e^x \text{ w. r. t. } \sqrt{x}$$

 [Watch Video Solution](#)

**85.** Differentiate the following w.r.t. as indicated:

$$\log_{10} x \text{ w. r. t. } x^2$$

 [Watch Video Solution](#)

**86.** Differentiate the following w.r.t. as indicated:

$$\sin x^2 \text{ w. r. t. } x^3$$

 [Watch Video Solution](#)

87. Differentiate  $\sqrt{1+x^2}$  w.r.t.  $\tan^{-1}x$ .

 [Watch Video Solution](#)

88. Prove that derivative of  $\tan^{-1}\left(\frac{x}{1+\sqrt{1-x^2}}\right)$  w.r.t  $\sin^{-1}x$  is independent of  $x$ .

 [Watch Video Solution](#)

89. Prove that derivative of  $\tan^{-1}\left(\frac{\sqrt{1+x^2}-1}{x}\right)$  w.r.t.  $\tan^{-1}x$  is independent of  $x$ .

 [Watch Video Solution](#)



90. Differentiate  $\tan^{-1}\left(\frac{\sqrt{1+x^2} - \sqrt{1-x^2}}{\sqrt{1+x^2} + \sqrt{1-x^2}}\right)$  w. r. t.  $\sin^{-1}\left(\frac{2x}{1+x^2}\right)$

 [Watch Video Solution](#)

91. Differentiate  $\tan^{-1}\left\{\frac{\sqrt{1+x^2} + \sqrt{1-x^2}}{\sqrt{1+x^2} - \sqrt{1-x^2}}\right\}$  w.r.t.x

 [Watch Video Solution](#)

92. Find  $\frac{dy}{dx}$  if  $y = x^x$

 [Watch Video Solution](#)

93. Differentiate  $x^{x^x}$  w.r.t. x.

 [Watch Video Solution](#)

 Watch Video Solution

94. Find  $f'(x)$  if  $f(x) = (\sin x)^{\sin x}$  for all  $x \in \mathbb{R}$

 Watch Video Solution

95. Differentiate  $(x^{\tan x} + (\sin x)^{\cos x})$  w. r. t.  $x$

 Watch Video Solution

96. If  $x^y \cdot y^x = 1$ , then prove that :

$$\frac{dy}{dx} = \frac{-y(y + x \log x)}{x(y \log x + x)}$$

 Watch Video Solution

97. If  $x^y = e^{X-Y}$ , prove that  $\frac{dy}{dx} = \frac{\log x}{(1 + \log x)^2}$ .



[Watch Video Solution](#)

98. If  $x^Y = e^{X-Y}$ , prove that  $\frac{dy}{dx} = \frac{\log x}{(1 + \log x)^2}$ .



[Watch Video Solution](#)

99. Find  $\frac{dy}{dx}$ , if  $y^x + x^y + x^x = a^b$



[Watch Video Solution](#)

100. Differentiate  $3^x x^{5+x} \cos^{-1} x$  w. r. t.  $x$ .



[Watch Video Solution](#)

101. IF  $f(x) = \left[ \frac{3+x}{1+x} \right]^{2+3x}$  find  $f'(0)$ .

 [Watch Video Solution](#)

102. If  $y = \sqrt{2^x + \sqrt{2^x + \sqrt{2^x + \dots \infty}}}$ , then prove that :

$$(2y - 1) \frac{dy}{dx} = 2^x \log 2.$$

 [Watch Video Solution](#)

103. If  $y = \sqrt{\log x + \sqrt{\log + x \sqrt{\log x + \dots \infty}}}$  then find  $\frac{dy}{dx}$

 [Watch Video Solution](#)

**104.** Differentiate the following w.r.t.x.

$$y = e^{x+ex+ex^{-10\infty}}, \text{ prove that } \frac{dy}{dx} = \frac{y}{1-y}$$



**Watch Video Solution**

**105.** Find the second derivative of  $\sin^{-1}x$



**Watch Video Solution**

**106.** If  $y = 500e^{7x} + 600e^{-7x}$  show that  $\left(d^2 \frac{y}{dx^2}\right) = 49y$



**Watch Video Solution**

**107.** If  $x = a(\cos t + t \sin t)$  and  $y = a(\sin t - t \cos t)$ ,  $0 < t < \frac{\pi}{2}$ , find  $\frac{d^2x}{dt^2}$ ,  $\frac{d^2y}{dt^2}$

 [Watch Video Solution](#)

**108.** If  $x = \tan\left(\frac{1}{2}\log y\right)$ , then show that  $(1 + x^2)\frac{d^2y}{dx^2} = (a - 2x)\frac{dy}{dx}$ .

 [Watch Video Solution](#)

**109.** If  $x = a\cos\theta + b\sin\theta$  and  $y = a\sin\theta - b\cos\theta$ , then prove that

$$y^2 \frac{d^2y}{dx^2} - \frac{dy}{dx} + y = 0$$

 [Watch Video Solution](#)

110. If  $y = a\sin(\log x) + b\cos(\log x)$ , then prove that :

$$x^2 d^2 \frac{y}{dx^2} + x \frac{dy}{dx} + y = 0.$$

 [Watch Video Solution](#)

111. If  $x \cos(a+y) = \cos y$ , then prove that  $\frac{dy}{dx} = \frac{\cos^2(a+y)}{\sin a}$ . Hence,

show that  $\sin a \frac{d^2 y}{dx^2} + \sin 2(a+y) \frac{dy}{dx} = 0$

 [Watch Video Solution](#)

112. If  $x = a \left( \cos \theta + \log \tan \left( \frac{\theta}{2} \right) \right)$  and  $y = a \sin \theta$ , find the value of

$$\frac{d^2 y}{dx^2} \text{ at } \theta = \frac{\pi}{4}$$

 [Watch Video Solution](#)

113. IF  $y = x^x$ , show that  $\left[ \left( d^2 \frac{y}{dx^2} \right) - \frac{1}{y} \left( \frac{dy}{dx} \right)^2 - \frac{y}{x} = 0 \right]$

 [Watch Video Solution](#)

114. If  $y = \operatorname{cosec}^{-1}x, x > 1$ , then show that :

$$x(x^2 - 1) \frac{d^2y}{dx^2} + (2x^2 - 1) \frac{dy}{dx} = 0$$

 [Watch Video Solution](#)

115. Find the second order derivative of the following functions

If  $y = e^{\tan x}$ , prove that  $\cos^2 x \frac{d^2y}{dx^2} - (1 + \sin 2x) \frac{dy}{dx} = 0$

 [Watch Video Solution](#)

116. If  $y = e^x(\sin x + \cos x)$ , prove that  $\frac{d^2y}{dx^2} - 2 \frac{dy}{dx} + 2y = 0$



 [Watch Video Solution](#)

117. If  $y = e^{2\tan^{-1}x}$ , then show that

$$(1 + x^2)^2 \frac{d^2y}{dx^2} + 2x(1 + x^2) \frac{dy}{dx} = 4y$$

 [Watch Video Solution](#)

118. Verify Rolle's Theorem for the function :

$$f(x) = x^2 - x - 12 \in [-3, 4]$$

 [Watch Video Solution](#)

119. Discuss the applicability of Rolle's Theorem for the function

$$f(x) = (x - 1)^{2/5} \text{ in the interval } [0, 3]$$

 [Watch Video Solution](#)

**120.** Let  $f(x) = x(x-1)(x-2), x \in [0,2]$ . Prove that 'f' satisfies the conditions of Rolle's Theorem and there is more than one 'c' in  $(0,2)$  such that  $f'(C) = 0$

 [Watch Video Solution](#)

**121.** Verify Rolle's theorem for the following functions

$$f(x) = \cos 2\left(x - \frac{\pi}{4}\right) \text{ in the interval } \left[0, \frac{\pi}{2}\right].$$

 [Watch Video Solution](#)

**122.** Discuss the applicability of Rolle's Theorem for the function :

$$f(x) \begin{cases} (x^2 + 1) & \text{when } 0 \leq x \leq 1 \\ 3 - x & \text{when } 1 < x \leq 2 \end{cases}$$

 [Watch Video Solution](#)

**123.** At what point on the curve  $y = (\cos x - 1)$  in  $[0, 2\pi]$ , is the tangent parallel to x-axis?

 [Watch Video Solution](#)

**124.** It is given that for the function 'f' given by :

$f(x) = x^3 + bx^2 + ax, x \in [1, 3]$  Rolle's Theorem holds with

$c = 2 + \frac{1}{\sqrt{3}}$ . Find the values of 'a' and 'b'.

 [Watch Video Solution](#)

**125.** Discuss the applicability of Lagrange's Mean Value Theorem to

$f(x) = x(x - 1)(x - 2)$  in  $\left[0, \frac{1}{2}\right]$

 [Watch Video Solution](#)

**126.** Discuss the applicability of Lagrange's Mean Value Theorem to

$$f(x) = \cos x \in [0, \pi/2]$$



[Watch Video Solution](#)

**127.** Find 'c' of the Lagrange's Mean Value Theorem when  $f(x) = x(x-2)$  in  $[1, 2]$



[Watch Video Solution](#)

**128.** Find a point on the parabola  $y = (x - 3)^2$ , where the tangent is parallel to the chord joining  $(3, 0)$  and  $(4, 1)$



[Watch Video Solution](#)

**129.** Lagrange's Theorem to determine a point P on the curve  $f(x) = \sqrt{x-2}$  defined in the interval  $[2,3]$ , where the tangent is parallel to the chord joining the end points on the curve.

 [Watch Video Solution](#)

**130.** Prove that the function  $f(x) = 5x-3$  is continuous at  $x = 0$

 [Watch Video Solution](#)

**131.** Examine the continuity of the function  $f(x) = 2x^2 - 1$  at  $x = 3$

 [Watch Video Solution](#)

**132.** Examine the following function for continuity:  $f(x) = x - 5$

 [Watch Video Solution](#)

 Watch Video Solution

**133.** Examine the following function for continuity:

$$f(x) = \frac{1}{x - 5}, x \neq 5$$

 Watch Video Solution

**134.** Examine the following function for continuity:

$$f(x) = \frac{x^2 - 25}{x + 5}, x \neq -5$$

 Watch Video Solution

**135.** Examine the following function for continuity:  $f(x) = |x - 5|$

 Watch Video Solution

**136.** Prove that the function  $f(x) = x^n$ , is continuous at  $x = n$ , where  $n$  is a positive integer.

 [Watch Video Solution](#)

**137.** Is the function  $f$  defined by  $f(x) = \begin{cases} x & \text{if } x \leq 1 \\ 5 & \text{if } x > 1 \end{cases}$  continuous at,  $x=0$ ? At  $x=1$ ? At  $x=2$  ?

 [Watch Video Solution](#)

**138.** Find all the points of discontinuity of  $f$ , where  $f$  is defined by

$$f(x) = \begin{cases} 2x + 3, & \text{if } x \leq 2 \\ 2x - 3, & \text{if } x > 2 \end{cases}$$

 [Watch Video Solution](#)

**139.** Find all points of discontinuity of  $f$ , where  $f$  is defined by :  $f(x) =$

$$\left\{ \begin{array}{ll} |x|+3, & \text{if } x \leq -3 \\ -2x, & \text{if } -3 < x \end{array} \right\}$$

 [Watch Video Solution](#)

**140.** Find all points of discontinuity of  $f$ , where  $f$  is defined by :

$$f(x) = \begin{cases} \frac{|x|}{x} & \text{if } x \neq 0 \\ 0 & \text{if } x = 0 \end{cases}$$

 [Watch Video Solution](#)

**141.** Find all points of discontinuity of  $f$ , where  $f$  is defined by:

$$f(x) = \begin{cases} \frac{x}{|x|} & \text{if } x < 0 \\ -1 & \text{if } x \geq 0 \end{cases}$$

 [Watch Video Solution](#)



**142.** Find all points of discontinuity of  $f$ , where  $f$  is defined by

$$f(x) = \begin{cases} x + 1 & \text{if } x \geq 1 \\ x^2 + 1 & \text{if } x < 1 \end{cases}$$

 [Watch Video Solution](#)

**143.** Find all points of discontinuity of  $f$ , where  $f$  is defined by :

$$f(x) = \begin{cases} x^3 - 3 & x \leq 2 \\ x^2 + 1 & x > 2 \end{cases}$$

 [Watch Video Solution](#)

**144.** Find all points of discontinuity of  $f$ , where  $f$  is defined by

$$f(x) = \begin{cases} x^{10} - 1 & \text{if } x \leq 1 \\ x - 5 & \text{if } x > 1 \end{cases}$$

 [Watch Video Solution](#)

145. Discuss the continuity of the function

$$f(x) = \begin{cases} 3, & \text{if } 0 \leq x \leq 1 \\ 4, & \text{if } 1 < x < 3 \\ 5, & \text{if } 3 \leq x \leq 10 \end{cases}$$

 [Watch Video Solution](#)

146. Discuss the continuity of the function  $f$ , where  $f$  is defined by:

$$f(x) = \begin{cases} 2x & \text{if } x < 0 \\ 0 & \text{if } 0 \leq x \leq 1 \\ 4x & \text{if } x > 1 \end{cases}$$

 [Watch Video Solution](#)

147. Find all points of discontinuity of  $f$ , where  $f$  is defined by  $f(x) =$

$$(-2, \text{ if } x \leq -1), (2x, \text{ if } -1 < x < 1), (2, \text{ if } x > 1) : \}$$



 [Watch Video Solution](#)

**148.** Find the relationship between  $a$  and  $b$  so that the function  $f$

$$\text{defined by: } f(x) = \begin{cases} ax + 1 & \text{if } x \leq 3 \\ bx + 3 & \text{if } x > 3 \end{cases} \text{ is continuous at } x = 3$$

 [Watch Video Solution](#)

**149.** For what value of  $\lambda$  is the function defined by

$$f(x) = \begin{cases} \lambda(x^2 - 2x) & \text{if } x \leq 0 \\ 4x + 1 & \text{if } x > 0 \end{cases} \text{ continuous at } x = 0? \text{ What}$$

about continuity at  $x = 1$ ?

 [Watch Video Solution](#)

**150.** Show that the function defined by  $g(x) = x - [x]$  is discontinuous at all integral points. Here  $[x]$  denotes the greatest

integer less than or equal to  $x$ .

 [Watch Video Solution](#)

**151.** Is the function defined by  $f(x) = x^2 - \sin x + 5$  continuous at  $x = \pi$

 [Watch Video Solution](#)

**152.** Discuss the continuity of the following function:  
 $f(x) = \sin x + \cos x$

 [Watch Video Solution](#)

**153.** Discuss the continuity of the following function:  
 $f(x) = \sin x - \cos x$

 [Watch Video Solution](#)

 [Watch Video Solution](#)

**154.** Discuss the continuity of the following function:

$$f(x) = \sin x \cdot \cos x$$

 [Watch Video Solution](#)

**155.** Discuss the continuity of the cosine, cosecant, secant and cotangent functions.

 [Watch Video Solution](#)

**156.** Find all points of discontinuity of  $f$ , where:

$$f(x) = \begin{cases} \frac{\sin x}{x} & \text{if } x < 0 \\ x + 1 & \text{if } x \geq 0 \end{cases}$$

 [Watch Video Solution](#)

157. Determine if  $f$  defined by :  $f(x) = \begin{cases} x^2 \sin\left(\frac{1}{x}\right) & \text{if } x \neq 0 \\ 0 & \text{if } x = 0 \end{cases}$  is

a continuous function?

 [Watch Video Solution](#)

158. Discuss the continuity of the following function:

$$f(x) = \sin x - \cos x$$

 [Watch Video Solution](#)

159. Find the values of  $k$  so that the function  $f$  is continuous at the

indicated point :  $f(x) = \begin{cases} k \frac{\cos x}{\pi - 2x} & \text{if } x \neq \frac{\pi}{2} \\ 3 & \text{if } x = \frac{\pi}{2} \end{cases}$  at  $x = \frac{\pi}{2}$



Watch Video Solution

160. Find the values of  $k$  so that the function  $f$  is continuous at the

$$\text{indicated point : } f(x) = \begin{cases} kx^2 & \text{if } x \leq 2 \\ 3 & \text{if } x > 2 \end{cases} \text{ at } x = 2$$



Watch Video Solution

161. Find the values of  $k$  so that the function  $f$  is continuous at the

$$\text{indicated point : } f(x) = \begin{cases} k \frac{\cos x}{\pi - 2x} & \text{if } x \neq \frac{\pi}{2} \\ 3 & \text{if } x = \frac{\pi}{2} \end{cases} \text{ at } x = \frac{\pi}{2}$$



Watch Video Solution

**162.** Find the values of  $k$  so that the function  $f$  is continuous at the

$$\text{indicated point : } f(x) = \begin{cases} kx + 1 & \text{if } x \leq 5 \\ 3x - 5 & \text{if } x > 5 \end{cases} \text{ at } x = 5$$

 [Watch Video Solution](#)

**163.** Find the values of  $a$  and  $b$  such that the function defined by :

$$f(x) = \begin{cases} 5, & \text{if } x \leq 2 \\ ax + b, & \text{if } x > 2 \end{cases}$$

 [Watch Video Solution](#)

**164.** Show that the function defined by  $f(x) = \cos(x^2)$  is a continuous function.

 [Watch Video Solution](#)



**165.** Show that the function defined by  $f(x) = |\cos x|$  is a continuous function.

 [Watch Video Solution](#)

**166.** Find all the points of discontinuity of  $f$  defined by  $f(x) = |x| - |x + 1|$

 [Watch Video Solution](#)

**167.** Differentiate the functions with respect to  $x$

$$\sin(x^2 + 5)$$

 [Watch Video Solution](#)

**168.** Differentiate the functions with respect to  $x$

$$\cos(\sin x)$$

 [Watch Video Solution](#)

**169.** Differentiate the functions with respect to  $x$

$$\sin(ax+b)$$

 [Watch Video Solution](#)

**170.** Differentiate the functions with respect to  $x$

$$\sec\left(\tan\left(\sqrt{x}\right)\right)$$

 [Watch Video Solution](#)

**171.** Differentiate the functions with respect to  $x$ :  $\frac{\sin(ax + b)}{\cos(cx + d)}$



[Watch Video Solution](#)

**172.** Differentiate the functions with respect to  $x$

$$\cos x^3 \cdot \sin^2(x^5)$$



[Watch Video Solution](#)

**173.** Differentiate the functions with respect to  $x$

$$2\sqrt{\cot(x^2)}$$



[Watch Video Solution](#)

**174.** Differentiate the functions with respect to  $x$

$$\cos(\sqrt{x})$$



[Watch Video Solution](#)

**175.** Prove that the function  $f$  given by :  $f(x) = |x - 1|, x \in R$  is not differentiable at  $x = 1$

 [Watch Video Solution](#)

**176.** Prove that  $f(x) = [x], 0 < x < 3$  is not differentiable at  $x = 1$  but  $x = 2$ .

 [Watch Video Solution](#)

**177.** Find  $\frac{dy}{dx}$  in the following:

$$2x + 3y = \sin x$$

 [Watch Video Solution](#)

178. Find  $\frac{dy}{dx}$  in the following:  $2x + 3y = \sin x$

 [Watch Video Solution](#)

179. Find  $\frac{dy}{dx}$  in the following:

$$ax + by^2 = \cos y$$

 [Watch Video Solution](#)

180. Find  $\frac{dy}{dx}$  in the following:

$$xy + y^2 = \sin x + y$$

 [Watch Video Solution](#)

**181.** Find  $\frac{dy}{dx}$  in the following:

$$x^2 + xy + y^2 = 100$$



[Watch Video Solution](#)

**182.** Find  $\frac{dy}{dx}$  in the following:

$$x^3 + x^2y + xy^2 + y^3 = 81$$



[Watch Video Solution](#)

