



MATHS

BOOKS - ACCURATE PUBLICATION

CONTINUITY

Questions Carrying 4 Marks Examples

1. Discuss the continuity of following at x=0 if

$$f(x) = \left\{ egin{array}{c} rac{\sqrt{1+3x} - \sqrt{1-3x}}{\sin x}, & x
eq 0 \ 3, & x = 0 \end{array}
ight.$$

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2. Discuss the continuity of the function

$$f(x)=\left\{egin{array}{ccc} rac{ert x-2ert}{2-x}, & x
eq 2\ -1, & x=2 \end{array}
ight.$$
at $x=2.$



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4. Examine the continuity of the function f'atx = 4, if $f(x) = \frac{|x-4|}{|x-4|}$

4)),(1):}, ((x ne 4),(x =4))`

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5. Test the continuity of the following functions at indicated points :

$$f(x)=egin{cases}x^2{
m sin}rac{1}{x}, & x
eq 0\ 0, & x=0 \end{cases}$$
 at $x=0$

6. Test the continuity of the following functions at indicated points :

$$f(x)=\left\{egin{array}{cc} (x){
m sin}rac{1}{x}, & x
eq 0\ 0, & x=0 \end{array}
ight.$$
at $x=0$

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7. Show that the following function are continuous at x=0:

$$f(x) = \begin{cases} x \cos\left(\frac{1}{x}\right) & whenx \neq 0\\ 0 & whenx = 0 \end{cases}$$
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8. Determine the constant k, so that the function

$$f(x)= egin{cases} rac{x^2-9}{x-3}, & x
eq 3\ k, & x=3 \end{cases}$$
 is continuous at x=3.

9. Determine the constant k, so that function f (x) is continuous at the

indicated points :
$$f(x) = egin{cases} rac{x^2-3x+2}{x-1} & ext{if} & x
eq 1 \ k & ext{if} & x = 1 \end{cases}$$
 at x=1.



10. (a) Determine the value of k so that the following function f(x) is continous at x=0

$$f(x) = \left\{egin{array}{cc} rac{\sin 2x}{x} &, ext{if} \quad x
eq 0 \ k &, ext{if} \quad x = 0 \end{array}
ight.$$

(b) Determine k, if the following function is continuous at x=0:

$$f(x)=\left\{egin{array}{ccc} rac{\sin3x}{4x}&,&x
eq0\ k&,&x=0 \end{array}
ight.$$

(c) Determine k so that the following function f(x) is continuous at x=0

$$f(x)=\left\{egin{array}{ccc} rac{\sin5x}{3x}&,&x
eq 0\ k&,&x=0 \end{array}
ight.$$

11. Determine the value of constant A so that the function

$$f(x)=egin{cases} rac{1-\cos x}{x^2} &, x
eq 0\ A &, x=0 \end{cases}$$
 is continuous at x=0

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12. (i) Given
$$f(x)=egin{cases}rac{1-\cos 4x}{x^2} \ , \ x
eq 0\ k \ , \ x=0 \end{cases}$$

If f(x) is continuous at x=0, find the value of k.

(ii) Given
$$f(x)=\left\{egin{array}{cc} rac{1-\cos4x}{8x^2} &, & x
eq 0\ k &, & x=0 \end{array}
ight.$$

If f(x) is continuous at x=0, find the value of k.

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13. If
$$f(x)$$
 is continuous at $x=0$, find a, where $f(x)=egin{cases} rac{1-\cos ax}{x\sin x}, & x
eq 0\ rac{1}{2}, & x=0 \end{cases}$

14. Find the value of A ' if the function 'f' at y = 0 is continuous when

$$f(x) = egin{cases} rac{1-\cos y}{y\sin y} & y
eq 0 \ igg(rac{1}{2}ig)A & y = 0 \end{cases}$$

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15. If
$$f(x)$$
 is continuous at $x = 0$, find a, where $f(x) = \begin{cases} rac{1-\cos ax}{x\sin x}, & x
eq 0 \\ rac{1}{2}, & x = 0 \end{cases}$

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16. For what value of 'k' the function 'f ' defined by
$$f(x) = \begin{cases} kx^2 & x \leq 4\\ 3 & x > 4 \end{cases}$$
 is continuous at x = 4.

