



# MATHS

## BOOKS - MODERN PUBLICATION

### PROBABILITY

#### Example

1. If a four digit number is formed by using the digits 1,2,3 and 5 with no repetition, then the probability that the number is divisible by 5 is :



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2. If a leap year is selected at random, what is the chance that it will contain 53 tuesdays?



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3. If  $P(A) = \frac{1}{5}$  and  $P(A - B) = \frac{1}{6}$ , find the value of  $P(A \cap B)$ .



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4. IF  $P(A) = \frac{4}{5}$  and  $P\left(\frac{B}{A}\right) = \frac{2}{5}$ , find  $P(A \cap B)$ .



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5. Ten cards numbered 1 to 10 are placed in a box, mixed up thoroughly and then one card is drawn randomly. If it is known that the number on the drawn card is more than 3, what is the probability that it is an even number?



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6. A die is thrown three times. Events A and B are defined as below: A : 4 on the third throw B : 6 on the first and 5 on the second throw Find the probability of A given that B has already occurred.



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7. Consider the experiment of tossing a coin. If the coin shows head, toss it again but if it shows tail, then throw a die. Find the conditional probability of the event that the die

shows a number greater than 4, given that there is at least one tail.



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8. If  $P(A) = \frac{2}{5}$  and  $P(B) = \frac{1}{3}$ , A and B are independent events, then find the value of  $P(A \cap B)$ .



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9. If A and B are independent events such that

$$P(A) = \frac{3}{10}, P(B) = \frac{2}{5}, \quad \text{then find } :$$

$$P(A \text{ and } B)$$



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10. If A and B are independent events such that

$$P(A) = \frac{3}{10}, P(B) = \frac{2}{5}, \quad \text{then find } :$$

$$P(A \text{ or } B)$$



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**11.** One card is drawn from a pack of 52 cards so that each card is equally likely to be selected. Prove that the following cases are independent:  
A: " The card drawn is a spade" B:" the card drawn is an ace".



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**12.** One card is drawn from a pack of 52 cards so that each card is equally likely to be selected. Prove that the following cases are independent:

A: "the card drawn is black" B: "the card drawn is a king"



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**13.** An unbiased die is thrown twice. Let the event A be 'odd number on the first throw' and B the event 'odd number on the second throw'. Check the independence of the events A and B.



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**14.** Three coins are tossed simultaneously. Consider the event E 'three heads or three tails', F 'at least two heads' and G 'at most two heads'. Of the pairs (E,F), (E,G) and (F,G), which are independent? which are dependent?



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**15.** The probability of student A passing an examination is  $\frac{2}{9}$  and of student B is  $\frac{5}{9}$ . Assuming the two events : 'A passes', 'B passes'

as independent. Find the probability of: only A passing the examination



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**16.** The probability of student A passing an examination is  $\frac{2}{9}$  and of student B is  $\frac{5}{9}$ .

Assuming the two events : 'A passes', 'B passes' as independent. Find the probability of: only one of them passing the examination.



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17. A husband and his wife appear for an interview for two parts. The probability of husband's selection is  $\frac{1}{7}$  and that of wife's selection is  $\frac{1}{5}$ . What is probability that only one of them is selected?



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18. In a hockey match two teams A and B scored same number of goals upto the end of the games so as to decide the winner, the referee asked both the captains to throw a die

alternately and decided that the team, whose captain gets a six first, will be declared the winner. If the captain of team A was asked to start, find their respective probabilities of winning the match and state whether the decision of the referee was fair or not.



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**19.** A speaks truth in 60% of the cases, while B in 90% of the cases. In what percentage are they likely to contradict each other in stating the same fact? In the case of contradiction do you

think , the statement of B will carry more weight as he speaks truth in more number of case than A?



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**20.** The probabilities of two students A and B coming to the school in time are  $\frac{3}{7}$  and  $\frac{5}{7}$  respectively. Assuming that the events, 'A coming in time' and 'B coming in time' are independent, find the probability of only one of them coming to the school in time. Write at

least one advantage of coming to school in time.



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**21.** A and B throw a pair of dice alternately. A wins the game if he gets a total of 7 and B wins if he gets a total of 10. If A starts the game, find the probability that B wins.



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**22.** A bag A contains 8 white and 7 black balls while the other bag B contains 5 white and 4 black balls. One ball is randomly picked up from the bag A and mixed up with the balls in the bag B. Then a ball is randomly drawn out from it. Find the probability that the ball drawn is white.



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**23.** If A and B are two independent events such that :  $P(\bar{A} \cap B) = \frac{2}{15}$  and  $P(A \cap \bar{B}) = \frac{1}{6}$ ,

then find  $P(A)$  and  $P(B)$ .



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**24.** When two coins are tossed simultaneously.

Find the probability of getting.

at least one head



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**25.** How many times must a fair coin be tossed so that the probability of getting at least one



head is more than 80%?



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26. If A and B are two independent events, then the probability of occurrence of at least one of A and B is given by  $= 1 - P(A')P(B')$



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27. A and B appeared for an interview. The probability of their selection is  $\frac{1}{5}$  and  $\frac{1}{3}$

respectively. Find the probability that both selected



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**28.** A and B appeared for an interview. The probability of their selection is  $\frac{1}{2}$  and  $\frac{1}{3}$  respectively. Find the probability that at least one of them selected



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**29.** A problem in Mathematics is given to three students whose chances of solving it are  $\frac{1}{2}$ ,  $\frac{1}{3}$ ,  $\frac{1}{4}$ . What is the probability in the following cases? : that the problem is solved.



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**30.** A problem in Mathematics is given the three students whose chances of solving it are  $\frac{1}{2}$ ,  $\frac{1}{3}$ ,  $\frac{1}{4}$ . What is the probability in the following cases ? : Only one of them solves it correctly.



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**31.** A problem in Mathematics is given the three students whose chances of solving it are  $\frac{1}{2}$ ,  $\frac{1}{3}$ ,  $\frac{1}{4}$ . What is the probability in the following cases ? : At least one of them solves it.



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**32.** In a set of 10 coins, 2 coins with heads on both sides. A coin is selected at random from this set and tossed five times. Of all the five

times, the result was head, find the probability that the selected coin had heads on both sides.



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**33.** A person has undertaken a construction job. The probabilities are 0.65 that there will be strikes 0.80, that the construction job will be completed on time if there is no strike, and 0.32 that the construction job will be completed on time if there is a strike. Determine the probability that the construction job will be completed on time.



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**34.** There are two bags I and II. Bag I contains 4 white and 3 red balls while another Bag II contains 3 white and 7 red balls. One ball is drawn at random from one of the bags and it is found to be white. Find the probability that it was drawn from Bag I.



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**35.** A bag X contains 4 white balls and 2 black balls, while another bag Y contains 3 white balls and 3 black balls. Two balls are drawn (without replacement) at random from one of the bags and were found to be one white and one black. Find the probability that the balls were drawn from bag Y.



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**36.** Assume that the chances of a patient having a heart attack is 40%. It is also assumed that a

meditation and yoga course reduce the risk of heart attack by 30% and prescription of certain drug reduces its chances by 25%. At a time a patient can choose any one of the two options with equal probabilities. It is given that after going through one of the two options the patient selected at random suffers a heart attack. Find the probability that the patient followed a course of meditation and yoga?



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**37.** An insurance company insured 2000 scooter drivers, 4000 car drivers and 6000 truck drivers. The probability of an accidents are 0.01, 0.03 and 0.15 respectively. One of the insured persons meets with an accident. What is the probability that he is a scooter driver?



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**38.** A card from a pack of 52 playing cards is lost. From the remaining cards of the pack, three cards are drawn at random (without

replacement) and re found to be all spades.

Find the probability that the lost card being a spade.



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**39.** Three persons A,B and C apply for a job of manager in a private company. Chances of their selection are in the ratio 1:2:4. The probabilities that A,B and C can introduce changes to improve profits of the company are 0.8, 0.5 and 0.3 respectively. If the change does not take

place, find the probability that it is due to appointment of C.



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**40.** A man is known to speak the truth 3 out of 5 times. He throws a die and reported that it is a number greater than 4. Find the probability that it is actually a number greater than 4.



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**41.** In a bolt factory, machines A, B and C manufacture respectively 25%, 35%, 40% of the total. Of their output 5, 4 and 2% are defective. A bolt is drawn at random from the product. What is the probability that the bolt drawn is defective?



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**42.** In a bolt factory, three machines A, B and C manufacturers 25, 35 and 40 percent of the total bolts . Of their output 5, 4 and 2 percent

are defective respectively. A bolt is drawn at random and found to be defective. Find the probability that it was manufactured by machine B.



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**43.** In answering a question in a multiple choice test a student either knows the answer or guesses. Let  $\frac{3}{4}$  be the probability that he knows the answer and  $\frac{1}{4}$  be the probability that he guesses. Assuming that a student who guesses at the answer will be correct with probability  $\frac{1}{4}$

. What is the probability that a student knows the answer, given that he answered it correctly ?



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**44.** A girl throws a die. If she gets 5 or 6, she tosses a coin three times and notes the number of heads. If she gets 1, 2, 3 or 4, she tosses a coin two times and notes the number of heads. If she obtained exactly two heads, what is the probability that she throws 1, 2, 3 or 4 with the die.



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**45.** Bag I contains 3 red and 4 black balls and Bag II contains 4 red and 5 black balls. One ball is transferred from Bag I to Bag II and then a ball is drawn from Bag II. The ball so drawn is found to be red in colour. Find the probability that the transferred ball is black



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**46.** There are three coins, one is a two-headed coin (having head on both the faces), another is a biased coin that comes up heads 75% of the time and the third is an unbiased coin. One of the three coins is chosen at random and tossed. If it shows head, what is the probability that it was the two-headed coin?



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**47.** Suppose that the reliability of a HIV test is specified as follows: Of people having HIV, 90%



of the test detect the disease but 10% go undetected. Of people free of HIV, 99% of the test are judged HIV–ive but 1% are diagnosed as showing HIV+ive. From a large population of which only 0.1% have HIV, one person is selected at random, given the HIV test, and the pathologist reports him/her as HIV+ive. What is the probability that the person actually has HIV?



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**48.** A random variable 'X' has a probability distribution  $P(X)$  of the following form (K is constant):

X :	0	1	2	3
P(X) :	3K	2K	K	0

Find K.



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**49.** A bag contains 2 white and 1 red ball. One ball is drawn at random and then put back in the bag after noting its colour. The process is

repeated again. If 'X' denotes the number of red balls recorded in the two draws, describe 'X'.



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**50.** A person plays a game of tossing a coin thrice. For each head he is given Rs 2 by the organiser of the game and for each tail he has to give Rs 1.50 to the organiser. Let  $X$  denote the amount gained or lost by the person. Show that 'X' is a random variable and exhibit it as a function on the sample space of the experiment.



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**51.** A fair die is tossed twice. If the number appearing on the top is less than 3, it is a success, find the probability distribution of successes.



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**52.** A coin is biased so that the head is 3 times as likely to occur as tail. If the coin is tossed 3

times, find the probability distribution of number of tails.



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**53.** Find the probability distribution of number of heads in two tosses of a coin



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**54.** Find the probability distribution for the number of girls in a family with three children,

assuming equal probability for a child being a boy or a girl.



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**55.** Four defective oranges are accidentally mixed with 16 good ones and by looking at them it is not possible to differentiate between them. Three oranges are drawn at random from the lot. Find the probability distribution of  $X$ , the number of defective oranges.



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**56.** Let a pair of dice be thrown and the random variable  $X$  be the sum of the numbers that appear on the two dice. Find the mean (or expectation) of  $X$ .



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**57.** Find the mean and variance of the number obtained on a throw of an unbiased die.



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**58.** Find the mean and variance of the number of heads on the throw of three coins.



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**59.** Two cards are drawn simultaneously (without replacement) from a well-shuffled pack of 52 cards . Find the mean and variance of the number of red cards .



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**60.** A die tossed twice . Getting a number greater than 4 is considered a success . Find the variance of the probability distribution of the number of successes .



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**61.** From a lot of 10 items containing 3 defective items a sample of 4 items is drawn at random. Let the random variable 'X' denote the number of defective items in the sample. If the sample is

drawn without replacement, find: the probability distribution of  $X$ .



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**62.** From a lot of 10 items containing 3 defective items a sample of 4 items is drawn at random. Let the random variable ' $X$ ' denote the number of defective items in the sample. If the sample is drawn without replacement, find: mean of  $X$ .



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**63.** From a lot of 10 items containing 3 defective items a sample of 4 items is drawn at random. Let the random variable 'X' denote the number of defective items in the sample. If the sample is drawn without replacement, find: variance of X.



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**64.** There is a group of 50 people who are patriotic out of which 20 believe in non-violence. Two persons are selected at random out of them, write the probability distribution

for the selected persons who are non-violent.

Also find the mean of the distribution. Explain the importance of non-violence in patriotism.



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**65.** Three numbers are selected at random (without replacement) from first 6 positive integers. Let  $X$  denote the largest of the three numbers obtained. Find the probability distribution of  $X$ . Also, find the mean and variance of the distribution.



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**66.** Six balls are drawn successively from an urn containing 7 red and 9 black balls. Tell whether or not the trials of drawing black balls are Bernoulli trials when after each draw the ball drawn is : replaced in the urn.



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**67.** Six balls are drawn successively from an urn containing 7 red and 9 black balls. Tell whether

or not the trials of drawing black balls are Bernoulli trials when after each draw the ball drawn is : not replaced in the urn.



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**68.** An experiment succeeds thrice as often as it fails. Find the probability that in the next five trials, there will be at least 3 successes.



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**69.** A coin is tossed 6 times. Find the probability of obtaining no head.



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**70.** A coin is tossed 6 times. Find the probability of obtaining 4 heads.



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**71.** A pair of dice is thrown 4 times. If getting a doublet is considered a success, find the probability distribution of number of successes.



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**72.** A pair of dice is thrown 4 times. If getting a doublet is considered a success then find the probability of exactly 2 successes.



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**73.** The probability that a student entering the university will graduate is 0.4. Find the probability that out of 3 students of the University: none will graduate.



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**74.** The probability that a student entering the university will graduate is 0.4. Find the probability that out of 3 students of the University: only one will graduate.



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**75.** The probability that a student entering the university will graduate is 0.4. Find the probability that out of 3 students of the University: all will graduate. Why graduation is minimum qualification for all good well paid jobs?



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**76.** Ten eggs are drawn successively with replacement from a lot containing 10%

defective eggs. Find the probability that there is at least one defective egg.



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77. An owner of a small hotel with 5 rooms is thinking of buying T.V. sets to rent them to room occupants when demanded. He expects that about half of his customers will be willing to get sets on rent. He buys three T.V. sets. Assuming 100% occupancy at all times, find out the probability that: a customer who requests for T.V. will get one.



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**78.** An owner of a small hotel with 5 rooms is thinking of buying T.V. sets to rent them to room occupants when demanded. He expects that about half of his customers will be willing to get sets on rent. He buys three T.V. sets. Assuming 100% occupancy at all times, find out the probability that: some demand will be refused.



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**79.** The probability of a shooter hitting a target is  $\frac{3}{4}$ . How many minimum number of times must he/she fire so that the probability of hitting the target at least once is more than 0.99?



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**80.** Five dice are thrown 729 times. How many times do you expect that at least four dice to show five or six?