**183.** Find  $\frac{dy}{dx}$  in the following:

$$\sin^2y + \cos xy = \pi$$



[Watch Video Solution](#)

**184.** Find  $\frac{dy}{dx}$  in the following:

$$\sin^2 x + \cos^2 y = 9$$

 [Watch Video Solution](#)

**185.** Find  $\frac{dy}{dx}$  in the following:

$$y = \sin^{-1} \left( 2 \frac{x}{1+x^2} \right)$$

 [Watch Video Solution](#)

**186.** Differentiate the following w.r.t.  $x$ :

$$\tan^{-1} \left( \frac{3x - x^3}{1 - 3x^2} \right), \quad -\frac{1}{\sqrt{3}} < x < \frac{1}{\sqrt{3}}$$

 [Watch Video Solution](#)

**187.** Find  $\frac{dy}{dx}$  in the following:

$$y = \cos^{-1}\left(\frac{1-x^2}{1+x^2}\right), 0 < x < 1$$

 [Watch Video Solution](#)

**188.** Differentiate the following w.r.t.  $x$ :

$$\sin^{-1}\left(\frac{1-x^2}{1+x^2}\right), 0 < x < 1$$

 [Watch Video Solution](#)

**189.** Differentiate the following w.r.t.  $x$ :

$$\cos^{-1}\left(2\frac{x}{1+x^2}\right), -1 < x < 1$$

 [Watch Video Solution](#)



190. Find  $\frac{dy}{dx}$  in the following:  $y = \sin^{-1}\left(2x\sqrt{1-x^2}\right)$ ,  $-\frac{1}{\sqrt{2}} < x < \frac{1}{\sqrt{2}}$

 [Watch Video Solution](#)

191. Find  $\frac{dy}{dx}$  in the following:  $y = \sec^{-1}\left(\frac{1}{2x^2-1}\right)$ ,  $0 < x < \frac{1}{\sqrt{2}}$

 [Watch Video Solution](#)

192. Differentiate the following w.r.t.  $x$  :

$$\frac{e^x}{\sin x}$$

 [Watch Video Solution](#)

**193.** Differentiate the following w.r.t.  $x$  :

$$e^{\sin^{-1}x}$$



**Watch Video Solution**

**194.** Differentiate the following w.r.t.  $x$ :  $e^x \wedge 3$



**Watch Video Solution**

**195.** Differentiate the following w.r.t  $x$

$$\sin\left(\tan^{-1}\left(e^{-x}\right)\right)$$



**Watch Video Solution**

**196.** Differentiate the following w.r.t  $x$

$$\log(\cos(e^x))$$



[Watch Video Solution](#)

**197.** Differentiate the following w.r.t.  $x$ :  $e^x + e^{x^2} + \dots + e^{x^5}$



[Watch Video Solution](#)

**198.** Differentiate the following w.r.t.  $x$ :

$$\sqrt{e^{\sqrt{x}}}, x > 0$$



[Watch Video Solution](#)

**199.** Differentiate the following w.r.t.x:

$$\frac{\cos x}{\log x}, x > 0$$



**Watch Video Solution**

**200.** Differentiate the following w.r.t x

$$\cos(\log x + e^x), x > 0$$



**Watch Video Solution**

**201.** Differentiate the following w.r.t. x :

$$\cos x \cdot \cos 2x \cdot \cos 3x$$



**Watch Video Solution**

**202.** Differentiate the following w.r.t x

$$(\log x)^{\cos x}$$



**Watch Video Solution**

**203.** Differentiate the following w.r.t. x:

$$x^x - 2^{\sin x}$$



**Watch Video Solution**

**204.** Differentiate the following w.r.t.x .

$$(x + 3)^2(x + 4)^3(x + 5)^4$$



**Watch Video Solution**

**205.** Differentiate the following w.r.t.  $x$  :

$$\left(x + \frac{1}{x}\right)^x + x^{x + \frac{1}{x}}$$



**Watch Video Solution**

**206.** Differentiate the following w.r.t.  $x$ :

$$(x)^{\log x} + (\log x)^x$$



**Watch Video Solution**

**207.** Differentiate the following w.r.t.  $x$ :

$$(\sin x)^x + \sin^{-1} \sqrt{x}$$



**Watch Video Solution**

**208.** Differentiate the following w.r.t.  $x$ :

$$x^{\sin x} + (\sin x)^{\cos x}$$

 [Watch Video Solution](#)

**209.** Differentiate the function w.r.t.  $x$  :  $x^{x \cos x} + \frac{x^2 + 1}{x^2 - 1}$

 [Watch Video Solution](#)

**210.** Differentiate the following w.r.t.  $x$ :

$$(x \cos x)^x + (x \sin x)^{1/x}$$

 [Watch Video Solution](#)

**211.** Find  $\frac{dy}{dx}$  of the function :  $x^y + y^x = 1$

 [Watch Video Solution](#)

212. Find  $\frac{dy}{dx}$ , if  $y^x = x^y$

 [Watch Video Solution](#)

213. Find  $\frac{dy}{dx}$  of the function :  $(\cos x)^y = (\cos y)^x$

 [Watch Video Solution](#)

214. Find  $\frac{dy}{dx}$  of the function :  $xy = e^{x-y}$

 [Watch Video Solution](#)



**215.** Find the derivative of the function given by

$$f(x) = (1 + x)(1 + x^2)(1 + x^4)(1 + x^8) \text{ and hence find } f'(1)$$

 [Watch Video Solution](#)

**216.** Differentiate  $(x^2 - 5x + 8)(x^3 + 7x + 9)$  by using product rule.

 [Watch Video Solution](#)

**217.** Differentiate  $(x^2 - 5x + 8)(x^3 + 7x + 9)$  by expanding the product to obtain a single polynomial.

 [Watch Video Solution](#)

**218.** Differentiate  $(x^2 - 5x + 8)(x^3 + 7x + 9)$  by logarithmic differentiation.

 [Watch Video Solution](#)

**219.** If  $u$ ,  $v$  and  $w$  are functions of  $x$ , then show that  $\frac{d}{dx}(u \cdot v \cdot w) = \frac{du}{dx}(v \cdot w) + u \cdot \frac{dv}{dx} \cdot w + u \cdot v \cdot \frac{dw}{dx}$  in two ways - first by repeated application of product rule, second by logarithmic differentiation.

 [Watch Video Solution](#)

**220.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = 2at^2, y = at^4$$

 [Watch Video Solution](#)

221. If  $x$  and  $y$  are connected parameterically by the equation ,  
without eliminating the parameter , find  $\frac{dy}{dx}$

$$x = a\cos(\theta), y = b\sin(\theta)$$

 [Watch Video Solution](#)

222. Find  $\frac{dy}{dx}$  if  $x = \sin t$  and  $y = \cos 2t$ .

 [Watch Video Solution](#)

223. Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parameterically by the  
equations, given below without eliminating the parameter.

$$x = 4t, y = \frac{4}{t}$$

 [Watch Video Solution](#)

224. Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x \cos \theta - \cos 2\theta, y = \sin \theta - \sin 2\theta$$

 [Watch Video Solution](#)

225. Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = a(\theta - \sin \theta), y = a(1 + \cos \theta)$$

 [Watch Video Solution](#)

226. If  $x$  and  $y$  are connected parametrically by the equations given in Exercises 1 to 10, without eliminating the parameter, Find  $\frac{dy}{dx}$  :

$$x = a \left( \cos t + \frac{\log \tan t}{2} \right), y = a \sin t$$

 [Watch Video Solution](#)

**227.** If  $x$  and  $y$  are connected parametrically by the equation ,  
without eliminating parameter , find  $\frac{dy}{dx}$

$$x = a \sec(\theta), y = b \tan(\theta)$$

 [Watch Video Solution](#)

**228.** If  $x$  and  $y$  are connected parametrically by the equations given  
in Exercises 1 to 10, without eliminating the parameter, Find  $\frac{dy}{dx}$  :

$$x = a(\cos \theta + \theta \sin \theta), y = a(\sin \theta - \theta \cos \theta)$$

 [Watch Video Solution](#)

229. Find  $\frac{dy}{dx} = -\frac{y}{x}$  if  $x = \sqrt{a^{\sin^{-1}t}}$ ,  $y = \sqrt{a^{\cos^{-1}t}}$

 [Watch Video Solution](#)

230. Find the second order derivatives of the function :  $x^2 + 3x + 2$

 [Watch Video Solution](#)

231. Find the second order derivatives of the function:  $x^{20}$

 [Watch Video Solution](#)

232. Find the second order derivatives of the function :  $x \cdot \cos x$

 [Watch Video Solution](#)

**233.** Find the second order derivatives of the function :  $\log x$

 [Watch Video Solution](#)

**234.** Find the second order derivatives of the function :  $x^3 \log x$

 [Watch Video Solution](#)

**235.** Find the second order derivatives of the function :  $e^x \sin 5x$

 [Watch Video Solution](#)

**236.** Find the second order derivatives of the function :  $e^{6x} \cos 3x$

 [Watch Video Solution](#)

237. Find the second order derivatives of the function :  $\tan^{-1}x$

 [Watch Video Solution](#)

238. Find the second order derivatives of the function :  $\log(\log x)$

 [Watch Video Solution](#)

239. Find the second order derivatives of the function :  $\sin(\log x)$

 [Watch Video Solution](#)

240.  $y = 5\cos x - 3\sin x$ , prove that  $\frac{d^2y}{dx^2} + y = 0$

 [Watch Video Solution](#)



241. If  $y = \cos^{-1}x$  Find  $\left(d^2\frac{y}{dx^2}\right)$  in terms of  $y$  alone.

 Watch Video Solution

242. If  $y = 3\cos(\log x) + 4\sin(\log x)$  show that  $x^2y_2 + xy_1 + y = 0$

 Watch Video Solution

243. If  $y = Ae^{mx} + Be^{nx}$ , Show that  $\left(\frac{d^2}{dx^2}y\right) - (m+n)\frac{dy}{dx} + mny = 0$

 Watch Video Solution

244. If  $y = 500e^{7x}$ , show that  $\frac{d^2y}{dx^2} = 49y$

 Watch Video Solution

245. If  $e^y(x+1) = 1$  show that  $\left(d^2 \frac{y}{dx^2}\right) = \left(\frac{dy}{dx}\right)^2$  है।

 [Watch Video Solution](#)

246. If  $y = [\tan^{-1}x]^2$ , then prove that :

$$(x^2 + 1)^2 y_2 + 2x(x^2 + 1)y_1 = 2.$$

 [Watch Video Solution](#)

247. Verify Rolle's theorem for the function

$$f(x) = x^2 + 2x - 8, x \in [-4, 2]$$

 [Watch Video Solution](#)

**248.** Examine if Rolle's theorem is applicable to any of the following functions. Can you say some thing about the converse of Rolle's theorem from these example?  $f(x) = [x]$  for  $x \in [5, 9]$

 [Watch Video Solution](#)

**249.** Examine if Rolle's theorem is applicable to any of the following functions. Can you say some thing about the converse of Rolle's theorem from these example?  $f(x) = [x]$  for  $x \in [-2, 2]$

 [Watch Video Solution](#)

**250.** Examine if Rolle's theorem is applicable to any of the following functions. Can you say some thing about the converse of Rolle's theorem from these example?  $f(x) = x^2 - 1$  for  $x \in [1, 2]$

 [Watch Video Solution](#)

**251.** If  $f: [-5, 5] \rightarrow \mathbb{R}$  is a differentiable function and if  $f'(x)$  does not vanish anywhere, then prove that  $f(-5) \neq f(5)$

 [Watch Video Solution](#)

**252.** Verify Mean Value Theorem, if  $f(x) = x^2 - 4x - 3$ , in the interval  $[a, b]$ , where  $a = 1$  and  $b = 4$ .

 [Watch Video Solution](#)

**253.** Examine the applicability of Mean Value Theorem for all three functions given in the above exercise 2. (i)  $f(x) = [x]$  for  $x \in [5, 9]$  (ii)  $f(x) = [x]$  for  $x \in [-2, 2]$  (iii)  $f(x) = [x\sqrt{-1}]$  for  $x \in [1, 2]$

 [Watch Video Solution](#)

254. Differentiate w.r.t.  $x$  the function :  $(3x^2 - 9x + 5)^9$

 [Watch Video Solution](#)

255. Differentiate w.r.t.  $x$  the function :  $\sin^3 x + \cos^6 x$

 [Watch Video Solution](#)

256. Differentiate w.r.t.  $x$  the function :  $(5x)^{3\cos 2x}$

 [Watch Video Solution](#)

257. Differentiate w.r.t.  $x$  the function :  $\sin^{-1}(x\sqrt{x}), 0 \leq x \leq 1$

 [Watch Video Solution](#)

$$\cos^{-1}\left(\frac{x}{2}\right)$$

**258.** Differentiate w.r.t.  $x$  the function :  $\frac{\cos^{-1}\left(\frac{x}{2}\right)}{\sqrt{2x+7}}$ ,  $x$  lies between -2

and 2

 [Watch Video Solution](#)

**259.** Differentiate w.r.t.  $x$  the function :  $(\log x)^{\log x}$ ,  $x > 1$

 [Watch Video Solution](#)

**260.** Differentiate w.r.t.  $x$  the function :  $\cos(ax + b \sin x)$ , for some constant  $a$  and  $b$ .

 [Watch Video Solution](#)

261. Differentiate w.r.t.  $x$  the function :

$(\sin x - \cos x)^{\sin x - \cos x}$ , *lies between*  $\frac{\pi}{4}$  and  $3\frac{\pi}{4}$

 [Watch Video Solution](#)

262. Differentiate w.r.t.  $x$  the function :  $x^x + x^a + a^x + a^a$ , for some fixed  $a > 0$  and  $x > 0$

 [Watch Video Solution](#)

263. Differentiate w.r.t.  $x$  the function :  $x^{x^2-3} + (x-3)^{x^2}$ ,  $f$  or  $x > 3$

 [Watch Video Solution](#)

264. Find  $dy/dx$  if  $y = 12(1 - \cos t)$ ,  $x = 10(t - \sin t)$

 [Watch Video Solution](#)

 Watch Video Solution

265. Find  $\frac{dy}{dx}$  if  $y = \sin^{-1}x + \sin^{-1}\sqrt{1-x^2}$ ,  $0 < x < 1$

 Watch Video Solution

266. If  $x\sqrt{1+y} + y\sqrt{1+x} = 0$  then  $\frac{dy}{dx}$  equals.

 Watch Video Solution

267. If  $\cos y = x \cos(a + y)$ , with  $\cos a \neq \pm 1$ , prove that

$$\frac{dy}{dx} = \frac{\cos^2(a + y)}{\sin a}$$

 Watch Video Solution



268. If  $x = a(\cos t + t \sin t)$  and  $y = a(\sin t - t \cos t)$ , find  $\frac{d^2y}{dx^2}$

 [Watch Video Solution](#)

269. If  $f(x) = |x|^3$  show that  $f'(x)$  exists for all real  $x$  and find it.

 [Watch Video Solution](#)

270. Using mathematical induction prove that  $d \frac{x^n}{dx} = nx^{n-1}$  for all positive integers  $n$ .

 [Watch Video Solution](#)

271. Using the fact that  $\sin(A + B) = \sin A \cos B + \cos A \sin B$  and the differentiation, obtain the sum formula for cosines.



 Watch Video Solution

272. Does there exist a function which is continuous everywhere but not differentiable at exactly two points? Justify your answer.

 Watch Video Solution

273. If  $y = \begin{vmatrix} f(x) & g(x) & h(x) \\ 1 & m & n \\ a & b & c \end{vmatrix}$ , prove that  $\frac{dy}{dx} = \begin{vmatrix} f'(x) & g'(x) & h'(x) \\ l & m & n \\ a & b & c \end{vmatrix}$

 Watch Video Solution

274. If  $y = e^{a \cos^{-1} x}$ ,  $-1 \leq x \leq 1$ , show that

$$(1 - x^2) \frac{d^2 y}{dx^2} - x \left( \frac{dy}{dx} \right) - a^2 y = 0$$

 Watch Video Solution

275. If  $f(x) = \begin{cases} \frac{x^3 + x^2 - 16x + 20}{(x-2)^2} & x \neq 2 \\ k & x = 2 \end{cases}$  is continuous at  $x=2$ , find the

value of 'k'.

 [Watch Video Solution](#)

276. The derivative of  $f(x) = |x|$  at  $x=0$  is

 [Watch Video Solution](#)

277. If  $y = \tan x + \sec x$ , prove that  $\frac{d^2y}{dx^2} = \frac{\cos x}{(1 - \sin x)^2}$

 [Watch Video Solution](#)

278. If  $f(x) = \frac{\sqrt{2}\cos x - 1}{\cot x - 1}$ ,  $x \neq \frac{\pi}{4}$ , find the value of  $f\left(\frac{\pi}{4}\right)$  so that  $f(x)$  becomes continuous at  $x = \frac{\pi}{4}$

 [Watch Video Solution](#)

279. Examine the differentiability of the function 'f' defined by:

$$f(x) = \begin{cases} 2x + 3 & \text{if } -3 \leq x < -2 \\ x + 1 & \text{if } -2 \leq x < 0 \\ x + 2 & \text{if } 0 \leq x \leq 1 \end{cases}$$

 [Watch Video Solution](#)

280. Differentiate  $\left[ \tan^{-1} \left\{ \frac{\sqrt{1-x^2}}{x} \right\} \right]$  with respect to  $\left[ \cos^{-1} \left\{ 2x\sqrt{1-x^2} \right\} \right]$

 [Watch Video Solution](#)

281. If  $f(x) = \begin{cases} x \sin\left(\frac{1}{x}\right) & x \neq 0 \\ 0 & x = 0 \end{cases}$  Show that 'f' is not differentiable at x

=0

 [Watch Video Solution](#)

282. Show that  $f(x) = \begin{cases} x \sin\frac{1}{x}, & \text{when } x \neq 0 \\ 0, & \text{when } x = 0 \end{cases}$  is continuous but not

differentiable at  $x = 0$

 [Watch Video Solution](#)

283. If  $f(x) = \begin{cases} x \sin\left(\frac{1}{x}\right) & x \neq 0 \\ 0 & x = 0 \end{cases}$  Show that 'f' is not differentiable at

$x=0$

 [Watch Video Solution](#)

284. Show that  $f(x) = \begin{cases} |2x - 3|[x] & x \geq 1 \\ \sin\left(\frac{\pi x}{2}\right) & x < 1 \end{cases}$  is continuous but not

differentiable at  $x=1$ .

 [Watch Video Solution](#)

285. Does there exist a function which is continuous everywhere but not differentiable at exactly two points? Justify your answer.

 [Watch Video Solution](#)

286. Is  $|\sin x|$  differentiable? What about  $\cos|x|$ ?

 [Watch Video Solution](#)

287. Find the derivative of  $\frac{\sin^{-1}x}{x}$  w. r. t.  $x$ .

 [Watch Video Solution](#)

288. Differentiate the following w.r.t.  $x$ :

$$\sqrt{3x+2} + \frac{1}{\sqrt{2x^2+4}}$$

 [Watch Video Solution](#)

**289.** Differentiate the following w.r.t.x:

$$e^{\sec^2 x} + 3\cos^{-1}x$$



**Watch Video Solution**

**290.** Differentiate the following w.r.t x

$$(3x^2 - 9x + 5)^9$$



**Watch Video Solution**

**291.** Differentiate the following w.r.t. x:  $\sin^3 x + \cos^6 x$



**Watch Video Solution**

**292.** Differentiate the following w.r.t. x:  $e^{\log x}$



**Watch Video Solution**



 Watch Video Solution

293. Differentiate the following w.r.t.  $x$ :  $e^{2\log x + 3}$

 Watch Video Solution

294. Prove that  $\cot^{-1}x + \cot^{-1}\left(\frac{1}{x}\right)$  is a constant.

 Watch Video Solution

295. If  $y = f\left(\frac{2x - 1}{x^2 + 1}\right)$  and  $f(x) = \sin x^2$ , then find  $\frac{dy}{dx}$ .

 Watch Video Solution

**296.** Find the derivative of the following w.r.t  $x$ ,

$$\log\left(\frac{1}{\sqrt{x}}\right) + 5x^a - 3a^x + \sqrt[3]{x^{-2}} + 6\sqrt[4]{x^{-3}}$$

 [Watch Video Solution](#)

**297.** If  $y = \tan^{-1}\left(\frac{e^{2x} + 1}{e^{2x} - 1}\right)$ , prove that:  $\frac{dy}{dx} = -\frac{2e^{2x}}{1 + e^{4x}}$

 [Watch Video Solution](#)

**298.** If the derivative of  $\tan^{-1}(a + bx)$  takes the value 1 at  $x=0$ , prove that  $1 + a^2 = b$

 [Watch Video Solution](#)

**299.** Using the fact that  $\sin(A + B) = \sin A \cos B + \cos A \sin B$  and the differentiation, obtain the sum formula for cosines.

