

MATHS

BOOKS - BETTER CHOICE PUBLICATION

DIFFERENTIAL EQUATIONS

Solved Examples Multiple Choice Questions Section I

1. The degree of the differential equation
$$\left(\frac{d^2y}{dx^2}\right)^3 + \left(\frac{dy}{dx}\right)^2 + \sin\left(\frac{dy}{dx}\right) + 1 = 0$$
 is :

A. 3

B. 2

C. 1

D. Not defined

Answer: D





Answer: A



3. The number of arbitrary constants in the particular solution of a differential equation of Second order is :

A. 2

B. 1

C. 3

D. 0

Answer: D



4. The number of arbitrary constants in the particular solution of a differential equation of Fourth order is :

A. 0

B. 2

C. 3

D. 4

Answer: D

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5. Which of the following differential equations has $y = c_1 e^x + c_2 e^{-x}$ as the general solution?

A.
$$\displaystyle rac{d^2y}{dx^2}+y=0$$

B. $\displaystyle rac{d^2y}{dx^2}-y=0$
C. $\displaystyle rac{d^2y}{dx^2}+1=0$
D. $\displaystyle rac{d^2y}{dx^2}-1=0$

Answer: B



6. The Integrating. factor of the differential equation

$$x\left(rac{dy}{dx}
ight)-3y=e^{-2x}$$
 is :
A. $rac{1}{x}$
B. $rac{1}{x^2}$
C. $rac{1}{x^3}$

D. x^3`

Answer: C



Solved Examples Section Ii Short Answer Type Questions

1. Verify that given function (explicit or implicit), $y=e^x+1$

is a solution of differential equation y - y' = 1.



2. Verify that $y = x \sin x$ is a solution of differential equation

$$xy'=y+x\sqrt{x^2-y^2}$$



3. Form a differential equation representing the given family of curves by eliminating arbitrary constants a and b: $\frac{x}{a} + \frac{y}{b} = 1$



4. Form a differential equation representing the family of curves $y^2 = a(b^2 - x^2)$ by eliminating a and b.

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5. In $y = ae^{3x} + be^{-2x}$ form the differential equation by

eliminating arbitrary constant a and b.



6. In $y = e^x(a\cos x + b\sin x)$ form the differential equation

by eliminating arbitrary constants a and b.

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7. Form the differential equation representing the family of curves given by $(x - a)^2 + 2y^2 = a^2$, where a is an arbitrary constant.

8. Form the differential equation of the family of parabolas

having vertex at origin and axis along positive y-axis.

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9. Form the differential equation of the family of circles touching the y-axis at origin.



10. Form the differential equation of the family of ellipses

having foci on y-axis and centre at origin.

11. Form the differential equation of the family of circles

having centre on y-axis and radius 3 units.



3. Find the general solution of differential equation : $\sec^2 x \tan y dx + \sec^2 y \tan x dy = 0$



4. Find the general solution of the differential equation

$$ig(e^x+e^{-x}ig)dy-ig(e^x-e^{-x}ig)dx=0$$

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5. Find the general solution of differential equation $rac{dy}{dx} = \left(1+x^2
ight)\left(1+y^2
ight)$

6. Find the general solution of differential equation $y \log y dx - x dy = 0.$

7. Find the general solution of the differential equation:

$$\left(rac{dy}{dx}
ight)+\sqrt{rac{1-y^2}{1-x^2}}=0$$

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8. Find the particular solution of $\log \left(rac{dy}{dx}
ight) = 2x + 3y$ given

that x = 0, y = 0.

9. Find the particular solution of the following differential equation : $\frac{dy}{dx} = 1 + x^2 + y^2 + x^2 y^2$, given that y = 1 when x = 0.

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Solved Examples Section Iv

1. Solve the differential equation $(x+y)rac{dy}{dx}=1$

2. Solve the differential equation $\sin^{-1}\left(\frac{dy}{dx}\right) = x + y.$

3. Find the Particular solution of differential equation $log\left(\frac{dy}{dx}\right) = 2x + y$ given that x = 0 , y =0 **Vatch Video Solution**

Solved Examples Section V

1. Solve the differential equation $y' = \frac{x+y}{x}$.





5. Show that the given differential equation is homogeneous

and solve it: $\left\{x\cos\left(\frac{y}{x}\right) + y\sin\left(\frac{y}{x}\right)\right\}ydx = \left\{y\sin\left(\frac{y}{x}\right) - x\cos\left(\frac{y}{x}\right)\right\}xdy$

6. For the differential equation, find the particular solution

satisfying the given condition:(x+y)dy+(x-y)dx=0, y=1 when x=1

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7. Find the particular solution of the differential equation $\frac{dy}{dx} - \frac{y}{x} + \cos ec \left(\frac{y}{x} \right) = 0, (x \neq 0),$ given that y = 0, x = 1.