17. Examine the continuity of the function $f(x) = egin{cases} x+1 & x\leq 2 \\ 2x-1 & x>2 \end{bmatrix}$ at x

= 2



18. Examine the continuity of the following function at x = 2:

$$f(x)=egin{cases} 2x+1, & x\leq 2\ 3x-1, & x>2 \end{cases}$$

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19. Examine the continuity of the following function at x = 2:

$$f(x)=egin{cases} 3x+1, & x\leq 2\ 4x-1, & x>2 \end{cases}$$

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Questions Carrying 1 Marks Mcq S Type I

1.
$$\lim_{x} \rightarrow 0 \frac{e^{x} - 1}{x}$$
 is equal to :
A. 0
B. 1
C. e

Answer: B

D. 2

2.
$$\lim_{x} \rightarrow 0 \frac{e^{\sin x} - 1}{x}$$
 is equal to :
A. 2
B. 1
C. e
D. 0

Answer: B



3.
$$\lim_{x} \rightarrow 0 \left(\frac{\log(1+x)}{\sin x} \text{ is equal to :} \right)$$

A. 0
B. 1
C. e
D. 2

Answer: B



4. If
$$f(x) = \begin{cases} rac{x^2-25}{x-5} & , \quad x
eq 5 \\ k & , \quad x = 5 \end{cases}$$
 is continuous at x=5, then k is equal

to:

A. 10	
B. 5	
C. 0	
D. 4	

Answer: A

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5. If
$$f(x) = \begin{cases} \frac{x^2-9}{x-3} & x \neq 3\\ m & x = 3 \end{cases}$$
 is continuous at x = 3, then value of m
is :
A. 3
B. 6
C. 2
D. 1

Answer: B

6. If the function f is defined by $f(x)=egin{cases} 3 & x
eq & 0 \\ a+1 & x & = & 0 \end{bmatrix}$ and f is

continuous at x = 0, then value of a is :

А.	I
В.	2
C.	3
D.	4

۸ 1

Answer: B

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7. If the function f is defined by $f(x) = \begin{cases} 5 & x \neq 0 \\ a-1 & x = 0 \end{cases}$ and f is continuous at x = 0, then value of a is :

R	5
υ.	2

C. 6

D. 7

Answer: C

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8. If
$$f(x)=egin{cases} kx-1&,&x\leq5\\ 3x-5&,&x>5 \end{cases}$$
 is continuous at x=5 then value of k

is:

A.
$$\frac{3}{5}$$

B. $\frac{11}{5}$
C. $\frac{8}{5}$
D. $\frac{9}{5}$

Answer: B

9. If
$$f(x) = \begin{cases} kx+2 & , \quad x \leq 5 \\ 3x-4 & , \quad x > 5 \end{cases}$$
 is continuous at x=5 then value of k is:

A.
$$\frac{3}{5}$$

B. $\frac{4}{5}$
C. $\frac{8}{5}$
D. $\frac{9}{5}$

Answer: D



A.
$$\frac{9}{5}$$

B. $\frac{5}{9}$

C.
$$\frac{5}{3}$$

D. $\frac{3}{5}$

Answer: A



11. If
$$f(x) = \begin{cases} mx-1 & x \leq 5 \\ 3x-5 & x > 0 \end{cases}$$
 is continuous, then the value of m

is :

A.
$$\frac{11}{5}$$

B. $\frac{5}{11}$
C. $\frac{5}{3}$
D. $\frac{3}{5}$

Answer: A

12. If $f(x)=egin{cases} kx^2&x<&2\\ 3&x\geq&2 \end{bmatrix}$ is continuous at x = 2, then the value of

'k' is :

A.
$$\frac{2}{3}$$

B. $\frac{4}{3}$
C. $\frac{3}{2}$
D. $\frac{3}{4}$

Answer: D

13. If
$$f(x) = \begin{cases} kx^2 \\ 3 \end{cases}$$
, $\begin{pmatrix} x < 3 \\ x \ge 3 \end{pmatrix}$ and f is continuous at x = 3 then value of k is :