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**81.** In a backward state, there are 729 families having six children each. If probability of survival of a girl is  $\frac{1}{3}$  and that of a boy is  $\frac{2}{3}$ , find the number of families having 2 girls and 4 boys. Do you believe that a female child is neglected in backward areas. What steps should be taken to restore respect of a female child in society?



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**82.** A die is thrown again and again until three sixes are obtained. Find the probability of obtaining the third six in the sixth trial of the die.



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**83.** In an exam, 10 questions of true-false type are asked. A student tosses a fair coin to determine his answer to each question. If the coin falls heads, he answers true and if it falls tails, he answers false. Show that the

probability that he answers at most 7 questions correctly is  $\frac{121}{128}$ .



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**84.** Find the mean of the binomial distribution

$$B\left(5, \frac{1}{2}\right)$$



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**85.** The sum of the mean and variance of a Binomial distribution of 6 trials is  $\frac{10}{3}$ , find the



Binomial distribution.



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**86.** The sum of mean and variance of a binomial distribution is 15 and the sum of their squares is 117. Find the Binomial distribution.



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**87.** The mean and variance of the binomial distribution are 4 and  $\frac{4}{3}$  respectively. Find  $p$ .



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**88.** A and B are two candidates seeking admission in a college. The probability that A is selected is 0.7 and the probability that exactly one of them is selected is 0.6. Find the probability that B is selected.



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**89.** The probability of simultaneous occurrence of at least one of two events A and B is  $p$ . If  $p$  is

the probability that exactly one A, B occurs is  $q$ ,

then prove that :

$$P(A') + P(B') = 2 - 2p + q$$



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**90.** 10% of the bulbs produced in a factory are red colour and 2% are red and defective. If one bulb is picked up at random, determine the probability of its being defective if it is red.



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91. Three machines  $E_1, E_2, E_3$  in a certain factory produce 50%, 25% and 25% respectively of the total daily output of electric tubes. It is known that 4% of the tubes produced by each of machines  $E_1$  and  $E_2$  are defective, and that 5% of those produced on  $E_3$  are defective. If one tube is picked up at random from a day's production, calculate the probability that it is defective.



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92. Determine variance and S.D. of the number of heads in three tosses of a coin.



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## Exercise

1. Compute  $P(A | B)$ , if  $P(B) = 0.5$  and  $P(A \cap B) = 0.32$



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2. If  $P(A) = \frac{7}{13}$ ,  $P(B) = \frac{9}{13}$  and  $P(A \cap B) = \frac{4}{13}$ , evaluate  $P(A | B)$



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3. If A and B are two events such that  $P(A) = \frac{1}{4}$ ,  $P(B) = \frac{1}{2}$  and  $P(A \cap B) = \frac{1}{8}$  find  $P(\neg A \text{ and } \neg B)$



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4.

If

$$P(A) = 0.8, P(B) = 0.5 \text{ and } P\left(\frac{B}{A}\right) = 0.4,$$

find :  $P(A \cap B)$



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5. If  $P(A) = 0.8, P(B) = 0.5$  and

$P(B/A) = 0.4$ , find

(i)  $P(A \cap B)$

(ii)  $P(A/B)$

(iii)  $P(A \cup B)$



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6. If  $P(A) = 0.8$ ,  $P(B) = 0.5$  and

$P(B/A) = 0.4$ , find

(i)  $P(A \cap B)$

(ii)  $P(A/B)$

(iii)  $P(A \cup B)$



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7. If  $P(A) = 0.3$ ,  $P(B) = 0.6$  and

$P(B/A) = 0.5$ , find  $P(A/B)$ .





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8. If  $P(A) = \frac{6}{11}$ ,  $P(B) = \frac{5}{11}$  and  
 $P(A \cup B) = \frac{7}{11}$  find:  $P(A \cap B)$

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9. If  $P(A) = \frac{6}{11}$ ,  $P(B) = \frac{5}{11}$  and  
 $P(A \cup B) = \frac{7}{11}$  find:  $P(A | B)$

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10. If  $P(A) = \frac{6}{11}$ ,  $P(B) = \frac{5}{11}$  and  $P(A \cup B) = \frac{7}{11}$  find:  $P(B | A)$



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11. If

$$P(A) = 0.6, P(B) = 0.7 \text{ and } P(A \cup B) = 0.9$$

, then find  $P\left(\frac{A}{B}\right)$  and  $P\left(\frac{B}{A}\right)$



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**12.** Determine  $P(E | F)$  if A coin is tossed three times, where : E : head on third toss , F : heads on first two tosses



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**13.** Determine  $P(E | F)$  if A coin is tossed three times, where : E : at least two heads , F : at most two heads



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14. Determine  $P(E | F)$  : if A coin is tossed three times, where : E : at most two tails , F : at least one tail



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15. A die is thrown three times :

E : 4 appears on the third toss .

F : 6 and 5 appear repectively on first two torses.

Find  $P(E / F)$  .



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16. Determine  $P(E | F)$  Mother, father and son line up at random for a family picture :E : son on one end, F : father in middle



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17. A black and a red dice are rolled :Find the conditional probability of obtaining a sum greater than 9, given that the black die resulted in a 5.



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**18.** A black and a red dice are rolled: Find the conditional probability of obtaining the sum 8, given that the red die resulted in a number less than 4.



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**19.** Let  $E$  and  $F$  be events with  $P(E) = \frac{3}{5}$ ,  $P(F) = \frac{3}{10}$  and  $P(E \cap F) = \frac{1}{5}$ .

Are  $E$  and  $F$  independent?



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20. A fair die is rolled. Consider events

$$E = \{1, 3, 5\}, F = \{2, 3\}, \text{ and } G = \{2, 3, 4, 5\}$$

find :  $P(E | F)$  and  $P(F | E)$



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21. A fair die is rolled. Consider events

$$E = \{1, 3, 5\}, F = \{2, 3\}, \text{ and } G = \{2, 3, 4, 5\}$$

find :  $P(E | G)$  and  $P(G | E)$



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22. A fair die is rolled. Consider events

$E = \{1, 3, 5\}$ ,  $F = \{2, 3\}$ , and  $G = \{2, 3, 4, 5\}$

find :  $P(E \cup F | G)$  and  $P(E \cap F | G)$



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23. A family has two children. What is the probability that both the children are boys given that at least one of them is a boy ?



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**24.** A family has two children. What is the probability that both the children are boys given that at least one of them is a boy ?



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**25.** If there are two children in a family, find the probability that there is at least one girl in a family.



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**26.** Two coins are tossed. What is the probability of getting 2 heads if it is known that at least one head comes up?



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**27.** In a school, there are 1000 students, out of which 430 are girls. It is known that out of 430, 10% of the girls study in class XII. What is the probability that a student chosen randomly studies in Class XII given that the chosen student is a girl?



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**28.** A die is thrown twice and the sum of the numbers appearing is observed to be 6. What is the conditional probability that the number 4 has appeared at least once?



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**29.** Given that the two numbers appearing on throwing two dice are different. Find the

probability of the event 'the sum of numbers on the dice is 4'.



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**30.** Assume that each born child is equally likely to be a boy or a girl. If a family has two children, what is the conditional probability that both are girls given that the youngest is a girl.



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**31.** Assume that each born child is equally likely to be a boy or a girl. If a family has two children, what is the conditional probability that both are girls given that at least one is a girl?



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**32.** Let  $E$  and  $F$  be events with

$$P(E) = \frac{3}{5}, P(F) = \frac{3}{10} \text{ and } P(E \cap F) = \frac{1}{5}.$$

Are  $E$  and  $F$  independent?



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**33.** Two events  $E$  and  $F$  are such that:

$$P(E) = 0.6, P(F) = 0.2 \text{ and } P(E \cup F) = 0.68$$

. Are  $E$  and  $F$  independent?



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**34.** A die marked 1, 2, 3 in red and 4, 5, 6 in green is tossed. Let  $A$  be the event, 'the number is even,' and  $B$  be the event, 'the number is red'.

Are  $A$  and  $B$  independent?



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**35.** Let A and B be independent events with

$P(A) = 0.3$  and  $P(B) = 0.4$  Find:  $P(A \cap B)$



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**36.** Let A and B be independent events with

$P(A) = 0.3$  and  $P(B) = 0.4$  Find:  $P(A \cup B)$



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**37.** Let  $A$  and  $B$  be independent events with

$P(A) = 0.3$  and  $P(B) = 0.4$  Find:  $P(A | B)$



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**38.** Let  $A$  and  $B$  be independent events with

$P(A) = 0.3$  and  $P(B) = 0.4$  Find:  $P(B | A)$



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**39.** If  $P(A) = \frac{1}{2}$ ,  $P(B) = \frac{7}{12}P(\text{not } A \text{ or not } B) = \frac{1}{4}$

State whether A and B are independent .



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**40.** If A and B are two events such that  $P(A) = \frac{1}{4}$ ,  $P(B) = \frac{1}{3}$  and  $P(A \cup B) = \frac{1}{2}$ ,

show that A and B are independent events.



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**41.** Given two independent events A and B such that  $P(A) = 0.3$ , and  $P(B) = 0.6$  Find:  $P(A$  and B)



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**42.** Given two independent events A and B such that  $P(A) = 0.3$ , and  $P(B) = 0.6$  Find:  $P(A$  and not B )



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**43.** Given two independent events A and B such that  $P(A) = 0.3$ , and  $P(B) = 0.6$  Find: P(A or B)



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**44.** Given two independent events A and B such that  $P(A) = 0.3$ , and  $P(B) = 0.6$  Find: P(neither A nor B)



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45. If  $P(A) = 0.2$ ,  $P(A \cup B) = 0.5$ , find  $P(B)$ .

Here A and B are independent events .



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46. If  $P(A) = 0.35$ ,  $P(A \cup B) = 0.60$ , find

$P(B)$ . where A and B are independent events.



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47. If A and B are two independent events such

that  $P(A \cup B) = 0.6$  and  $P(A) = 0.2$  find

$P(B)$ .



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48. If  $P(A) = 0.5$ ,  $P(A \cup B) = 0.7$ , find  $P(B)$  .

Here A and B are independent events .



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49. Given that the events A and B are such that

$$P(A) = \frac{1}{2}, P(A \cup B) = \frac{3}{5} \quad \text{and} \quad P(B) = p$$

.Find p if they are independent.

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50. If  $P(A) = \frac{1}{3}$ ,  $P(B) = \frac{1}{5}$  and  $P(A \cup B) = \frac{11}{30}$ , then find  $P(A/B)$ .

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51. Let A and B be two independent events such that:  $P(A) = \frac{1}{4}$ ,  $P(B) = \frac{1}{2}$ , find  $P(A \text{ or } B)$

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**52.** Let A and B be two independent events such that:  $P(A) = \frac{1}{4}$ ,  $P(B) = \frac{1}{2}$ , find : P(neither A nor B)



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**53.** A coin is tossed thrice and all eight outcomes are assumed equally likely. In which of the following cases are the events A and B independent? A: "the first throw results in head" B: "the last throw results in tail"



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**54.** A coin is tossed thrice and all eight outcomes are assumed equally likely. In which of the following cases are the events A and B independent? A: " the number of heads is two"  
B:"the last throw results in head"



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**55.** A die is thrown. If E is the event 'the number appearing is a multiple of 3' and F be the event



'the number appearing is even' then find whether E and F are independent ?



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**56.** One card is drawn at random from a pack of well shuffled deck of 52 cards. IN which of the following cards are the events E and F independent? : E: the card drawn is spade F: the card drawn is an ace



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**57.** One card is drawn at random from a well shuffled deck of 52 cards. In which of the following cases are the events E and F independent ? E : 'the card drawn is black' F : 'the card drawn is a king'



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**58.** One card is drawn at random from a well shuffled deck of 52 cards. In which of the following cases are the events E and F

independent ?E : 'the card drawn is a king or queen' F : 'the card drawn is a queen or jack'.



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**59.** The odds in favour of an event are 3 : 4. Find the probability of : occurrence



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**60.** The odds in favour of an event are 3 : 4. Find the probability of : non-occurrence of the event.



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**61.** Two cards are drawn at random and without replacement from a pack of 52 playing cards. Find the probability that both the cards are black.



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**62.** The probability of student A passing an examination is  $\frac{3}{7}$  and of student B passing is  $\frac{5}{7}$ . Assuming the two events "A passes, B passes",

as independent, find the probability of : only A passing the examination.



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**63.** The probability of student A passing an examination is  $\frac{3}{7}$  and of student B passing is  $\frac{5}{7}$ . Assuming the two events "A passes, B passes", as independent, find the probability of : only one of them passing the examination



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**64.** Given that the two numbers appearing on throwing two dice are different. Find the probability of the event 'the sum of numbers on the dice is 4'.



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**65.** A box of oranges is inspected by examining three randomly selected oranges drawn without replacement. If all the three oranges are good, the box is approved for sale, otherwise, it is rejected. Find the probability

that a box containing 15 oranges out of which 12 are good and 3 are bad ones will be approved for sale.



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**66.** A die is thrown. If  $E$  is the event 'the number appearing is a multiple of 3' and  $F$  be the event 'the number appearing is even' then find whether  $E$  and  $F$  are independent ?



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**67.** Two balls are drawn at random with replacement from a box containing 10 black and 8 red balls. Find the probability that both balls are red.



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**68.** Two balls are drawn at random with replacement from a box containing 10 black and 8 red balls. Find the probability that first ball is black and second is red.



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**69.** Two balls are drawn at random with replacement from a box containing 10 black and 8 red balls. Find the probability that one of them is black and other is red.



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**70.** An urn contains 10 black and 5 white balls. Two balls are drawn from the urn one after the other without replacement. What is the probability that both drawn balls are black?



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**71.** A bag contains 5 white and 3 black balls. Four balls are successively drawn out without replacement . What is the probability that they are alternately of different colours ?



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**72.** A bag contains 4 red and 3 black balls. A second bag contains 2 red and 4 black balls. One bag is selected at random. From the

selected bag, one ball is drawn. Find the probability that the ball drawn is red.



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**73.** Three cards are drawn successively, without replacement from a pack of 52 well shuffled cards. What is the probability that first two cards are kings and the third card drawn is an ace?



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**74.** A bag A contains 6 white and 7 black balls while the other bag B contains 4 white and 5 black balls. A ball is transferred from the bag A to the bag B. Then a ball is drawn from the bag B. Find the probability that the ball drawn is white.



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**75.** There are three urns A, B and C . Urn A contains 4 white balls and 5 blue balls . Urn B contains 3 white balls and 4 blue balls . Urn C

contains 3 white balls and 6 blue balls . One ball is drawn from each of these urns . What is the probability that out of these three balls drawn, two are white balls and one is a blue ball ?



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**76.** A speaks truth in 70 % of the cases and B in 80 % of the cases. In what percent of cases are they likely to agree in stating the fact ? Do you think, when they agree mean both are speaking truth ?



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**77.** A speaks truth in  $75\%$  of cases and B in  $80\%$  of cases. The percentage of cases they are likely to contradict each other in stating the same fact, is



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**78.** A and B toss a coin alternately till one of them tosses a head and wins the game. If A

starts the game, find their respective probability of winning.



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**79.** A and B throw a die alternatively till one of them gets a '6' and wins the game. Find their respective probabilities of winning, if A starts first.



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**80.** A and B throw a die alternatively till one of them gets a '6' and wins the game. Find their respective probabilities of winning, if A starts first.



