



# MATHS

BOOKS - UNITED BOOK HOUSE

## HIGHER SECONDARY EXAMINATION 2020.

### Exercise

1.  $\vec{a}$  and  $\vec{b}$  are two vectors such that  $|\vec{a} + \vec{b}| = |\vec{a} - \vec{b}|$  then angle between  $\vec{a}$  and  $\vec{b}$  is

A.  $30^\circ$

B.  $60^\circ$

C.  $90^\circ$

D.  $120^\circ$

**Answer:**



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2. If  $\omega$  be an imaginary cube root of 1 then the

value of  $\begin{vmatrix} 1 & \omega^2 & \omega \\ \omega & 1 & \omega^2 \\ \omega^2 & \omega & 1 \end{vmatrix}$  is

A.  $-1$

B.  $\omega^3$

C.  $0$

D.  $-\omega^2$

**Answer:**



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3. Let  $\mathbb{R}$  be the set of real numbers and the mapping  $f: \mathbb{R} \rightarrow \mathbb{R}$  and  $g: \mathbb{R} \rightarrow \mathbb{R}$  be defined by  $f(x) = 5 - x^2$  and  $g(x) = 3x - 4$ , then the value of  $(f \circ g)(-1)$  is

A. 8

B. -44

C. 54

D. 16

**Answer:**



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4. a straight line makes an angle  $45^\circ$  with positive direction of x-axis and  $60^\circ$  with positive direction of z-axis. If the line makes an angle  $\theta$  with positive direction of y-axis then  $\theta$  is equal to-

A.  $45^\circ$

B.  $60^\circ$

C.  $120^\circ$

D.  $135^\circ$

**Answer:**



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5. Value of  $\int_0^{\frac{\pi}{2}} (\sin^{2200} x - \cos^{2200} x) dx$  is-

A. 0

B. 1

C.  $\frac{1}{2200}$

D.  $\frac{1}{1100}$

**Answer:**



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6. The principal value of  $\sin^{-1}\left(\sin\left(\frac{5\pi}{6}\right)\right)$  is-

A.  $\frac{\pi}{6}$

B.  $\frac{5\pi}{6}$

C.  $\frac{7\pi}{6}$

D.  $\frac{\pi}{3}$

**Answer:**



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7. Evaluate :  $\sec^2(\tan^{-1} 2) + \operatorname{cosec}^2(\cot^{-1} 3)$ .



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8. Show that 
$$\begin{vmatrix} 1 & \log_a b & \log_a c \\ \log_b a & 1 & \log_b c \\ \log_c a & \log_c b & 1 \end{vmatrix} = 0,$$

( $a>0, b>0, c>0$ )



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9. Find the differential equation of  $xy = Ae^x + Be^{-x} + x^2$  by eliminating A and B (A,B are constants).



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10. If  $x^2 = a^{\sin^{-1}t}$  and  $y^2 = a^{\cos^{-1}t}$  then show that  $\frac{dy}{dx} = -\frac{y}{x}$ .



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11. If  $f(x) = \frac{\sin 5x}{2x}$  (when  $x \neq 0$ )  
 $= \frac{5k}{4}$  (when  $x=0$ ), and  $f(x)$  is continuous at  $x=0$ , find  $k$ .



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12. If  $x > 0, y > 0$  and  $xy = 100$ , find the minimum value of  $(x+y)$

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13. Evaluate:  $\int \left( \frac{\cos x + x \sin x}{x(x + \cos x)} \right) dx.$

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14. If  $f(x) = -f(-x)$  then show that  $\int_{-a}^a f(x) dx = 0.$

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**15.** Find a vector of magnitude 14 in the direction of the vector  $-3\hat{i} + 6\hat{j} - 2\hat{k}$ .



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**16.** Find the direction cosines of a straight line which is situated on the  $yz$ -plane and inclined at an angle  $60^\circ$  with the positive direction of the  $z$ -axis.



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17. If  $P(A) = \frac{1}{4}$ ,  $P(B) = \frac{1}{3}$  and  $P(A - B) = \frac{1}{6}$  then verify whether A and B are two independent events or not.



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18. The mean and variance of a binomial distribution  $B(n, p)$  are 4 and 3.2 respectively. Find the value of  $n$  and  $p$ .



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19.  $*$  is an operation defined on  $Z$  set of all integers as  $a*b = a+b-2$  for all  $a, b \in z$ .

