



# MATHS

# **BOOKS - OMEGA PUBLICATION**

# **APPLICATION OF INTEGRALS**

Questions

**1.** Find the area of the region bounded by  $x^2 = 4y, y = 2, y = 4$  and y-axis the first quadrant.



**3.** Find the area of the region bounded by ellipse  $rac{x^2}{16} + rac{y^2}{9} = 1.$ 

4. Find the area of the region bounded by the

ellipse 
$$\displaystyle rac{x^2}{4} + \displaystyle rac{y^2}{9}$$
 = 1

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5. Find the area of the region bounded by the curve  $y^2 = x$  and the lines x = 1, x = 4 and the x-axis in the first quadrant.

6. Find the area of the region bounded by  $y^2 = 9x, x = 2, x = 4$  and the x-axis in the fill quadrant.





$$y = x^2$$

**8.** Find the area of the region enclosed by the parabola  $x^2 = y$ , the liney = x + 2 and the x-axis.





10. Find the area of the region bounded by the parabola  $y = x^2$  and the lines y = |x|. Watch Video Solution



12. Find the area lying above x-axis and included between the circle  $x^2 + y^2 = 8x$  and the parabola  $y^2 = 4x$ .

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between the two circles

 $x^{2} + y^{2} = 1$  and  $(x - 1)^{2} + y^{2} = 1$ .

**14.** Find the area of the region bounded by the parabola  $y = x^2 + 2$  and the lines y = x, x = 0 and x = 3. Watch Video Solution

**15.** Find the area of the region included between : the parabola  $4y = 3x^2$  and the line 3x - 2y + 12 = 0.

16. Find the area of the region bounded by two

parabolas  $y = x^2$  and  $y^2 = x$ .



17. Find the area of the region bounded by

 $x^2=4y, y=2, y=4$  and y-axis the first

quadrant.

18. Find the area of enclosed by the ellipse

$$rac{x^2}{a^2} + rac{y^2}{b^2} = 1.$$

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19. Find the area of the region bounded by ellipse  $rac{x^2}{16}+rac{y^2}{9}=1.$ 

20. Find the area of the region bounded by the

ellipse 
$$\displaystyle rac{x^2}{4} + \displaystyle rac{y^2}{9}$$
 = 1

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**21.** Find the area of the region bounded by the curve  $y^2 = x$  and the lines x = 1, x = 4 and the x-axis in the first quadrant.

22. Find the area of the region bounded by  $y^2 = 9x, x = 2, x = 4$  and the x-axis in the fill quadrant.





$$y = x^2$$

**24.** Find the area of the region enclosed by the parabola  $x^2 = y$ , the liney = x + 2 and the x-axis.





26. Find the area of the region bounded by the parabola  $y = x^2$  and the lines y = |x|.



28. The area lying above x-axis and included between the circle  $x^2 + y^2 = 8x$  and the parabola  $y^2 = 4x$  is

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between the two circles

 $x^{2} + y^{2} = 1$  and  $(x - 1)^{2} + y^{2} = 1$ .

30. Find the area of the region bounded by the

parabola  $y=x^2+2$  and the lines

y = x, x = 0 and x = 3.

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**31.** Find the area of the region included between : the parabola  $4y = 3x^2$  and the line

3x - 2y + 12 = 0.

**32.** Find the area of the region bounded by two parabolas  $y = x^2$  and  $y^2 = x$ .



**1.** Using integration find the area of region bounded by the triangle whose vertices are (1, 0), (2, 2) and (3, 1).

**2.** Using integration, find the area of the triangle ABC, co ordinate of whose vertics are A(2,0),B(4,5) and C(6,3).



**3.** Using integration find the area of regeion bounded by the triangle whose vertices are (-1,0), (1,3) and (3,2)

4. Sketch the graph of y = |x + 3| and evaluate the area under the curve y = |x + 3|above x-axis and between x = -6 and x = 0.



5. Make a rough sketch of the region given below and find its area, using integration :  $\{(x,y): y^2 \le 4x, 4x^2 + 4y^2 \le 9\}$ 

6. Find the area of smaller regioni bounded by







8. Find the area enclosed between the parabola  $y^2 = 4ax$  and the line y = mx

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9. Find the area of smaller region founded by the ellipse  $rac{x^2}{9}+rac{y^2}{4}=1$  and the straight line  $rac{x}{3}+rac{y}{2}=1$ 

10. Find the area bounded by curves  $(x-1)^2 + y^2 = 1$  and  $x^2 + y^2 = 1$ . Watch Video Solution

**11.** Using integration find the area of region bounded by the triangle whose vertices are (1, 0), (2, 2) and (3, 1).



**12.** Using integration, find the area of the triangle ABC, co ordinate of whose vertics are A(2,0),B(4,5) and C(6,3).



**13.** Using integration find the area of the region bounded by triangle whose vertices are

AI(-1, 0), B(1, 3) and C(3, 2).



14. Sketch the graph of y = |x + 3| and evaluate the area under the curve y = |x + 3|above x-axis and between x = -6 and x = 0.