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**81.** A and B throw a pair of dice alternately, till one of them gets a total of 10 and wins the game. Find their respective probabilities of winning if A starts first.



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82. A, B and C in tum throw a die and one who gets a 6 first wins the game. A takes the first chance followed by B and C, and the process is repeated till one of them who gets a 6, wins the game. Find the probabilities of each for winning the game .



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**83.** A, B and C in tum throw a die and one who gets a 6 first wins the game. A takes the first chance followed by B and C, and the process is repeated till one of them who gets a 6, wins the game. Find the probabilities of each for winning the game .



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**84.** Three ships A, B, C sail from England to India. Odds in favour of their arriving safely are

2: 5, 3: 7, 6: 1 respectively. Find the chance that they will arrive safely.



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**85.** A husband and his wife appear for an interview for two parts. The probability of husband's selection is  $\frac{1}{7}$  and that of wife's selection is  $\frac{1}{5}$ . What is probability that both of them will be selected?



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**86.** Amit and Nisha appear for an interview for two vacancies in a company. The probability of Amit's selection is  $\frac{1}{5}$  and that of Nisha's selection is  $\frac{1}{6}$ . What is the probability that both of them are selected?



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**87.** A problem is given to three students, whose chances of solving it are :  $\frac{1}{3}$ ,  $\frac{1}{2}$  and  $\frac{1}{5}$  respectively. Find the probability that exactly one of them may solve it.



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**88.** A bag contains 50 tickets numbered 1, 2, 3, ..., 50 of which 5 are drawn at random and arranged in ascending order of magnitude  $x_1 < x_2 < x_3 < x_4 < x_5$ . Find the probability that  $x_3 = 30$ .

a.  $\frac{{}^{.20}C_2 \times {}^{.29}C_2}{{}^{.50}C_5}$

b.  $\frac{{}^{.20}C_2}{{}^{.50}C_5}$

c.  $\frac{{}^{.29}C_2}{{}^{.50}C_5}$

d. None of these



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**89.** A bag contains 100 bolts and 300 nuts, 50% of each have been rusted. One item is chosen at random. Find the probability that chosen item is rusted or a bolt.



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**90.** If  $A$  and  $B$  are two events such that  $P(A) = \frac{1}{4}$ ,  $P(B) = \frac{1}{2}$  and  $P(A \cap B) = \frac{1}{8}$  find  $P(\neg A)$  and  $P(\neg B)$



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**91.** Three coins are tossed once. Find the probability of getting: at least two tails.



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**92.** Three coins are tossed once. Find the probability of getting at least two heads.



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**93.** The probability of A and B achieving a target is  $\frac{3}{4}$  and  $\frac{5}{6}$  respectively. If both of them try then find the probability that at least one of them will achieve the target



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**94.** The probability of A hitting a target is  $\frac{4}{5}$  and that of B hitting it is  $\frac{2}{3}$ . They both fire at the target . Find the probability that : only one of them will hit the target.



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**95.** A die is tossed thrice. Find the probability of getting an odd number at least once.



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**96.** A problem in Mathematics is given to three students whose chances of solving it are :  $\frac{1}{2}$ ,  $\frac{1}{4}$  and  $\frac{1}{5}$ . What is the probability that at least one of them may solve it?



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**97.** A problem is given to three students, whose chances of solving it are :  $\frac{1}{3}$ ,  $\frac{1}{5}$  and  $\frac{1}{6}$ . What is the probability that exactly one of them may solve it.



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**98.** A and B try to solve the problem independently. The probability that A solves the problem is  $\frac{1}{2}$  and that B solves the problem is  $\frac{1}{3}$ . Find the probability that : both of them solve the problem.



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**99.** Probability of solving specific problem independently by A and B are  $\frac{1}{2}$  and  $\frac{1}{3}$  respectively. If both try to solve the problem independently, find the probability that the problem is solved.



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**100.** A and B appeared for an interview. The probability of their selection is  $\frac{1}{3}$  and  $\frac{1}{4}$

respectively. Find the probability that both selected



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**101.** A and B appeared for interview. The probability of their selection is :  $\frac{1}{3}$  and  $\frac{1}{4}$  respectively. Find the probability that : at least one of them selected.



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**102.** A husband and his wife appear for an interview for two parts. The probability of husband's selection is  $\frac{1}{7}$  and that of wife's selection is  $\frac{1}{5}$ . What is probability that both of them will be selected?



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**103.** A husband and his wife appear for an interview for two parts. The probability of husband's selection is  $\frac{1}{7}$  and that of wife's

selection is  $\frac{1}{5}$ . What is probability that only one of them is selected?



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**104.** A husband and his wife appear for an interview for two parts. The probability of husband's selection is  $\frac{1}{7}$  and that of wife's selection is  $\frac{1}{5}$ . What is probability that at least one of them will be selected?



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**105.** A husband and his wife appear for an interview for two parts. The probability of husband's selection is  $\frac{1}{7}$  and that of wife's selection is  $\frac{1}{5}$ . What is probability that none of them will be selected?



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**106.** A can solve 90% of the problems given in a book and B can solve only 70% problems. What is the probability that at least one of them will

solve the problem selected at random from the book?



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**107.** An anti-air craft gun can take maximum four at an enemy plane, moving away from it. The probabilities of hitting the plane at first, second, third and fourth shot are 0.4, 0.3, 0.2 and 0.1 respectively. What is the probability that the gun hits the plane? Do you agree with us that the success will raise the morale of Indian Army?





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**108.** In a lot of 12 microwave ovens, there are 3 defective units. A person has ordered 4 of these units and since each is identically packed. What is the probability that : all units are good.



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**109.** In a lot of 12 microwave ovens, there are 3 defective units. A person has ordered 4 of these

units and since each is identically packed. What is the probability that : exactly 3 units are good.



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**110.** A card from a pack of 52 cards is lost. From the remaining cards of the pack, two cards are drawn and are found to be both diamonds. Find the probability of the lost card being a diamond.



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**111.** A card from a pack of 52 playing cards is lost. From the remaining cards of the pack, two cards are drawn and are found to be all both clubs. Find the probability that the lost card being a clubs.



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**112.** A man is known to speak the truth 3 out of 4 times. He throws a die and reports that it is a six. Find the probability that it is actually a six.



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**113.** Two bags contain : 4 red and 4 black. 2 red and 6 black balls One ball is drawn at random from one of the bags and found to be red. Find the probability that it was drawn from the second bag.



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**114.** Two bags contain 6 red and 3 black, 5 red and 5 black balls. One ball is drawn at random from one of the bags and found to be red. Find

the probability that it was drawn from the second bag.



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**115.** Two bags contain 6 red and 4 black, 3 red and 3 black balls. One ball is drawn at random from one of the bags and found to be red. Find the probability that it was drawn from the second bag.



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**116.** Bag I contains 3 red and 4 black balls while another Bag II contains 5 red and 6 black balls. One ball is drawn at random from one of the bags and it is found to be red. Find the probability that it was drawn from Bag II.



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**117.** There are two bags I and II . Bag I contains 4 white and 3 red balls and bag II contains 6 white and 5 red balls. One ball is drawn at random from one of the bags and is found to

be red. Find the probability that it was drawn from bag II.



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**118.** A bag contains 4 red and 4 black balls, another bag contains 2 red and 6 black balls. One of the two bags is selected at random and a ball is drawn from the bag which is found to be red. Find the probability that the ball is drawn from the first bag.



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**119.** Bag I contains 3 red and 4 black balls, Bag II contains 5 red and 6 black balls. One bag is chosen at random and a ball is drawn which is found to be red. Find the probability that it was drawn from Bag I.



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**120.** Bag I contains 5 red and 7 white balls and bag II contains 4 red and 8 white balls. One of the bags is selected at random and a ball is



drawn from it. The ball is found to be red. Find the probability that ball is drawn from bag II.



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**121.** Give three identical boxes I , II and III, each containing two coins. In box I both coins are gold coins, in box II both are silver coins and in box III there is one gold and one silver coin. A person chooses a box at random and takes out a coin. If the coin is of gold, what is the probability that the other coin in the box is also of gold ?



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**122.** In a tape recorder factory, three machines A, B and C produced 50%, 30% and 20% of total production. The percentage of the defective output of these machines are 3%, 4% and 5% respectively. A tape recorder is selected randomly and found to be defective, find the probability that it is produced by machine A.



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**123.** A motorcycle manufacturing company has two plants A and B. Plant A produces 70 % of motorcycle and plant B produces 30 % . At plant A, 80 of motorcycles are rated as of standard quality and at plant B, 90 % of the motorcycles are rated as of standard quality . A motorcycle is chosen at random and is found to be of standard quality . What is the chance that it has come from plant A ?



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**124.** A motorcycle manufacturing company has two plants A and B. Plant A produces 70 % of motorcycle and plant B produces 30 % . At plant A, 80 of motorcycles are rated as of standard quality and at plant B, 90 % of the motorcycles are rated as of standard quality . A motorcycle is chosen at random and is found to be of standard quality . What is the chance that it has come from plant A ?



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**125.** An insurance company insured 2000 scooters and 3000 motorcycles. The probability of an accident involving scooter and a motorcycle is 0.01 and 0.02. What is the probability that the accidented vehicle was a motorcycle.



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**126.** A doctor is to visit a patient. From the past experience, it is known that the probabilities that he will come by train, bus, scooter or by

other means of transport are respectively  $\frac{3}{10}$ ,  $\frac{1}{5}$ ,  $\frac{1}{10}$  and  $\frac{2}{5}$ . The probabilities that he will be late are  $\frac{1}{4}$ ,  $\frac{1}{3}$ ,  $\frac{1}{12}$ , if he comes by train, bus and scooter respectively, but if he comes by other means of transport, then he will not be late. When he arrives, he is late. What is the probability that he comes by train?



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**127.** A man is known to speak the truth 3 out of 4 times. He throws a die and reports that it is a six. Find the probability that it is actually a six.



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**128.** A bag contains 4 balls. Two balls are drawn at random and are found to be white. What is the probability that all balls are white?



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**129.** Of the students in a college, it is known that 60% reside in hostel and 40% are day scholars (not residing in hostel). Previous year results report that 30% of all students who

reside in hostel attain A grade and 20% of day scholars attain A grade in their annual examination. At the end of the year, one student is chosen at random from the college and he has an A grade, what is the probability that the student is a hostlier?



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**130.** A laboratory blood test is 99% effective in detecting a certain disease when it is in fact, present. However, the test also yields a false positive result for 0.5% of the healthy person



tested (i.e. if a healthy person is tested, then, with probability 0.005, the test will imply he has the disease). If 0.1 percent of the population actually has the disease, what is the probability that a person has the disease given that his test result is positive ?



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**131.** Suppose a girl throws a die. If she gets a 5 or 6, she tosses a coin three times and notes the numbers of heads. If she gets 1,2,3, or 4, she tosses a coin once and notes whether a head or

a tail is obtained. If she attained exactly one head what is the probability that she threw 1,2,3, or 4 with the die?



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**132.** There are three coins, one is a two-headed coin (having head on both the faces), another is a biased coin that comes up heads 75% of the time and the third is an unbiased coin. One of the three coins is chosen at random and tossed. If it shows head, what is the probability that it was the two-headed coin?



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**133.** In a certain college, 4% of boys and 1% of girls are taller than 1.75 metres. Furthermore, 60% of the students in the college are girls. A student is selected at random from the college and is found to be taller than 1.75 metres. Find the probability that the selected student is girl.



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**134.** Coloured balls are distributed in three bags as shown in the following table:

Bag	Colour of the ball		
	Black	White	Red
I	1	2	3
II	2	4	1
III	4	5	3

A bag is selected at random and then two balls are randomly drawn from the selected bag. They happen to be black and red. Find the probability that they come from bag I?



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**135.** Three bags contain balls as shown in the table below:

Bag	Number of white balls	Number of Black balls	Number of Red balls
I	1	2	3
II	2	1	1
III	4	3	2

A bag is

chosen at random and two balls are drawn from it. They happen to be white and red. What is the probability that they come from the III bag?



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**136.** An urn contains 5 red and 2 black balls. Two balls are randomly drawn. Let  $X$  represent the

number of black balls. What are the possible values of  $X$ ? Is  $X$  a random variable ?



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**137.** Let  $X$  represent the difference between the number of heads and the number of tails obtained when a coin is tossed 6 times. What are possible values of  $X$ ?



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**138.** A random variable 'X' has the following probability distribution:

X:	-2	-1	0	1	2	3
P(X):	0.1	K	0.2	2K	0.3	K

Find the

value of K



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**139.** A random variable 'X' has the following probability distribution:

X:	-2	-1	0	1	2	3
P(X):	0.1	K	0.2	2K	0.3	K

Find

$$P(X \leq 1)$$



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**140.** A random variable 'X' has the following probability distribution:

X:	-2	-1	0	1	2	3
P(X):	0.1	K	0.2	2K	0.3	K

Find

$$P(X \geq 0)$$



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141. A random variable has the following probability distribution :

X:	0	1	2	3	4	5	6	7
P(X):	0	K	2K	2K	3K	$K^2$	$2K^2$	$7K^2 + K$

Find K.



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142. A random variable has the following probability distribution :

$X:$	0	1	2	3	4	5	6	7
$P(X):$	0	$K$	$2K$	$2K$	$3K$	$K^2$	$2K^2$	$7K^2 + K$

Obtain

$$P(X \leq 5) \text{ and } P(2 \leq X \leq 5)$$



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**143.** An unbiased coin is thrown thrice. If the random variable  $X$  denotes the number of heads obtained, describe the probability distribution of  $X$ .



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**144.** Find the probability distribution of the number of tails when two coins are tossed.



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**145.** Find the probability distribution of the number of tails when two coins are tossed.



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**146.** A coin is tossed 5 times .  $X$  is the number of heads of observed . Find the probability

distribution of  $X$  .



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**147.** Find the Probability distribution of the number of heads when three coins are tossed.



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**148.** Find the probability distribution of the number of tails when three coins are tossed simultaneously.





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**149.** Find the probability distribution of number of heads in four tosses of a coin.



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**150.** Find the Probability distribution of the number of heads when three coins are tossed.



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**151.** Find the probability distribution of the number of sixes in two tosses of a die .



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**152.** Find the probability distribution of number of doublets in three throws of a pair of dice.



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**153.** Find the probability distribution of the number of successes in two tosses of a die,

where a success is defined as : number greater than 4



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**154.** Find the probability distribution of the number of successes in two tosses of a die, where a success is defined as : six appears on at least one die.



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**155.** Find the probability distribution of number of doublets in three throws of a pair of dice.



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**156.** A pair of dice is thrown 4 times. If getting a doublet is considered a success, find the probability distribution of number of successes.



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**157.** Let  $X$  denote the number of hours you study during a randomly selected school day. The probability that  $X$  can take the values  $x$ , has the following form, where  $k$  is some unknown constant.:

$$P(X = x) = \begin{cases} 0.1 & \text{if } x = 0 \\ kx & \text{if } x = 1 \text{ or } 2 \\ k(5 - x) & \text{if } x = 3 \text{ or } 4 \\ 0 & \text{otherwise} \end{cases}$$

Find the value of  $k$ .