 [Watch Video Solution](#)

**300.** If  $\sqrt{y+x} + \sqrt{y-x} = c$ , where  $c \neq 0$ , then  $\frac{dy}{dx}$  has the value equal to

 [Watch Video Solution](#)

**301.** If  $\sin x = y \sin(x + b)$ , show that  $\frac{dy}{dx} = \frac{\sin b}{\sin^2(x + b)}$

 [Watch Video Solution](#)

**302.** If  $x \sin(a+y) + \sin a \cos(a+y) = 0$ , then prove that :

$$\frac{dy}{dx} = \frac{\sin^2(a+y)}{\sin a}$$

 [Watch Video Solution](#)

**303.** If  $y = x \sin(a+y)$ , prove that  $\frac{dy}{dx} = \frac{\sin^2(a+y)}{\sin(a+y) - y \cos(a+y)}$

 [Watch Video Solution](#)

**304.** Differentiate  $\log[\log(\log x)]$  w.r.t.  $x$ .

 [Watch Video Solution](#)

**305.** If  $y = e^{x e^2}$  Find :  $\frac{dy}{dx}$

 [Watch Video Solution](#)

306. Find  $\frac{dy}{dx}$  when :

$$y = x^{\sin x - \cos x} + \frac{x^2 - 1}{x^2 + 1}$$

 [Watch Video Solution](#)

307. Find  $\frac{dy}{dx}$  when :

$$y = x^{\cot x} + \frac{2x^2 - 3}{x^2 + x + 2}$$

 [Watch Video Solution](#)

308. If  $y = x^{x^x}$  prove that  $\frac{dy}{dx} = x^{x+x^x} \left[ \frac{1}{x} + (1 + \log x) \log x \right]$

 [Watch Video Solution](#)

**309.** If  $y = (\tan x)^{\tan x^{\tan x}}$ , then prove that  $\left(\frac{dy}{dx} = 2\right) \text{ at } x = \frac{\pi}{4}$

 [Watch Video Solution](#)

**310.** Differentiate  $\tan x \tan 2x \tan 3x \tan 4x$  in two ways: by taking logarithms.

 [Watch Video Solution](#)

**311.** Differentiate  $\tan x \tan 2x \tan 3x \tan 4x$  in two ways: by repeatedly applying product rule.

 [Watch Video Solution](#)

**312.** if  $x = \sec\theta - \cos\theta$  and  $y = \sec^n\theta - \cos^n\theta$ , then show that

$$\left(x^2 + 4\right)\left(\frac{dy}{dx}\right)^2 = n^2\left(y^2 + 4\right)$$

 [Watch Video Solution](#)

**313.** For what choices of a,b,c if any , does the function

$$f(x) = \begin{cases} ax^2 + bx + c & 0 \leq x \leq 1 \\ bx - c & 1 \leq x \leq 2 \\ c & x > 2 \end{cases} \text{ become differentiable at } x = 1$$

and  $x=2$ ?

 [Watch Video Solution](#)

**314.** Using mathematical induction prove that  $d\frac{x^n}{dx} = nx^{n-1}$  for all positive integers n.

 [Watch Video Solution](#)

**315.** If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ , prove that

$$C_1 + 2C_2 + 3C_3 + \dots + nC_n = n \cdot 2^{n-1}$$

 [Watch Video Solution](#)

**316.** If  $(1 + x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$ , then prove that :

$$C_1 - 2C_2 + \dots + (-1)^{n-1}nC_n = 0$$

 [Watch Video Solution](#)

**317.** Are the following functions continuous at each point of their domains?  $e^x$

 [Watch Video Solution](#)



**318.** Are the following functions continuous at each point of their domains?  $\sin x$

 [Watch Video Solution](#)

**319.** Prove that the following functions are continuous at all points of their domains:  $f(x) = \cos x$

 [Watch Video Solution](#)

**320.** The greatest integer function  $[x]$  is continuous everywhere?..

 [Watch Video Solution](#)

**321.** Find  $\frac{dy}{dx}$  when  $2x+3y = \cos x$ .

 [Watch Video Solution](#)

322. The derivative of  $\cos^{-1} x$  is.....

 [Watch Video Solution](#)

323. Differentiate  $e^{\sin^{-1}x}$ , w. r. t.  $x$

 [Watch Video Solution](#)

324. If  $y = \log(\operatorname{cose}^x)$ , then  $\frac{dy}{dx} = \dots\dots\dots$

 [Watch Video Solution](#)

325. Find  $\frac{d^2y}{dx^2}$  when  $y = \log x + x$ .

 [Watch Video Solution](#)

326. Find  $\frac{d^2y}{dx^2}$  when  $y = e^x + \cos x$

 [Watch Video Solution](#)

327. Verify Rolle's theorem for  $f(x) = x, x \in [1, 2]$

 [Watch Video Solution](#)

328. Verify LMV theorem :  $f(x) = x(x - 2) \in [1, 3]$ .

 [Watch Video Solution](#)

Exercise

1. If  $f(x) = \begin{cases} kx^2 & x < 2 \\ 3 & x \geq 2 \end{cases}$  is continuous at  $x = 2$ , then the value of 'k' is :

 [Watch Video Solution](#)

2. Check the continuity of the function f given by  $f(x) = 2x + 3$  at  $x = 1$

 [Watch Video Solution](#)

3. Check the continuity of the following functions:  $f(x) = x^2$  at  $x = 0$

 [Watch Video Solution](#)

4. Examine the continuity of the function  $f(x) = 2x^2 - 1$  at  $x = 3$



[Watch Video Solution](#)

5. Examine the function  $f(x) = 2x^2 - 5$  for its continuity at the point  $x = 3$ .



[Watch Video Solution](#)

6. Is the function defined by  $f(x) = |x|$ , a continuous function?



[Watch Video Solution](#)

7. Find the point at which the function  $f(x) = [x]$  is not continuous in  $(-1, 4)$ . ( $[x]$  is the largest function).



[Watch Video Solution](#)

8. Examine the following function for continuity:  $f(x) = x - 5$

 [Watch Video Solution](#)

9. Examine the following functions for continuity:  $f(x) = x^3 + x^2 - 1$

 [Watch Video Solution](#)

10. Examine the following function for continuity:  $f(x) = \frac{1}{x - 5}, x \neq 5$

 [Watch Video Solution](#)

11. Examine the following function for continuity:

$$f(x) = \frac{x^2 - 25}{x + 5}, x \neq -5$$

 [Watch Video Solution](#)

12. Examine the following function for continuity:  $f(x) = |x - 5|$

 [Watch Video Solution](#)

13. Prove that the following functions are continuous at all points of their domains:  $f(x) = \cos x$

 [Watch Video Solution](#)

14. Prove that the following functions are continuous at all points of their domains:  $f(x) = e^x + e^{-x}$

 [Watch Video Solution](#)

15. Prove that the following functions are continuous at all points of their domains:  $f(x) = \tan x$



[Watch Video Solution](#)

16. Discuss the continuity of the following function:

$$f(x) = \sin x + \cos x$$



[Watch Video Solution](#)

17. Discuss the continuity of the following function:

$$f(x) = \sin x \cdot \cos x$$



[Watch Video Solution](#)

18. Discuss the continuity of the following function:

$$f(x) = \sin x \cdot \cos x$$



[Watch Video Solution](#)



19. Discuss the continuity of the following functions:

$$f(x) = \frac{\sin x}{\cos x}$$



Watch Video Solution

20. Prove that  $f(x) = |\sin x|$  is continuous at all point of its dominin.



Watch Video Solution

21. Examine if  $\sin |x|$  is a continuous function.



Watch Video Solution

22. Is the function defined by  $f(x) = x^2 - \sin x + 5$  continuous at

$$x = \pi$$



Watch Video Solution

 Watch Video Solution

23. Show that  $f(x) = x - |x|, x \in R$  is continuous at  $x=0$

 Watch Video Solution

24. Find all points of discontinuity of  $f$ , where  $f$  is defined by :

$$f(x) = \begin{cases} x + 1 & x \geq 1 \\ x^2 + 1 & x < 1 \end{cases}$$

 Watch Video Solution

25. Find all points of discontinuity of  $f$ , where  $f$  is defined by :

$$f(x) = \begin{cases} x^3 - 3 & x \leq 2 \\ x^2 + 1 & x > 2 \end{cases}$$

 Watch Video Solution

26. Find all points of discontinuity of  $f$ , where  $f$  is defined by :

$$f(x) = \begin{cases} x^{10} - 1 & x \leq 1 \\ x^2 & x > 1 \end{cases}$$

 [Watch Video Solution](#)

27. Find all the points of discontinuity of  $f$ , where  $f$  is defined by

$$f(x) = \begin{cases} 2x + 3, & \text{if } x \leq 2 \\ 2x - 3, & \text{if } x > 2 \end{cases}$$

 [Watch Video Solution](#)

28. Find all points of discontinuity of  $f$ , where  $f$  is defined by :

$$f(x) = \begin{cases} \frac{|x|}{x} & \text{if } x \neq 0 \\ 0 & \text{if } x = 0 \end{cases}$$

 [Watch Video Solution](#)

29. Find all points of discontinuity of  $f$ , where  $f$  is defined by:

$$f(x) = \begin{cases} \frac{x}{|x|} & \text{if } x < 0 \\ -1 & \text{if } x \geq 0 \end{cases}$$

 [Watch Video Solution](#)

30. Discuss the continuity of the function defined by:

$$\begin{cases} x + 5 & \text{if } x \leq 1 \\ x - 5 & \text{if } x > 1 \end{cases}$$

 [Watch Video Solution](#)

31. Is the function  $f$  defined by  $f(x) = \begin{cases} x & \text{if } x \leq 1 \\ 5 & \text{if } x > 1 \end{cases}$

continuous at,  $x=0$ ? At  $x=1$ ? At  $x=2$  ?

 [Watch Video Solution](#)

32. Show that the function:

$$\begin{cases} x^3 + 3 & \text{if } x \neq 0 \\ 1 & \text{if } x = 0 \end{cases} \text{ is not continuous at } x = 0.$$

 [Watch Video Solution](#)

33. Discuss the continuity of the function  $f$  defined by

$$f(x) = \frac{1}{x}, x \neq 0$$

 [Watch Video Solution](#)

34. Discuss the continuity of the function  $f$  given by:

$$f(x) = \begin{cases} x & \text{if } x \geq 0 \\ x^2 & \text{if } x < 0 \end{cases}$$

 [Watch Video Solution](#)

35. Discuss the continuity of the function defined by:

$$f(x) = \begin{cases} x + 2 & \text{if } x < 0 \\ -x + 2 & \text{if } x > 0 \end{cases}$$

 [Watch Video Solution](#)

36. Discuss the continuity of the function:

$$f(x) = \begin{cases} 1 + x^2 & 0 \leq x \leq 1 \\ 2 - x & x > 1 \end{cases} \quad \text{at } x=1$$

 [Watch Video Solution](#)

37. Examine the continuity of the function  $f(x) = \begin{cases} x + 1 & x \leq 2 \\ 2x - 1 & x > 2 \end{cases}$  at  $x = 2$

 [Watch Video Solution](#)

**38.** Discuss the continuity of the function  $f(x)$  at  $x = 5$ , if

$$f(x) = \begin{cases} \frac{x^2-25}{x-5}, & \text{if } x \neq 5 \\ 10, & \text{if } x = 5 \end{cases}$$

 [Watch Video Solution](#)

**39.** Discuss the continuity of the function

$$f(x) = \begin{cases} \frac{|x-2|}{2-x}, & x \neq 2 \\ -1, & x = 2 \end{cases} \text{ at } x = 2.$$

 [Watch Video Solution](#)

**40.** Discuss the continuity of the function

$$f(x) = \begin{cases} \frac{|x-2|}{2-x}, & x \neq 2 \\ -1, & x = 2 \end{cases} \text{ at } x = 2.$$



[Watch Video Solution](#)

41. Discuss the continuity of the function :

$$f(x) = \begin{cases} \frac{|x-a|}{x-a} & \text{when } x \neq a \\ 1 & \text{when } x = a \end{cases} \quad \text{at } x = a$$



[Watch Video Solution](#)

42. Discuss the continuity of the function :

$$f(x) = \begin{cases} -2 & \text{if } 0 \leq x \leq 1 \\ 4 & \text{if } 1 < x < 3 \\ 5 & \text{if } 3 \leq x \leq 10 \end{cases}$$



[Watch Video Solution](#)



43. Differentiation of the function :

$$f(x) = 4x + 3$$

 [Watch Video Solution](#)

44. Show that the following function are continuous at  $x=0$ :

$$f(x) = |x|\cos\left(\frac{1}{x}\right) \text{ or } x \neq 0 \text{ } f(0) = 0$$

 [Watch Video Solution](#)

45. Show that the following function are continuous at  $x=0$ :

$$f(x) = \begin{cases} x\cos\left(\frac{1}{x}\right) & \text{when } x \neq 0 \\ 0 & \text{when } x = 0 \end{cases}$$

 [Watch Video Solution](#)

46. Test the continuity of the following functions at indicated points :

$$f(x) = \begin{cases} x^2 \sin \frac{1}{x}, & x \neq 0 \\ 0, & x = 0 \end{cases} \text{ at } x = 0$$

 [Watch Video Solution](#)

47. Examine the continuity of the function 'f' at  $x = 0$ , if  $f(x) = \begin{cases} x \sin(1/x), & (x \neq 0) \\ 0, & (x = 0) \end{cases}$

 [Watch Video Solution](#)

48. Examine the continuity of the function  $f(x)$  at  $x = 0$ ,

$$f(x) = \begin{cases} \frac{|\sin x|}{x} & \text{when } x \neq 0 \\ 1 & \text{when } x = 0 \end{cases}$$

 [Watch Video Solution](#)

49. Discuss the continuity of the function defined by

$$f(x) = \begin{cases} \frac{\tan 2x}{3x}, & x \neq 0 \\ \frac{3}{2}, & x = 0 \end{cases}$$

 [Watch Video Solution](#)

50. Discuss the continuity of the cosine, cosecant, secant and cotangent functions.

 [Watch Video Solution](#)

51. Test the continuity of the following functions at indicated points :

$$f(x) = \begin{cases} (x - a)\cos\frac{1}{x-a}, & x \neq a \\ 0, & x = a \end{cases} \text{ at } x = a$$

 [Watch Video Solution](#)

**52.** Examine the function for continuity at  $x = 0$ :

$$f(x) = \begin{cases} \frac{\sin x}{x} & \text{when } x < 0 \\ x + 1 & \text{when } x \geq 0 \end{cases}$$

 [Watch Video Solution](#)

**53.** Discuss the continuity of  $f(x)$  at  $x = 0$  if:

$$f(x) = \begin{cases} \frac{\sqrt{1+x} - \sqrt{1-x}}{\sin x} & \text{when } x \neq 0 \\ 0 & \text{when } x = 0 \end{cases}$$

 [Watch Video Solution](#)

**54.** In the following, determine the constant so that given function is continuous at indicated point:

$$f(x) = \begin{cases} kx^2 & \text{if } x \leq 2 \\ 2 & \text{if } x > 2 \end{cases} \text{ at } x=2$$

 [Watch Video Solution](#)

**55.** In the following, determine the constant so that given function is continuous at indicated point:

$$f(x) = \begin{cases} kx + 1 & \text{if } x \leq \pi \\ \cos x & \text{if } x > \pi \end{cases} \text{ at } x = \pi$$

 [Watch Video Solution](#)

**56.** In the following, determine the constant so that given function is continuous at indicated point:

$$f(x) = \{(kx + 5, \text{ when } x \leq 2), (x - 1), \text{ when } x > 2\} \text{ at } x=2$$



[Watch Video Solution](#)

**57.** In the following, determine the constant so that given function is continuous at indicated point:

$$f(x) = \begin{cases} (3k - 2x), & \text{when } x < 1 \\ (2k + 1), & \text{when } x \geq 1 \end{cases} \text{ at } x = 1$$



[Watch Video Solution](#)

**58.** In the following, determine the constant so that given function is continuous at indicated point:

$$f(x) = \begin{cases} (3x - 8), & \text{if } x \leq 5 \\ (2k), & \text{if } x > 5 \end{cases} \text{ at } x = 5$$



[Watch Video Solution](#)

**59.** In the following, determine the constant so that given function is continuous at indicated point:

$$f(x) = \begin{cases} \frac{\sin 2x}{5x} & \text{when } x \neq 0 \\ m & \text{when } x = 0 \end{cases} \text{ at } x=0$$

 [Watch Video Solution](#)

**60.** Find the values of  $k$  so that the function  $f$  is continuous at the

$$\text{indicated point : } f(x) = \begin{cases} k \frac{\cos x}{\pi - 2x} & \text{if } x \neq \frac{\pi}{2} \\ 3 & \text{if } x = \frac{\pi}{2} \end{cases} \text{ at } x = \frac{\pi}{2}$$

 [Watch Video Solution](#)

**61.** In the following, determine the constant so that given function is continuous at indicated point:

$$f(x) = \begin{cases} \frac{x^2 - 3x + 2}{x - 1} & \text{if } x \neq 1 \\ k & \text{if } x = 1 \end{cases} \text{ at } x=1$$



Watch Video Solution

**62.** In the following, determine the constant so that given function is continuous at indicated point:

$$f(x) = \begin{cases} \frac{x^2-1}{x-1} & \text{if } x \neq 1 \\ k & \text{if } x = 1 \end{cases} \text{ at } x=1$$



Watch Video Solution

**63.** For what value of 'k' is the function defined by

$$f(x) = \begin{cases} k(x^2 + 2) & \text{if } x \leq 0 \\ 3x + 1 & \text{if } x > 0 \end{cases} \text{ continuous at } x = 0? \text{ Also write}$$

whether the function is continuous at  $x = 1$ .



Watch Video Solution



64. If the function defined by :

$$f(x) = \begin{cases} 2x - 1 & x < 2 \\ a & x = 2 \\ x + 1 & x > 2 \end{cases}$$
 is continuous at  $x = 2$ , find the value of 'a'. Also

discuss the continuity of  $f(x)$  at  $x = 3$ .