A.
$$\frac{1}{3}$$

B. $\frac{1}{9}$
C. $\frac{3}{7}$

$$\mathsf{D}.\,\frac{7}{3}$$

Answer: A

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14.
$$f(x) = \begin{cases} \frac{\sin x}{x} & x \neq 0\\ k-1 & x = 0 \end{cases}$$
 is continuous at x = 0, then k is :
A. 2
B. 0
C. -1
D. 1, 1

Answer: A

15. If function defined by : $f(x)=egin{cases} rac{\sin 3x}{2x} & x
eq 0 \ k+1 & x=0 \end{bmatrix}$ is continuous

at x = 0, then value of k is :

A. 0 B. $\frac{3}{2}$ C. $\frac{1}{2}$

D. 1

Answer: C

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16. If function defined by : $f(x) = \begin{cases} rac{\sin 3x}{4x} & x
eq 0 \\ k+1 & x = 0 \end{cases}$ is continuous

at x = 0, then value of k is :

A.
$$\frac{1}{2}$$

B. $-\frac{1}{2}$

C.
$$\frac{1}{4}$$

D. $-\frac{1}{4}$

Answer: D



17. If
$$f(x) = \begin{cases} \frac{\sin 5x}{2x} & x \neq 0\\ k & x = 0 \end{cases}$$
 is continuous at x = 0 then value of k
is :
A. $\frac{2}{5}$
B. $\frac{5}{2}$
C. $\frac{3}{2}$

Answer: B

 $\mathsf{D}.\,\frac{2}{3}$

18. The function $f(x)= egin{cases} rac{\sin x}{x}+\cos x & ext{ if } x
eq 0 \\ k & ext{ if } x=0 \end{cases}$ is continuous at x = 0, then then value of 'k' is A. 3 B. 2 C. 1 D. 1.5 Answer: B Watch Video Solution

19. The function f(x) = [x], where [x] denotes the greatest integer function,

is continuous at

A. 4

B. 2

C. 1

D. 1.5

Answer: D

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21. The function given by f(x)=tax x is discontinuous on the set

A.
$$\{n\pi : n \in Z\}$$

B. $\{2n\pi : n \in Z\}$
C. $\left\{(2n+1)\frac{\pi}{2} : n \in Z\right\}$
D. $\left\{\frac{n\pi}{2} : n \in Z\right\}$

Answer: C

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22. The function f(x) = |x| + |x - 1| is

A. continuous at x=0 as well as at x=1

B. continuous at x=1 but not at x=0

C. discontinuous at x=0 as well as at x=1

D. continuous at x=0 but not at x=1

Answer: A



23. The value of 'k' which makes the function defined by : $(\cdot, (\cdot))$

$$f(x) = egin{cases} \sin\left(rac{1}{x}
ight) & ext{if} \ x
eq 0 \ k & ext{if} \ x = 0 \end{cases}$$
 continuous at x =0 is

A. 8

B. 1

C. -1

D. none of these

Answer: D



24. If (x) = 2x and $g(x) = rac{x^2}{2} + 1$, then which of the following can be

a discontinuous function

A. f(x) + g(x)B. f(x) - g(x)C. f(x). g(x)D. $\frac{g(x)}{f(x)}$.

Answer: D

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25. The function
$$f(x)=rac{4-x^2}{4x-x^3}$$
 is

A. discontinuous at only one point

B. discontinuous at exactly two points

C. discontinuous at exactly three points

D. none of these

Answer: C



26. The function $f(x) = \cot x$ is discontinuous on the set

Ì

A.
$$\{x=n\pi:n\in Z\}$$

B. $\{x=2n\pi:n\in Z\}$
C. $\{x=(2n+1))rac{\pi}{2}, n\in Z$
D. $\left\{x=rac{n\pi}{2}, n\in Z
ight\}$

Answer: A

27. If $f(x) = x^2 \sin \frac{1}{x}$, where $x \neq 0$ then the value of the function f at x=0, so that the function is continuous at x=0, is