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**158.** Let  $X$  denote the number of hours you study during a randomly selected school day. The probability that  $X$  can take the values  $x$ , has the following form, where  $k$  is some unknown constant.:

$$P(X = x) = \begin{cases} 0.1 & \text{if } x = 0 \\ kx & \text{if } x = 1 \text{ or } 2 \\ k(5 - x) & \text{if } x = 3 \text{ or } 4 \\ 0 & \text{otherwise} \end{cases}$$

What is the probability that you study at least two hours ? Exactly two hours? At most two hours?



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**159.** Let  $X$  denote the number of hours you study during a randomly selected school day. The probability that  $X$  can take the values  $x$ , has the following form, where  $k$  is some unknown constant.:

$$P(X = x) = \begin{cases} 0.1 & \text{if } x = 0 \\ kx & \text{if } x = 1 \text{ or } 2 \\ k(5 - x) & \text{if } x = 3 \text{ or } 4 \\ 0 & \text{otherwise} \end{cases}$$

What is the probability that you study at least two hours ? Exactly two hours? At most two hours?



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**160.** Let  $X$  denote the number of hours you study during a randomly selected school day. The probability that  $X$  can take the values  $x$ , has the following form, where  $k$  is some unknown constant.:

$$P(X = x) = \begin{cases} 0.1 & \text{if } x = 0 \\ kx & \text{if } x = 1 \text{ or } 2 \\ k(5 - x) & \text{if } x = 3 \text{ or } 4 \\ 0 & \text{otherwise} \end{cases}$$

What is the probability that you study at least two hours ? Exactly two hours? At most two hours?



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**161.** Two cards are drawn successively with replacement from a well-shuffled deck of 52 cards. Find the probability distribution of the number of aces.



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**162.** Two cards are drawn successively with replacement from a well-shuffled pack of 52 cards. Find the probability distribution of the number of kings and hence find the mean of the distribution .



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**163.** Two cards are drawn from a well shuffled pack of 52 cards. Find the probability distribution of queens if cards are drawn at random.



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**164.** Two cards are drawn successively with replacement from a well-shuffled deck of 52

cards. Find the probability distribution of the number of aces.



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**165.** Two cards are drawn successively with replacement from a well-shuffled pack of 52 cards. Find the probability distribution of the number of kings and hence find the mean of the distribution .



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**166.** Two cards are drawn one by one without replacement from a well shuffled deck of 52 cards. Find the probability distribution of the number of face cards.



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**167.** Two cards are drawn one by one without replacement from a well shuffled deck of 52 cards. Find the probability distribution of the number of spades.



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**168.** Two cards are drawn successively with replacement from a well-shuffled deck of 52 cards. Find the probability distribution of the number of aces.



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**169.** Two cards are drawn successively with replacement from a well-shuffled deck of 52 cards. Find the probability distribution of the number of aces.



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**170.** From a lot of 30 bulbs which include 6 defectives, a sample of 4 bulbs is drawn at random with replacement. Find the probability distribution of the number of defective bulbs.



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**171.** Three cards are drawn successively with replacement from well- shuffled deck of 52 cards. A random variable  $X$  denotes the

number of spades in three cards. Determine the probability distribution of  $X$ .



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**172.** An urn contains 4 white and 3 red balls. Let 'X' be the number of red balls in a random draw of three balls. Find the mean and variance of X.



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**173.** A coin is biased so that the head is 3 times as likely to occur as tail. If the coin is tossed twice, find the probability distribution of number of tails.



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**174.** A die tossed twice . Getting a number greater than 4 is considered a success . Find the variance of the probability distribution of the number of successes .



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**175.** Find the probability distribution of green balls drawn when 3 balls are drawn one by one without replacement from a bag containing 3 green and 5 white balls



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**176.** 3 defective bulbs are mixed up with 7 good ones. 3 bulbs are drawn at random. Find the probability distribution of the defective bulbs.



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**177.** A coin is biased so that the head is 3 times as likely to occur as tail. If a coin is tossed twice, find the probability distribution of number of tails.



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**178.** We take 8 identical slips of paper, write the number 0 on one of them, number 1 on three of the slips, the number 2 on three of the slips and

number 3 on one of the slips. These slips are folded, put in a box and thoroughly mixed. One slip is then drawn at random from the box. If  $Z$  is the random variable denoting the number written on the drawn slip, find the probability distribution of  $Z$ .



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**179.** From a lot of 10 bulbs which include 3 defectives, a sample of 2 bulbs is drawn at random. Find the probability distribution of the number of defective bulbs.



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**180.** A coin is tossed 5 times .  $X$  is the number of heads of observed . Find the probability distribution of  $X$  .



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**181.** The mean of the number of heads in the two tosses of a coin is \_\_\_\_\_.



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**182.** A random variable has the following probability distribution :

X:	-1	0	1	2
P(X):	$\frac{1}{3}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{3}$

Does it

represent a probability function?



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**183.** A random variable has the following probability distribution :

X:	-1	0	1	2
P(X):	$\frac{1}{3}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{3}$

If yes,

find its mean and variance.



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**184.** Find the mean, variance for the following probability distribution:

X:	0	1	2	3
P(X):	$\frac{1}{8}$	$\frac{3}{8}$	$\frac{3}{5}$	$\frac{1}{8}$



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185. Find  $\mu$ ,  $\sigma_x^2$  and  $\sigma_x$  for the following probability distributions:

X :	0	1	3	5
P(X) :	0.2	0.5	0.2	0.1



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186. Find  $\mu$ ,  $\sigma_x^2$  and  $\sigma_x$  for the following probability distributions:

X :	-2	-1	0	1	2
P(X) :	0.2	0.2	0.4	0.2	0.1



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187. Find  $\mu$ ,  $\sigma_x^2$  and  $\sigma_x$  for the following probability distributions:

X :	-3	-1	0	4
P(X) :	0.2	0.4	0.3	0.1



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188. Find  $\mu$ ,  $\sigma_x^2$  and  $\sigma_x$  for the following probability distributions:

X :	1	2	3	-2	-1
P(X) :	0.10	0.35	0.20	0.30	0.05



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**189.** Two dice are thrown simultaneously. If  $X$  denotes the number of sixes, find the expectation of  $X$ .



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**190.** Find the mean and variance of the number obtained on a throw of an unbiased die.



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**191.** Let  $X$  denote the sum of the numbers obtained when two fair dice are rolled. Find the variance and standard deviation of  $X$ .



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**192.** Find the mean and variance of the probability distribution of the number of sixes in three tosses of a die.



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**193.** Find the probability distribution of number of doublets in three throws of a pair of dice.



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**194.** Two cards are drawn simultaneously (without replacement) from a well-shuffled pack of 52 cards . Find the mean and variance of the number of red cards .



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**195.** Two cards are drawn simultaneously (or successively without replacement) from a well shuffled pack of 52 cards. Find the mean, variance and standard deviation of the number of kings.



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**196.** Two cards are drawn successively with replacement from a well-shuffled deck of 52 cards. Find the probability distribution of the number of aces.





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**197.** A coin is tossed 4 times. Let  $X$  denote the number of heads. Find the probability distribution of  $X$ , its mean and variance.



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**198.** Find the mean and variance of the number of heads on the throw of three coins.



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**199.** Two numbers are selected at random (without replacement) from the first six positive integers. Let  $X$  denote the larger of the two numbers obtained. Find  $E(X)$ .



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**200.** Two bad eggs are mixed accidentally with 10 good ones. Find the probability distribution of the number of bad eggs in 3 eggs drawn at random in succession, without replacement from a lot. Find the mean number of bad eggs drawn.



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**201.** A class has 15 students whose ages are 14, 17, 15, 14, 21, 17, 19, 20, 16, 18, 20, 17, 16, 19 and 20 years. One student is selected in such a manner that each has the same chance of being chosen and the age  $X$  of the selected student is recorded. What is the probability distribution of the random variable  $X$ ? Find mean, variance and standard deviation of  $X$ .



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**202.** There are 40 scholars in a class, out of which 10 are sports- persons. Three scholars are selected at random out of them. Find the probability distribution for the selected persons who are sports-persons. Find the mean of the distribution.



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203.

X:	1	2	3	4	5
P(X):	$\frac{1}{2}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{16}$	$p$

The

probability distribution of a random variable 'X', taking values 1,2,3,4,5 is given: Find the value of p.



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204.

X:	1	2	3	4	5
P(X):	$\frac{1}{2}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{16}$	$p$

The

probability distribution of a random variable 'X', taking values 1,2,3,4,5 is given: Find the mean of X.



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205.

X:	1	2	3	4	5
P(X):	$\frac{1}{2}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{16}$	$p$

The

probability distribution of a random variable 'X', taking values 1,2,3,4,5 is given: Find the variance of X.



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206. From a lot of 15 bulbs which include 5 defectives, a sample of 4 bulbs is drawn one by

one with replacement. Find the probability distribution of the number of defective bulbs.

Hence, find the mean of the distribution.



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**207.** Find the probability distribution of white balls drawn when 3 balls are drawn one by one without replacement from a bag containing 4 white and 6 red balls .



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**208.** Two numbers are selected at random (without replacement) from the first six positive integers. Let  $X$  denote the larger of the two numbers obtained. Find  $E(X)$ .



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**209.** An urn contains 3 white and 6 red balls. 4 balls are drawn one by one with replacement from the urn. Find the probability distribution of the number of red balls drawn. Also find mean and variance of the distribution.

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**210.** Obtain binomial distribution, if :

$n = 6, p = \frac{1}{3}$ . Find the mean

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**211.** Obtain binomial distribution, if :

$n = 5, p = \frac{1}{6}$

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**212.** Suppose  $X$  has a binomial distribution  $B\left(6, \frac{1}{2}\right)$ . Show that  $X = 3$  is the most likely outcome .



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**213.** A coin is tossed 7 times. What is the probability that head appears on odd number of times?



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**214.** A coin is tossed 7 times. What is the probability that tail appears on odd number of times?



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**215.** A coin is tossed 5 times. What is the probability that head appears on odd number of times?



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**216.** A coin is tossed 5 times . What is the probability of getting at least 3 heads ?



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**217.** A coin is tossed 5 times. What is the probability of getting : at most 2 heads.



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**218.** A coin is tossed 5 times. What is the probability of getting : no head.



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**219.** A coin is tossed 5 times. What is the probability of getting : 3 heads?



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**220.** A coin is tossed 6 times. Find the probability of obtaining 4 heads.



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**221.** If a fair coin is tossed 10 times, find the probability of: exactly six heads



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**222.** If a fair coin is tossed 10 times, find the probability of: at least six heads



**Watch Video Solution**

**223.** If a fair coin is tossed 10 times, find the probability of: at most six heads



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**224.** Find the probability of getting 5 exactly twice in 7 throws of a die.



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**225.** Find the probability of throwing at most 2 sixes in 6 throws of a single die.



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**226.** A die is thrown 6 times. If getting an odd number is a success, what is the probability of at least 4 successes.



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**227.** A die is thrown 6 times. If 'getting an odd number' is a success, what is the probability of 5 successes?



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**228.** A die is thrown 6 times. If getting an odd number is a success, what is the probability of at least 4 successes.



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**229.** A die is thrown 6 times. If getting an 'odd number' is success, find the probability of 5 successes.



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**230.** A die is thrown 6 times. If getting an 'odd (even) number' is success, find the probability no success?



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**231.** A die is thrown 10 times. If getting an even number is considered a success, find the probability of at least 9 successes.



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**232.** A pair of dice is thrown 7 times. If 'getting a total of 7' is considered 'success', find the probability of getting : no success.



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**233.** A pair of dice is thrown 7 times. If 'getting a total of 7' is considered 'success', find the probability of getting : at least 6 successes.



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**234.** Ten eggs are drawn successively with replacement, from a lot containing 10% defectice eggs. Find the probability that there is at least one defective egg.



**Watch Video Solution**

**235.** Find the probability of getting 5 exactly twice in 7 throws of a die.



**Watch Video Solution**

**236.** Find the probability of throwing at most 2 sixes in 6 throws of a single die.



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**237.** The probability of a shooter hitting a target is  $\frac{3}{4}$ . If he shoots 10 times, find the probability of hitting 8 targets successfully.



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**238.** Suppose that 90% of people are right-handed. What is the probability that at most 6 of a random sample of 10 people are right-handed?



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**239.** Four dice are thrown simultaneously. If the occurrence of 2, 4 or 6 in single die is considered a success, find the probability of at least three successes.



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**240.** Four dice are thrown simultaneously. If the occurrence of 2, 3 or 4 in single die is considered a success, find the probability of at least three successes.



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**241.** A bag consists of 10 balls each marked with one of the digits 0 to 9. If four balls are drawn successively with replacement from the bag,

what is the probability that none is marked with the digit 0?



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**242.** An urn contains 25 balls of which 10 balls bear a mark 'X' and the remaining 15 bear a mark 'Y'. A ball is drawn at random from the urn, its mark is noted down and it is replaced. If 6 balls are drawn in this way, find the probability that all will bear 'X' mark.



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**243.** An urn contains 25 balls of which 10 balls bear a mark 'X' and the remaining 15 bear a mark 'Y'. A ball is drawn at random from the urn, its mark is noted down and it is replaced. If 6 balls are drawn in this way, find the probability that not more than 2 will bear 'Y' mark.



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**244.** An urn contains 25 balls of which 10 balls bear a mark 'X' and the remaining 15 bear a mark 'Y'. A ball is drawn at random from the urn,

its mark is noted down and it is replaced. If 6 balls are drawn in this way, find the probability that at least one ball will bear 'Y' mark.



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**245.** An urn contains 25 balls of which 10 balls bear a mark 'X' and the remaining 15 bear a mark 'Y'. A ball is drawn at random from the urn, its mark is noted down and it is replaced. If 6 balls are drawn in this way, find the probability that the number of balls with 'X' mark and 'Y' mark will be equal.



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**246.** There are 5% defective items in a large bulk of items. What is the probability that a sample of 10 items will include not more than one defective item?



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**247.** The items produced by a company contain 10% defective items. Show that the probability

of getting 2 defective items in a sample of 8

times is  $\frac{28 \times 9^6}{10^8}$ .



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**248.** In a box containing 100 bulbs, 10 are defective. The probability that out of a sample of 5 bulbs none is defective is :



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**249.** In a box containing 100 bulbs, 10 are defective. What is the probability that out of a sample of 5 bulbs, exactly 2 are defective?



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**250.** The probability that a bulb produced by a factory will fuse after 150 days of use is 0.05. Find the probability that out of 5 such bulbs more than one will fuse after 150 days of use.



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**251.** In a hurdle race, a player has to cross 10 hurdles. The probability that he will clear each hurdle is  $\frac{5}{6}$ . What is the probability that he will knock down fewer than 2 hurdles?



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**252.** Assume that on an average one telephone number out of 15 called between 2 P.M. and 3 P.M. on week days is busy. What is the probability that if six randomly selected



telephone numbers are called, at least three of them will be busy?



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**253.** If getting a '5' or a '6' in the throw of an unbiased die is a 'success' and the random variable 'X' denotes the number of successes in six throws of the die, find  $P_X[X \geq 4]$



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**254.** On a multiple choice examination with three possible answers for each of the five questions, what is the probability that a candidate would get four or more correct answers just by guessing ?



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**255.** In a hospital, there are 5 dialysis machine. The chance of any one of them being defective during a day is  $\frac{1}{10}$ . Find the probability that two machines will be out of order on the same

day. What is the probability that at least one machine is in working order? Is this situation alright for a small hospital?