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15. Find the area of the region  $\{(x,y): y^2 \leq 4x, 4x^2 + 4y^2 \leq 9\}.$ 

16. Find the area of smaller regioni bounded by the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  and the line  $\frac{x}{a} + \frac{y}{b} = 1.$ 





**18.** Find the area enclosed between the parabola  $y^2 = 4ax$  and the line y = mx

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19. Find the area of smaller region founded by the ellipse  $\frac{x^2}{9} + \frac{y^2}{4} = 1$  and the straight line  $\frac{x}{3} + \frac{y}{2} = 1$ 

20. Find the area bounded by curves  $(x-1)^2 + y^2 = 1$  and  $x^2 + y^2 = 1$ . Watch Video Solution

# **Multiple Choice Questions**

1. Area lying in the first quadrant and bounded by the circle  $x^2 + y^2 = 4$  and the lines x = 0and x = 2 is :

B. 
$$\frac{\pi}{2}$$
  
C.  $\frac{\pi}{3}$   
D.  $\frac{\pi}{4}$ 

## Answer: A

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2. Area of the region bounded by the curve  $y^2=4x, \;$  y-axis and the line y=3 is

B. 
$$\frac{9}{4}$$
  
C.  $\frac{9}{3}$   
D.  $\frac{9}{2}$ 

### Answer: B

**3.** (a) (i)Find the area of the circle 
$$x^2 + y^2 = 16$$
, which is exterior to the parabola  $y^2 = 6x$ .

A. 
$$rac{4}{3} (4\pi - \sqrt{3})$$
  
B.  $rac{4}{3} (4\pi + \sqrt{3})$   
C.  $rac{4}{3} (8\pi - \sqrt{3})$   
D.  $rac{4}{3} (8\pi + \sqrt{3})$ 

#### Answer: C



A. 
$$2(\pi-2)$$

#### $\mathsf{B.}\,\pi-2$

- $\mathsf{C.}\,2\pi-1$
- D.  $2(\pi+2)$

#### Answer: B

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5. Area lying between the curve  $y^2 = 4x$  and the line y = 2x is :

A. 
$$\frac{2}{3}$$
  
B.  $\frac{1}{3}$   
C.  $\frac{1}{4}$   
D.  $\frac{3}{4}$ 

## Answer: B

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**6.** Area bounded by the curve  $y=x^3$ , the x-

axis and the ordinates x = -2, x = 1 is:

B.  $\frac{-15}{4}$ C.  $\frac{15}{4}$ D.  $\frac{17}{4}$ 

 $A_{-} - 9$ 

## Answer: D

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7. The area bounded by the curve y = x |x|,x-axis and the ordinates x = -1, x = 1 is given by:

B.  $\frac{1}{3}$ C.  $\frac{2}{3}$ D.  $\frac{4}{3}$ 

A. 0

## Answer: C

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8. The aera bounded by the Y-axis, $y=\cos x$  and  $y=\sin x, 0\geq x\leq \left(\pi
ight)/2$  is

A. 
$$2ig(\sqrt{2}-1ig)$$

B. 
$$\sqrt{2}-1$$

$$\mathsf{C}.\sqrt{2}+1$$

D. 
$$\sqrt{2}$$

#### Answer: B

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9. Area lying in the first quadrant and bounded by the circle  $x^2 + y^2 = 4$  and the lines x = 0and x = 2 is : A.  $\pi$ 

B. 
$$\frac{\pi}{2}$$
  
C.  $\frac{\pi}{3}$   
D.  $\frac{\pi}{4}$ 



10. Area of the region bounded by the curve

 $y^2=4x,\,$  y-axis and the line y=3 is

A. 2 B.  $\frac{9}{4}$ 

C. 
$$\frac{9}{3}$$
  
D.  $\frac{9}{2}$ 

## Answer: B

11. (a) (i)Find the area of the circle 
$$x^2+y^2=16$$
, which is exterior to the parabola  $y^2=6x$ .

A. 
$$rac{4}{3} (4\pi - \sqrt{3})$$
  
B.  $rac{4}{3} (4\pi + \sqrt{3})$   
C.  $rac{4}{3} (8\pi - \sqrt{3})$   
D.  $rac{4}{3} (8\pi + \sqrt{3})$ 

#### Answer: C

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# 12. Smaller area enclosed by the circle $x^2 + y^2 = 4$ and the line x + y = 2 is:

A. 
$$2(\pi-2)$$

#### B. $\pi-2$

- $\mathsf{C.}\,2\pi-1$
- D.  $2(\pi+2)$

#### **Answer: B**

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13. Area lying between the curve  $y^2=4x$  and

the line y = 2x is :

A. 
$$\frac{2}{3}$$
  
B.  $\frac{1}{3}$   
C.  $\frac{1}{4}$   
D.  $\frac{3}{4}$ 

## Answer: B

# Watch Video Solution

14. Area bounded by the curve  $y=x^3$ , the x-

axis and the ordinates x = -2, x = 1 is:

B.  $\frac{-15}{4}$ C.  $\frac{15}{4}$ D.  $\frac{17}{4}$ 

 $A_{-} - 9$ 

## Answer: D

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15. The area bounded by the curve y = x|x|,x-axis and the ordinates x = -1, x = 1 is given by:

B.  $\frac{1}{3}$ C.  $\frac{2}{3}$ D.  $\frac{4}{3}$ 

A. 0

## Answer: C

# Watch Video Solution

16. The aera bounded by the Y-axis, $y = \cos x$ 

and  $y=\sin x, 0\geq x\leq \left(\pi
ight)/2$  is

A. 
$$2ig(\sqrt{2}-1ig)$$

B. 
$$\sqrt{2}-1$$

$$\mathsf{C}.\sqrt{2}+1$$

D. 
$$\sqrt{2}$$

#### Answer: B

