



## MATHS

**BOOKS - VGS PUBLICATION-BRILLIANT**

**MATHEMATICS-II(B) MODEL PAPER 3**

### Section A

1. Find the equation of the circle passing through  $(3,4)$  and having the centre at  $(-3,4)$



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2. If the length of the tangent from  $(5, 4)$  to the circle  $x^2 + y^2 + 2ky = 0$  is 1 then find  $k$ .



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3. If the angle between the circles

$$x^2 + y^2 - 12x - 6y + 41 = 0$$

and

$$x^2 + y^2 + kx + 6y - 59 = 0$$
 is  $45^\circ$  find  $k$ .



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4. If  $(\frac{1}{2}, 2)$  is one extremity of a focal chord of the parabola  $y^2 = 8x$ . Find the co-ordinates of the other extremity.



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5. Find the equation of the hyperbola whose vertices are  $(\pm 5, 0)$  the transverse axis is of length 8.



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6. Evaluate the integrals.

$$\int \frac{(3x + 1)^2}{2x} dx \quad x \in I \subset \mathbb{R} \setminus \{0\}$$



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7. Evaluate :  $\int \frac{\log x}{x} dx$  .



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8. Evaluate  $\lim_{n \rightarrow \infty} \frac{2^k + 4^k + 6^k + \dots + (2n)^k}{n^{k+1}}$  by

using the method of finding definite integral as the limit of a sum.

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9. Find the value of the integral

$$\int_0^{2\pi} \sin^2 x \cos^4 x dx$$

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10. Solve  $\frac{dy}{dx} = e^{x-y} + x^2 e^{-y}$ .

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1. Find the equation of the circle with centre  $(-2, 3)$  cutting a chord length 2 units on  $3x + 4y + 4 = 0$



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2. Find the equation of the circle which passes through the origin and intersects each of the following circles orthogonally.

$$x^2 + y^2 - 4x + 6y + 10, x^2 + y^2 + 12y + 6 = 0$$



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3. Find the length of major axis, minor axis, latus rectum, eccentricity co-ordinates of centre, foci and the equations of directrices of the following ellipse.

$$4x^2 + y^2 - 8x + 2y + 1 = 0$$



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4. A circle of radius 4, is concentric with the ellipse  $3x^2 + 13y^2 = 78$ . Prove that a common tangent is inclined to the major axis at an angle  $\frac{\pi}{4}$



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5. Tangents to the hyperbola  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$  make angle  $\theta_1, \theta_2$  with transverse axis of a hyperbola. Show that the points of intersection of these tangents lies on the curve  $2xy = k(x^2 - a^2)$  when  $\tan \theta_1 + \tan \theta_2 = k$



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6. Evaluate :  $\int_0^{\frac{\pi}{4}} \log(1 + \tan x) dx$



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7. Solve  $\frac{1}{x} \frac{dy}{dx} + y \cdot e^x = e^{(1-x)e^x}$



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## Section C

1. Find the equation of the circle passing through (2, 1), (5, 5), (-6, 7).



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2. Show that

$$x^2 + y^2 - 6x - 9y + 13 = 0, x^2 + y^2 - 2x - 16y = 0$$

touch each other . Find the point of contact and the equation of common tangent at their point of contact.



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3. Find the equation of the parabola whose axis is parallel to X-axis and which passes through these points.

$(-2,1), (1,2),$  and  $(-1,3)$



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4.  $\int (6x + 5) \sqrt{6 - 2x^2 + x} dx$



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5. Show that

If  $I_n = \int \cos^n x dx$ , then show that

$$I_n = \frac{1}{n} \cos^{n-1} x \sin x + \frac{n-1}{n} I_{n-2}.$$



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6.  $\int_0^\pi \frac{x}{1 + \cos^2 x} dx =$

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7. Solve  $(x^3 - 3xy^2)dx + (3x^2y - y^3)dy = 0$

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