 [Watch Video Solution](#)

65. If the following function  $f(x)$  is continuous at  $x = 0$ , find the value of 'a':

$$f(x) = \begin{cases} \left( \frac{1 - \cos 4x}{x} \right)^2, & x < 0 \\ a, & x = 0 \\ \left( \frac{\sqrt{x}}{\sqrt{16 + \sqrt{x}} - 4} \right), & x > 0 \end{cases}$$

 [Watch Video Solution](#)

66. Determine the constants 'a' and 'b' so that the function 'f' defined below is continuous everywhere:

$$f(x) = \begin{cases} 5, & \text{if } x \leq 2 \\ ax + b, & \text{if } 2 < x < 10 \\ 21, & \text{if } x \geq 10 \end{cases}$$

 [Watch Video Solution](#)

**67.** Determine the constants 'a' and 'b' so that the function 'f' defined below is continuous everywhere:

$$f(x) = \begin{cases} x + 2 & x \leq 2 \\ ax + b & 2 < x < 5 \\ 3x - 2 & x \geq 5 \end{cases}$$

 [Watch Video Solution](#)

**68.** If the function  $f(x)$  given by:

$$f(x) = \begin{cases} 2ax + b & \text{if } x > 1 \\ 9 & \text{if } x = 1 \\ 6ax - 2b & \text{if } x < 1 \end{cases}$$
 is continuous at  $x=1$ , find the values 'a'

and 'b'.

 [Watch Video Solution](#)

69. Find the values of  $a$  and  $b$  so that the following function is continuous at  $x = 3$  and  $x=5$ :

$$f(x) = \begin{cases} 1 & \text{if } x \leq 3 \\ ax + b & \text{if } 3 < x < 5 \\ 7 & \text{if } 5 \leq x \end{cases}$$

 [Watch Video Solution](#)

70. Find 'a' and 'b' if the function:

$$f(x) = \begin{cases} \frac{\sin x}{x} & -2 \leq x < 0 \\ a \cdot 2^x & 0 \leq x \leq 1 \\ b + x & 1 < x \leq 2 \end{cases} \text{ is a continuous function on } [-2,2]$$

 [Watch Video Solution](#)

71. Find the values of 'p' and 'q' for which:

$$f(x) = \begin{cases} \left( \frac{1 - \sin^3 x}{3\cos^2 x}, & \text{if } x < \frac{\pi}{2} \right), \\ p, & \text{if } x = \frac{\pi}{2}, \\ \left( \frac{q(1 - \sin x)}{(\pi - 2x)^2}, & \text{if } x > \frac{\pi}{2} \right) \end{cases}$$

is continuous at  $x = \pi/2$

 [Watch Video Solution](#)

72. The function  $f(x)$  is defined as follows:

$$f(x) = \begin{cases} x^2 + ax + b & 0 \leq x < 2 \\ 3x + 2 & 2 \leq x \leq 4 \\ 2ax + 5b & 4 < x \leq 8 \end{cases}$$

If  $f(x)$  is continuous on  $[0,8]$ , find the

values of 'a' and 'b'.

 [Watch Video Solution](#)

**73.** A man is driving a car on the dangerous path given by:

$$f(x) = \begin{cases} \frac{1-x^m}{1-x} & x \neq 1 \\ m-1 & x = 1 \end{cases}, m \in \mathbb{N}. \text{ Find the dangerous point (point of}$$

discontinuity) on the path. Whether the driver should pass that point or not? Justify your answer?

 [Watch Video Solution](#)

**74.** Find all the points of discontinuity of the function  $f$  defined by

$$f(x) = \begin{cases} x + 2 & \text{if } x < 1 \\ 0 & \text{if } x = 1 \\ x - 2 & \text{if } x > 1 \end{cases}$$

 [Watch Video Solution](#)

75. Find all points of discontinuity of  $f$ , where  $f$  is defined by :  $f(x) =$

$$\begin{cases} |x|+3, & \text{if } x \leq -3 \\ -2x, & \text{if } -3 < x \end{cases}$$

 [Watch Video Solution](#)

76. Find all the points of discontinuity of  $f$ , where  $f$  is defined by

$$f(x) = \begin{cases} 2x + 3, & \text{if } x \leq 2 \\ 2x - 3, & \text{if } x > 2 \end{cases}$$

 [Watch Video Solution](#)

77. Show that the following functions are continuous:

$$f(x) = \sin(x^2)$$

 [Watch Video Solution](#)

**78.** Show that the following functions are continuous:

$$f(x) = \cos(x^2)$$



**Watch Video Solution**

**79.** Show that the following functions are continuous:

$$f(x) = |\cos x|$$



**Watch Video Solution**

**80.** Show that the function 'f' given by:

$$f(x) = |x| + |x - 1|, x \in R \text{ is continuous both at } x = 0 \text{ and } x=1$$



**Watch Video Solution**

**81.** Show that the function 'f' given by:

$$f(x) = |x - 1| + |x - 2|, x \in R \text{ is continuous both at } x=1 \text{ and } x=2$$

 [Watch Video Solution](#)

**82.** Locate the points of discontinuity of the function:

$$f(x) = \begin{cases} \frac{x^4 - 16}{x - 2} & \text{if } x \neq 2 \\ 16 & \text{if } x = 2 \end{cases}$$

 [Watch Video Solution](#)

**83.** Examine the derivability of the following functions at the specified points:

$$|x| \text{ at } x=0$$

 [Watch Video Solution](#)



**84.** Examine the derivability of the following functions at the specified points:

$[x]$  at  $x=1$

 [Watch Video Solution](#)

**85.** Examine the derivability of the following functions at the specified points:

$|x|^2 \sin x = 0$

 [Watch Video Solution](#)

**86.** Examine the derivability of the following functions at the specified points:

$x^3 \sin x = 2$

 [Watch Video Solution](#)

 Watch Video Solution

87. If 'f' is differentiable at  $x = a$ , find  $\left( \lim_{x \rightarrow a} \frac{x^2 f(a) - a^2 f(x)}{x - a} \right)$

 Watch Video Solution

88. If  $F(x) = f(Ax)$  and  $f(ax)$  is differentiable, then prove that  $F'(x) = af'(ax)$ ,  $a \neq 0$

 Watch Video Solution

89. If  $f(x) = \begin{cases} x \sin\left(\frac{1}{x}\right) & x \neq 0 \\ 0 & x = 0 \end{cases}$  Show that 'f' is not differentiable at  $x = 0$

 Watch Video Solution

90. Show that the function defined by:

$$f(x) = \begin{cases} 3 - 2x & \text{if } x < 2 \\ 3x - 7 & \text{if } x \geq 2 \end{cases} \text{ is not derivable at } x = 2.$$

 [Watch Video Solution](#)

91. Discuss the continuity of  $f(x)$  at  $x = 0$ , when:

$$f(x) = \begin{cases} \frac{e^{1/x} - 1}{e^{1/x} + 1} & x \neq 0 \\ 0 & x = 0 \end{cases}$$

 [Watch Video Solution](#)

92. Show that the function:

$$f(x) = \begin{cases} 2 + x & \text{if } x \geq 0 \\ 2 - x & \text{if } x < 0 \end{cases} \text{ is continuous but not derivable at } x = 0$$

 [Watch Video Solution](#)

**93.** Show that the function 'f' defined as follows, is continuous at  $x = 2$ , but not differentiable there at:

$$f(x) = \begin{cases} 3x - 2 & 0 < x \leq 1 \\ 2x^2 - x & 1 < x \leq 2 \\ 5x - 4 & x > 2 \end{cases}$$

[Watch Video Solution](#)

**94.** The function 'f' defined as:

$$f(x) = \begin{cases} x^2 + 3x + a & \text{if } x \leq 1 \\ bx + 2 & \text{if } x > 1 \end{cases} \text{ is derivable for every } x, \text{ Find the}$$

values of 'a' and 'b'.

[Watch Video Solution](#)

95. For what values of 'a' and 'b' the function:

$$f(x) = \begin{cases} x^2 & x \leq c \\ ax + b & x > c \end{cases} \text{ is differentiable at } x = c.$$



[Watch Video Solution](#)

96. Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  ( $\mathbb{R}$  is the set of real numbers) be defined as follows:

$$f(x) = \begin{cases} (2 - x, & \text{if } 1 \leq x \leq 2), \\ \left(x - \frac{1}{2}x^2, & \text{if } x \geq 2 \right) \end{cases}: \text{ Examine the}$$

continuity and differentiability of  $f(x)$  at  $x=2$ .



[Watch Video Solution](#)

97. Show that  $f(x) = |x-3|$ ,  $x$  in  $\mathbb{R}$  is continuous but not differentiable at  $x=3$ .



[Watch Video Solution](#)

**98.** Write an example of a function, which is continuous everywhere but fails to be differentiable at exactly five points.

 [Watch Video Solution](#)

**99.** Use Chain Rule to find the derivatives of the following:

$$f(x) = (1 - 2x)^2$$

 [Watch Video Solution](#)

**100.** Find the derivatives of the following:

$$f(x) = (x^2 + 3x + 4).$$

 [Watch Video Solution](#)

**101.** Use Chain Rule to find the derivatives of the following:

$$f(x) = (3x^2 + 2)^3(5x - 1)^2$$



[Watch Video Solution](#)

**102.** Use Chain Rule to find the derivatives of the following:

$$f(x) = (2x^2 + 3)^{\frac{5}{3}}(x + 5)^{-\frac{1}{3}}$$



[Watch Video Solution](#)

**103.** Use Chain Rule to find the derivatives of the following:

$$f(x) = \frac{3}{2 - x}, x \neq 2$$



[Watch Video Solution](#)

**104.** Find the derivatives of the following:

$$h(x) = (x + 1)(x + 2)(x + 3)$$



**Watch Video Solution**

**105.** Use Chain Rule to find  $\frac{dy}{dx}$ , if  $y = \left( \frac{3x - 1}{(3x + 1)^2} \right)$



**Watch Video Solution**

**106.** Find  $\frac{dy}{dx}$ , if  $y = (4x^3 - 5x^2 + 1)$



**Watch Video Solution**

**107.** Find  $\frac{dy}{dx}$ , if  $y = 1 - 2\left(\frac{5x}{3x + 2}\right)^2 + \left(\frac{5x}{3x + 2}\right)^3$





 [Watch Video Solution](#)

**108.** Differentiate the following w.r.t.  $x$ :

$$\sin(x^2)$$

 [Watch Video Solution](#)

**109.** Differentiate the following w.r.t.  $x$ :

$$\sin(x^2 + 5)$$

 [Watch Video Solution](#)

**110.** Differentiate the following w.r.t.  $x$ :

$$\tan(3x+5)$$

 [Watch Video Solution](#)

**111.** Differentiate the following w.r.t.  $x$ :

$$\sin x^0$$



[Watch Video Solution](#)

**112.** Differentiate the following w.r.t.  $x$ :

$$\sin^4(ax + b)^2$$



[Watch Video Solution](#)

**113.** Differentiate the following w.r.t.  $x$ :

$$\sin(\cot x)$$



[Watch Video Solution](#)

**114.** Differentiate the following w.r.t.  $x$ :

$$\sin^2(x^5)$$



[Watch Video Solution](#)

**115.** Differentiate the following w.r.t.  $x$ :

$$\cos^2(x^3)$$



[Watch Video Solution](#)

**116.** Differentiate the following w.r.t.  $x$ :

$$\cos x^3 \cdot \sin^2(x^5)$$



[Watch Video Solution](#)

**117.** Differentiate the following w.r.t.  $x$ :

$$2\sqrt{\cot(x^2)}$$

 [Watch Video Solution](#)

**118.** Differentiate the following w.r.t.  $x$ :

$$\sqrt{3x+2} + \frac{1}{\sqrt{2x^2+4}}$$

 [Watch Video Solution](#)

**119.** Differentiate the following w.r.t.  $x$ :

$$\sqrt{10x^2 + x + 1}$$

 [Watch Video Solution](#)

120. Differentiate the following w.r.t. x:

$$\frac{\sin(ax - b)}{\cos(cx - d)}$$

 Watch Video Solution

121. Cos(a cos x + b sin x), for some constants 'a' and 'b'.

 Watch Video Solution

122. If  $y = \sin(ax^2 + bx + c)$ , then find  $\frac{dy}{dx}$

 Watch Video Solution

123. Find  $\frac{dy}{dx}$  if:

$$y = 9u^2, u = 1 - \frac{3}{2}x^2$$

 Watch Video Solution

124. Find  $\frac{dy}{dx}$  if :

$$y = \frac{3 - v}{2 + v}, v = \frac{4x}{1 - x^2}$$

 Watch Video Solution

125. Find  $\frac{dy}{dx}$  if :

$$y = at^2, t = \frac{x}{2a}$$

 Watch Video Solution

126. If  $x^{16} \cdot y^9 = (x^2 + y)^{17}$ , prove that  $\frac{dy}{dx} = \frac{2y}{x}$ .

 Watch Video Solution

**127.** Differentiate the following w.r.t.  $x$ :

$$|2x-1|$$



**Watch Video Solution**

**128.** Differentiate the following w.r.t.  $x$ :

$$|2x^2 - 3|$$



**Watch Video Solution**

**129.** If  $y + \sin y = \cos x$ , then find the values of ' $y$ ' for which  $\frac{dy}{dx}$  is valid.



**Watch Video Solution**

**130.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$x - y = \pi$$



[Watch Video Solution](#)

**131.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 2003$$



[Watch Video Solution](#)

**132.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$x^3 + x^2y + xy^2 + y^3 = 81$$



[Watch Video Solution](#)



**133.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$x^3 + 2x^2y + 3xy^2 + 4y^3 = 5$$



[Watch Video Solution](#)

**134.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$2x+3y=\sin x$$



[Watch Video Solution](#)

**135.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$2x+3y= \sin y.$$



[Watch Video Solution](#)

**136.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$ax + by^2 = \cos y$$



[Watch Video Solution](#)

**137.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$xy + y^2 = \tan x + y$$



[Watch Video Solution](#)

**138.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$\sin^2 y + \cos xy = \pi$$



[Watch Video Solution](#)

**139.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$\frac{1}{x} - \frac{1}{y} - 10 = 0$$



**Watch Video Solution**

**140.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$\sqrt{x} + \sqrt{y} = 20$$



**Watch Video Solution**

**141.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$y(y+1)=x(x+1)(x+2)$$



**Watch Video Solution**

**142.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$x^2 = \frac{x + 3y}{x - 3y}$$



[Watch Video Solution](#)

**143.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$\frac{y}{x + y} = 3 + x^3$$



[Watch Video Solution](#)

**144.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$y^2 = 4ax$$



[Watch Video Solution](#)

**145.** Find the derivative of  $y$  w.r.t  $x$  in each of the following:

$$y = \frac{4}{3}x^{3/4}$$



**Watch Video Solution**

**146.** Find the derivative of  $f(x)$  w.r.t  $x$  in the following:

$$f(x) = \sqrt[3]{2x^4 + x^2 - x}$$



**Watch Video Solution**

**147.** Find the derivative of  $f(x)$  w.r.t  $x$  in the following:

$$f(x) = \sqrt[3]{ax + b}$$



**Watch Video Solution**

**148.** Find the derivative of  $f(x)$  w.r.t  $x$  in the following:

$$f(x) = (x^2 + x + 5)^{1/3} (x^3 + 1)^{2/3}$$

 [Watch Video Solution](#)

**149.** Find the derivative of  $f(x)$  w.r.t  $x$  in the following:

$$g(x) = \sqrt[3]{5x - 9} \sqrt[3]{3x - 4}$$

 [Watch Video Solution](#)

**150.** Obtain  $\frac{dy}{dx}$  when:

$$x^2 + y^2 + 2axy = 0$$

 [Watch Video Solution](#)

151. Obtain  $\frac{dy}{dx}$  when:

$$x^3 + y^3 + 3axy = 0$$



Watch Video Solution

152. Obtain  $\frac{dy}{dx}$  when:

$$x^2 + y^2 + 2gx + 2fy + c = 0$$



Watch Video Solution

153. Obtain  $\frac{dy}{dx}$  when:

$$x^4 + y^4 + 4xy - 100 = 0$$



Watch Video Solution

154. If  $x\sqrt{1+y} + y\sqrt{1+x} = 0$  for  $x$  lies between  $-1$  and  $1$  prove that  $dy/dx = -1/(1+x)^2$

 [Watch Video Solution](#)

155. If  $y = \sqrt{x} + \frac{1}{\sqrt{x}}$ , then show that  $2x \frac{dy}{dx} + y = 2\sqrt{x}$

 [Watch Video Solution](#)

156. Find  $\frac{dy}{dx}$  for each of the following:

$$y = (x^2 + 3x + 5)(x^2 - 2)^2$$

 [Watch Video Solution](#)



157. Find  $\frac{dy}{dx}$  for each of the following:

$$y = \left( \sqrt{x} + \frac{1}{\sqrt{x}} \right) (1 + x + x^2)$$

 [Watch Video Solution](#)

158. Find  $\frac{dy}{dx}$  for each of the following:

$$y = \left( \frac{x - \sqrt{x}}{1 - 2x} \right)^2$$

 [Watch Video Solution](#)

159. Find  $\frac{dy}{dx}$  for each of the following:

$$y = \left( \frac{1}{1+x} \right) \left( x^{-2} + \frac{2}{x} - 1 \right) + \sqrt[3]{x} - \frac{1}{\sqrt[3]{x}}$$

 [Watch Video Solution](#)

160. Find  $\frac{dy}{dx}$  for each of the following:

$$y = \sqrt[3]{x^2(x^2 + 3)}$$

 [Watch Video Solution](#)

161. If  $\cos y = x \cos(a + y)$ , with  $\cos a \neq \pm 1$ , prove that

$$\frac{dy}{dx} = \frac{\cos^2(a + y)}{\sin a}$$

 [Watch Video Solution](#)

162. If  $\sin y = x \sin(a + y)$ , then show that:  $\frac{dy}{dx} = \frac{\sin a}{1 - 2x \cos a + x^2}$

 [Watch Video Solution](#)

**163.** Differentiate the following w.r.t.  $x$ :

$$\tan^{-1}\sqrt{x}$$



**Watch Video Solution**

**164.** Differentiate the following w.r.t.  $x$ :

$$\cos^{-1}\left(\frac{x}{x+1}\right)$$



**Watch Video Solution**

**165.** Differentiate the following w.r.t.  $x$ :

$$\sin^{-1}(x\sqrt{x}), 0 \leq x \leq 1$$



**Watch Video Solution**

**166.** Differentiate the following w.r.t.  $x$ :

$$\left(\tan^{-1}x\right)^2$$



[Watch Video Solution](#)

**167.** Differentiate the following w.r.t.  $x$ :

$$x \sec^{-1}x$$



[Watch Video Solution](#)

**168.** Differentiate the following w.r.t.  $x$ .

$$\cos^{-1}(\sin x)$$



[Watch Video Solution](#)

**169.** Differentiate the following w.r.t.  $x$ :

$$\tan(\sin^{-1}x)$$



**Watch Video Solution**

**170.** Differentiate the following w.r.t.  $x$ :

$$\sin^{-1}(2x)$$



**Watch Video Solution**

**171.** Differentiate the following w.r.t.  $x$ :

$$(\cot^{-1}x)^2$$



**Watch Video Solution**

172. Differentiate the following w.r.t. x:

$$\sin\left(2\sin^{-1}x\right)$$



Watch Video Solution

173. Differentiate the following w.r.t. x:

$$x\tan^{-1}x$$



Watch Video Solution

174. Differentiate the following w.r.t. x:

$$\tan^{-1}\left(\frac{\sin x}{1 + \cos x}\right)$$



Watch Video Solution

175. Differentiate the following w.r.t.  $x$ :

$$\tan^{-1}\left(\frac{\cos x}{1 + \sin x}\right)$$

 [Watch Video Solution](#)

176. Differentiate the following w.r.t.  $x$ :

$$\cot^{-1}\left(\frac{1 + \cos x}{\sin x}\right)$$

 [Watch Video Solution](#)

177. Differentiate the following w.r.t.  $x$ :

$$\sin^{-1}(1 - 2x^2)$$

 [Watch Video Solution](#)