A. 0

 $\mathsf{B.}-1$

C. 1

D. none of these

Answer: A

28. If
$$f(x) = \begin{cases} mx+1 & ext{, if } x \leq rac{\pi}{2} \\ \sin x + n & ext{, if } x > rac{\pi}{2} \end{cases}$$
, is continuous at x= $rac{\pi}{2}$, then

A.
$$m = 1, n = 0$$

B.
$$m=rac{n\pi}{2}+1$$
C. $n=rac{m\pi}{2}$

D.
$$m=n=rac{\pi}{2}$$

Answer: C



Questions Carrying 1 Marks Fill In The Blanks Questions Type Ii

1. If
$$f(x) = \begin{cases} rac{x^2-9}{x-3} & x
eq & 3 \\ m & x & = & 3 \end{cases}$$
 is continuous at x = 3 , then value of m

is :

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2. If the function f is defined by
$$f(x)= egin{cases} 7 &, x
eq 0 \\ a-1 &, x=0 \end{bmatrix}$$
 and f is continuous at x=0 then value of 'a' is _____

3. If
$$f(x) = \begin{cases} kx+1 & x \leq 5 \\ 3x-5 & x > 5 \end{cases}$$
 s is a continuous function then the value

of k is



4. If
$$f(x) = egin{cases} mx+1 & x &\leq & 5 \ 3x+5 & x &> & 5 \end{cases}$$
 is continuous, then the value of m

is :

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is :

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6. If function defined by :
$$f(x)=egin{cases}rac{\sin 5x}{3x}&x
eq 0\ k+1&x=&0 \end{cases}$$
 is continuous at

x = 0, then value of k is :

7. The number of points at which the function $f(x) = rac{1}{\log \lvert x \rvert}$ is discontinuous is ___

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8. If $f(x) = egin{cases} ax+1 & ext{if} \ x \geq 1 \ x+2 & ext{if} \ x < 1 \end{cases}$ is continuous, then 'a' should be equal

to ____

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Questions Carrying 1 Marks True Or False Questions Type Iii

1. For continuity, at x=a, each of $\lim_{x \to a^+} f(x)$ and $\lim_{x \to a^-} f(x)$ is equal to

f(a).



The function f(x) = |x-1| is a continuous function.

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3. A continuous function can have some points where limit does not exist.

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4. If f is continuous on its domain D, then |f| is also continuous on D.

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5. The composition of two continuous function is a continuous function.

6. If $f \cdot g$ is continuous at x=a, then f and g are separately continuous at

x=a.



10. Determine the constant k, so that the function

$$f(x)= egin{cases} rac{x^2-9}{x-3}, & x
eq 3\ k, & x=3 \end{cases}$$
 is continuous at x=3.

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11. The value of k so that the function $f(x) = \begin{cases} \frac{\sin 2x}{x} & \text{if } x \neq 0 \\ k & \text{if } x = 0 \end{cases}$ is continous at x=0 is: Watch Video Solution

12. Prove that $f(x) = |\sin x|$ is continous at all point of its domnin.

13. If f is continuous and g is a discontinuous function then f+g is continuous function.

Questions Carrying 4 Marks

1. Discuss the continuity of the function (x) at
$$x = 1$$
 if

$$f(x) = \left\{ egin{array}{cc} rac{x-1}{\sqrt{x^2-1}}, & x
eq 1 \ 0, & x = 1 \end{array}
ight.$$

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2. Discuss the continuity of the function :

$$f(x) = \left\{egin{array}{ccc} rac{|x-a|}{x-a} & whenx
eq a \ 1 & whenx = a \end{array}
ight.$$
at x = a

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3. Discuss the continuity of f(x) at x = 0 if:

$$f(x) = \left\{egin{array}{cc} rac{\sqrt{1+x}-\sqrt{1-x}}{\sin x} & whenx
eq 0 \ 0 & whenx = 0 \end{array}
ight.$$