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**256.** Calculate  $P(r)$  for  $r = 1, 2, 3, 4$  and  $5$  by using the recurrence formula of the binomial distribution for the following. Hence, draw the histogram for the distribution:  $p = \frac{1}{3}, n = 5$



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**257.** Calculate  $P(r)$  for  $r = 1, 2, 3, 4$  and  $5$  by using the recurrence formula of the binomial distribution for the following. Hence, draw the histogram for the distribution:  $p = \frac{1}{3}, n = 5$



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**258.** Five dice are thrown 729 times. How many times do you expect that at least four dice to show five or six?



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**259.** An unbiased coin is tossed 4 times. Find the mean and variance of the number of heads obtained.



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**260.** If the mean and variance of a binomial distribution are 9 and 6 respectively, find the number of trials.



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**261.** The sum of mean and variance of a binomial distribution of 18 trials is 10, find the Binomial distribution.



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**262.** If the sum of the mean and variance of a binomial distribution of 5 trials is  $\frac{35}{16}$ , find the distribution.



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**263.** The mean and variance of a binomial variable  $X$  are respectively 4 and  $\frac{4}{5}$ . Find

$$P(X \geq 3)$$



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**264.** If the sum of mean and variance of a binomial distribution is 1.8 for five trials, find the distribution.



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**265.** Determine the binomial distribution whose mean is 10 and whose standard deviation is  $2\sqrt{2}$ .



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**266.** Find the binomial distribution whose mean is 4 and variance is 3.



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**267.** Find the binomial distribution whose: mean is 9 and variance is 6.



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**268.** If 12 dice are rolled at random, obtain the mean and variance of the distribution of successes, if 'getting a number greater than 4' is considered a success.



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**269.** A die is thrown 20 times and getting a number 'greater than 4' is considered a success. Find the mean and the variance of the number of successes.



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**270.** 10 coins are tossed at random. Obtain the mean and variance of the number of heads obtained.



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**271.** The sum and product of the mean and variance of a binomial distribution are 3.5 and 3 respectively. Find the binomial distribution.



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**272.** A die is thrown 6 times. Find the mean and variance of the number of aces.



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**273.** Eight dice are rolled at random. Find the mean and variance of number of successes if : getting an odd number is success.



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**274.** Eight dice are rolled at random. Find the mean and variance of number of successes if : getting a number less than 3 is success.



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**275.** Two dice are rolled at random 5 times. Obtain the mean and variance of the distribution of doublets obtained.



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**276.** The mean and variance of a binomial variable  $X$  are respectively 4 and  $\frac{4}{3}$ . Find  $P(X \geq 1)$



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**277.** If the sum of mean and variance of a binomial distribution is 4.8 for five trials, find the distribution.



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**278.** A discrete random variable 'X' has mean equal to 3 and variance equal to 2. Assuming that the underlying distribution of 'X' is binomial, find the distribution and hence obtain:  $P(X = 0)$



**Watch Video Solution**

**279.** A discrete random variable 'X' has mean equal to 3 and variance equal to 2. Assuming that the underlying distribution of 'X' is binomial, find the distribution and hence obtain:  $P(X = 0)$



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**280.** Determine the binomial distribution whose mean is 10 and whose standard deviation is 8.





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**281.** Determine the binomial distribution whose mean is 10 and whose standard deviation is 8.



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**282.** The screws produced by a certain machine were checked by examining samples of 7. The following table shows the distribution of 128 samples according to the number of defective items they contained.



No. of defectives in a sample of 7 is

	0	1	2	3	4	5	6	7
No of samples	7	6	19	35	30	23	7	1
								$N = 128$

Fit a

binomial distribution and find the expected frequencies if the chance of screw being defective is  $\frac{1}{2}$ . Also find the mean and variance of the fitted distribution.



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**283.** Given that E and F are events such that  $P(E) = 0.6$ ,  $P(F) = 0.3$  and  $P(E \cap F) = 0.2$  find  $P(E | F)$  and  $P(F | E)$



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**284.** Compute  $P(A | B)$ , if  $P(B) = 0.5$  and  $P(A \cap B) = 0.32$



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**285.** If

$P(A) = 0.8$ ,  $P(B) = 0.5$  and  $P\left(\frac{B}{A}\right) = 0.4$ ,

find :  $P(A \cap B)$



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**286.** If  $P(A) = 0.8$ ,  $P(B) = 0.5$  and

$P(B | A) = 0.4$  find:  $P(A | B)$



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**287.**

if

$P(A) = 0.8$ ,  $P(B) = 0.5$  and  $P\left(\frac{B}{A}\right) = 0.4$ ,

find :  $P(A \cap B)$



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**288.** Evaluate  $P(A \cup B)$ , if  
 $2P(A) = P(B) = \frac{5}{13}$  and  $P(A/B) = \frac{2}{5}$ .



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**289.** If  $P(A) = \frac{6}{11}$ ,  $P(B) = \frac{5}{11}$  and  
 $P(A \cup B) = \frac{7}{11}$  find:  $P(A \cap B)$



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290. If  $P(A) = \frac{6}{11}$ ,  $P(B) = \frac{5}{11}$  and  
 $P(A \cup B) = \frac{7}{11}$  find:  $P(A | B)$



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291. If  $P(A) = \frac{6}{11}$ ,  $P(B) = \frac{5}{11}$  and  
 $P(A \cup B) = \frac{7}{11}$  find:  $P(B | A)$



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**292.** Determine  $P(E | F)$  if A coin is tossed three times, where : E : head on third toss , F : heads on first two tosses



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**293.** Determine  $P(E | F)$  if A coin is tossed three times, where : E : at least two heads , F : at most two heads



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**294.** Determine  $P(E | F)$  : if A coin is tossed three times, where : E : at most two tails , F : at least one tail



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**295.** Determine  $P(E | F)$  if two coins are tossed once, where : E : tail appears on one coin, F : one coin shows head



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**296.** Determine  $P(E | F)$  if two coins are tossed once, where : E : no tail appears, F : no head appears



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**297.** Determine  $P(E | F)$  if A die is thrown three times, where : E : 4 appears on the third toss, F : 6 and 5 appears respectively on first two tosses



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**298.** Determine  $P(E | F)$  Mother, father and son line up at random for a family picture :E : son on one end, F : father in middle



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**299.** A black and a red dice are rolled :Find the conditional probability of obtaining a sum greater than 9, given that the black die resulted in a 5.



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**300.** A black and a red dice are rolled: Find the conditional probability of obtaining the sum 8, given that the red die resulted in a number less than 4.



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**301.** A fair die is rolled. Consider events  $E = \{1, 3, 5\}$ ,  $F = \{2, 3\}$ , and  $G = \{2, 3, 4, 5\}$  find :  $P(E | F)$  and  $P(F | E)$



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**302.** A fair die is rolled. Consider events

$$E = \{1, 3, 5\}, F = \{2, 3\}, \text{ and } G = \{2, 3, 4, 5\}$$

find :  $P(E | G)$  and  $P(G | E)$



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**303.** A fair die is rolled. Consider events

$$E = \{1, 3, 5\}, F = \{2, 3\}, \text{ and } G = \{2, 3, 4, 5\}$$

find :  $P(E \cup F | G)$  and  $P(E \cap F | G)$



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**304.** Assume that each born child is equally likely to be a boy or a girl. If a family has two children, what is the conditional probability that both are girls given that the youngest is a girl.



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**305.** Assume that each born child is equally likely to be a boy or a girl. If a family has two children, what is the conditional probability

that both are girls given that at least one is a girl?



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**306.** An instructor has a question bank consisting of 300 easy True / False questions, 200 difficult True / False questions, 500 easy multiple choice questions and 400 difficult multiple choice questions. If a question is selected at random from the question bank, what is the probability that it will be an easy

question given that it is a multiple choice question?



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**307.** Given that the two numbers appearing on throwing two dice are different. Find the probability of the event 'the sum of numbers on the dice is 4'.



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**308.** Consider the experiment of throwing a die, if a multiple of 3 comes up, throw the die again and if any other number comes, toss a coin. Find the conditional probability of the event 'the coin shows a tail', given that 'at least one die shows a 3'.



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**309.** If  $P(A) = \frac{1}{2}$ ,  $P(B) = 0$ ,  $P(A//B)$  is :

A. 0

B.  $\frac{1}{2}$

C. not defined

D. 1

**Answer:**



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**310.** If  $A$  and  $B$  are two events such that

$$A \cap B \neq \phi, P\left(\frac{A}{B}\right) = P\left(\frac{B}{A}\right). \text{ Then.}$$

A.  $A \subset B$  but  $A \neq B$



B.  $A = B$

C.  $A \cap B = \phi$

D.  $P(A) = P(B)$

**Answer:**



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**311.** If  $P(A) = \frac{3}{5}$ ,  $P(B) = \frac{1}{5}$  find  $P(A \cap B)$  if

A and B are independent events.



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**312.** Two cards are drawn at random and without replacement from a pack of 52 playing cards. Find the probability that both the cards are black.



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**313.** A box of oranges is inspected by examining three randomly selected oranges drawn without replacement. If all the three oranges are good, the box is approved for sale, otherwise, it is rejected. Find the probability

that a box containing 15 oranges out of which 12 are good and 3 are bad ones will be approved for sale.



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**314.** A fair coin and an unbiased die are tossed. Let A be the event 'head appears on the coin' and B be the event '3 on the die'. Check whether A and B are independent events or not.



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**315.** A die marked 1, 2, 3 in red and 4, 5, 6 in green is tossed. Let A be the event, 'the number is even,' and B be the event, 'the number is red'. Are A and B independent?



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**316.** Let E and F be events with  $P(E) = \frac{3}{5}$ ,  $P(F) = \frac{3}{10}$  and  $P(E \cap F) = \frac{1}{5}$ . Are E and F independent?



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**317.** Given that the events A and B are such that

$$P(A) = \frac{1}{2}, P(A \cup B) = \frac{3}{5} \quad \text{and} \quad P(B) = p$$

.Find p if they are independent.



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**318.** Let A and B be independent events with

$$P(A) = 0.3 \text{ and } P(B) = 0.4 \text{ Find: } P(A \cap B)$$



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**319.** Let A and B be independent events with

$P(A) = 0.3$  and  $P(B) = 0.4$  Find:  $P(A \cup B)$



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**320.** Let A and B be independent events with

$P(A) = 0.3$  and  $P(B) = 0.4$  Find:  $P(A | B)$



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**321.** Let A and B be independent events with

$P(A) = 0.3$  and  $P(B) = 0.4$  Find:  $P(B | A)$



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**322.** If A and B are two events such that :

$P(A) = \frac{1}{4}$ ,  $P(B) = \frac{1}{2}$  and  $P(A \cap B) = \frac{1}{8}$ ,

find  $P(\text{not A and not B})$ .



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**323.** Events A and B are such that

$$P(A) = \frac{1}{2}, P(B) = \frac{7}{12} \text{ and } P(\text{not } A \text{ or not } B) = \frac{1}{4}. \text{ State whether A and B are independent.}$$



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**324.** Given two independent events A and B

such that  $P(A) = 0.3$ , and  $P(B) = 0.6$  Find:

$P(A \text{ and } B)$



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**325.** Given two independent events A and B such that  $P(A) = 0.3$ , and  $P(B) = 0.6$  Find:  
 $P(A \text{ and not } B)$



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**326.** Given two independent events A and B such that  $P(A) = 0.3$ , and  $P(B) = 0.6$  Find:  
 $P(A \text{ or } B)$



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**327.** Given two independent events A and B such that  $P(A) = 0.3$ , and  $P(B) = 0.6$  Find:  
P(neither A nor B)



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**328.** A die is tossed thrice. Find the probability of getting an odd number at least once.



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**329.** Two balls are drawn at random with replacement from a box containing 10 black and 8 red balls. Find the probability that both balls are red.



**Watch Video Solution**

**330.** Two balls are drawn at random with replacement from a box containing 10 black and 8 red balls. Find the probability that first ball is black and second is red.



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**331.** Two balls are drawn at random with replacement from a box containing 10 black and 8 red balls. Find the probability that one of them is black and other is red.



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**332.** Probability of solving specific problem independently by A and B are  $\frac{1}{2}$  and  $\frac{1}{3}$  respectively. If both try to solve the problem

independently, find the probability that the problem is solved.



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**333.** Probability of solving specific problem independently by A and B are  $\frac{1}{2}$  and  $\frac{1}{3}$  respectively. If both try to solve the problem independently, find the probability that exactly one of them solves the problem.



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**334.** One card is drawn at random from a pack of well shuffled deck of 52 cards. IN which of the following cards are the events E and F independent? : E: the card drawn is spade F: the card drawn is an ace



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**335.** One card is drawn at random from a pack of well shuffled deck of 52 cards. IN which of the following cards are the events E and F

independent? : E: the card drawn is black F: the card drawn is a king



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**336.** One card is drawn at random from a well shuffled deck of 52 cards. In which of the following cases are the events E and F independent ? E : 'the card drawn is a king or queen' F : 'the card drawn is a queen or jack'.



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**337.** In a hostel, 60% of the students read Hindi news paper, 40% read English news paper and 20% read both Hindi and English news papers. A student is selected at random. Find the probability that she reads neither Hindi nor English news papers.



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**338.** In a hostel, 60% of the students read Hindi newspaper, 40% read English newspaper and 20% read both Hindi and English news paper. A



student is selected at random. If she reads Hindi newspaper, find the probability that she reads English newspaper.



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**339.** In a hostel, 60% of the students read Hindi newspaper, 40% read English newspaper and 20% read both Hindi and English news paper. A student is selected at random. If she reads English newspaper, find the probability that she reads Hindi newspaper.



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**340.** The probability of obtaining an even prime number on each die, when a pair of dice is rolled is:

A. 0

B.  $\frac{1}{3}$

C.  $\frac{1}{12}$

D.  $\frac{1}{36}$

**Answer:**



**341.** Two events A and B will be independent, if:

A. A and B are mutually exclusive

B.  $P(A'B') = [1 - P(A)][1 - P(B)]$

C.  $P(A) = P(B)$

D.  $P(A) + P(B) = 1$

**Answer:**



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**342.** An urn contains 5 red and 5 black balls. A ball is drawn at random, its colour is noted and is returned to the urn. Moreover, 2 additional balls of the colour drawn are put in the urn and then a ball is drawn at random. What is the probability that the second ball is red?



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**343.** A bag contains 4 red and 4 black balls, another bag contains 2 red and 6 black balls. One of the two bags is selected at random and

a ball is drawn from the bag which is found to be red. Find the probability that the ball is drawn from the first bag.



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**344.** Of the students in a college, it is known that 60% reside in hostel and 40% are day scholars (not residing in hostel). Previous year results report that 30% of all students who reside in hostel attain A grade and 20% of day scholars attain A grade in their annual examination. At the end of the year, one

student is chosen at random from the college and he has an A grade, what is the probability that the student is a hostlier?



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**345.** In answering a question in a multiple choice test a student either knows the answer or guesses. Let  $\frac{3}{4}$  be the probability that he knows the answer and  $\frac{1}{4}$  be the probability that he guesses. Assuming that a student who guesses at the answer will be correct with probability  $\frac{1}{4}$ . What is the probability that a

student knows the answer, given that he answered it correctly ?



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**346.** A laboratory blood test is 99% effective in detecting a certain disease when it is in fact, present. However, the test also yields a false positive result for 0.5% of the healthy person tested (i.e. if a healthy person is tested, then, with probability 0.005, the test will imply he has the disease). If 0.1 percent of the population actually has the disease, what is the probability

that a person has the disease given that his test result is positive ?