**178.** Differentiate the following w.r.t.  $x$ :

$$\sin^{-1}\left(3x - 4x^3\right), \quad -\frac{1}{2} < x < \frac{1}{2}$$



**Watch Video Solution**

**179.** Differentiate the following w.r.t.  $x$ .

$$\cos^{-1}\left(4x^3 - 3x\right)$$



**Watch Video Solution**

**180.** Differentiate the following w.r.t.  $x$ :

$$\sin^{-1}\left(\frac{2x}{1+x^2}\right), \quad -1 < x < 1$$



**Watch Video Solution**



**181.** Differentiate the following w.r.t.x.

$$\operatorname{cosec}^{-1} \frac{1+x^2}{2x}$$

 [Watch Video Solution](#)

**182.** Differentiate the following w.r.t. x:

$$\sin^{-1} \left( \frac{1-x^2}{1+x^2} \right), 0 < x < 1$$

 [Watch Video Solution](#)

**183.** Differentiate the following w.r.t. x:

$$\cos^{-1} \left( \frac{1-x^2}{1+x^2} \right), 0 < x < 1$$

 [Watch Video Solution](#)

**184.** Differentiate the following w.r.t.  $x$ :

$$\cos^{-1}\left(2\frac{x}{1+x^2}\right), -1 < x < 1$$

 [Watch Video Solution](#)

**185.** Differentiate the following w.r.t.  $x$ :

$$\tan^{-1}\left(2\frac{x}{1-x^2}\right), 0 < x < 1$$

 [Watch Video Solution](#)

**186.** Differentiate the following w.r.t.  $x$ :

$$\tan^{-1}\left(\frac{3x-x^3}{1-3x^2}\right), -\frac{1}{\sqrt{3}} < x < \frac{1}{\sqrt{3}}$$

 [Watch Video Solution](#)

187. Differentiate the following w.r.t.  $x$ :  $\tan^{-1}\left(\frac{x^{1/3} + A^{1/3}}{1 - x^{1/3}a^{1/3}}\right)$

 [Watch Video Solution](#)

188. Differentiate the following w.r.t.  $x$ .

$$\tan^{-1}\left(\frac{x}{\sqrt{a^2 - x^2}}\right)$$

 [Watch Video Solution](#)

189. Differentiate the following w.r.t.  $x$ ,  $\tan^{-1}\left(\frac{\sqrt{1 + x^2} - 1}{x}\right)$

 [Watch Video Solution](#)

190. Differentiate the following w.r.t.  $x$ ,  $\tan^{-1}\left(\frac{\sqrt{1+x^2}-1}{x}\right)$

 [Watch Video Solution](#)

191. Differentiate the following w.r.t.  $x$ :

$$\cot^{-1}\left(\frac{1+x}{1-x}\right)$$

 [Watch Video Solution](#)

192. Differentiate the following w.r.t.  $x$ :

$$\cot^{-1}\left(\sqrt{1+x^2}+x\right)$$

 [Watch Video Solution](#)

**193.** Differentiate the following w.r.t.x.

$$\tan^{-1}(\sec x + \tan x)$$

 [Watch Video Solution](#)

**194.** Differentiate the following w.r.t. x:

$$\tan^{-1} \sqrt{\frac{1 - \cos x}{1 + \cos x}}$$

 [Watch Video Solution](#)

**195.** Differentiate the following w.r.t. x:  $\tan^{-1} \sqrt{\frac{1 + \sin x}{1 - \sin x}}$

 [Watch Video Solution](#)

196. Differentiate the following w.r.t.  $x$ :

$$\sin^{-1}x + \sin^{-1}\sqrt{1-x^2}, \quad -1 \leq x \leq 1$$

 [Watch Video Solution](#)

197. Differentiate the following w.r.t.  $x$ :

$$\sin^{-1}\left(\sqrt{\frac{1+x^2}{2}}\right)$$

 [Watch Video Solution](#)

198. If  $y = \cot^{-1}\left\{\frac{\sqrt{1+\sin x} + \sqrt{1-\sin x}}{\sqrt{1+\sin x} - \sqrt{1-\sin x}}\right\}$ ,  $0 < x < \frac{\pi}{2}$ , show that:

$\frac{dy}{dx}$  is independent of  $x$ .

 [Watch Video Solution](#)

199. Differentiate w.r.t  $x$  :  $\cot^{-1} \left\{ \frac{\sqrt{1 + \sin x} + \sqrt{1 - \sin x}}{\sqrt{1 + \sin x} - \sqrt{1 - \sin x}} \right\}$ ,  $0 < \theta < \frac{\pi}{2}$

 Watch Video Solution

200. If  $y = \tan^{-1} \left( \frac{5ax}{a^2 - 6x^2} \right)$ . Prove that  $\frac{dy}{dx} = \frac{3a}{a^2 + 9x^2} + \frac{2a}{a^2 + 4x^2}$

 Watch Video Solution

201. If  $y = \frac{\tan^{-1}(4x)}{1 + 5x^2} + \frac{\tan^{-1}(2 + 3x)}{3 - 2x}$ , prove that  $\frac{dy}{dx} = \frac{5}{1 + 25x^2}$

 Watch Video Solution

202. If  $f(x) = \tan^{-1}x$ ,  $g(x) = \tan^{-1} \left( \frac{1+x}{1-x} \right)$  for  $|x| < 1$ , show that  $f'(x) = g'(x)$  and  $g(x) - f(x) = \pi/4$



Watch Video Solution

203. If  $\sqrt{1-x^6} + \sqrt{1-y^6} = a^3(x^3 - y^3)$ , prove that :

$$\frac{dy}{dx} = \frac{x^2}{y^2} \sqrt{\frac{1-y^6}{1-x^6}}$$



Watch Video Solution

204. If  $y = \tan^{-1}(\cot x) + \cot^{-1}(\tan x)$ , then prove that :  $\frac{dy}{dx} + 2 = 0$



Watch Video Solution

205. Differentiate :  $\cos(2x + 3)$



Watch Video Solution



206. Differentiate:  $\cos x^2$



Watch Video Solution

207. Differentiate the following w.r.t.  $x$ :  $e^{-x}$



Watch Video Solution

208. Differentiate the following w.r.t.  $x$ :

$$e^{\cot^{-1}x^2}$$



Watch Video Solution

209. Differentiate the following w.r.t.  $x$ :

$$e^{m \log x}$$



Watch Video Solution

[Watch Video Solution](#)

**210.** Differentiate the following w.r.tx:

$$\sqrt{e^{\sqrt{x}}}, x > 0$$

 [Watch Video Solution](#)

**211.** Differentiate the following w.r.t x

$$\log(\log x), x > 1$$

 [Watch Video Solution](#)

**212.** Differentiate the following w.r.tx:

$$\log(\sin x)$$

 [Watch Video Solution](#)

213. Differentiate the following w.r.t.  $x$ :  $\log(\operatorname{cose}^x)$

 Watch Video Solution

214. Differentiate the following w.r.t.  $x$ :  $\sin(\tan^{-1}e^{-x})$

 Watch Video Solution

215. Differentiate the following w.r.t.  $x$ :

$$\frac{\cos x}{\log x}, x > 0$$

 Watch Video Solution

216. Differentiate the following w.r.t.  $x$ :

$$\sqrt{\tan x} \alpha^x$$

 Watch Video Solution

217. Differentiate the following w.r.t.  $x$ :  $e^{\cos x}$



[Watch Video Solution](#)

218. Differentiate the following w.r.t.  $x$ :

$$e^x \sin x$$



[Watch Video Solution](#)

219. Differentiate the following w.r.t.  $x$ :

$$x^{-1/3} e^x$$



[Watch Video Solution](#)

**220.** Differentiate the following w.r.tx:

$$x \sin x e^x$$



**Watch Video Solution**

**221.** Differentiate the following w.r.tx:

$$e^{\sin^{-1}(x+1)}$$



**Watch Video Solution**

**222.** Differentiate the following w.r.tx:

$$\tan\{\log(\sin x)\}$$



**Watch Video Solution**

**223.** Differentiate the following w.r.tx:

$$e^{\sin\sqrt{x}}$$

 [Watch Video Solution](#)

**224.** Differentiate the following w.r.tx:

$$e^{\cos^{-1}(x+1)}$$

 [Watch Video Solution](#)

**225.** Differentiate the following w.r.tx:

$$e^{\cos^{-1}x^2}$$

 [Watch Video Solution](#)

**226.** Differentiate the following w.r.tx:

$$\sqrt{1-x^2} \cdot e^{5x}$$

 [Watch Video Solution](#)

**227.** Differentiate the following w.r.tx:

$$e^{\sqrt{1-x^2}} \cdot \tan x$$

 [Watch Video Solution](#)

**228.** Differentiate the following w.r.tx:

$$\frac{\log x}{x}$$

 [Watch Video Solution](#)

**229.** Differentiate the following w.r.tx:

$$\frac{e^x}{x}$$

 [Watch Video Solution](#)

**230.** Differentiate the following w.r.tx:

$$\frac{\log x}{e^x}$$

 [Watch Video Solution](#)

**231.** Differentiate the following w.r.tx:

$$\log(\cos 5x)$$

 [Watch Video Solution](#)



**232.** Differentiate the following w.r.tx:

$$\frac{1}{\log \cos x}$$



**Watch Video Solution**

**233.** Differentiate the following w.r.tx:

$$(x^2 + 7x + 2)(e^x - \sin x)$$



**Watch Video Solution**

**234.** Differentiate the following w.r.tx:

$$e^{-3x} \sin^2 3x$$



**Watch Video Solution**

**235.** Differentiate the following w.r.tx:

$$e^{-x^2} \sin(\log x)$$

 [Watch Video Solution](#)

**236.** Differentiate the following w.r.tx:

$$\tan^{-1} \left( \frac{e^{2x} + 1}{e^{2x} - 1} \right)$$

 [Watch Video Solution](#)

**237.** Differentiate the following w.r.tx:

$$\log \left( (x + 3) + \sqrt{x^2 + 6x + 3} \right)$$

 [Watch Video Solution](#)

**238.** Differentiate the following w.r.t.x.  $\log\left(x + \sqrt{a^2 + x^2}\right)$

 [Watch Video Solution](#)

**239.** Differentiate the following w.r.tx:

$$x\sqrt{x^2 + 1} + \log\left(x + \sqrt{x^2 + 1}\right)$$

 [Watch Video Solution](#)

**240.** Differentiate the following w.r.tx:

$$\frac{e^x(x - 1)}{(x^2 + 1)}$$

 [Watch Video Solution](#)

**241.** Differentiate the following w.r.tx:

$$\frac{e^{ax}}{\sin(bx + c)}$$

 [Watch Video Solution](#)

**242.** Differentiate the following w.r.tx:

$$\frac{1}{3}e^x - 5e$$

 [Watch Video Solution](#)

**243.** Differentiate the following w.r.tx:

$$e^x + 2\cos x$$

 [Watch Video Solution](#)

**244.** Differentiate the following w.r.t.  $x$ :

$$x^2 e^x \sin x$$



**Watch Video Solution**

**245.** Differentiate the following w.r.t.  $x$ :

$$e^{\sec^2 x} + 3 \cos^{-1} x$$



**Watch Video Solution**

**246.** Differentiate the following w.r.t.  $x$ :

$$\log \left( \sin \sqrt{1 + x^2} \right)$$



**Watch Video Solution**

247. Differentiate the following w.r.t.  $x$ :  $\sin(\log x)$ ,  $x > 0$



Watch Video Solution

248. Differentiate the following w.r.t.  $x$ :

$$\log(\cos 5x)$$



Watch Video Solution

249. Differentiate the following w.r.t.  $x$ :

$$\cot\left(\log x + e^{\sqrt{x}}\right)$$



Watch Video Solution

250. Differentiate the following w.r.tx:

$$2l_n\left(\frac{x-1}{x+1}\right)$$

 [Watch Video Solution](#)

251. Differentiate the following w.r.tx:

$$x^2 l_n\left(\left(\sqrt{\frac{x^2+9}{x^2+4}}\right)\right)$$

 [Watch Video Solution](#)

252. Differentiate the following w.r.tx:

$$l_n(\sec x + \tan x)$$

 [Watch Video Solution](#)

**253.** Differentiate the following w.r.t.x:

$$\log\left(\frac{1+x}{1-x}\right)$$



**Watch Video Solution**

**254.** Differentiate the following w.r.t.x.

$$\log\tan\left(\frac{\pi}{4} + \frac{x}{2}\right)$$



**Watch Video Solution**

**255.** Differentiate the following w.r.t.x.

$$\sin^{-1}\left(2x\sqrt{1-x^2}\right)$$



**Watch Video Solution**



256. Find  $\frac{dy}{dx}$  if  $y = x^x$

 Watch Video Solution

257. Find  $\frac{dy}{dx}$  when:

$$xy + ce^{-y} + ye^x = x^2$$

 Watch Video Solution

258. If  $\frac{1}{2}(e^y - e^{-y}) = x$ , prove that  $\frac{dy}{dx} = \frac{1}{\sqrt{1+x^2}}$

 Watch Video Solution

259. If  $xy = e^{x-y}$ , prove that  $\frac{dy}{dx} = \frac{y(x-1)}{x(y+1)}$

 Watch Video Solution

260. If  $y = \frac{\sin^{-1}x}{\sqrt{1-x^2}}$ , prove that  $(1-x^2)\left(\frac{dy}{dx}\right) - xy = 1$

 [Watch Video Solution](#)

261. If  $x = \tan\left(\frac{1}{2}\log y\right)$ , then show that  $(1+x^2)\frac{d^2y}{dx^2} = (a-2x)\frac{dy}{dx}$ .

 [Watch Video Solution](#)

262. Differentiate  $\tan^{-1}\left(\frac{2^{x+1}}{1-4^x}\right)$  with respect to  $x$ .

 [Watch Video Solution](#)

263. If  $y = \log_{10}\sin x$ , prove that  $\frac{dy}{dx} = (\log_{10}e)\cot x$

 [Watch Video Solution](#)

264. If  $y = \sin[\sin(\log 3x)]$ . Find  $\frac{dy}{dx}$

 [Watch Video Solution](#)

265. Find, from first principle, the derivative of the following w.r.t.

x:

$$e^{2x}$$

 [Watch Video Solution](#)

266. Find, from first principle, the derivative of the following w.r.t.

x:

$$e^{\sqrt{x}}$$



Watch Video Solution

**267.** Differentiate the following w.r.t.  $x$ :  $e^{-x}$



Watch Video Solution

**268.** Find, from first principle , the derivative of the following w.r.t.

$x$ :

$$e^{\sin x}$$



Watch Video Solution

**269.** Find, from first principle , the derivative of the following w.r.t.

$x$ :

$$e^{\sqrt{\tan x}}$$



[Watch Video Solution](#)

**270.** Find, from first principle , the derivative of the following w.r.t.

x:

$\log(\sin x)$



[Watch Video Solution](#)

**271.** Find, from first principle , the derivative of the following w.r.t. x:

$\log(\cos x)$



[Watch Video Solution](#)

**272.** Find, from first principle , the derivative of the following w.r.t.

x:

$$\log x^2$$



[Watch Video Solution](#)

**273.** Find, from first principle , the derivative of the following w.r.t.

x:

$$\cos (\log x), \text{ where } x > 0$$



[Watch Video Solution](#)

**274.** Find  $\frac{dy}{dx}$ , if x and y are connected parametrically by the equations, given below without eliminating the parameter.

$$x = 2at^2, y = at^4$$



[Watch Video Solution](#)

**275.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = 4t, y = \frac{4}{t}$$

 [Watch Video Solution](#)

**276.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = -\frac{2t}{1+t^2}, y = \frac{1-t^2}{1+t^2}$$

 [Watch Video Solution](#)

**277.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = \frac{1 - t^2}{1 + t^2}, y = \frac{2t}{1 + t^2}$$

 [Watch Video Solution](#)

**278.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = \frac{a(1 + t^2)}{1 - t^2}, y = \frac{2t}{1 - t^2}$$

 [Watch Video Solution](#)

**279.** If  $x$  and  $y$  are connected parametrically by the equations given in Exercises 1 to 10, without eliminating the parameter, Find  $\frac{dy}{dx}$  :

$$x = \sin t, y = \cos 2t$$

 [Watch Video Solution](#)



**280.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = \log t, y = \sin t$$

 [Watch Video Solution](#)

**281.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = e^t \cos t, y = e^t \sin t. \text{ at } t = \frac{\pi}{2}$$

 [Watch Video Solution](#)

**282.** Find  $\frac{dy}{dx}$  in the following

$$x = a \cos \theta, y = a \sin \theta.$$

 [Watch Video Solution](#)

**283.** If  $x$  and  $y$  are connected parameterically by the equation ,  
without eliminating the parameter , find  $\frac{dy}{dx}$

$$x = a\cos(\theta), y = b\sin(\theta)$$

 [Watch Video Solution](#)

**284.** If  $x$  and  $y$  are connected parameterically by the equation ,  
without eliminating the parameter , find  $\frac{dy}{dx}$

$$x = a\cos(\theta), y = b\sin(\theta)$$

 [Watch Video Solution](#)

**285.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the  
equations, given below without eliminating the parameter.

$$x = a\cos^2\theta, y = b\sin^2\theta$$

 [Watch Video Solution](#)

**286.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = 2\cos^2\theta, y = 2\sin^2\theta$$



[Watch Video Solution](#)

**287.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = 2\cos^3\theta, y = 2\sin^3\theta$$



[Watch Video Solution](#)

**288.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = 3\cos^3\theta, y = 3\sin^3\theta$$

 [Watch Video Solution](#)

**289.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = c\tan\theta, y = c\cot\theta$$

 [Watch Video Solution](#)

**290.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = a(\theta + \sin\theta), y = a(1 - \cos\theta)$$

 [Watch Video Solution](#)

**291.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = a(\theta - \sin\theta), y = a(1 - \cos\theta)$$

 [Watch Video Solution](#)

**292.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = a(\theta - \sin\theta), y = a(1 + \cos\theta)$$

 [Watch Video Solution](#)

**293.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$y = a(\theta + \sin\theta), x = a(1 + \cos\theta)$$

 [Watch Video Solution](#)

**294.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = a(\theta - \sin\theta), y = a(1 + \cos\theta)$$

 [Watch Video Solution](#)

**295.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x\cos\theta - \cos 2\theta, y = \sin\theta - \sin 2\theta$$

 [Watch Video Solution](#)

**296.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = a(\cos\theta - \cos 2\theta), y = a(\sin\theta - \sin 2\theta)$$

 [Watch Video Solution](#)

**297.** If  $x$  and  $y$  are connected parametrically by the equations given

in Exercises 1 to 10, without eliminating the parameter, Find  $\frac{dy}{dx}$  :

$$x = a(\cos\theta + \theta\sin\theta), y = a(\sin\theta - \theta\cos\theta)$$

 [Watch Video Solution](#)

**298.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = \cos 2\theta + 2\cos\theta, y = \sin 2\theta - 2\sin\theta$$

 [Watch Video Solution](#)

**299.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$x = a\sin\theta, y = a\left(\cos\theta + \log\tan\left(\frac{\theta}{2}\right)\right)$$

 [Watch Video Solution](#)

**300.** Find  $\frac{dy}{dx}$ , if  $x$  and  $y$  are connected parametrically by the equations, given below without eliminating the parameter.

$$y = 12(1 - \cos t), x = 10(t - \sin t), -\frac{\pi}{2} < t < \frac{\pi}{2}$$

 [Watch Video Solution](#)

**301.** If  $x = 2\cos\theta - \cos 2\theta, y = 2\sin\theta - \sin 2\theta$ , find  $\frac{dy}{dx} \text{ at } \theta = \frac{\pi}{2}$

 [Watch Video Solution](#)



302. If  $x = a \left( \cos\theta + \log \tan \left( \frac{\theta}{2} \right) \right)$ ,  $y = a \sin\theta$  find  $\frac{dy}{dx}$  at  $\theta = \frac{\pi}{3}$

 [Watch Video Solution](#)

303. If  $x = ct$ ,  $y = \frac{c}{t}$ , find  $\frac{dy}{dx}$  at  $t = 2$

 [Watch Video Solution](#)

304. Find  $\frac{dy}{dx}$ , where  $x = t^3 + 1/t$  and  $y = (t + t^2)^3$

 [Watch Video Solution](#)

305. For a positive constant  $a$  find  $\frac{dy}{dx}$ , where

$$y = a^{t^+} \left( \frac{1}{t} \right), \text{ and } x = \left( t + \frac{1}{t} \right)^a$$



**306.** If  $(x = a\sin(2t)(1 + \cos(2t))$  and  $(y = b\cos(2t)(1 - \cos(2t))$ , then

show that  $\left( \left( \frac{dy}{dx} \right)_{t=\frac{\pi}{4}} = \frac{b}{a} \right)$ .