4. Determine the value of constant A so that the function

$$f(x)=\left\{egin{array}{ccc} rac{1-\cos x}{x^2} &, & x
eq 0\ A &, & x=0 \end{array}
ight.$$
 is continuous at x=0

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5. The function
$$f(x)=iggl\{rac{e^{rac{1}{x}}-1}{e^{rac{1}{x}}+1},x
eq 0, atx=0, f(x)=0$$

- a. is continuous at x=0
- b. is not continuous at x=0

c. is not continuous at $x=0,\,$ but can be made continuous at x=0

(d) none of these

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6. Determine k, so that $f(x) = \begin{cases} rac{x^2-36}{x-6}, & ext{if } x
eq 6 \\ k, & ext{if } x = 6 \end{cases}$ is continous at x = 6.

7. (a) Determine the value of k so that the following function f(x) is

continous at x=0

$$f(x) = \left\{egin{array}{cc} rac{\sin 2x}{x} &, ext{if} \quad x
eq 0 \ k &, ext{if} \quad x = 0 \end{array}
ight.$$

(b) Determine k, if the following function is continuous at x=0:

$$f(x)=\left\{egin{array}{ccc} rac{\sin3x}{4x}&,&x
eq 0\ k&,&x=0 \end{array}
ight.$$

(c) Determine k so that the following function f(x) is continuous at x=0

$$f(x)=\left\{egin{array}{ccc} rac{\sin5x}{3x}&,&x
eq0\ k&,&x=0 \end{array}
ight.$$

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8. Find the value of 'k', for which:

$$f(x)=iggl\{rac{\sqrt{1+kx}-\sqrt{1-kx}}{x}, \hspace{1em} ext{if} \hspace{1em} -1\leq x<0iggr), iggl(rac{2x+1}{x-1}, \hspace{1em} ext{if} \hspace{1em} 0\leq$$

is continuous at x=0

9. Find the values of k so that the function f is continuous at the

$$ext{indicated point}: f(x) = egin{cases} k rac{\cos x}{\pi-2x} & ext{if} \quad x
eq rac{\pi}{2} \\ 3 & ext{if} \quad x = rac{\pi}{2} \end{cases}$$
 at $x = rac{\pi}{2}$

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10. For what value of 'a' and 'b', the function 'f' defined as:

$$f(x)= egin{cases} 3ax+b & ext{if} \quad x<1\ 11 & ext{if} \quad x=1 ext{ is continuous at x=1}\ 5ax-2b & ext{if} \quad x>1 \end{cases}$$

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11. For what value of k is the following function continous at x = 2?

$$f(x) = \left\{egin{array}{ccc} 2x+1, & x < 2 \ k, & x = 2 \ 3x-1 & x > 2 \end{array}
ight.$$

12. If the function defined by :

 $f(x)= egin{cases} 2x-1 & x<2\ a & x=2\ x+1 & x>2 \end{cases}$ is continuous at x =2, find the value of 'a'. Also

discuss the continuity of f(x) at x = 3.



13. If
$$f(x) = \begin{cases} rac{x-5}{|x-5|} + a & ext{, if } x < 5 \\ a+b & ext{, if } x = 5 \\ rac{x-5}{|x-5|} + b & ext{, if } x > 5 \end{cases}$$
 is a continuous function, find

'a' and 'b'.

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14. Find the values of a and b such that the function defined by

$$f(x)egin{cases} 5 & ext{if} \quad x\geq 2\ ax+b & ext{if} \quad 2< x < 10 ext{ is continuous.}\ 21 & ext{if} \quad x\geq 10 \end{cases}$$

that the function is continuous at x = 0, is.....

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16. For what value of 'k' is the function defined by
$$f(x) = \begin{cases} k(x^2+2) & \text{if } x \leq 0 \\ 3x+1 & \text{if } x > 0 \end{cases}$$
 continuous at x =0? Also write

whether the function is continuous at x = 1.

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17. Find all points of discontinuity of f, where f is defined as follows:

$$f(x) = egin{cases} |x|+3 &, & x \leq -3 \ -2x &, & -3 < x < 3 \ 6x+2 &, & x \geq 2 \end{cases}$$