Solved Examples Section Vi

1. Find the general solution of the differential equation $\frac{dy}{dx} + 3y = e^{-2x}.$

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2. Find the general solution of differential equation $\frac{dy}{dx} + \frac{y}{x} = x^2.$

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3. Solve the differential equation
$$rac{dy}{dx} + (\sec x)y = \tan x (0 \le x < 1)$$

4. Solve the differential equation
$$\cos^2 x \frac{dy}{dx} + y = \tan x \Big(0 \le x < \frac{x}{2} \Big).$$

5. For the differential equation, find the general solution:

$$ig(1+x^2ig) dy+2xydx=\cot xdx(x
eq 0)$$

6.Solvethedifferentialequation
$$x \frac{dy}{dx} + y - x + xy \cot x = 0 (x
equation)$$
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7. Solve the differential equation

$$\left[\frac{e^{-2\sqrt{x}}}{\sqrt{x}} - \frac{y}{\sqrt{x}}\right] \frac{dy}{dx} = 1 (x \neq 0)$$
(Watch Video Solution
8. Solve the differential equation $(x + y)\frac{dy}{dx} = 1$
(Watch Video Solution
9. Solve the differential equation $(x + 3y^2)\frac{dy}{dx} = y, (y > 0)$
.
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10. Find particular solution of differential equation
$$\frac{dy}{dx} + 2y \tan x = \sin x, y = 0$$
, when $x = \frac{\pi}{3}$.

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11. For the differential equation, find a particular solution

satisfying the given condition:
$$ig(1+x^2ig)rac{dy}{dx}+2xy=rac{1}{1+x^2},y=0$$
 when $x=1$

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Assignment Section li

1. Find the differential equation of the family of curves $(x-a)^2 + (y-b)^2 = r^2$, where a and b are arbitrary constants.

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2. Form the differential equation of the family of circles in the

first quadrant which touch the coordinate axes.



3. Obtain the differential equation of the family of circles,

which touch the x-axis at the origin.



4. Form the differential equation of the family of circles touching the y-axis at origin.



1. Solve the following differential equations

$$rac{dy}{dx} = x^2 + \sin 3x$$

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2. Solve the following differential equations

$$rac{dy}{dx} - x^2 \sin^2 x = rac{1}{x \log x}$$



$$ig(1+x^2ig)rac{dy}{dx} - xy = 2 an^{-1}x$$

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4. Solve the following differential equations

$$rac{dy}{dx}=x^5+x^2-rac{2}{x}$$

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5. Find the particular solution of following differential equation

$$ig(x^3+x^2+x+1ig)rac{dy}{dx}=2x^2+x,y=1$$
when $x=0$



6. Find the particular solution of following differential

equation

$$\cos rac{dy}{dx} = 0 (a \in R) y = 1$$
 when $x = 0$



7. Solve the following differential equations

$$rac{dy}{dx}=rac{1+y^2}{1+x^2}$$

 $3e^x an y dx + (1-e^x) \mathrm{sec}^2 y dy = 0$



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10. Solve the following differential equations

$$4e^x an y dx + 3(1+e^x) \mathrm{sec}^2 y dy = 0$$

11. Solve the differential equation :
$$(1+e^{2x})dy+(1+y^2)e^{2x}dx=0$$
 given that $y=1whenx=0$

$$\log \frac{dy}{dx} = ax + by$$

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13. Solve the following differential equations

$$x^2(y-1)dx+y^2(x-1)dy=0$$

$$(e^x+1)dy+(y+1)e^xdx=0$$

15. Solve the following differential equations

$$(1+x)ig(1+y^2ig) dx + (1+y)ig(1+x^2ig) dy = 0$$

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16. Solve the following differential equations