 Watch Video Solution

**307.** If  $x = \frac{1 + \log t}{t^2}$ ,  $y = \frac{3 + 2\log t}{t}$ ,  $t > 0$ , prove that

$$y \left( \frac{dy}{dx} \right) - 2x \left( \frac{dy}{dx} \right)^2 = 1$$

 Watch Video Solution

**308.** Find  $\frac{dy}{dx}$  in the following

$$x = e^{\theta}(\sin\theta + \cos\theta), y = e^{\theta}(\sin\theta - \cos\theta)$$

 [Watch Video Solution](#)

**309.** Differentiate the following w.r.t.  $x$ :

$$(\sqrt{x})^{\sqrt{x}}$$

 [Watch Video Solution](#)

**310.** Differentiate the following w.r.t.  $x$ :

$$\left(\frac{1}{x}\right)^x$$

 [Watch Video Solution](#)

**311.** Differentiate the following w.r.t.  $x$ :

$$(x^x)^x$$

 [Watch Video Solution](#)

**312.** Differentiate the following w.r.t.  $x$ :

$$x^{x^2}$$

 [Watch Video Solution](#)

**313.** Differentiate the following w.r.t.  $x$ :

$$(5x)^{3\cos 2x}$$

 [Watch Video Solution](#)

**314.** Differentiate the following w.r.t.  $x$ :

$$x^{\sin x}, x > 0$$

 [Watch Video Solution](#)

**315.** Differentiate the following w.r.t. x:

$$(\sin x)^x$$



**Watch Video Solution**

**316.** Differentiate the following w.r.t. x:

$$x^{\sin^{-1}}$$



**Watch Video Solution**

**317.** Differentiate the following w.r.t. x:

$$x^x \sin \sqrt{x}$$



**Watch Video Solution**

**318.** Differentiate the following w.r.t.  $x$ :

$$(\sin x)^{\log x}, \sin x > 0$$



[Watch Video Solution](#)

**319.** Differentiate the following w.r.t.  $x$ :

$$(\sin x)^{\tan x}$$



[Watch Video Solution](#)

**320.** Differentiate the following w.r.t.  $x$ :

$$(\sin x)^{\sin x}$$



[Watch Video Solution](#)

**321.** Differentiate the following w.r.t. x:

$$\left(\sec^2 x\right)^{1/x}$$



**Watch Video Solution**

**322.** Differentiate the following w.r.t. x:

$$(x \cos x)^x$$



**Watch Video Solution**

**323.** Differentiate the following w.r.t. x:

$$(x)^{\log x}$$



**Watch Video Solution**

**324.** Differentiate the following w.r.t.  $x$ :

$$(\log x)^{\log x}, x > 1$$



**Watch Video Solution**

**325.** Differentiate the following w.r.t.  $x$ :

$$x^{\sin 2x + \cos 2x}$$



**Watch Video Solution**

**326.** Differentiate the following w.r.t.  $x$ :

$$x^{\sin x + \cos x}$$



**Watch Video Solution**



**327.** Differentiate the following w.r.t. x:

$$(\log x)^x$$



**Watch Video Solution**

**328.** Differentiate the following w.r.t. x:

$$\left(\sin^{-1}x\right)^x$$



**Watch Video Solution**

**329.** Differentiate the following w.r.t. x:

$$\left(\tan^{-1}x\right)^x$$



**Watch Video Solution**

**330.** Differentiate the following w.r.t.  $x$ :

$$x^{\cos^{-1}x}$$

 [Watch Video Solution](#)

**331.** Differentiate the following w.r.t.  $x$ :

$$(\sin x)^{\cos^{-1}x}$$

 [Watch Video Solution](#)

**332.** Differentiate the following w.r.t.  $x$ :

$$(\sin x - \cos x)^{\sin x - \cos x}, \quad \frac{\pi}{4} < x < \frac{3\pi}{4}$$

 [Watch Video Solution](#)

**333.** Differentiate the following w.r.t.  $x$ :

$$\cos(x^x)$$



[Watch Video Solution](#)

**334.** Differentiate the following w.r.t.  $x$ :

$$(1 + x)^{\log x}$$



[Watch Video Solution](#)

**335.** Differentiate the following w.r.t.  $x$

$$(\log x)^{\cos x}$$



[Watch Video Solution](#)

**336.** Differentiate the following w.r.t.  $x$ :

$$x^{\sin x} + (\sin x)^x$$



**Watch Video Solution**

**337.** Differentiate the following w.r.t.  $x$ :

$$(x)^{\log x} + (\log x)^x$$



**Watch Video Solution**

**338.** Differentiate the following w.r.t.  $x$ .

$$x^{\tan x} + (\tan x)^x.$$



**Watch Video Solution**

**339.** Differentiate the following w.r.t.  $x$ :

$$x^{\cot x} + (\cos x)^{\sin x}$$

 [Watch Video Solution](#)

**340.** Differentiate the following w.r.t.  $x$ :

$$x^{\cos x} + (\cos x)^x$$

 [Watch Video Solution](#)

**341.** Differentiate the following w.r.t.  $x$ :

$$x^{\cos x} + (\sin x)^{\tan x}$$

 [Watch Video Solution](#)

**342.** Differentiate the following w.r.t. x:

$$(\sin x)^{\cos x} + (\cos x)^{\sin x}$$



**Watch Video Solution**

**343.** Differentiate the following w.r.t. x:

$$(\sin x)^{\tan x} + (\cos x)^{\sec x}$$



**Watch Video Solution**

**344.** Differentiate the following w.r.t. x:

$$(\log x)^x + (x)^{\cos x}$$



**Watch Video Solution**

**345.** Differentiate the following w.r.t.  $x$ :

$$(x)^{\sin x} + (\log x)^x$$



**Watch Video Solution**

**346.** Differentiate the following w.r.t.  $x$ :

$$(x)^x + (\sin x)^x$$



**Watch Video Solution**

**347.** Differentiate the following w.r.t.  $x$ :

$$(x)^{\sin x} + (\cos x)^x$$



**Watch Video Solution**

**348.** Differentiate the following w.r.t.  $x$ :

$$x^{\sin x} + (\sin x)^{\cos x}$$

 [Watch Video Solution](#)

**349.** Differentiate the following w.r.t.  $x$ :

$$(\sin x)^{\sec x} + (\tan x)^{\cos x}$$

 [Watch Video Solution](#)

**350.** Differentiate the following w.r.t.  $x$ :

$$(\tan x)^{\cot x} + x^{\tan x}, 0 < x < \frac{\pi}{4}$$

 [Watch Video Solution](#)



**351.** Differentiate the following w.r.t. x:

$$(x)^{\cos x} + (\cos x)^{\sin x}$$

 [Watch Video Solution](#)

**352.** Differentiate the following w.r.t. x:

$$x^{\sin x} + (\sin x)^{\cos x}$$

 [Watch Video Solution](#)

**353.** Differentiate the following w.r.t. x:

$$(\sin x)^{\sec x} + (\tan x)^{\cos x}$$

 [Watch Video Solution](#)

**354.** Differentiate the following w.r.t.  $x$ :

$$(\tan x)^{\cot x} + x(\tan x), 0 < x < \frac{\pi}{4}$$



[Watch Video Solution](#)

**355.** Differentiate the following w.r.t.  $x$ :

$$x^{\sin x} + (\sin x)^{\cos x}$$



[Watch Video Solution](#)

**356.** Differentiate the following w.r.t.  $x$ :

$$(\sin x)^x + \sin^{-1} \sqrt{x}$$



[Watch Video Solution](#)

**357.** Differentiate the following w.r.t. x:

$$(x)^{\log x} + (\log x)^x$$

 [Watch Video Solution](#)

**358.** Differentiate the following w.r.t. x:

$$(\log x)^{\cos x} + \frac{x^2 + 1}{x^2 - 1}$$

 [Watch Video Solution](#)

**359.** Differentiate the following w.r.t. x:

$$(x \cos x)^x + (x \sin x)^{1/x}$$

 [Watch Video Solution](#)

**360.** Differentiate the following w.r.t.  $x$ :

$$(\cos x)^x + (\sin x)^{1/x}$$

 [Watch Video Solution](#)

**361.** Differentiate the following w.r.t.  $x$ :

$$e^{\sin x} + (\tan x)^x$$

 [Watch Video Solution](#)

**362.** Differentiate the following w.r.t.  $x$ :

$$x^x - 2^{\sin x}$$

 [Watch Video Solution](#)

**363.** Differentiate the following w.r.t.  $x$ :

$$\left(x + \frac{1}{2}\right)^x + x^{1 + \frac{1}{x}}$$

 [Watch Video Solution](#)

**364.** Differentiate the following w.r.t.  $x$ :

$$x^{x^2-3} + (x-3)^{x^2}, f \text{ or } x > 3$$

 [Watch Video Solution](#)

**365.** Differentiate the following w.r.t.  $x$ :

$$x^2 + (\sin x)^x$$

 [Watch Video Solution](#)

**366.** Differentiate the following w.r.t. x:

$$\frac{(ax + b)(cx + d)}{(ax - b)(cx - d)}, x \neq \frac{b}{a}, \frac{d}{c}$$



**Watch Video Solution**

**367.** Differentiate the following w.r.t. x:

$$\frac{\frac{\cos^{-1}x}{2}}{\sqrt{2x + 7}}, -2 < x < 2$$



**Watch Video Solution**

**368.** Differentiate the following w.r.t.x .

$$\frac{\sqrt{(x - 3)(x^2 + 4)}}{3x^2 + 4x + 5}$$



**Watch Video Solution**

**369.** Differentiate the following w.r.t.  $x$ :

$$x^2 e^x \sin x$$



[Watch Video Solution](#)

**370.** Differentiate the following w.r.t.  $x$ :

$$e^x \cos^3 x \sin^2 x$$



[Watch Video Solution](#)

**371.** Differentiate the following w.r.t.  $x$ :

$$(x + 6)^3 (x + 2)^4 (x + 5)^5$$



[Watch Video Solution](#)

**372.** Differentiate the following w.r.t.  $x$ :

$$\sqrt{(x-1)(x-2)(x-3)(x-4)}$$

 [Watch Video Solution](#)

**373.** If  $xy = e^{x-y}$ , find  $\frac{dy}{dx}$

 [Watch Video Solution](#)

**374.** If  $(\sin x)^y = (\sin y)^x$ , find  $\frac{dy}{dx}$  :

 [Watch Video Solution](#)

**375.** If  $(\cos x)^y = (\cos y)^x$ , find  $\frac{dy}{dx}$  .

 [Watch Video Solution](#)



**376.** Differentiate  $\log(x^x + \operatorname{cosec}^2 x)$  w. r. t.  $x$

 [Watch Video Solution](#)

**377.** If  $x^p \cdot y^q = (x + y)^{p+q}$ , show that  $\frac{dy}{dx} = \frac{y}{x}$ ;

 [Watch Video Solution](#)

**378.** If  $y = x^y$ , prove that  $\frac{dy}{dx} = \frac{y^2}{x(1 - y \log x)}$

 [Watch Video Solution](#)

**379.** Differentiate the following w.r.t.x.

If  $y^x = e^{y-x}$ , prove that  $\frac{dy}{dx} = \frac{(1 + \log y)^2}{\log y}$



 [Watch Video Solution](#)

380. If  $x^x + y^x = 1$ , prove that :  $\frac{dy}{dx} = - \left[ \frac{x^x(1 + \log x) + y^x \cdot \log y}{x \cdot y^{(x-1)}} \right]$

 [Watch Video Solution](#)

381. If  $x^y + y^x = 1$ , find  $\frac{dy}{dx}$

 [Watch Video Solution](#)

382. If  $x^y + y^x = \log a$ , find  $\frac{dy}{dx}$ .

 [Watch Video Solution](#)

**383.** Show that if  $x^y + y^x = m^n$ , then:

$$\frac{dy}{dx} = - \frac{y^x \log y + yx^{y-1}}{x^y \log x + xy^{x-1}}$$

 [Watch Video Solution](#)

**384.** Find the derivative of the function given by

$$f(x) = (1+x)(1+x^2)(1+x^4)(1+x^8) \text{ and hence find } f'(1)$$

 [Watch Video Solution](#)

**385.** Differentiate  $(x^2 - 5x + 8)(x^3 + 7x + 9)$  by using product rule.

 [Watch Video Solution](#)

**386.** Differentiate  $(x^2 - 5x + 8)(x^3 + 7x + 9)$  by expanding the product to obtain a single polynomial.

 [Watch Video Solution](#)

**387.** Differentiate  $(x^2 - 5x + 8)(x^3 + 7x + 9)$  by logarithmic differentiation.

 [Watch Video Solution](#)

**388.** If  $y = (\sqrt{x})^{\sqrt{x}^{\sqrt{x}} \dots \dots \rightarrow \infty}$ , prove that  $\frac{dy}{dx} = \frac{y^2}{x(2 - y \log x)}$

 [Watch Video Solution](#)

**389.** If  $y = \sqrt{\sqrt{\sqrt{\sqrt{x + \sqrt{x + \sqrt{x + \dots \dots \infty}}}}}}$ , show that  $(2y - 1) \frac{dy}{dx} = 1$



Watch Video Solution

390. If  $y = \sqrt{3^x + \sqrt{3^x + \sqrt{3^x + \dots \infty}}}$ , then prove that :

$$(2y - 1) \frac{dy}{dx} = 3^x \log 3.$$


Watch Video Solution

391. If  $y = x^y$ , prove that  $\frac{dy}{dx} = \frac{y^2}{x(1 - y \log x)}$



Watch Video Solution

392. If  $y = (\cos x)^{\cos x^{\cos x^{\dots \rightarrow \infty}}}$  prove that  $\frac{dy}{dx} = \frac{-y^2 \tan x}{1 - y \log \cos x}$



Watch Video Solution

393. If  $y = (\tan x)^{(\tan x)^{(\tan x)^{\dots \infty}}}$ , then prove that  $\frac{dy}{dx} = 2$  at  $x = \frac{\pi}{4}$ .

 [Watch Video Solution](#)

394. If  $y = \left( x^{x^{x^{\dots \dots \dots \rightarrow \infty}}} \right)$ , prove that  $x \frac{dy}{dx} = \frac{y^2}{1 - y \log x}$ .

 [Watch Video Solution](#)

395. Find (a)  $\frac{dy}{dx}$  and (b)  $= \frac{d^2y}{dx^2}$  when  $y$  is given by :

$$1+2x$$

 [Watch Video Solution](#)

396. Find (a)  $\frac{dy}{dx}$  and (b)  $= \frac{d^2y}{dx^2}$  when  $y$  is given by :

$$ax^3 + bx^2 + cx + d$$



Watch Video Solution

397. Find (a)  $\frac{dy}{dx}$  and (b)  $= \frac{d^2y}{dx^2}$  when y is given by :

$1/(2x+3)$ , x not equal to  $-3/2$



Watch Video Solution

398. Find (a)  $\frac{dy}{dx}$  and (b)  $= \frac{d^2y}{dx^2}$  when y is given by :

$\log x - x$



Watch Video Solution

399. Find (a)  $\frac{dy}{dx}$  and (b)  $= \frac{d^2y}{dx^2}$  when y is given by :

$e^x + \sin x$



Watch Video Solution

**400.** Find (a)  $\frac{dy}{dx}$  and (b)  $= \frac{d^2y}{dx^2}$  when  $y$  is given by :

$$e^x + x^4$$

 [Watch Video Solution](#)

**401.** Find the second derivative of the following functions:

$$x^{20}$$

 [Watch Video Solution](#)

**402.** Find the second derivative of the following functions:

$$x^2 + 3x + 2$$

 [Watch Video Solution](#)



**403.** Find the second order derivative of the function

$$x \cdot \cos x$$

 [Watch Video Solution](#)

**404.** Find the second derivative of the following functions:

$$x^3 + \tan x$$

 [Watch Video Solution](#)

**405.** Find the second derivative of the following functions:

$$\tan^{-1} x$$

 [Watch Video Solution](#)

**406.** Find the second derivative of the following functions:

$\log x$

 [Watch Video Solution](#)

**407.** Find the second order derivative of the following functions

$x^3 \log x$

 [Watch Video Solution](#)

**408.** Find the second derivative of the following functions:

$\log(\log x)$

 [Watch Video Solution](#)

**409.** Find the second derivative of the following functions:

$$\sin(\log x)$$

 [Watch Video Solution](#)

**410.** Find the second derivative of the following functions:

$$e^x \sin 5x$$

 [Watch Video Solution](#)

**411.** Find the second derivative of the following functions:

$$e^{6x} \cos 3x$$

 [Watch Video Solution](#)

**412.** Find the second derivative of the following functions:

$$e^{-x}\cos x$$



[Watch Video Solution](#)

**413.** Find the second derivative of the following functions:

$$\tan x + \sec x$$



[Watch Video Solution](#)

**414.** Find the second derivative of the following functions:

$$\frac{\log x}{x}$$



[Watch Video Solution](#)

**415.** Find the second derivative of the following functions:

$$x^{-x}$$

 [Watch Video Solution](#)

**416.** If  $y = \sin^{-1}x$ , then show that  $(1 - x^2) \frac{d^2y}{dx^2} - x \frac{dy}{dx} = 0$

 [Watch Video Solution](#)

**417.** If  $y = \sin^{-1}x$ , show that :  $(1 - x^2) d^2 \frac{y}{dx^2} - x \frac{dy}{dx} = 0$

 [Watch Video Solution](#)

**418.** If  $y = 3e^{2x} + 2e^{3x}$ , prove that  $d^2 \frac{y}{dx^2} - 5 \frac{dy}{dx} + 6y = 0$ .

 [Watch Video Solution](#)

419. If  $y = Ae^{mx} + Be^{nx}$ , Show that  $\left(\frac{d^2}{dx^2}y\right) - (m + n)\frac{dy}{dx} + mny = 0$

 [Watch Video Solution](#)

420. Find the second order derivative of the following functions

If  $y = Pe^{ax} + Qe^{bx}$  show that  $\frac{d^2y}{dx^2} - (a + b)\frac{dy}{dx} + aby = 0$

 [Watch Video Solution](#)

421.  $y = 5\cos x - 3\sin x$ , prove that  $\frac{d^2y}{dx^2} + y = 0$

 [Watch Video Solution](#)

422. If  $e^y(x+1) = 1$  show that  $\left(d^2 \frac{y}{dx^2}\right) = \left(\frac{dy}{dx}\right)^2$  है।

 Watch Video Solution

423. If  $y = A\sin x + B\cos x$  then prove that  $d^2 \frac{y}{dx^2} + y = 0$

 Watch Video Solution

424. Find  $\frac{d^2}{dx^2}$  in the following :

$$x = at^2, y = 2at$$

 Watch Video Solution

425. Find  $\frac{d^2}{dx^2}$  in the following :

$$x = a\cos\theta, y = b\sin\theta$$

 [Watch Video Solution](#)

426. Find  $\frac{d^2}{dx^2}$  in the following :

$$x = a\cos^3\theta, y = a\sin^3\theta$$

 [Watch Video Solution](#)