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**347.** A coin is tossed 5 times . What is the probability of getting 5 heads ?



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**348.** A die is tossed once. The probability of getting an odd number is :







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**349.** A factory has two machines A and B. Past record shows that machine A produced 60% of the items of output and machine B produced 40% of the items. Further, 2% of the items produced by machine A and 1% produced by machine B were defective. All the items are put into one stockpile and then one item is chosen at random from this and is found to be defective. What is the probability that it was produced by machine B?



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**350.** Two cars are 351 km apart. They start at the same time and drive towards each other. One travels at 70 km/hr and the other travels at 65 km/hr. How much time do they take to meet each other?



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**351.** A coin is tossed once, what is the probability that one head occurs?



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**352.** A manufacturer has three machine operators A, B and C. The first operator A produces 1% defective items, where as the other two operators B and C produce 5% and 7% defective items respectively. A is on the job for 50% of the time, B is on the job for 30% of the time and C is on the job for 20% of the time. A defective item is produced, what is the probability that it was produced by A?



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**353.** A card from a pack of 52 cards is lost. From the remaining cards of the pack, two cards are drawn and are found to be both diamonds. Find the probability of the lost card being a diamond.



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**354.** Probability that A speaks truth is  $\frac{4}{5}$ . A coin is tossed. A reports that a head appears. The probability that actually there was head is

A.  $\frac{4}{5}$

B.  $\frac{1}{2}$

C.  $\frac{1}{5}$

D.  $\frac{2}{5}$

**Answer:**



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**355.** If  $A$  and  $B$  are two events such that  $A \subset B$  and  $P(B) \neq 0$ , then which of the following is correct?

A.  $P\left(\frac{A}{B}\right) = \frac{P(B)}{P(A)}$

B.  $P\left(\frac{A}{B}\right) < P(A)$

C.  $P\left(\frac{A}{B}\right) \geq P(A)$

D. none of these

**Answer:**



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**356.** State which of the following are not the probability distributions of a random variable.

Give reasons for your answer.

X	0	1	2
P(X)	0.4	0.4	0.2



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**357.** State which of the following are not the probability distributions of a random variable.

Give reasons for your answer.

X	0	1	2	3	4
P(X)	0.1	0.5	0.2	-0.1	0.3



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**358.** State which of the following are not the probability distributions of a random variable.

Give reasons for your answer.

$Y$	$-1$	$0$	$1$
$P(Y)$	$0.6$	$0.1$	$0.2$



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**359.** State which of the following are not the probability distributions of a random variable.



Give reasons for your answer.

Z	3	2	1	0	-1
P(Z)	0.3	0.2	0.4	0.1	0.05



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**360.** An urn contains 5 red and 2 black balls. Two balls are randomly drawn. Let  $X$  represent the number of black balls. What are the possible values of  $X$ ? Is  $X$  a random variable ?



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**361.** Let  $X$  represent the difference between the number of heads and the number of tails obtained when a coin is tossed 6 times. What are possible values of  $X$ ?



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**362.** Find the probability distribution of number of heads in two tosses of a coin



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**363.** Find the probability distribution of number of tails in the simultaneous tosses of three coins.



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**364.** Find the probability distribution of number of heads in four tosses of a coin.



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**365.** Find the probability distribution of the number of successes in two tosses of a die, where a success is defined as : number greater than 4



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**366.** Find the probability distribution of the number of successes in two tosses of a die, where a success is defined as : six appears on at least one die.



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**367.** From a lot of 30 bulbs which include 6 defectives, a sample of 4 bulbs is drawn at random with replacement. Find the probability distribution of the number of defective bulbs.



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**368.** A coin is biased so that the head is 3 times as likely to occur as tail. If the coin is tossed

twice, find the probability distribution of number of tails.



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**369.** A random variable has the following probability distribution :

X	0	1	2	3	4	5	6	7
P(X)	0	$k$	$2k$	$2k$	$3k$	$k^2$	$2k^2$	$7k^2 + k$

Find K.



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**370.** A random variable has the following probability distribution :

X	0	1	2	3	4	5	6	7
P(X)	0	k	2k	2k	3k	k <sup>2</sup>	2k <sup>2</sup>	7k <sup>2</sup> +k

Find

$$P(X < 3)$$



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**371.** A random variable has the following probability distribution :

X	0	1	2	3	4	5	6	7
P(X)	0	k	2k	2k	3k	k <sup>2</sup>	2k <sup>2</sup>	7k <sup>2</sup> + k

Find

$$P(X > 6)$$



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**372.** A random variable has the following probability distribution :

X	0	1	2	3	4	5	6	7
P(X)	0	k	2k	2k	3k	k <sup>2</sup>	2k <sup>2</sup>	7k <sup>2</sup> + k

Find P(0



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**373.** The random variable  $X$  has a probability distribution  $P(X)$  of the following form, where  $k$  is some number :

$$P(x) = \{(k, \text{ if } x = 0), (2k, \text{ if } x = 1), (3k, \text{ if } x = 2), (0, \text{ if } x = 3)\}$$

Determine the value of  $k$ .



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**374.** The random variable  $X$  has a probability distribution  $P(X)$  of the following form, where  $k$  is some number :

$$P(x) = \{(k, \text{ if } x = 0), (2k, \text{ if } x = 1), (3k, \text{ if } x = 2), (0, \text{ if } x = 3)\}$$

$x = 2), (0, , , , ) : \}$

find

$P(X < 2), P(X \leq 2), P(X \geq 2).$



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**375.** Find the mean number of heads in three tosses of a fair coin.



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**376.** Two dice are thrown simultaneously. If  $X$  denotes the number of sixes, find the

expectation of  $X$ .



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**377.** Two numbers are selected at random (without replacement) from the first six positive integers. Let  $X$  denote the larger of the two numbers obtained. Find  $E(X)$ .



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**378.** Let  $X$  denote the sum of the numbers obtained when two fair dice are rolled. Find the variance and standard deviation of  $X$ .



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**379.** A class has 15 students whose ages are 14, 17, 15, 14, 21, 17, 19, 20, 16, 18, 20, 17, 16, 19 and 20 years. One student is selected in such a manner that each has the same chance of being chosen and the age  $X$  of the selected student is recorded. What is the probability distribution of

the random variable  $X$ ? Find mean, variance and standard deviation of  $X$ .



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**380.** In a meeting, 70% of the members favour and 30% oppose a certain proposal. A member is selected at random and we take  $X = 0$  if he opposed, and  $X = 1$  if he is in favour. Find  $E(X)$  and  $Var(X)$ .



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**381.** The mean of the numbers obtained on throwing a die having written 1 on three faces, 2 on two faces and 5 on one face is:

A. 1

B. 2

C. 5

D.  $\frac{8}{3}$

**Answer:**



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**382.** Suppose that two cards are drawn at random from a deck of cards. Let  $X$  be the number of aces obtained. Then the value of  $E(X)$  is:

A.  $\frac{37}{221}$

B.  $\frac{5}{13}$

C.  $\frac{1}{13}$

D.  $\frac{2}{13}$

**Answer:**



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**383.** A die is thrown 6 times. If 'getting an odd number' is a success, what is the probability of 5 successes?



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**384.** A die is thrown 6 times. If getting an odd number is a success, what is the probability of at least 4 successes.



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**385.** A die is thrown 6 times. If getting an 'odd number' is success, find the probability at most 5 successes.



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**386.** A pair of dice is thrown 4 times. If getting a doublet is considered a success then find the probability of exactly 2 successes.



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**387.** There are 5% defective items in a large bulk of items. What is the probability that a sample of 10 items will include not more than one defective item?



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**388.** Five cards are drawn successively with replacement from a well-shuffled deck of 52 cards. What is the probability that all the five cards are spades?



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**389.** Five cards are drawn successively with replacement from a well-shuffled deck of 52 cards. What is the probability that only 3 cards are spades?



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**390.** Five cards are drawn successively with replacement from a well-shuffled deck of 52 cards. What is the probability that none is a spade?



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**391.** The probability that a bulb produced by a factory will fuse after 150 days of use is 0.05. Find the probability that out of 5 such bulbs none will fuse after 150 days of use.



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**392.** The probability that a bulb produced by a factory will fuse after 150 days of use is 0.05. Find the probability that out of 5 such bulbs

not more than one will fuse after 150 days of use.



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**393.** The probability that a bulb produced by a factory will fuse after 150 days of use is 0.05. Find the probability that out of 5 such bulbs more than one will fuse after 150 days of use.



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**394.** The probability that a bulb produced by a factory will fuse after 150 days of use is 0.05. Find the probability that out of 5 such bulbs at least one bulb will fuse after 150 days of use.



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**395.** A bag consists of 10 balls each marked with one of the digits 0 to 9. If four balls are drawn successively with replacement from the bag, what is the probability that none is marked with the digit 0?



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**396.** In an examination, 20 questions of true-false type are asked. Suppose a student tosses a fair coin to determine his answer to each question. If the coin falls heads, he answers 'true', if it falls tails, he answers 'false'. Find the probability that he answers at least 12 questions correctly.



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**397.** Suppose  $X$  has a binomial distribution  $B\left(6, \frac{1}{2}\right)$ . Show that  $X = 3$  is the most likely outcome .



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**398.** On a multiple choice examination with three possible answers for each of the five questions, what is the probability that a candidate would get four or more correct answers just by guessing ?



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**399.** A person buys a lottery ticket in 50 lotteries, in each of which his chance of winning a prize is  $\frac{1}{100}$ . What is the probability that he will win a prize at least once.



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**400.** A person buys a lottery ticket in 50 lotteries, in each of which his chance of winning

a prize is  $\frac{1}{100}$ . What is the probability that he will win a prize exactly once.



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**401.** A person buys a lottery ticket in 50 lotteries, in each of which his chance of winning a prize is  $\frac{1}{100}$ . What is the probability that he will win a prize at least twice?



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**402.** Find the probability of getting 5 exactly twice in 7 throws of a die.



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**403.** Find the probability of throwing at most 2 sixes in 6 throws of a single die.



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**404.** It is known that 10% of certain articles manufactured are defective. What is the probability that in a random sample of 12 such articles, 9 are defective?



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**405.** In a box containing 100 bulbs, 10 are defective. The probability that out of a sample of 5 bulbs none is defective is :

A.  $10^{-1}$

B.  $\left(\frac{1}{2}\right)^5$

C.  $\left(\frac{9}{10}\right)^5$

D.  $\frac{9}{10}$

**Answer:**



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**406.** The probability that a student is not a swimmer is  $\frac{1}{5}$ . Then the probability that out of five students, four are swimmers is:

A.  ${}^5C_4 \left(\frac{4}{5}\right)^4 \frac{1}{5}$

B.  $\left(\frac{4}{5}\right)^4 \frac{1}{5}$

C.  ${}^5C_1 \frac{1}{5} \left(\frac{4}{5}\right)^4$

D. none of these

**Answer:**



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**407.** A and B are two events such that  $P(A) \neq 0$ . Find  $P(B | A)$ , if : A is a subset of B



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**408.** A and B are two events such that  $P(A) \neq 0$ . Find  $P(B | A)$ , if  $A \cap B = \phi$



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**409.** A family has two children. What is the probability that both the children are boys given that at least one of them is a boy?



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**410.** A couple has two children, find the probability that both children are females, if it is known that the elder child is a female.



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**411.** Suppose that 5% of men and 0.25% of women have grey hair. A grey haired person is selected at random. What is the probability of this person being male? Assume that there are equal number of males and females.



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**412.** Suppose that 90% of people are right-handed. What is the probability that at most 6 of a random sample of 10 people are right-handed?



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**413.** An urn contains 25 balls of which 10 balls bear a mark 'X' and the remaining 15 bear a mark 'Y'. A ball is drawn at random from the urn, its mark is noted down and it is replaced. If 6

balls are drawn in this way, find the probability that all will bear 'X' mark.



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**414.** An urn contains 25 balls of which 10 balls bear a mark 'X' and the remaining 15 bear a mark 'Y'. A ball is drawn at random from the urn, its mark is noted down and it is replaced. If 6 balls are drawn in this way, find the probability that not more than 2 will bear 'Y' mark.



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**415.** An urn contains 25 balls of which 10 balls bear a mark 'X' and the remaining 15 bear a mark 'Y'. A ball is drawn at random from the urn, its mark is noted down and it is replaced. If 6 balls are drawn in this way, find the probability that at least one ball will bear 'Y' mark.



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**416.** An urn contains 25 balls of which 10 balls bear a mark 'X' and the remaining 15 bear a mark 'Y'. A ball is drawn at random from the urn,

its mark is noted down and it is replaced. If 6 balls are drawn in this way, find the probability that the number of balls with 'X' mark and 'Y' mark will be equal.



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**417.** In a hurdle race, a player has to cross 10 hurdles. The probability that he will clear each hurdle is  $\frac{5}{6}$ . What is the probability that he will knock down fewer than 2 hurdles?



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**418.** A die is thrown again and again until three sixes are obtained. Find the probability of obtaining the third six in the sixth throw of the die.



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**419.** If a leap year is selected at random, what is the chance that it will contain 53 tuesdays?



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**420.** Two dice are thrown simultaneously. Find the probability of getting six as a product.



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**421.** How many times must a man toss a fair coin so that the probability of getting at least one head is more than 90%?



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**422.** In a game, a man wins a rupee for a six and loses a rupee for any other number when a fair die is thrown. The man decided to throw a die thrice but to quit as and when he gets a six. Find the expected value of the amount he wins / loses.



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**423.** Suppose we have four boxes A,B,C and D containing coloured marbles as given below:

Box	Marble colour		
	Red	White	Black
A	1	6	3
B	6	2	2
C	8	1	1
D	0	6	4

One of

the boxes has been selected at random and a single marble is drawn from it. If the marble is red, what is the probability that it was drawn from box A?



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**424.** Suppose we have four boxes A,B,C and D containing coloured marbles as given below:

Box	Marble colour		
	Red	White	Black
A	1	6	3
B	6	2	2
C	8	1	1
D	0	6	4

One of

the boxes has been selected at random and a single marble is drawn from it. If the marble is red, what is the probability that it was drawn from box B?



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425. Suppose we have four boxes A,B,C and D containing coloured marbles as given below:

Box	Marble colour		
	Red	White	Black
A	1	6	3
B	6	2	2
C	8	1	1
D	0	6	4

One of

the boxes has been selected at random and a single marble is drawn from it. If the marble is red, what is the probability that it was drawn from box C?



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**426.** Assume that the chances of a patient having a heart attack is 40%. It is also assumed that a meditation and yoga course reduce the risk of heart attack by 30% and prescription of certain drug reduces its chances by 25%. At a time a patient can choose any one of the two options with equal probabilities. It is given that after going through one of the two options the patient selected at random suffers a heart attack. Find the probability that the patient followed a course of meditation and yoga?