$$rac{dy}{dx} = 1 + x + y + xy$$

17. Solve the following differential equations ;

$$\frac{dy}{dx} - \frac{y}{x} = 2x^2$$

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18. Find the particular solution of following

$$(x+1)rac{dy}{dx}=2e^{-y}-1,y=0$$
 when $x=0$

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19. Find the particular solution of following

$$rac{dy}{dx} = y \sin 2x$$
, given that $y(0) = 1$

20. Find the particular solution of following

$$ig(1+y^2ig)(1+\log x)dx+xdy=0$$
 when $x=1,y=1$



Assignment Section Iv

1. Solve the following differential equations

$$(x-y)^2rac{dy}{dx}=a^2$$

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2. Solve the following differential equations

$$rac{dy}{dx}=\left(4x+y+1
ight)^{2}$$



$$\sin(x+y)rac{dy}{dx}=1$$

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4. Solve the following differential equations

$$\cos(x+y)rac{dy}{dx}=1$$

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5. Solve the following differential equations

$$rac{dy}{dx}+1=e^{x+y}$$

Assignment Section V

1. Solve the following differential equations

$$x^2rac{dy}{dx} = y(x+y)$$

2. Solve the following differential equations

$$rac{dy}{dx} = rac{y-x}{x+y}$$

$$rac{dy}{dx} + 4y = 5x$$

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4. Solve the following differential equations

$$y^2x^2rac{dy}{dx}=xyrac{dy}{dx}$$



5. Solve the following differential equations

$$2xyrac{dy}{dx}=x^2+y^2$$

$$x^2rac{dy}{dx}=2xy+y^2$$



7. Solve the following differential equations

$$ig(y^2-x^2ig)dy=3xydx$$

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8. Solve the following differential equations

$$xdy-ydx=\sqrt{x^2+y^2}dx$$

$$ig(x^3+y^3ig) dy = x^2 y dx$$

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10. Solve the following differential equations

$$xrac{dy}{dx}-y+x anrac{y}{x}=0$$

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11. Solve the following differential equations

$$\Big(x\sinrac{y}{x}\Big)dy=\Big(y\sinrac{y}{x}-x\Big)dx$$

$$xy\log\Bigl(rac{y}{x}\Bigr)dx + \Bigl\{y^2-x^2\log\Bigl(rac{y}{x}\Bigr)\Bigr\}dy = 0$$

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13. For the differential equation, find the particular solution

satisfying the given condition: $x^2 dy + ig(xy + y^2ig) dx = 0, y = 1$ when x = 1

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14. Find the particular solution of the following differential equations, satisfying the given condition

$$ig(x^2+y^2ig) dx=2xydy, y=0$$
 when $x=1$.

15. Find the particular solution of the following differential equations, satisfying the given condition

$$ig(x^2-y^2ig)dx+2xydy=0,y=1$$
 when $x=1$

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16. For the differential equation, find the particular solution

satisfying the given condition: $2xy+y^2-2x^2rac{dy}{dx}=0, y=2$ when x=1

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17. Find the particular solution of the following differential equations, satisfying the given condition

$$2x^2y_1 - 2xy + y^2 = 0, y(e) = e$$

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Assignment Section Vi

1. Solve the following differential equations

 $rac{dy}{dx} - rac{y}{x} = 2x^2$

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2. Solve the following differential equations

$$2xrac{dy}{dx}+y=6x^3$$

$$\frac{dy}{dx} + 4y = 5x$$

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4. Solve the following differential equations

$$rac{dy}{dx} + y = \cos x$$



5. Solve the following differential equations

$$rac{dy}{dx} + y = \sin x$$

 $rac{dy}{dx} - y = \cos x$



7. Solve the following differential equations

$$rac{dy}{dx} + 2y = \sin 3x$$

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8. Solve the following differential equations

$$rac{dy}{dx} + 2y = \sin 5x$$



$$rac{dy}{dx}-rac{2x}{1+x^2}y=x^2+2$$

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10. Solve the following differential equations

$$ig(x^2-1ig)rac{dy}{dx}+2xy=rac{2}{x^2-1}$$

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11. Solve the following differential equations

$$ig(1+x^2ig)rac{dy}{dx}+y=e$$

 $rac{dy}{dx}+y=\cos x-\sin x$

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13. Solve the following differential equations