427. Find  $\frac{d^2y}{dx^2}$  in the following

$$x = a\cos^3\theta, y = a\sin^3\theta$$

 [Watch Video Solution](#)



428. Find  $\frac{d^2}{dx^2}$  in the following :

If  $x = a\cos^3\theta$  and  $y = a\sin^3\theta$ , then find the value of  $d^2\frac{y}{dx^2}$  at  $\theta = \frac{\pi}{6}$

 [Watch Video Solution](#)

429. Find  $\frac{d^2}{dx^2}$  in the following :

$x = a(\cos t + t \sin t)$ ,  $y = a(\sin t - t \cos t)$

 [Watch Video Solution](#)

430. Find  $\frac{dy^2}{dx^2}$  in the following :

$x = a(\theta - \sin\theta)$ ,  $y = a(1 + \cos\theta)$

 [Watch Video Solution](#)

**431.** Find  $\frac{d^2y}{dx^2}$  at  $\theta = \frac{\pi}{2}$  when:

$$x = a(\theta - \sin\theta), y = a(1 + \cos\theta)$$

 [Watch Video Solution](#)

**432.** Find  $\frac{d^2y}{dx^2}$  at  $\theta = \frac{\pi}{2}$  when:

$$x = a(1 - \cos\theta), y = a(\theta + \sin\theta)$$

 [Watch Video Solution](#)

**433.** Find  $\frac{d^2y}{dx^2}$  at  $\theta = \frac{\pi}{2}$  when:

$$x = a(\theta - \sin\theta), y = a(1 - \cos\theta)$$

 [Watch Video Solution](#)

434. Find  $\frac{d^2y}{dx^2}$  when :  $x = 2\cos\theta - \cos 2\theta$  and  $y = 2\sin\theta - \sin 2\theta$ .

 [Watch Video Solution](#)

435. If  $x = a\sin t$  and  $y = a\left(\cos t + \log \tan\left(\frac{t}{2}\right)\right)$ , find  $\frac{d^2y}{dx^2}$

 [Watch Video Solution](#)

436. If  $y = (\sin^{-1}x)^2$ , then prove that  $(1-x)^2 \frac{d^2y}{dx^2} - x \frac{dy}{dx} = 2$

 [Watch Video Solution](#)

437. If  $y = (\cos^{-1}x)^2$  show that  $(1-x^2)^2 y_2 - xy_1 = 2$

 [Watch Video Solution](#)

**438.** If  $y = \left[ \tan^{-1}x \right]^2$ , then prove that :

$$\left( x^2 + 1 \right)^2 y_2 + 2x \left( x^2 + 1 \right) y_1 = 2.$$

 [Watch Video Solution](#)

**439.** Verify the truth of Rolle's Theorem for the following functions:

$$f(x) = x^2 + 2. a = -2, \text{ and } b = 2$$

 [Watch Video Solution](#)

**440.** Verify the truth of Rolle's Theorem for the following functions:

$$f(x) = \frac{x^3}{3} - \frac{5}{3}x^2 + 2x, x \in [0, 3]$$

 [Watch Video Solution](#)

**441.** Verify the truth of Rolle's Theorem for the following functions:

$$f(x) = \frac{x(x-2)}{x-1} \text{ on } [0,2]$$

 [Watch Video Solution](#)

**442.** Verify the truth of Rolle's Theorem for the following functions:

$$f(x) = x^2 + 2x - 8 \text{ defined in the interval } [-4,2]$$

 [Watch Video Solution](#)

**443.** Verify the truth of Rolle's Theorem for the following functions:

$$f(x) = x^2 \in [-1, 1]$$

 [Watch Video Solution](#)

**444.** Verify the truth of Rolle's Theorem for the following functions:

$$f(x) = x^{1/3} \in [-1, 1]$$

 [Watch Video Solution](#)

**445.** Verify the truth of Rolle's Theorem for the following functions:

$$f(x) = |x| \in [-1, 1]$$

 [Watch Video Solution](#)

**446.** Verify the truth of Rolle's Theorem for the following functions:

$$f(x) = |x-1| \text{ in } [1, 2]$$

 [Watch Video Solution](#)

**447.** Verify the truth of Rolle's Theorem for the following functions:

$$f(x) = \sqrt{x - 2} \text{ in } [1, 2]$$

 [Watch Video Solution](#)

**448.** Verify the truth of Rolle's Theorem for the following functions:

$$f(x) = [x] \text{ in } [-1, 1]$$

 [Watch Video Solution](#)

**449.** Verify the conditions of Rolle's Theorem in the following problems. In each case, find a point in the interval where the derivative vanishes:

$$x^{20} \text{ on } [-1, 1]$$

 [Watch Video Solution](#)

**450.** Verify the conditions of Rolle's Theorem in the following problems. In each case, find a point in the interval where the derivative vanishes:

$$(x + 1)(x - 2) \text{ on } [-1, 2]$$

 [Watch Video Solution](#)

**451.** Verify the conditions of Rolle's Theorem in the following problems. In each case, find a point in the interval where the derivative vanishes:

$$\sin x - \sin 2x \text{ on } [0, \pi]$$

 [Watch Video Solution](#)

**452.** Verify the conditions of Rolle's Theorem in the following problems. In each case, find a point in the interval where the



derivative vanishes:

$$\log(x^2 + 2) - \log 3 \text{ on } [-1, 1]$$

 [Watch Video Solution](#)

**453.** Verify the conditions of Rolle's Theorem in the following problems. In each case, find a point in the interval where the derivative vanishes:

$$e^{1-x^2} \text{ on } [-1, 1]$$

 [Watch Video Solution](#)

**454.** Verify the truth of Rolle's Theorem for the following function:

$$f(x) = x^2 - 5x + 4 \text{ on } [1, 4]$$

 [Watch Video Solution](#)

**455.** Verify the truth of Rolle's Theorem for the following function:

$$f(x) = 4x^2 - 12x + 9 \text{ in the interval } 0 \leq x \leq 3$$



[Watch Video Solution](#)

**456.** Verify the Rolle's Theorem for the following function:

$$f(x) = x^2 + 2x - 8 \text{ in the interval } [-4,2]$$



[Watch Video Solution](#)

**457.** Verify the truth of Rolle's Theorem for the following function:

$$f(x) = x^2 - x - 12 \text{ in the interval } [-3,4]$$



[Watch Video Solution](#)

**458.** Verify the truth of Rolle's Theorem for the following function:

$$f(x) = (x - 2)(x - 3)(x - 4) \text{ in the interval } 2 \leq x \leq 4$$

 [Watch Video Solution](#)

**459.** Verify the truth of Rolle's Theorem for the following function:

$$f(x) = x^3 - 4x \text{ in the interval } -2 \leq x \leq 2$$

 [Watch Video Solution](#)

**460.** Verify the truth of Rolle's Theorem for the following function:

$$f(x) = x(x - 1)^2 \text{ in the interval } [0,1]$$

 [Watch Video Solution](#)

**461.** Verify Rolle's theorem for the following functions

$$f(x) = (x - 2)(x - 4)^2 \text{ in the interval } [2, 4]$$

 [Watch Video Solution](#)

**462.** Verify Rolle's Theorem in the interval  $[a,b]$  for the fraction:

$$f(x) = (x - a)^m(x - b)^n, m \text{ and } n \text{ being positive integers. Find the value of 'c'.$$

 [Watch Video Solution](#)

**463.** Examine the applicability of Rolle's Theorem for the fraction:

$$f(x) = 2 + (x - 1)^{2/3} \text{ in the interval } 0 \leq x \leq 2$$

 [Watch Video Solution](#)

**464.** Verify Rolle's Theorem for the function:

$$f(x) = \sin^2 x, \text{ defined in the interval } [0, \pi]$$

 [Watch Video Solution](#)

**465.** Verify Rolle's Theorem for the function:

$$f(x) = \cos x, \text{ defined in the interval } \left[ \frac{\pi}{2}, \frac{\pi}{2} \right]$$

 [Watch Video Solution](#)

**466.** Verify Rolle's Theorem for the function:

$$f(x) = \tan x, \text{ define in the interval } [0, \pi]$$

 [Watch Video Solution](#)

**467.** Verify Rolle's Theorem for the function:

$$f(x) = \sin x + \cos x \in \left[0, \frac{\pi}{2}\right]$$

 [Watch Video Solution](#)

**468.** Verify Rolle's Theorem for the function:

$$f(x) = \sin x + \cos x - 1 \in \left[0, \frac{\pi}{2}\right]$$

 [Watch Video Solution](#)

**469.** Verify Rolle's Theorem for the function:

$$f(x) = \sin x + \cos x \in \left[0, \frac{\pi}{2}\right]$$

 [Watch Video Solution](#)

**470.** Verify Rolle's Theorem for the function:

$$f(x) = \sin^4 x + \cos^4 x \text{ in the interval } \left[0, \frac{\pi}{2}\right]$$

 [Watch Video Solution](#)

**471.** Find the value of  $f(x)$  when  $x=5$ :

$$f(x) = -4x + 5$$

 [Watch Video Solution](#)

**472.** At what points on the following curve, is the tangent parallel to x-axis?  $y = x^2$  on  $[-2, 2]$

 [Watch Video Solution](#)

**473.** At what points on the following curve, is the tangent parallel to x-axis?  $y = \cos x - 1$  on  $[0, 2\pi]$

 [Watch Video Solution](#)

**474.** For the function  $f(x) = x^3 - 6x^2 + ax + b$ , it is given that  $f(1) = f(3) = 0$ . Find the values of 'a' and 'b', and hence verify Rolle's Theorem on  $[1,3]$

 [Watch Video Solution](#)

**475.** Let  $f(x) = (x - 1)(x - 2)(x - 3)$  on the interval  $[1,3]$ . Prove that there is more than one  $c$  in  $(1,3)$  such that  $f'(c) = 0$

 [Watch Video Solution](#)



**476.** Discuss the applicability of Lagrange's Mean Value Theorem to

$$f(x) = x^2 - 1 \text{ on } [1, 2]$$

 [Watch Video Solution](#)

**477.** Discuss the applicability of Lagrange's Mean Value Theorem to

$$f(x) = x^2 \text{ on } [2, 4]$$

 [Watch Video Solution](#)

**478.** Discuss the applicability of Lagrange's Mean Value Theorem to

$$f(x) = x^2 - 2x + 3 \in [0, 4]$$

 [Watch Video Solution](#)

**479.** Discuss the applicability of Lagrange's Mean Value Theorem to

$$f(x) = 2x^2 - 10x + 29 \in [2, 7]$$

 [Watch Video Solution](#)

**480.** Discuss the applicability of Lagrange's Mean Value Theorem to

$$f(x) = x^2 - 4x - 3 \in [1, 4]$$

 [Watch Video Solution](#)

**481.** Discuss the applicability of Lagrange's Mean Value Theorem to

$$f(x) = 2x - x^2 \in [0, 1]$$

 [Watch Video Solution](#)

**482.** Discuss the applicability of Lagrange's Mean Value Theorem to

$$f(x) = 2x - x^2 \in [0, 1]$$

 [Watch Video Solution](#)

**483.** Verify Lagrange's mean value theorem for the following functions

$$f(x) = x^3 - 2x^2 - x + 3 \text{ in the interval } [0, 1]$$

 [Watch Video Solution](#)

**484.** Discuss the applicability of Lagrange's Mean Value Theorem to

$$f(x) = x^3 - 5x^2 - 3x \in [1, 3]$$

 [Watch Video Solution](#)

**485.** Verify Lagrange's Mean Value Theorem for the function :

$$f(x) = x(x - 1)(x - 2)(x - 3) \text{ in the interval } [0, 4]$$

 [Watch Video Solution](#)

**486.** Verify the conditions of Mean Value Theorem in the following.

In each case. Find a point in the interval as stated by the Mean

Value Theorem:

$$f(x) = x \text{ on } [a, b]$$

 [Watch Video Solution](#)

**487.** Verify the conditions of Mean Value Theorem in the following.

In each case. Find a point in the interval as stated by the Mean

Value Theorem:

$$f(x) = x + \frac{1}{x} \text{ on } [1, 3]$$



[Watch Video Solution](#)

**488.** Verify the conditions of Mean Value Theorem in the following.

In each case. Find a point in the interval as stated by the Mean

Value Theorem:

$$f(x) = ax^2 + bx + ex + don[0, 1]$$



[Watch Video Solution](#)

**489.** Verify the conditions of Mean Value Theorem in the following.

In each case. Find a point in the interval as stated by the Mean

Value Theorem:

$$f(x) = ax^2 + ex + e \text{ on } [0,1]$$



[Watch Video Solution](#)

**490.** Verify the conditions of Mean Value Theorem in the following.

In each case. Find a point in the interval as stated by the Mean

Value Theorem:

$$f(x) = \sin x - \sin 2x \text{ on } [0, 2\pi]$$



[Watch Video Solution](#)

**491.** Verify the conditions of Mean Value Theorem in the following.

In each case. Find a point in the interval as stated by the Mean

Value Theorem:

$$f(x) = \sin x - \sin 2x \text{ on } [0, \pi]$$



[Watch Video Solution](#)

**492.** Verify the Lagrange's Mean Value Theorem for the functions:

$$f(x) = x^{1/3} \text{ in the interval } [-1, 1]$$

 [Watch Video Solution](#)

**493.** Verify Lagrange's mean value theorem for the following functions

$$f(x) = (x - 1)^{2/3} \text{ in the interval } [1, 2]$$

 [Watch Video Solution](#)

**494.** Verify the Lagrange's Mean Value Theorem for the functions:

$$f(x) = \frac{1}{x} \text{ in the interval } [-1, 2]$$

 [Watch Video Solution](#)

**495.** Verify the Lagrange's Mean Value Theorem for the functions:

$$f(x) = \frac{1}{4x - 1}, \text{ in the interval } [-1, 4]$$

 [Watch Video Solution](#)

Watch Video Solution

**496.** Verify the Lagrange's Mean Value Theorem for the functions:

$$f(x) = |x| \text{ in the interval } [-1,1]$$



Watch Video Solution

**497.** Verify the Lagrange's Mean Value Theorem for the functions:

$$f(x) = \sqrt{x^2 - 4} \text{ in the interval } [2,4]$$



Watch Video Solution

**498.** Verify the Lagrange's Mean Value Theorem for the functions:

$$f(x) = \sqrt{25 - x^2} \text{ in the interval } [-3,4]$$



Watch Video Solution



**499.** Verify the Lagrange's Mean Value Theorem for the functions:

$$f(x) = \log_e x \text{ in the interval } [1,2]$$



[Watch Video Solution](#)

**500.** Verify the Lagrange's Mean Value Theorem for the functions:

$$f(x) = \alpha \sin x \text{ on } [a, b]$$



[Watch Video Solution](#)

**501.** Find 'c' of Lagrange's Mean Value Theorem for the functions:

$$f(x) = 2x^2 - 1 \text{ in the interval } [1,2]$$



[Watch Video Solution](#)

**502.** Find 'c' of Lagrange's Mean Value Theorem for the functions:

$$f(x) = \log x \text{ in the interval } [1, e]$$

 [Watch Video Solution](#)

**503.** Find 'c' of Lagrange's Mean Value Theorem for the functions:

$$f(x) = e^x \text{ in the interval } [0, 1]$$

 [Watch Video Solution](#)

**504.** Verify Mean Value Theorem, if  $f(x) = x^3 - 5x^2 - 3x$ , in the interval  $[a, b]$ , where  $a = 1$  and  $b = 3$ . Find all  $c \in (1, 3)$  for which  $f'(c) = 0$ .

 [Watch Video Solution](#)

**505.** Verify Lagrange's Mean Value Theorem for the function :

$$f(x) = x(x - 1)(x - 2)(x - 3) \text{ in the interval } [0, 4]$$

 [Watch Video Solution](#)

**506.** Verify Lagrang'e Mean value Theorem for the function:

$$f(x) = \begin{cases} 2 + x^3 & \text{if } x \leq 1 \\ 3x & \text{if } x > 1 \end{cases} \text{ on } [-1, 2]$$

 [Watch Video Solution](#)

**507.** Find a point on the parabola  $y = (x - 2)^2$ , where the tangent is parallel to the chord joining (2,4) and (4,4)

 [Watch Video Solution](#)

**508.** Find a point on the curve  $y = x^3$ , where the tangent to the curve is parallel to the chord joining the points (1, 1) and (3, 27).

 [Watch Video Solution](#)

**509.** Find a point on the curve  $y = x^3 - 3x$ , where the tangent is parallel to the chord joining (1,-2) and (2,2)

 [Watch Video Solution](#)

**510.** Find the co-ordinates of the point at which the tangent to the curve given by  $f(x) = x^2 - 6x + 1$  is parallel to the chord joining the points (1,-4) and (3,-8)

 [Watch Video Solution](#)

**511.** Use Lagrange's Mean value Theorem to determine a point P on the curve  $y = \sqrt{x-2}$ , where the tangent is parallel to the chord joining (2,0) and (3,1)

 [Watch Video Solution](#)

**512.** Examine the continuity of the function:

$$f(x) = \begin{cases} \frac{x-4}{2(x-4)} & \text{if } x \neq 4 \\ 0 & \text{if } x = 4 \end{cases} \text{ at } x=4$$

 [Watch Video Solution](#)

**513.** Find the value of 'k', such that the function :

$$f(x) = \left\{ \begin{array}{l} \frac{2x^{x+2} - 16}{4^x - 16}, \text{ if } x \neq 2 \\ k, \text{ if } x = 2 \end{array} \right\} \text{ is continuous at } x=2$$

 [Watch Video Solution](#)

514. Given  $f(x) = \frac{1}{x-1}$ . Find the points of discontinuity of the composite function  $f(f(x))$

 [Watch Video Solution](#)

515. Find  $f'(x)$  when  $f(x) = 2^{\cos^2 x}$

 [Watch Video Solution](#)

516. Find  $f'(x)$  when  $f(x) = \sin^{-1}\left(\frac{1}{\sqrt{x+1}}\right)$

 [Watch Video Solution](#)

517. If  $\sin x = \frac{2t}{1+t^2}$ ,  $\tan y = \frac{2t}{1-t^2}$ , find  $\frac{dy}{dx}$

 [Watch Video Solution](#)

518. If  $y = \sec^{-1}\left(\frac{1}{4x^3 - 3x}\right)$ , find  $\frac{dy}{dx}$

 [Watch Video Solution](#)

519. Find  $\frac{dy}{dx}$  when  $\tan^{-1}(x^2 + y^2) = 0$

 [Watch Video Solution](#)

520. Examine the differentiability of the function

$$f(x) = \begin{cases} x[x] & \text{if } 0 \leq x < 2 \\ (x-1)x & \text{if } 2 \leq x < 3 \end{cases} \text{ at } x=2$$

 [Watch Video Solution](#)

**521.** Show that  $|x-5|$  is continuous but not differentiable at  $x = 5$ .

 [Watch Video Solution](#)

**522.** A function  $f: \mathbb{R} \rightarrow \mathbb{R}$  satisfies the equation  $f(x + y) = f(x) \cdot f(y)$  for all,  $f(x) \neq 0$ . Suppose that the function is differentiable at  $x = 0$  and  $f'(0) = 2$ . Then,

 [Watch Video Solution](#)

**523.** If  $x = e^{x/y}$ , prove that  $\frac{dy}{dx} = \frac{x - y}{x \log x}$

 [Watch Video Solution](#)



**524.** Verify the Lagrange's Mean Value Theorem for the functions:

$$f(x) = \frac{1}{4x - 1}, \text{ in the interval } [-1, 4]$$



[Watch Video Solution](#)

**525.** Verify LMV Theorem for the following:

$$f(x) = \sin x - \sin 2x \text{ in } [0, \pi]$$



[Watch Video Solution](#)