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**427.** If each element of a second order determinant is either zero or one, what is the probability that the value of the determinant is positive? (Assume that the individual entries of the determinant are chosen independently, each value being assumed with probability  $\frac{1}{2}$ )



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**428.** An electronic assembly consists of two subsystems, say, A and B. From previous testing

procedures, the following probabilities are assumed to be known :  $P(A \text{ fails } ) = 0.2$ ,  $P(B \text{ fails alone } ) = 0.15$ ,  $P(A \text{ and } B \text{ fail } ) = 0.15$

Evaluate the following probabilities:  $P(A \text{ fails } | B \text{ has failed } )$



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**429.** An electronic assembly consists of two subsystems, say, A and B. From previous testing procedures, the following probabilities are assumed to be known :  $P(A \text{ fails } ) = 0.2$ ,  $P(B \text{ fails alone } ) = 0.15$ ,  $P(A \text{ and } B \text{ fail } ) = 0.15$

Evaluate the following probabilities:  $P(A \text{ fails} \mid B \text{ has failed})$



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**430.** Bag I contains 3 red and 4 black balls and Bag II contains 4 red and 5 black balls. One ball is transferred from Bag I to Bag II and then a ball is drawn from Bag II. The ball so drawn is found to be red in colour. Find the probability that the transferred ball is black



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**431.** If  $A$  and  $B$  are two events such that

$$P(A) \neq 0 \text{ and } P\left(\frac{B}{A}\right) = 1, \text{ then}$$

A.  $A \subset B$

B.  $B \subset A$

C.  $B = \phi$

D.  $A = \phi$

**Answer:**



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432. If  $P\left(\frac{A}{B}\right) > P(A)$ , then which of the following is correct ::

A.  $P\left(\frac{B}{A}\right) < P(B)$

B.  $P(A \cap B) < P(A) \cdot P(B)$

C.  $P\left(\frac{B}{A}\right) > P(B)$

D.  $P\left(\frac{B}{A}\right) = P(B)$

**Answer:**



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**433.** If A and B are any two events such that :

$P(A) + P(B) - P(A \text{ and } B) = P(A)$ , then

A.  $P\left(\frac{B}{A}\right) = 1$

B.  $P\left(\frac{A}{B}\right) = 1$

C.  $P\left(\frac{B}{A}\right) = 0$

D.  $P\left(\frac{A}{B}\right) = 0$

**Answer:**



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**434.** A committee of 4 students is selected at random from a group consisting 8 boys and 4 girls. Given that there is at least one girl in the committee, calculate the probability that there are exactly 2 girls in the committee.



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**435.** A bag contains 5 red marbles and 3 black marbles. Three marbles are drawn one by one without replacement. What is the probability

that at least one of three marbles drawn be black if the first marble is red?



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**436.** A and B throw a pair of dice alternately. A wins the game if he gets a total of 6 and B wins if he gets a total of 7. If A starts the game, find the probability of winning the game by A in third row of pair of dice.



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**437.** Four balls are to be drawn without replacement from a box containing 8 red and 4 white balls. If  $X$  denotes the number of red balls drawn, find the probability distribution of  $X$ .



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**438.** Find the probability that in 10 throws of a fair die a score, which is a multiple of 3, will be obtained in at least 8 of the throws.



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**439.** If A and B are two events such that  $P(A) \neq 0$  and  $P\left(\frac{B}{A}\right) = 1$ , then



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**440.** A and B are two events such that  $P(A) \neq 0$ . Find  $P(B | A)$ , if  $A \cap B = \phi$



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**441.** Coloured balls are distributed in four boxes as shown in the following table:

in the following table :

Box	Colour			
	Black	White	Red	Blue
I	3	4	5	6
II	2	2	2	2
III	1	2	3	1
IV	4	3	1	5

A box is

selected at random and then a ball is randomly drawn from the selected box. The colour of the ball is black, what is the probability that ball is drawn from the box III?



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442. Suppose we have four boxes A,B,C and D containing coloured marbles as given below:

Box	Marble colour		
	Red	White	Black
A	1	6	3
B	6	2	2
C	8	1	1
D	0	6	4

One of

the boxes has been selected at random and a single marble is drawn from it. If the marble is red, what is the probability that it was drawn from box A?



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443. Suppose we have four boxes A,B,C and D containing coloured marbles as given below:

Box	Marble colour		
	Red	White	Black
A	1	6	3
B	6	2	2
C	8	1	1
D	0	6	4

One of

the boxes has been selected at random and a single marble is drawn from it. If the marble is red, what is the probability that it was drawn from box B?



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444. Suppose we have four boxes A,B,C and D containing coloured marbles as given below:

Box	Marble colour		
	Red	White	Black
A	1	6	3
B	6	2	2
C	8	1	1
D	0	6	4

One of

the boxes has been selected at random and a single marble is drawn from it. If the marble is red, what is the probability that it was drawn from box C?



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**445.** Bag I contains 3 red and 4 black balls and Bag II contains 4 red and 5 black balls. One ball is transferred from Bag I to Bag II and then a ball is drawn from Bag II. The ball so drawn is found to be red in colour. Find the probability that the transferred ball is black



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**446.** Suppose that 5% of men and 0.25% of women have grey hair. A grey haired person is selected at random. What is the probability of

this person being male? Assume that there are equal number of males and females.



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**447.** Assume that the chances of a patient having a heart attack is 40%. It is also assumed that a meditation and yoga course reduce the risk of heart attack by 30% and prescription of certain drug reduces its chances by 25%. At a time a patient can choose any one of the two options with equal probabilities. It is given that after going through one of the two options the

patient selected at random suffers a heart attack. Find the probability that the patient followed a course of meditation and yoga?



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**448.** If each element of a second order determinant is either zero or one, what is the probability that the value of the determinant is positive? (Assume that the individual entries of the determinant are chosen independently, each value being assumed with probability  $\frac{1}{2}$ )



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**449.** An electronic assembly consists of two subsystems, say, A and B. From previous testing procedures, the following probabilities are assumed to be known :  $P(A \text{ fails}) = 0.2$ ,  $P(B \text{ fails alone}) = 0.15$ ,  $P(A \text{ and B fail}) = 0.15$   
Evaluate the following probabilities:  $P(A \text{ fails} \mid B \text{ has failed})$



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**450.** An electronic assembly consists of two subsystems, say, A and B. From previous testing procedures, the following probabilities are assumed to be known :  $P(A \text{ fails}) = 0.2$ ,  $P(B \text{ fails alone}) = 0.15$ ,  $P(A \text{ and B fail}) = 0.15$  Evaluate the following probabilities:  $P(A \text{ fails alone})$



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**451.** A box contains 16 bulbs out of which 4 bulbs are defective. 3 bulbs are drawn one by

one from the box without replacement. Find the probability distribution of the number of defective bulbs.



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**452.** From a lot of 30 bulbs which include 6 defectives, a sample of 4 bulbs is drawn at random with replacement. Find the probability distribution of the number of defective bulbs.



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**453.** In a game, a man wins a rupee for a six and loses a rupee for any other number when a fair die is thrown. The man decided to throw a die thrice but to quit as and when he gets a six. Find the expected value of the amount he wins / loses.



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**454.** A die is thrown 7 times. If getting an "even number" is "success", find the probability of getting at least 6 successes.





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**455.** A die is thrown 8 times. If getting an even number is considered a success, find the probability of at least 7 successes.



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**456.** A die is thrown 3 times. If getting a multiple of 3 is considered a success, find the probability of at least 2 successes.



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**457.** If on an average, out of 10 ships, one is drowned, then what is the probability that out of 5 ships, atleast 4 each safely?



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**458.** Suppose that a radio tube insrted into a certain type of set has a probability0.2 of functioning more than 500 hours. If we test 4 tubes, what is the probability that exactly three of these function for more than 500 hours,`.



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**459.** A die is thrown again and again until three sixes are obtained. Find the probability of obtaining the third six in the sixth throw of the die.



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**460.** An experiment succeeds twice as often as it fails. Find the probability that in the next six trials, there will be at least 4 successes.



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**461.** How many times must a man toss a fair coin so that the probability of getting at least one head is more than 90%?



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**462.** Fit a binomial distribution to the following data:

X :	0	1	2	3	4
f :	28	62	46	10	4



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**463.** A man takes a step forward with probability 0.4 and backward with probability 0.6. Then, find the probability that at the end of eleven steps he is one step away from the starting point



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**464.** Out of  $(2n+1)$  tickets consecutively numbered, three are drawn at random. Find the

chance that the numbers on them are in AP.



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**465.** If  $A$  and  $B$  are mutually exclusive, then  $P(A \cap B)$  is equal to \_\_\_\_\_.



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**466.** Let  $E$  and  $F$  be events with  $P(E) = \frac{3}{5}$ ,  $P(F) = \frac{3}{10}$  and  $P(E \cap F) = \frac{1}{5}$ .

Are  $E$  and  $F$  independent?





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**467.** If A and B are two independent events such

that  $P(A) = \frac{5}{13}$ ,  $P(B) = \frac{2}{13}$ , then

$P(A \cap B)$  is equal to \_\_\_\_\_.



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**468.** A pair of dice is tossed once and X denotes

the sum of numbers that appears on the two

dice, then  $P(X \leq 4) = \_ \_ \_$ .



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**469.** A die is tossed thrice. Find the probability of getting an odd number at least once.



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**470.** Write the formula of Bayes' Theorem with its conditions.



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**471.** The mean of the number of heads in the two tosses of a coin is \_\_\_\_\_.



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**472.** Obtain binomial distribution, if :

$n = 6, p = \frac{1}{3}$ . Find the mean



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**473.** Suppose  $X$  has a probability distribution  $B\left(6, \frac{1}{2}\right)$ . find which value of  $X$  is most likely outcome.



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**474.** If the mean and variance of a binomial distribution are 9 and 6 respectively, find the number of trials.



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475. If  $P(A) = \frac{1}{2}$ ,  $P(B) = 0$ ,  $P(A//B)$  is :

A. 0

B.  $\frac{1}{2}$

C. not defined

D. 1

**Answer:**



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476. If  $A$  and  $B$  are events such that

$$P\left(\frac{A}{B}\right) = P\left(\frac{B}{A}\right), \text{ then}$$

A.  $A \subset B$  but  $A \neq B$

B.  $A = B$

C.  $A \cap B = \phi$

D.  $P(A) = P(B)$

**Answer:**



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477. The probability of obtaining an even prime number on each die, when a pair of dice is rolled is:

A. 0

B.  $\frac{1}{3}$

C.  $\frac{1}{12}$

D.  $\frac{1}{36}$

**Answer:**



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**478.** Two events A and B will be independent, if:

A. A and B are mutually exclusive

B.  $P(A'B') = [1 - P(A)][1 - P(B)]$

C.  $P(A) = P(B)$

D.  $P(A) + P(B) = 1$

**Answer:**



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**479.** Probability that A speaks truth is  $\frac{4}{5}$ . A coin is tossed. A reports that a head appears. The probability that actually there was head is

A.  $\frac{4}{5}$

B.  $\frac{1}{2}$

C.  $\frac{1}{5}$

D.  $\frac{2}{5}$

**Answer:**



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**480.** If  $A$  and  $B$  are two events such that  $A \subset B$  and  $P(B) \neq 0$ , then which of the following is correct?

A.  $P\left(\frac{A}{B}\right) = \frac{P(B)}{P(A)}$

B.  $P\left(\frac{A}{B}\right) < P(A)$

C.  $P\left(\frac{A}{B}\right) \geq P(A)$

D. none of these

**Answer:**



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**481.** If  $A$  and  $B$  are two events such that

$$P(A) \neq 0 \text{ and } P\left(\frac{B}{A}\right) = 1, \text{ then}$$

A.  $A \subset B$

B.  $B \subset A$

C.  $B = \phi$

D.  $A = \phi$

**Answer:**



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482. If  $P\left(\frac{A}{B}\right) > P(A)$ , then which of the following is correct ::

A.  $P\left(\frac{B}{A}\right) < P(B)$

B.  $P(A \cap B) < P(A) \cdot P(B)$

C.  $P\left(\frac{B}{A}\right) > P(B)$

D.  $P\left(\frac{B}{A}\right) = P(B)$

**Answer:**



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**483.** If A and B are any two events such that :

$P(A) + P(B) - P(A \text{ and } B) = P(A)$ , then

A.  $P\left(\frac{B}{A}\right) = 1$

B.  $P\left(\frac{A}{B}\right) = 1$

C.  $P\left(\frac{B}{A}\right) = 0$

D.  $P\left(\frac{A}{B}\right) = 0$

**Answer:**



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**484.** The mean of the numbers obtained on throwing a die having written 1 on three faces, 2 on two faces and 5 on one face is:

A. 1

B. 2

C. 5

D.  $\frac{8}{3}$

**Answer:**



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**485.** Suppose that two cards are drawn at random from a deck of cards. Let  $X$  be the number of aces obtained. Then the value of  $E(X)$  is:

A.  $\frac{37}{221}$

B.  $\frac{5}{13}$

C.  $\frac{1}{13}$

D.  $\frac{2}{13}$

**Answer:**



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**486.** In a box containing 100 bulbs, 10 are defective. The probability that out of a sample of 5 bulbs none is defective is :

A.  $10^{-1}$

B.  $\left(\frac{1}{2}\right)^5$

C.  $\left(\frac{9}{10}\right)^5$

D.  $\frac{9}{10}$

**Answer:**



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**487.** The probability that a student is not a swimmer is  $\frac{1}{5}$ . Then the probability that out of five students, four are swimmers is:

A.  ${}^5C_4 \left(\frac{4}{5}\right)^4 \frac{1}{5}$

B.  $\left(\frac{4}{5}\right)^4 \frac{1}{5}$

C.  ${}^5C_1 \frac{1}{5} \left(\frac{4}{5}\right)^4$

D. none of these

**Answer:**



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**488.** A die is thrown once, then the probability of getting a number greater than 3 is :

A.  $\frac{1}{2}$

B.  $\frac{2}{3}$

C. 6

D. 0

**Answer:**



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489.

If

$$P(A) = 0.2, P(B) = 0.4, P(A \cup B) = 0.6 \quad ,$$

then  $P(A/B)$  is equal to

A. 0.8

B. 0.5

C. 0.3

D. 0

**Answer:**



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490. Let  $A$  and  $B$  be two events. If

$$P(A) = 0.6, P(B) = 0.2, P\left(\frac{A}{B}\right) = 0.5, \text{ then}$$

$P(A \cap B)$  is equal to :

A.  $\frac{1}{10}$

B.  $\frac{3}{10}$

C.  $\frac{3}{8}$

D.  $\frac{6}{7}$

**Answer:**



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**491.** If  $A$  and  $B$  are independent events such that  $0 < P(A) < 1$  and  $0 < P(B) < 1$  then which of the following is not correct ?

- A.  $A$  and  $B$  are mutually exclusive
- B.  $A$  and  $B'$  are independent
- C.  $A'$  and  $B$  are independent
- D.  $A'$  and  $B'$  are independent

**Answer:**



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492. Let 'X' be a discrete random variable. The probability distribution of X is given below:

X :	30	10	-10
P(X) :	$\frac{1}{5}$	$\frac{3}{10}$	$\frac{1}{2}$

Then

E(X) is equal to :

- A. 6
- B. 4
- C. 3
- D. -5

**Answer:**



**493.** Let 'X' be a discrete random variable assuming values  $x_1, x_2, \dots, x_n$  with probabilities  $p_1, p_2, \dots, p_n$  respectively.