$$xdy-ig(y+2x^2ig)dx=0$$

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14. Solve the following differential equations

$$ig(y+3x^2ig)rac{dx}{dy}=x$$

$$xdy+ig(y-x^3ig)dx=0$$

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16. Solve the following differential equations

$$rac{dy}{dx} + rac{4x}{x^2+1}y = rac{1}{\left(x^2+1
ight)^3}$$

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17. Solve the following differential equations

$$rac{dy}{dx} + y \cot x = \ - x^2 \cot x + 2x$$

$$\cos x rac{dy}{dx} = y \sin x$$

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19. Solve the following differential equations

$$ig(x+2y^3ig)rac{dy}{dx}=y$$

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20. Solve the following differential equations

$$ydx+ig(x-y^2ig)dy=0$$

$$ig(an^{-1}y-xig)dy=ig(1+y^2ig)dx$$

22. Solve the following differential equations

$$rac{dy}{dx} = x^2 y + y$$

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23. Find the particular solution of following differential

equations

$$xrac{dy}{dx}+2y=x^2, (x
eq 0)$$
 : $y=1$ when $x=2$

24. Find the particular solution of following differential equations

$$xy^1-y=\log x, y(1)=0$$

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25. Find the particular solution of the differential equation

 $rac{dx}{dy}+y\cot x=2x+x^2\cot x(x
eq 0)$ given that y = 0 when $x=rac{\pi}{2}$

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26. Find the particular solution of following differential equations

$$rac{dy}{dx} + y\cot x = 4x, y\Big(rac{\pi}{2}\Big) = 0$$



27. Find the particular solution of following differential

$$rac{dy}{dx}+rac{2x}{x^2+1}y=rac{1}{\left(x^2+1
ight)^2},y(0)=0$$

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Previous Years Board S Questions For Practice Multiple Choice Questions Choose The Correct Option

1. I.F. of the differential equation
$$: rac{dy}{dx} + 2y = e^{2x}$$
 is:

A.
$$e^{2x}$$

equations

 $\mathsf{B.}\,e^2$

 $\mathsf{C.}\,2$

 $\mathsf{D}.\log 2$

Answer: A





D. None of these

Answer: C



3. The degree of differential equation
$$\left(\frac{d^2y}{dx^2}\right)^3 + \left(\frac{dy}{dx}\right)^2 + \sin\left(\frac{dy}{dx}\right) + 1 = 0$$
 is

A. 3

B. 2

C. 1

D. Not defined

Answer: D



4. Degree of the differential equation :

$$log \left(\frac{dy}{dx}\right)^{\frac{1}{2}} = 3x + 4y \text{ is :}$$
A. 2
B. 1
C. 0
D. 3
Answer: B
S. Degree of differential equation $\left(\frac{ds}{dt}\right)^2 + 4s\frac{d^2s}{dt^2} = 0$ is

B. 2

C. 4

D. None of these

Answer: C

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6. The general solution of differential equation : ydx - xdy = 0 is :

A. xy = c

 $\mathsf{B.}\, x = cy^2$

 $\mathsf{C}.\, y = cx$

D. $y = cx^2$

Answer: C





B. 2

C. 1

D. None of these

Answer: C



 $x\cos ydy = (xe^x\log x + e^x)dx$

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2. Solve the following differential equation

$$ig(x^2-yx^2ig)dy-ig(y^2-xy^2ig)dx=0$$

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3. Solve the following differential equation

$$xrac{dy}{dx}-y=y^2+1$$

$$e^x an y dx + (1-e^x) \mathrm{sec}^2 y dy = 0$$

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5. Solve the following differential equation

$$yig(1-x^2ig)dy+xig(1+y^2ig)dx=0$$

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6. Find the particular solution of following differential

equations

$$\log\!\left(rac{dy}{dx}
ight)=3x+2y, x=0, y=0$$

7. Find the particular solution of following differential

equations

$$\log\!\left(rac{dy}{dx}
ight)=x+2y, x=0, y=0$$

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8. Find the general solution of following differential equations

$$ig(1+y^2ig)+ \Big(x-e^{ an^{-1}y}\Big)rac{dy}{dx}=0$$

9. Find the particular solution of following differential equations

xdx + ydy = 0 , given that y = 4 when x = 3

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10. Find the general solution of following differential

equations

$$x\log xrac{dy}{dx}+y=rac{2}{x}{\log x}$$

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11. Find the general solution of following differential equations

$$xrac{dy}{dx} = y - x$$



12. Find the particular solution of following differential

equations

$$xrac{dy}{dx}+2y=x^2, (x
eq 0)\,{:}\,y=1$$
 when $x=2$

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13. Find the general solution of following differential

equations

$$rac{dy}{dx} = rac{x-y}{x+y}$$

14. Form the differential equation representing the family of parabolas having vertex at origin and axis along positive direction of x-axis.