**526.** Verify LMV Theorem for the following:

$$f(x) = \sqrt{25 - x^2} \text{ in } [1, 5]$$



[Watch Video Solution](#)

527. The function  $f(x) = \begin{cases} \frac{\sin x}{x} + \cos x & \text{if } x \neq 0 \\ k & \text{if } x = 0 \end{cases}$  is continuous at

$x = 0$ , then the value of 'k' is

A. 3

B. 2

C. 1

D. 1.5

**Answer:**

 [Watch Video Solution](#)

528. The function  $f(x) = [x]$ , where  $[x]$  denotes the greatest integer function, is continuous at

A. 4

B. -2

C. 1

D. 1.5

**Answer:**



**Watch Video Solution**

**529.** The value of 'k' which makes the function defined by :

$$f(x) = \begin{cases} \sin\left(\frac{1}{x}\right) & \text{if } x \neq 0 \\ k & \text{if } x = 0 \end{cases} \text{ continuous at } x=0 \text{ is}$$

A. 8

B. 1

C. -1

D. None of these

**Answer:**



[Watch Video Solution](#)

530. If  $u = \sin^{-1}\left(2\frac{x}{(1+x)^2}\right)$  and  $v = \tan^{-1}\left(2\frac{x}{1-x^2}\right)$ , the  $d\frac{u}{d}v$  is

A.  $\frac{1}{2}$

B.  $x$

C.  $\frac{1-x^2}{1+x^2}$

D.  $1$

**Answer:**



[Watch Video Solution](#)

531. If  $x = t^2$ ,  $y = t^3$ , then  $\frac{d^2y}{dx^2}$  is

A.  $\frac{3}{2}$

B.  $\frac{3}{4t}$

C.  $\frac{3}{2t}$

D.  $\frac{3t}{2}$

**Answer:**



[Watch Video Solution](#)

532. The value of 'c' in Rolle's Theorem for the function

$f(x) = x^3 - 3x$  in the interval  $[0, \sqrt{3}]$  is

A. 1

B. -1

C.  $\frac{3}{2}$

D.  $\frac{1}{3}$

**Answer:**



[Watch Video Solution](#)

**533.** The value of 'c' in mean Value Theorem for the function

$$f(x) = x(x - 2) \in [1, 2] \text{ is}$$

A.  $\frac{3}{2}$

B.  $\frac{2}{3}$

C.  $\frac{1}{2}$

D.  $\frac{3}{4}$

**Answer:**



[Watch Video Solution](#)

534. The derivative of  $f(x) = |x|$  at  $x=0$  is

A. 1

B. 0

C. -1

D. Does not exist.

**Answer:**



[Watch Video Solution](#)

535. The derivative of  $\log(ax+b)$  is

A.  $\frac{1}{ax + b}$

B.  $\frac{b}{ax + b}$

C.  $\frac{a}{ax + b}$

D.  $\frac{A + b}{ax + b}$

**Answer:**



**Watch Video Solution**

**536.** If  $f(x) = \begin{cases} kx + 1 & x \leq 5 \\ 3x - 5 & x > 5 \end{cases}$  is a continuous function then the

value of k is

A.  $\frac{9}{5}$

B. 3

C.  $\frac{11}{5}$

D. None of these

**Answer:**





 Watch Video Solution

537. The derivative of  $\sin^3(x^5)$  w.r.t.  $x$  is

A.  $\cos^3(x^5)$

B.  $3\sin^2(5x^4)$

C.  $15\sin^2(x^5)x^4$

D. None of these

**Answer:**

 Watch Video Solution

538. If  $y = \log(\operatorname{cose}^x)$ , then  $\frac{dy}{dx} = \dots\dots\dots$

A.  $-\tan(e^x) \cdot e^x$

B.  $\frac{e^x}{\operatorname{cose}^x}$

C.  $\frac{1}{\sin(e^x)}$

D. None of these

**Answer:**



**Watch Video Solution**

539. If  $y = e^{\sin(\log x)}$ , then the value of  $\frac{dy}{dx}$  is

A.  $e^{\cos(\log x)}$

B.  $e^{\sin(\log x)} \cdot \cos(\log x)$

C.  $\left( \frac{e^{\sin(\log x)} \cdot \cos(\log x)}{x} \right)$

D. None of these

**Answer:**



Watch Video Solution

540. If  $x^3 + y^3 = 10$ , then the value of  $\frac{dy}{dx}$  is

A.  $-\frac{y^2}{x^2}$

B.  $-\frac{x^2}{y^2}$

C.  $\frac{x^2}{y^2}$

D. None of these

Answer:



Watch Video Solution

541. If  $f(x) = \begin{cases} kx^2 & x < 2 \\ 3 & x \geq 2 \end{cases}$  is continuous at  $x=2$ , the value of 'k' is

A.  $\frac{2}{3}$

B.  $\frac{4}{3}$

C.  $\frac{3}{2}$

D.  $\frac{3}{4}$

**Answer:**



[Watch Video Solution](#)

**542.** If  $x = 2at, y = at^2$ , then  $\frac{dx}{dy}$  is equal to :

A.  $\frac{1}{t}$

B.  $t$

C.  $-\frac{1}{t}$

D.  $-t$

**Answer:**

 [Watch Video Solution](#)

543. If the function  $f$  is defined by  $f(x) = \begin{cases} 3 & x \neq 0 \\ a + 1 & x = 0 \end{cases}$  and  $f$

is continuous at  $x = 0$ , then value of  $a$  is :

- A. 1
- B. 2
- C. 3
- D. 4

**Answer:**

 [Watch Video Solution](#)

544. The derivative of  $\cos^{-1}(e^x)$  is

A.  $\sin^{-1}(e^x) \cdot e^x$

B.  $\frac{-e^x}{\sqrt{1-e^{2x}}}$

C.  $\frac{e^x}{\sqrt{1-e^{2x}}}$

D. None of these

**Answer:**



**Watch Video Solution**

545. Find the derivative of  $\sin(\log x)$  ( $x > 0$ ) w.r.t.  $x$

A.  $\frac{\cos(\log x)}{x}$

B.  $x \cos(\log x)$

C.  $\log x \cos(\log x)$

D. None of these

**Answer:**

 [Watch Video Solution](#)

**546.** The derivative of  $\log (\operatorname{cosec} x)$  is

- A.  $-\cot x$
- B.  $-\operatorname{cosec} x$
- C.  $-\operatorname{cosec} x \cot x$
- D.  $\sin x \tan x$ .

**Answer:**

 [Watch Video Solution](#)

547. The derivative of  $\sin x^2$  w. r. t.  $x^2$  is

A.  $\cos x^2$

B.  $2x \cos x^2$

C.  $\frac{\sin 2x}{2x}$

D.  $\frac{\cos x^2}{2x}$

**Answer:**



**Watch Video Solution**

548. If  $y = \log x - x^2$ , then value of  $\frac{d^2y}{dx^2}$  is

A.  $-\frac{1}{x^2} + 1$

B.  $-\frac{1}{x^2}$

C.  $\frac{1}{x} - 2x$



D.  $-\frac{1}{x^2} - 2$

**Answer:**

 [Watch Video Solution](#)

**549.** The function  $f(x) = |x| + |x-1| + |x-2|$  is continuous but not differentiable at for all  $x \in \mathbb{R}$   $x=-1$  and  $x=1$

 [Watch Video Solution](#)

**550.** The value of 'c' for which Lagrange's Mean value Theorem is applicable to  $f(x) = x^{1/2}$  in  $[0,4]$  is

A. 1

B. 4

C. 2

D.  $\frac{1}{4}$

**Answer:**

 [Watch Video Solution](#)

**551.** At  $x = 0$ , the function  $f(x) = |x|$  is

- A. Continuous but not differentiable
- B. Differentiable but not continuous
- C. Both continuous and differentiable
- D. Neither continuous nor differentiable.

**Answer:**

 [Watch Video Solution](#)

552. How many of the function  $f(x) = |x|$ ,  $g(x) = |x^2|$  and  $h(x) = [x]^3$  are not differentiable at  $x = 0$ ?

- A. 0
- B. 1
- C. 2
- D. 3

**Answer:**

 [Watch Video Solution](#)

553.  $f(x) = \begin{cases} \frac{x^2-4}{x-2} & x \neq 2 \\ 2k & x = 2 \end{cases}$  is continuous at  $x=2$  then  $k=$

- A. 2

B. 4

C. 6

D. None of these

**Answer:**



[Watch Video Solution](#)

**554.** If  $f(x) = x^2 + 5x + 2$ , then  $f'(3)$  is

A. 11

B. 12

C. 10

D. None of these

**Answer:**



[Watch Video Solution](#)

555. The derivative of  $\cos 5x$  w.r.t  $x$  is

A.  $5 \sin 5x$

B.  $\sin 5x$

C.  $-5\sin 5x$

D. None of these

**Answer:**

 Watch Video Solution

556. If  $x = at^2$ ,  $y = 2at$ , then  $\frac{dy}{dx}$  is

A.  $t$

B.  $\frac{2}{t}$

C.  $\frac{1}{t}$

D. None of these

**Answer:**



**Watch Video Solution**

557. If function defined by :  $f(x) = \begin{cases} \frac{\sin 3x}{2x} & x \neq 0 \\ k + 1 & x = 0 \end{cases}$  is continuous

at  $x = 0$ , then value of  $k$  is :

A. 0

B.  $\frac{3}{2}$

C.  $\frac{1}{2}$

D. 1

**Answer:**



Watch Video Solution

558. If  $f(x) = \log_x(\log x)$  then the value of  $f'(e)$  is

A.  $e$

B.  $\frac{2}{e}$

C.  $\frac{1}{e}$

D. 0

Answer:



Watch Video Solution

559. If  $f(x) = \log_x\{\ln(x)\}$  then  $f'(x)$  at  $x = e$ , is

A. 0

B. 1

C.  $\frac{1}{e}$

D.  $\frac{1}{2e}$

**Answer:**



**Watch Video Solution**

**560.** If  $x = ct, y = \frac{c}{t}$ , find  $\frac{dy}{dx}$  at  $t = 2$

A.  $\frac{1}{4}$

B. 4

C.  $-\frac{1}{4}$

D. 0

**Answer:**





561. Let  $f(x) = \begin{cases} ax + 3 & x \leq 2 \\ a^2x - 1 & x > 2 \end{cases}$ . Then the value of 'a' for which 'f' is continuous for all x are

- A. 1 and -2
- B. 1 and 2
- C. -1 and 2
- D. -1 and -2

**Answer:**

[Watch Video Solution](#)

562. Let  $R$  be the set of all real numbers. Let  $f: R \rightarrow R$  be a function such that :  $|f(x) - f(y)|^2 \leq |x - y|^2, \forall x, y \in R$ . Then  $f(x) =$

A.  $x$

B. 1

C. 0

D.  $x^2$

**Answer:**



**Watch Video Solution**

**563.** Let  $f(x) = x^2 + bx + 7$ . If  $f'(5) = 2f'\left(\frac{7}{2}\right)$ , then the value of 'b' is

A. 4

B. 3

C. -4

D. -3

**Answer:**



**Watch Video Solution**

**564.** The function  $f(x) = \begin{cases} 2x^2 - 1 & \text{if } 1 \leq x \leq 4 \\ 151 - 30x & \text{if } 4 < x \leq 5 \end{cases}$  is not suitable

to apply Rolle's theorem since

- A.  $f(x)$  is not continuous on  $[1,5]$
- B.  $f(x) \neq f(5)$
- C.  $f(x)$  is continuous only  $x = 4$
- D.  $f(x)$  is not differentiable in  $(4,5)$

**Answer:**



**Watch Video Solution**

565. Let  $f(x)$  be a differentiable function and  $f'(4) = 5$ , then:

$$\lim_{x \rightarrow 2} \frac{f(4) - f(x^2)}{x - 2} \text{ equals:}$$

- A. 0
- B. 5
- C. 20
- D. -20

**Answer:**

 [Watch Video Solution](#)

566. Determine if  $f$  defined by :  $f(x) = \begin{cases} x^2 \sin\left(\frac{1}{x}\right) & \text{if } x \neq 0 \\ 0 & \text{if } x = 0 \end{cases}$

is a continuous function?

A.  $f$  satisfies the conditions of Rolle's theorem on  $[-1,1]$

B.  $f$  satisfies the conditions of Lagrange's Mean value theorem on  $[-1,1]$

C.  $f$  satisfies the conditions of Rolle's theorem on  $[0,1]$

D.  $f$  satisfies the conditions of Lagrange's Mean value of theorem on  $[0,1]$

**Answer:**



[Watch Video Solution](#)

567. If  $y = (1 + x)(1 + x^2)(1 + x^4)$ , then  $\frac{dy}{dx}$  at  $x = 1$  is

A. 20

B. 28

C. 1

D. 0

**Answer:**

 [Watch Video Solution](#)

**568.** The value of  $\frac{d}{dx} \left\{ \tan^{-1}(\cos x) \right\}$  for  $x = 30$  is equal to

A.  $\frac{1}{2}$

B.  $\frac{1}{-2}$

C. 1

D.  $\frac{\sin x}{(1 + \sin x)^2}$

**Answer:**

 [Watch Video Solution](#)

569. If  $f(x) = \begin{cases} \frac{x^2 - (a+2)x + a}{x-2} & x \neq 2 \\ 2 & x = 2 \end{cases}$  is continuous at  $x = 2$ , then the

value of  $a$  is

A. -1

B. -6

C. 0

D. 1

**Answer:**

 [Watch Video Solution](#)

570. Let  $g(x) = \frac{(x-1)^3}{\log(x-1)}$  Find  $g(5)$ .

 [Watch Video Solution](#)

571. Let  $y$  be an implicit function of  $x$  defined by  $x^{2x} - 2x^x \cot y - 1 = 0$

Then  $y'(1)$  equals

A. -2

B. 1

C.  $\log 2$

D.  $-\log 2$

**Answer:**



[Watch Video Solution](#)

572. Let  $f: (-1, 1) \rightarrow \mathbb{R}$  be a differentiable function with  $f(0) = -1$  and  $f'(0) = 1$  let  $g(x) = [f(2f(x)+2)]^2$ , then  $g'(0) =$

A. 4



B. -4

C.  $\log 2$

D.  $-\log 2$

**Answer:**



**Watch Video Solution**

573. If 'f' is differentiable at  $x = a$ , find  $\left( \lim_{x \rightarrow a} \frac{x^2 f(a) - a^2 f(x)}{x - a} \right)$

A.  $a^2 f(a)$

B.  $af(a) - a^2 f'(a)$

C.  $2af(a) - a^2 f'$

D.  $2af(a) + a^2 f'(a)$

**Answer:**



Watch Video Solution

574. If  $f: R \rightarrow R$  is a function defined by:  $f(x) = [x] \cos\left(\frac{2x - 1}{2}\right)\pi$ ,

where  $[x]$  denotes the greatest integer function, then 'f' is

- A. continuous for every real x
- B. discontinuous only at  $x = 0$
- C. discontinuous only at non-zero integral values of x
- D. continuous only at  $x = 0$

Answer:



Watch Video Solution

575. Let  $f(x) = \begin{cases} x^2 \left| \cos \frac{\pi}{x} \right|, & x \neq 0 \\ 0, & x = 0 \end{cases}$ ,  $x \in \mathbb{R}$ , then  $f$  is

- a. differentiable both at  $x = 0$  and at  $x = 2$
  - b. differentiable at  $x = 0$  but not differentiable at  $x = 2$
  - c. not differentiable at  $x = 0$  but differentiable at  $x = 2$
  - d. differentiable neither at  $x = 0$  nor at  $x = 2$
- 
- A. differentiable both at  $x = 0$  and at  $x = 2$
  - B. differentiable at  $x = 0$  but not differentiable at  $x = 2$
  - C. not differentiable at  $x = 0$  but differentiable at  $x = 2$
  - D. differentiable neither at  $x = 0$  nor at  $x = 2$

**Answer:**

 [Watch Video Solution](#)

576. If  $y = \sec(\tan^{-1}x)$ , then  $\frac{dy}{dx}$  at  $x = 1$  is equal to

A.  $\frac{1}{2}$

B. 1

C.  $\sqrt{2}$

D.  $\frac{1}{\sqrt{2}}$

**Answer:**



**Watch Video Solution**

**577.** If  $g$  is the inverse of a function  $f$  and  $f'(x) = \frac{1}{1+x^5}$  then  $g'(x)$  is equal to

A.  $5x^4$

B.  $\frac{1}{1+g(x)^5}$

C.  $1+(g(x))^5$

D.  $1+x^5$

**Answer:**

 [Watch Video Solution](#)

578. If the function  $g(x) = \begin{cases} k\sqrt{x+1}, & 0 \leq x \leq 3 \\ mx+2, & 3 < x \leq 5 \end{cases}$  is differentiable,

then the value of  $k + m$  is

A. 2

B.  $\frac{16}{5}$

C.  $\frac{10}{3}$

D. 4

**Answer:**

 [Watch Video Solution](#)

579. For  $x \in \mathbb{R}$ ,  $f(x) = |\log 2 - \sin x|$  and  $g(x) = f(f(x))$ , then

- A.  $g$  is not differentiable at  $x = 0$
- B.  $g'(0) = \cos(\log 2)$
- C.  $g'(0) = -\cos(\log 2)$
- D.  $g$  is differentiable at  $x = 0$  and  $g'(0) = -\sin(\log 2)$

**Answer:**



[Watch Video Solution](#)

580. A function  $f: \mathbb{R} \rightarrow \mathbb{R}$  is defined as follows:

$$f(x) = \begin{cases} x & \text{if } x \leq 1 \\ 5 & \text{if } x > 1 \end{cases} \text{ which one of the following is true?}$$

- A.  $f$  is continuous at 0 and 1
- B.  $f$  is continuous at 1 and 2

C.  $f$  is continuous at 0 and 2

D.  $f$  is continuous at 0,1 and 2

**Answer:**

 [Watch Video Solution](#)

581. If  $\sqrt{x} + \sqrt{y} = 4$ , then  $\frac{dy}{dx}$  is

A.  $-\sqrt{\left(\frac{x}{y}\right)}$

B.  $-\sqrt{\frac{y}{x}}$

C.  $\sqrt{\frac{x}{y}}$

D.  $\sqrt{\frac{y}{x}}$

**Answer:**

 [Watch Video Solution](#)

582. Find  $\frac{dy}{dx}$  when  $x = 4t, y = \frac{4}{t}$

 [Watch Video Solution](#)

583. The function  $f(x)$  is defined as follows:

$$f(x) = \begin{cases} x^2 + ax + b & 0 \leq x < 2 \\ 3x + 2 & 2 \leq x \leq 4 \\ 2ax + 5b & 4 < x \leq 8 \end{cases}$$

If  $f(x)$  is continuous on  $[0,8]$ , find the

values of 'a' and 'b'.

 [Watch Video Solution](#)

584. If  $y = \tan^{-1} \left( \frac{\sqrt{1+x^2} - \sqrt{1-x^2}}{\sqrt{1+x^2} + \sqrt{1-x^2}} \right)$ , then show that

$$\frac{dy}{dx} = \frac{x}{\sqrt{1-x^4}}$$





Watch Video Solution

585. If  $x^Y = e^{X-Y}$ , prove that  $\frac{dy}{dx} = \frac{\log x}{(1 + \log x)^2}$ .



Watch Video Solution

586. If  $y = e^{ax} \sin bx$ , prove that  $d^2 \frac{y}{dx^2} - 2a \frac{dy}{dx} + (a^2 + b^2)y = 0$ .



Watch Video Solution

587. Verify Rolle's theorem for function  $f(x) = \sin x + \cos x$  in the interval  $[0, 2\pi]$ .



Watch Video Solution

588. Find  $\frac{dy}{dx}$ , if  $y^x + x^y + x^x = a^b$



Watch Video Solution