Find identity element of  $*$



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20.  $*$  is an operation defined on  $Z$  set of all integers as  $a*b = a+b-2$  for all  $a, b \in z$ .

Find the inverse of an element  $a \in Z$ .



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21.

Show

that

$$\sin^{-1}\left(\frac{12}{13}\right) + \cos^{-1}\left(\frac{4}{5}\right) + \tan^{-1}\left(\frac{63}{16}\right) = \pi.$$



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22.

If

$$A = \begin{bmatrix} 0 & 6 & 7 \\ -6 & 0 & 8 \\ 7 & -8 & 0 \end{bmatrix}, B = \begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 2 \\ 1 & 2 & 0 \end{bmatrix}, C = \begin{bmatrix} 2 \\ -2 \\ 3 \end{bmatrix}$$

Calculate  $AC$ ,  $BC$  and  $(A+B)C$ . Also show

that  $(A+B)C=AC+BC$ .



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23. If  $A = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$  show that

$$A^n = \begin{pmatrix} \cos n\theta & \sin n\theta \\ -\sin n\theta & \cos n\theta \end{pmatrix} \quad n = \text{positive integer.}$$



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24. show that

$$\begin{vmatrix} 1 & x & x^2 \\ x^2 & 1 & x \\ x & x^2 & 1 \end{vmatrix} = (1 - x^3)^2$$



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25. If  $(\cos x)^y = (\cos y)^x$  then show that

$$\frac{dy}{dx} = \frac{y \tan x + \log \cos y}{x \tan y + \log \cos x}.$$



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26. If  $y = (\tan^{-1} x)^2$ , then show that

$$(1 + x^2)^2 \frac{d^2 y}{dx^2} + 2x(1 + x^2) \frac{dy}{dx} = 2.$$



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27. Evaluate:  $\int \frac{2dx}{(1-x)(1+x^2)}$



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28. Evaluate:  $\int (\sqrt{\tan x} + \sqrt{\cot x}) dx$







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29. Solve:  $xy \frac{dy}{dx} = (x + 2)(y + 2)$ , given  $x = 1$ ,  
when  $y = -1$ .



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30. Solve:  $x^2 dy + (xy + y^2) dx = 0$ , given  $x = 1$  and  
 $y = 1$ .



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**31.** If  $\vec{a}, \vec{b}, \vec{c}$  be three vectors such that  $\vec{a} + \vec{b} + \vec{c} = 0$ ,  $|\vec{a}| = 3$ ,  $|\vec{b}| = 5$  and  $|\vec{c}| = 7$  find the angle between the vectors  $\vec{a}$  and  $\vec{b}$ .



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**32.** Show that the points  $A=(2,-1,1), B=(1,-3,-5)$  and  $C=(3,-4,-4)$  are vertices of a right angled triangle (using vector method).



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33. Show that:  $\int_0^1 \left( \frac{\log(1+x)}{1+x^2} \right) dx = \frac{\pi}{8} \log 2.$



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34. Let  $A$  and  $B$  be two events such that  $P(A) = \frac{1}{3}$ ,  $P(B) = \frac{1}{4}$  and  $P(A \cap B) = \frac{1}{4}$ .

Find  $P(A/B)$ ,  $P(B/A)$ ,  $P(A \cup B)$ .



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35. Prove that all points of the curve

$y^2 = 4a \left[ x + a \frac{\sin x}{a} \right]$  at which the tangent is

parallel to the axis of  $x$ , lie on a parabola.



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36. Solve:  $\frac{dy}{dx} - 3y \cot x = \sin 2x$ , given  $y=2$  when  $x = \frac{\pi}{2}$



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37. Find two positive numbers  $x$  and  $y$  such that  $x + y = 60$  and  $xy^3$  is maximum.



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38. Evaluate the following integral  $\int_1^3 (x^2 + x) dx$ .



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39. A variable plane which is at a constant distance  $3p$  from origin cuts the coordinate axes at A,B,C respectively. Show that locus of the centroid of the

$$\triangle ABC \text{ is } \frac{1}{x^2} + \frac{1}{y^2} + \frac{1}{z^2} = \frac{1}{p^2}.$$



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40. Find the equation of the plane which passes through the points (3,4,1) and (0,1,0) and parallel to the line  $\frac{x + 3}{2} = \frac{y - 3}{7} = \frac{z - 2}{5}$



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