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15. Form the differential equation representing the family of

ellipses having foci on x-axis and centre at the origin.



16. Solve the following differential equations

$$rac{dy}{dx} = \sqrt{4-y^2}(-2 < y < 2)$$

$$rac{dy}{dx} = rac{x+1}{2-y}$$

18. Solve the following differential equations

$$ig(x^2+xyig)dy=ig(x^2+y^2ig)dx$$

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19. Show that the given differential equation is homogeneous

and solve it:
$$\Big(1+e^{rac{x}{y}}\Big)dx+e^{rac{x}{y}}igg(1-igg(rac{x}{y}igg)igg)dy=0$$

20. Find the differential equation from the equation : $y = e^x(a\cos 2x + b\sin 2x)$ where a and b are arbitrary constants.

21. Solve the following differential equations at its initial values

$$xig(1+y^2ig)dx-yig(1+x^2ig)dy=0,y=0$$
 when $x=1$

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22. Solve the following differential equations at its initial values

$$ig(1+e^{2x}ig)dy+ig(1+y^2ig)e^xdx=0,y=1$$
 when $x=0$



24. Find the general solution of the following

$$ig(x^2+xyig)dy+ig(3xy+y^2ig)dx=0$$

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25. Find the general solution of the following

$$xrac{dy}{dx}+y=x\log x$$

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26. Find the general solution of the following

$$x\log xrac{dy}{dx}+y=2\log x$$

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27. Form the differential equation of the family of hyperbolas

having foci on x-axis and centre at origin.



28. Solve the following differential equations

$$e^x an y dx + (1-e^x) \mathrm{sec}^2 y dy = 0$$

$$(x-y)rac{dy}{dx}=x+2y$$

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30. Solve the following differential equations

$$xrac{dy}{dx}-y+x\sin\Bigl(rac{y}{x}\Bigr)=0$$

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31. Solve :
$$\displaystyle rac{dy}{dx} + 2y = \sin x$$

32. Solve the differential equation :
$$x^2(y+1)dx + y^2(x-1)dy = 0$$

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$$ig(x^2y+x^2ig)dx+ig(xy^2-y^2ig)dy=0$$

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34. Solve the following differential equations

$$x\cos\Bigl(rac{y}{x}\Bigr)rac{dy}{dx}=y\cos\Bigl(rac{y}{x}\Bigr)+x$$

$$ydx+x\Bigl(\lograc{y}{x}\Bigr)dy-2xdy=0$$

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36. Find the particular solution of the differential equation ;

$$\log\!\left(rac{dy}{dx}
ight)=3x+4y$$
 , given that y = 0 when x = 0

37. Solve the following differential equation
$$\frac{dy}{dx} = x^5 + x^2 - \frac{2}{x}$$
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38. Find the general solution of the Differential Equation : $2xydx+ig(x^2+2y^2ig)dy=0$ Watch Video Solution Solve the differential equation 39. $(x^2-y^2)dx+2xydy=0.$ Watch Video Solution

40. Solve the following differential equations

$$ig(y^2-2xyig)dx=ig(x^2-2xyig)dy$$

41. Solve the differential equation : $x \frac{dy}{dx} - y = 2x^3$.



44. Find the particular solution of the differential equation

$$igg(rac{dy}{dx}igg) - 3y\cot x = \sin 2x, \, (x
eq 0)$$
 given that $y=0,\,x=rac{\pi}{2}.$

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45. Solve
$$\cot^{-1} \left(\frac{dy}{dx}
ight) = x + y$$

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46. Solve the differential equation $ig(x^2+y^2ig)dx=2xydy$



49. Form the differential equation of the family of circles

touching the y-axis at origin.



50. Solve the differential equation :
$$x \left(rac{dy}{dx}
ight) + 2y = x^2 \log x$$