Then variance of 'X' is given by :

A.  $E(X^2)$

B.  $E(X^2) + E(X)$

C.  $E(X)^2 - [E(X)]^2$

D.  $\sqrt{E(X^2) - [E(X)]^2}$

**Answer:**



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**494.** Two events A and B will be independent, if:

A. A and B are mutually exclusive

B.  $P(A'B') = [1 - P(A)][1 - P(B)]$

C.  $P(A) = P(B)$

D.  $P(A) + P(B) = 1$

**Answer:**

495. If  $A$  and  $B$  are two events such that

$$A \cap B \neq \phi, P\left(\frac{A}{B}\right) = P\left(\frac{B}{A}\right). \text{ Then.}$$

A.  $A \subset B$  but  $A \neq B$

B.  $A = B$

C.  $A \cap B = \phi$

D.  $P(A) = P(B)$

**Answer:**

496.

If

$$P(E) = \frac{11}{36}, P(F) = \frac{5}{36} \text{ and } P(E \cap F) = \frac{2}{36}$$

, then the value of  $P\left(\frac{E}{F}\right)$  is :

A.  $\frac{11}{5}$

B.  $\frac{5}{11}$

C.  $\frac{2}{5}$

D.  $\frac{2}{11}$

**Answer:**



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**497.** Two cards are drawn at random and without replacement from a pack of 52 playing cards. Find the probability that both the cards are black.

A.  $\frac{25}{102}$

B.  $\frac{1}{4}$

C.  $\frac{1}{2}$

D. none of these

**Answer:**



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**498.** An urn contains 10 black and 5 white balls. Two balls are drawn from the urn one after the other without replacement. What is the probability that both drawn balls are black?

A.  $\frac{3}{7}$

B.  $\frac{4}{9}$

C.  $\frac{2}{21}$

D. none of these

**Answer:**



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**499.** Probability distribution of X is given below,

X :	1	2	3	4
P(X) :	1/4	K	2K	K

then the

value of K is :

A.  $\frac{1}{4}$

B.  $\frac{3}{16}$

C.  $\frac{1}{8}$

D. none of these

**Answer:**



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**500.** If A and B are any two events such that :

$P(A) + P(B) - P(A \text{ and } B) = P(A)$ , then

A.  $P\left(\frac{B}{A}\right) = 1$

B.  $P\left(\frac{A}{B}\right) = 1$

C.  $P\left(\frac{B}{A}\right) = 0$

$$D. P\left(\frac{A}{B}\right) = 0$$

**Answer:**



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**501.** In a single throw of a pair of die, the probability of getting total of 3 or 4 is:

A.  $\frac{3}{36}$

B.  $\frac{4}{36}$

C.  $\frac{5}{36}$

D. none of these

**Answer:**



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**502.** A and B are two mutually exclusive events of an experiment. If  $P(\text{not } A) = 0.65$ ,  $P(A \cup B) = 0.65$ , and  $P(B) = p$ , find the value of  $p$ .

A. 0.35

B. 0.3

C. 0.65

D. none of these

**Answer:**



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503.  $P\left(\frac{E}{F}\right)$  is equal to :

A.  $\frac{P(E \cup F)}{P(F)}$

B.  $\frac{P(E \cap F)}{P(E)}$

C.  $\frac{P(E \cap F)}{P(F)}$

D.  $P(E) \cdot P(F)$

**Answer:**



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**504.** If  $P(A) = 0.3, P(B) = 0.4,$  find  $P(A \cup B).$  where A and B are independent events.

A. 0.48

B. 0.51



C. 0.52

D. 0.58

**Answer:**



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**505.** A pair of coins is tossed once. Find the probability of showing at least one head is :

A.  $\frac{1}{2}$

B.  $\frac{2}{3}$

C.  $\frac{3}{4}$

D.  $\frac{1}{4}$

**Answer:**



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**506.** A and B are events such that

$$2P(A) = P(B) = \frac{5}{13}, P\left(\frac{A}{B}\right) = \frac{2}{5}, \quad \text{then}$$

$P(A \cup B)$  is equal to :

A.  $\frac{25}{27}$

B.  $\frac{3}{8}$

C.  $\frac{11}{26}$

D.  $\frac{2}{15}$

**Answer:**



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**507.** The probability of obtaining an even prime number on each die, when a pair of dice is rolled is :

A. 0

B.  $\frac{1}{3}$

C.  $\frac{1}{12}$

D.  $\frac{1}{36}$

**Answer:**



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**508.** If  $P(A) = \frac{3}{5}$  and  $P(B) = \frac{1}{5}$ , find

$P(A \cap B)$  if A and B are independent events.

A.  $\frac{3}{25}$

B.  $\frac{1}{3}$

C.  $\frac{25}{3}$

D. none of these

**Answer:**



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**509.**

if

$$P(A) = \frac{7}{13}, P(B) = \frac{9}{13} \text{ and } P(A \cap B) = \frac{4}{13}$$

, evaluate  $P\left(\frac{A}{B}\right)$ .

A.  $\frac{4}{9}$

B.  $\frac{9}{4}$

C.  $\frac{7}{9}$

D.  $\frac{4}{7}$

**Answer:**



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**510.** If  $A$  and  $B$  are events such that

$$P(A) = 0.4, P(B) = 0.5 \text{ and } P\left(\frac{B}{A}\right) = 0.6,$$

then  $P(\overline{A \cap B})$  is :

A. 0.76

B. 0.48

C. 0.32

D. 0.24

**Answer:**



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511. If  $P(A) = \frac{1}{2}$ ,  $P(B) = 0$  then  $P(A | B)$  is

:

A. 0

B.  $\frac{1}{2}$

C. not defined

D. 1

**Answer:**



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**512.** In a box containing 100 bulbs, 10 bulbs are defective. Probability that out of a sample of 5 bulbs, none is defective, is



A.  $10^{-1}$

B.  $\left(\frac{1}{2}\right)^5$

C.  $\left(\frac{9}{10}\right)^5$

D.  $\frac{9}{10}$

**Answer:**



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**513.** In rolling of two fair six faced dice, the probability of getting total 7 is :

A. 0

B.  $\frac{1}{6}$

C.  $\frac{5}{36}$

D. 1

**Answer:**



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**514.** Three dice are rolled once. The chance of getting a score of 5 is :

A.  $\frac{5}{216}$

B.  $\frac{1}{6}$

C.  $\frac{1}{36}$

D.  $\frac{1}{7^2}$

**Answer:**



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**515.** The probability distribution of 'X' is :

X :	0	1	2	3
P(X) :	0-2	k	k	2k

find the

value of k:

A. 0.2

B. 0.3

C. 0.4

D. 0.1

**Answer:**



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**516.** If two dice are thrown simultaneously, then the probability that the sum of the numbers which come up on the dice to be more than 5 is :

A.  $\frac{5}{36}$

B.  $\frac{1}{6}$

C.  $\frac{5}{18}$

D.  $\frac{7}{18}$

**Answer:**



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517. A fair six-faced die is rolled 12 times. The probability that each face turns up twice is equal to :

A.  $\frac{12!}{6!6!6^{12}}$

B.  $\frac{2^{12}}{2^6 6^{12}}$

C.  $\frac{12!}{2^6 6^{12}}$

D.  $\frac{12!}{6^2 6^{12}}$

**Answer:**



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**518.** In a box containing 100 bulbs, 10 bulbs are defective. Probability that out of a sample of 5 bulbs, none is defective, is

A.  $\frac{9}{10}$

B.  $\left(\frac{1}{10}\right)^5$

C.  $\left(\frac{9}{10}\right)^5$

D.  $\left(\frac{1}{2}\right)^5$

**Answer:**



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**519.** It is given that the events A and B are such that

$$P(A) = \frac{1}{4}, P\left(\frac{A}{B}\right) = \frac{1}{2} \text{ and } p\left(\frac{B}{A}\right) = \frac{2}{3}.$$

Then P(B) is:

A.  $\frac{1}{2}$

B.  $\frac{1}{6}$

C.  $\frac{1}{3}$

D.  $\frac{2}{3}$

**Answer:**





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**520.** A die is thrown. Let  $A$  be the event that the number obtained is greater than 3. Let  $B$  be the event that the number obtained is less than 5.

Then  $P(A \cup B)$  is

A.  $\frac{2}{5}$

B.  $\frac{3}{5}$

C. 0

D. 1

**Answer:**



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**521.** One ticket is selected at random from 50 tickets numbered 00, 01, 02, ... , 49. Then the probability that the sum of the digits on the selected ticket is 8, given that the product of these digits is zero, equals

A.  $\frac{1}{7}$

B.  $\frac{5}{14}$

C.  $\frac{1}{50}$

D.  $\frac{1}{14}$

**Answer:**



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**522.** An urn contains nine balls of which three are red, four are blue and two are green. Three balls are drawn at random without replacement from the urn. The probability that the three balls have different colour, is

A.  $\frac{1}{3}$

B.  $\frac{2}{7}$

C.  $\frac{1}{21}$

D.  $\frac{2}{23}$

**Answer:**



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**523.** A signal which can be green or red with probability  $\frac{4}{5}$  and  $\frac{1}{5}$  respectively, is received by station A and then transmitted to station B.

The probability of each station receiving the signal correctly is  $\frac{3}{4}$ . If the signal received at station B is green, then the probability that original signal was green is

A.  $\frac{3}{5}$

B.  $\frac{6}{7}$

C.  $\frac{20}{23}$

D.  $\frac{9}{20}$

**Answer:**



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**524.** If  $C$  and  $D$  are two events such that  $C \subset D$  and  $P(D) \neq 0$ , then the correct statement among the following is :

A.  $P\left(\frac{C}{D}\right) = P(C)$

B.  $P\left(\frac{C}{D}\right) \geq P(C)$

C.  $P\left(\frac{C}{D}\right) < P(C)$

D.  $P\left(\frac{C}{D}\right) = \frac{P(D)}{P(C)}$

**Answer:**



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525. Consider 5 independent Bernoulli's trials each with probability of success  $P$ . If the probability of at least one failure is greater than or equal to  $\frac{31}{32}$ , then  $P$  lies in the interval.

A.  $\left(\frac{1}{2}, \frac{3}{4}\right]$

B.  $\left(\frac{3}{4}, \frac{11}{12}\right]$

C.  $\left[0, \frac{1}{2}\right]$

D.  $\left(\frac{11}{12}, 1\right]$

**Answer:**



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526. Let  $A, B, C$  be pairwise independent events with  $P(C) > 0$  and  $P(A \cap B \cap C) = 0$ . Then

$$P\left(\frac{A^c \cap B^c}{C}\right).$$

A.  $P(A) - P(B^c)$

B.  $P(A^c) + P(B^c)$

C.  $P(A^c) - P(B^c)$

D.  $P(A^c) - P(B)$

**Answer:**



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**527.** Three numbers are chosen at random without replacement from  $\{1, 2, 3, \dots, 8\}$ . The probability that their minimum is 3, given that their maximum is 6, is

A.  $\frac{3}{8}$

B.  $\frac{1}{5}$

C.  $\frac{1}{4}$

D.  $\frac{2}{5}$

**Answer:**



**528.** Four fair dice ,  $D_1, D_2, D_3$  and  $D_4$  each having six faces numbered 1,2,3,4,5 and 6 are rolled simultaneously. The probability that  $D_4$  shows a number appearing on one of  $D_1, D_2$  and  $D_3$  is

A.  $\frac{91}{216}$

B.  $\frac{108}{216}$

C.  $\frac{125}{216}$

D.  $\frac{127}{216}$

**Answer:**



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**529.** Four person independently solve a certain problem correctly with probabilities  $\frac{1}{2}$ ,  $\frac{3}{4}$ ,  $\frac{1}{4}$ ,  $\frac{1}{8}$ . Then the probability that he problem is solve correctly by at least one of them is

A.  $\frac{235}{256}$

B.  $\frac{21}{256}$

C.  $\frac{3}{256}$

D.  $\frac{253}{256}$

**Answer:**



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**530.** Let  $A$  and  $B$  be two events such that

$$P(\overline{A \cup B}) = \frac{1}{6}, P(A \cap B) = \frac{1}{4} \text{ and } P\overline{A} = \frac{1}{4}$$

,where  $\overline{A}$  stands for complement of event  $A$ .

then , events  $A$  and  $B$  are

A. equally likely but not independent

B. independent but not equally likely

C. independent and equally likely

D. mutually exclusive and independent

**Answer:**



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**531.** if 12 identical balls are to be placed in 3 identical boxes, then the probability that one of the boxes contains exactly 3 balls , is

A.  $\frac{55}{3} \left(\frac{2}{3}\right)^{11}$

B.  $\frac{55}{3} \left(\frac{2}{3}\right)^{10}$

C.  $220 \left(\frac{1}{3}\right)^{12}$

D.  $22 \left(\frac{11}{3}\right)^{11}$

**Answer:**



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**532.** Let two fair six-faced dice A and B be thrown simultaneously. If  $E_1$  is the event that die A shows up four,  $E_2$  is the event that die B

shows up two and  $E_3$  is the event that the sum of numbers on both dice is odd, then which of the following statement is NOT True ?

- A.  $E_1$  and  $E_2$  are not independent
- B.  $E_1$  and  $E_3$  are independent
- C.  $E_1, E_2$  and  $E_3$  are independent
- D.  $E_1$  and  $E_2$  are independent

**Answer:**



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533.

If

$$P(A) = \frac{7}{13}, P(B) = \frac{9}{13} \text{ and } P(A \cap B) = \frac{4}{13}$$

, evaluate  $P\left(\frac{A}{B}\right)$ .



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534. Let E and F be events with

$$P(E) = \frac{3}{5}, P(F) = \frac{3}{10} \text{ and } P(E \cap F) = \frac{1}{5}.$$

Are E and F independent?



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**535.** An urn contains 10 black and 5 white balls. Two balls are drawn from the urn one after the other without replacement. What is the probability that both drawn balls are black?



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**536.** Probability of solving specific problem independently by A and B are  $\frac{1}{2}$  and  $\frac{1}{3}$  respectively. If both try to solve the problem independently, find the probability that the problem is solved.



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**537.** Probability of solving specific problem independently by A and B are  $\frac{1}{2}$  and  $\frac{1}{3}$  respectively. If both try to solve the problem independently, find the probability that exactly one of them solves the problem.



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**538.** From a lot of 30 bulbs which include 6 defectives, a sample of 4 bulbs is drawn at

random with replacement. Find the probability distribution of the number of defective bulbs.



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**539.** Find the probability distribution of number of doublets in three throws of a pair of dice.



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**540.** Ten eggs are drawn successively with replacement from a lot containing 10%

defective eggs. Find the probability that there is at least one defective egg.



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**541.** Assume that the chances of a patient having a heart attack is 40%. It is also assumed that a meditation and yoga course reduce the risk of heart attack by 30% and prescription of certain drug reduces its chances by 25%. At a time a patient can choose any one of the two options with equal probabilities. It is given that after going through one of the two options the

patient selected at random suffers a heart attack. Find the probability that the patient followed a course of meditation and yoga?



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**542.** The random variable  $X$  has a probability distribution  $P(X)$  of the following form, where  $k$  is some number :  $P(x) = \{(k, , \text{if}, x = 0), (2k, , \text{if}, x = 1), (3k, , \text{if}, x = 2), (0, , , , ) : \}$  Determine the value of  $k$ .



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**543.** The random variable  $X$  has a probability distribution  $P(X)$  of the following form, where  $k$

is some number :  $P(x) = \{(k, \text{ if, } x = 0), (2k, \text{ if, } x = 1), (3k, \text{ if, } x = 2), (0, \text{ , , , } ) : \}$  find

$P(X < 2), P(X \leq 2), P(X \geq 2)$ .



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